

**A HIGH-FREQUENCY QUAD-MODULUS PRESCALER  
FOR FRACTIONAL-N FREQUENCY SYNTHESIZER**

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## SUMMARY

A fully integrated fractional-N frequency synthesizer which utilizes high-frequency, fast-switching quad-modulus prescaler is proposed and demonstrated in this thesis. In this proposed design, a quad-modulus prescaler with a divide-by-4/5/6 core is implemented to minimize dynamic power consumption, avoid glitches and jitter due to mismatch in input signals' phases whilst maintaining high-frequency, fast-switching capability. Besides, fast-lock function has been instigated in the synthesizer design to reduce the frequency-locking time, and Multi-stage noise SHaping (MASH) technique has been utilized to reduce the overall phase noise and spurs. The proposed frequency synthesizer offers technological robustness, fast locking capability, versatility, low noise contribution, superior integration and deployment capacity, and multi-modulus flexibility.

The proposed design has been studied, simulated at both circuit and system levels and implemented to examine its performances. The actual circuit performances are verified via measurements conducted after fabrication and packaging.



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# CHAPTER 1

## INTRODUCTION

### 1.1 Motivation

The wireless communication market has been expanding, resulting in increasingly stringent requirements for low cost, low power consumption, higher operating frequencies and miniaturization on circuits due to limited battery life and highly competitive market environment. Gallium Arsenide (GaAs) technology was used in the early 80's for implementation of circuits operating in the GHz bands. However, silicon wafers is still preferred for its lower manufacturing cost, and improved unity-gain bandwidth over the years via device scaling, new materials for interconnection, and additional metal layers. Recent publications have highlighted the increasing importance of CMOS RF circuits due to its compatibility with CMOS digital building block, enabling the implementation of full RF System-on-Chip (SoC) [1].

Frequency synthesizer is one of the critical building blocks in integrated transceivers. Conventional RF synthesizers are mostly integer-N synthesizers with output frequencies fixed at integer multiples of reference frequency. Fractional-N synthesizer is introduced because it allows deployment of higher reference frequency, contributing to higher loop bandwidth, better phase noise suppression, faster loop settling time and frequency flexibility. The only two blocks operating at full frequency in a synthesizer are the voltage-controlled oscillator (VCO) and prescaler. In current CMOS technology, it is easy to design high-frequency VCO but the prescaler remains as a



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major challenge in high-frequency synthesizer design [2]. High-speed multi-modulus prescaler are more intricate to be constructed as compared to fixed-division-ratio divider and dual-modulus prescaler because the additional logic gates might slow down the system.

Recent publications have demonstrated an increasing trend of proposing phase-switching prescaler to rectify the lower operating speed inherited by conventional synchronous divider [2, 3, 4]. However, phase-switching technique has glitches and jitters due to phases mismatch issues which have to be addressed during implementation. Besides, the need for Multiplexer and switching control blocks increases the complexity of the circuit.

## **1.2 Thesis Organization**

In Chapter 2, the principles of frequency synthesizer and the functionality of PLL are discussed. Various frequency synthesizer architectures, together with their pros and cons, are examined.

In Chapter 3, the fundamentals of prescaler are reviewed. Various divide-by-2 topologies, and their advantages and disadvantages are discussed. Besides, the differences between synchronous and asynchronous dividers, dual-modulus and multi-modulus prescalers are highlighted.

---

In Chapter 4, the circuit overview and implementations of the proposed frequency synthesizer are presented, which includes counters, fast-lock timer, interface, mode register, PFD, charge pump, quad-modulus prescaler, loop filter, etc..

In Chapter 5, the testbench setups, simulation results and measurement results of the proposed design are presented.

In Chapter 6, a summary of the research has been outlined.

---

## CHAPTER 2

### FREQUENCY SYNTHESIZER

The output frequency of oscillator in an RF transceiver (transmitter-receiver) has to meet the stringent requirements of high precision and capability of varying in small, accurate steps. Hence, it is usually embedded in synthesizer which synthesizes clean, fast-switching and programmable frequencies from one or more fixed reference frequencies. Figure 2.1 shows the role of synthesizer in common transceiver architecture.

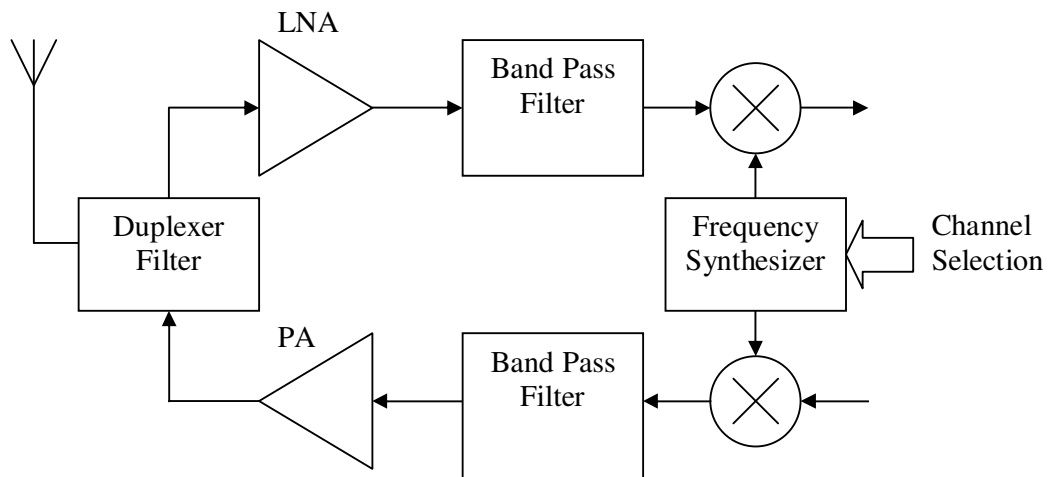


Figure 2.1 Role of frequency synthesizer in common transceiver

#### 2.1 Phase-Locked Loop (PLL)

PLL is a feedback system operating on the excess phase of nominally periodic signals. Figure 2.2 shows a simple PLL comprising of phase detector (PD), low-pass filter

(LPF), and voltage-controlled oscillator (VCO). The loop is locked when the phase difference,  $\Delta\Phi$ , is constant with time, resulting in equal input and output frequencies.

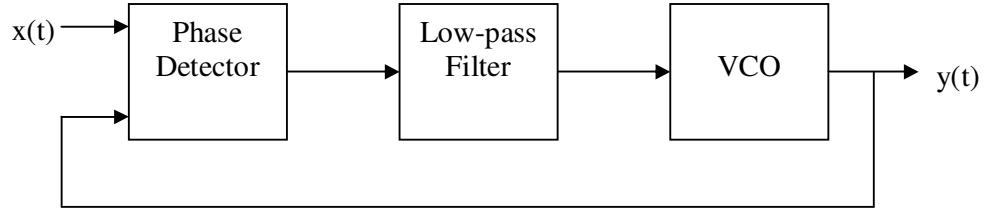


Figure 2.2 Phase-locked loop

PD acts as “error amplifier” in the feedback loop by minimizing  $\Delta\Phi$  between  $x(t)$  and  $y(t)$ . Under locked condition, it will produce an output with dc value that is proportional to  $\Delta\Phi$  (Figure 2.3),

$$\overline{v_{out}} = K_{PD} * \Delta\Phi \quad (2.1)$$

where  $K_{PD}$  is the “gain” of the phase detector in V/rad. The LPF will pass the dc value of the PD output while suppressing the high-frequency components. The dc value is used to control the VCO such that it will oscillate at a frequency equals to the input frequency but with a phase difference of  $\Delta\Phi$  [5]. Hence, VCO can be characterized by

$$\omega_{out} = \omega_{FR} + K_{VCO} v_{out} \text{ and } y(t) = A_C \cos \left[ (\omega_{FR} * t) + K_{VCO} \int_{-\infty}^t v_{out}(t) dt \right], \text{ with the input-}$$

output transfer function given by

$$\frac{\Phi_{out}}{V_{out}}(s) = \frac{K_{VCO}}{s} \quad (2.2)$$

where  $\omega_{FR}$  is the “free-running” frequency and  $K_{VCO}$  is the “gain” of VCO in rad/s/V. Figure 2.4 shows an example of the signals at various points in a PLL with both input and output signals having same frequency but finite phase difference.

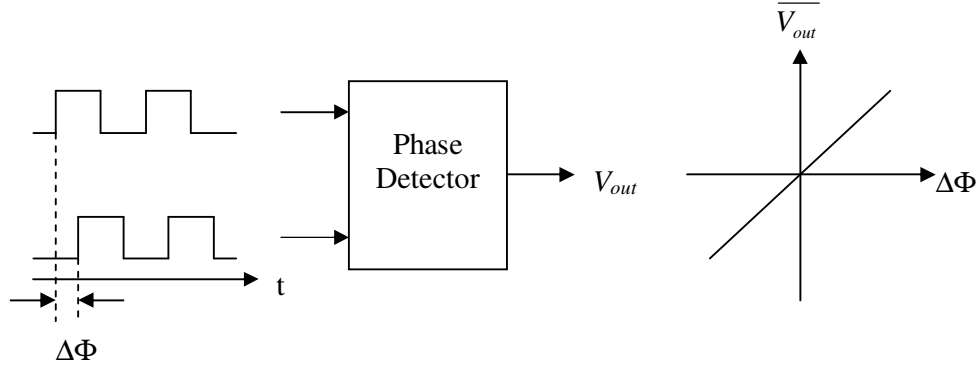


Figure 2.3 Characteristic of phase detector

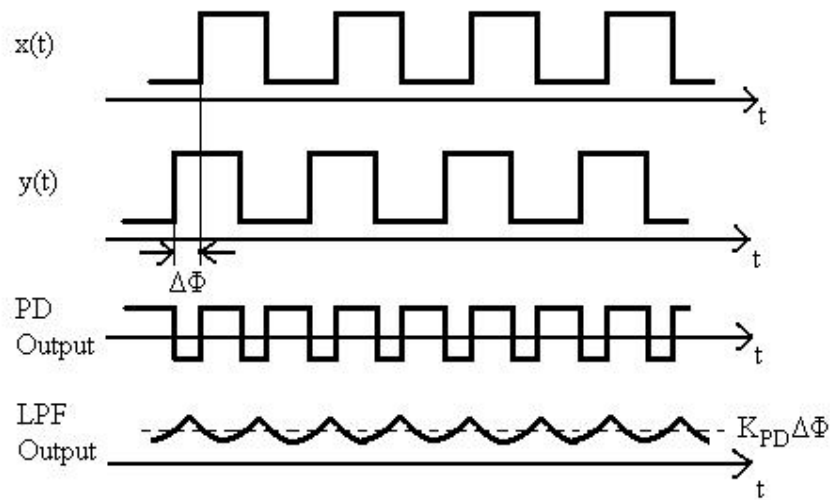


Figure 2.4 Signals in a PLL

As shown in Figure 2.5, when a locked PLL experiences a small increase in frequency: the input frequency,  $\omega_{in}$ , will be greater than the output frequency,  $\omega_{out}$ , temporarily;  $x(t)$  will accumulate phase faster than  $y(t)$ ; PD will progressively generate wider pulses. Wider pulse contributes to higher dc value at the LPF output, resulting in an increase in VCO frequency. The increase in VCO frequency will reduce the difference between  $\omega_{in}$  and  $\omega_{out}$ , resulting in the reduction of the width of PD output pulses and the eventual settlement of dc value at a value which is slightly greater than its initial locked-phase value [6]. Hence, the loop is locked only after both “frequency acquisition” and “phase acquisition” are satisfied.

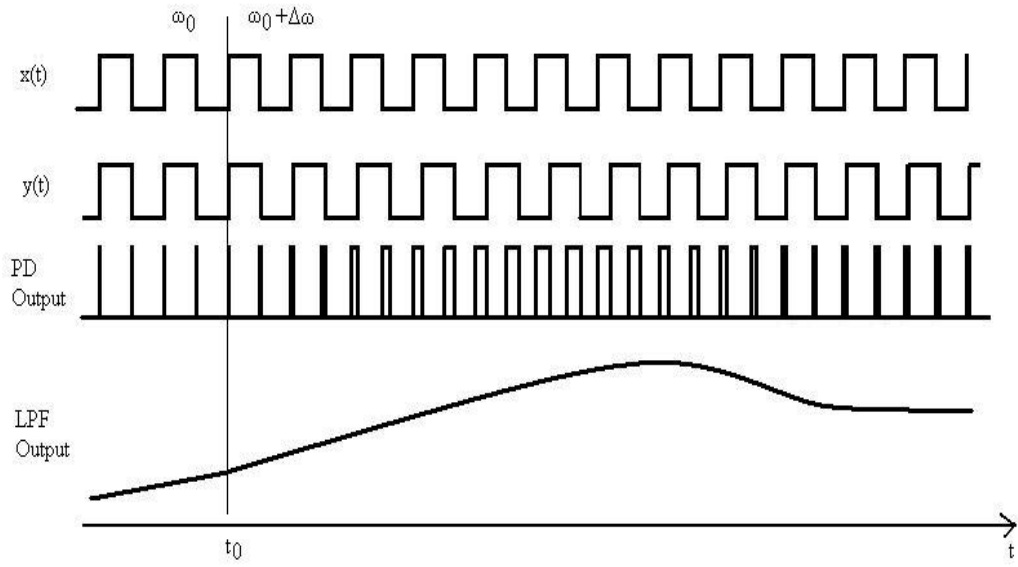


Figure 2.5 Response of PLL to a small increase in frequency

Although PLL has a nonlinear transient response, a linear approximation is used to estimate its performance as shown in Figure 2.6. The closed-loop transfer function, or jitter transfer function, is given by,

$$H(s) = \frac{\Phi_{out}(s)}{\Phi_{in}(s)} = \frac{K_{PD}K_{VCO}G_{LPF}(s)}{s + K_{PD}K_{VCO}G_{LPF}(s)} \quad (2.3)$$

$$\text{If } G_{LPF}(s) = \frac{1}{1 + \frac{s}{\omega_{LPF}}} \text{ and } \omega_{LPF} = \frac{1}{RC},$$

$$H(s) = \frac{K_{PD}K_{VCO}}{\frac{s^2}{\omega_{LPF}^2} + s + K_{PD}K_{VCO}} \quad (2.4)$$

$$H(s) = \frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} \quad (2.5)$$

where

$$\omega_n = \sqrt{\omega_{LPF} K} \quad (2.6)$$

$$\zeta = \frac{1}{2} \sqrt{\frac{\omega_{LPF}}{K}} \quad (2.7)$$

where  $K_{PD}K_{VCO}$  is the “loop gain” in rad/sec,  $\zeta$  is the damping factor, and  $\omega_n$  is the natural frequency of the system. According to the equations,  $\omega_n$  depicts the gain-bandwidth product of the loop while  $\zeta$  shows the degree of loop stability.

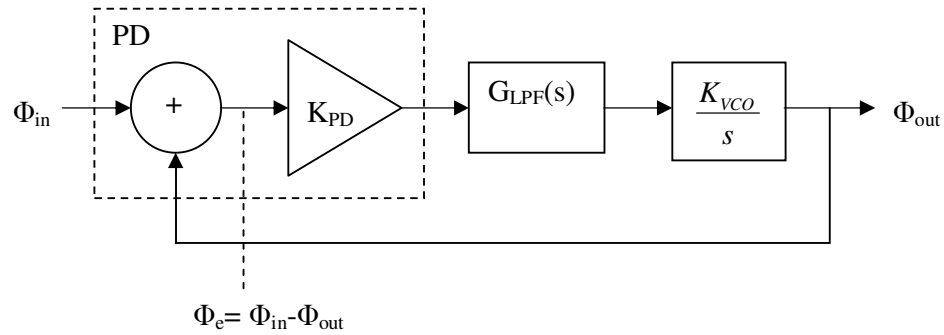


Figure 2.6 Linear approximation of PLL

### 2.1.1 Frequency Multiplication

The output frequency of PLL is usually required to be multiple of input frequency, resulting in the need of a frequency divider to divide down the output signal in the feedback loop (Figure 2.7). In the process of frequency multiplication, input phase noise is also being amplified.

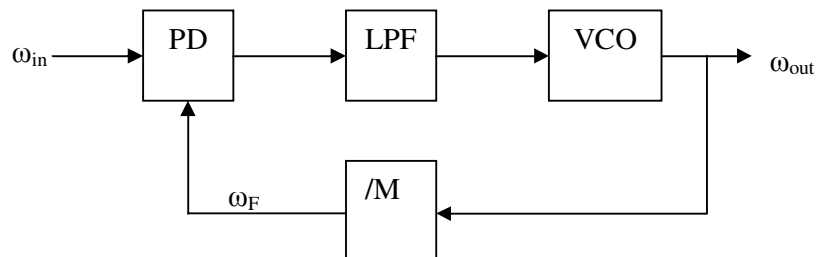


Figure 2.7 Frequency multiplication of PLL

---

## 2.2 Frequency Synthesizer Architectures

The output frequencies,  $f_{out}$ , of frequency synthesizers vary in steps of multiplications of channel spacing:  $f_{out} = f_0 + kf_{ch}$ , where  $f_0$  is the lower limit of frequency,  $k$  is the number of channels and  $f_{ch}$  is the channel spacing. The use of PLL is often required due to the requirement for high precision in the definition of  $f_0$  and  $f_{ch}$ . Some of the frequency synthesizer architectures will be discussed in the following sections.

### 2.2.1 Direct Digital Frequency Synthesizer

A Direct Digital Frequency Synthesizer (DDFS) generates signal in digital domain and uses a digital-to-analog converter (DAC) to convert the signal into waveform in analog domain. The counter counts in unity, increment steps until maximum count before it restarts from zero again, generating a periodic, saw-tooth output waveform. The ROM will convert the number generated by the counter to a digital amplitude value based on the lookup table stored in it. Then, the values are converted to analog waveform by the DAC, with high-frequency components being filtered-off by the LPF [7, 8, 9].

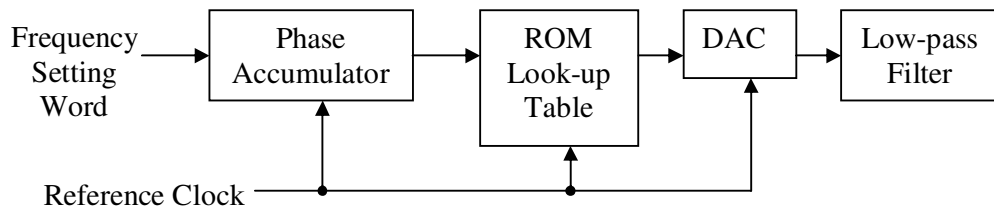


Figure 2.8 Direct digital frequency synthesizer with accumulator

Figure 2.8 shows an example of DDFS with an accumulator. The output frequency is given by

$$f_{out} = P \frac{f_{CK}}{2^M} \quad (2.8)$$



---

where  $f_{CK}$  is the clock frequency,  $P$  is the programmable step and  $M$  is the register bit number.

DDFS has the following advantages: low phase noise due to avoidance of use of analog VCO; fine frequency increments but at the expense of complexity; faster channel switching capability as compared to PLL; continuous-phase channel switching; direct modulation of output signal in digital domain. However, DDFS has the following drawbacks: speed limitation due to highest-frequency limitation according to Nyquist's sampling theorem [5, 10, 11, 12]; spectral purity is limited by the speed, resolution and power dissipation of DAC.

### 2.2.2 Integer-N Frequency Synthesizer

The integer-N frequency synthesizer is one of the most commonly used architecture. As shown in Figure 2.9, the output frequency is given by  $f_{out} = N * f_{REF} = f_0 + kf_{ch}$ , where  $N = N_L + k$ ;  $k=0, 1, \dots, P$ . It shows that input reference frequency and channel spacing must be the same.

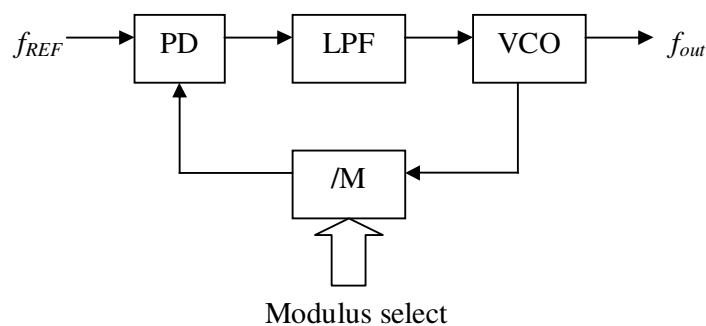


Figure 2.9 An integer-N frequency synthesizer

A low  $f_{REF}$ , which requires a narrow loop bandwidth to block the signal components at  $f_{REF}$  and its harmonics, is desired for small channel spacing. Settling time will increase

and VCO noise suppression capability will decrease as a result of narrow loop bandwidth. A divider with larger division value is needed for low  $f_{REF}$  but this will result in the increase of VCO in-band phase noise. Hence, this topology is not suitable for systems which require low phase noise, fast switching time and small frequency spacing [13].

A prescaler can be added when the VCO output frequency is higher than the programmable divider maximum clock frequency, as shown in Figure 2.10. Under locked condition,  $f_{out} = P * N_p * f_{REF}$ , where  $P$  is the programmable frequency divider division ratio,  $N_p$  is the prescaler division ratio, and  $N_p * f_{REF}$  is the frequency channel spacing. The drawbacks of this topology are larger frequency channel spacing, smaller reference frequency, longer lock-on time, and sidebands.

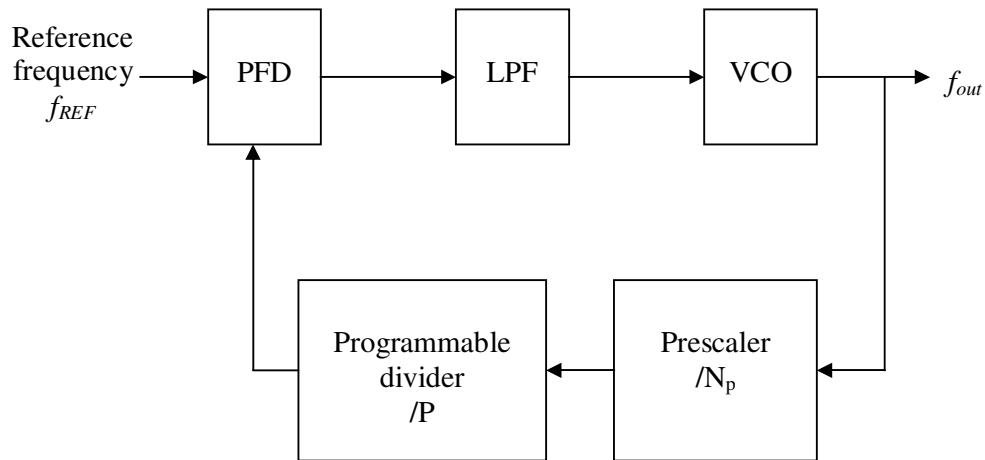


Figure 2.10 Frequency synthesizer with single modulus prescaler

Dual-modulus prescaler is able to solve the frequency resolution problem by providing two division ratios, i.e.  $N_p$  and  $(N_p+1)$ , with the control signal from additional logic circuit. Hence, a high-frequency programmable divider can be formed by combining a dual-modulus prescaler with two counters, as shown in Figure 2.11.

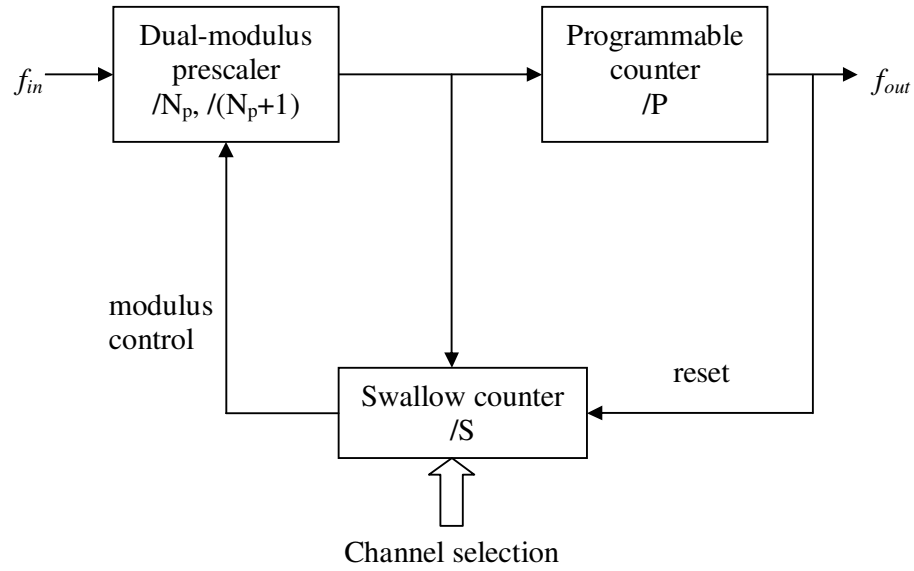


Figure 2.11 High-frequency programmable divider

The prescaler will first divide by  $(N_p+1)$  and the swallow counter will start counting till it overflows at  $S$ . Then, the overflow bit will set the division ratio of prescaler to  $N_p$  while the program counter will start counting till it overflows at  $P$ . Both the  $S$ -counter and  $P$ -counter will be reset and the division cycle repeats again. The overall division is given by

$$N = [(N_p + 1)S] + [N_p(P - S)] = PN_p + S \quad (2.9)$$

where  $P$  must be larger than  $S$  for proper reset operation by program counter, and

$$N_{\min} = (P_{\min} N_p) + S_{\min} = ((N_p - 1)N_p) + 0 = (N_p^2 - N_p) \quad (2.10)$$

$$N_{\max} = (P_{\max} N_p) + S_{\max} \quad (2.11)$$

This topology has the following drawbacks: occurrence of reference spur; limited loop bandwidth; higher close-in phase noise at the output.

---

### 2.2.3 Fractional-N Frequency Synthesizer

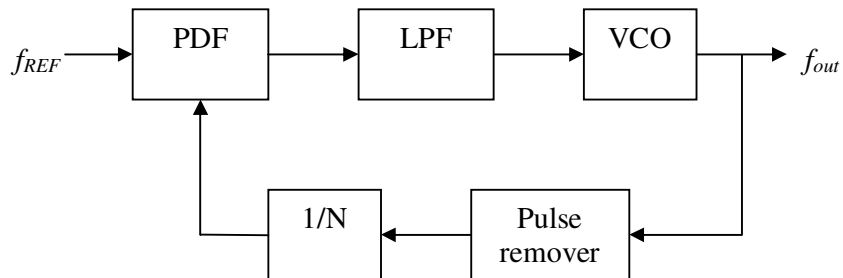
As shown in Figure 2.12 is two fractional-N frequency synthesizer topologies. The conventional design as shown in Figure 2.12(a) includes a pulse-remover which removes one output pulse upon activation. The average output frequency is given by

$$f_{out} = f_{ref} + \frac{1}{T_p} \quad (2.12)$$

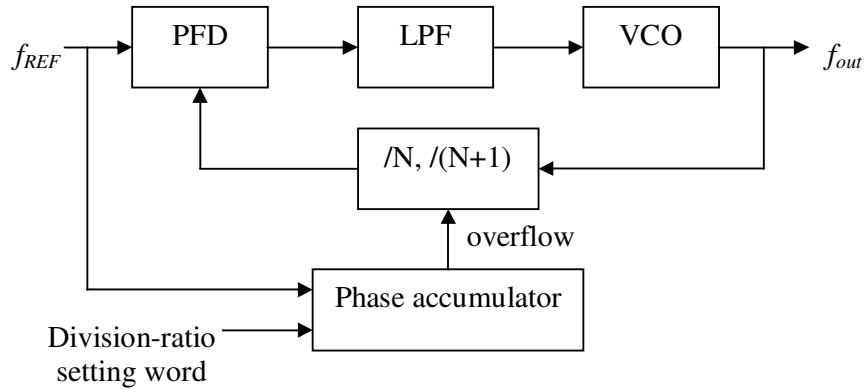
where  $T_p$  is the period when pulse-remove command is activated. Figure 2.12(b) shows an alternative design using dual-modulus prescaler, with the phase accumulator being clocked at reference frequency. Assuming a word of length  $L_{div}$  represents a division-ratio setting at each clock cycle, the dual-modulus prescaler will divide by  $N$  while the phase accumulator accumulates its output. Once the phase-accumulator-output overflows, the prescaler will divide by  $(N+1)$ . For an accumulator of length  $L_{acc}$ , the accumulator will overflow  $L_{div}$  times per cycle. Hence, the average division ratio is given by

$$N_{ave} = \frac{N(L_{acc} - L_{div}) + (N + 1)L_{div}}{L_{acc}} = N + \frac{L_{div}}{L_{acc}} \quad (2.13)$$

$$f_{out} = f_{ref} \left( N + \frac{L_{div}}{L_{acc}} \right) \quad (2.14)$$



(a)



(b)

Figure 2.12 Fractional-N synthesizer with: (a) pulse remover, (b) dual-modulus prescaler

The fractional-N frequency synthesizer allows for higher PLL loop bandwidths but the main drawback is the appearance of fractional spurs. Under closed-loop condition, with VCO output of  $(N + \alpha)f_{REF}$  and periodic, ramp LPF output waveform of period  $1/(\alpha f_{REF})$ , sidebands will appear at  $\alpha f_{REF}$ ,  $2\alpha f_{REF}$ , etc. with respect to centre frequency. Fractional compensation can be implemented to suppress the fractional spurs by injecting another current pulse series of similar width but opposite direction to the low-pass filter. However, the major limitation is the inaccuracy due to mismatches in the compensation current. Alternatively,  $\Sigma-\Delta$  modulation method (Figure 2.13) can be used to average out the division factor and convert the fractional spurs to random noise before shaping the resultant noise spectrum and push it beyond the loop bandwidth [13-18].

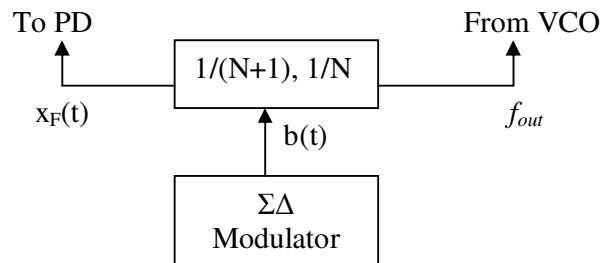


Figure 2.13 Noise shaping using  $\Sigma-\Delta$  modulator

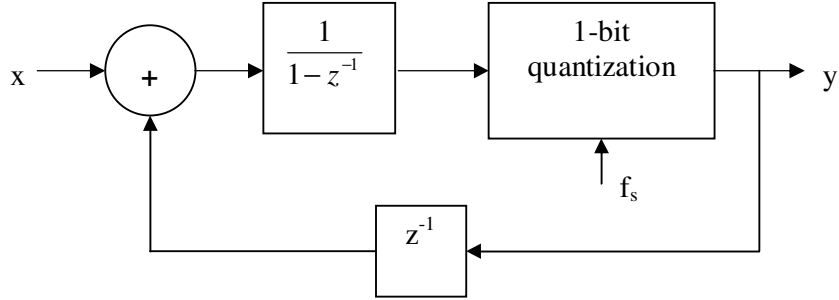


Figure 2.14 First-order  $\Sigma-\Delta$  modulator

As shown in Figure 2.14 is a first-order  $\Sigma-\Delta$  modulator. Input signal representing the fractional value is input to the integrator before passing through the quantizer, which is operating at higher sampling frequency with respect to the Nyquist frequency. The transfer function of the integrator is given by

$$H(z) = \frac{1}{1-z^{-1}} \quad (2.15)$$

The output of the first-order  $\Sigma-\Delta$  modulator can be expressed as

$$y(z) = \left( \frac{H(z)}{1+z^{-1}H(z)} \right) x(z) + \left( \frac{1}{1+z^{-1}H(z)} \right) q(z) \quad (2.16)$$

$$= x(z) + (1-z^{-1})q(z) \quad (2.17)$$

$$= x(z) + H_{noise}^{-1}(z)q(z) \quad (2.18)$$

where  $x(z)$  is the input signal and  $q(z)$  is the quantization noise.  $H_{noise}$ , which is a high-frequency component, can be filtered out by passing the signal via a low-pass filter.

A dithering enabled  $\Sigma-\Delta$  modulator will further reduce the unwanted fractional spurs. Dithering is a method of introducing random noise to the  $\Sigma-\Delta$  modulator. One technique involves one LSB dithering at the DC input but at the compromise of

synthesizer resolution because any changes in the DC input will directly affect the output frequency. Another technique involves initializing the input word of first stage accumulator to a value which is independent to the long term average of the  $\Sigma$ - $\Delta$  modulator [19].

#### 2.2.4 Delay-Locked Loop (DLL) Frequency Synthesizer

Figure 2.15 shows a DLL frequency synthesizer with a voltage controlled delay line in-place of the voltage controlled oscillator [20]. Under “locked” condition, the difference between input and output of delay line is one reference clock cycle,  $T_{REF}$ . Hence, a synthesizer with N-delay stages will experience a delay of  $T_{REF}/N$  for each stage. Each transition in the delay-line output will trigger a transition at the edge combiner, causing the latter to produce an output frequency of  $Nf_{REF}$ .

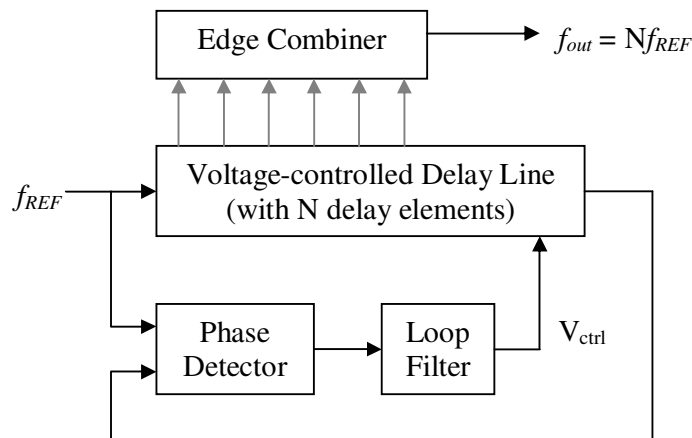


Figure 2.15 Delay-locked loop frequency synthesizer

This topology has the following advantages: jitter will not be carried forward to successive cycles; lower phase noise for adjacent frequencies; it does not require high Q. However, it is not suitable for applications that entail frequency tuning because of the fixed output frequency, which is determined by the number of delay stages.

---

## CHAPTER 3

### PRESCALER

Due to the inherent limitation to switching speed of CMOS digital cells [21], prescaler is needed to divide down the VCO frequency before transmitting the signal to programmable divider in high-frequency PLL-based synthesizer system [22]. Despite the current advancement of CMOS process, the prescaler remains as a major challenge in high-frequency design due to the trade-off between functionality and operating speed [2, 3, 23, 24]. The various divider topologies and common implementations of prescaler will be discussed in the following sections. Usually, the first few divider blocks will utilize fast-switching, high-frequency divider topologies such as current mode logic (CML) (also called source-coupled logic (SCL)) [25] and injection-locked [26, 27]. Subsequent divider blocks, which operate at lower frequency, can utilize simpler topologies such as True Single-Phase Clock (TSPC) to minimize overall power consumption.

#### 3.1 Divide-by-2 Topologies

Figure 3.1 shows a divide-by-2 structure (also called Johnson Counter) that is formed using two cascaded latches. The maximum operating speed is determined by the propagation delay of latches ( $delay_1, delay_2$ ), i.e. the time taken for the input signal of each latch to propagate to its respective output, and the setup time of latches ( $T_s$ )

$$\frac{T_{in}}{2} > delay_{1,2} + T_s \quad (3.1)$$



There are various ways of implementing the latch, depending on the speed and power consumption requirements of the system, as shown in Table 3.1.

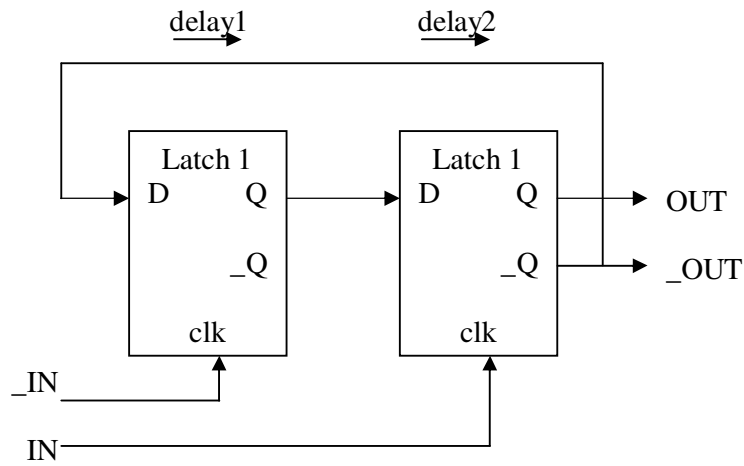
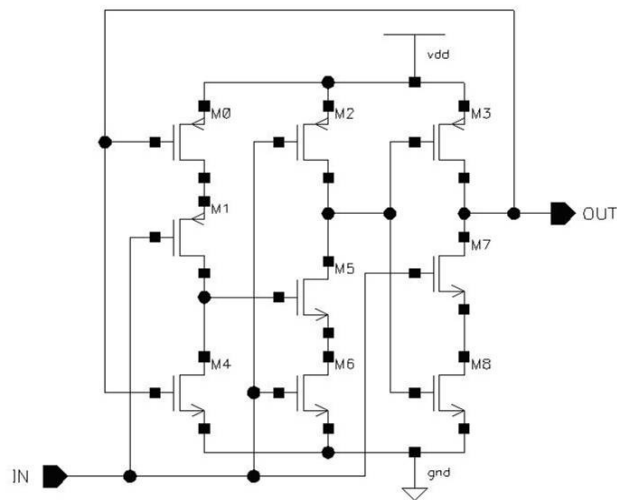


Figure 3.1 Divide-by-2 circuit

Table 3.1 Latch topologies

A) TSPC



Advantages:

- i) moderately fast
- ii) compact
- iii) without static power dissipation
- iv) only requires single-ended clock input

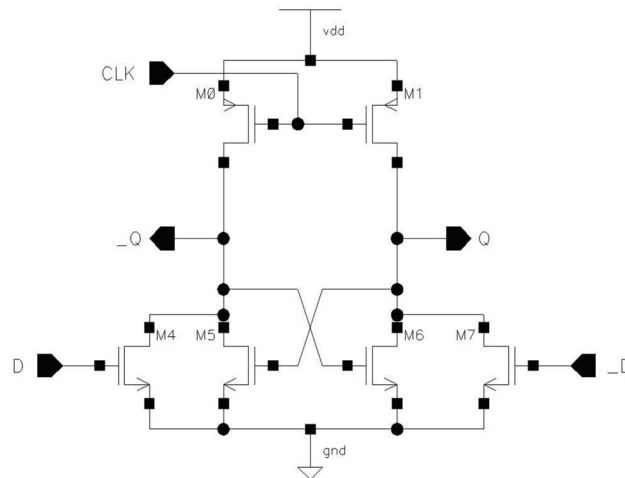
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Drawbacks:

- i) slower speed due to stacked PMOS
- ii) signal passes through three gates per cycle
- iii) requires full-swing input signal

---

B) Razavi's [28]



Advantages:

- i) fast due to absence of stacked PMOS
- ii) signal passes through two gates per cycle

Drawbacks:

- i) presence of static power dissipation
- ii) requires full-swing, differential input signals

---

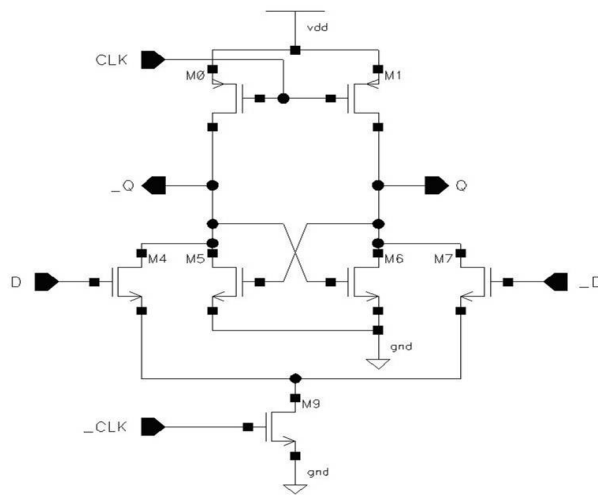
C) Wang's [29]

Advantages:

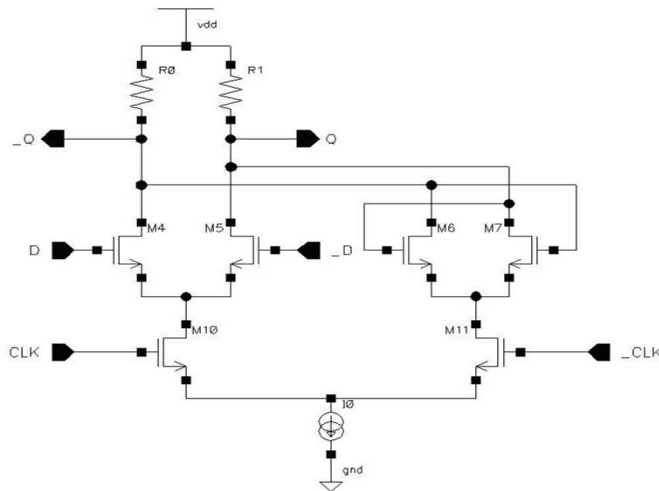
- i) fast due to absence of stacked PMOS
- ii) signal passes through two gates per cycle

Drawbacks:

- i) presence of static power dissipation
- ii) requires full-swing, differential input signals



#### D) CML



Advantages:

- i) very fast due to absence of PMOS
- ii) signal passes through two gates per cycle
- iii) requires smaller input swing

Drawbacks:

- i) presence of static power dissipation
- ii) requires differential input signals and biasing
- iii) occupies larger chip area

---

## 3.2 Synchronous and Asynchronous Dividers

A synchronous divider uses a single clock signal to feed all the clock inputs simultaneously, as shown in Figure 3.2. This approach introduces lower jitter but higher power consumption due to high frequency operation of all registers, and higher loading on the clock to drive all registers simultaneously. Figure 3.3 shows an asynchronous divider with each divide-by-2 stage being clocked by the output of the preceding stage. Hence, this approach introduces lower power consumption with subsequent stages consume lesser power while operating at lower frequency, and lesser loading on the clock which only needs to drive the first stage but larger jitter.

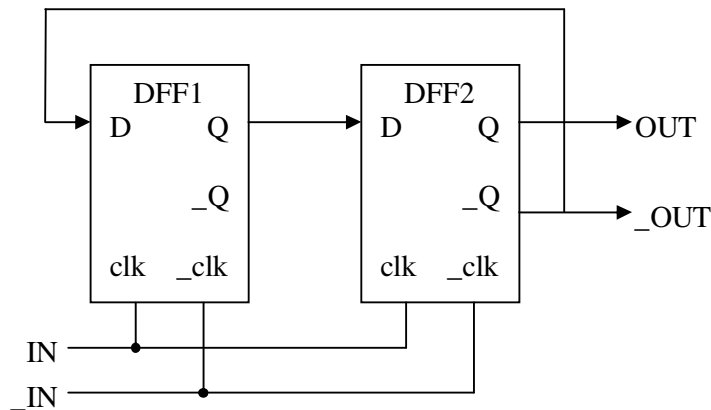


Figure 3.2 Synchronous divider

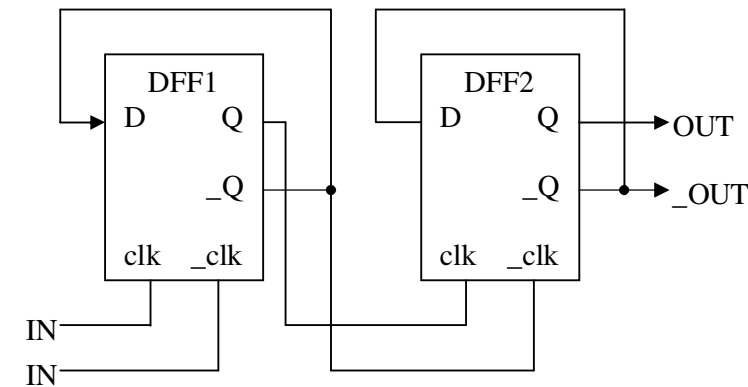


Figure 3.3 Asynchronous divider

### 3.3 Dual-modulus Prescaler

A dual-modulus prescaler provides two division ratios,  $N$  and  $N+1$ , e.g. 16/17, 32/33, 64/65, 128/129, etc. [4]. Figure 3.4 shows a traditional synchronous divide-by-4/5 design. A modulus control signal,  $M$ , is used to control the division ratio to divide by either  $N$  or  $N+1$ . As shown, when  $M=0$ ,  $D1$  and  $D2$  will form a divide-by-4 with  $q_3$  remaining at 'High' and  $NAND1$  behaving like a *NOT* gate. When  $M=1$ ,  $NAND2$  will behave like a *NOT* gate and  $NAND1$  will output '0' when both  $q_2$  and  $q_3$  are at 'High'. Hence,  $q_1$  will change from high-to-low after 3 cycles of  $f_{clk}$ , forming a divide-by-5.

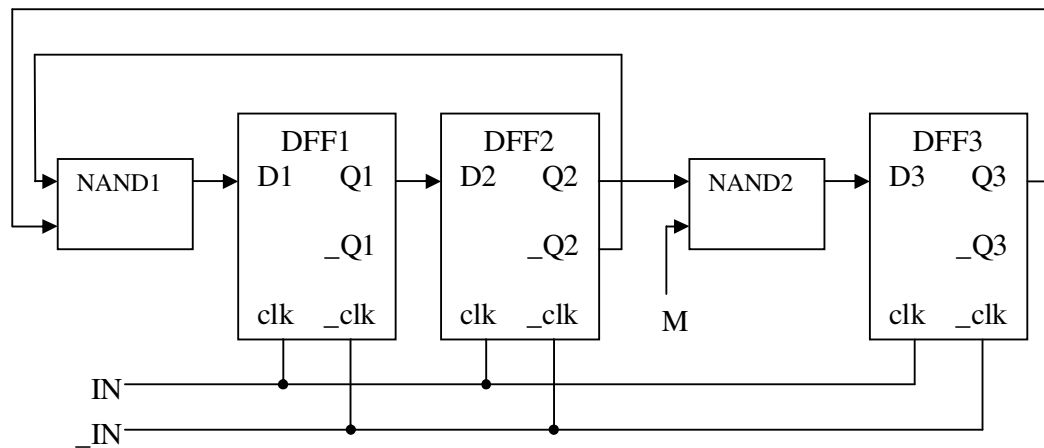


Figure 3.4 Synchronous divide-by-4/5 circuit

### 3.4 Multi-modulus Prescaler

A multi-modulus prescaler provides multiple division ratios that are selected via external control signals, which extend the functional frequency range of the system [2, 30].

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### 3.4.1 Ring Prescaler

A series of divide-by-2/3 dividers can be cascaded to form a divider with division ratios ranging from  $2^n$  to  $2^{n+1}-1$  [31, 32]. Figure 3.5 shows a cascaded divide-by-2/3 design [33, 34]. The asynchronous topology allows the divider to function at a higher speed with lower power consumption, but at the expense of accumulation of jitters.

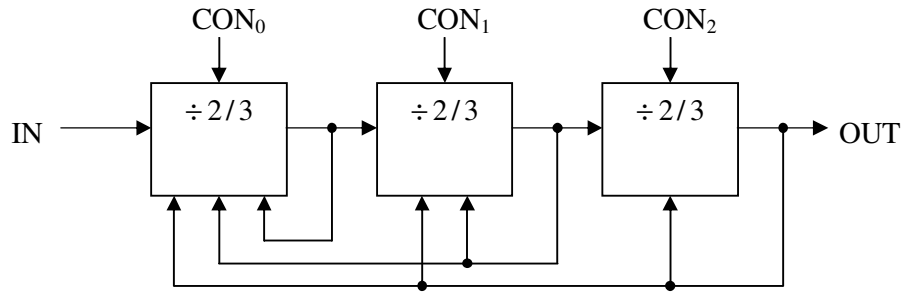


Figure 3.5 A cascaded divide-by-2/3 programmable prescaler

### 3.4.2 Phase-switching Prescaler

Referring to Figure 3.6, the maximum operating speed of a divide-by-2/3 structure is slower than basic divide-by-2 (Eqn. 3.1) due to the presence of gating logics

$$\frac{T_{in}}{2} > delay_{1,2} + delay_3 + T_s \quad (3.2)$$

Hence, phase-switching topology is utilized to realize a divide-by-2/3 by multiplexing the outputs of a divide-by-2 circuit (Figure 3.7). The maximum operating speed of this structure is equivalent to the speed of a basic divide-by-2, with the multiplexer operating at half of the input frequency. However, conventional phase-switching prescaler that switches in “increasing cycle” (or anticlockwise) manner between output phases may suffer from glitches [2, 3], and special attention is needed to ensure that there is no mismatch in phases to avoid jitter.

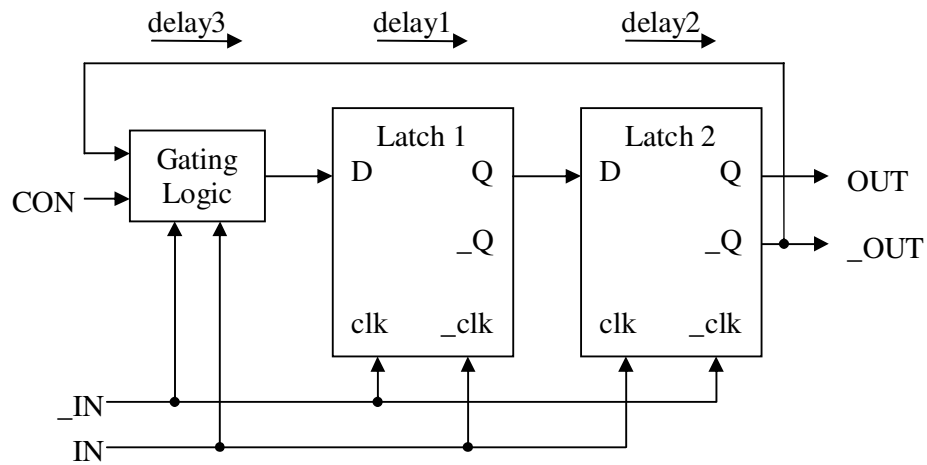


Figure 3.6 A divide-by-2/3 core circuit

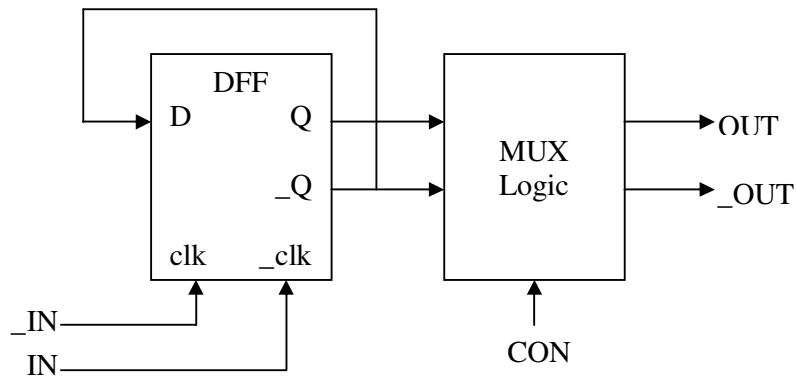


Figure 3.7 A divide-by-2/3 using phase-switching

Prescaler is required in high-frequency PLL system to overcome the issue of process limitations. Higher modulus prescaler is desired to achieve larger N-value range, especially the minimum N value [24]. The choice of prescaler architecture to be implemented in a system will depend on the system's requirements, such as power consumption, phase noise, spurious level, etc..

Although phase-switching topology seems to be the most preferred architecture recommended by literatures, it may face the issue of unwanted glitches during phase

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switching [23, 24]. Literatures have suggested various ways to remove the glitches [2-4, 35]. A re-timer circuit is suggested by [35] to synchronize the input signals of phase-switching control block at the expense of circuit complexity, power consumption and die size. In [36], glitches are removed by reversing the switching sequence but the switching control logic may not be sufficiently fast to detect the switching from one phase to another. In [24], “time borrowing” technique is suggested to overcome the switch-control-logic speed problem at the expense of power consumption and additional pulse-generator block. In [2, 3], 8 output phases are used to produce desired output signals and to reduce the error window but with increased circuit complexity. Unfortunately, all these glitch-removing techniques either increase circuit power consumption and/or reduce maximum operating frequency.

Other topologies possess respective shortcomings such as large power consumption, lower maximum operating frequency, narrow locking range, large die size, etc. [2, 3, 26]. In [37], injection-locked technique is proposed for very high frequency operation at the expense of very narrow operating range. In [38, 39], TSPC is used but this topology has low input sensitivity due to the need for rail-to-rail input signal swing and high switching noise. In [40],  $n$  divide-by-2/3 blocks are cascaded to form multi-modulus prescaler. Although the cascaded structure provides option for power optimization and reusability, special care is required in the design of divider because reduction in time window between arrival of input feedback signal and successive input clock edge will limit the maximum operating frequency.

Hence, high-speed, low-power and robust prescaler design remains as a challenge in high-frequency synthesizer design.



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## CHAPTER 4

### CIRCUIT DESIGN AND IMPLEMENTATION

As discussed in Chapter 2, fractional-N frequency synthesizer offers an improvement on the phase noise by  $20 \times \log(F)$ , theoretically, while remaining competitive in terms of current consumption, circuit complexity, and die size. The major concern with this implementation is the spurious signal at VCO, caused by the phase perturbation during divide-ratios switching. Delta-sigma modulation technique is a widely implemented solution to address this problem. If the divide-ratio remains unchanged with increasing switching frequency over  $F$  cycles, phase noise will be pushed to higher frequencies before being filtered out by loop filter. Hence, the remaining noise will only exist at low frequency, resulting in an overall improvement of phase noise performance. Instead of direct phase-noise cancellation, this noise-shaping technique utilizes switching-pattern modification to suppress the low frequency spectral caused by divide-ratio switching.

#### 4.1 Fractional-N Frequency Synthesizer Circuit Overview, Architecture, and Layout

A high-frequency, fast-locking fractional-N PLL frequency synthesizer that utilizes quad-modulus prescaler has been designed. In this design, fast-lock timer has been incorporated to shorten the frequency locking time, Multi-stage noise Shaping (MASH) technique is implemented to reduce the phase noise and spurs, and quad-

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modulus prescaler is employed to extend the system's functional frequency range. Hence, the proposed design offers technology robustness, versatility, fast locking ability, low noise contribution, high integration competency, multi-modulus flexibility, and ease of future expansion and deployment activities.

The design was realized using Chartered Semiconductor 0.35 $\mu$ m, 2P4M, CMOS technology with MIM capacitor option. The system and circuit levels' analyses, designs and simulations were carried out in Cadence IC5.0.33 under Redhat 8.0 and Cadence IC5.1.41 under Red Hat Enterprise Linux WS release 4 (Nahant Update 4). All the basic digital cells are Synopsys standard cells.

Figure 4.1 shows the topology of the fractional-N frequency synthesizer design. The design consists of the following building blocks: R-Counter, N-Counter, Fast-lock Timer, MASH, Interface, Mode Register, MUX\_Output, Phase-Frequency Detector (PFD), Charge Pump, Fast-lock Control Switch, Quad-modulus Prescaler, and Loop Filter. R-Counter will divide down the input reference frequency. Then, PFD will compare this divided reference signal with the divided Local Oscillator (LO) signal and generate two outputs which are not complementary. The PFD outputs are used to drive charge pump that provides several gains to cater for the variation in VCO gain. The variable charge pump gain ensures that the PLL loop gain is stable. Loop filter is implemented with fast-lock function to shorten the locking time significantly. Subsequently, the filtered signal is used to control the VCO frequency.

Then, the VCO differential output signals are divided by quad-modulus prescaler before transmitting to N-Counter because digital circuit usually has lower functional

frequency. N-Counter, which supports 910MHz and 2450MHz operations, provides whole-number division to the signal while the 3<sup>rd</sup>/4<sup>th</sup> order MASH produces fractional output frequency. The divided signal is then compared with the divided reference frequency. Hence, frequency locking is accomplished through these procedures. Table 4.1 lists the proposed design specification for the frequency synthesizer design.

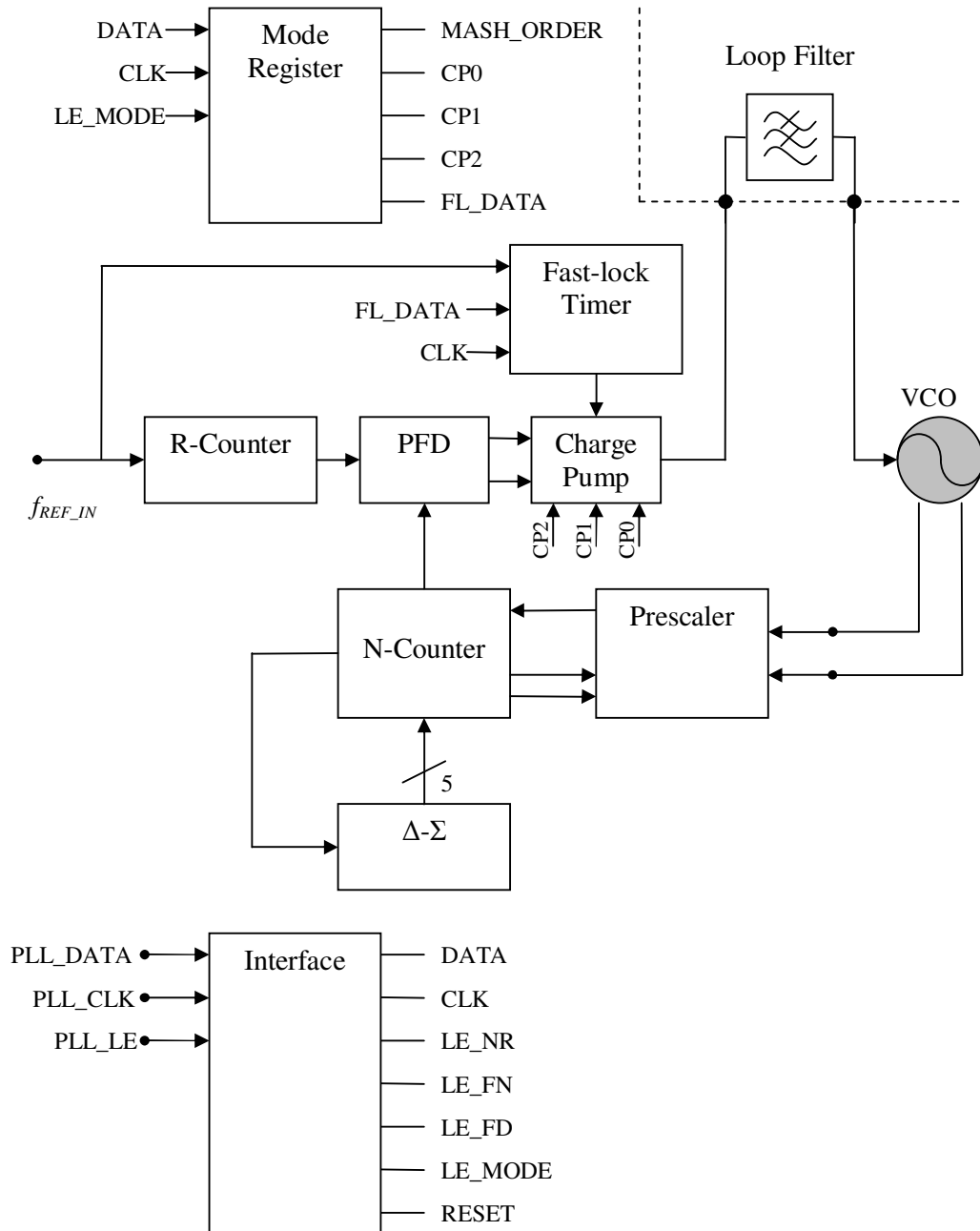


Figure 4.1 Fractional-N frequency synthesizer block diagram

Table 4.1 Proposed design specification for frequency synthesizer

| Parameter              | Unit           | Min    | Typ         | Max    |
|------------------------|----------------|--------|-------------|--------|
| Operating frequency    | MHz            | 2400.0 | 2450.0      | 2500.0 |
| Operating voltage      | V              | 3.0    | 3.3         | 3.6    |
| Current consumption    | mA             |        | <25.0       |        |
| Operating temperature  | <sup>0</sup> C | -40.0  |             | +85.0  |
| Simulation temperature | <sup>0</sup> C | -40.0  | +27.0       | +90.0  |
| Reference frequency    | MHz            |        | 25.0        |        |
| Channel spacing        | kHz            |        | 50.0        |        |
| Modulus P              |                |        | 16/17/20/21 |        |

#### 4.1.1 Counters

There are three counters, namely R-Counter, N-Counter and Fast-lock Timer. Both the R-Counter and Fast-lock Timer have same counting units, which are implemented using complete synchronous logic design for easy expansion to higher number of bits, but different control units. There are hardware handshaking signals between the counting unit and control unit, and there is no process-related delay cell involved so as to ease the deployment of the counters to other process. N-counter consists of A-Counter, B-Counter and C-Counter. It is capable of supporting 910MHz and 2450MHz operations, with its initial value varying according to the output of MASH.

Table 4.2 shows the register map for the six registers in the frequency synthesizer, namely: R-Counter Register, N-Counter Register, FN Register, FD Register, Fast-lock Timer Register, and Operational Mode Register.

Table 4.2 PLL frequency synthesizer and operational mode register map

| Counter/<br>Register | C0 | C1 | 2   | 3   | 4   | 5   | 6   | 7   | 8   | 9   | 10  | 11            | 12  | 13/<br>18 | 14/<br>19 |
|----------------------|----|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|---------------|-----|-----------|-----------|
| RN                   | 0  | 0  | R0  | R1  | R2  | R3  | N0  | N1  | N2  | N3  | N4  | N5            | N6  | N7        | N8        |
| FN                   | 1  | 0  | FN0 | FN1 | FN2 | FN3 | FN4 | FN5 | FN6 | FN7 | FN8 | X(Don't Care) |     |           |           |
| FD                   | 0  | 1  | FD0 | FD1 | FD2 | FD3 | FD4 | FD5 | FD6 | FD7 | FD8 | X(Don't Care) |     |           |           |
| MODE                 | 1  | 1  | MO  | CO0 | CO1 | CP0 | CP1 | CP2 | FLE | FL0 | FL2 | FL3           | ... | FL10      | FL11      |

The R-Counter Register has 4 bits, represented by R0 (least significant bit, LSB) to R3 (most significant bit, R3); N-Counter Register has 9 bits, represented by N0 (LSB) to N8 (MSB); FN Register has 9 bits, represented by FN0 (LSB) to FN8 (MSB); FD Register has 9 bits, represented by FD0 (LSB) to FD8 (MSB); Operational Mode Register has 7 bits, represented by MO, CO0, CO1, CP0, CP1, CP2 and FLE.

### **R-Counter**

R-Counter divides down the frequency of input reference signal, and PFD will compare the divided reference signal to the divided LO signal. Assuming the R-Counter input signal has frequency  $f_{REF\_IN}$ , R-Counter output signal has frequency  $f_{REF}$ , and R-Counter has value R,

$$f_{REF} = \frac{f_{REF\_IN}}{R} \quad (4.1)$$

If the built-in crystal PAD and external crystal are the reference source,  $f_{REF\_IN}$  is the oscillating frequency of the crystal.

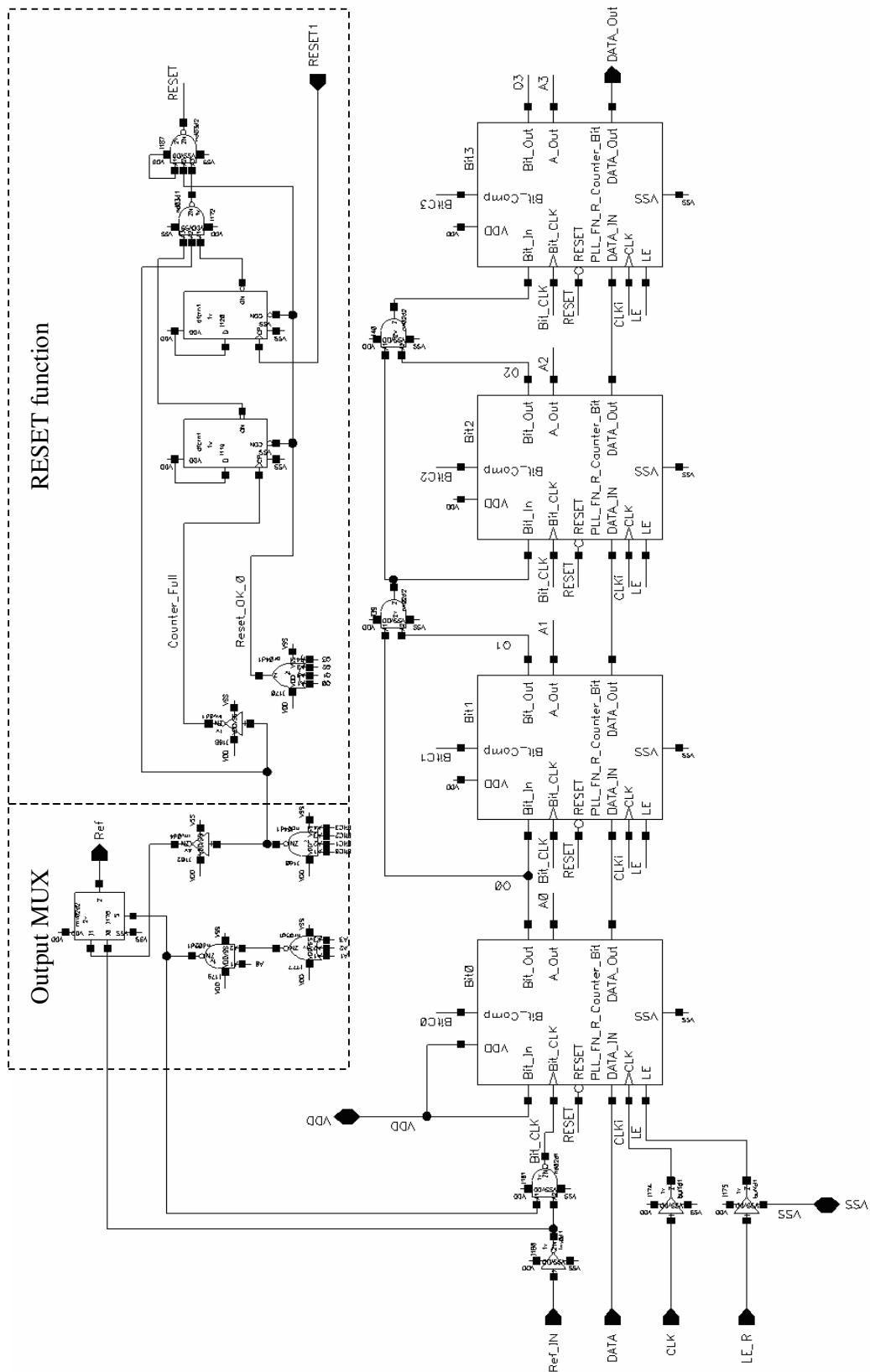


Figure 4.2 R\_Counter block diagram

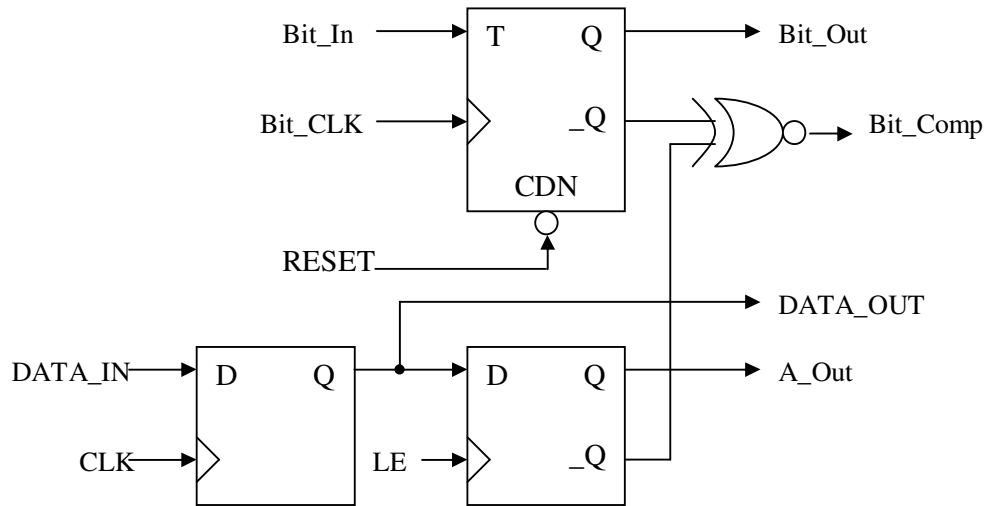


Figure 4.3 R\_Counter\_Bit schematic

Figure 4.2 shows the block diagram of reference counter (i.e. R\_Counter), which consists of 4-bit shift register, 4-bit synchronous counter, comparator and reset function when counter is full. Each bit counter (i.e. R\_Counter\_Bit) is implemented as shown in Figure 4.3. After the data (i.e. R0-R3) from the register has been latched onto R-Counter, bit-comparator will start comparing each data bit with the respective counter's output bit. The synchronous counter will start counting from "0000" until all  $DATA\_OUT = Bit\_Out$ , and  $f_{REF\_IN}$  is being divided by R during the process and output as  $f_{REF}$ . Then, RESET function will send a "0" to all bit counters to clear the counter back to "0000". Once the reset is accomplished, signal will be fed back to the reset logic. RESET will send a "1" to all bit counters and R-Counter is ready for the next counting cycle.

### N-Counter

Figure 4.4 shows the implementation of N-Counter, which is formed by A-Counter, B-Counter and C-Counter. Assuming the minimum division ratio of prescaler is P and it is a multiple of 4, the counters must satisfy the following conditions:

$$C = N \text{ div } P, A = N \text{ mod } P \quad (4.2)$$

$$B = (N - A - P * C) / 4 \quad (4.3)$$

$$N = (P * C) + (4 * B) + A \quad (4.4)$$

with  $C \geq \max\{A, B\}$ ,  $A < 4$  and  $B < P/4$ .

Both A-Counter and B-Counter are 2-bit synchronous counters, and C-Counter is a 6-bit synchronous counter. Each counter bit is implemented as shown in Figure 4.5.

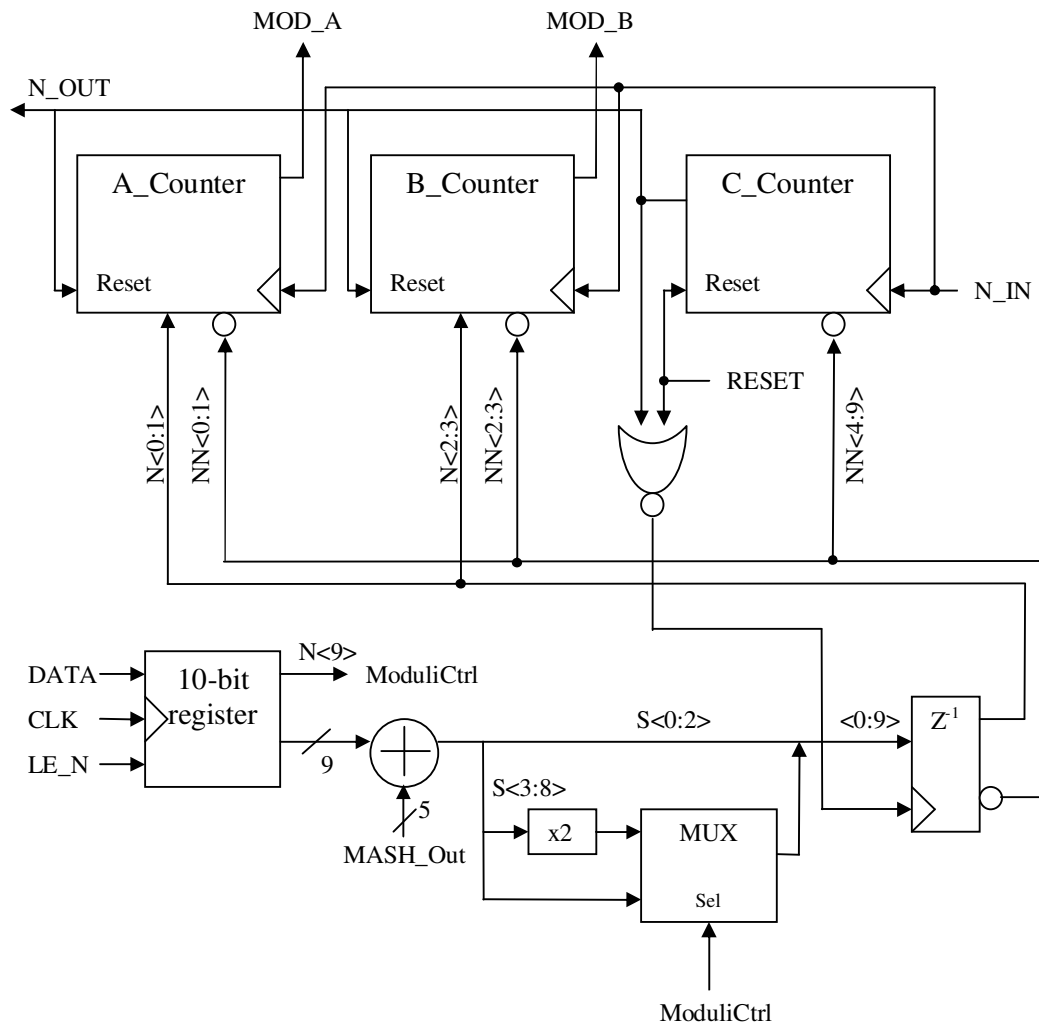


Figure 4.4 N\_Counter block diagram



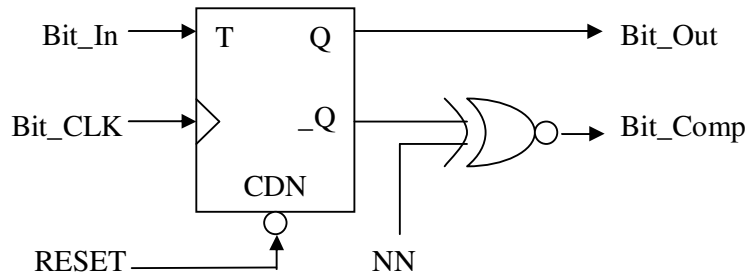


Figure 4.5 Counter\_Bit schematic

The pseudo-random number from MASH is added to the N-Counter register value, and set as the initial value for N-Counter. N-Counter will divide down the Prescaler output frequency before feeding the signal back to MASH and PFD, and generate the Prescaler division-ratio control signals (MOD\_A and MOD\_B).

#### 4.1.2 MASH

MASH generates pseudo-random numbers based on the numerator and denominator value set by FN Register and FD Register respectively, and can function as a third-order or forth-order modulator. The generated pseudo-random number is added to the value indicated by N-Counter Register, and set as initial value of N-Counter. N-Counter divides down the frequency of LO signal, and PFD will compare the divided LO signal to the divided reference signal. Assuming LO signal has frequency  $f_{LO}$ , and prescaler has modulus value  $P$ ,

$$f_{LO} = P * \left( N + \frac{FN}{FD} \right) * f_{REF} \quad (4.5)$$

where N is the value of N-Counter Register, FN is the value of FN Register, and FD is the value of FD Register. Figure 4.6 shows the block diagram of MASH, and Figure

4.7 shows the implementation of four order MASH with option of choosing either 3<sup>rd</sup> or 4<sup>th</sup> order via the “ORDER” pin.

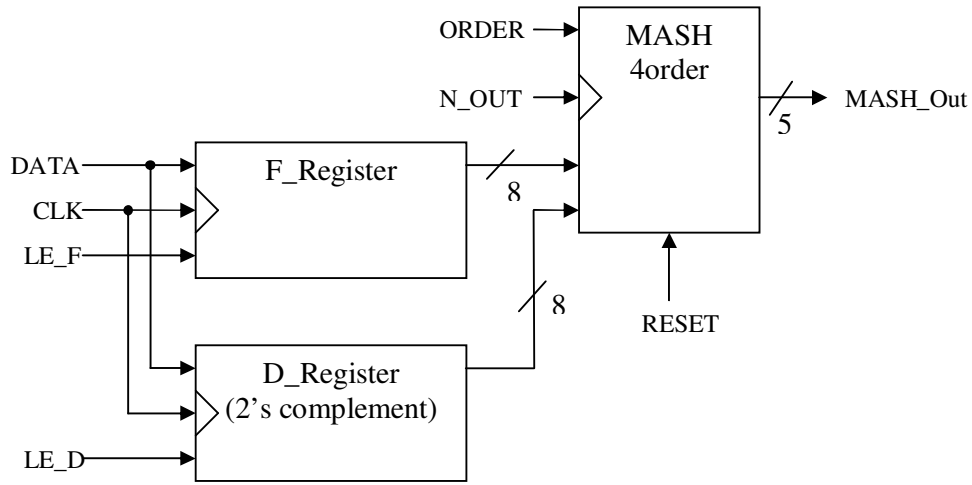


Figure 4.6 MASH block diagram

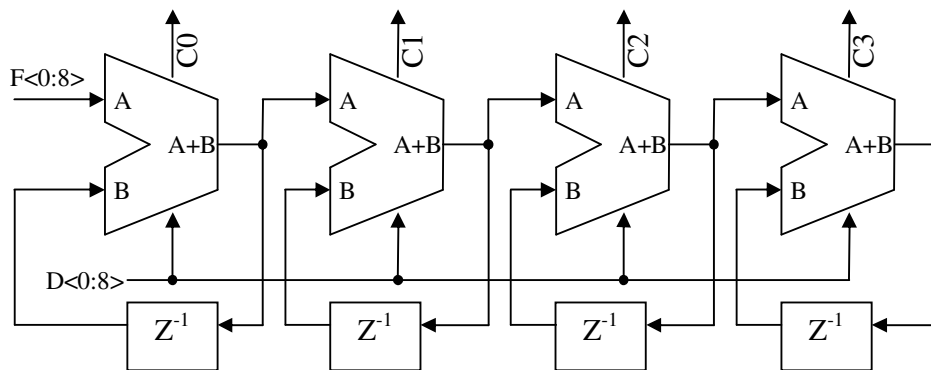
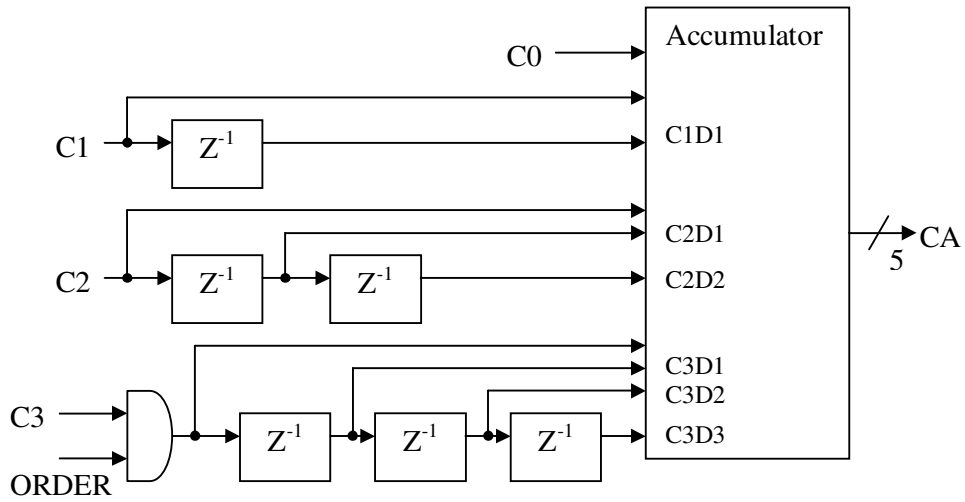


Figure 4.7 MASH\_4order schematic

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After the DATA is latched to the outputs of F-register (denotes as FO) and D-register (denotes as DO) respectively, at the rising edge of N\_OUT pulse (i.e. the clock for MASH\_4order)

For  $i = 0,1,2,3$ ,

$$Sum(i) = pSum(i-1) + pSum(i) \quad (4.6)$$

If  $Sum(i) \geq DO$ ,

$$Ci = 1; pSum(i) = Sum(i) - DO \quad (4.7)$$

Else

$$Ci = 0; pSum(i) = Sum(i) \quad (4.8)$$

If  $ORDER = 3$ ,

$$MO3 = C0 + C1 - C1D1 + C2 - (2 * C2D1) + C2D2 \quad (4.9)$$

If  $ORDER = 4$ ,

$$MO4 = MO3 + C3 - (3 * C3D1) + (3 * C3D2) - C3D3 \quad (4.10)$$

where  $pSum(-1) = FO$ ,  $MO3 = \text{MASH\_Out } 3^{\text{rd}}$  order,  $MO4 = \text{MASH\_Out } 4^{\text{th}}$  order.

### 4.1.3 Interface

The 3-wire serial interface is designed for receiving external PLL control commands, enabling frequency setting and output signal selection. It abides by an industrial standard timing diagram. Figure 4.8 illustrates the block diagram of Interface.

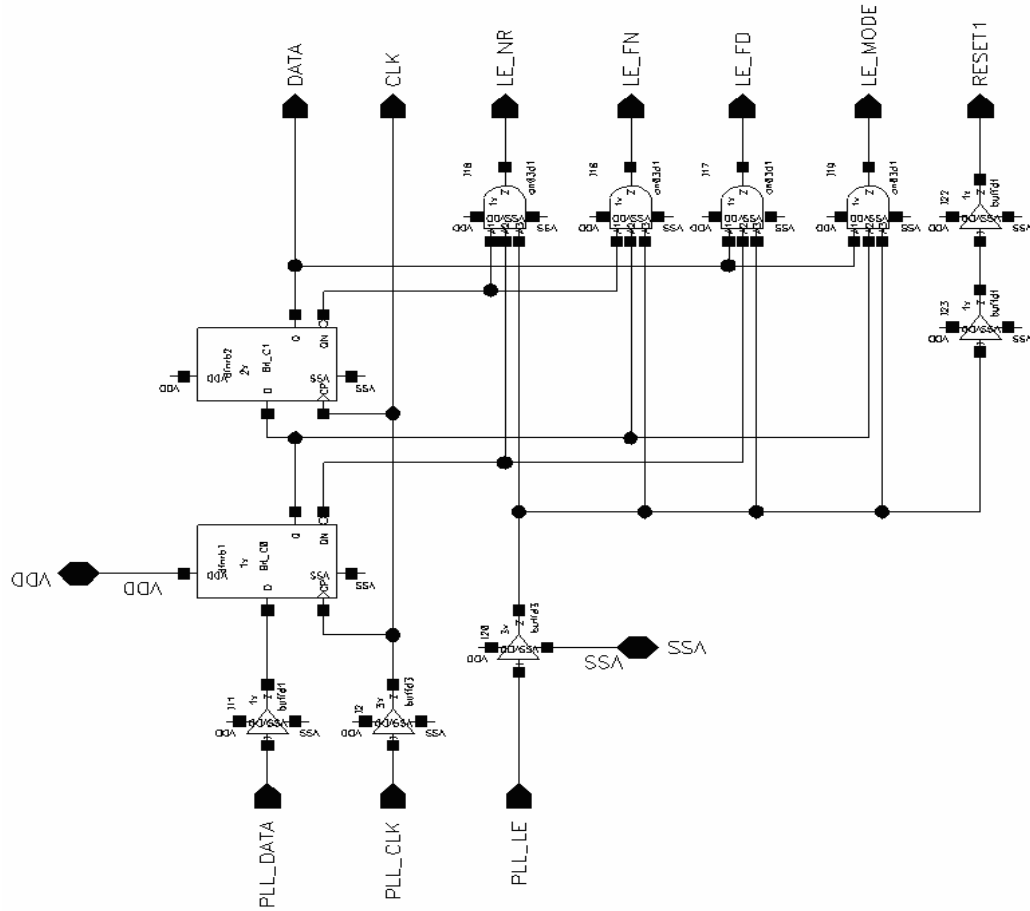
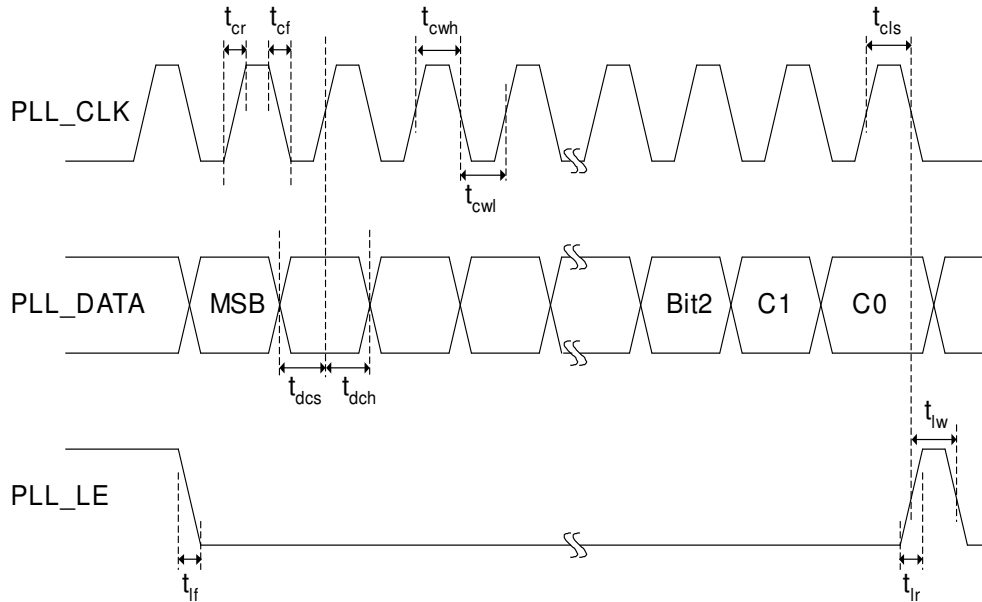


Figure 4.8 Interface block diagram

Data is latched into selective register(s) via the use control bits, i.e. C0 and C1, of the Interface (Table 4.2). R-Counter Register and N-Counter Register share the same control-bits configuration, while Operational Mode Register and Fast-lock Timer Register share the same configuration. The serial data is clocked on the rising edge of the serial clock, and is latched into the destined registers on the rising edge of PLL\_LE, as shown in Figure 4.9.



\*Symbol definitions are defined in Table 4.12

Figure 4.9 PLL synthesizer serial interface timing diagram

#### 4.1.4 Mode Register

Mode Register is used to set the MASH order, output signal from frequency synthesizer, and the charge pump current. Figure 4.10 shows the Mode Register block diagram, which is formed by 6-bit serial-in, parallel-out shift register and 6-bit parallel-in, parallel-out shift register.

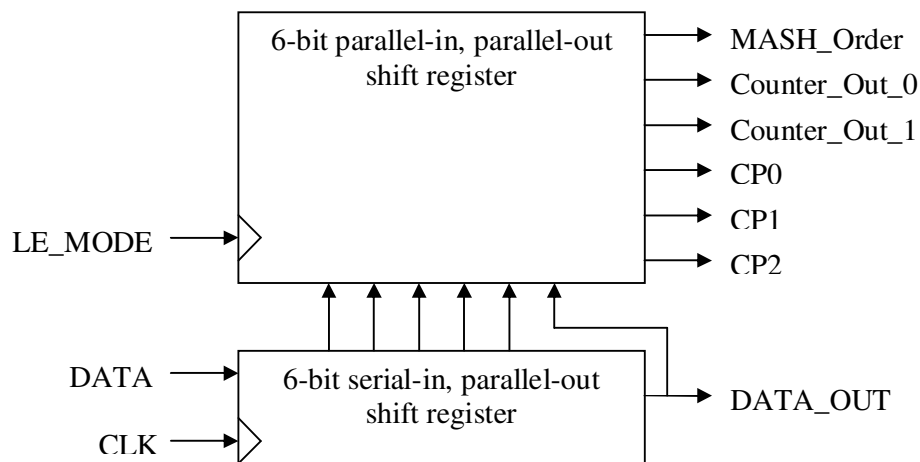


Figure 4.10 Mode Register block diagram

Operating Mode Register has 7 bits, i.e. MO, CO0, CO1, CP0, CP1, CP2 and FLE (Table 4.2). The order of MASH, i.e. 3<sup>rd</sup> order or 4<sup>th</sup> order, is set by MO as depicted by Table 4.3.

Table 4.3 Setting for order of MASH

| MO | MASH order |
|----|------------|
| 0  | 3          |
| 1  | 4          |

CO0 and CO1 are used to select the output signal to be transmitted to “Counter\_Out” pin, from the output of R-Counter, Prescaler, Divider\_N or Lock Detect. The settings are as defined in Table 4.4.

Table 4.4 Settings for output signal at “Counter\_Out” pin

| CO0 | CO1 | Output at “Counter_Out” |
|-----|-----|-------------------------|
| 0   | 0   | R-Counter               |
| 1   | 0   | Prescaler               |
| 0   | 1   | Divider_N               |
| 1   | 1   | Lock Detect             |

Fast-Lock Enable (FLE) bit is used to activate or de-activate the fast-lock function with bit value “1” or “0”, respectively. FLE, CP0, CP1 and CP2 will set the Charge Pump current, in accordance with Table 4.5.

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Table 4.5 Charge Pump current control table

| CP2 | CP1 | CP0 | Current<br>( $\mu$ A) |
|-----|-----|-----|-----------------------|
| 0   | 0   | 0   | 200                   |
| 0   | 0   | 1   | 400                   |
| 0   | 1   | 0   | 600                   |
| 0   | 1   | 1   | 800                   |
| 1   | 0   | 0   | 2000                  |
| 1   | 0   | 1   | 3200                  |

---

#### 4.1.5 MUX\_Output

MUX\_Output is an output driver for the selection and transmission of output signals from R-Counter, prescaler, divider and lock detector.

#### 4.1.6 PFD and Charge Pump

PFD compares the phase and frequency difference between reference signal and divided LO signal while Charge Pump will either source or sink current from the external loop-filter. In this design, Charge Pump supports fast-lock function and has six available current selections.

The operation of the PFD is as follow:

- if  $f_{REF\_IN} > f_{DIV\_IN}$ , positive pulses will be generated at UP while DN=0
- if  $f_{REF\_IN} < f_{DIV\_IN}$ , positive pulses will be generated at DN while UP=0

- if  $f_{REF\_IN} = f_{DIV\_IN}$ , positive pulses will be generated at either UP or DN with width equals to phase difference between REF\_IN and DIV\_IN.

Figure 4.11 shows the PFD state diagram, Figure 4.12 shows the block diagram for PFD [41, 42] and Figure 4.13 shows the implementation of the edge-triggered flip-flop. Figure 4.14 shows the design for Charge Pump, with 4 control pins: CP0, CP1, CP2 and FastLock. A feedback amplifier is added to the Charge Pump output to maintain the output dc voltage at close to  $V_{dd}/2$ . Table 4.6 shows the control table for decoder.

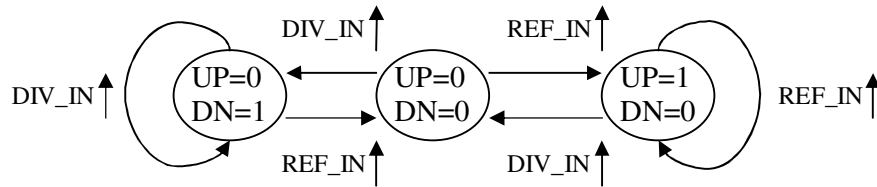


Figure 4.11 PFD state diagram

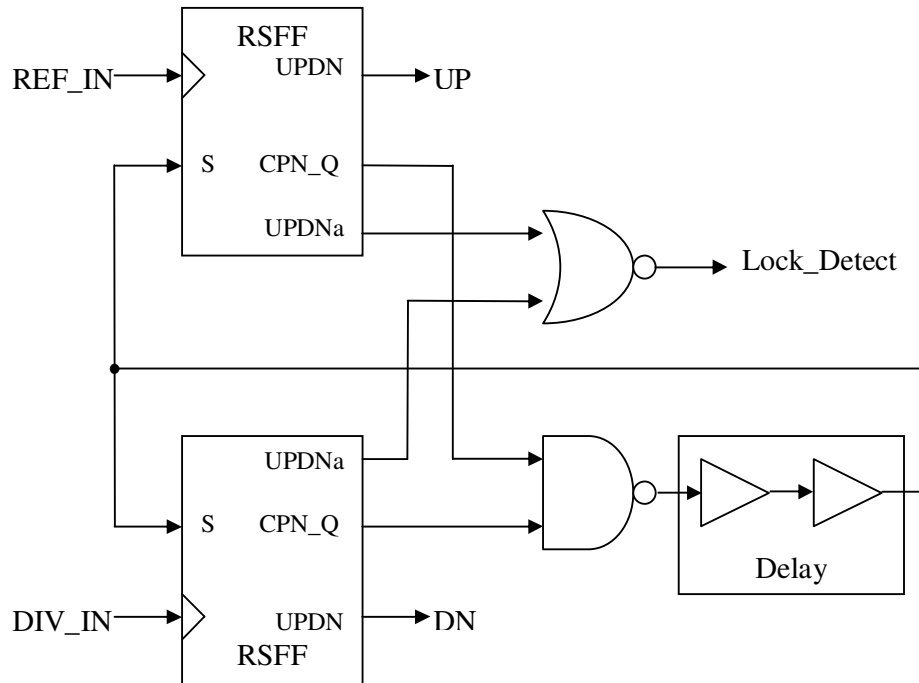


Figure 4.12 PFD block diagram



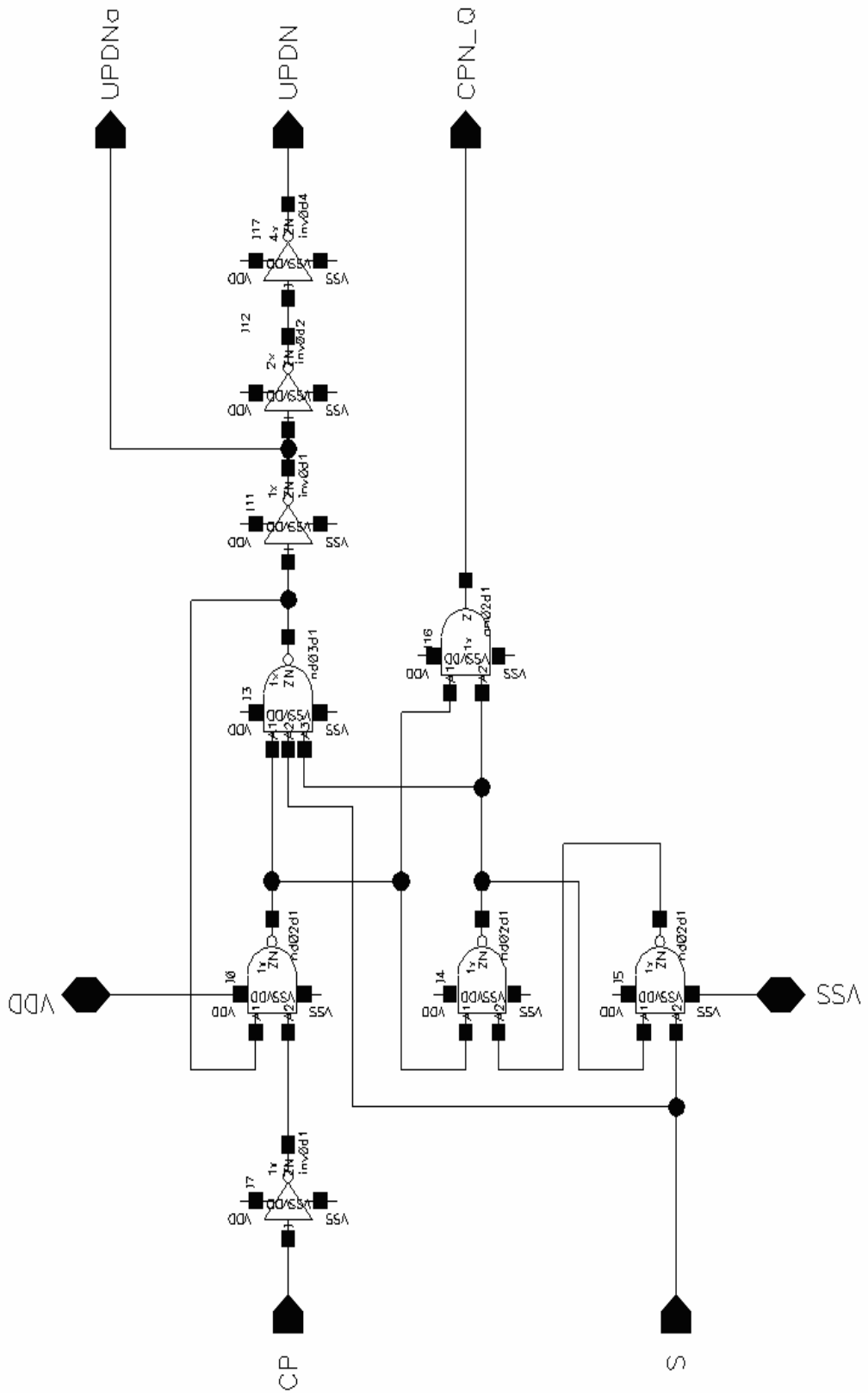


Figure 4.13 PFD\_RSFF schematic

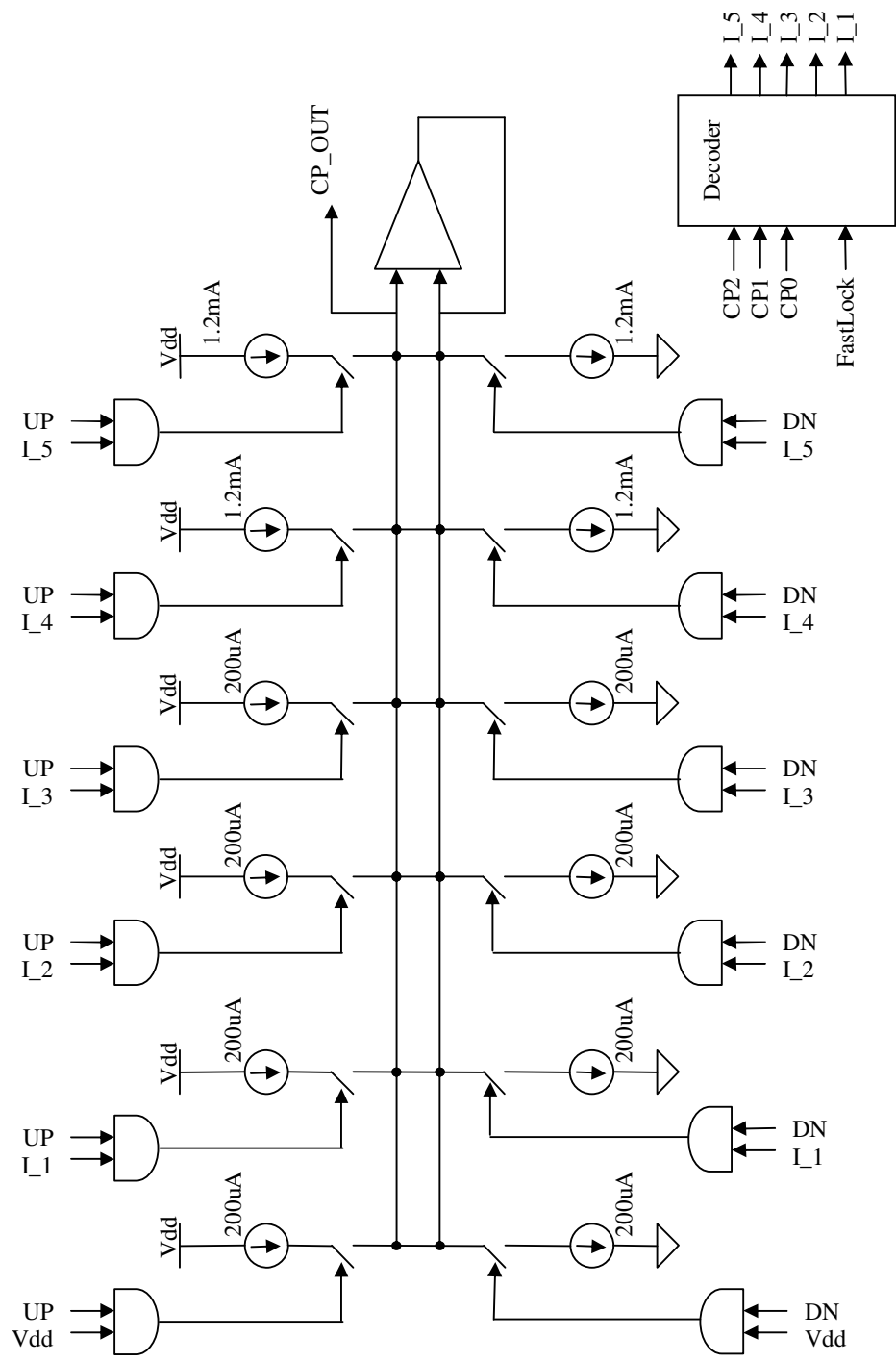


Figure 4.14 CP block diagram

Table 4.6 Decoder control table

| Fastlock | CP2 | CP1 | CP0 | Decoder output |     |     |     |     |     | CP_OUT<br>( $\mu$ A) |
|----------|-----|-----|-----|----------------|-----|-----|-----|-----|-----|----------------------|
|          |     |     |     | I_5            | I_4 | I_3 | I_2 | I_1 | I_0 |                      |
| 0        | 0   | 0   | 0   | 0              | 0   | 0   | 0   | 0   | 1   | 200                  |
| 0        | 0   | 0   | 1   | 0              | 0   | 0   | 0   | 1   | 1   | 400                  |
| 0        | 0   | 1   | 0   | 0              | 0   | 0   | 1   | 1   | 1   | 600                  |
| 0        | 0   | 1   | 1   | 0              | 0   | 1   | 1   | 1   | 1   | 800                  |
| 0        | 1   | 0   | 0   | 0              | 1   | 1   | 1   | 1   | 1   | 2000                 |
| 0        | 1   | 0   | 1   | 1              | 1   | 1   | 1   | 1   | 1   | 3200                 |
| 0        | 1   | 1   | 0   | 0              | 0   | 1   | 1   | 1   | 1   | 800                  |
| 0        | 1   | 1   | 1   | 0              | 0   | 1   | 1   | 1   | 1   | 800                  |
| 1        | x   | x   | x   | 1              | 1   | 1   | 1   | 1   | 1   | 3200                 |

#### 4.1.7 Loop Filter and VCO

Loop Filter is constructed by external resistors and capacitors, and modified according to measurement results. VCO is represented by Verilog-A code for the functional test of the synthesizer. In order to analyze the loop filter, the entire PLL loop has to be taken into consideration. Figure 4.15 shows the linear model of PLL.

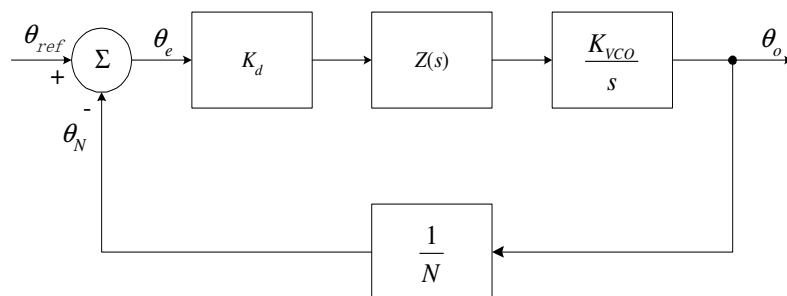


Figure 4.15 Linear model of PLL

The output current of PFD and Charge Pump is given by

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$$I_d(t) = K_d \theta_e \quad (4.11)$$

where  $\theta_e$  is the phase error and  $K_d$  is the PFD gain. The VCO angular frequency  $\omega$  is

$$\omega(t) = \omega_0 + K_{VCO} u_f(f) \quad (4.12)$$

where  $K_{VCO}$  is the VCO gain in  $rad.s^{-1}.V^{-1}$ . The open-loop gain of PLL is defined as

$$G(s) = \frac{\theta_N}{\theta_e} = \frac{K_d K_{VCO}}{N} \frac{Z(s)}{s} \quad (4.13)$$

where  $N$  is the division ratio of frequency divider and  $Z(s)$  is the loop filter transfer function.

The fourth order PLL has a third order loop filter as demonstrated by the schematic in Figure 4.16.

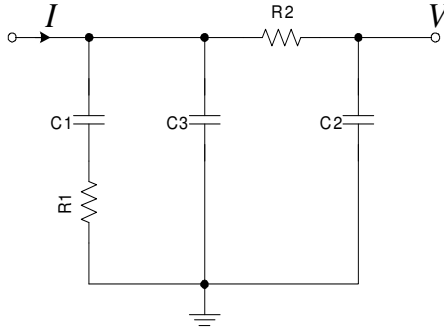


Figure 4.16 Schematic of third order loop filter

The transfer impedance of loop filter can be expressed as

$$Z(s) = \frac{V}{I} = \frac{1}{sC_2 \left( 1 + \frac{Z_2}{Z_1} + \frac{Z_2}{Z_3} \right)} = \frac{1}{sC_2 \left[ 1 + \frac{\left( R_2 + \frac{1}{sC_2} \right) \left( R_2 + \frac{1}{sC_2} \right)}{\left( R_1 + \frac{1}{sC_1} \right) \left( \frac{1}{sC_3} \right)} \right]} \quad (4.14)$$

---

where  $Z_1 = R_1 + \left(\frac{1}{sC_1}\right)$ ,  $Z_2 = R_2 + \left(\frac{1}{sC_2}\right)$ ,  $Z_3 = \frac{1}{sC_3}$ .

Eq. (4.14) can be further expanded and factorized to

$$Z(s) = \frac{1 + sR_1C_1}{s(C_1 + C_2 + C_3) + s^2(R_1C_1C_2 + R_1C_1C_3 + R_2C_1C_2 + R_2C_2C_3) + s^3R_1R_2C_1C_2C_3} \quad (4.15)$$

$$Z(s) = \frac{1 + s\tau_1}{s(as^2 + bs + c)} = \frac{1 + s\tau_1}{s(s + s_1)(s + s_2)}, \quad s_{1,2} = \frac{b \pm \sqrt{\Delta}}{2a} > 0 \quad (4.16)$$

where

$$\tau_1 = R_1C_1, \quad \tau_2 = R_2C_2, \quad a = \tau_1\tau_2C_3, \quad b = \tau_1(C_2 + C_3) + \tau_2(C_1 + C_3), \quad c = C_1 + C_2 + C_3$$

$$\Delta = b^2 - 4ac = [\tau_1(C_2 + C_3) - \tau_2(C_1 + C_3)]^2 + 4\tau_1\tau_2C_1C_2 > 0$$

Substituting Eq. (4.16) into Eq. (4.13) will give

$$G(s) = \frac{K_d K_{VCO}}{N} \frac{1 + s\tau_1}{s^2(s + s_1)(s + s_2)} \quad (4.17)$$

From Eq. (4.17), it can be observed that there are one zero and two poles in the open left-half plan and two poles at the origin, rendering the PLL not absolutely stable.

A second order loop filter should be used for better implementation of Fast-lock function. If  $R_2$  and  $C_2$  in Figure 4.16 are set to zero, the loop filter will become second order with the following transfer impedance

$$Z(s) = \frac{1 + sR_1C_1}{s(C_1 + C_3) + s^2R_1C_1C_3} \quad (4.18)$$

$$Z(s) = \frac{\tau_2}{C_3\tau_1} \frac{1 + s\tau_1}{s(1 + s\tau_2)} \quad (4.19)$$

---

where  $\tau_1 = R_1 C_1$  and  $\tau_2 = R_1 \left( \frac{C_1 C_3}{C_1 + C_3} \right)$ . The open loop gain Eq. (4.17) is redefined as

$$G(s) = \frac{K_d K_{VCO}}{N} \frac{\tau_2}{C_3 \tau_1} \left[ \frac{1 + s \tau_1}{s^2 (1 + s \tau_2)} \right] \quad (4.20)$$

With  $s = j\omega$ , Eq. (4.20) can be expressed as

$$G(j\omega) = - \left[ \frac{K_d K_{VCO}}{N} \frac{\tau_2}{\omega^2 C_3 \tau_1} \frac{1 + j\omega \tau_1}{1 + j\omega \tau_2} \right] \quad (4.21)$$

Phase of  $G(j\omega)$  is given by

$$\phi(\omega) = \tan^{-1}(\omega \tau_1) - \tan^{-1}(\omega \tau_2) - 180^\circ \quad (4.22)$$

Phase margin is defined as

$$\phi_{margin}(\omega) = \tan^{-1}(\omega \tau_1) - \tan^{-1}(\omega \tau_2) \quad (4.23)$$

In order to execute the Fast-lock function, resistor of the loop filter has to be resized.

Let  $R_1' = \frac{R_1}{n}$ ,

$$\tau_1' = \frac{\tau_1}{n}, \quad \tau_2' = \frac{\tau_2}{n}, \quad \phi'(\omega') = \tan^{-1}\left(\frac{\omega'}{n} \tau_1\right) - \tan^{-1}\left(\frac{\omega'}{n} \tau_2\right) \quad (4.24)$$

To maintain constant phase margin as obtained from Eq. (4.21),

$$\phi'(\omega') = \tan^{-1}\left(\frac{\omega'}{n} \tau_1\right) - \tan^{-1}\left(\frac{\omega'}{n} \tau_2\right) = \phi(\omega) = \tan^{-1}(\omega \tau_1) - \tan^{-1}(\omega \tau_2) \quad (4.25)$$

From Eq. (4.25), it shows that the loop bandwidth has been extended by  $n$  time ( $\omega' = n\omega$ ), resulting in the reduction of locking time by  $n$  times. In order to maintain constant gain with extended bandwidth,

$$G'(j\omega') = -\left[ \frac{K_d' K_{VCO}}{N} \frac{\tau_2'}{\omega'^2 C_3 \tau_1'} \frac{1+j\omega'\tau_1'}{1+j\omega'\tau_2'} \right] = G(j\omega) = -\left[ \frac{K_d K_{VCO}}{N} \frac{\tau_2}{\omega^2 C_3 \tau_1} \frac{1+j\omega\tau_1}{1+j\omega\tau_2} \right] \quad (4.26)$$

where  $\frac{K_d'}{\omega'^2} = \frac{K_d}{\omega^2}$ ,  $K_d' = \frac{\omega'^2}{\omega^2} K_d = n^2 K_d$ . Hence, the conditions for bandwidth extension are  $R_1' = \frac{R_1}{n}$ ,  $K_d' = n^2 K_d$  and  $\omega' = n\omega$ .

Figure 4.17 illustrates the schematic of Loop Filter with Fast-lock function. “FL” is the fast-lock function control switch that has to be connected to the chip’s “Fast-lock Control” pin. For enhanced fast-lock performance, R2\* should be shorted and C2\* should be opened. Otherwise, R2\* and C2\* can be optimized for enhanced noise suppression capability.

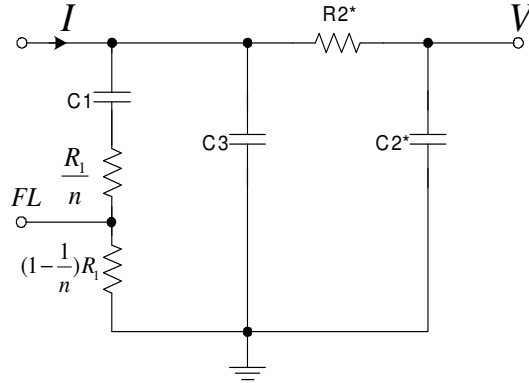


Figure 4.17 Schematic of loop filter with Fast-lock function

Figure 4.18 shows the schematic of actual Loop Filter design which is used for PLL locking simulation. The expected locking time for this fast-lock-incorporated loop filter is 4 times shorter than normal loop filter without fast-lock function.

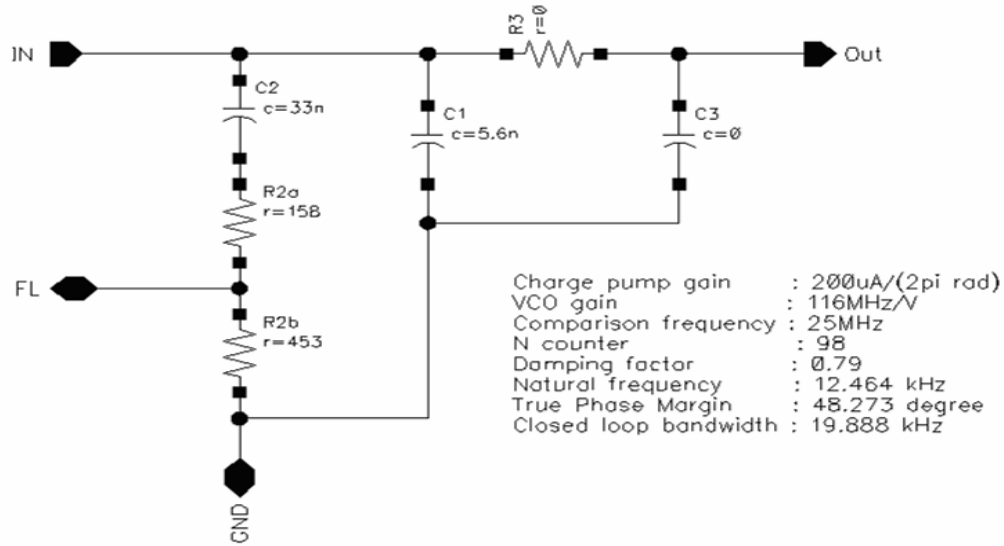


Figure 4.18 LP\_Filter schematic

#### 4.1.8 Fast-lock Control Switch

Fast-lock Timer Register has 12 bits, represented by FL0 (LSB) to FL11 (MSB) (Table 4.2). When FLE is set to “1” and Fast-lock Timer Register has a non-zero preset value, the fast-lock function will be activated. The Fast-lock Control switch will be turned on, and Charge Pump will function at its maximum supply current of 3.2mA. Once any of the registers (as listed in Table 4.2) is set, the Fast-lock Timer will start counting the number of input-reference-signal pulses. When the number of pulses fulfills the preset value, fast-lock function will be deactivated and Fast-lock Control switch will be turned off, leaving the Charge Pump to function at the supply current set by CP0, CP1 and CP2.

Assuming the preset value of Fast-lock Timer is FL and the period of Fast-lock Timer is  $t_{Fast-lock}$ ,

$$t_{Fast-lock} = \frac{FL}{f_{REF\_IN}} \quad (4.27)$$



Figure 4.19 shows the design of Fast-lock Counter, which consists of 12-bit shift register, 12-bit synchronous counter, comparator and reset function when counter is full. Each bit counter design is as shown in Figure 4.3. Fast-lock Control Switch is an analog switch that functions with Fast-lock Timer and external loop-filter by connecting the “FL\_Gnd” pin to external ground when the Fast-lock function is activated.

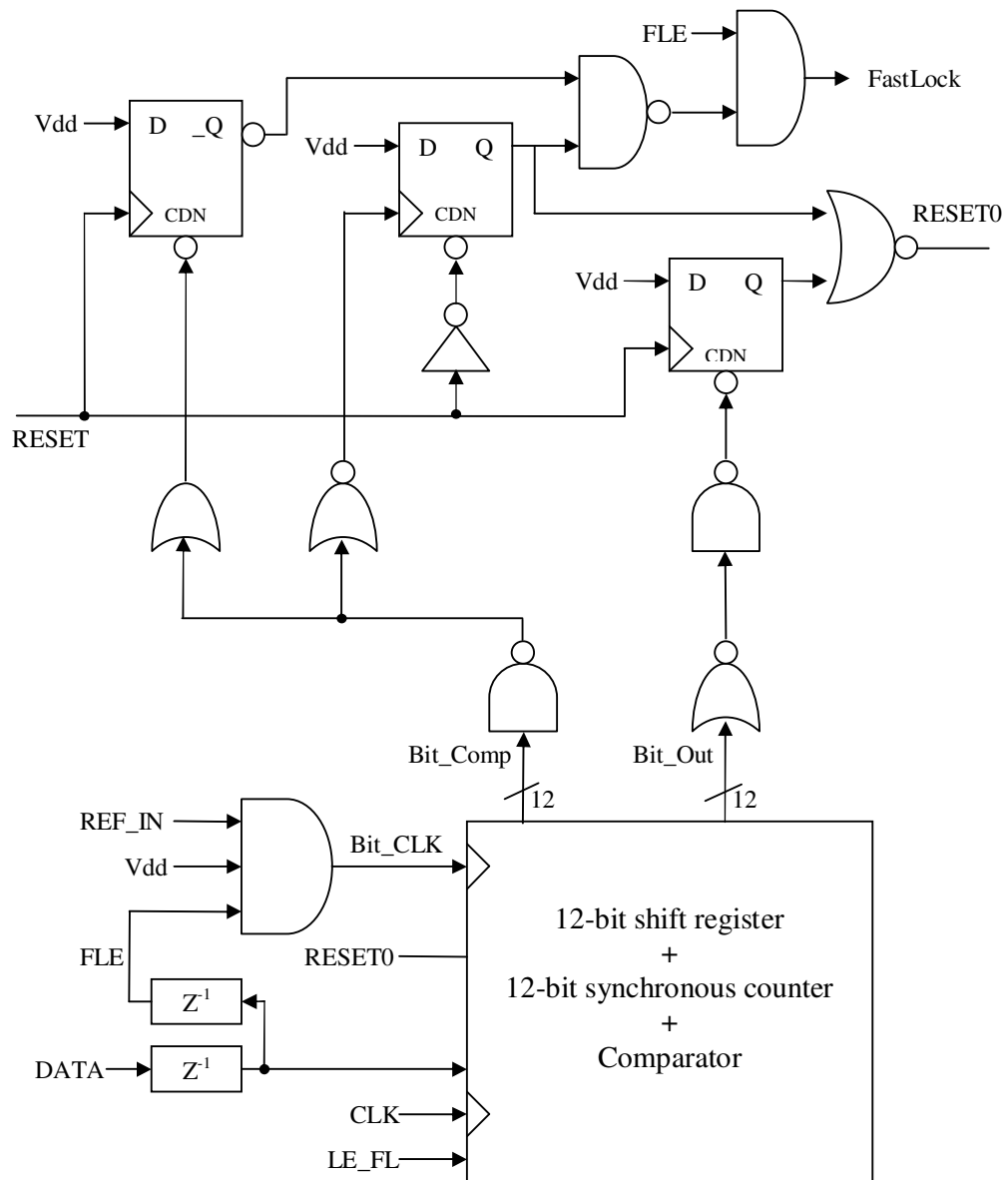


Figure 4.19 Fast-lock Counter block diagram

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### 4.1.9 Quad-modulus Prescaler

Quad-modulus Prescaler which provides four division ratios, i.e. divide-by-16/17/20/21 is designed for the 2450MHz frequency band operation. A higher modulus prescaler enables the system to achieve lower minimum continuous divide ratio and attain wider range of N-Counter value. However, the maximum operating frequency might be lower for prescaler with similar topology but higher modulus.

Table 4.7 illustrates effect of prescaler moduli on the minimum N-Counter value.

Table 4.7 Effect of prescaler moduli on minimum continuous divide ratio

| Prescaler             | Type         | Minimum N-Counter value |
|-----------------------|--------------|-------------------------|
| $P/(P+1)$             | dual-modulus | $P*(P-1)$               |
| e.g. 4/5              |              | 12                      |
| e.g. 8/9              |              | 56                      |
| $P/(P+1)/(P+4)/(P+5)$ | quad-modulus | $\max\{P/4 - 1, 3\}*P$  |
| e.g. 4/5/8/9          |              | 12                      |
| e.g. 8/9/12/13        |              | 24                      |

Although the prescaler provides four division ratios, only three will be used to produce a given N-Counter value.

## 4.2 Quad-Modulus Prescaler Circuit Design

The proposed quad-modulus prescaler design consists of a 3-modulus core divider, an asynchronous divide-by-4 divider and modulus-control logic block. Conventional synchronous divide-by-4/5 counters is modified to form a divide-by-4/5/6, and

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employed in the core divider design such that the maximum operating frequency is comparable to a dual-modulus prescaler while providing multi-modulus operations.

The state diagrams of the core divider are illustrated in Figure 4.20. From the state-transition diagram, it shows that the core divider design concept is feasible because the divider will be able to perform the desired division for respective modulus. Although there is a possibility that the prescaler might not be able to self-start when operating in modulus 6 due to the presence of looping between state “2” and “5”, this potential problem has been eliminated by forcing the prescaler to start from state “0” for every modulus change and the output signal of core divider is picked up at terminal “Q<sub>0</sub>”.

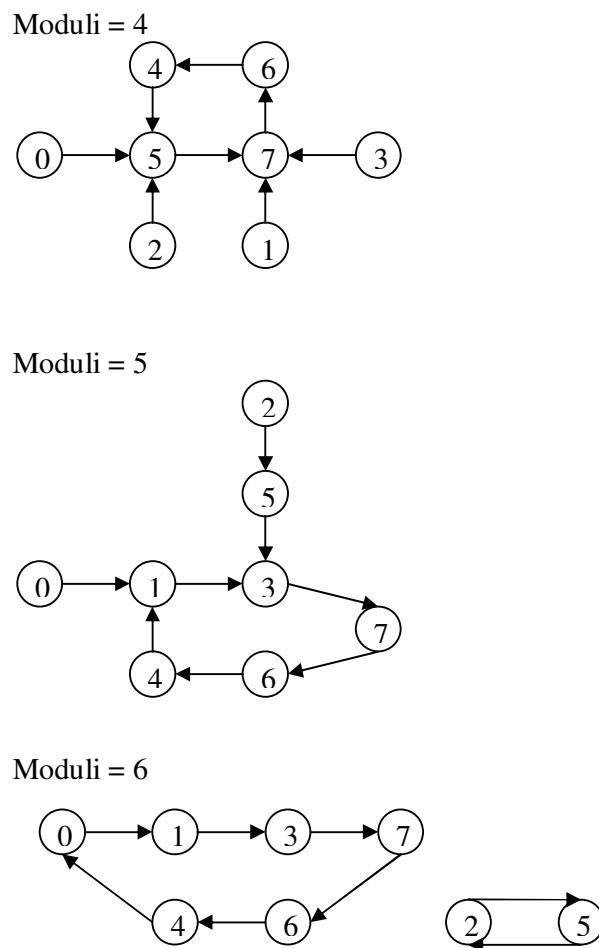


Figure 4.20 State diagrams prescaler core

MOD\_A and MOD\_B are the control signals from N-Counter, which are used to control the division ratio of the prescaler according to the setting listed in Table 4.8.

| Table 4.8 Moduli-control pins setting |       |                |        |
|---------------------------------------|-------|----------------|--------|
| MOD_B                                 | MOD_A | Division ratio |        |
| 0                                     | 0     | $4*4$          | $= 16$ |
| 0                                     | 1     | $(4*3) + 5$    | $= 17$ |
| 1                                     | 0     | $5*4$          | $= 20$ |
| 1                                     | 1     | $(5*3) + 6$    | $= 21$ |

Figure 4.21 shows the design of quad-modulus prescaler which consists of a core divide-by-4/5/6 divider operating at highest frequency, an asynchronous divide-by-4 divider, a high frequency input buffer, a differential-to-single-ended output buffer and modulus-control logic block.

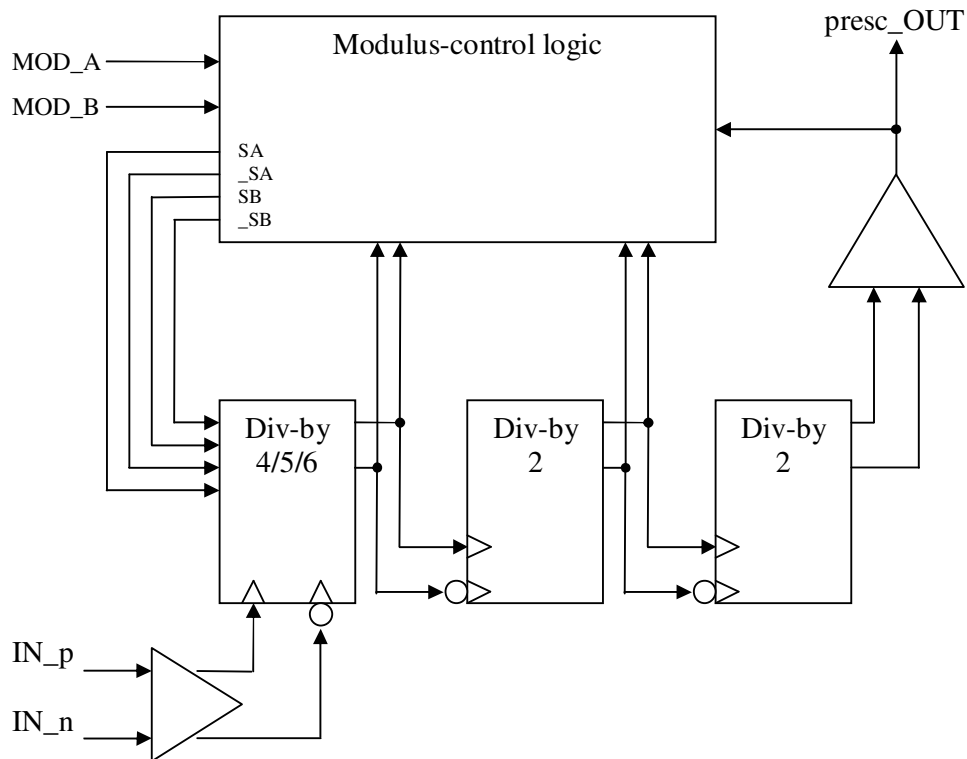


Figure 4.21 Div16172021\_top diagram

Figure 4.22 shows the design of a high speed, high frequency input buffer which has a differential-in, differential-out structure. R0 and R1 are the feedback resistors; C0 and C1 are the ac coupling capacitors. The ac-coupled input buffer is included to prevent loading effect on the VCO whilst providing sufficient voltage swing for the subsequent synchronous divider. Since the structure is ac-coupled to the previous block, feedback resistors are needed to maintain the DC voltage level of input and output ports. Biasing circuit is included for better control of power optimization.

Value of the feedback resistors has to be carefully selected to ensure the stability of buffer and its feedback loading effect, as demonstrated in Figure 4.23. If feedback resistor value is too small, the loading effect of feedback is high. However, as the feedback resistor value increases, the buffer might become conditionally stable with  $K_f < 1$  and  $B_{1f} > 0$ .

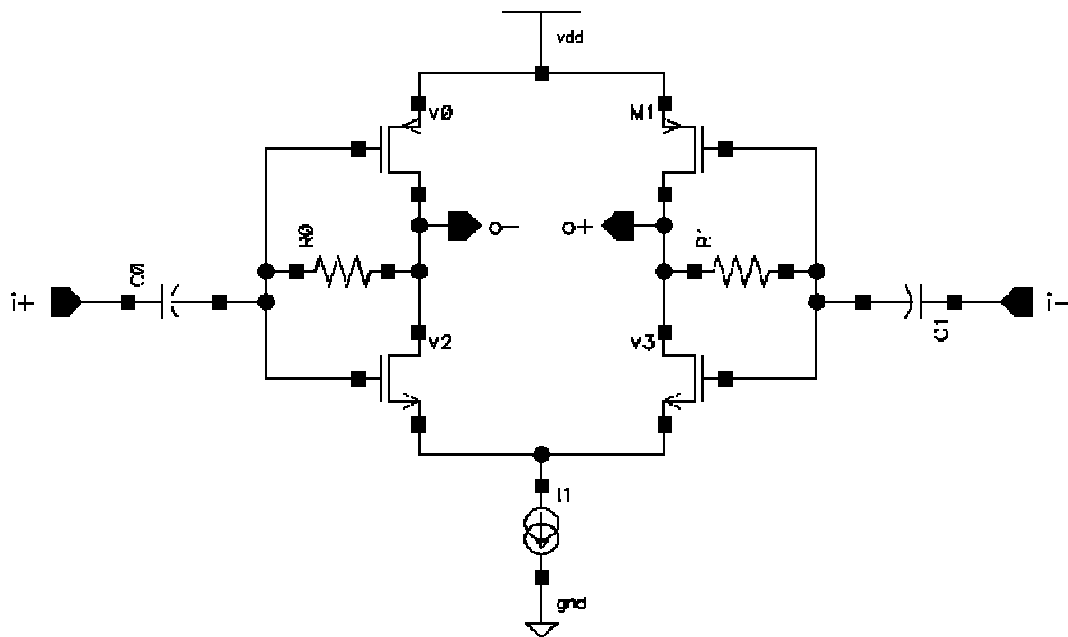


Figure 4.22 Input buffer schematic

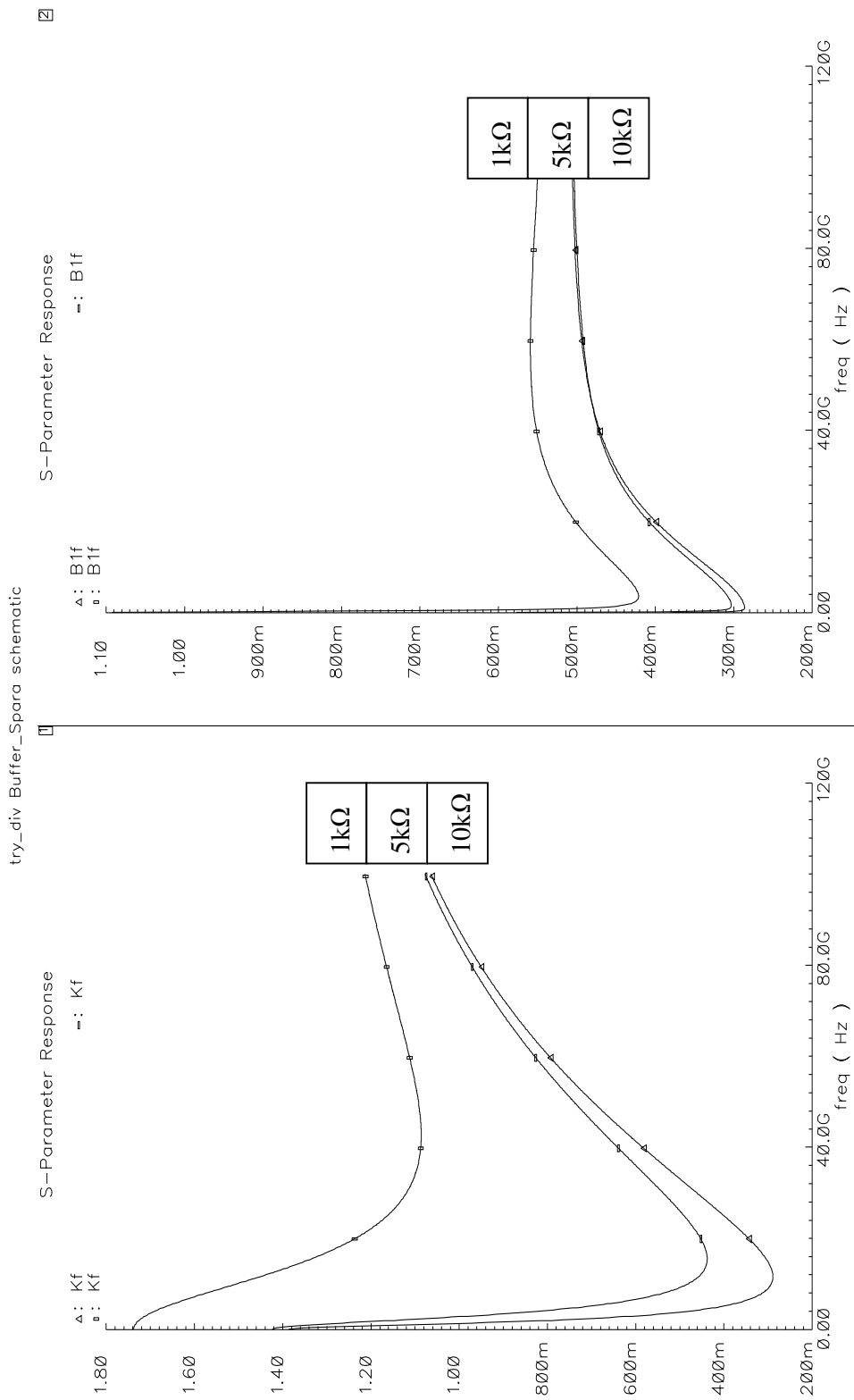


Figure 4.23 Effect of feedback resistor on buffer stability

Figure 4.24 shows the core divider design that consists of three synchronous DFF which are constructed to form a divide-by-4/5/6 divider. SA and SB are the control pins for selecting the division ratio of the core divider. Although the three dividers are operating at the highest frequency, total power consumption can be reduced with proper sizing of transistors and implementation of biasing circuit.

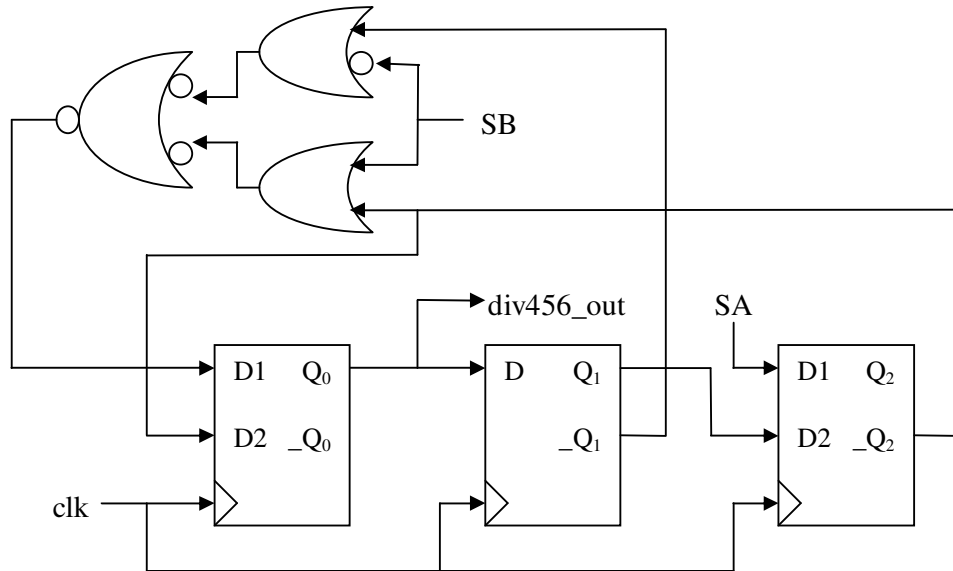


Figure 4.24 Div456\_top block diagram

Table 4.9 shows the settings for div456\_top which correspond to respective divide ratios.

| SB | SA | Divide ratio |
|----|----|--------------|
| 1  | 1  | 4            |
| 1  | 0  | 5            |
| 0  | 0  | 6            |

When both SA and SB are at logic “1”, the inverse output of third DFF (i.e.  $\_Q_2$ ) will remain at “0” and the output frequency of core divider is determined by the first 2 DFFs, which forms a divide-by-4 divider.

When SB is at logic “1” but SA is at logic “0”, the loop will be momentarily closed over the 3 DFFs. When  $Q_0=Q_1=0$ ,  $\_Q_1=\_Q_2=1$  and a “1” will be injected to the first DFF, causing a delay which is equivalent to a divide-by-5 operation. When both SA and SB are at logic “0”, the 3 DFFs will form a divide-by-6.

Differential-signal-pair concept is implemented throughout the entire architecture instead of the usual single-ended structure because the former provides immunity towards common-mode noise, supply voltage variation and fabrication process variation. Figure 4.25 shows the current mode logic (CML) latch which is used for constructing the master-slave DFFs in the divider. This topology is opted for the various advantages which it offers as compared to conventional CMOS static circuit.

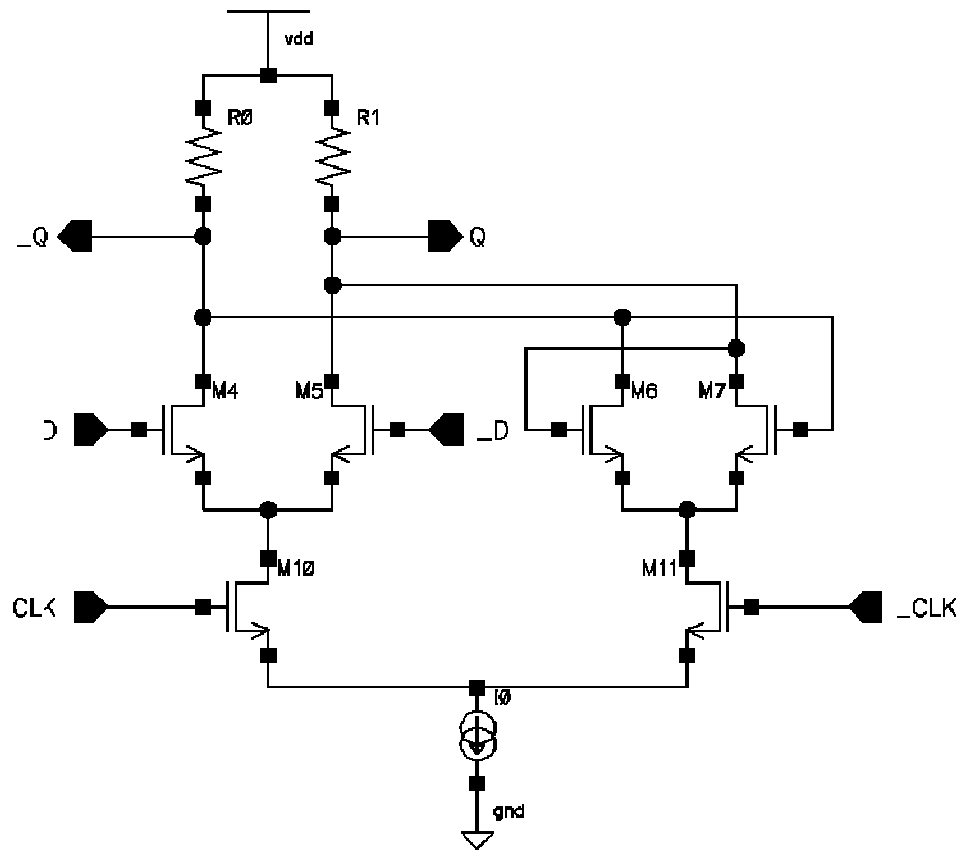


Figure 4.25 CML latch schematic



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The propagation delay (D), dynamic power dissipation (P), power delay (PD) and energy delay (ED) of CML structure is given by [42]

$$D_{CML} = NRC = \frac{N * C * \Delta V}{I} \quad (4.28)$$

$$P_{CML} = N * I * V_{dd} \quad (4.29)$$

$$PD_{CML} = NIV_{dd} * \frac{NC\Delta V}{I} = N^2 * C * \Delta V * V_{dd} \quad (4.30)$$

$$ED_{CML} = N^2 C (\Delta V) V_{dd} * \frac{NV(\Delta V)}{I} = \frac{N^3 C^2 (\Delta V)^2 V_{dd}}{I} \quad (4.31)$$

where N is the number of identical gate, C is the load capacitance, I is the biasing current and  $\Delta V (=I*R)$  is the output voltage swing. According to the equations, CML latches can be optimized by reducing the supply voltage, reducing signal voltage swing and/or increasing biasing current.

The constant current drawn by the source-coupled transistors in CML can suppress the common-mode noise which is caused by current spikes during switching. The differential-signal pair in CML also minimizes the injection of current into substrate and reduces switching noise significantly. Besides, the low input voltage swing requirement also improves the circuit's input sensitivity and enables the circuit to function at higher speed due to shorter toggle time.

The core divider has to function at the highest speed possible but the major bottleneck is the gates in the core divider loop. Figure 4.26 shows the implementation of CML with embedded OR-gate. This topology minimizes the delay and power consumption

caused by additional logic gates and enables the divider to function at higher frequency. An additional cascode transistor (i.e. M8) is added to ensure symmetrical transfer function of the OR-gate.

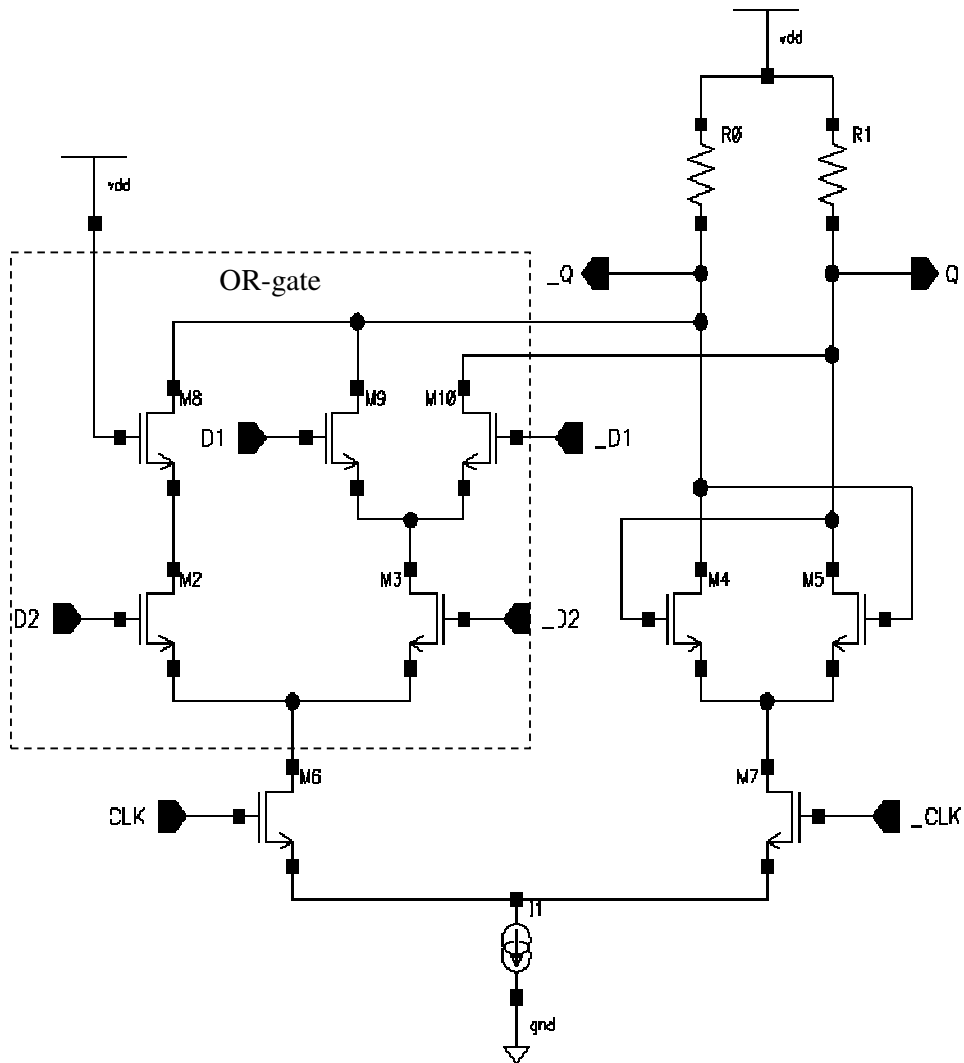


Figure 4.26 OR-embedded CML latch schematic

In order to prevent the logic gates from slowing down the divider, especially those in the core divider, the logic gates need to be able to function as fast as the DFFs. Figure 4.27 shows the schematic of dynamic OR-gate. A cascode transistor (i.e. M4) is added to ensure symmetrical function of the logic gate.



### 4.3 Frequency Synthesizer and Prescaler Layout

The layout view for fractional-N frequency synthesizer is illustrated in Figure 4.28.

The entire design occupied an area of approximately  $0.699\text{mm}^2$ .

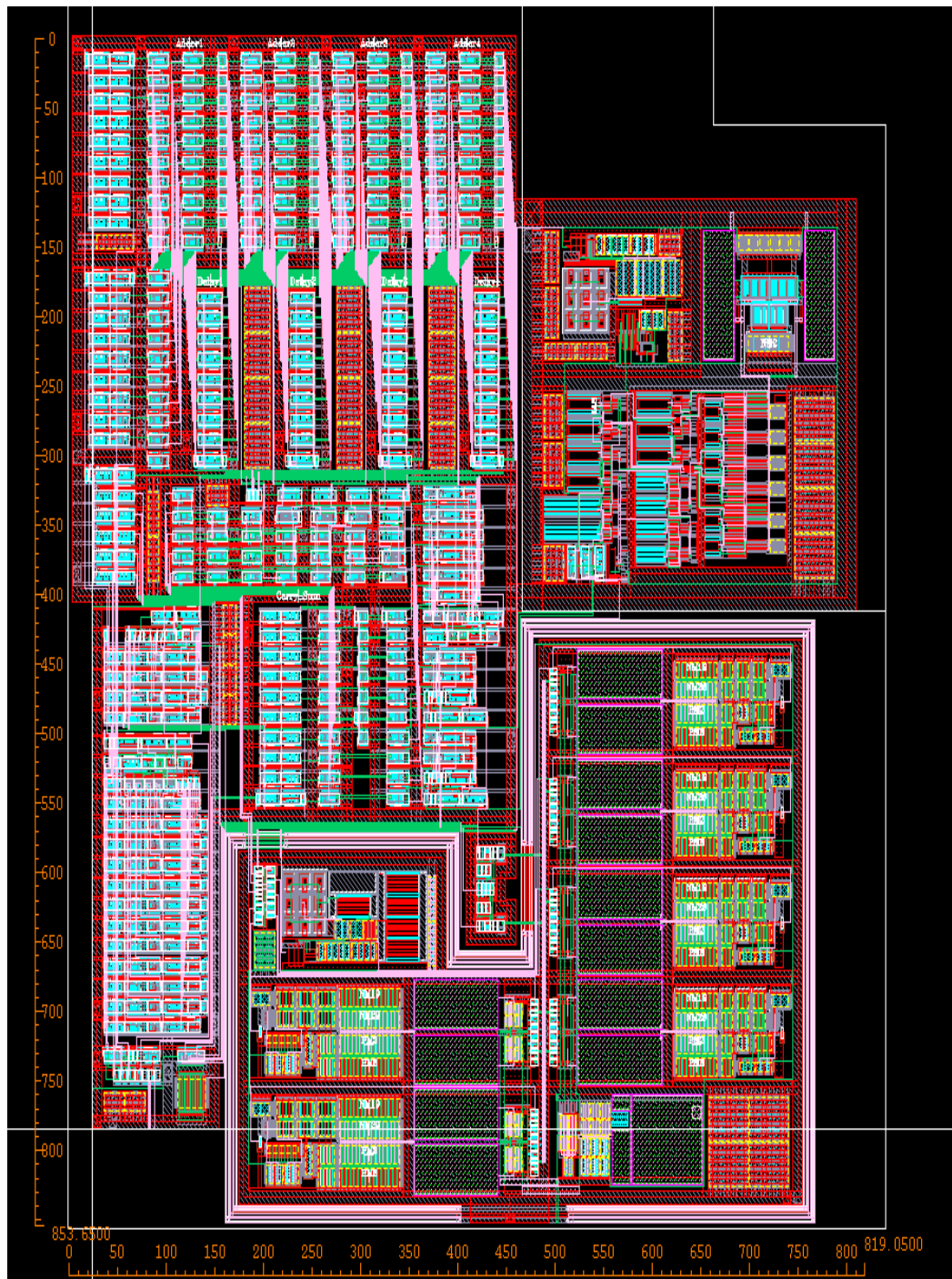


Figure 4.28 Layout view of fractional-N frequency synthesizer

Figure 4.29 shows the layout view for quad-modulus prescaler. The size of the prescaler is approximately  $0.102\text{mm}^2$ .

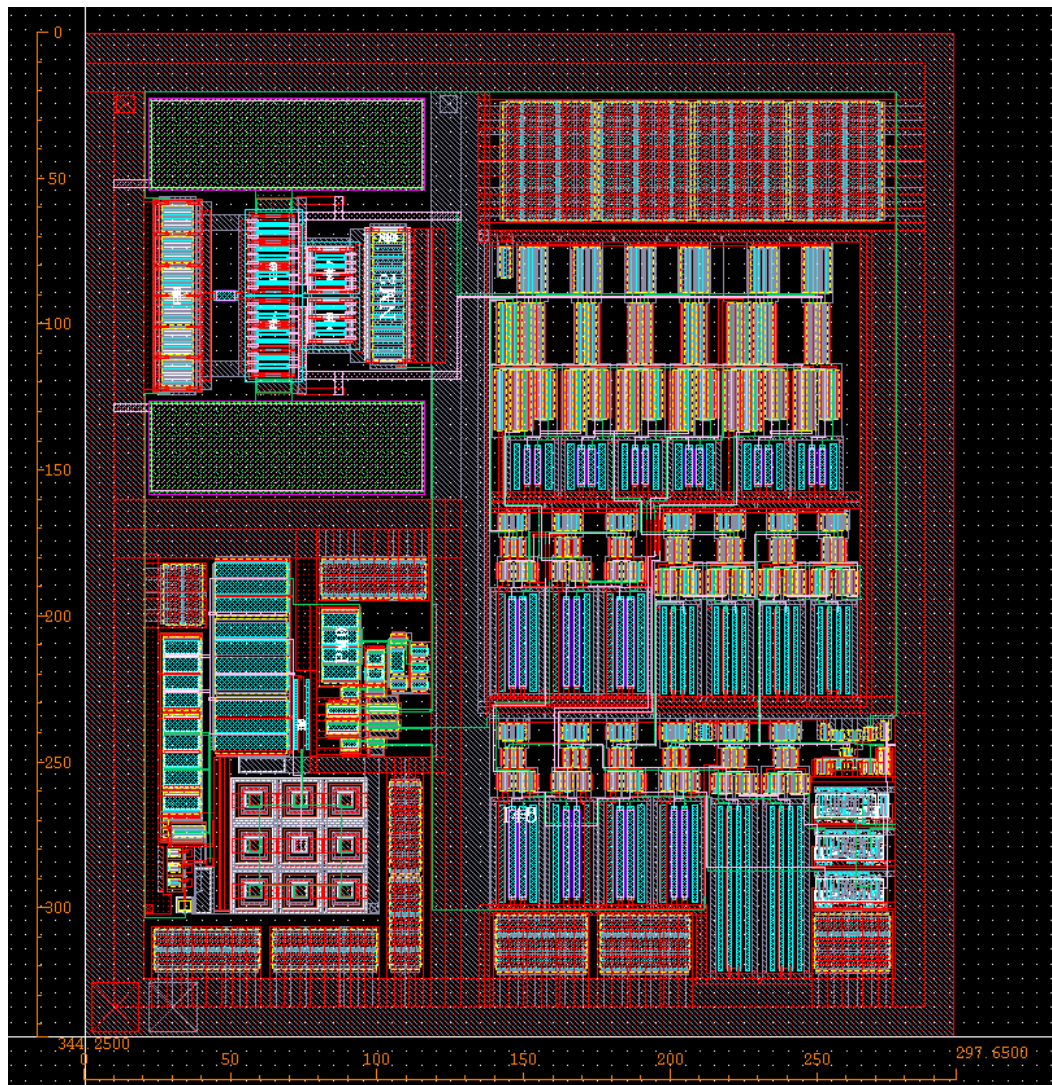


Figure 4.29 Layout view of quad-modulus prescaler

#### 4.4 Design Specifications

Table 4.10 shows the power supply specification for PLL. The minimum and maximum values for the supply current were obtained from the transient simulation results of 45 corners.

| Parameter      | Symbol   | Conditions                           | Value |     |     |
|----------------|----------|--------------------------------------|-------|-----|-----|
|                |          |                                      | Min   | Typ | Max |
| Supply voltage | Vdd (V)  |                                      | 3.0   | 3.3 | 3.6 |
| Supply current | Idd (mA) | Without Prescaler<br>and Charge Pump | 0.4   | 0.6 | 0.9 |

Table 4.11 shows the number of bits and range of the counters, timer and registers. The values are stored in binary code.

Table 4.11 Parameters of PLL counters, timer and registers

| Building block     | Bits | Value |      |
|--------------------|------|-------|------|
|                    |      | Min   | Max  |
| R-Counter          | 4    | 1     | 15   |
| Fast-lock Timer    | 12   | 0     | 4095 |
| N-Counter          | 9    | 64    | 511  |
| FN Register        | 9    | 0     | 511  |
| FD Register        | 9    | 1     | 511  |
| Interface Register | 2    | 0     | 3    |
| Mode Register      | 6    | 0     | 63   |

Table 4.12 shows the theoretical frequency range of the frequency synthesizer using ideal prescaler. Based on this design topology, the ideal synthesizer is capable of functioning from 1675MHz till 12724.95MHz when operating in the 2450MHz frequency band (with reference frequency of 25MHz and channel spacing of 50kHz), and functioning from 700MHz till 10179.95MHz when operating in the 910MHz frequency band (with reference frequency of 20MHz and channel spacing of 50kHz).

However, the actual attainable maximum frequency will be restricted by the performances of counters, VCO and prescaler.

| Band (MHz) | Reference (MHz) | Modulus P   | Channel spacing (kHz) | Min Frequency (MHz) | Max Frequency (MHz) |
|------------|-----------------|-------------|-----------------------|---------------------|---------------------|
| 2450       | 25              | 16/17/20/21 | 50                    | 1675.00             | 12724.95*           |
| 910        | 20              | 8/9/12/13   | 50                    | 700.00              | 10179.95*           |

\* The actual frequency range might be narrower, depending on the performances of counters, VCO and prescaler.

Table 4.13 shows the timing specifications of the frequency synthesizer settings, which includes the setup time, rise/fall time, hold time, and pulse width of PLL\_DATA, PLL\_CLK and PLL\_LE signals.

Table 4.13 Specifications for timing diagram of frequency synthesizer settings

|                             | Symbol    | Min (ns) | Typ (ns) | Max (ns) |
|-----------------------------|-----------|----------|----------|----------|
| PLL_DATA/PLL_CLK Setup Time | $t_{dcs}$ | 10       | -        | -        |
| PLL_DATA/PLL_CLK Hold Time  | $t_{dch}$ | 10       | -        | -        |
| PLL_CLK Rising Edge         | $t_{cr}$  | -        | -        | 100      |
| PLL_CLK Falling Edge        | $t_{cf}$  | -        | -        | 100      |
| PLL_CLK Width (High)        | $t_{cwh}$ | 10       | -        | -        |
| PLL_CLK Width (Low)         | $t_{cwl}$ | 10       | -        | -        |
| PLL_CLK/PLL_LE Setup Time   | $t_{cls}$ | 10       | -        | -        |
| PLL_LE Rising Edge          | $t_{lr}$  | -        | -        | 100      |
| PLL_LE Falling Edge         | $t_{lf}$  | -        | -        | 100      |
| PLL_LE Pulse Width          | $t_{lw}$  | 10       | -        | -        |

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## 4.5 PC Program for PLL Frequency Synthesizer Setting

A program was written for adjusting the PLL frequency synthesizer setting through parallel port of PC with the aid of Visual C++ 6.0 compiler.

### 4.5.1 User Interface

There are three available user interfaces. Figure 4.30 and Figure 4.31 show the first two interfaces: the former displays the bit-numbers and the latter displays the values of respective counters. The switching between two interfaces can be executed by depressing “1” or “1” key. The green-colour alphabets represent the letters to be depressed in order to invoke respective predefined functions or input menu of parameters.

```

                                Fractional-N PLL Initialization Version 1.1
                                Cyripts Pte Ltd, 10 January 2007
                                All rights reserved

----- Initial Parameters -----

Frequency= 2450.000 MHz, Clock= 25.0 MHz, Detector= 25.0 MHz
Prescaler= 16, ABC_Counter= 9 bit, R_Counter= 4 bit
FN_FD_Counter= 9 bit, Moduli= 0(0x0)
MASH_Order= 4, Counter_Out= 2,
Charge_Pump_Current= 200uA, Fastlock= 100us
Baudrate= 500.0000 kbps

-----
[ Key in A,C,D,e,F,g,I,k,l,M,N,o,P,R,u,+,-,
                                Test,Help,Quit or frequency directly]
_
```

Figure 4.30 Main user interface for synthesizer setting



```

                                Fractional-N PLL Initialization Version 1.1
                                Cyripts Pte Ltd, 10 January 2007
                                All rights reserved

----- Initial Parameters -----

Frequency= 2450.000 MHz, Clock= 25.0 MHz, Detector= 25.0 MHz
Prescaler= 16, ABC_Counter= 98(0x62), R_Counter= 1(0x1)
FN_Counter/FD_Counter= 0(0x0)/1(0x1), Moduli= 0(0x0)
MASH_Order= 4, Counter_Out= Fractional-N output
Charge_Pump_Current= 0(0x0), Fastlock= 2500(0x9C4)
Baudrate= 500.0000 kbps

-----
[ Key in A,C,D,e,F,g,I,k,l,M,N,o,P,R,u,+,-,
                                Test,Help,Quit or frequency directly]
-

```

Figure 4.31 Second user interface for synthesizer setting

Figure 4.32 shows the third user interface which contains the “Help” information. This page can be invoked by depressing “H” key and revoked by depressing any random key.

```

                                Fractional-N PLL Initialization Version 1.1
                                Cyripts Pte Ltd, 10 January 2007
                                All rights reserved

----- Usage -----

Windows      : Click the icon of Fractional_N_PLL.exe

Command line: Fractional_N_PLL
              Fractional_N_PLL read <ADDRESS>
              Fractional_N_PLL write <ADDRESS> <DATA>

IEEE 1284-A : Pin2 -> Data, Pin3 -> CLK, Pin4 -> LE

-----
-

```

Figure 4.32 Third user interface displaying “Help” information

---

## 4.5.2 Hardware Interface

The parallel port found on PC may provide +3.3V or +5.0V interface voltage for PLL frequency synthesizer setting but the chip-under-test might require a lower interface voltage. A high-to-low level shifter from Philips Semiconductors (74HC4050) is used to bridge the chip and parallel port. Power supply voltage of the chip is used as a reference level by the level shifter to convert the parallel port voltage accordingly for smooth interfacing. Figure 4.33 shows the assigned parallel port pins which will output PLL\_DATA, PLL\_CLK and PLL\_LE signals respectively.

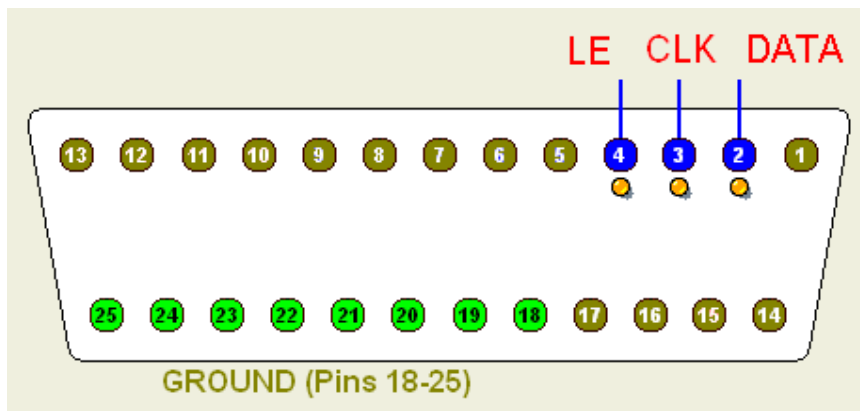


Figure 4.33 PLL setting through parallel port



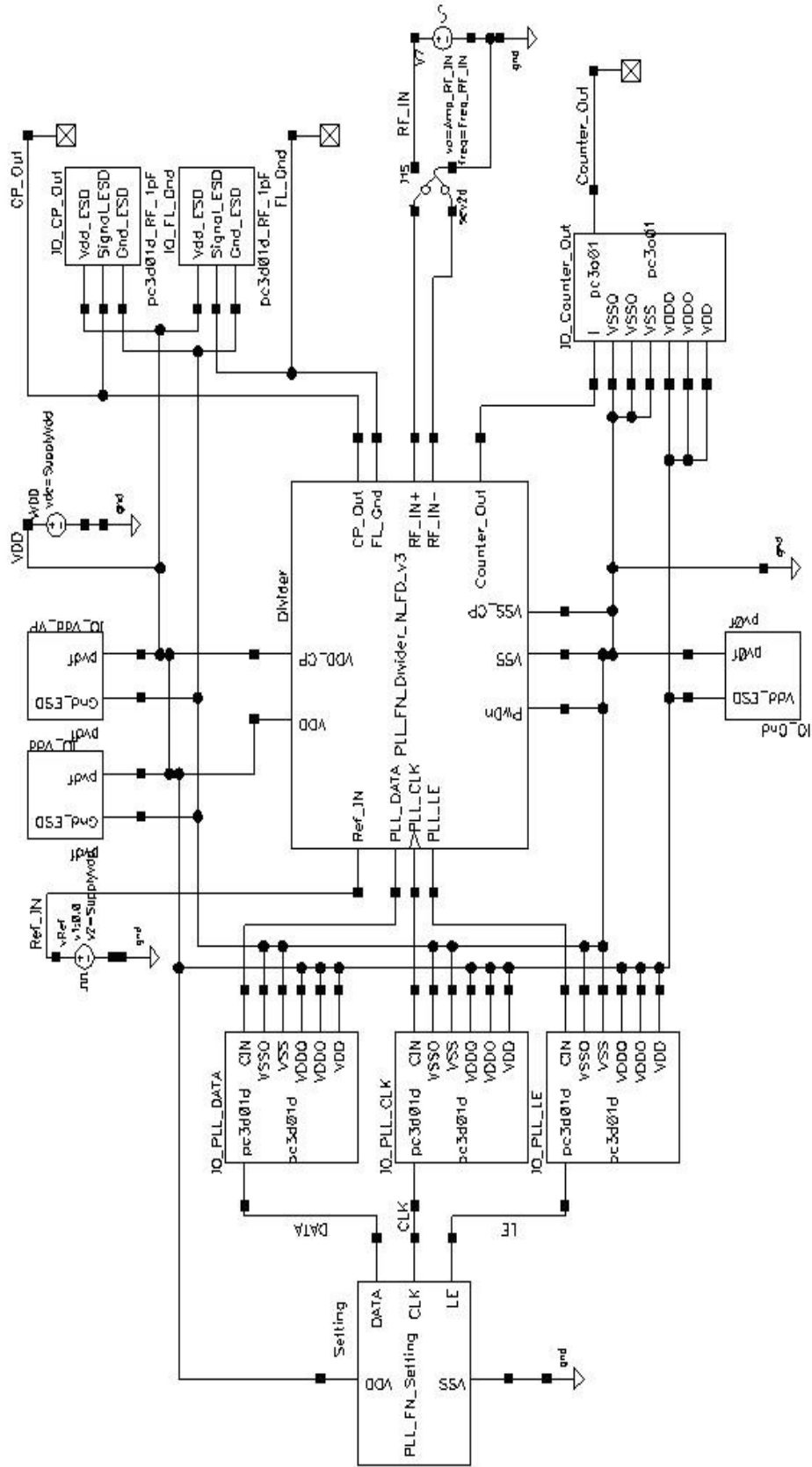


Figure 5.2 Top level simulation testbench





Transient Response

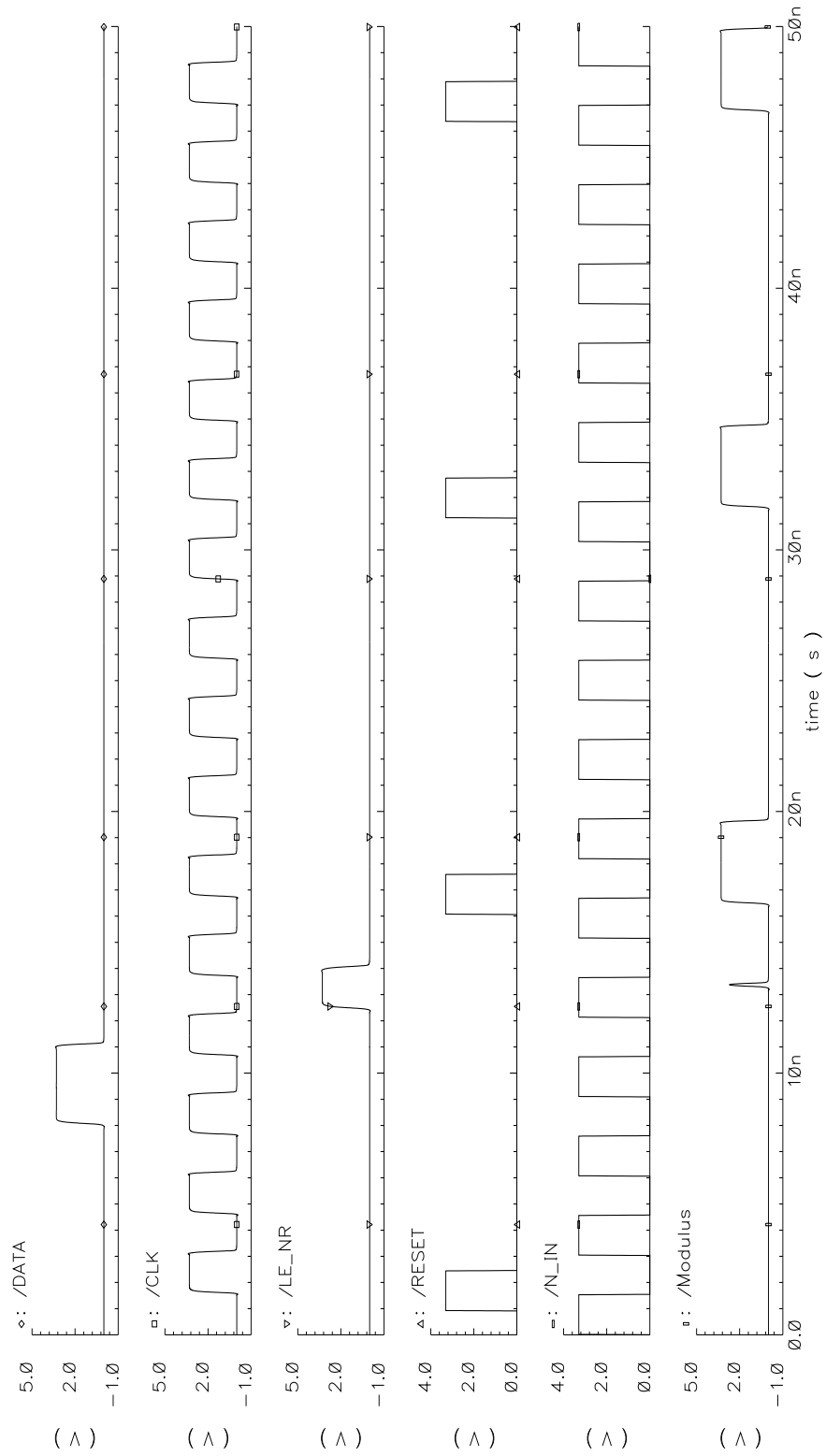


Figure 5.4 Transient simulation results of AB\_Counter





Transient Response

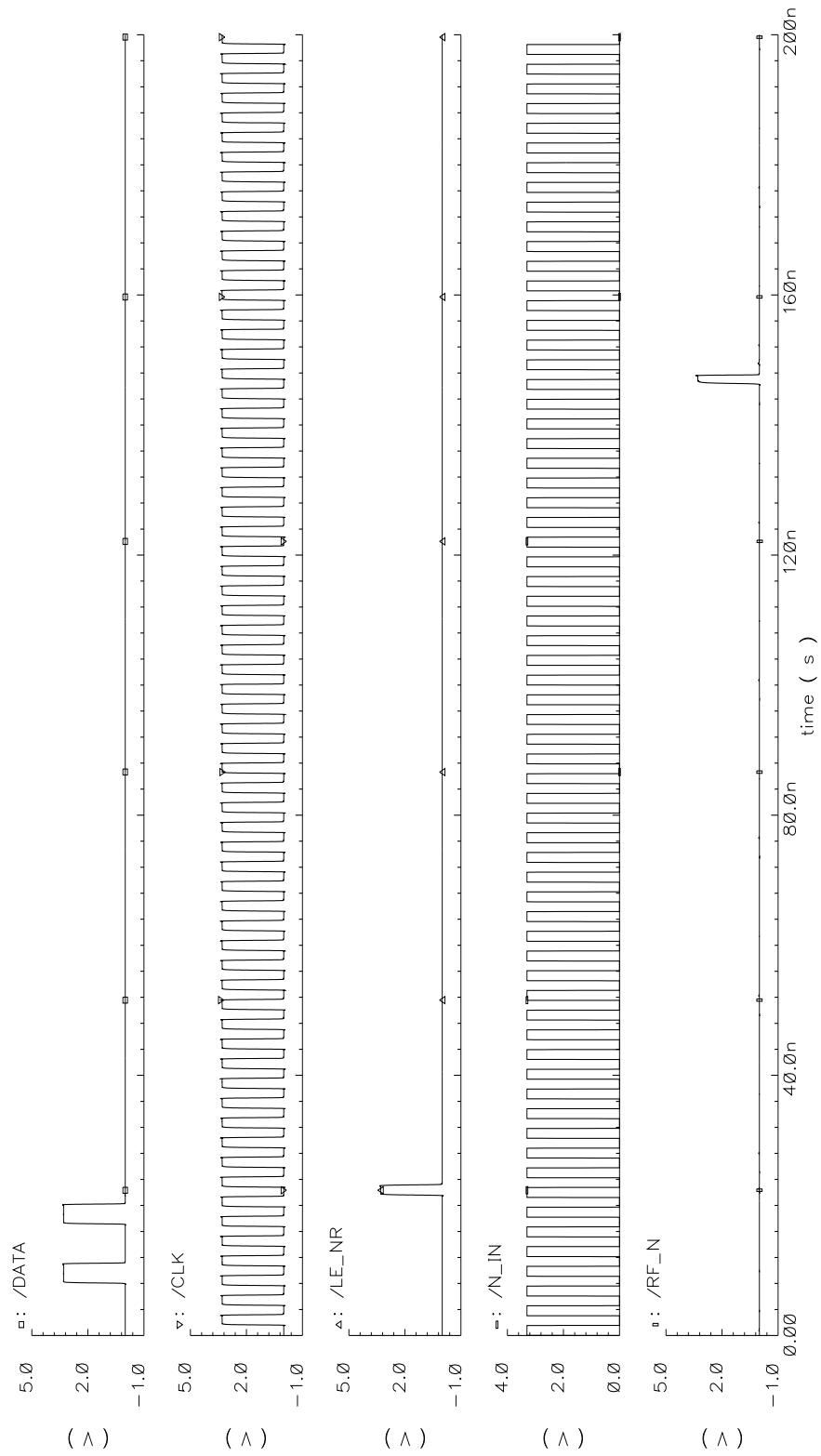


Figure 5.6 Transient simulation results of C\_Counter



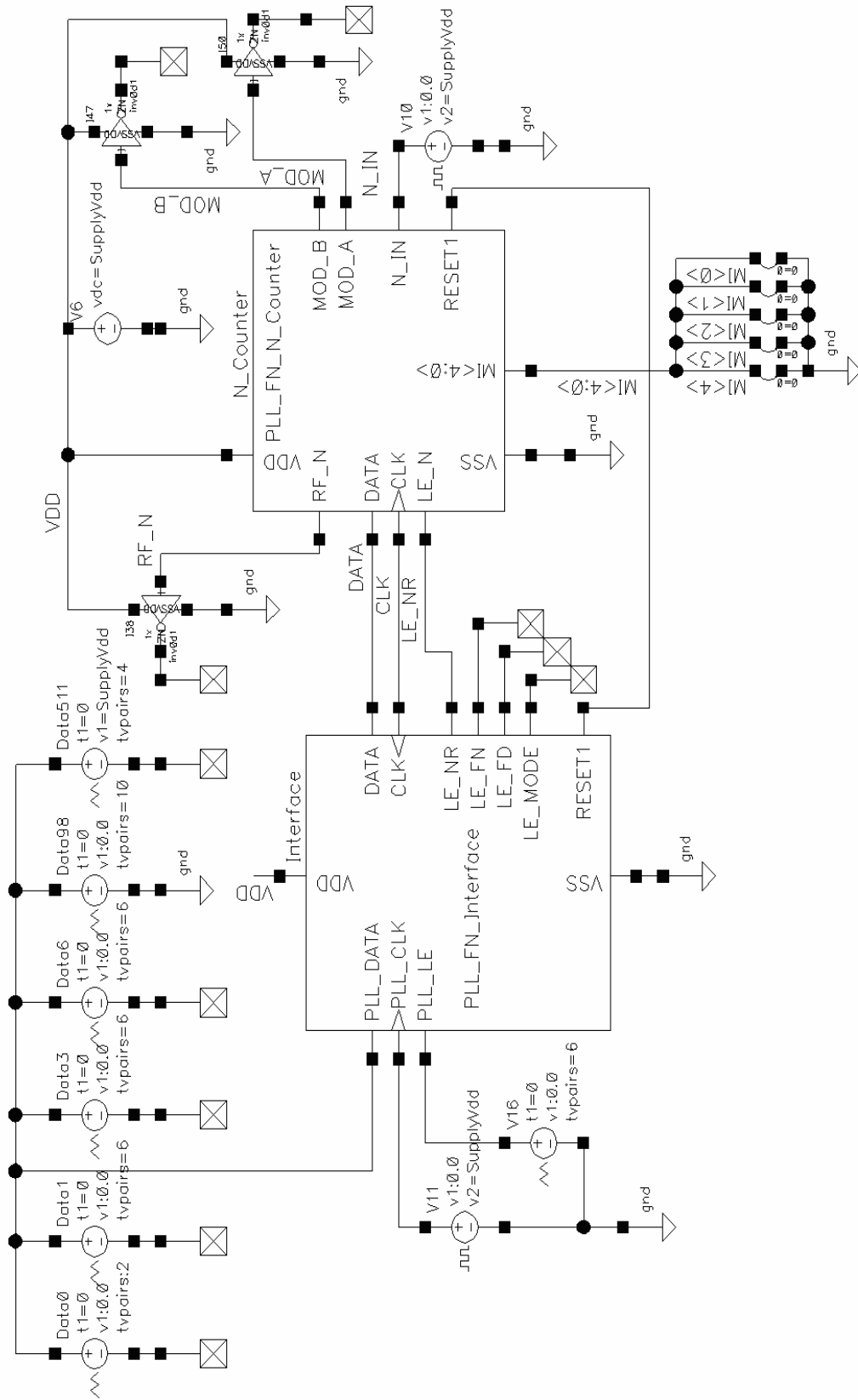


Figure 5.7 Testbench for N\_Counter functionality test



Transient Response

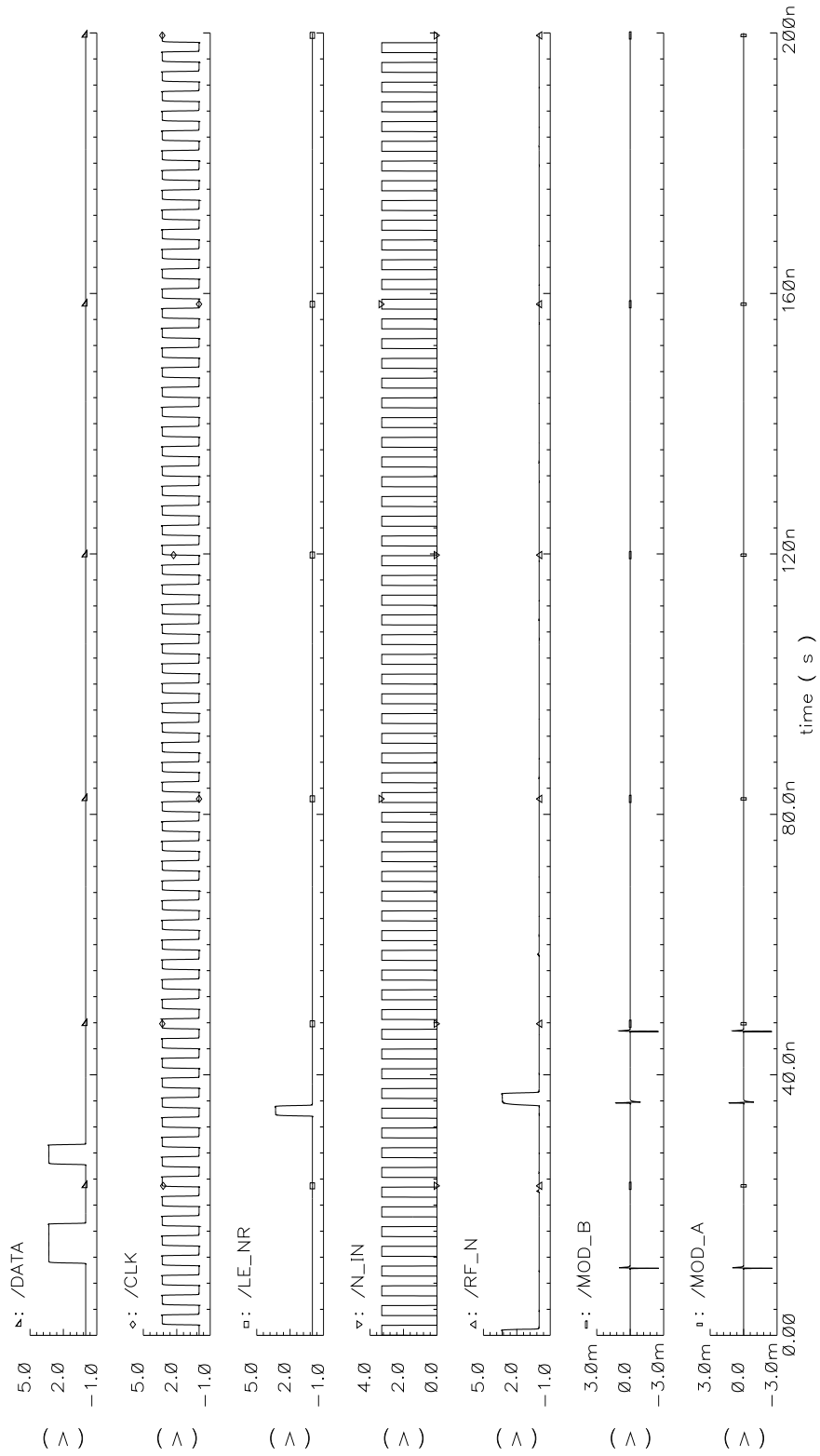


Figure 5.8 Transient simulation results of N\_Counter





Transient Response

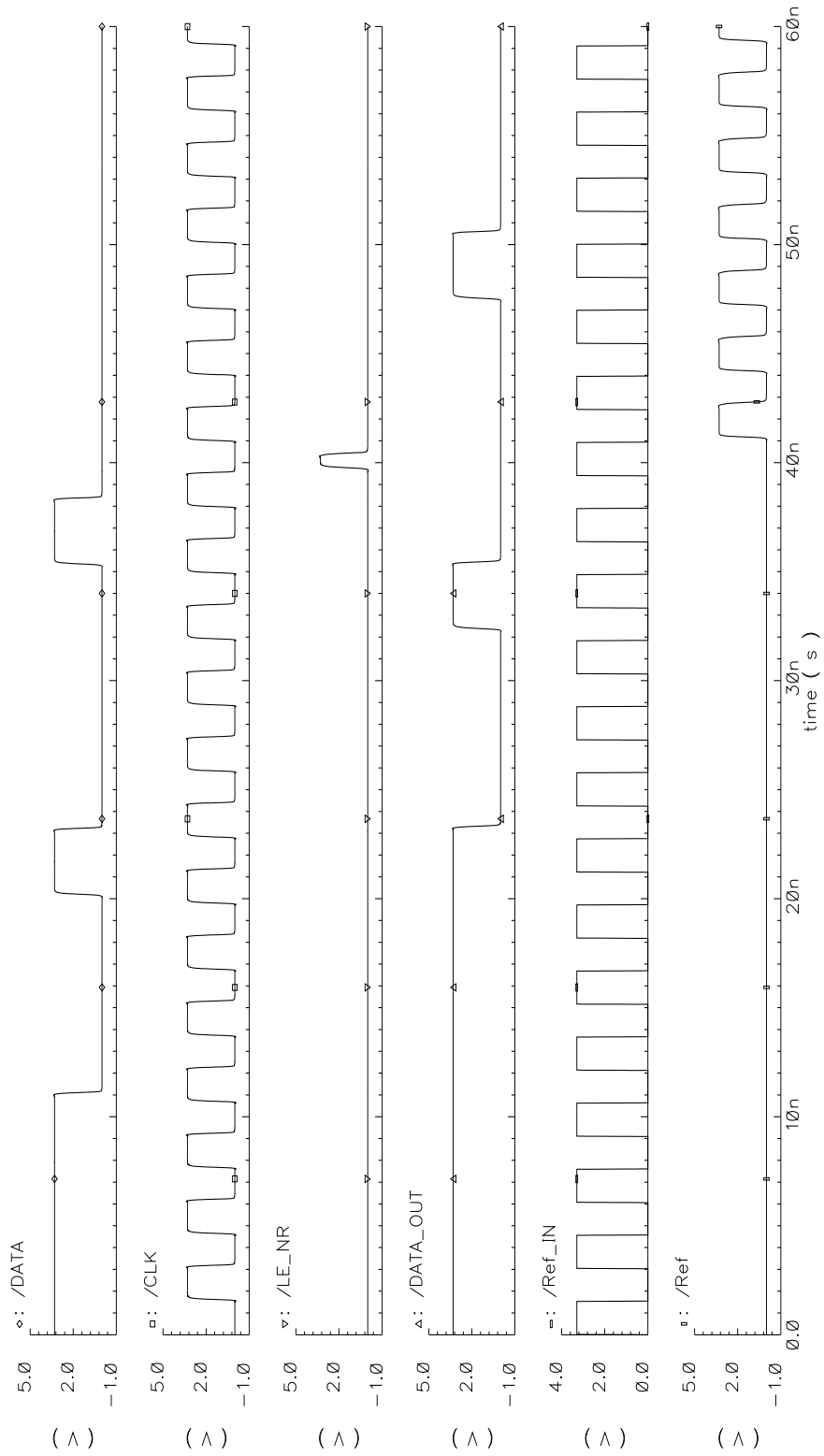


Figure 5.10 Transient simulation results of R\_Counter



try PLL\_FN\_MASH\_4order\_test schematic : Oct 31 08:32:18 2008

Expressions

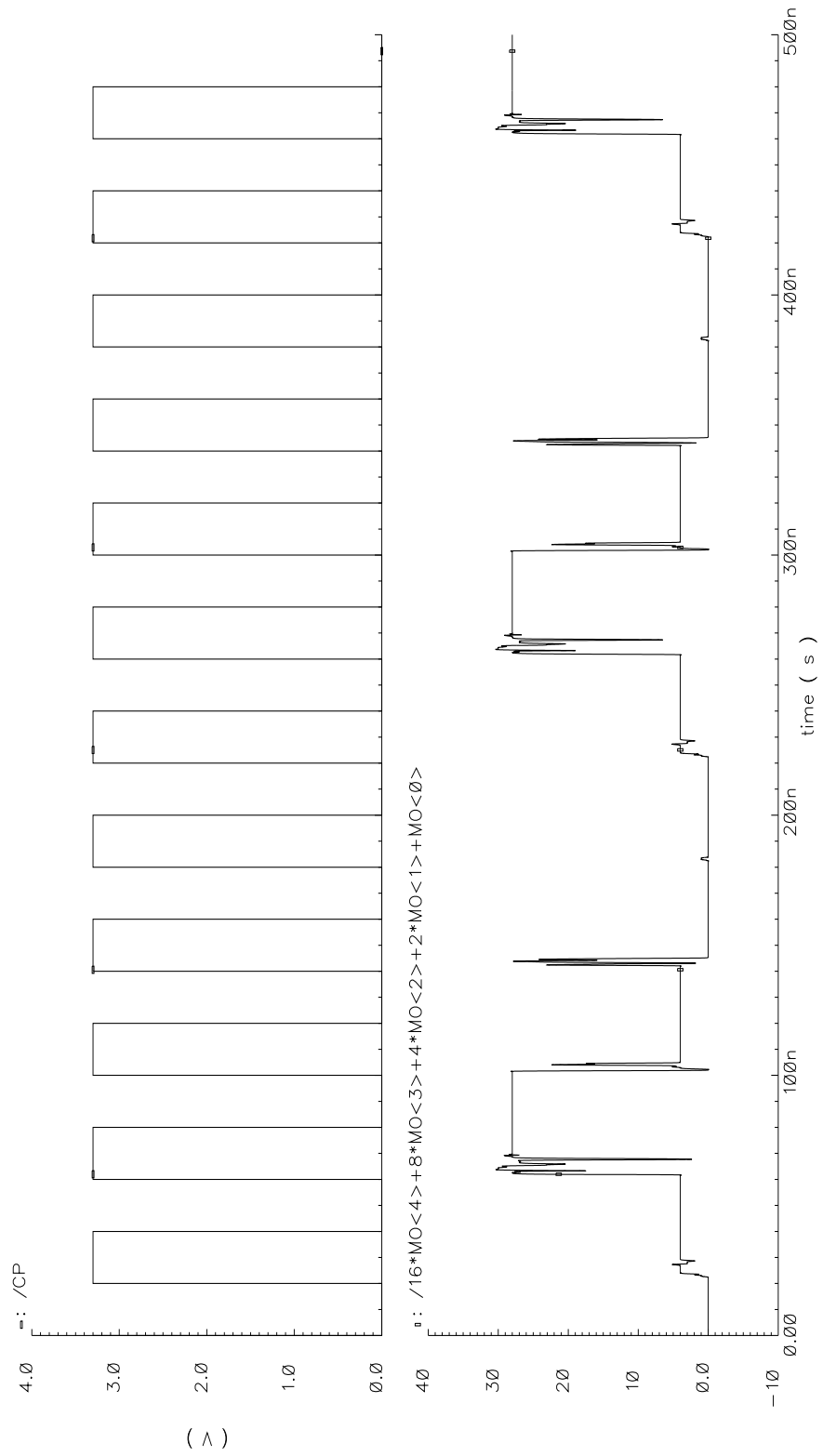


Figure 5.12 Transient simulation result of MASH\_4order

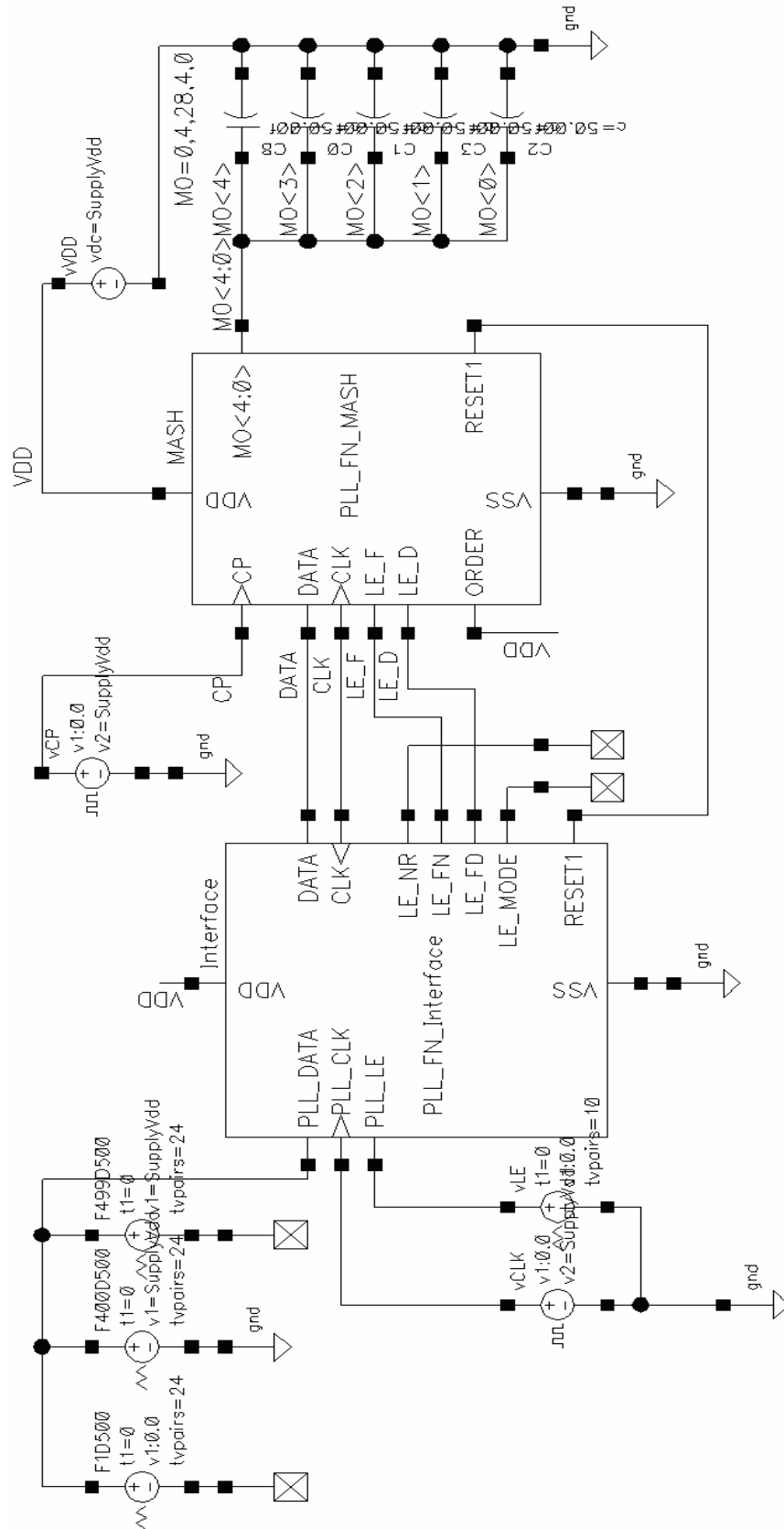


Figure 5.13 Testbench for MASH top cell functionality test

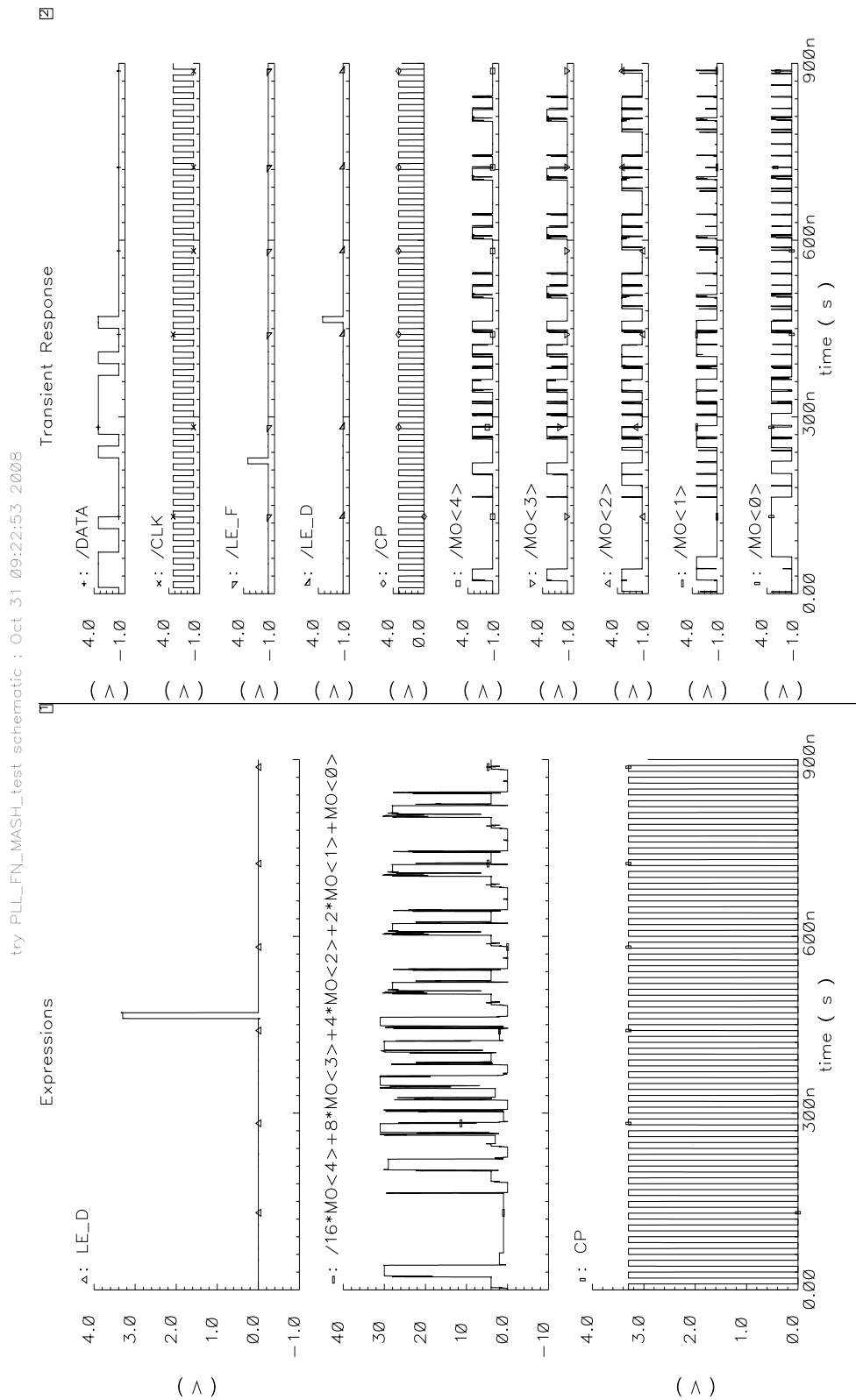


Figure 5.14 Transient response of MASH top cell



### 5.1.3 Interface

Figure 5.15 shows the testbench for Interface functionality test and the results are shown in Figure 5.16.

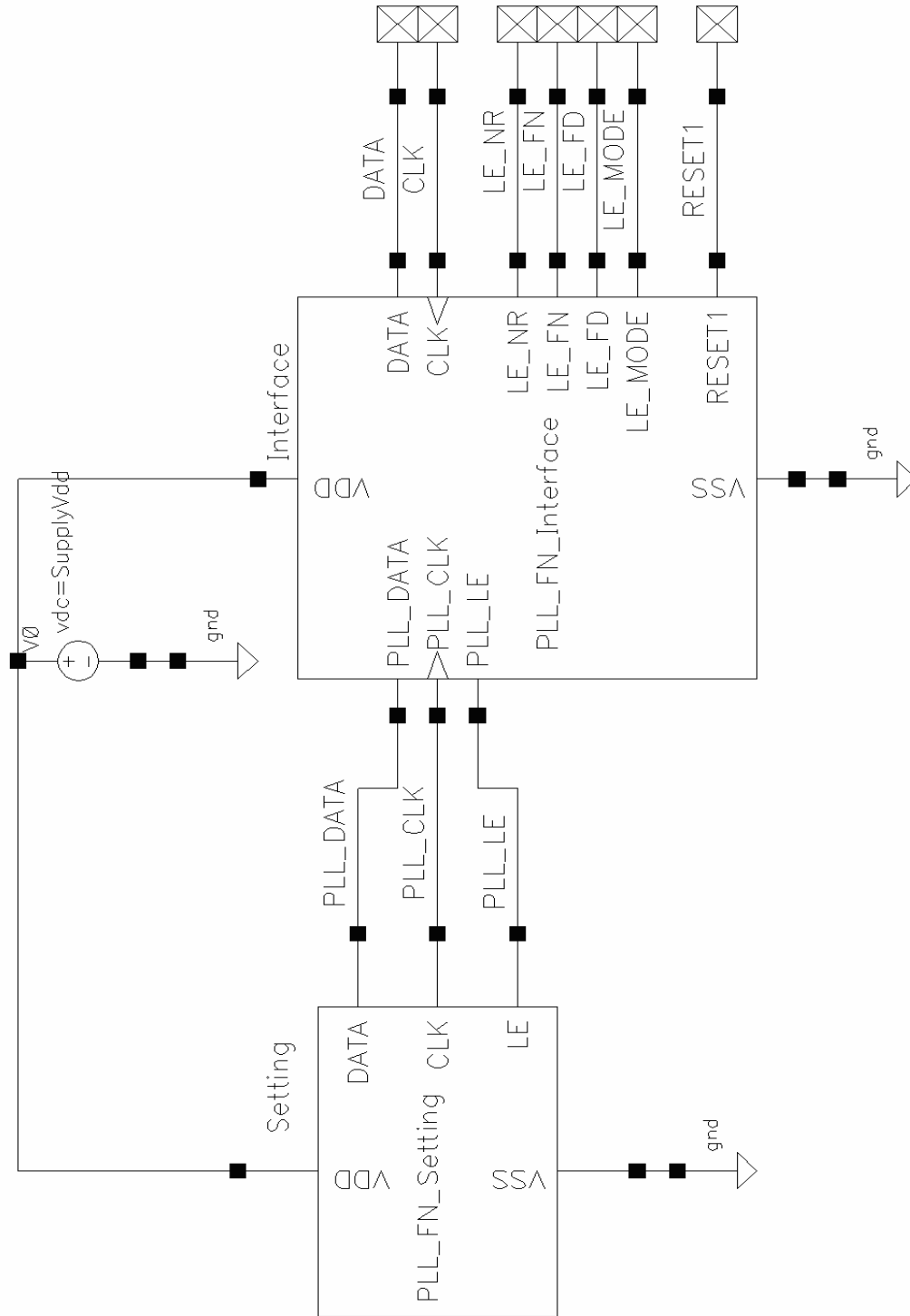


Figure 5.15 Testbench for Interface functionality test



Transient Response

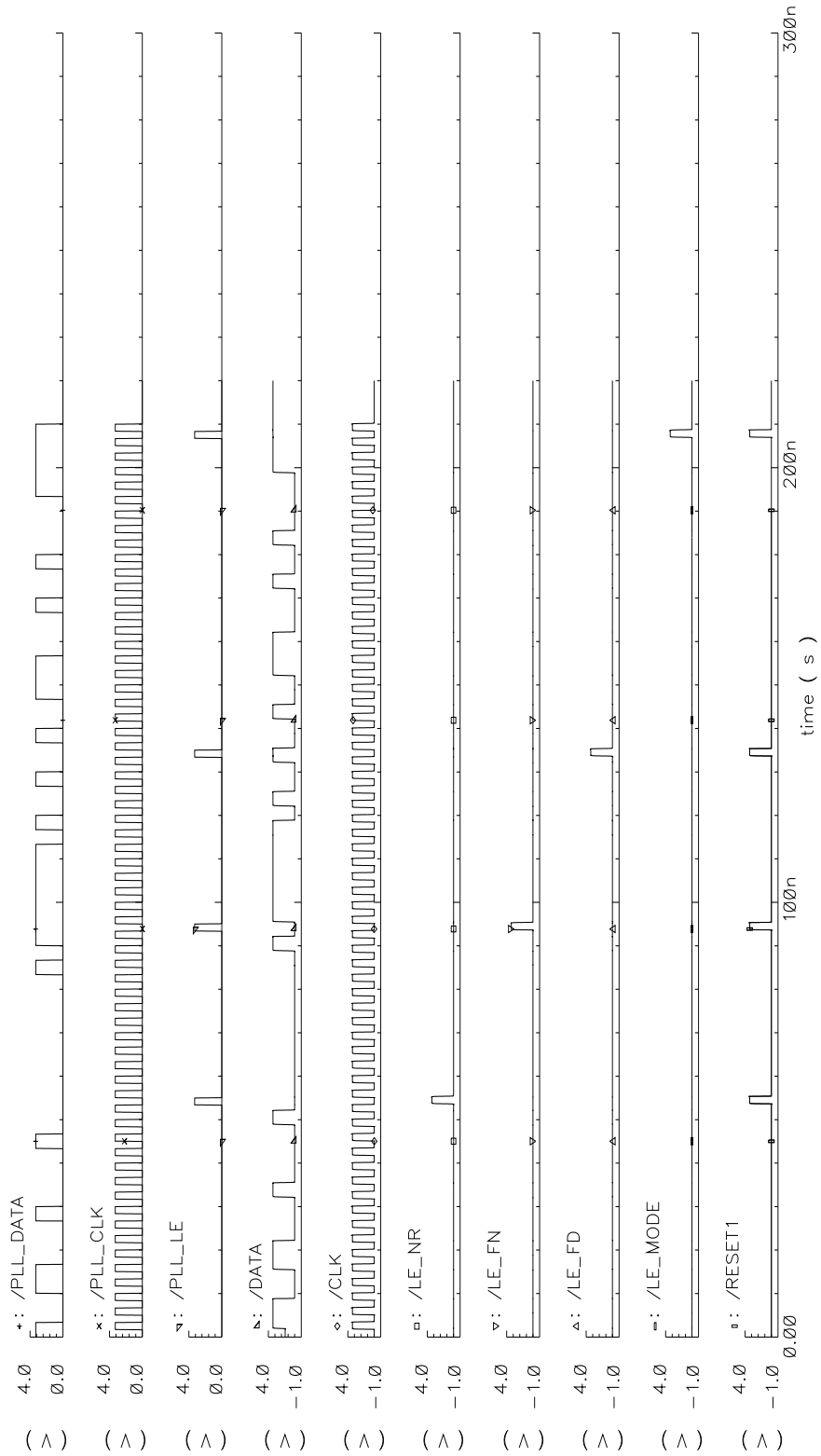


Figure 5.16 Transient simulation results of Interface

### 5.1.4 Mode Register

Figure 5.17 shows the simulation setups for testing the functionality of Mode Register and Figure 5.18 shows its transient simulation results.

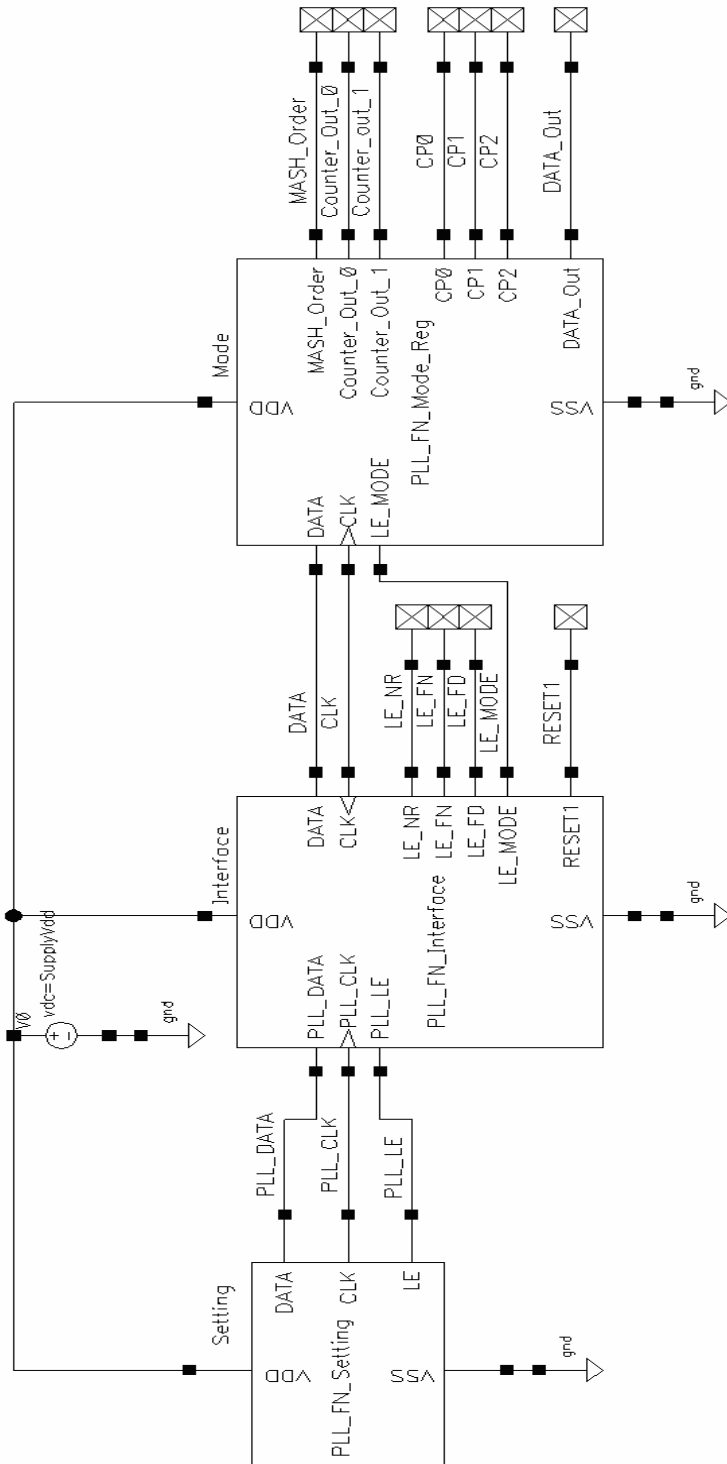


Figure 5.17 Testbench for Mode Register functionality test



Transient Response

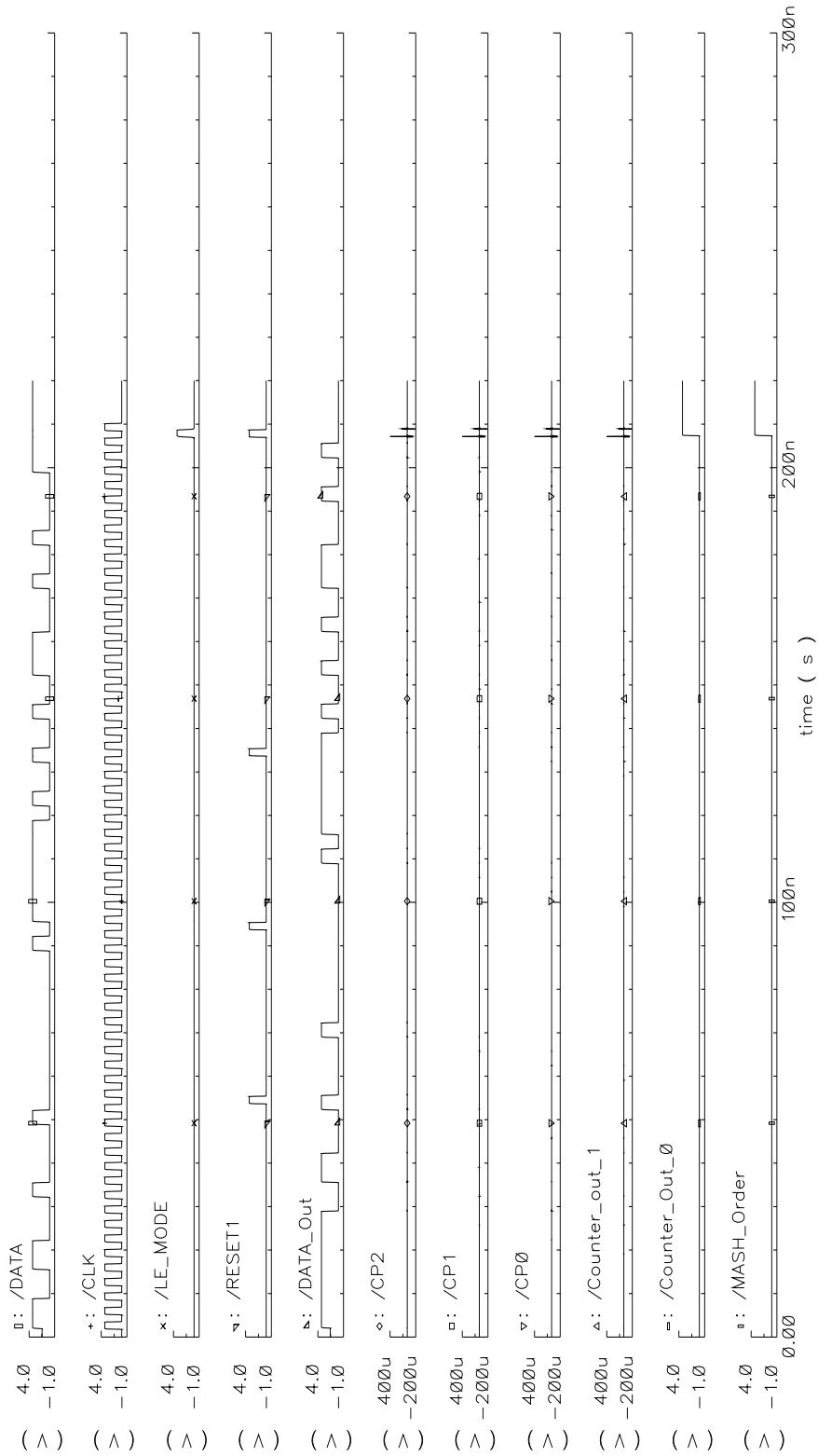


Figure 5.18 Transient response of Mode\_Reg

### 5.1.5 Fastlock

Figure 5.19 demonstrates the testbench for Fastlock functionality test and the simulation results is as shown in Figure 5.20.

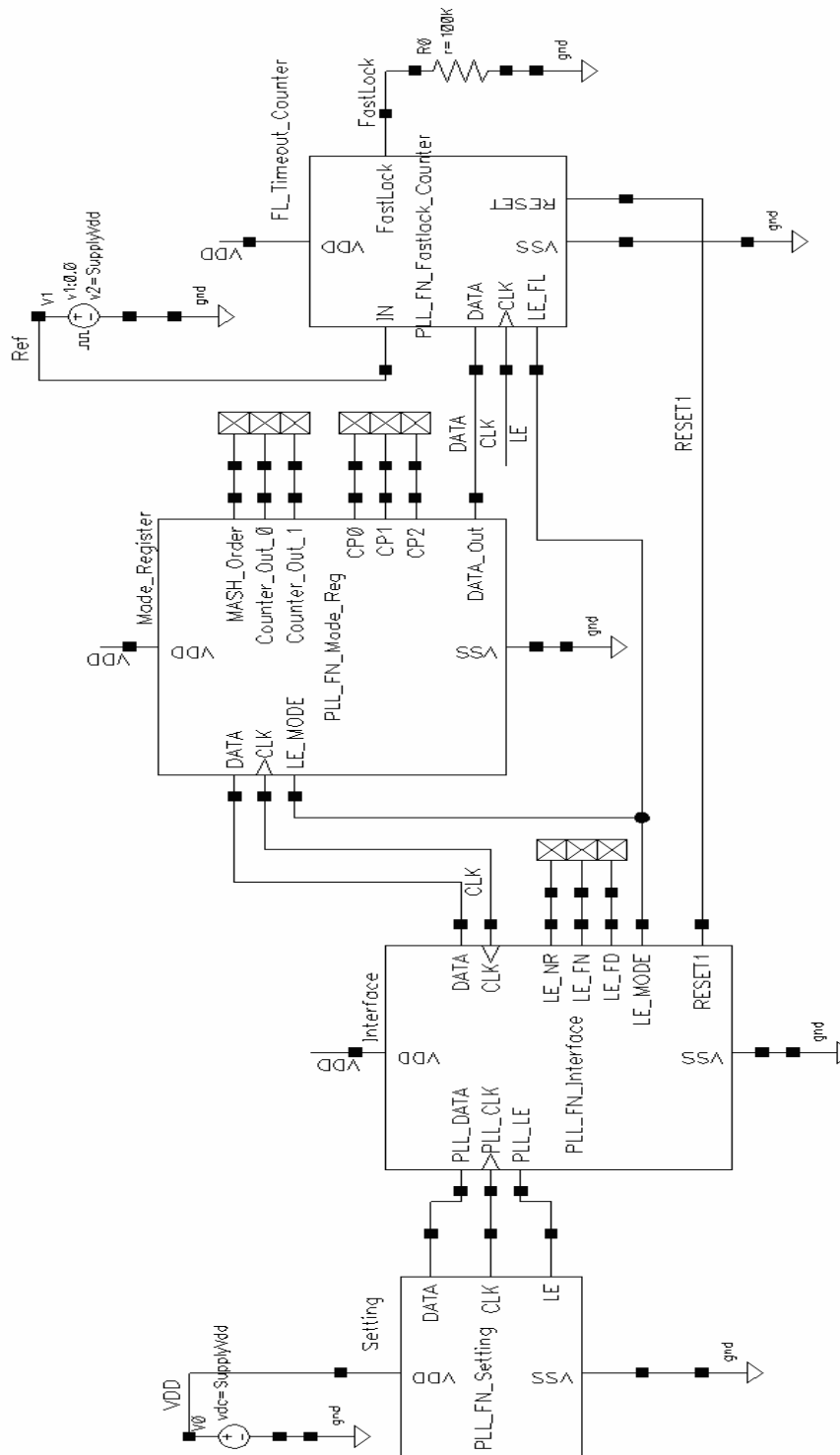


Figure 5.19 Testbench for Fastlock Counter functionality test



Transient Response

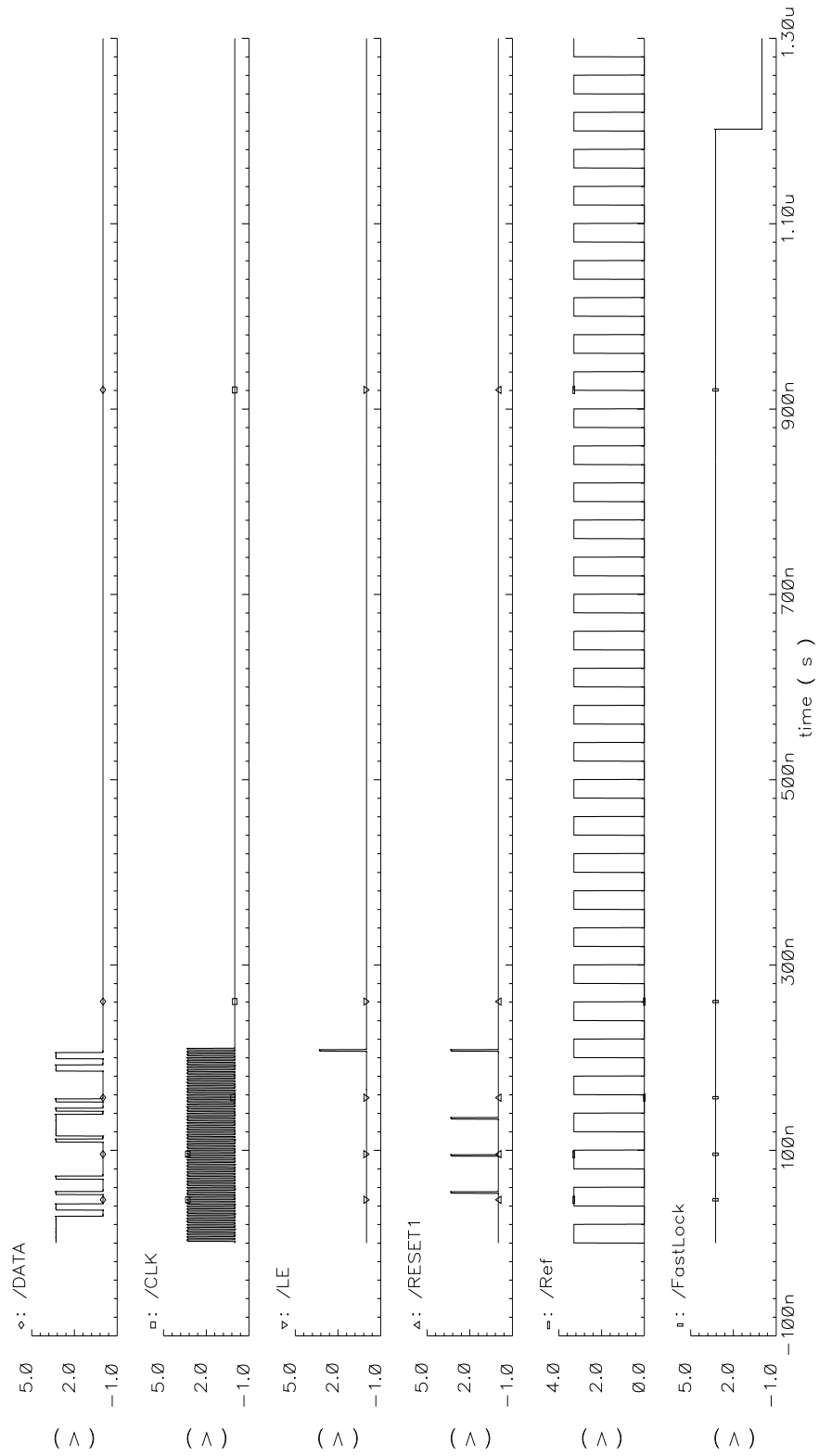


Figure 5.20 Transient response of Fastlock\_Counter

## 5.1.6 Prescaler

Figure 5.21 shows the testbench for quad-modulus prescaler using the Prescaler\_Mode\_Controller (with delay).

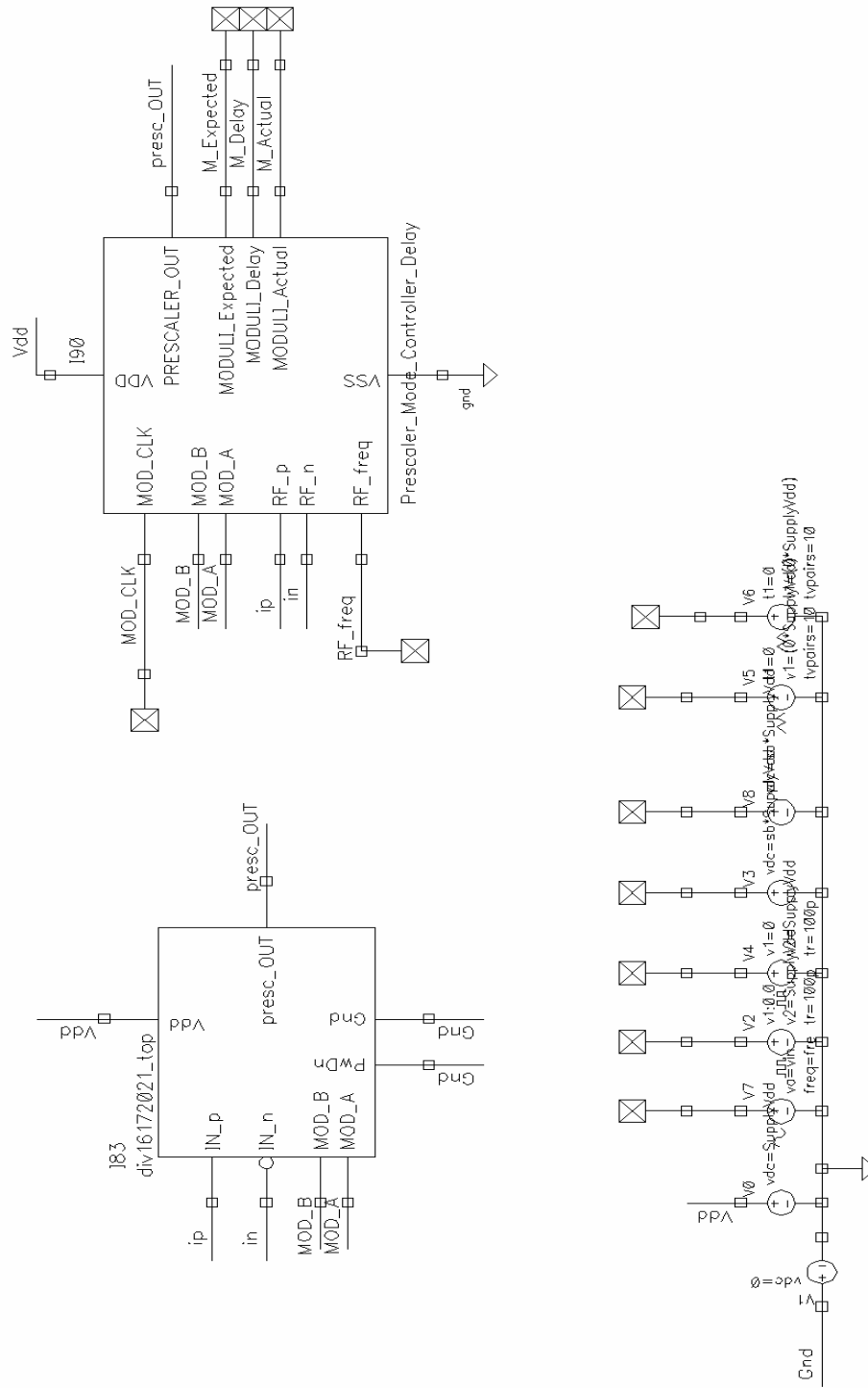


Figure 5.21 Testbench for div16172021\_top functionality test

---

## 5.2 Simulation Results

Simulations for the proposed frequency synthesizer design were carried out in Cadence IC5.1.41 under Red Hat Enterprise Linux WS release 4 (Nahant Update 4).

### 5.2.1 Prescaler

Prescaler has a minimum input signal voltage amplitude requirement for the circuit to function properly. The performance of prescaler with various differential input signal amplitudes was simulated. Figure 5.22 shows the simulation results at Typical condition (TT, 3.3V, 25<sup>0</sup>C). It was observed that the input sensitivity of the proposed prescaler design was very high with minimum differential input signal amplitude required of 350mV.

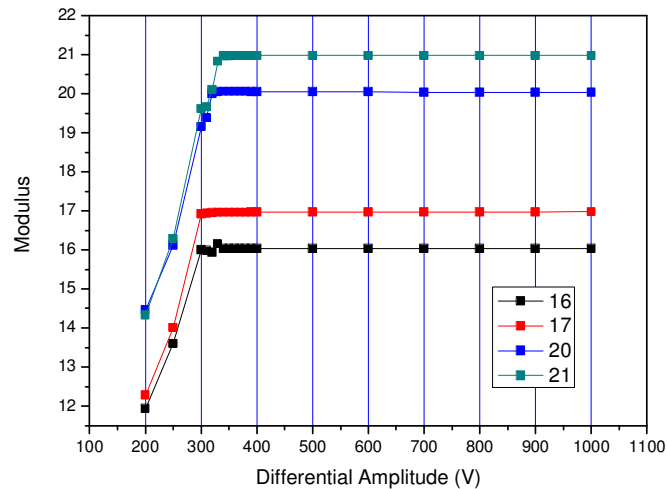


Figure 5.22 Minimum input signal amplitude requirement for prescaler

The operating ranges of prescaler, simulated at 100MHz-step increments, were obtained with the help of Verilog-A view of PLL\_FN\_Prescaler\_mode\_controller. At Typical condition (TT, 3.3V, 25<sup>0</sup>C), the prescaler was able to function up till 3.87GHz with ac current consumption of 21.09mA and functioned up till 3.05GHz with ac



current consumption of 18.09mA. Table 5.1 shows the process corners simulation results of the prescaler with supply current of 18.09mA (at Typical condition).

| Table 5.1 Operating ranges of prescaler in 45 cases |         |            |                                       |             |
|---|---------|------------|---------------------------------------|-------------|
| Process corner                                      | Vdd (V) | Temp. (°C) | Maximum operating frequency (GHz)     |             |
|   |         |            | Schematic (30fF parasitic capacitors) | Extracted_C |
| FF  | 3.0     | 25         | 3.00                                  | 3.00        |
| FF  | 3.0     | -40        | 3.00                                  | 3.00        |
| FF  | 3.0     | 90         | 3.00                                  | 2.95        |
| FF  | 3.3     | 25         | 3.00                                  | 3.00        |
| FF  | 3.3     | -40        | 3.00                                  | 3.00        |
| FF  | 3.3     | 90         | 3.00                                  | 2.95        |
| FF  | 3.6     | 25         | 3.00                                  | 3.00        |
| FF  | 3.6     | -40        | 3.00                                  | 3.00        |
| FF  | 3.6     | 90         | 3.00                                  | 3.00        |
| FS  | 3.0     | 25         | 3.00                                  | 3.00        |
| FS  | 3.0     | -40        | 3.00                                  | 3.00        |
| FS  | 3.0     | 90         | 2.95                                  | 2.95        |
| FS  | 3.3     | 25         | 3.00                                  | 3.00        |
| FS  | 3.3     | -40        | 3.00                                  | 3.00        |
| FS  | 3.3     | 90         | 2.95                                  | 2.95        |
| FS  | 3.6     | 25         | 3.00                                  | 3.00        |
| FS  | 3.6     | -40        | 3.00                                  | 3.00        |
| FS  | 3.6     | 90         | 3.00                                  | 3.00        |

| Process corner | Vdd (V) | Temp. (°C) | Maximum operating frequency (GHz)        |             |
|----------------|---------|------------|--|-------------|
|                |         |            | Schematic<br>(30fF parasitic capacitors) | Extracted_C |
| SF             | 3.0     | 25         | 3.00                                     | 2.90        |
| SF             | 3.0     | -40        | 3.00                                     | 3.00        |
| SF             | 3.0     | 90         | 2.85                                     | 2.75        |
| SF             | 3.3     | 25         | 3.00                                     | 2.95        |
| SF             | 3.3     | -40        | 3.00                                     | 3.00        |
| SF             | 3.3     | 90         | 2.80                                     | 2.75        |
| SF             | 3.6     | 25         | 3.00                                     | 2.95        |
| SF             | 3.6     | -40        | 3.00                                     | 3.00        |
| SF             | 3.6     | 90         | 2.80                                     | 2.80        |
| SS             | 3.0     | 25         | 3.00                                     | 2.90        |
| SS             | 3.0     | -40        | 3.00                                     | 3.00        |
| SS             | 3.0     | 90         | 2.90                                     | 2.80        |
| SS             | 3.3     | 25         | 3.00                                     | 2.95        |
| SS             | 3.3     | -40        | 3.00                                     | 3.00        |
| SS             | 3.3     | 90         | 2.80                                     | 2.75        |
| SS             | 3.6     | 25         | 3.00                                     | 2.95        |
| SS             | 3.6     | -40        | 3.00                                     | 3.00        |
| SS             | 3.6     | 90         | 2.80                                     | 2.80        |
| TT             | 3.0     | 25         | 3.00                                     | 3.00        |
| TT             | 3.0     | -40        | 3.00                                     | 3.00        |
| TT             | 3.0     | 90         | 2.85                                     | 2.85        |

| Process corner | Vdd (V) | Temp. (°C) | Maximum operating frequency (GHz)        |             |
|----------------|---------|------------|--|-------------|
|                |         |            | Schematic<br>(30fF parasitic capacitors) | Extracted_C |
| TT             | 3.3     | 25         | 3.05                                     | 3.05        |
| TT             | 3.3     | -40        | 3.00                                     | 3.00        |
| TT             | 3.3     | 90         | 2.90                                     | 2.90        |
| TT             | 3.6     | 25         | 3.00                                     | 3.00        |
| TT             | 3.6     | -40        | 3.00                                     | 3.00        |
| TT             | 3.6     | 90         | 2.90                                     | 2.90        |

### 5.2.2 Frequency Synthesizer Current Consumption

Table 5.2 Current consumptions of synthesizer building blocks at Typical conditions (TT, 3.3V, 25°C, 2450.05MHz)

| Building block | Current        |
|----------------|----------------|
| MASH           | 1.66 mA        |
| N-Counter      | 1.22 mA        |
| R-Counter      | 15.64 $\mu$ A  |
| FL Counter     | 88.01 $\mu$ A  |
| Counter_Out    | 153.28 $\mu$ A |
| Interface      | 0.58 nA        |
| PFD            | 115.32 $\mu$ A |
| Prescaler      | 18.09 mA       |
| Total          | 21.34 mA       |

In order to investigate the performance of the fractional-N frequency synthesizer, simulations were being carried out in all 45 cases which consisted of combinations

from five process corners (Typical (TT); Slow-Slow (SS); Fast-Fast (FF); Slow-Fast (SF); Fast-Slow (FS)), three supply voltages (3.0V; 3.3V; 3.6V) and three temperatures (-40°C; 25°C, 90°C). The average ac current consumptions of the digital circuits are measured over the period from 1μs to 3μs, and tabulated in Table 5.2. Figure 5.23 shows the current consumption of MASH and Table 5.3 lists summary of the average current consumptions for synthesizer building blocks in all 45 cases.

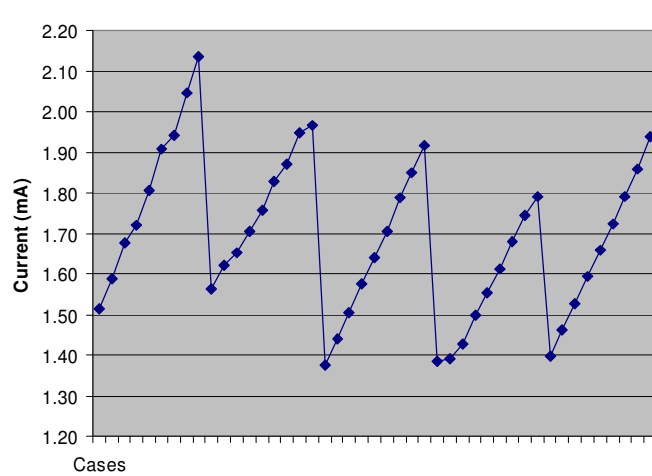


Figure 5.23 Current consumption of MASH in 45 cases

Table 5.3 Average current consumptions of synthesizer building blocks in 45 cases

| Building block | Current |         |           |
|----------------|---------|---------|-----------|
|                | Maximum | Average | Minimum   |
| MASH           | 2.14    | 1.69    | 1.38 mA   |
| N-Counter      | 1.56    | 1.23    | 0.97 mA   |
| R-Counter      | 21.50   | 15.86   | 11.61 μA  |
| FL Counter     | 117.78  | 89.65   | 69.15 μA  |
| Counter_Out    | 228.06  | 155.71  | 101.39 μA |
| Interface      | 50.38   | 5.94    | 0.26 nA   |
| PFD            | 143.26  | 115.96  | 93.95 μA  |
| Total          | 4.21    | 3.30    | 2.62 mA   |

### 5.2.3 PLL Settings

With a crystal oscillator of 25MHz, the typical values for counters, registers and timer are as shown in Table 5.4.

Table 5.4 Typical values of counters, registers and timer (crystal oscillator frequency= 25MHz)

| Building block      | Value | Note  |
|---------------------|-------|---|
| R-Counter           | 1     | Reference frequency= 25MHz                                  |
| N-Counter           | 98    | LO frequency= 2450.05MHz                                    |
| FN Register         | 1     |   |
| FD Register         | 500   |   |
| MASH order          | 1     | MASH order=4  |
| Counter_Out         | 1     | Prescaler output will be transmitted to<br>“Counter_Out”pin |
| Charge Pump current | 0     | Charge Pump current= 200 $\mu$ A                            |
| Fast-lock Timer     | 20    | Initial value of Fast-lock Timer= 20 $\mu$ s                |

Figure 5.24 shows the timing diagram of PLL setting which was generated by the Verilog-A view of PLL\_FN\_setting.

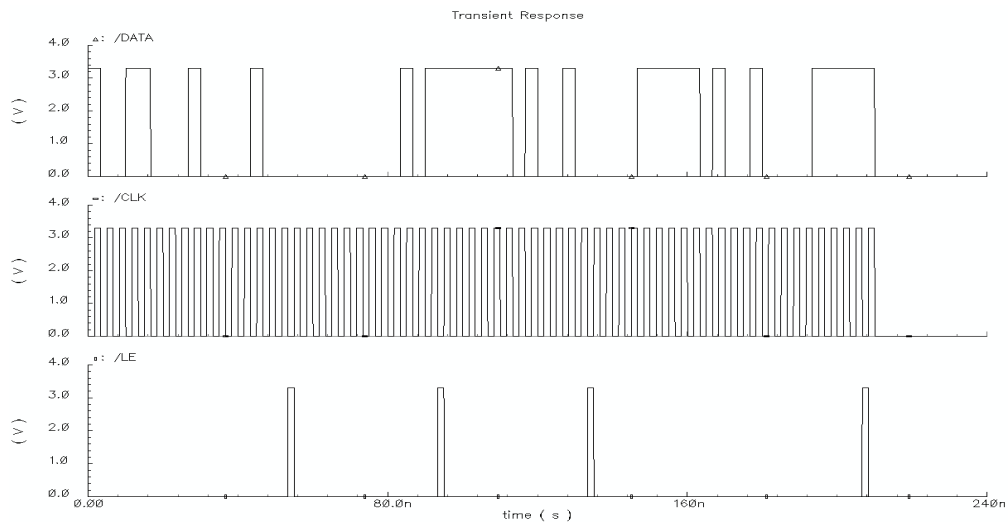


Figure 5.24 Timing diagram of PLL setting

## 5.2.4 Prescaler Controller

Prescaler Controller was used to test the dynamic characteristic of prescaler in a more efficient manner. The desired modulus waveform, actual modulus waveform and their discrepancies were plotted. Figure 5.25 shows an example of the test results at Typical condition (TT, 3.3V, 25<sup>0</sup>C) with 50MHz-step increments in schematic view.

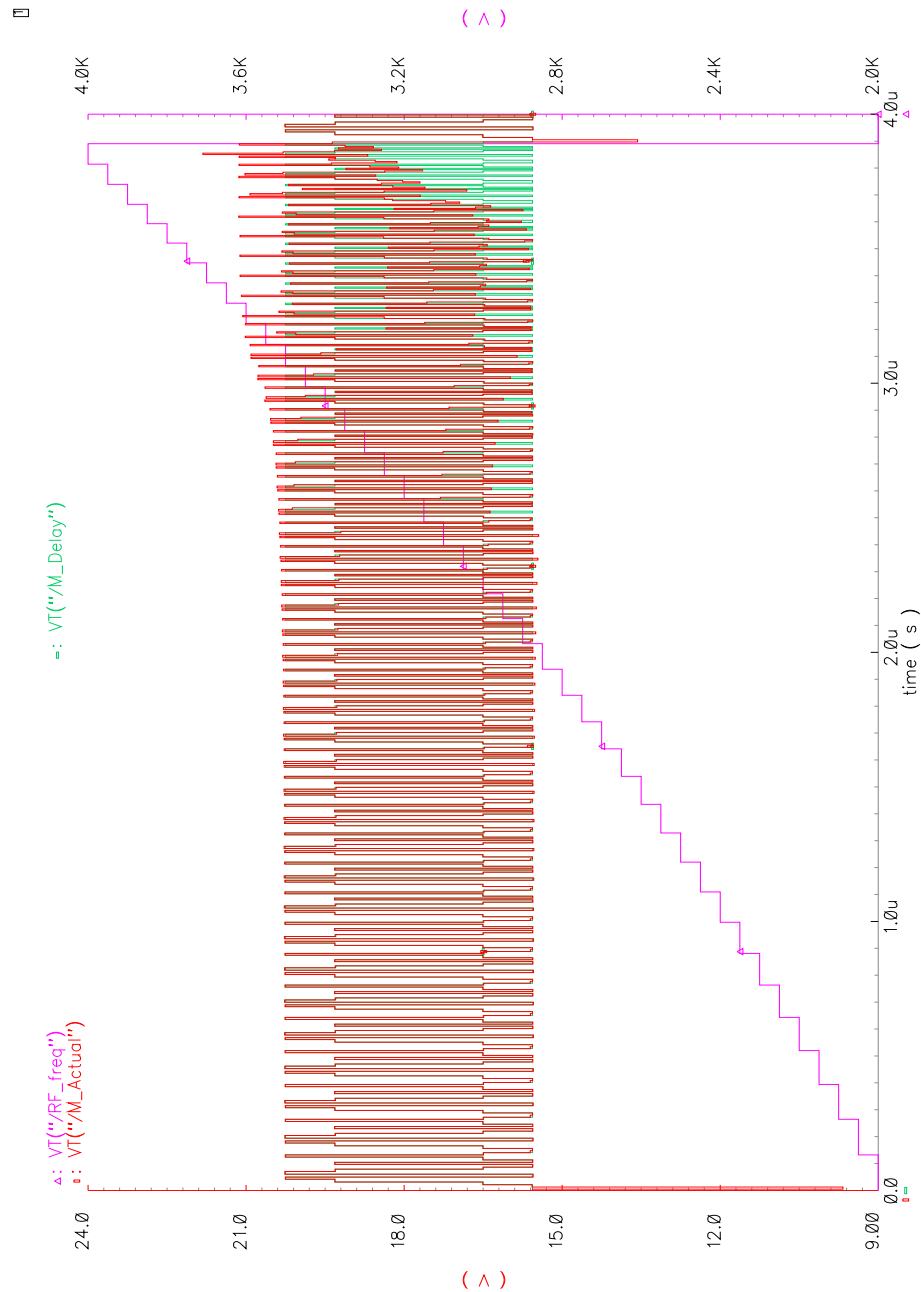


Figure 5.25 Dynamic characteristic of prescaler at Typical condition

According to the graphs, the prescaler functioned properly for operating frequency below 3500MHz and errors were detected in the division ratios for operating frequency beyond 3450MHz.

Although there were 12 modulus-changing patterns, not all were involved in the 2450MHz frequency band operations. For operating frequency= 2400~2500MHz with step size= 50kHz and MASH order= 3 or 4, the 8 modulus-changing patterns involved were: 16→17, 17→16, 16→20, 20→16, 21→16, 16→21, 21→20, 21→17 while the following 4 modulus-changing patterns were not involved: 17→20, 20→21, 20→17, 17→21, as illustrated in Figure 5.26.

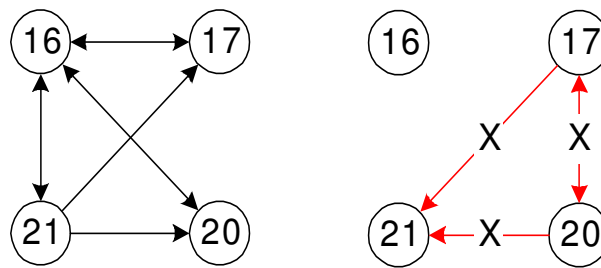


Figure 5.26 Modulus-changing patterns in 2450MHz band

If the design specifications for prescaler are very stringent, the ability to switch between uninvolved modulus-changing patterns may be ignored. However, this will limit the usable range of the prescaler.

### 5.2.5 N-Counter and MASH

The pulse interval of N-Counter output in Typical condition (TT, 3.3V, 25<sup>0</sup>C) at 2450.05MHz and MASH order= 4 is shown in Figure 5.27. The pseudo-random number for pulse interval was controlled by the MASH.

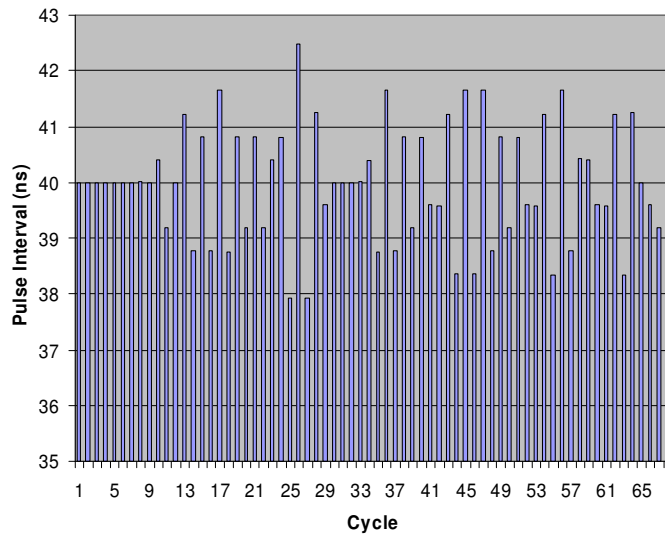


Figure 5.27 Pulse interval of N-Counter output

The division ratio of FN over FD was simplified by using greatest common divisor (GCD) method. Figure 5.28 illustrates the GCD value calculated via method of exhaustion. Upon obtaining the GCD value, the respective period of pseudo-random series was determined from Table 5.5.

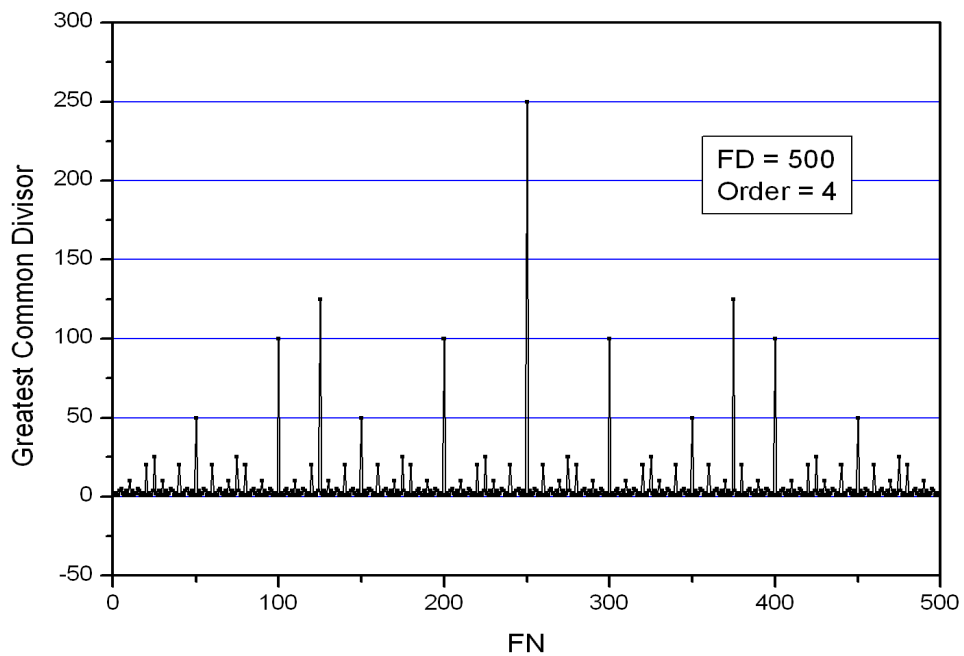


Figure 5.28 Greatest common divisor of FN and FD



| Table 5.5 |      | Period of pseudo-random series |     |     |     |    |    |    |     |     |     |     |
|-----------|------|--------------------------------|-----|-----|-----|----|----|----|-----|-----|-----|-----|
| GCD       | 1    | 2                              | 4   | 5   | 10  | 20 | 25 | 50 | 100 | 125 | 250 | 500 |
| Period    | 2000 | 1000                           | 125 | 400 | 200 | 25 | 80 | 40 | 5   | 16  | 8   | 1   |

Figure 5.29 shows the error for pulse interval of N-Counter output at 2450.05MHz and MASH order= 4, with reference to theoretical results. The maximum error was found to be less than  $15 \times 10^{-4}$ . Table 5.6 lists the pulse interval error of N-Counter output at various frequencies and MASH orders for the schematic views and extracted\_C views, respectively.

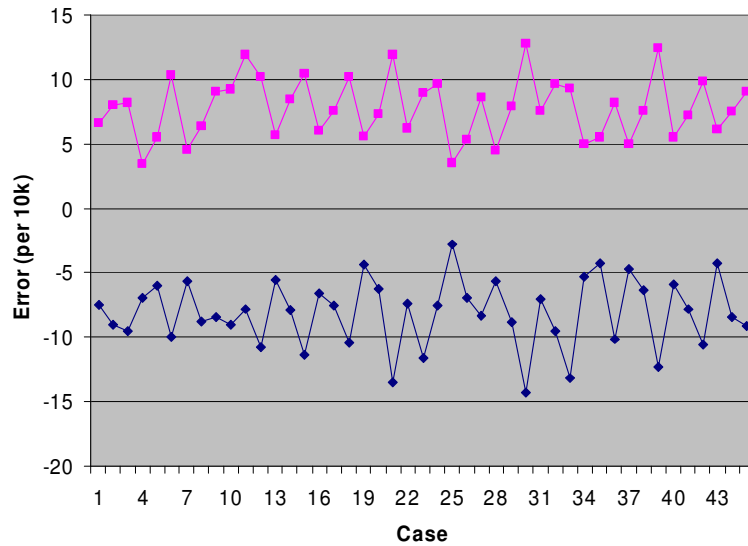


Figure 5.29 Error for pulse interval of N-Counter output

Table 5.6 Pulse interval error of N-Counter output at various frequencies and MASH order (FD= 500)

| Frequency (MHz) | MASH order | FN  | Schematic (per 10k) | Extracted (per 10k) |
|-----------------|------------|-----|---------------------|---------------------|
| 2420.00         | 3          | 400 | 6.60                | 4.08                |
| 2450.05         | 3          | 1   | 0.89                | 0.69                |
| 2474.95         | 3          | 499 | 0.54                | 0.39                |

|         |   |     |      |      |
|---------|---|-----|------|------|
| 2420.00 | 4 | 400 | 6.97 | 4.25 |
| 2450.05 | 4 | 1   | 7.08 | 4.22 |
| 2474.95 | 4 | 499 | 6.79 | 4.30 |

According to Table 5.6, the error for pulse interval of N-Counter output at various frequencies was observed to be relatively smaller for 3<sup>rd</sup> order MASH.

Figure 5.30 illustrates the theoretical noise shift characteristic of MASH at FN= 1, FD=500 and  $f_{REF} = 25\text{MHz}$ . Figure 5.31 shows the noise level of PDF output at 6.25kHz with  $f_{REF} = 25\text{MHz}$ . It was observed that 4<sup>th</sup> order MASH had the best noise-suppressing capability at low frequency, and the differences between noise levels of adjacent MASH orders were around 56dB.

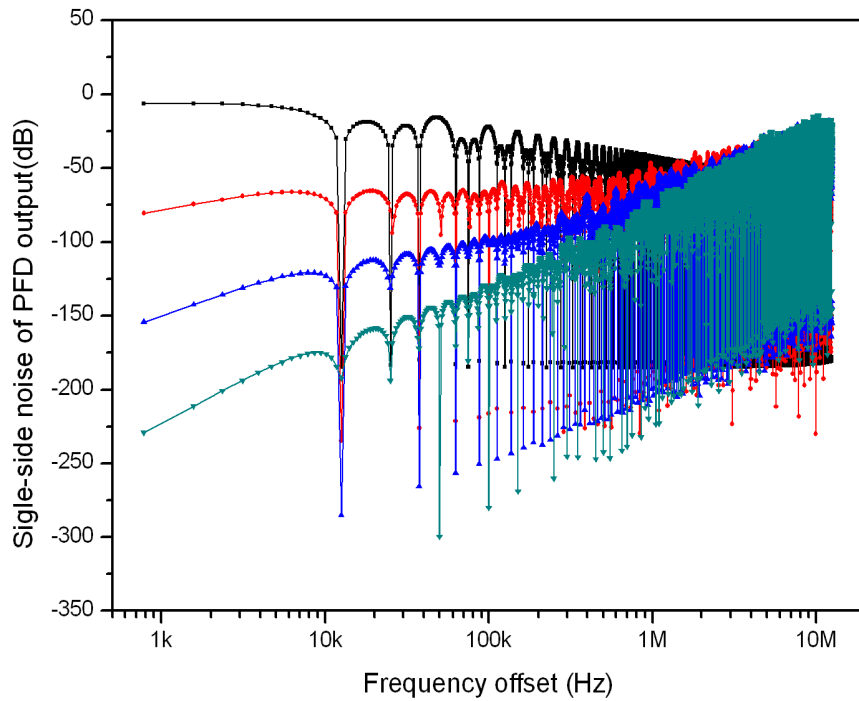


Figure 5.30 Noise shift characteristic of MASH

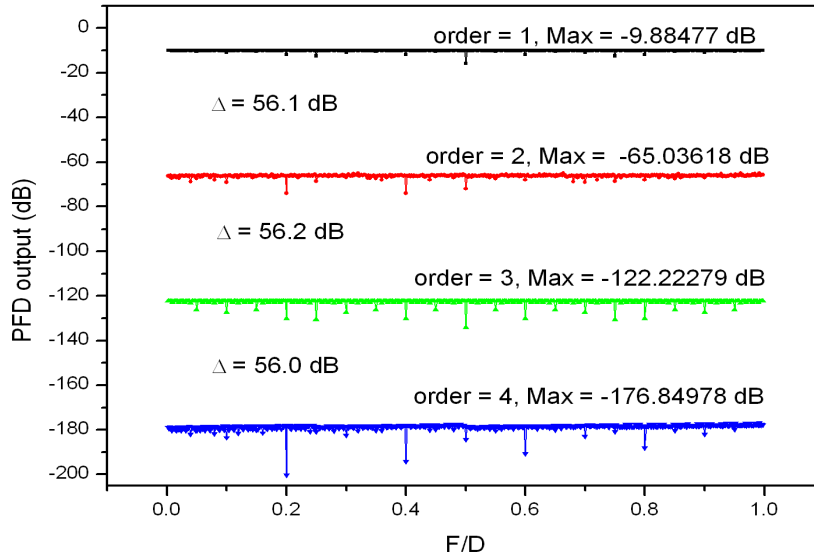


Figure 5.31 Noise level of PFD output at 6.25kHz ( $f_{REF} = 25\text{MHz}$ )

### 5.2.6 Modulus Control

In this design, MOD\_A and MOD\_B were the control lines for switching the modulus of prescaler. Both lines had delay in terms of nanosecond, which was taken into consideration during the design phase of prescaler. Figure 5.32 and Figure 5.33 show the delay of MOD\_A and MOD\_B, respectively, in all 45 cases.

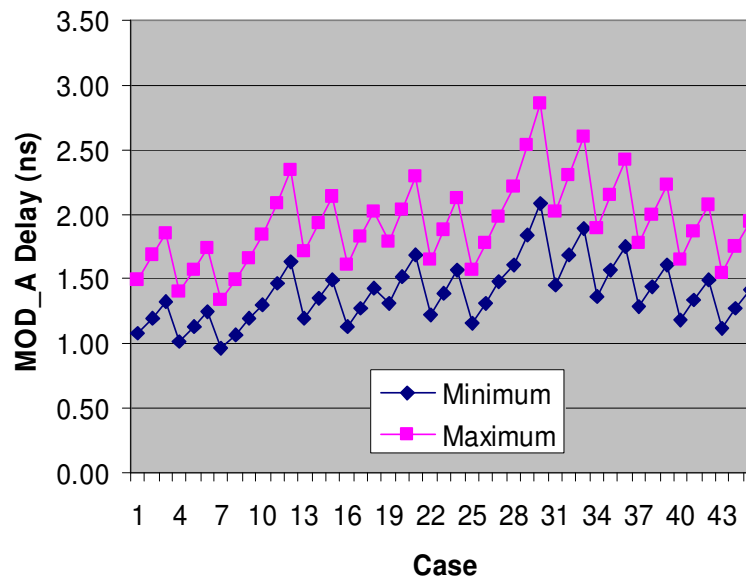


Figure 5.32 Delay of MOD\_A in 45 cases

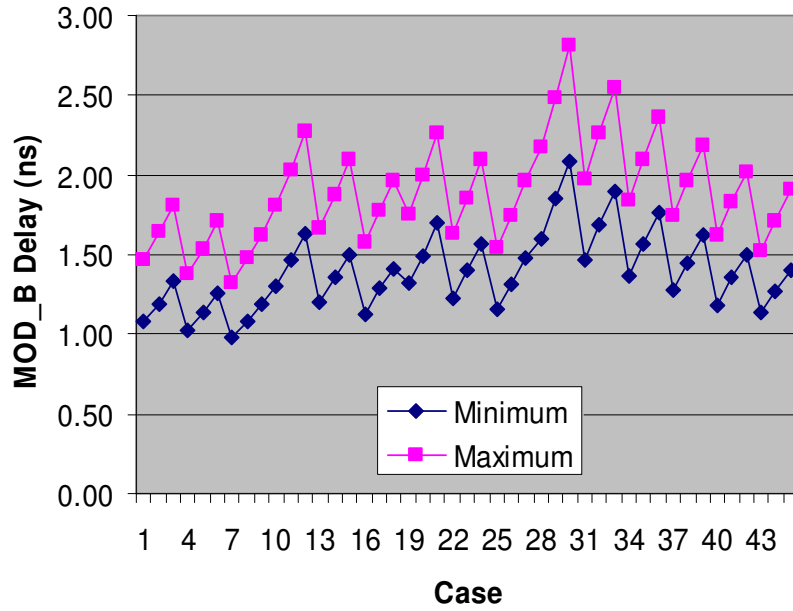


Figure 5.33 Delay of MOD\_B in 45cases

### 5.2.7 PFD and Charge Pump

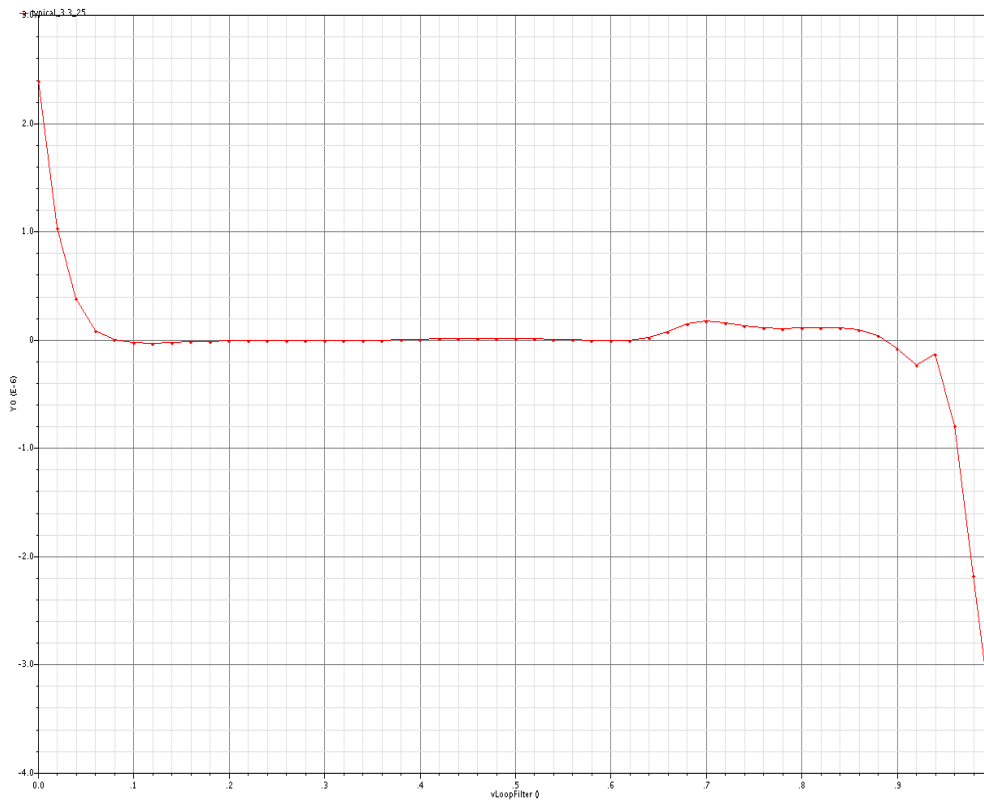


Figure 5.34 Intercept of charge pump current in Typical condition

The intercept of charge pump current is a vital parameter for approximating the linearity of charge pump and PFD. Hence, its absolute value was kept to be as small as possible when the LO signal was synchronous with the reference signal. Figure 5.34 illustrates the intercept of charge pump current at various loop filter voltages (i.e., 0V to 3.3V) in Typical condition (TT, 3.3V, 25<sup>0</sup>C). Figure 5.35 demonstrates the intercept of charge pump current at various loop filter voltages in 45 cases, showing optimal performance when loop filter voltage is within the range of (0.1\*V<sub>dd</sub>) to (0.8\*V<sub>dd</sub>).

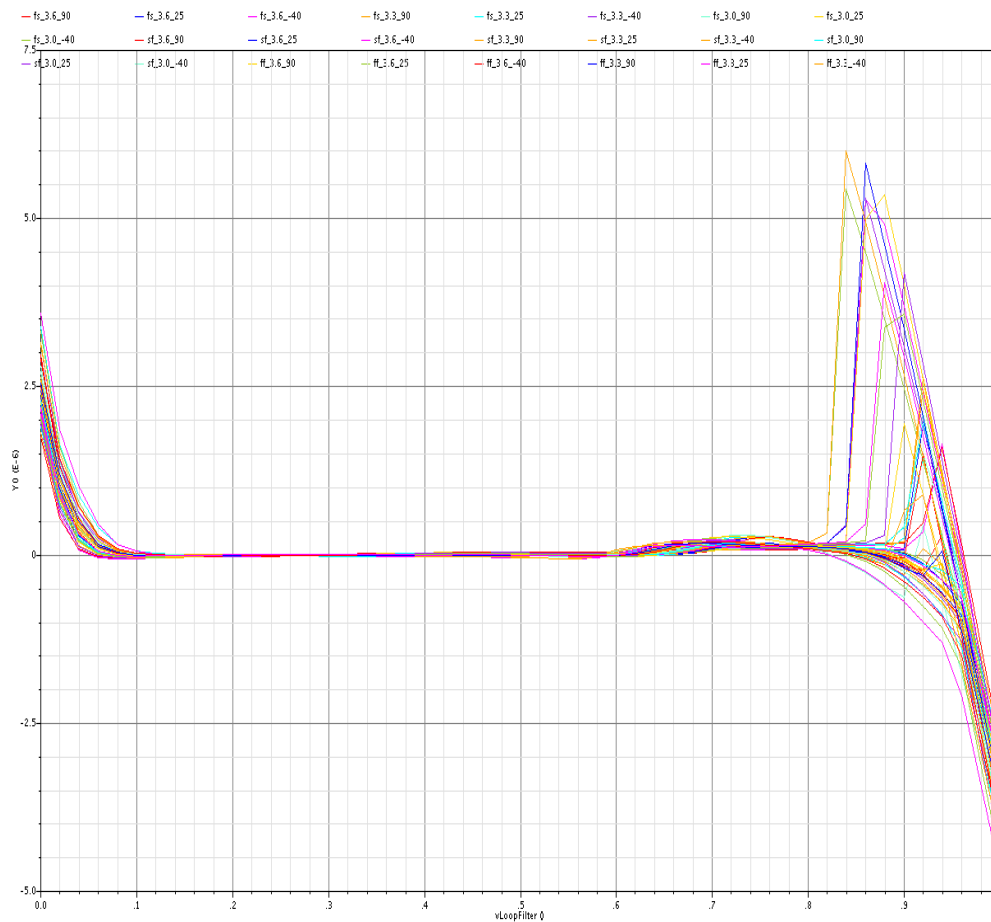


Figure 5.35 Intercept of charge pump current in 45 cases

Linearity of charge pump current is another key issue which needs to be addressed, especially when the PLL is locked. Figure 5.36 and Figure 5.37 show the linearity of

charge pump current with PFD at Typical condition (TT, 3.3V, 25°C). According to the figure, PFD and Charge Pump functioned optimally when loop filter voltage was within the range of  $(0.1 \cdot V_{dd})$  to  $(0.8 \cdot V_{dd})$ , and the linearity was degenerated when loop filter voltage was adjacent to supply voltages. The period of the linearity curve was less than  $2\pi$  because two delay cells were implemented to remove the dead-zone in PFD and Charge Pump.

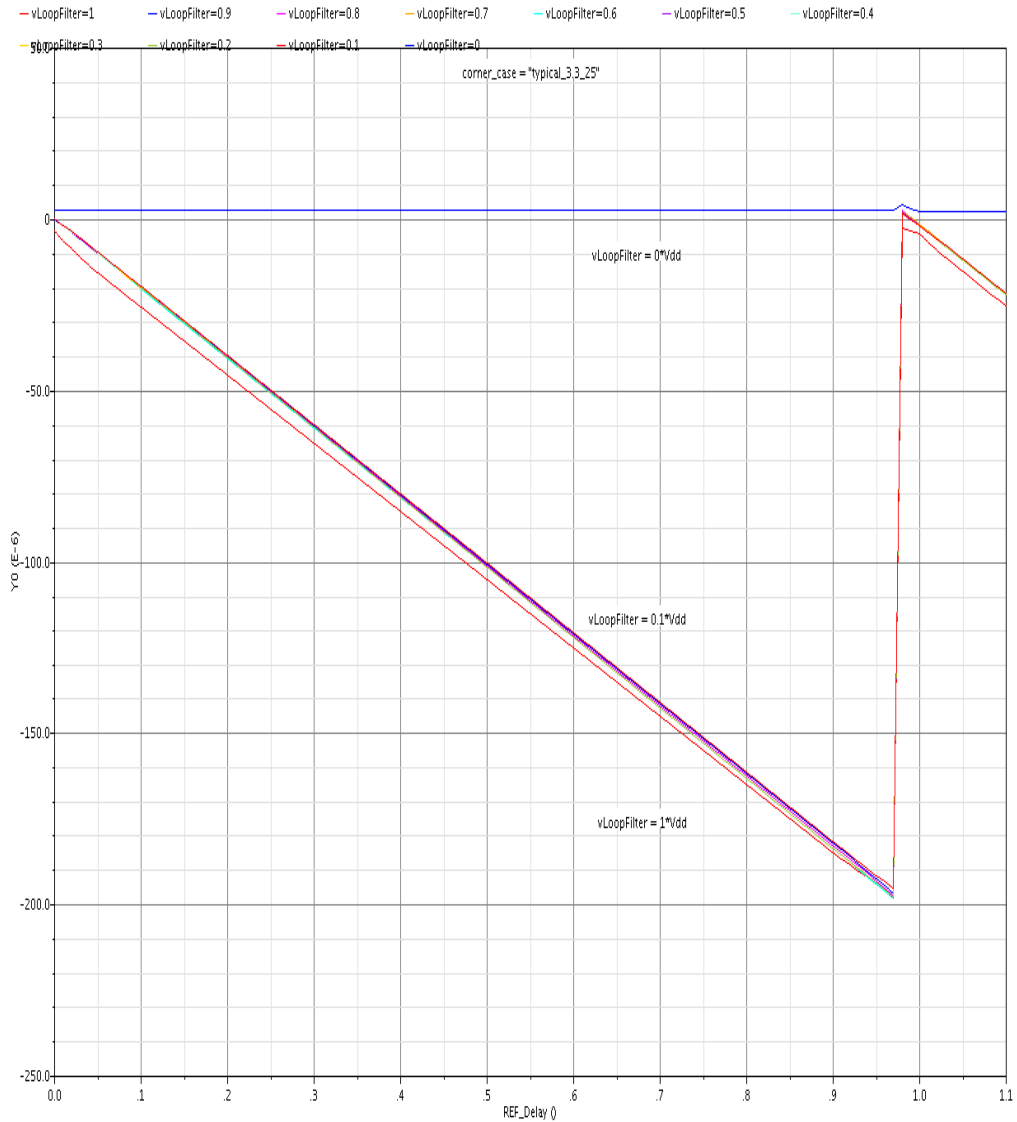


Figure 5.36 Linearity of charge pump current with PFD at Typical condition

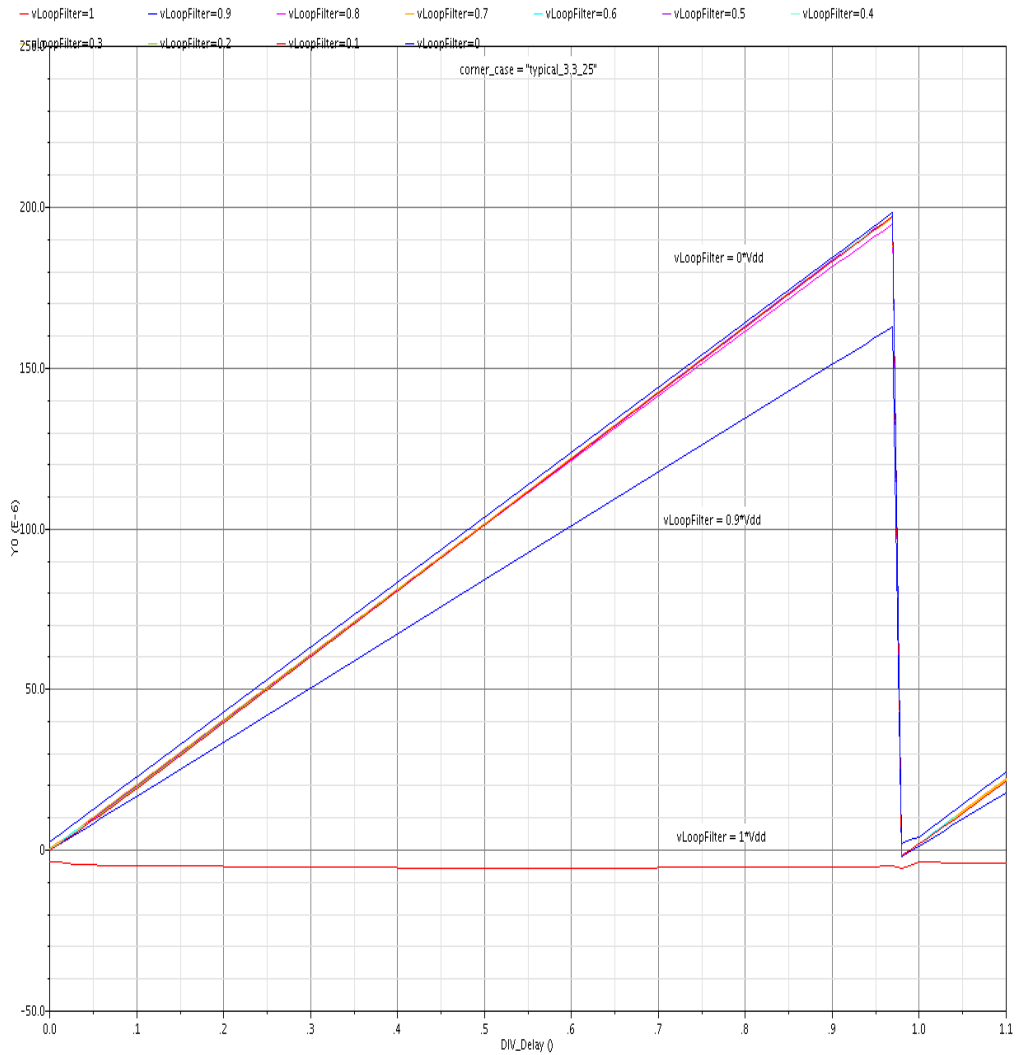


Figure 5.37 Linearity of charge pump current with PFD at Typical condition

### 5.2.8 Loop Filter

Simulations were carried out to check the locking property of PLL with PFD, Charge Pump, Virtual Ground and Loop Filter in Schematic view whilst the remaining building blocks in Verilog-A view. Figure 5.38 shows the locking curve of PLL without activating the Fast-lock function at Typical condition (TT, 3.3V, 27<sup>0</sup>C), with expected frequency of 2450.05MHz and final frequency of 2454.12MHz in 397μs from free-running point.

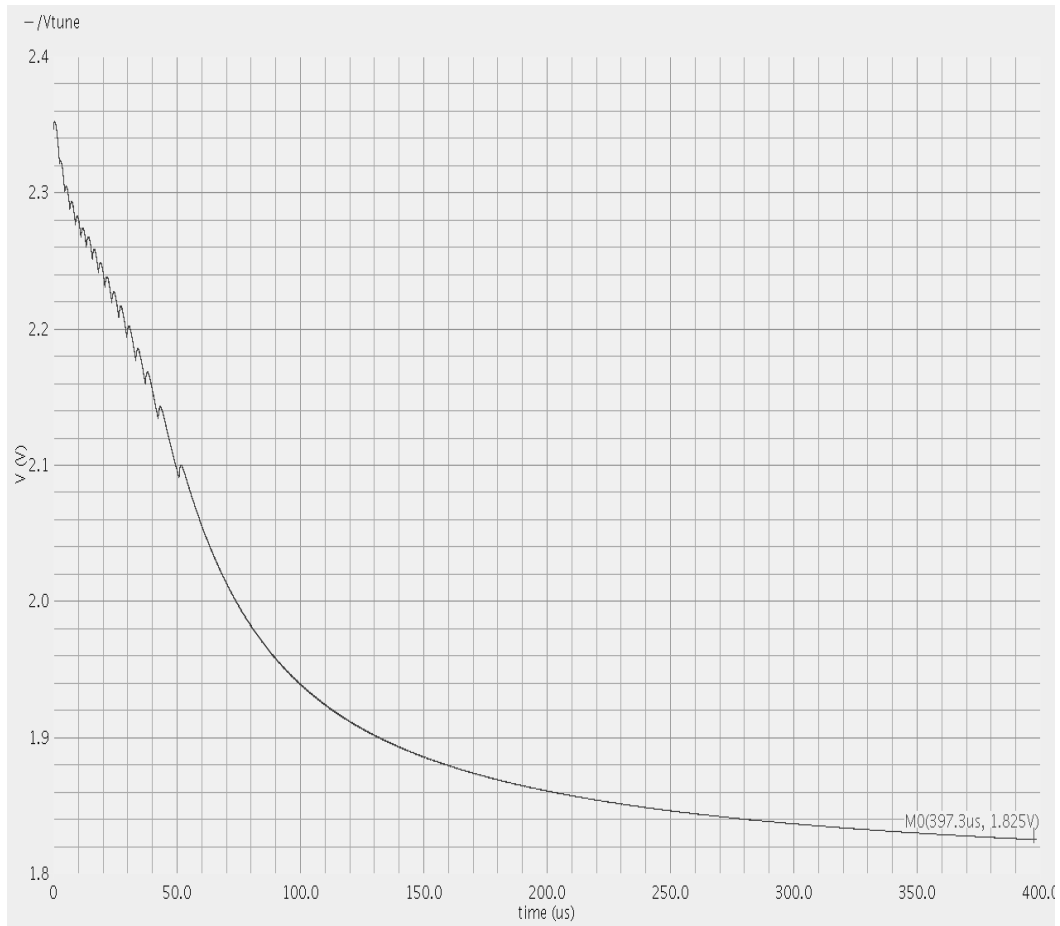


Figure 5.38 Locking curve of PLL without Fast-lock function at Typical condition

Figure 5.39 shows the PLL locking curve with Fast-lock Timer set at 20 $\mu$ s at Typical condition (TT, 3.3V, 27 $^{\circ}$ C). The expected frequencies monitored were 2474.95MHz, 2450.05MHz and 2420.00MHz, respectively. According to the simulation results, PLL was found to be able to lock faster upon activation of Fast-lock function.



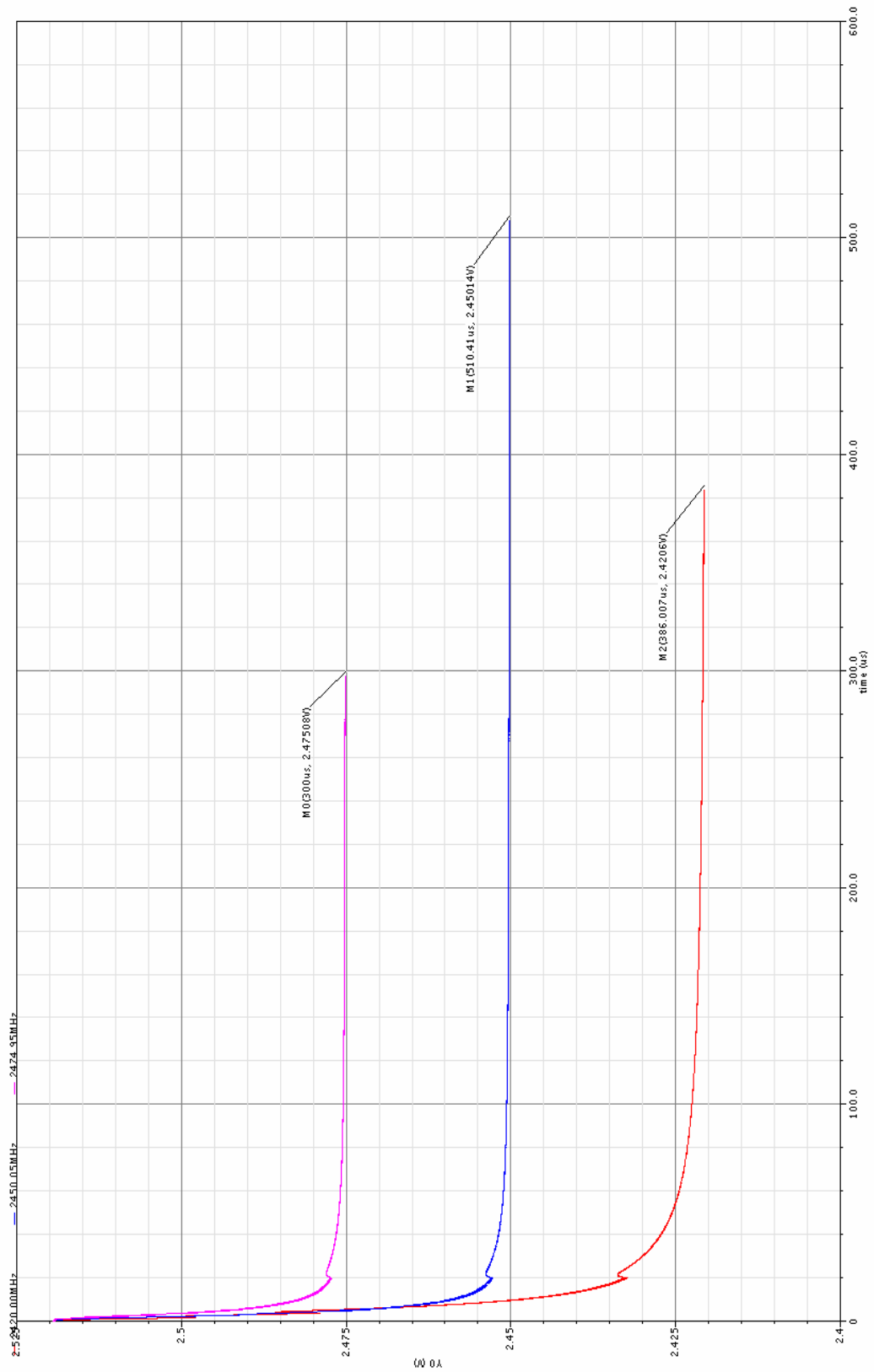


Figure 5.39 Locking curve of PLL with Fast-lock function at Typical condition

Figure 5.40 shows the responses of synthesizer when frequency jumped from 2400MHz to 2500MHz and vice versa at Typical condition (TT, 3.3V, 27°C), with the Fast-lock Timer set at 30μs. Frequency ripple was caused by the inherently inconstant division ratio of N-Counter, due to MASH, as depicted by Figure 5.41. The ripple had a period of around 40ns which was comparable to the period of 25MHz reference signal, and amplitude of less than 300Hz which could be further reduced via narrow-bandwidth loop filter. This 300Hz ripple was identified to be 0.125ppm of the 2400MHz center frequency.

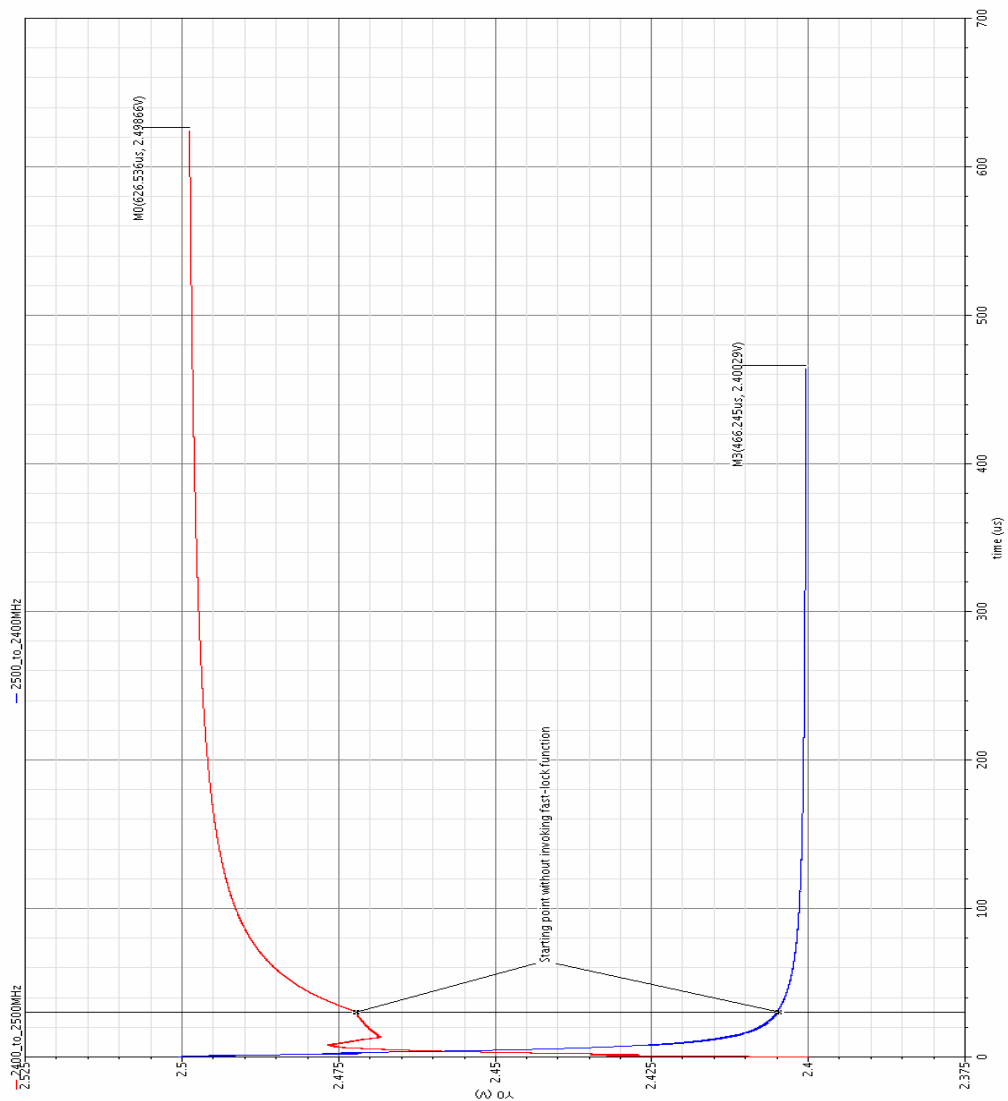


Figure 5.40 Synthesizer responses to frequency jumps

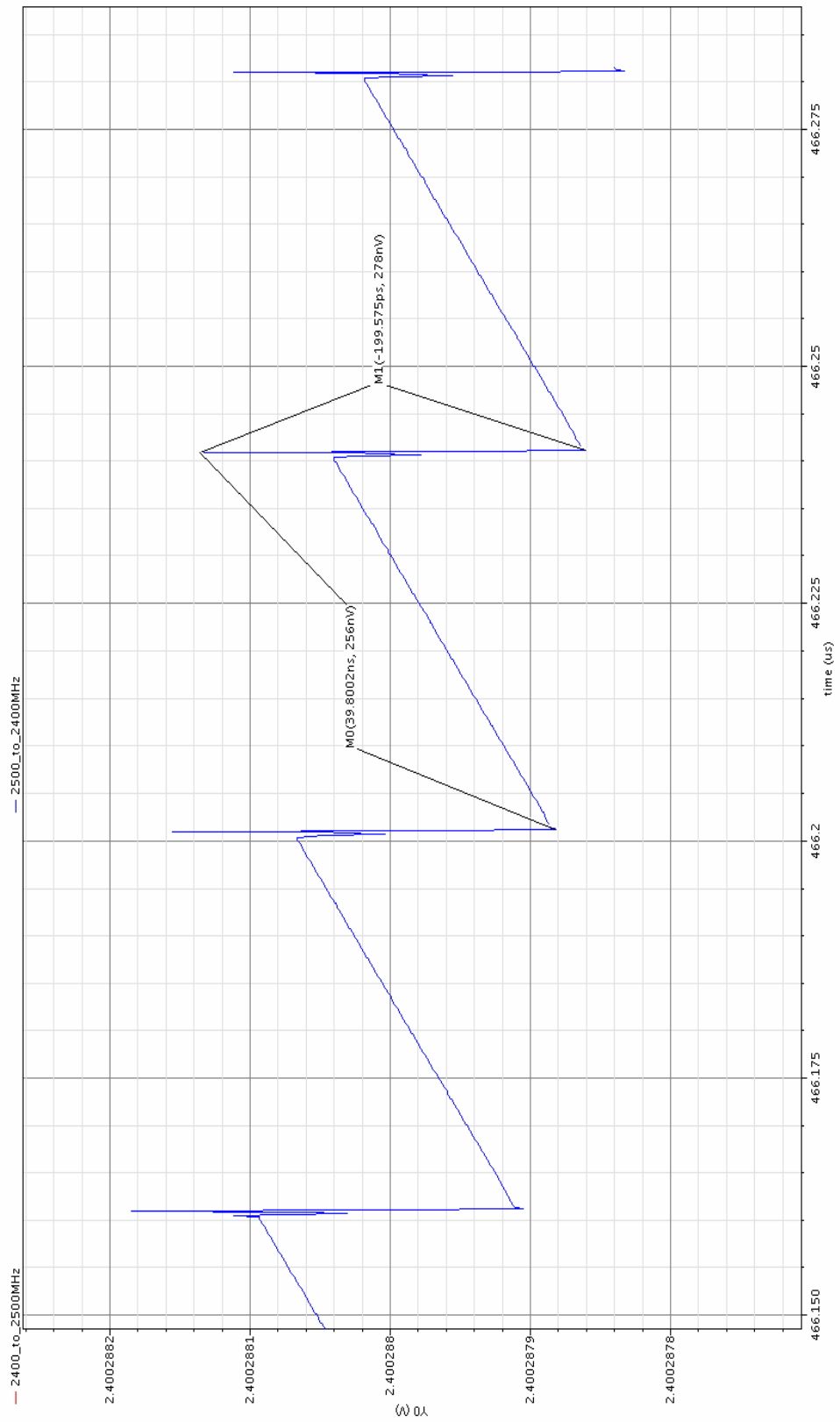


Figure 5.41 Frequency ripple of synthesizer

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### 5.3 Measurement Results

The frequency synthesizer design was taped-out for facilitating the study of its actual performance. Five samples were obtained, and the performances of frequency synthesizer were measured with an integrated VCO that is designed for 2450MHz frequency band operation.

#### 5.3.1 Test Plan

Table 5.7 shows the test conditions whilst Table 5.8 lists the measurement equipments used for measuring the performances of frequency synthesizer.

| Parameter                       | Unit | Test condition   |
|---------------------------------|------|--|
| PLL current consumption         | mA   | Vdd= 3.0; 3.3; 3.6V  |
| Charge Pump current consumption | μA   | Vdd= 3.0; 3.3; 3.6V  |
| Operating frequency range       | MHz  | Vdd= 3.0; 3.3; 3.6V<br>Span= 1MHz for 2450MHz;<br>100kHz for 25MHz |

| Description                       | Manufacturer | Model  | Quantity |
|-----------------------------------|--------------|--------|----------|
| 22GHz Microwave Spectrum Analyzer | HP           | 8593E  | 1        |
| 9kHz~2.9GHz Spectrum Analyzer     | HP           | 8594E  | 1        |
| BenchLink Spectrum Analyzer       | Agilent      | E4444A | 1        |
| USB/GPIB Interface                | Agilent      | 82357A | 1        |
|                                   | Technologies |        |          |
| DC Power Supply                   | KENWOOD      |        | 1        |

| Description         | Manufacturer | Model  | Quantity |
|---------------------|--------------|--------|----------|
| Multimeter          | HP           | 34401A | 1        |
| PC                  |              |        | 1        |
| PLL Control Program |              |        |          |

### 5.3.2 Operating Frequency Range

Table 5.9 lists the measured operating frequency ranges for five samples at three operating voltages (3.0, 3.3 and 3.6V) respectively, and the extracted\_C simulation results. The maximum operating frequency measured was limited by the operating range of the VCO which was designed for 2450MHz band.

| Sample                        | Operating frequency (MHz) |           |           |         |
|-------------------------------|---------------------------|-----------|-----------|---------|
|                               | Vdd= 3.0V                 | Vdd= 3.3V | Vdd= 3.6V |         |
|                               | Max                       | Min       | Max       | Max     |
| extracted_C simulation result | 3000.00                   | -         | 3005.00   | 3000.00 |
| #1                            | 2550.70                   | 2066.40   | 2564.05   | 2577.05 |
| #2                            | 2561.10                   | 2076.95   | 2574.50   | 2588.70 |
| #3                            | 2539.80                   | 2057.30   | 2554.15   | 2566.30 |
| #4                            | 2543.70                   | 2058.55   | 2557.85   | 2571.15 |
| #5                            | 2539.05                   | 2043.00   | 2554.25   | 2564.95 |

### 5.3.3 PLL Setting

Figure 5.42 shows the timing diagram of PLL settings: channel 1 represented PLL\_DATA, channel 2 represented PLL\_CLK, and channel 3 represented PLL\_LE.



Figure 5.42 Timing diagram for PLL setting

### 5.3.4 Reference Spurs

Reference spur is one of the most common contributors to the spurious levels on the PLL output spectrum. These spurs can be observed at an offset of  $\pm f_{REF}$  from the PLL output frequency, and are instigated by the non-idealities in PLL components, namely:

- leakage current in VCO tuning node
- mismatch in PFD and Charge Pump propagation delay
- mismatch in CP current, and charge injection.

Table 5.10 summarizes the reference spurious levels at  $f_{REF}$  with carrier frequency set at 2450MHz and operating voltage of 3.3V. Figures 5.43-5.45 show the reference spur

plots for Sample #5. Reference spur plots for Samples #1-#4 are attached in Appendix

A.

| Sample | Table 5.10 Frequency synthesizer reference spurs |                   |                  |
|--------|--|-------------------|------------------|
|        | Spurious level (dBc)                             |                   |                  |
|        | at 10.80MHz_left                                 | at 25.05MHz_right | at 25.80MHz_left |
| #1     | -61.98   | -71.10            | -68.89           |
| #2     | -62.45   | -71.82            | -69.41           |
| #3     | -63.08   | -71.61            | -69.26           |
| #4     | -62.14   | -71.43            | -69.42           |
| #5     | -62.82   | -71.38            | -70.26           |

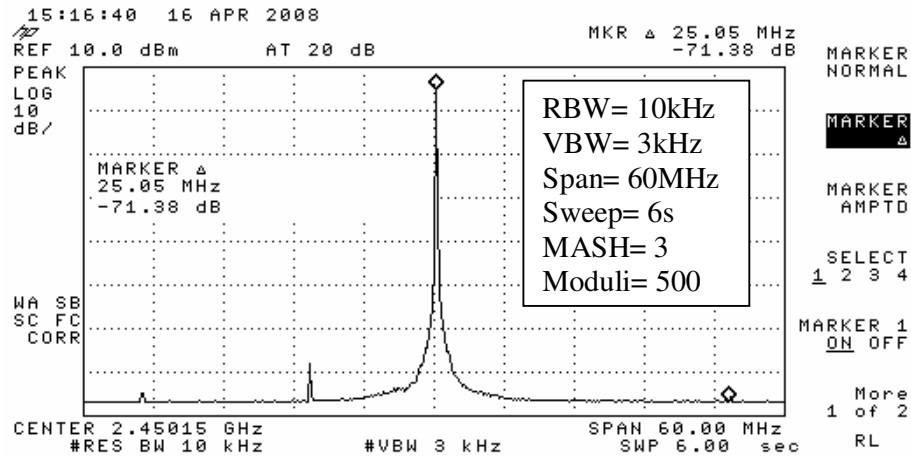


Figure 5.43 #5 frequency synthesizer reference spur plot at ~25MHz offset (right)

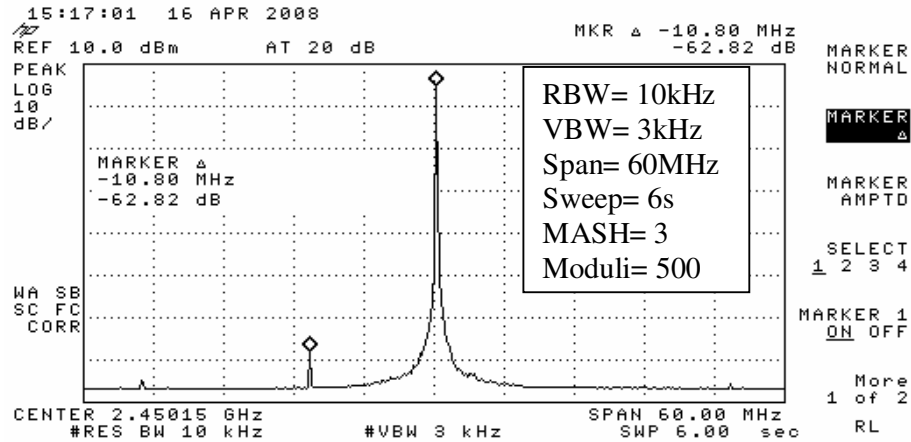


Figure 5.44 #5 frequency synthesizer reference spur plot at 10.80MHz offset (left)

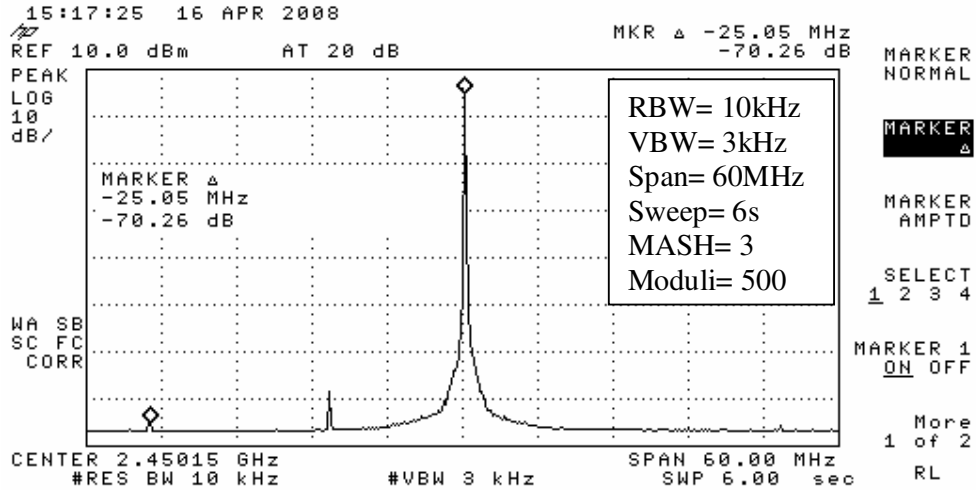


Figure 5.45 #5 frequency synthesizer reference spur plot at ~25MHz offset (left)

### 5.3.5 Fractional Spurs

Fractional spurs can be observed at spacings equal to the channel spacing, i.e. 50kHz, of the synthesizer. This phenomenon could be due to the following:

- inability of modulator to adequately correlate the output samples, especially for inputs which are close to integer value
- non-linear mixing in PFD generates down-conversion of tones which are intrinsically present around  $f_{REF}/2$ .

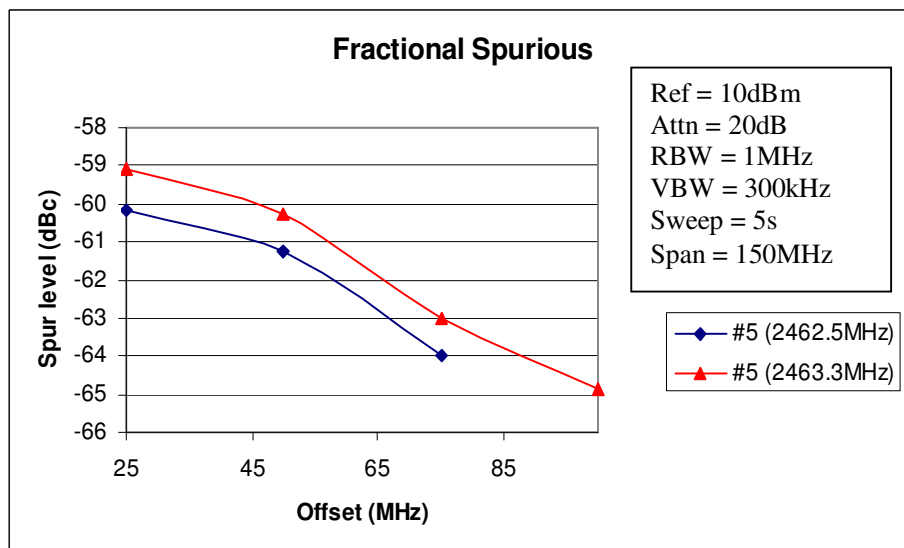


Figure 5.46 Fractional spurious levels at 2462.5MHz and 2463.3MHz



Figure 5.46 shows the comparison of fractional spurious levels at 2462.5MHz and 2463.3MHz. Table 5.11 lists the fractional spurious levels at offsets of 25MHz, 50MHz, 75MHz, and 100MHz from carrier frequency of 2462.5MHz~2463.3MHz, at channel spacing of 50kHz and loop filter bandwidth of 20kHz. Fractional spurs plots for Sample #5 are attached in Appendix B.

| Carrier frequency<br>(MHz) | Spurious level (dBc) |                    |                    |                     |
|----------------------------|----------------------|--------------------|--------------------|---------------------|
|                            | at 25MHz<br>offset   | at 50MHz<br>offset | at 75MHz<br>offset | at 100MHz<br>offset |
| 2462.50                    | -60.16               | -61.26             | -64.00             | -                   |
| 2462.55                    | -60.20               | -60.76             | -63.24             | -                   |
| 2462.60                    | -60.05               | -60.65             | -63.51             | -                   |
| 2462.65                    | -60.26               | -60.58             | -63.41             | -                   |
| 2462.70                    | -60.07               | -60.02             | -62.80             | -65.33              |
| 2462.75                    | -59.99               | -59.96             | -63.64             | -65.02              |
| 2462.80                    | -60.49               | -60.10             | -62.82             | -65.13              |
| 2462.85                    | -60.78               | -60.37             | -62.96             | -65.40              |
| 2462.90                    | -60.32               | -60.46             | -63.04             | -65.26              |
| 2462.95                    | -60.67               | -60.65             | -63.70             | -65.54              |
| 2463.00                    | -57.33               | -57.37             | -59.21             | -60.79              |
| 2463.05                    | -59.28               | -59.77             | -62.71             | -65.42              |
| 2463.10                    | -60.52               | -60.01             | -62.63             | -65.06              |
| 2463.15                    | -59.59               | -59.88             | -62.62             | -64.91              |
| 2463.20                    | -59.41               | -60.14             | -62.60             | -65.00              |
| 2463.25                    | -59.09               | -59.65             | -62.62             | -64.25              |
| 2463.30                    | -59.08               | -60.25             | -63.00             | -64.84              |

### 5.3.6 Integer-N Boundary Spur

Integer-N boundary spurs might appear when VCO frequency interacts with PFD frequency and produces spurious sidebands on the VCO output spectrum at an offset frequency equals to the difference between integer multiple of PFD frequency and VCO frequency. These spurs are more apparent when VCO/PLL is programmed to frequencies that are close to the harmonic multiples of PFD frequency. Higher PFD frequency will create fewer integer channels in the desired band. Hence, reducing the occurrences of integer boundary spurs.

Figure 5.47 and Figure 5.48 show the integer boundary spurious levels with loop filter of 20kHz and operating voltage of 3.3V. The carrier frequencies were set at 50kHz increments from 2450MHz. The graphs illustrate a general trend of reducing integer boundary spurious level as the carrier frequency increases. Integer-N boundary spurious levels and plots for Sample #5 are attached in Appendix C.

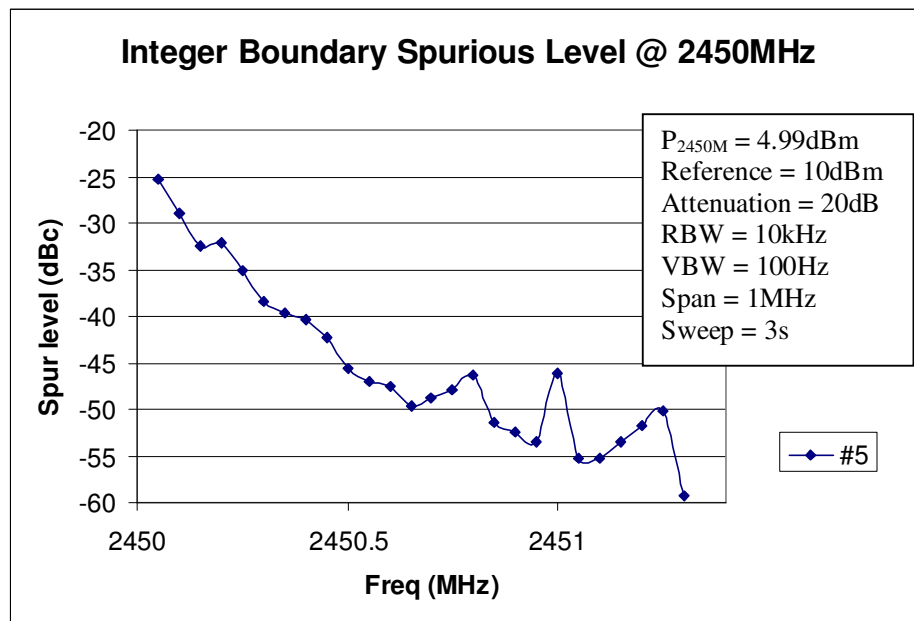


Figure 5.47 Integer-N boundary spurs for 2450.05MHz~2451.30MHz

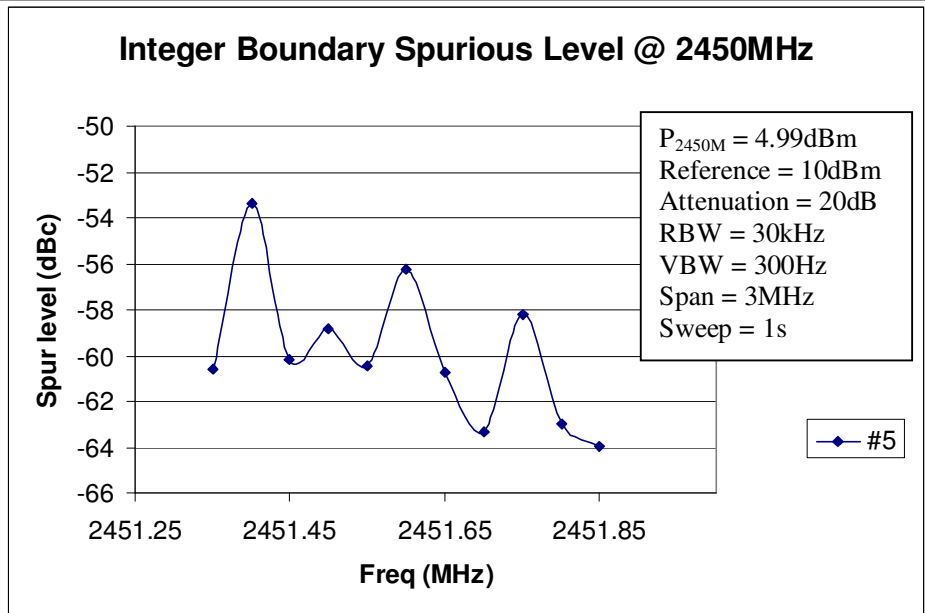


Figure 5.48 Integer-N boundary spurs for 2451.35MHz~2451.85MHz

Figure 5.49 and Figure 5.50 show effect of denominator on the integer-N boundary spurious levels at carrier frequency of 2451MHz and offset of 1MHz, with Moduli= 500 and Moduli= 501 respectively. Figure 5.51 demonstrates an overview of the denominator's effect on averaging the integer boundary spurious levels. From the graphs, it was observed that higher denominator value would reduce the overall integer boundary spurious levels.

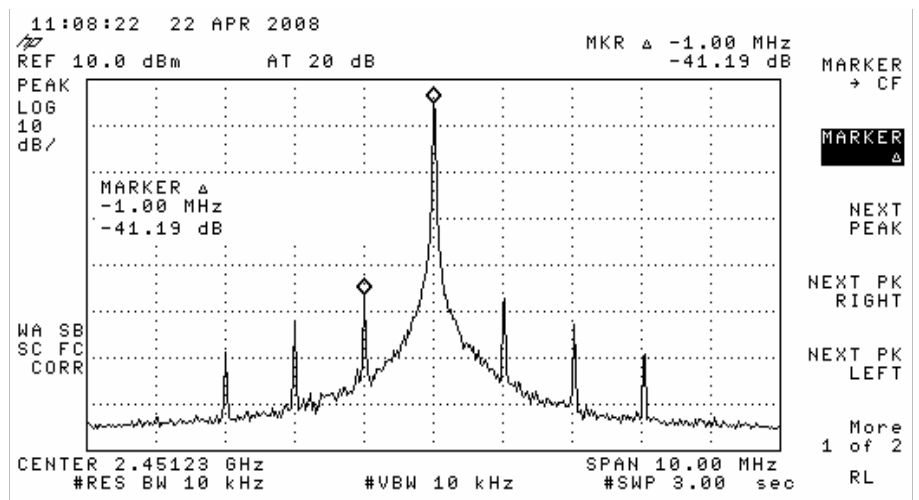


Figure 5.49 Integer-N boundary spurs at carrier frequency of 2451MHz and offset of 1MHz with Moduli= 500, MASH=3, FN= 20

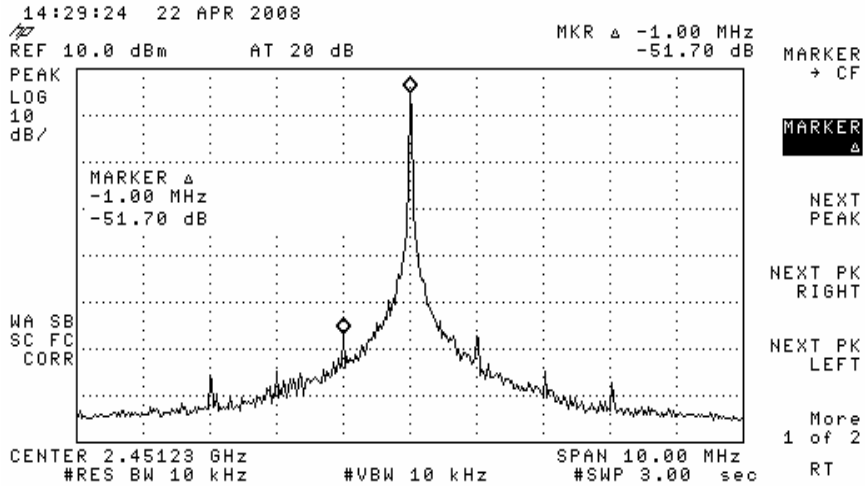


Figure 5.50 Integer-N boundary spurs at carrier frequency of 2451MHz and offset of 1MHz with Moduli= 501, MASH= 3, FN= 20

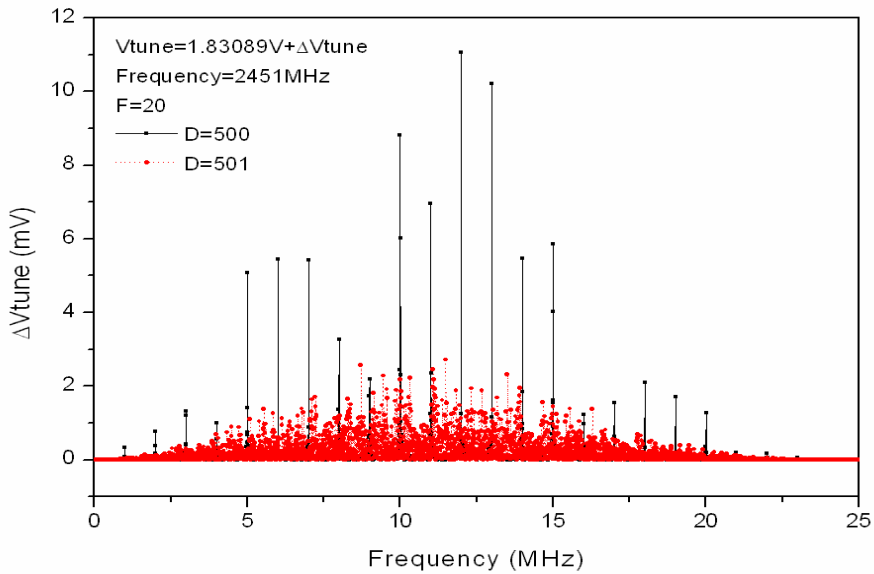


Figure 5.51 Effect of denominator on averaging the integer-N boundary spurious levels

Figure 5.52 shows the effect of MASH order (i.e. MASH=3 and MASH=4) on the integer-N boundary spurious levels at carrier frequency of 2451MHz with various moduli values (Table C.2). According to the graph, synthesizer with MASH=3 had lower spurious level as compared to MASH=4, with maximum level at -40.44dBc and minimum level at -46.57dBc.

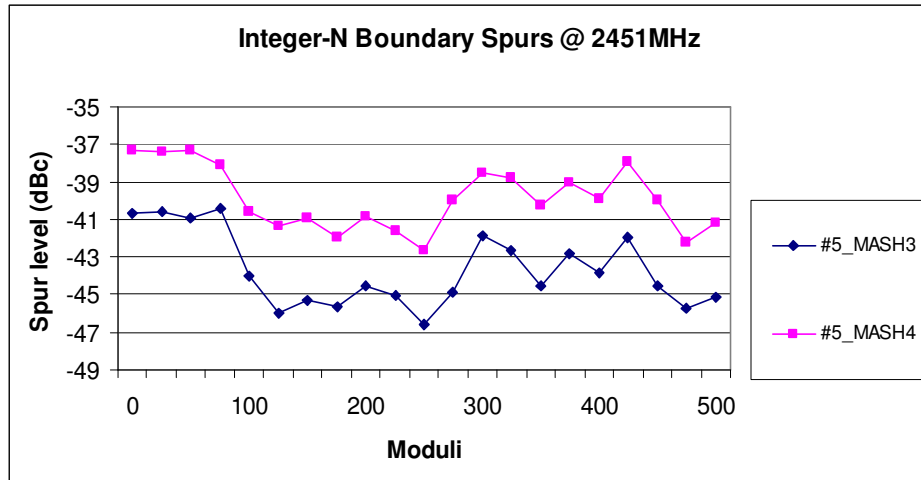


Figure 5.52 Effect of MASH order on integer-N boundary spurious levels

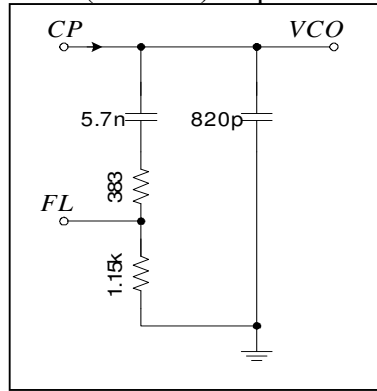
### 5.3.7 Loop Filter

Table 5.12 shows various loop filter designs with respective loop-filter order and loop bandwidth.

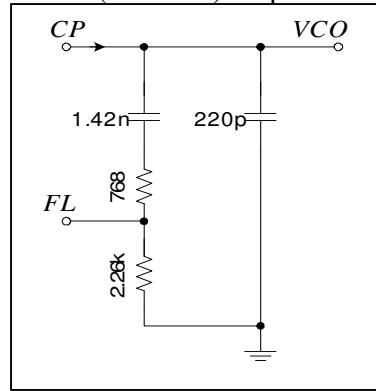
Table 5.12 Loop filter designs

| 1kHz (2 <sup>nd</sup> order) loop bandwidth | 5kHz (2 <sup>nd</sup> order) loop bandwidth |
|---|---|
|   |   |
|   |   |

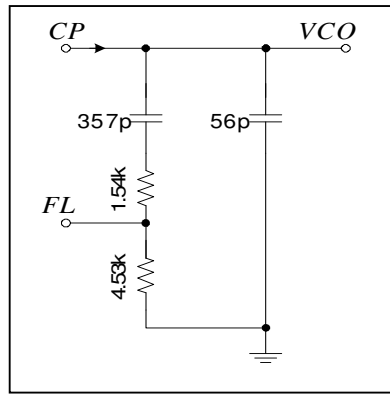
50kHz (2<sup>nd</sup> order) loop bandwidth



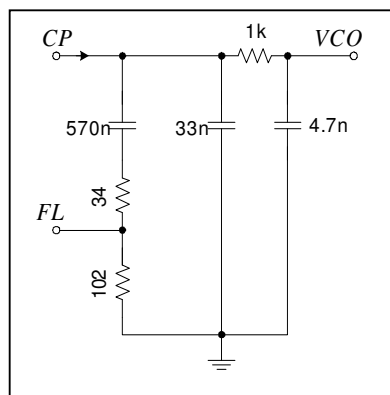
100kHz (2<sup>nd</sup> order) loop bandwidth



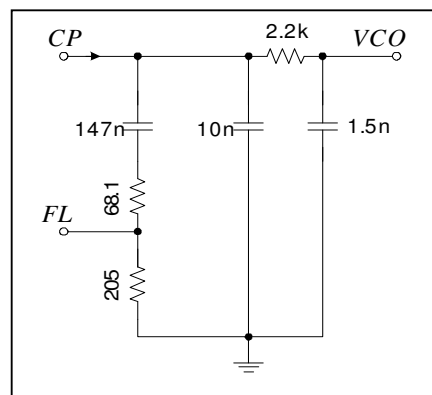
200kHz (2<sup>nd</sup> order) loop bandwidth



5kHz (3<sup>rd</sup> order) loop bandwidth



10kHz (3<sup>rd</sup> order) loop bandwidth



### 5.3.8 Phase Noise

Figure 5.53 shows the frequency synthesizer's phase noise performances at 10kHz, 20kHz, 50kHz and 200kHz offsets from the carrier frequency of 2450MHz with various loop bandwidths (at 2<sup>nd</sup> order), respectively. As shown, the phase noise suppression nearer to carrier frequency improved as the loop bandwidth increased. The loop filter's order would only affect the phase noise suppression at offsets farther from the carrier frequency. The phase noise performances plots for Sample #1-#5 are attached in Appendix D.

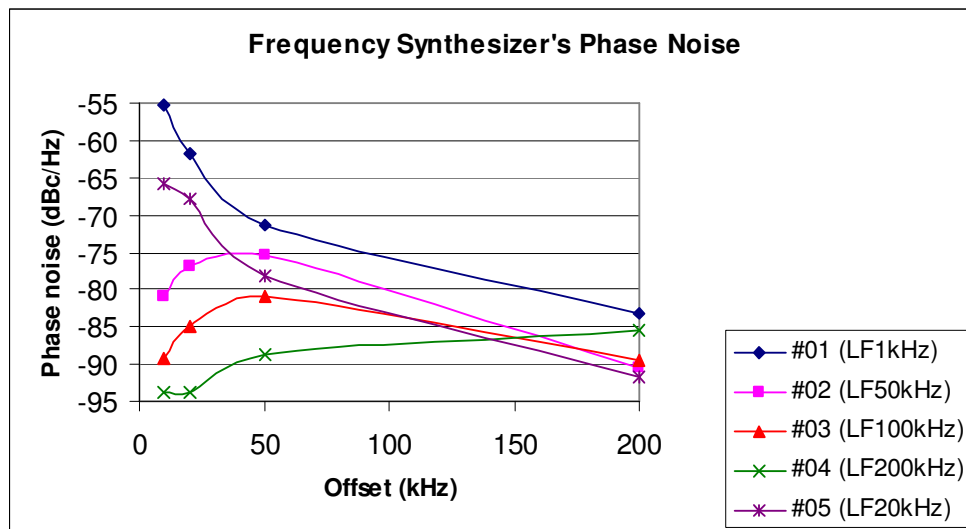


Figure 5.53 Frequency synthesizer's phase noise performances

### 5.3.9 Crystal Oscillating Frequency

Table 5.13 lists the crystal oscillating frequency range at various operating voltages (i.e. 3.0V~3.3V).

| Parameter             | Value           |                 |                 |
|-----------------------|-----------------|-----------------|-----------------|
| Operating voltage (V) | 3.0             | 3.3             | 3.6             |
| Frequency (MHz)       | 25.0023~25.0028 | 25.0028~25.0030 | 25.0030~25.0033 |

---

### 5.3.10 Effect of Loop Bandwidth on Settling Time

Table 5.14 demonstrates the effect of loop bandwidth on the settling time of output signal rising and falling edges for 2<sup>nd</sup> order loop filters when fastlock= 0 $\mu$ s. According to the table, when fastlock was set at 0 $\mu$ s, larger loop bandwidth would result in shorter settling time. Besides, 2<sup>nd</sup> order loop filter would result in slightly shorter settling time as compared to 3<sup>rd</sup> order loop filter with the same loop bandwidth.

Table 5.14 Effect of loop bandwidth on settling time

| Sample             | #1<br>(LF 1kHz) |       | #5<br>(LF 20kHz) |      | #2<br>(LF 50kHz) |      | #3<br>(LF 100kHz) |      | #4<br>(LF 200kHz) |      |
|--------------------|-----------------|-------|------------------|------|------------------|------|-------------------|------|-------------------|------|
|                    | rise            | fall  | rise             | fall | rise             | fall | rise              | fall | rise              | fall |
| Edge               | rise            | fall  | rise             | fall | rise             | fall | rise              | fall | rise              | fall |
| Settling time (ms) | 955.38          | 56.65 | 5.45             | 0.18 | 0.09             | 0.05 | 0.04              | 0.03 | 0.03              | 0.03 |

### 5.3.11 Effect of Fastlock Function on Settling Time

Table 5.15 shows the effect of fastlock function on the settling time of output signal rising and falling edges for 2<sup>nd</sup> order loop filters with respective loop bandwidths. According to the table, it was demonstrated that

- For loop bandwidth less than 50kHz (i.e. LF<50kHz), increment in fastlock timing will shorten the settling time and the effect became noticeable for larger loop bandwidth. Generally, the settling time would be faster when fastlock timing was around 20 $\mu$ s. Thereafter, the settling time would increase with further increments in fastlock timing.
- For loop bandwidth equal to, and larger than, 50kHz (i.e. LF  $\geq$ 50kHz), increment in fastlock timing would significantly lengthen the settling time.



| Fastlock<br>( $\mu$ s) | Settling time (ms) |       |                  |      |                  |      |                   |      |                   |      |      |
|------------------------|--------------------|-------|------------------|------|------------------|------|-------------------|------|-------------------|------|------|
|                        | #1<br>(LF 1kHz)    |       | #5<br>(LF 20kHz) |      | #2<br>(LF 50kHz) |      | #3<br>(LF 100kHz) |      | #4<br>(LF 200kHz) |      |      |
|                        | rise               | fall  | rise             | fall | rise             | fall | rise              | fall | rise              | fall |      |
| 0                      | 955.38             | 56.65 | 5.45             | 0.18 | 0.09             | 0.05 | 0.04              | 0.03 | 0.03              | 0.03 | 0.03 |
| 1                      | -                  | -     | -                | -    | 0.19             | 0.04 | 0.20              | 0.20 | -                 | -    | -    |
| 20                     | -                  | -     | 0.06             | 0.07 | -                | -    | -                 | -    | -                 | -    | -    |
| 163                    | 955.38             | 51.01 | 0.19             | 0.20 | 0.19             | 0.03 | 0.19              | 0.19 | 0.19              | 0.19 | 0.19 |

### 5.3.12 PC Program for PLL Setting (User Interface)

Figure 5.54 shows the user interface of PC program for PLL setting, as depicted in Chapter 4.6.

```

Fractional-N PLL Initialization Version 1.4
Cyrips Pte Ltd, 26 March 2008
All rights reserved

----- Initial Parameters -----

Frequency= 2399.950 MHz, Clock= 25.0 MHz, Detector= 25.0 MHz
Prescaler= 16, ABC_Counter= 9 bit, R_Counter= 4 bit
FN_FD_Counter= 9 bit, Moduli= 500(0x1F4)
MASH_Order= 3, Counter_Out= 3,
Charge_Pump_Current= 200uA, Fastlock= 20us
Baudrate= 500.0000 kbps

-----
[ Key in A,C,D,e,F,g,I,k,l,M,N,o,P,R,u,+,-,
Test,Help,Quit or frequency directly]
Frequency= 2500.05_

```

Figure 5.54 User interface for PLL setting

---

## CHAPTER 6

### CONCLUSION

A high frequency, robust, fast switching quad-modulus prescaler in a fully integrated, versatile, low noise and fast-locking fractional-N frequency synthesizer has been proposed and implemented with a 0.35 $\mu$ m CMOS technology.

The proposed frequency synthesizer consists of R-Counter, N-Counter, Fast-lock Timer and Fast-lock Control Switch, MASH, Interface, Mode Register, MUX\_Output, PFD, Charge Pump and Quad-modulus Prescaler. Interface will receive external PLL control commands and pass the data to respective blocks and R-Counter will divide down the input reference frequency. The PFD serves as a phase- and frequency-difference evaluator between divided reference frequency and divided LO frequency, and outputs UP/DN pulses. Then, the outputs are fed to Charge Pump which offers 6 different current settings. Fast-lock function is integrated to shorten the frequency locking time. The advantages of Charge Pump PLL are: the capture range is only restricted by VCO output frequency range, and no static phase error if mismatches and offsets are negligible. The dead-zone in PFD has been eliminated by implementation of delay cells. The Charge Pump current will pass through loop filter, and the DC voltage is used to control the VCO. The Loop filter is connected externally to eliminate the issues of process sensitivity, temperature variations and aging. Then, the VCO output frequency will be divided down by Prescaler, which offers 4 division ratios.

---

Prescaler block faced the most challenge in this synthesizer design because the 0.35 $\mu$ m CMOS technology used for this design had a Transit frequency ( $f_T$ ) of less than 50GHz, which restrained the maximum achievable operating frequency for multi-modulus divider. Hence, much work was needed in optimizing and compromising between the maximum operating frequency, power consumption, die size, and other properties. In the proposed quad-modulus prescaler design, CML topology was implemented in the construction of dividers to optimize the circuit's maximum operating frequency and minimize the switching noise contributed by hard-switching of MOSFETs in other topologies. Besides, analog logic gates and gate-embedded latches were used to meet the high-speed, high-frequency operation requirement. The total dynamic power consumption was controlled by allowing only three synchronous divider operating at highest frequency, with each having current biasing to control the total current consumption during switching. The subsequent asynchronous dividers had been optimized to minimize the overall power consumption since they are operating at a lower frequency. The overall architecture of the prescaler was designed in such a way that it can be easily deployed for other division ratio with minimal amendments required.

A MASH which offers 3<sup>rd</sup> and 4<sup>th</sup> order selection was designed to produce fractional output frequency. The generated pseudo-random number is added to the N-Counter register value, and set as the initial value for N-Counter. N-Counter will then divide down the Prescaler output frequency before feeding the signal to MASH and PFD, and generate modulus-selection signals for Prescaler. Mode Register will set the MASH order, frequency synthesizer output and charge pump current, and MUX\_Output will

select signal from R-Counter output, prescaler output, divider output or lock detector output to be transmitted out for testing purpose.

The proposed design had been analyzed, implemented and simulated at both circuit and system levels. The actual performances of the circuit were further verified via testing and measurements which were carried out after fabrication and packaging. The chip area of the design was  $853.65\mu\text{m} * 819.05\mu\text{m}$ . Table 6.1 summarizes the measured performances of the fractional-N frequency synthesizer. Unless otherwise stated, the measurements were carried out in the following conditions:  $V_{dd}= 3.3\text{V}$ ,  $\text{Temp.}= 25^{\circ}\text{C}$ , loop bandwidth= 20kHz (2<sup>nd</sup> order), MASH order= 3, operating frequency= 2450MHz.

Table 6.1 Summary table for fractional-N frequency synthesizer performance

| Parameter                     | Value   |         |         | Unit   |
|-------------------------------|---|---------|---------|--------|
|                               | Min   | Typ     | Max     |        |
| Crystal oscillating frequency | 25.0026   | 25.0029 | 25.0032 | MHz    |
| Operating frequency           | 2076.95   |         | 2574.50 | MHz    |
| Reference spurs               |   |         |         |        |
| @ 25MHz offset                |   | -71.38  |         | dBc    |
| Fractional spurs @ 2462.50MHz |   |         |         |        |
| @ 25MHz offset                |   | -60.61  |         | dBc    |
| @ 50MHz offset                |   | -61.26  |         | dBc    |
| @ 75MHz offset                |   | -64.00  |         | dBc    |
| Integer-N boundary spurs      | <i>- refer to Figure 5.47 and Figure 5.48 -</i> |         |         |        |
| Phase noise                   |   |         |         |        |
| @ 10kHz offset                |   | -65.84  |         | dBc/Hz |

|                 |        |        |
|-----------------|--------|--------|
| @ 20kHz offset  | -67.78 | dBc/Hz |
| @ 50kHz offset  | -78.24 | dBc/Hz |
| @ 200kHz offset | -91.75 | dBc/Hz |

Table 6.2 Performance comparison with a few reported frequency synthesizers

| Parameter                           | References  |           |           |        |             | Unit             |
|-------------------------------------|-------------|-----------|-----------|--------|-------------|------------------|
|                                     | S1M8837     | [45]      | [46]      | [47]   | This work   |                  |
| Technology                          | -           | 0.35      | 0.18      | 0.18   | 0.35        | $\mu\text{m}$    |
| VDD                                 | 2.7/4.0     | 3.0       | 1.8       | -      | 3.0/3.3     | V<br>(min/max)   |
| Area                                | -           | 4.200     | 1.500     | 2.700  | 0.699       | $\text{mm}^2$    |
| Prescaler modulus                   | 16/17/20/21 | 32/33     | -         | -      | 16/17/20/21 |                  |
| RF input frequency                  | 500/2500    | 2375/2500 | 1470/2500 | 3600   | 2077/2574   | MHz<br>(min/max) |
| Reference input frequency           | 45/520      | 1         | 26        | 50     | 25          | MHz<br>(min/max) |
| Bandwidth                           |             | 10        | 200       | 1000   | 20          | kHz              |
| Phase noise                         | -90         | < -110    | < -92     | -98    | < -92       | dBc/Hz           |
| Reference spur                      | -           | -110.0    | < -62.0   |        | < -71.5     | dBc              |
| Integer-boundary spur @ 1MHz offset | -           | -         | -66.00    | -45.00 | -46.13      | dBc              |
| Fractional spurious                 | < 80        | -         | -         | -      | < -64       | dBc              |

|                            |        |   |   |      |          |                      |
|----------------------------|--------|---|---|------|----------|----------------------|
| Channel switching time     | < 500  | - | - | 6600 | < 37     | $\mu$ s              |
| Charge pump output current | 50/800 | - | - | -    | 200/3200 | $\mu$ A<br>(min/max) |

Table 6.2 summarizes the performance comparison between the proposed design and a few reported fractional-N frequency synthesizer. The results show that with proper circuit optimizations and careful components sizing, the total chip area has been reduced while remaining competitive in terms of noise performance despite implemented with a 0.35 $\mu$ m technology. The implementation of Fast-lock function has shortened the channel switching time significantly. Besides, the utilization of decoder to select various combinations of current branches provides a wide selection of charge pump output current.

The significance of this research is to demonstrate the feasibility of implementing a 2.4GHz fractional-N frequency synthesizer for used in the 2450MHz band (and also support the 910MHz band operation) which offers technological robustness, versatility, fast locking capability, low noise contribution, superior integration capacity and multi-modulus flexibility using a low cost 0.35 $\mu$ m CMOS technology. The counters utilize complete synchronous logic design which offers the flexibility for bits expansion. Besides, the counters were constructed with standard digital cells for ease of deployment to other process technology. And the locking range of the proposed design is only limited by the VCO locking range. In a nutshell, this multi-mode design can be easily implemented in multiple applications with the flexibility that it offers.

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Future works which may be carried out include expanding the bit number of FN and FD registers to 23 bits to reduce the spurious levels of various spurs, and implementing a programmable digital loop filter.

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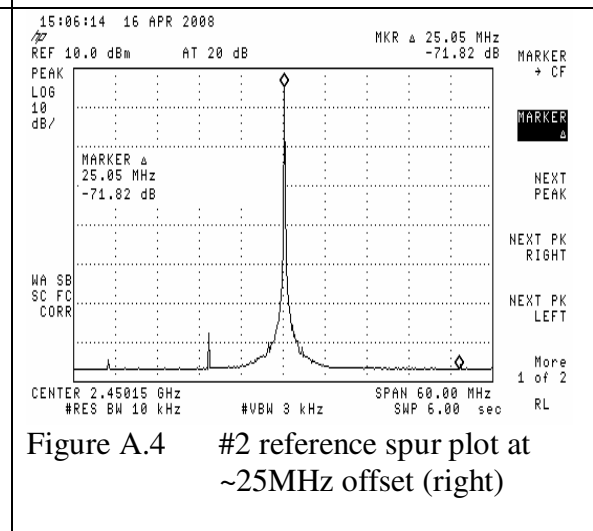
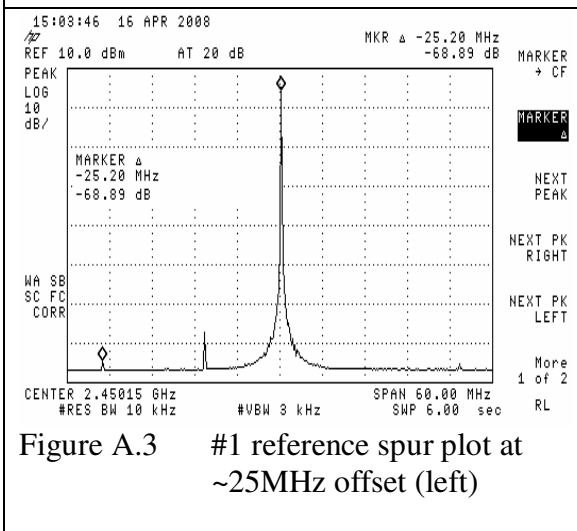
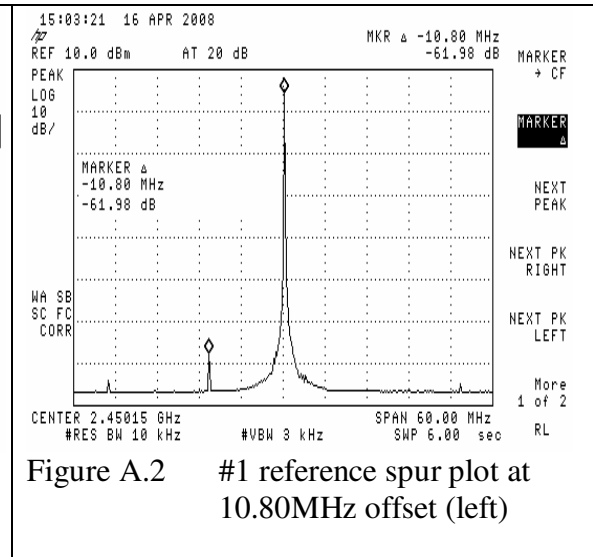
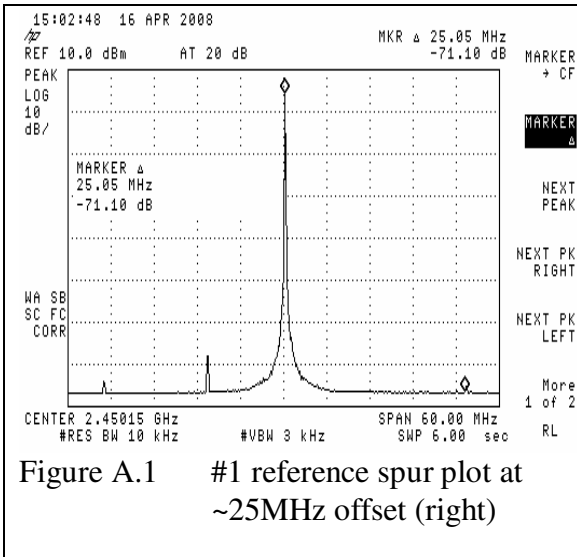
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# APPENDICES

## Appendix A Reference Spur Plots

Unless otherwise stated, the settings for the measurements are as follow:

- RBW= 10kHz; VBW= 3kHz; Span= 60MHz; Sweep= 6s
- MASH= 3
- Moduli= 500



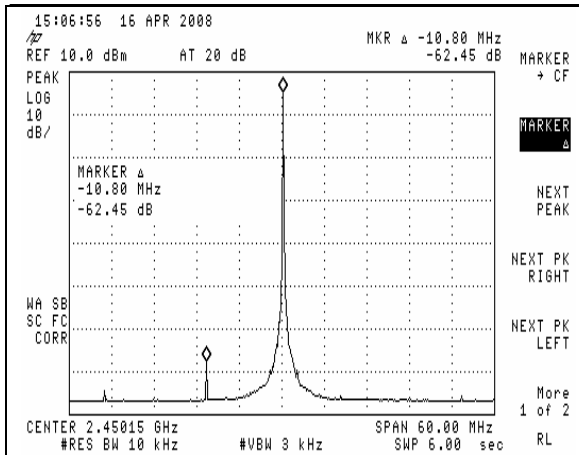


Figure A.5 #2 reference spur plot at 10.80MHz offset (left)

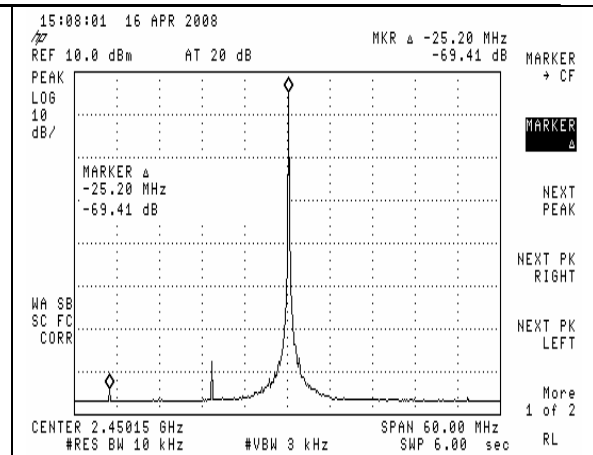


Figure A.6 #2 reference spur plot at ~25MHz offset (left)

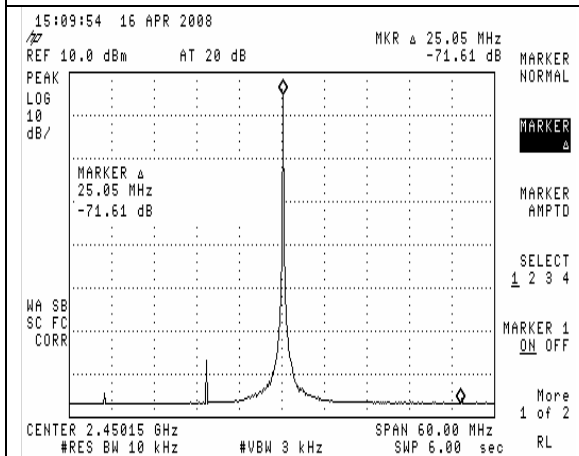


Figure A.7 #3 reference spur plot at ~25MHz offset (right)

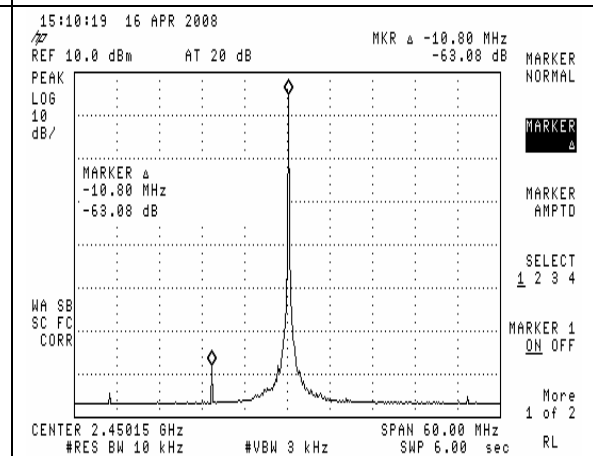


Figure A.8 #3 reference spur plot at 10.80MHz offset (left)

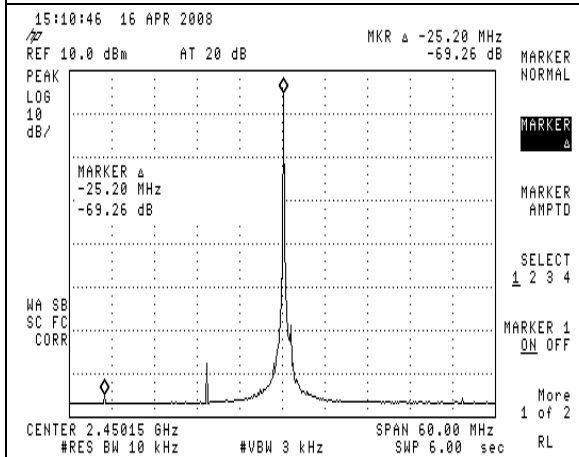


Figure A.9 #3 reference spur plot at ~25MHz offset (left)

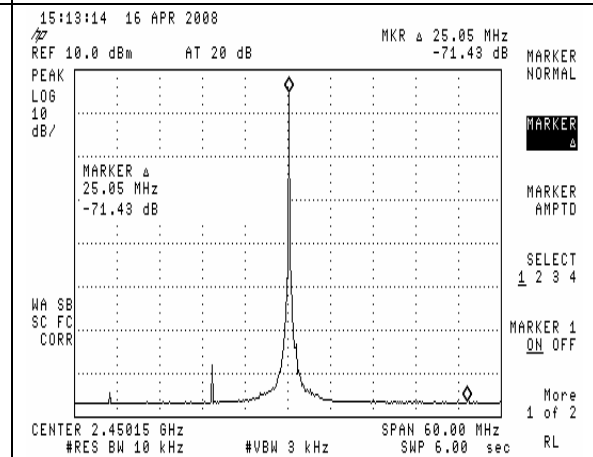
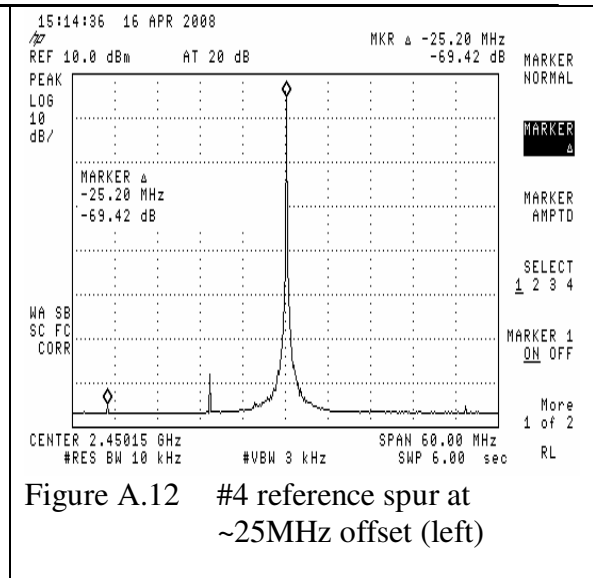
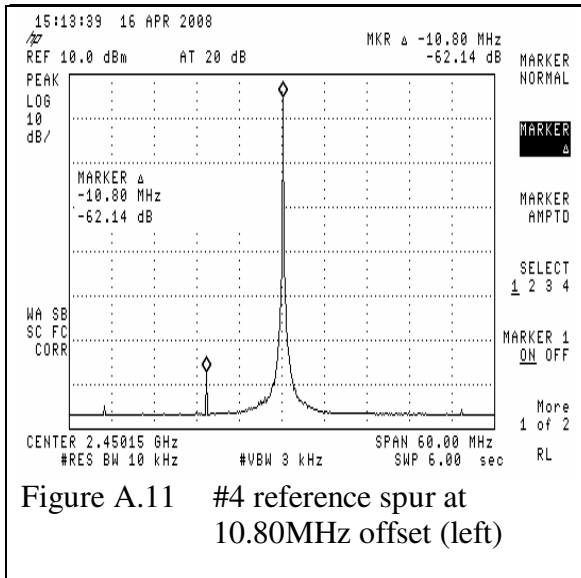


Figure A.10 #4 reference spur plot at ~25MHz offset (right)





## Appendix B Fractional Spur Plots

Sample #5 (with loop filter of 20kHz) was used for fractional spurs measurements. Unless otherwise stated, the settings for the measurements are as follow:

- Reference= 10dBm; Attenuation= 20dB
- RBW= 1MHz; VBW= 300kHz; Span= 150MHz; Sweep= 5s
- MASH= 3; Moduli= 500

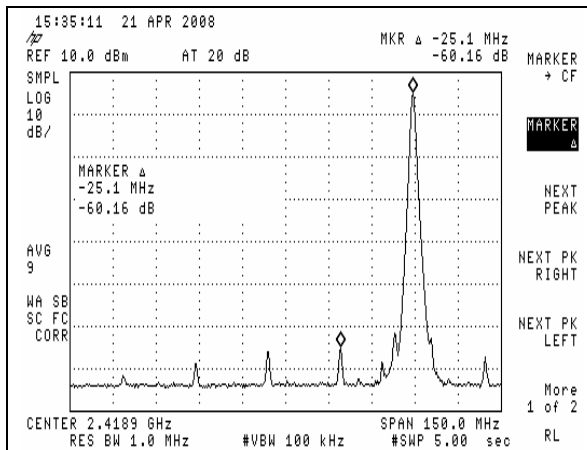


Figure B.1 Fractional spur with carrier frequency of 2462.50MHz and offset at 25MHz

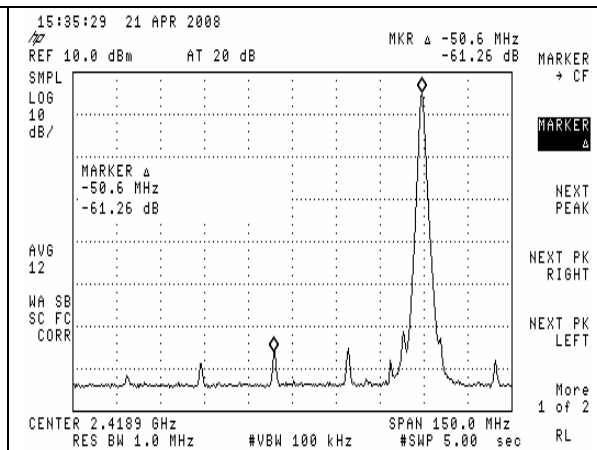


Figure B.2 Fractional spur with carrier frequency of 2462.50MHz and offset at 50MHz

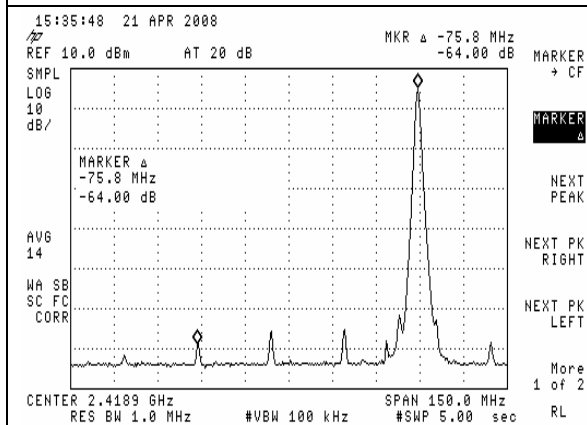


Figure B.3 Fractional spur with carrier frequency of 2462.50MHz and offset at 75MHz

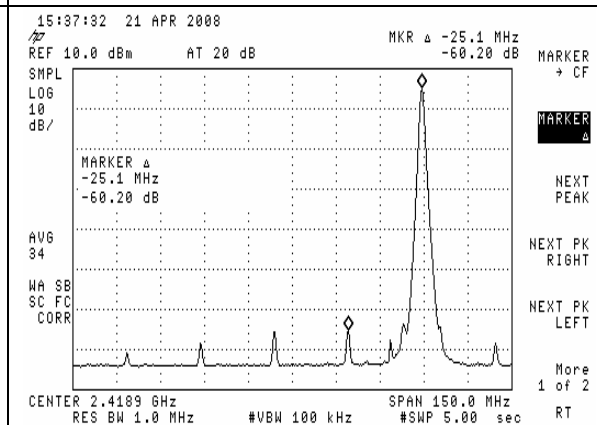
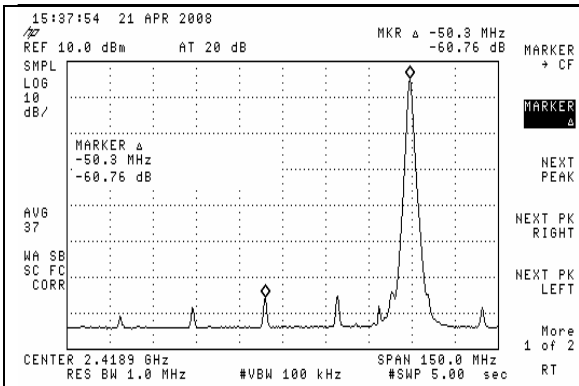
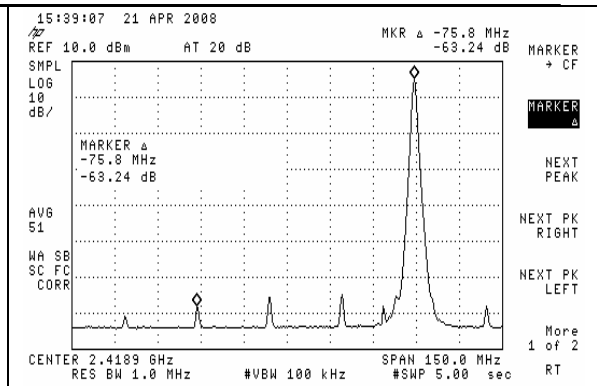


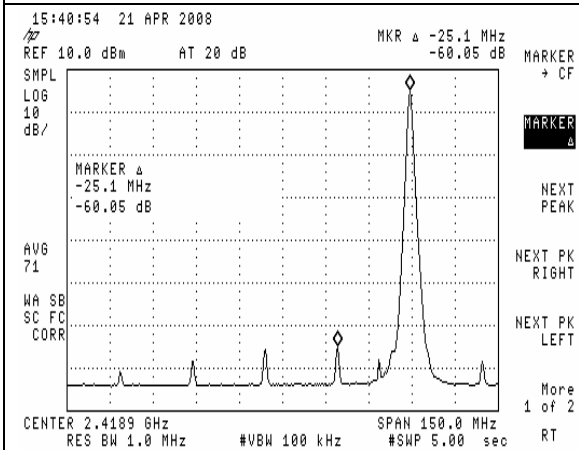
Figure B.4 Fractional spur with carrier frequency of 2462.55MHz and offset at 25MHz



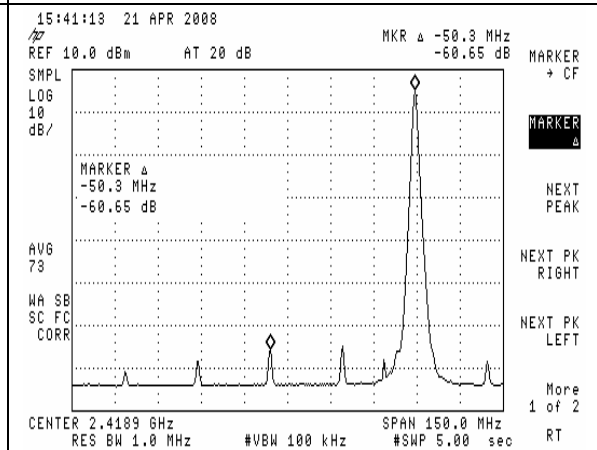
**Figure B.5** Fractional spur with carrier frequency of 2462.55 MHz and offset at 50 MHz



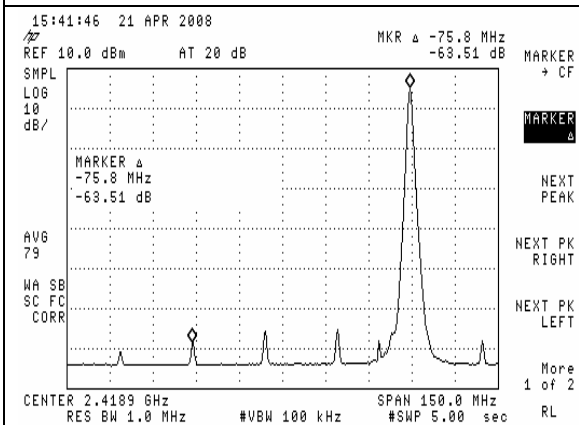
**Figure B.6** Fractional spur with carrier frequency of 2462.55 MHz and offset at 75 MHz



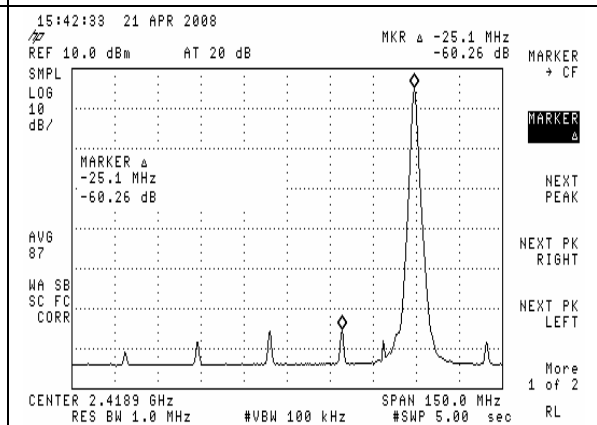
**Figure B.7** Fractional spur with carrier frequency of 2462.60 MHz and offset at 25 MHz



**Figure B.8** Fractional spur with carrier frequency of 2462.60 MHz and offset at 50 MHz



**Figure B.9** Fractional spur with carrier frequency of 2462.60 MHz and offset at 75 MHz



**Figure B.10** Fractional spur with carrier frequency of 2462.65 MHz and offset at 25 MHz

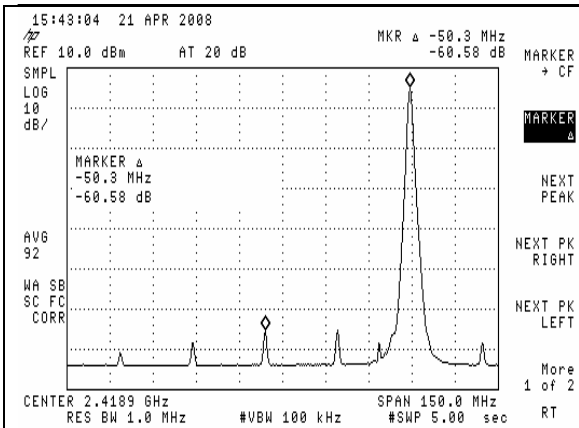


Figure B.11 Fractional spur with carrier frequency of 2462.65MHz and offset at 50MHz

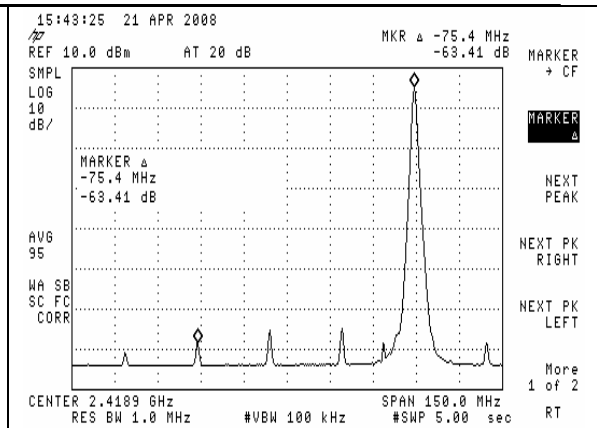


Figure B.12 Fractional spur with carrier frequency of 2462.65MHz and offset at 75MHz

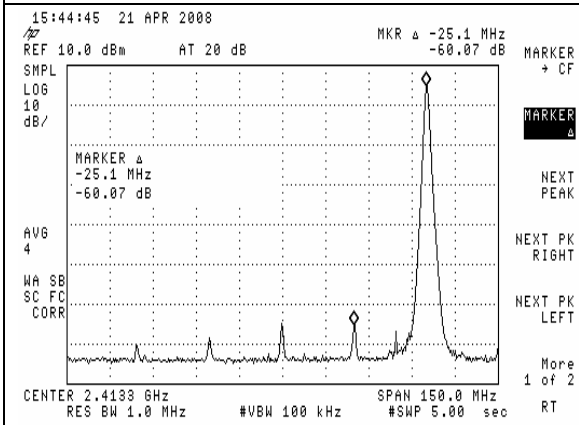


Figure B.13 Fractional spur with carrier frequency of 2462.70MHz and offset at 25MHz

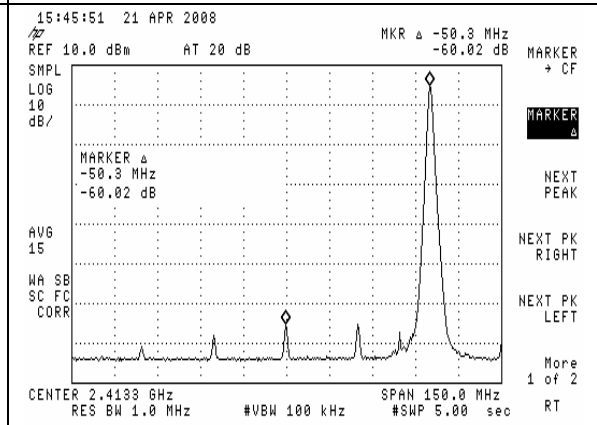


Figure B.14 Fractional spur with carrier frequency of 2462.70MHz and offset at 50MHz

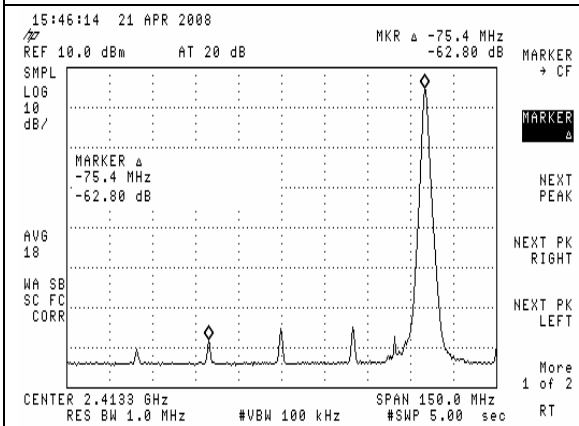


Figure B.15 Fractional spur with carrier frequency of 2462.70MHz and offset at 75MHz

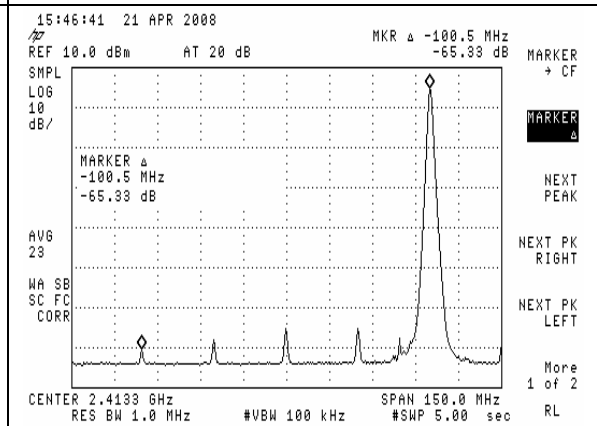


Figure B.16 Fractional spur with carrier frequency of 2462.70MHz and offset at 100MHz

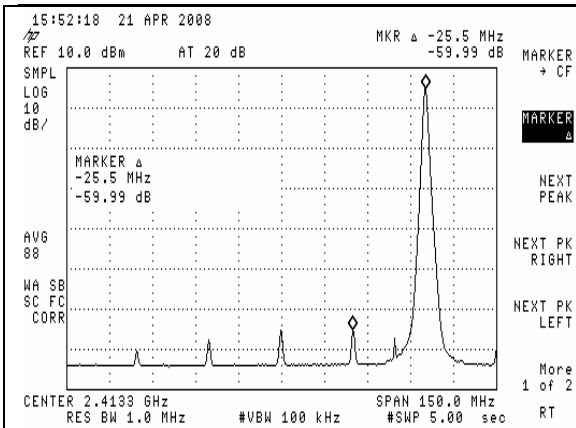


Figure B.17 Fractional spur with carrier frequency of 2462.75MHz and offset at 25MHz

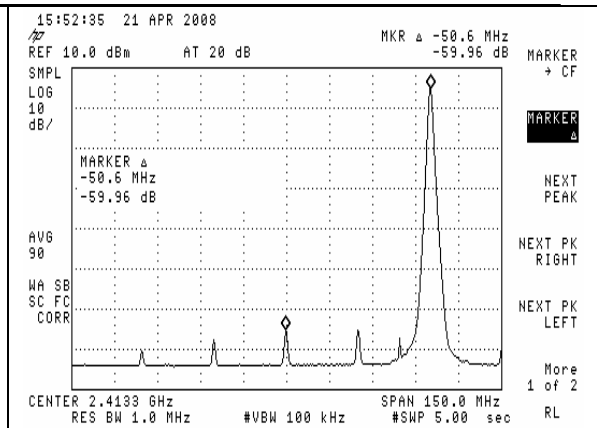


Figure B.18 Fractional spur with carrier frequency of 2462.75MHz and offset at 50MHz

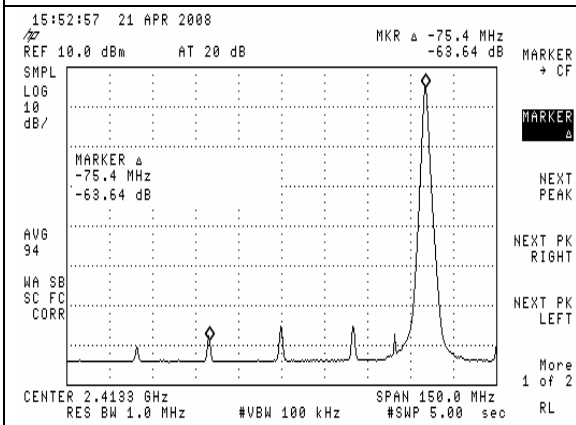


Figure B.19 Fractional spur with carrier frequency of 2462.75MHz and offset at 75MHz

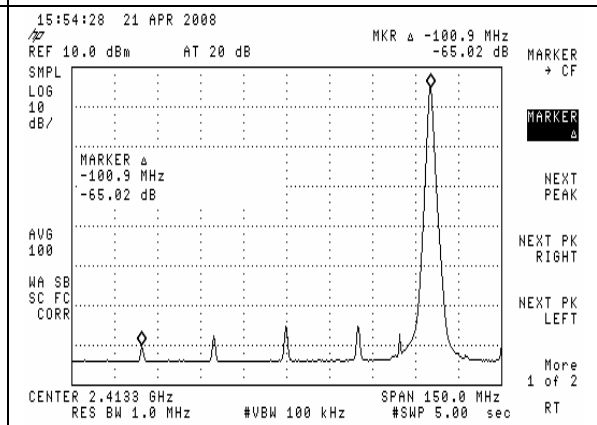


Figure B.20 Fractional spur with carrier frequency of 2462.75MHz and offset at 100MHz

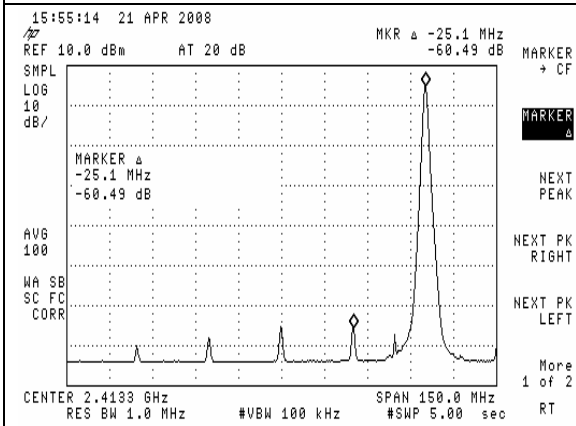


Figure B.21 Fractional spur with carrier frequency of 2462.80MHz and offset at 25MHz

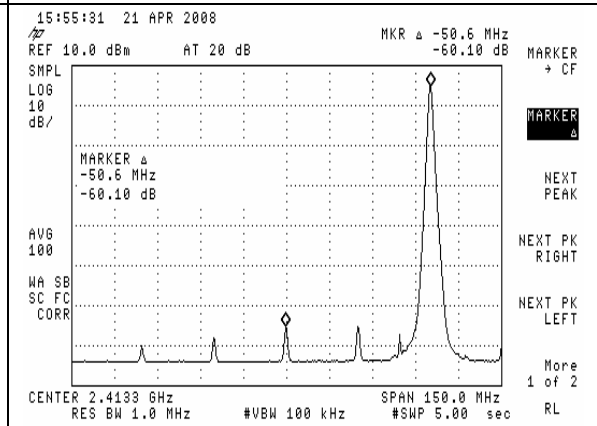
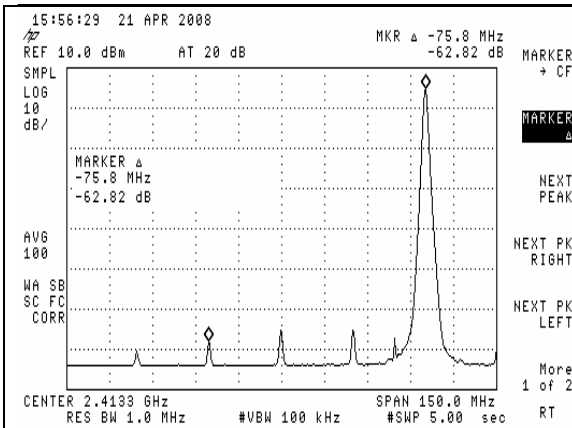
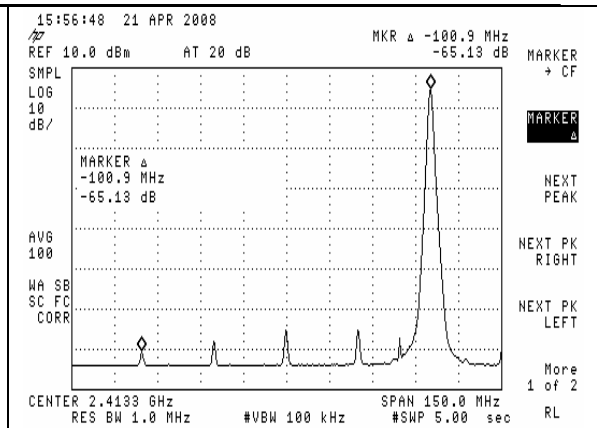


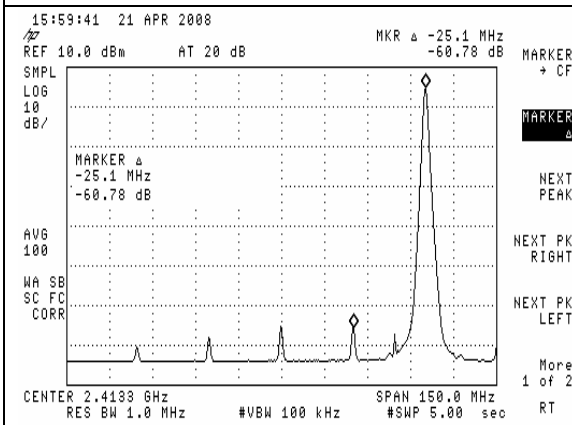
Figure B.22 Fractional spur with carrier frequency of 2462.80MHz and offset at 50MHz



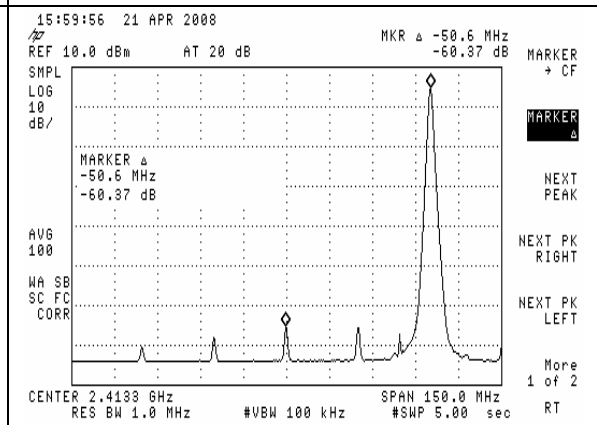
**Figure B.23** Fractional spur with carrier frequency of 2462.80MHz and offset at 75MHz



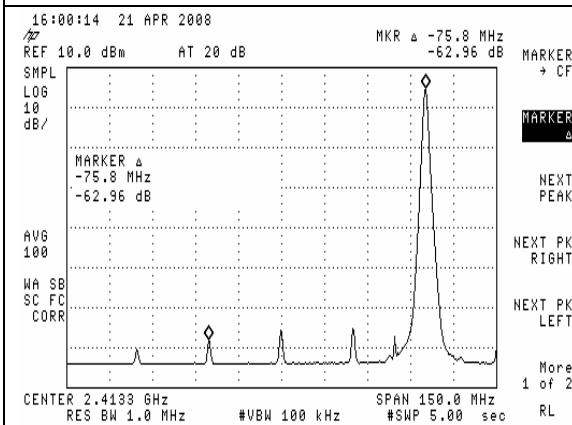
**Figure B.24** Fractional spur with carrier frequency of 2462.80MHz and offset at 100MHz



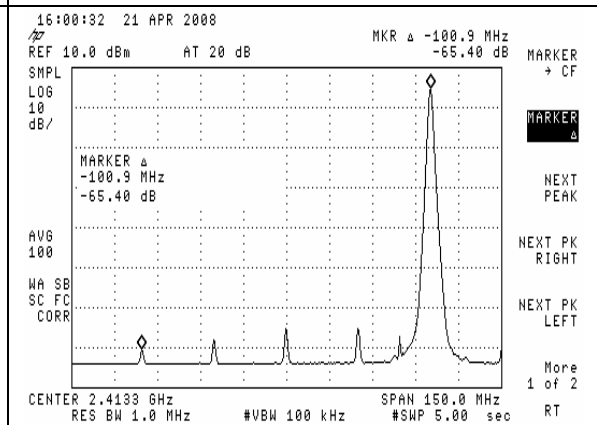
**Figure B.25** Fractional spur with carrier frequency of 2462.85MHz and offset at 25MHz



**Figure B.26** Fractional spur with carrier frequency of 2462.85MHz and offset at 50MHz



**Figure B.27** Fractional spur with carrier frequency of 2462.85MHz and offset at 75MHz



**Figure B.28** Fractional spur with carrier frequency of 2462.85MHz and offset at 100MHz

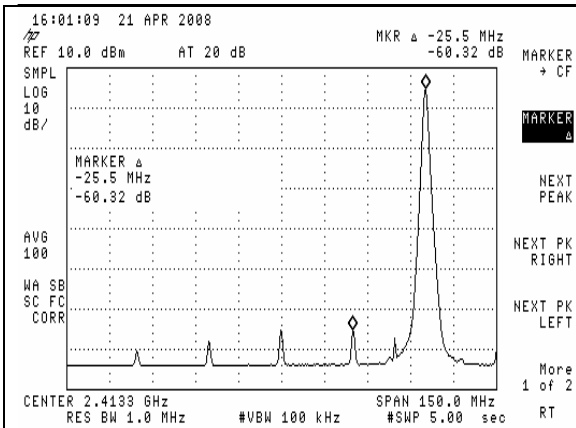


Figure B.29 Fractional spur with carrier frequency of 2462.90MHz and offset at 25MHz

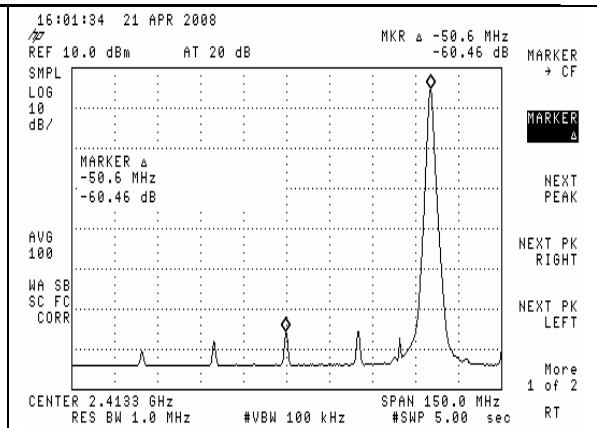


Figure B.30 Fractional spur with carrier frequency of 2462.90MHz and offset at 50MHz

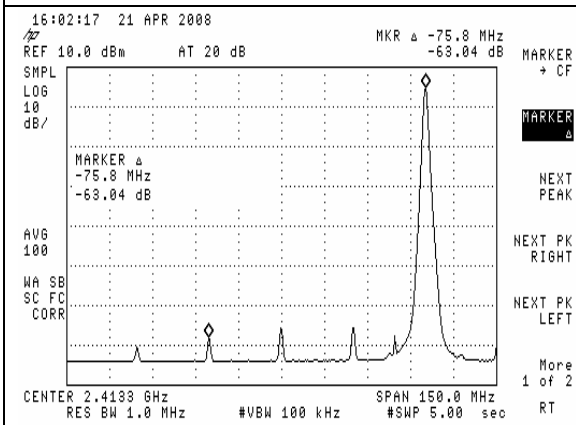


Figure B.31 Fractional spur with carrier frequency of 2462.90MHz and offset at 75MHz

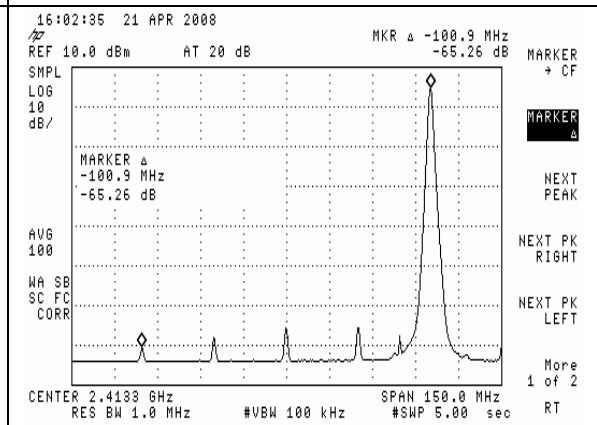


Figure B.32 Fractional spur with carrier frequency of 2462.90MHz and offset at 100MHz

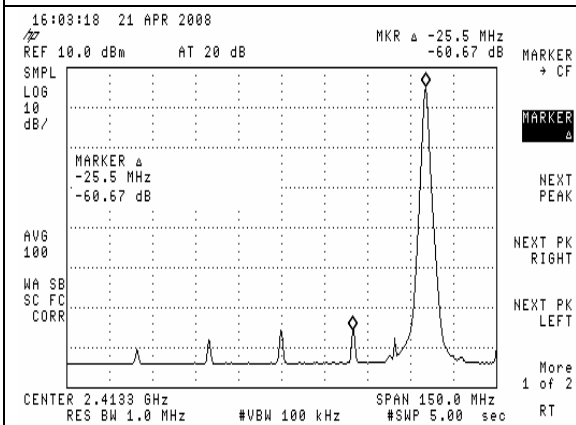


Figure B.33 Fractional spur with carrier frequency of 2462.95MHz and offset at 25MHz

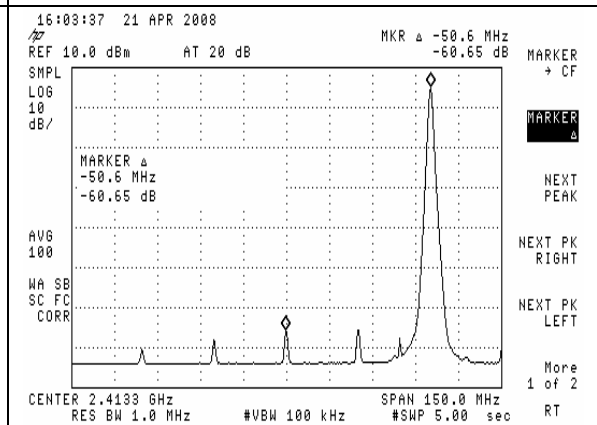


Figure B.34 Fractional spur with carrier frequency of 2462.95MHz and offset at 50MHz

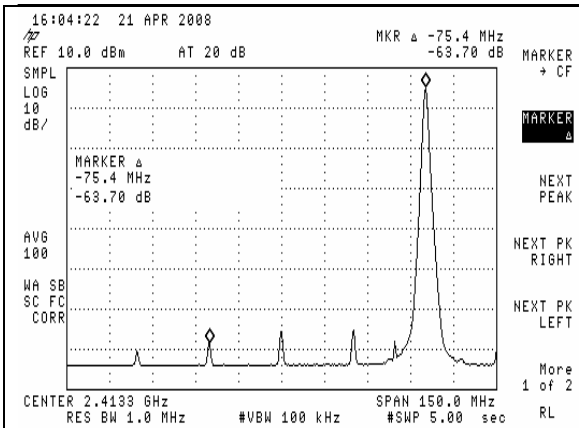


Figure B.35 Fractional spur with carrier frequency of 2462.95MHz and offset at 75MHz

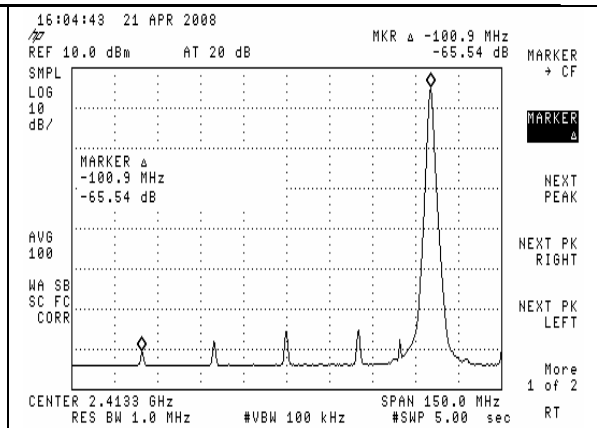


Figure B.36 Fractional spur with carrier frequency of 2462.95MHz and offset at 100MHz

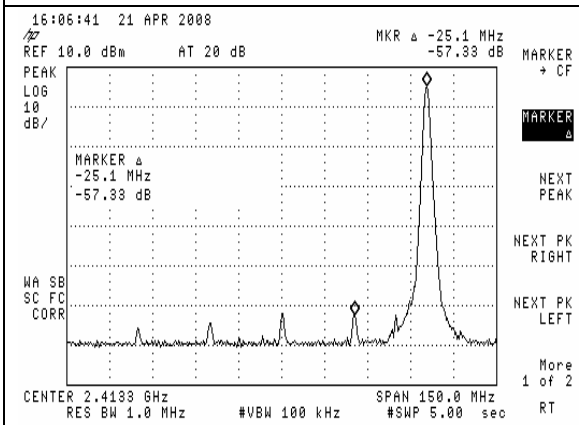


Figure B.37 Fractional spur with carrier frequency of 2463.00MHz and offset at 25MHz

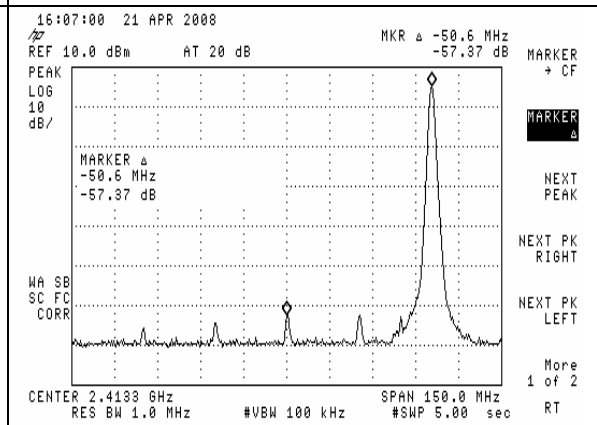


Figure B.38 Fractional spur with carrier frequency of 2463.00MHz and offset at 50MHz

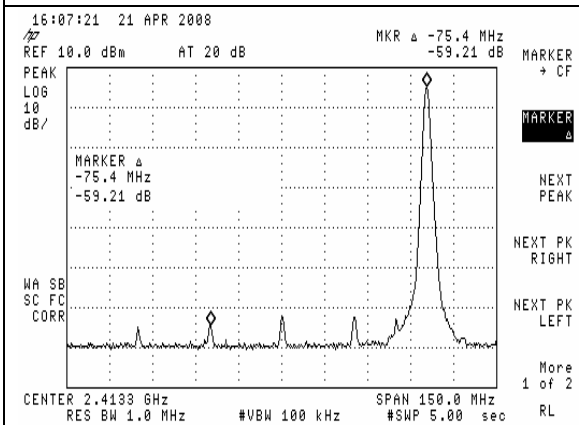


Figure B.39 Fractional spur with carrier frequency of 2463.00MHz and offset at 75MHz

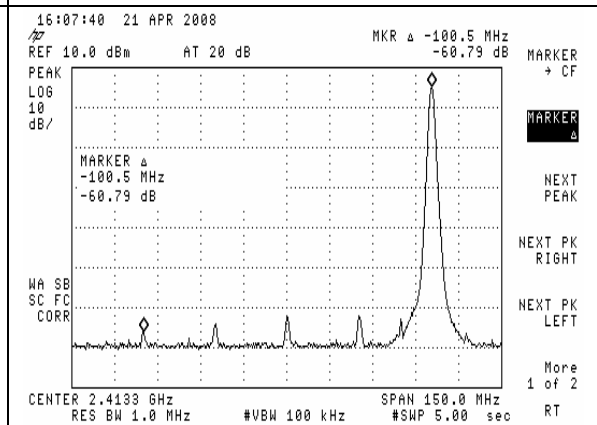


Figure B.40 Fractional spur with carrier frequency of 2463.00MHz and offset at 100MHz



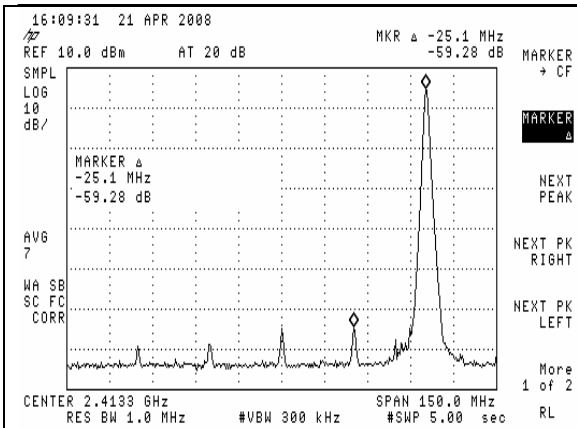


Figure B.41 Fractional spur with carrier frequency of 2463.05MHz and offset at 25MHz

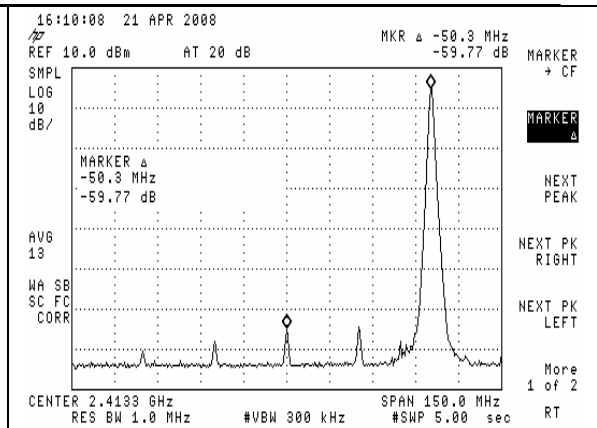


Figure B.42 Fractional spur with carrier frequency of 2463.05MHz and offset at 50MHz

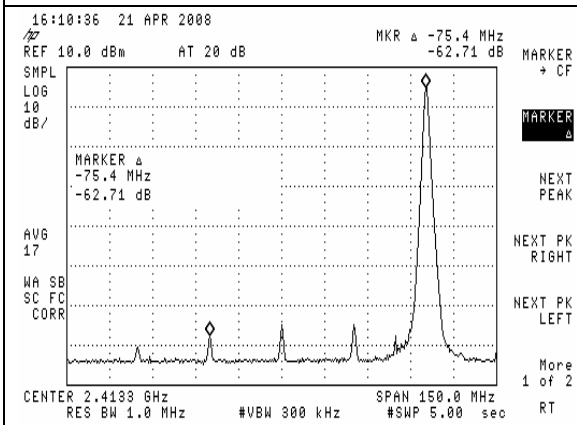


Figure B.43 Fractional spur with carrier frequency of 2463.05MHz and offset at 75MHz

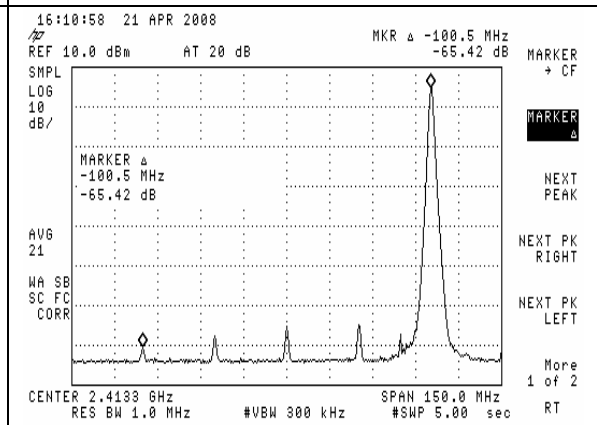


Figure B.44 Fractional spur with carrier frequency of 2463.05MHz and offset at 100MHz

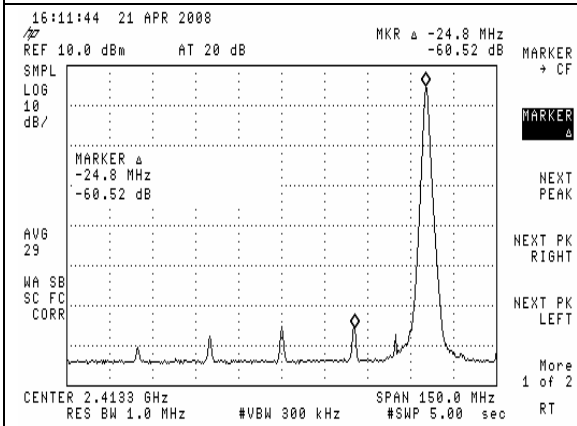


Figure B.45 Fractional spur with carrier frequency of 2463.10MHz and offset at 25MHz

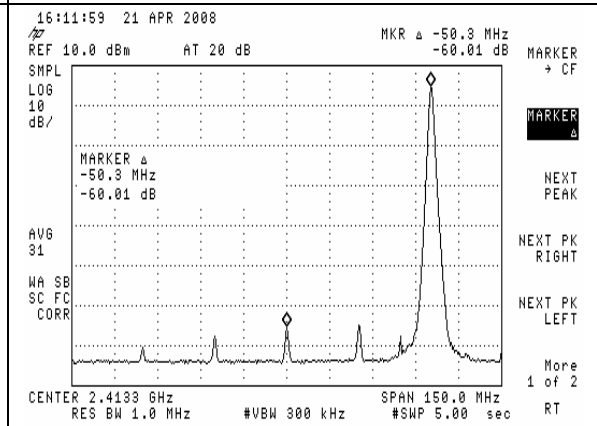


Figure B.46 Fractional spur with carrier frequency of 2463.10MHz and offset at 50MHz

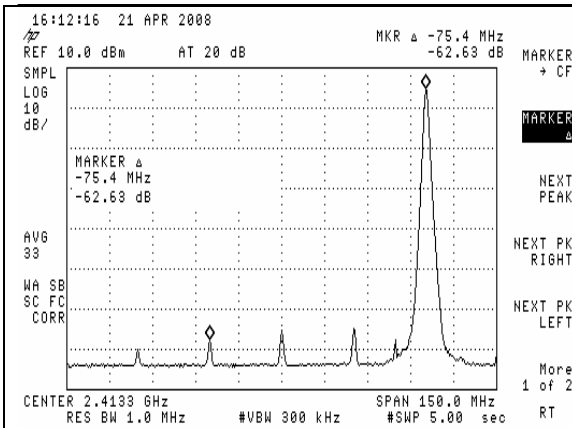


Figure B.47 Fractional spur with carrier frequency of 2463.10MHz and offset at 75MHz

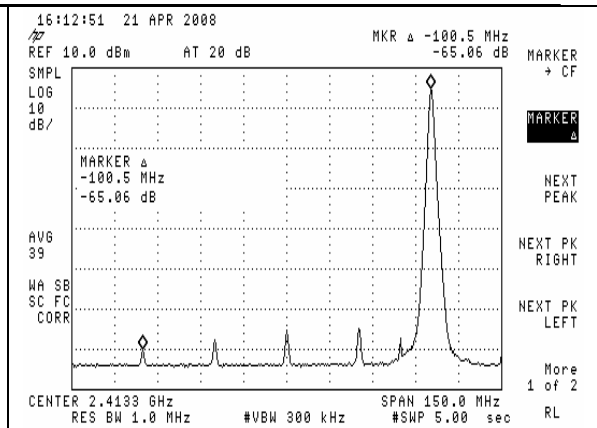


Figure B.48 Fractional spur with carrier frequency of 2463.10MHz and offset at 100MHz

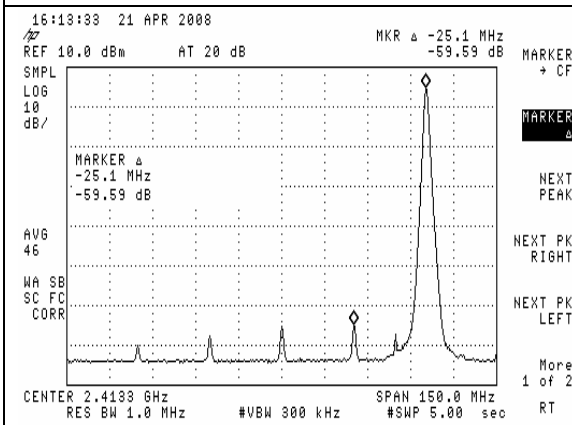


Figure B.49 Fractional spur with carrier frequency of 2463.15MHz and offset at 25MHz

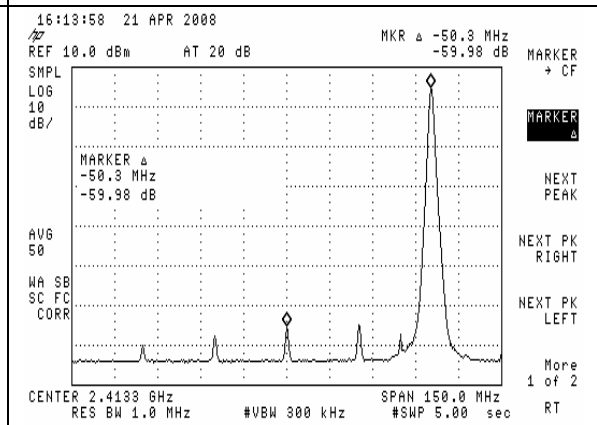


Figure B.50 Fractional spur with carrier frequency of 2463.15MHz and offset at 50MHz

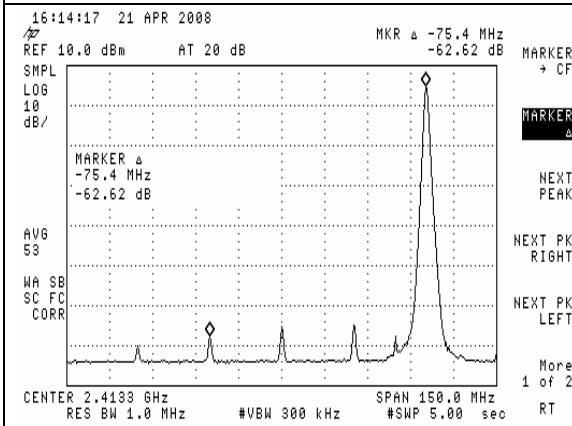


Figure B.51 Fractional spur with carrier frequency of 2463.15MHz and offset at 75MHz

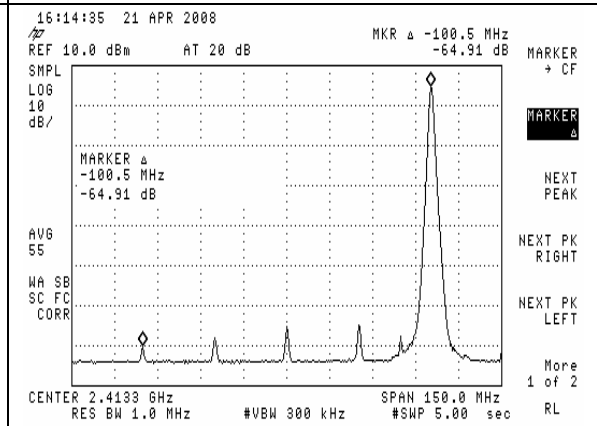
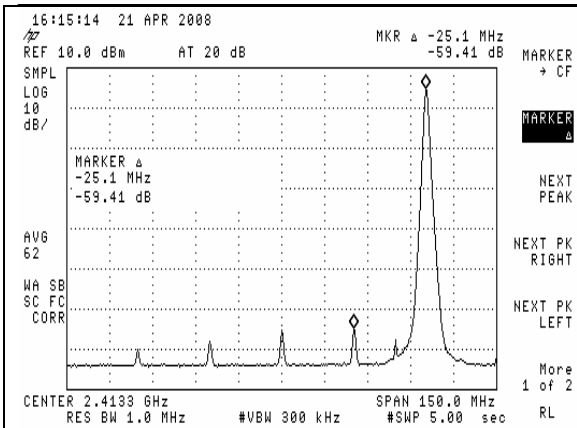
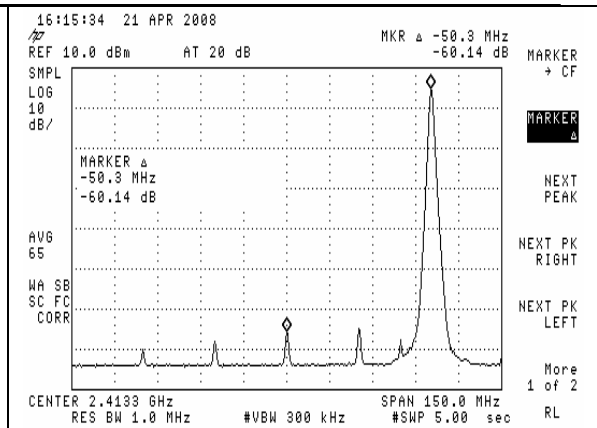


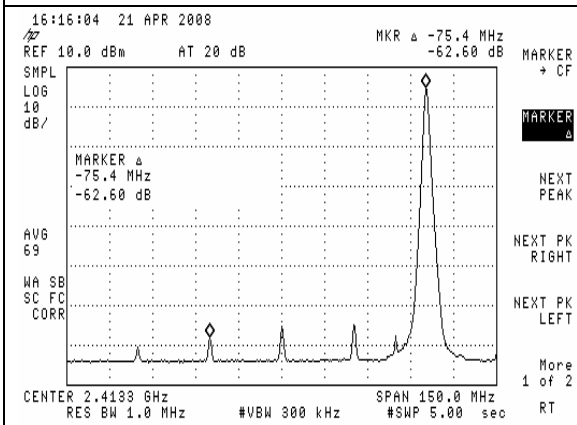
Figure B.52 Fractional spur with carrier frequency of 2463.15MHz and offset at 100MHz



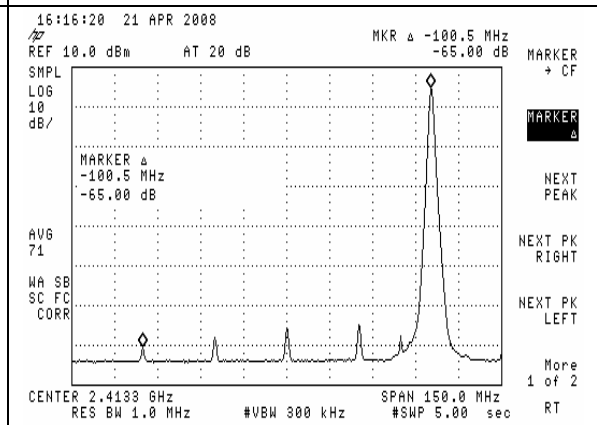
**Figure B.53** Fractional spur with carrier frequency of 2463.20MHz and offset at 25MHz



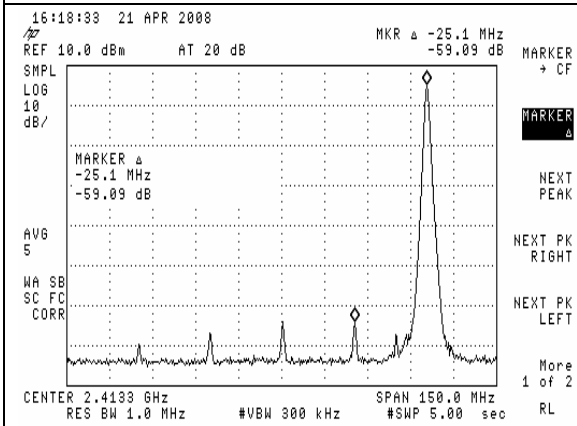
**Figure B.54** Fractional spur with carrier frequency of 2463.20MHz and offset at 50MHz



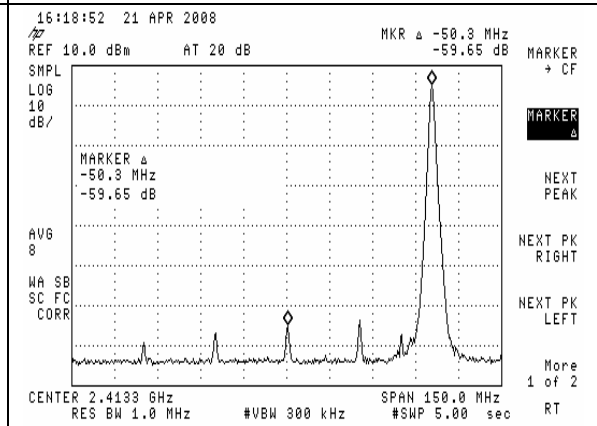
**Figure B.55** Fractional spur with carrier frequency of 2463.20MHz and offset at 75MHz



**Figure B.56** Fractional spur with carrier frequency of 2463.20MHz and offset at 100MHz



**Figure B.57** Fractional spur with carrier frequency of 2463.25MHz and offset at 25MHz



**Figure B.58** Fractional spur with carrier frequency of 2463.25MHz and offset at 50MHz

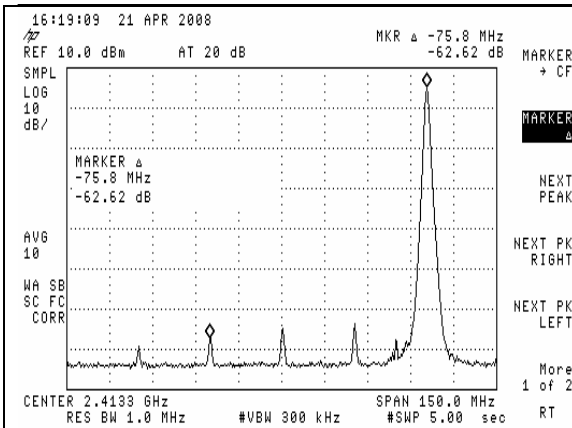


Figure B.59 Fractional spur with carrier frequency of 2463.25MHz and offset at 75MHz

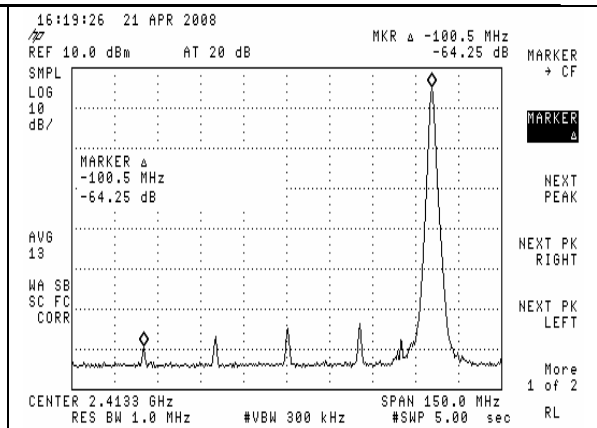


Figure B.60 Fractional spur with carrier frequency of 2463.25MHz and offset at 100MHz

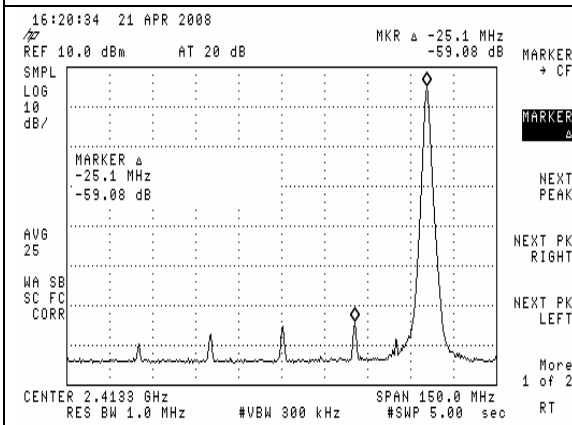


Figure B.61 Fractional spur with carrier frequency of 2463.30MHz and offset at 25MHz

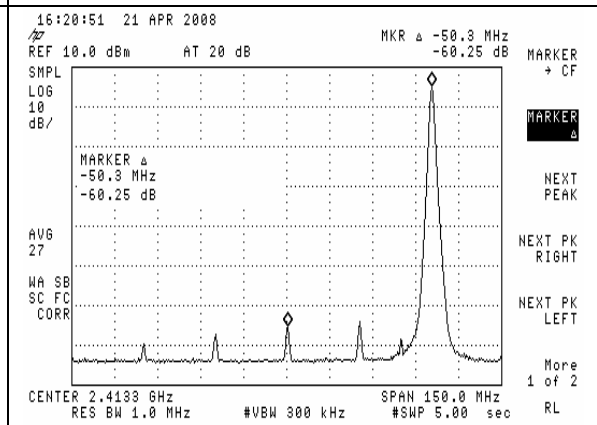


Figure B.62 Fractional spur with carrier frequency of 2463.30MHz and offset at 50MHz

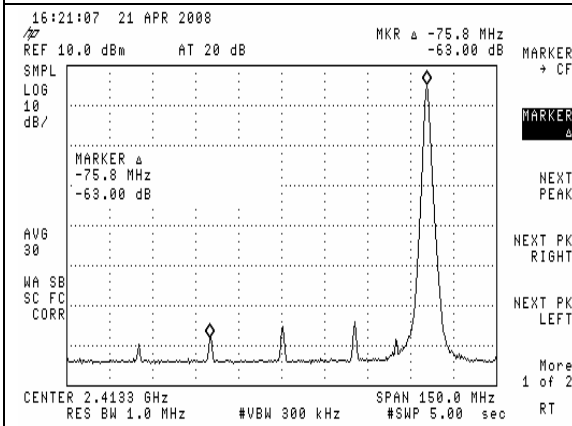


Figure B.63 Fractional spur with carrier frequency of 2463.30MHz and offset at 75MHz

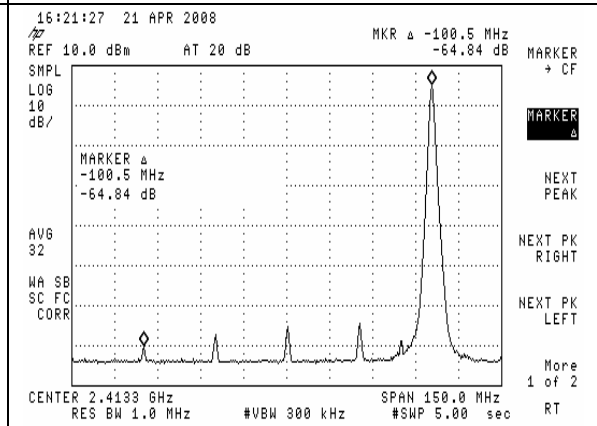


Figure B.64 Fractional spur with carrier frequency of 2463.30MHz and offset at 100MHz

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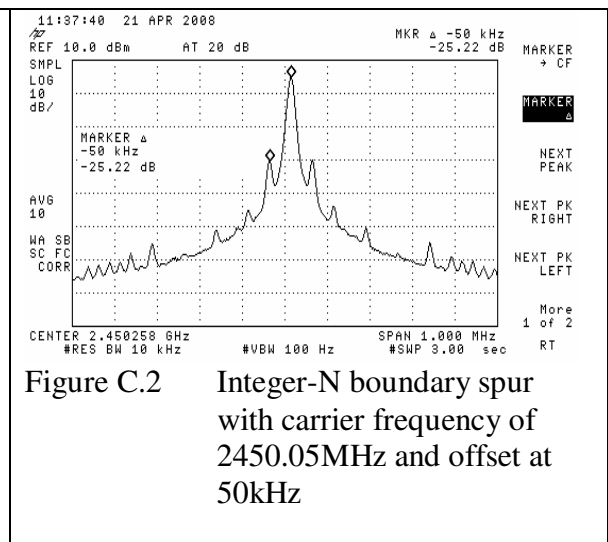
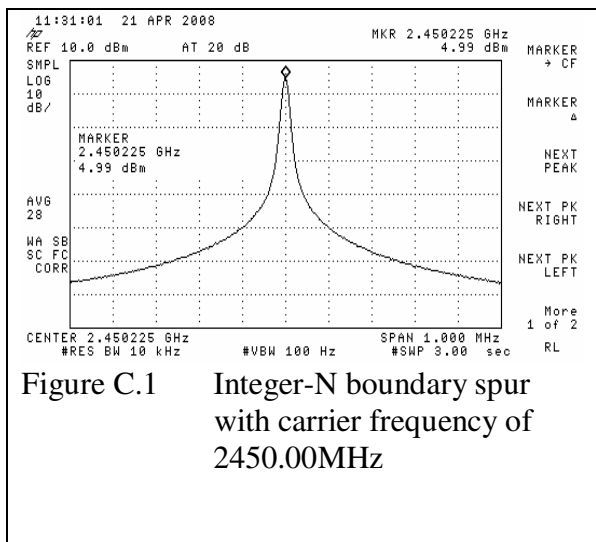
## Appendix C Integer-N Boundary Spurs

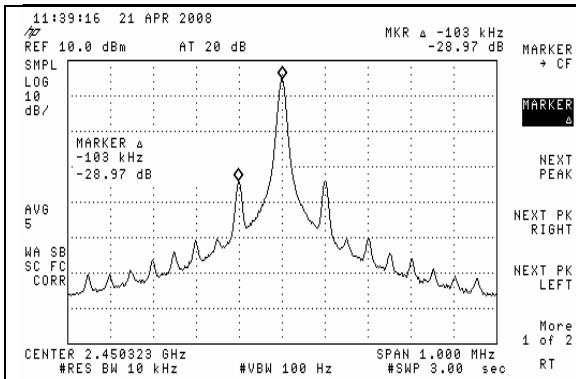
Sample #5 (with loop filter of 20kHz) was used for integer-N boundary spurs measurements. Unless otherwise stated, the settings for the measurements are as follow:

- i) at carrier frequency= 2450.05MHz~2451.50MHz
  - $P_{2450M}$ = 4.99dBm
  - Reference= 10dBm; Attenuation= 20dB
  - RBW= 10kHz; VBW= 100Hz; Span= 1MHz; Sweep= 3s
  - MASH=3; Moduli= 500; FN= 20
- ii) at carrier frequency= 2451.35MHz~2451.85MHz
  - $P_{2450M}$ = 4.99dBm
  - Reference= 10dBm; Attenuation= 20dB
  - RBW= 10kHz; VBW= 100Hz; Span= 3MHz; Sweep= 1s
  - MASH= 3; Moduli= 500; FN= 20

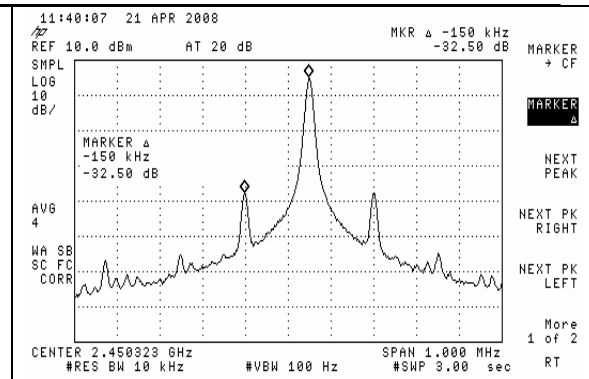
| Carrier frequency (MHz) | Spurious level at 2450MHz (dBc) | Carrier frequency (MHz) | Spurious level at 2450MHz (dBc) |
|-------------------------|---------------------------------|-------------------------|---------------------------------|
| 2450.00                 | +4.99                           | 2450.95                 | -53.44                          |
| 2450.05                 | -25.22                          | 2451.00                 | -46.13                          |
| 2450.10                 | -28.97                          | 2451.05                 | -55.26                          |
| 2450.15                 | -32.50                          | 2451.10                 | -55.35                          |
| 2450.20                 | -32.10                          | 2451.15                 | -53.52                          |
| 2450.25                 | -35.17                          | 2451.20                 | -51.84                          |

| Carrier frequency (MHz) | Spurious level at 2450MHz (dBc) | Carrier frequency (MHz) | Spurious level at 2450MHz (dBc) |
|-------------------------|---------------------------------|-------------------------|---------------------------------|
| 2450.30                 | -38.41                          | 2451.25                 | -50.13                          |
| 2450.35                 | -39.69                          | 2451.30                 | -59.32                          |
| 2450.40                 | -40.28                          | 2451.35                 | -60.59                          |
| 2450.45                 | -42.24                          | 2451.40                 | -53.37                          |
| 2450.50                 | -45.53                          | 2451.45                 | -60.21                          |
| 2450.55                 | -47.01                          | 2451.50                 | -58.87                          |
| 2450.60                 | -47.57                          | 2451.55                 | -60.49                          |
| 2450.65                 | -49.61                          | 2451.60                 | -56.23                          |
| 2450.70                 | -48.83                          | 2451.65                 | -60.73                          |
| 2450.75                 | -47.98                          | 2451.70                 | -63.30                          |
| 2450.80                 | -46.27                          | 2451.75                 | -59.23                          |
| 2450.85                 | -51.37                          | 2451.80                 | -63.01                          |
| 2450.90                 | -52.42                          | 2451.85                 | -63.98                          |

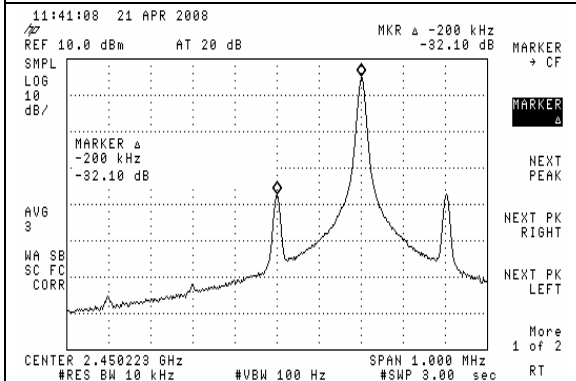




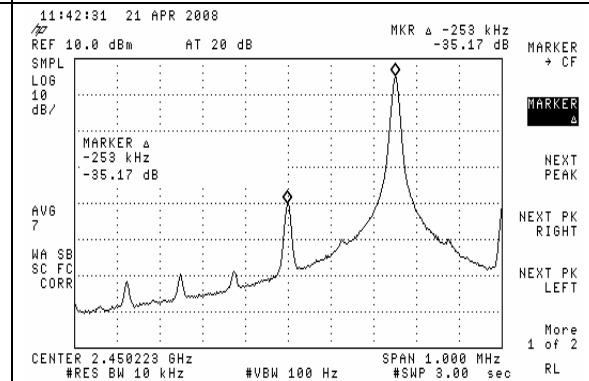
**Figure C.3** Integer-N boundary spur with carrier frequency of 2450.10MHz and offset at 100kHz



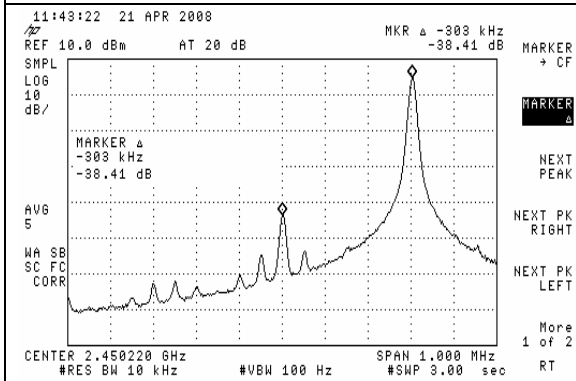
**Figure C.4** Integer-N boundary spur with carrier frequency of 2450.15MHz and offset at 150kHz



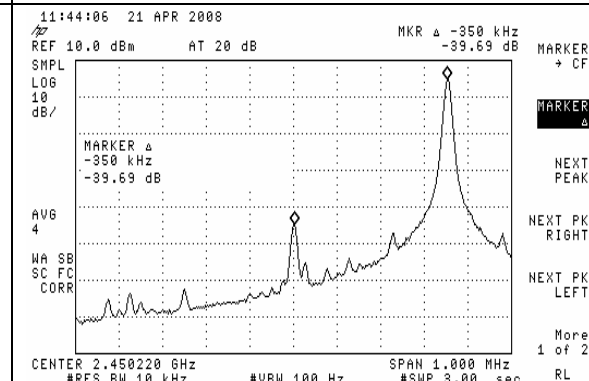
**Figure C.5** Integer-N boundary spur with carrier frequency of 2450.20MHz and offset at 200kHz



**Figure C.6** Integer-N boundary spur with carrier frequency of 2450.25MHz and offset at 250kHz



**Figure C.7** Integer-N boundary spur with carrier frequency of 2450.30MHz and offset at 300kHz



**Figure C.8** Integer-N boundary spur with carrier frequency of 2450.35MHz and offset at 350kHz

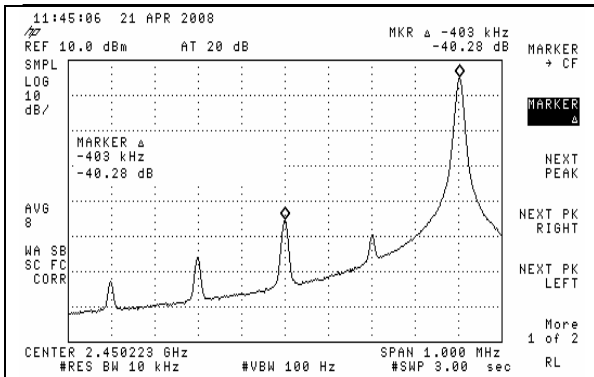


Figure C.9 Integer-N boundary spur with carrier frequency of 2450.40MHz and offset at 400kHz

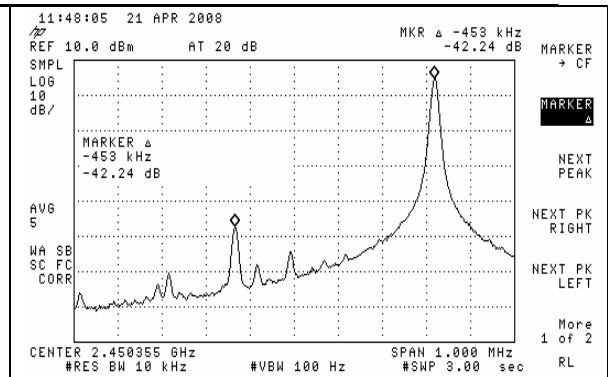


Figure C.10 Integer-N boundary spur with carrier frequency of 2450.45MHz and offset at 450kHz

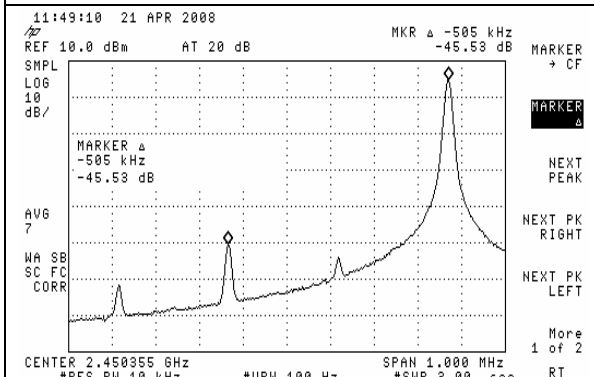


Figure C.11 Integer-N boundary spur with carrier frequency of 2450.50MHz and offset at 500kHz

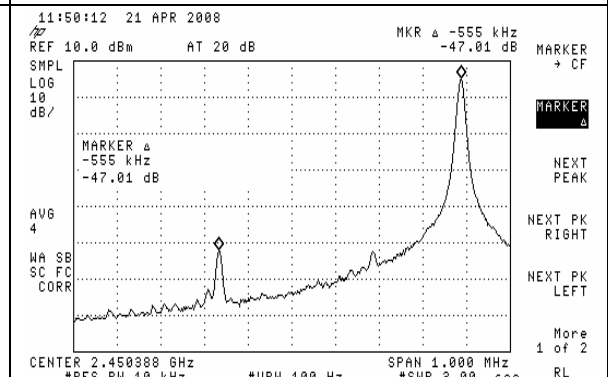


Figure C.12 Integer-N boundary spur with carrier frequency of 2450.55MHz and offset at 550kHz

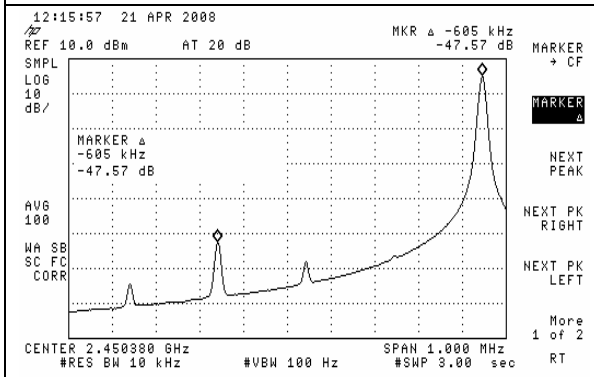


Figure C.13 Integer-N boundary spur with carrier frequency of 2450.60MHz and offset at 600kHz

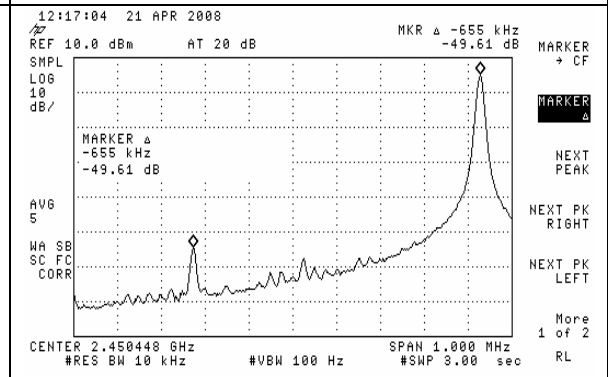


Figure C.14 Integer-N boundary spur with carrier frequency of 2450.65MHz and offset at 650kHz



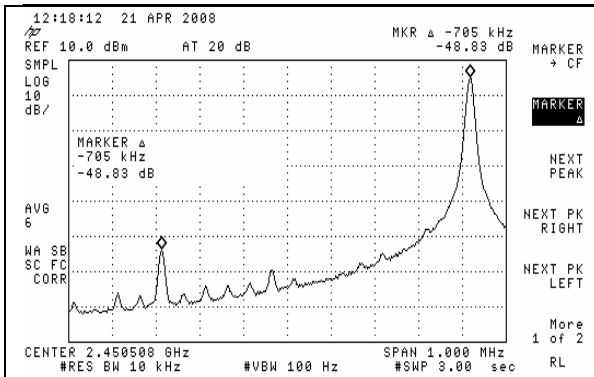


Figure C.15 Integer-N boundary spur with carrier frequency of 2450.70MHz and offset at 700kHz

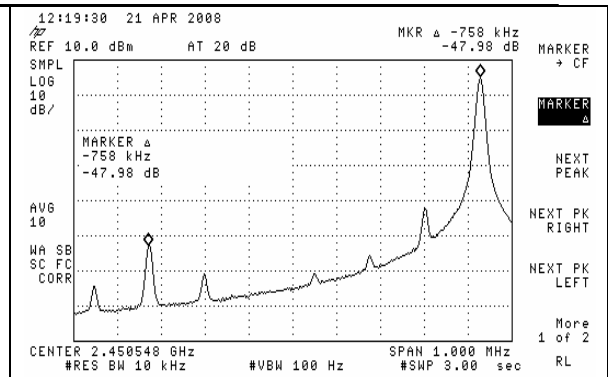


Figure C.16 Integer-N boundary spur with carrier frequency of 2450.75MHz and offset at 750kHz

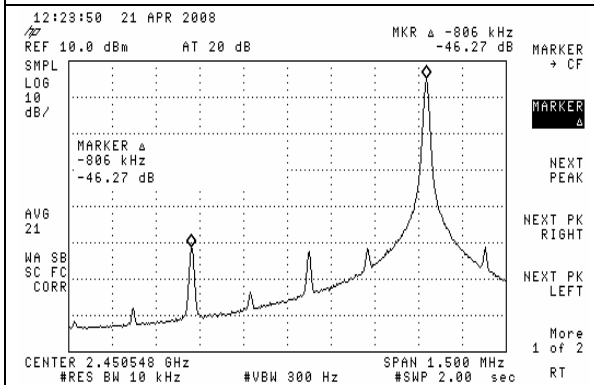


Figure C.17 Integer-N boundary spur with carrier frequency of 2450.80MHz and offset at 800kHz

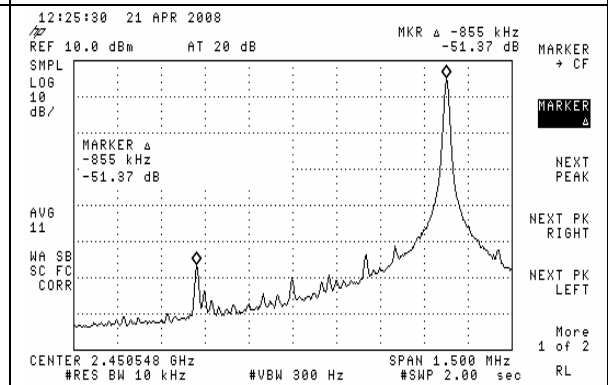


Figure C.18 Integer-N boundary spur with carrier frequency of 2450.85MHz and offset at 850kHz

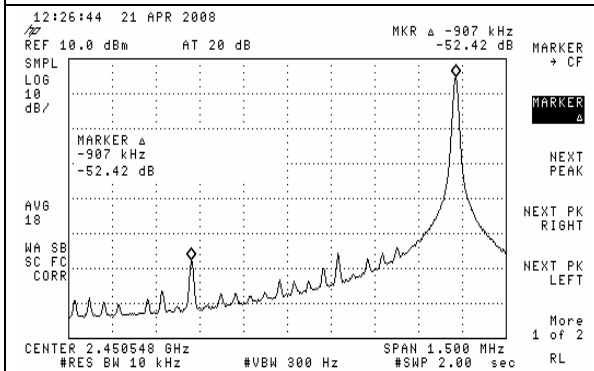


Figure C.19 Integer-N boundary spur with carrier frequency of 2450.90MHz and offset at 900kHz

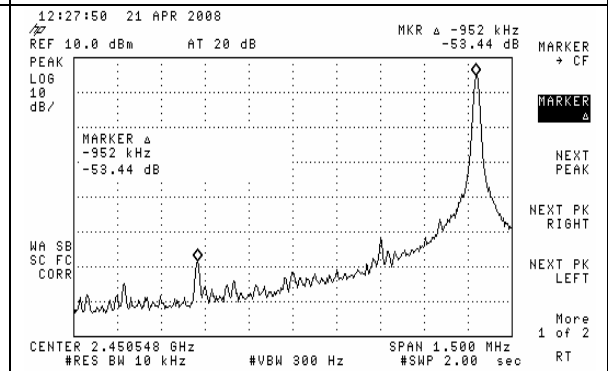


Figure C.20 Integer-N boundary spur with carrier frequency of 2450.95MHz and offset at 950kHz

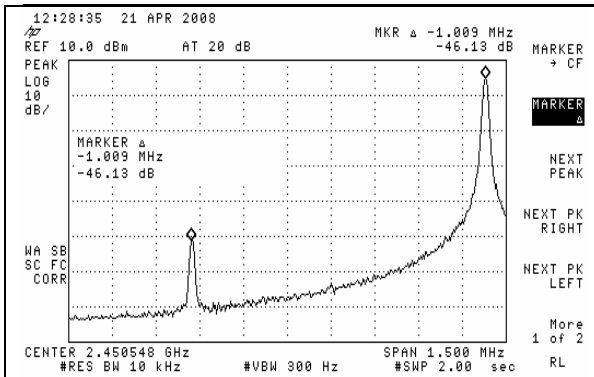


Figure C.21 Integer-N boundary spur with carrier frequency of 2451.00MHz and offset at 1.00MHz

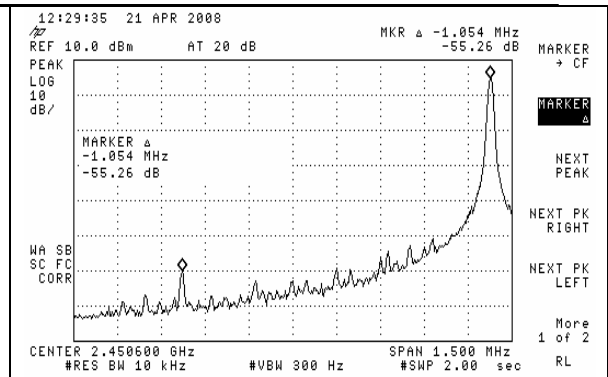


Figure C.22 Integer-N boundary spur with carrier frequency of 2451.05MHz and offset at 1.05MHz

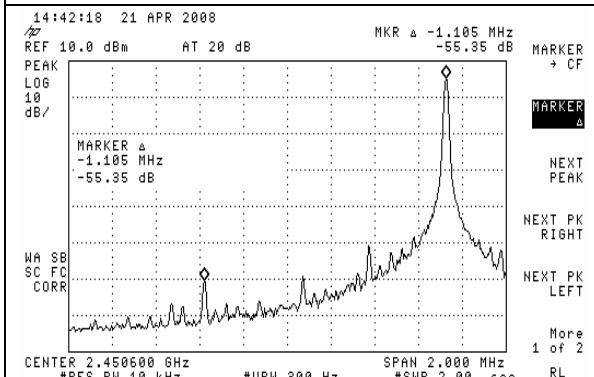


Figure C.23 Integer-N boundary spur with carrier frequency of 2451.10MHz and offset at 1.10MHz

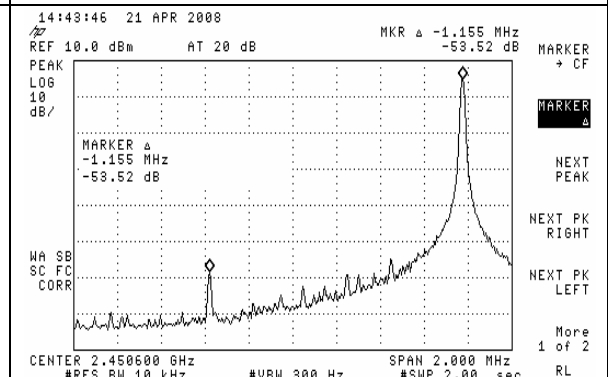


Figure C.24 Integer-N boundary spur with carrier frequency of 2451.15MHz and offset at 1.15MHz

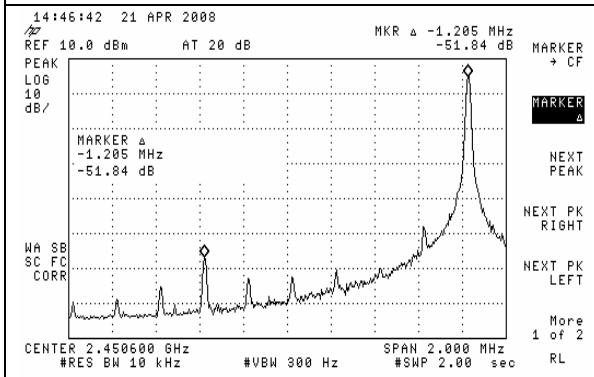


Figure C.25 Integer-N boundary spur with carrier frequency of 2451.20MHz and offset at 1.20MHz

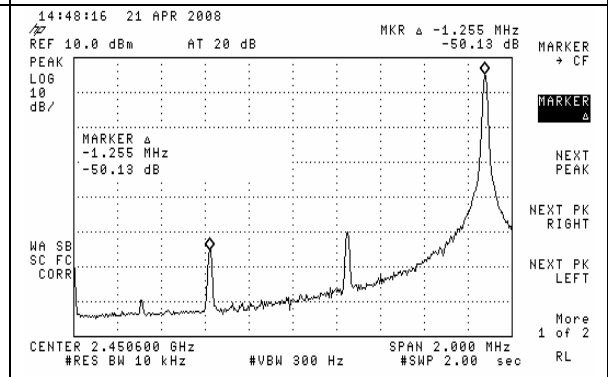


Figure C.26 Integer-N boundary spur with carrier frequency of 2451.25MHz and offset at 1.25MHz

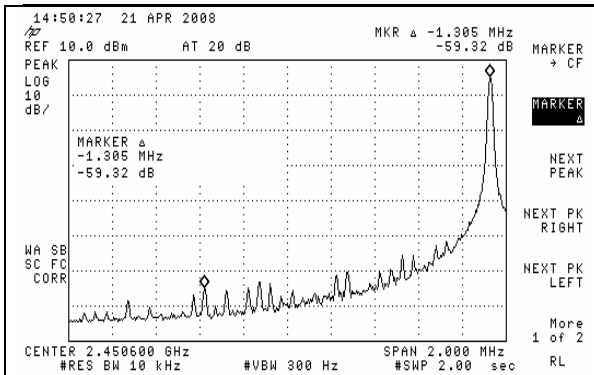


Figure C.27 Integer-N boundary spur with carrier frequency of 2451.30MHz and offset at 1.30MHz

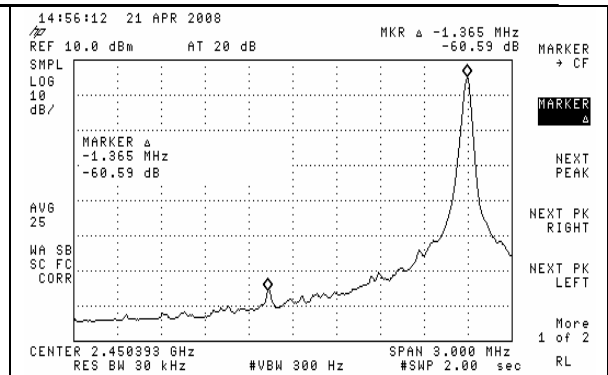


Figure C.28 Integer-N boundary spur with carrier frequency of 2451.35MHz and offset at 1.35MHz

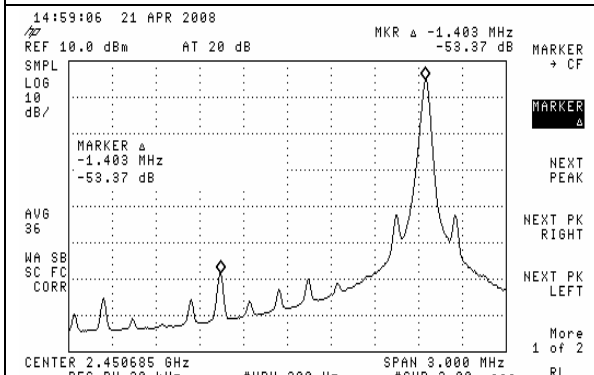


Figure C.29 Integer-N boundary spur with carrier frequency of 2451.40MHz and offset at 1.40MHz

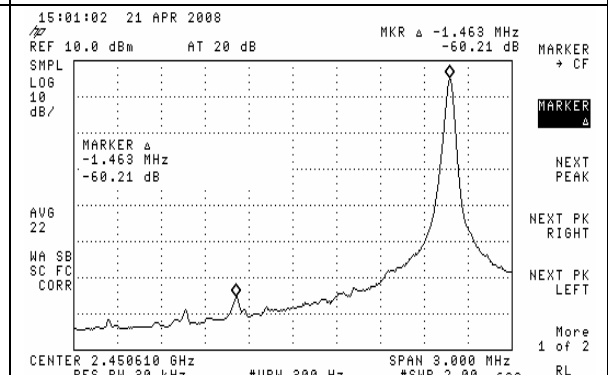


Figure C.30 Integer-N boundary spur with carrier frequency of 2451.45MHz and offset at 1.45MHz

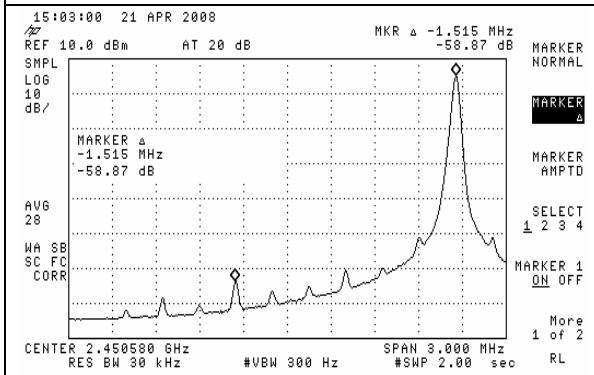


Figure C.31 Integer-N boundary spur with carrier frequency of 2451.50MHz and offset at 1.50MHz

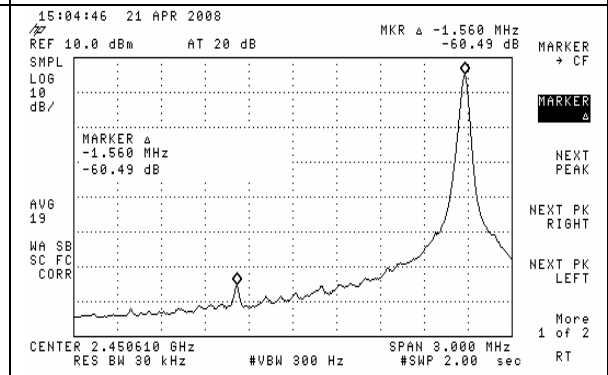


Figure C.32 Integer-N boundary spur with carrier frequency of 2451.55MHz and offset at 1.55MHz

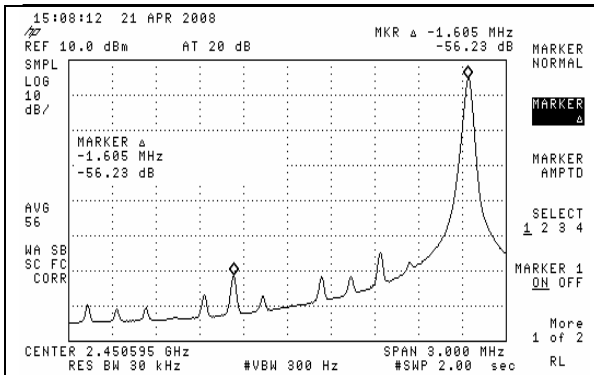


Figure C.33 Integer-N boundary spur with carrier frequency of 2451.60MHz and offset at 1.60MHz

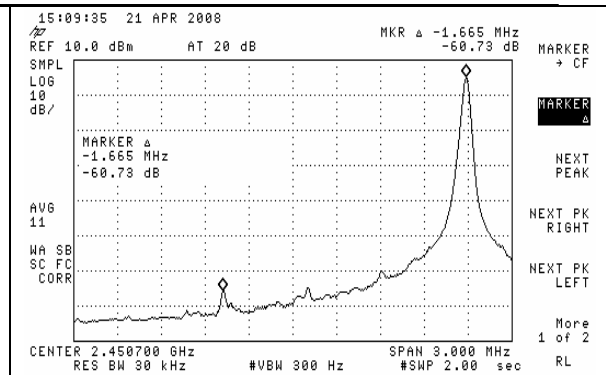


Figure C.34 Integer-N boundary spur with carrier frequency of 2451.65MHz and offset at 1.65MHz

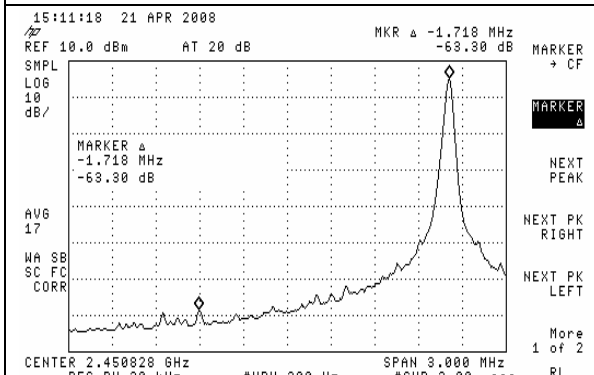


Figure C.35 Integer-N boundary spur with carrier frequency of 2451.70MHz and offset at 1.70MHz

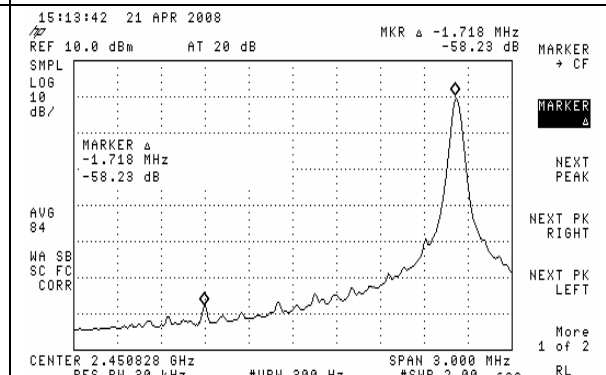


Figure C.36 Integer-N boundary spur with carrier frequency of 2451.75MHz and offset at 1.75MHz

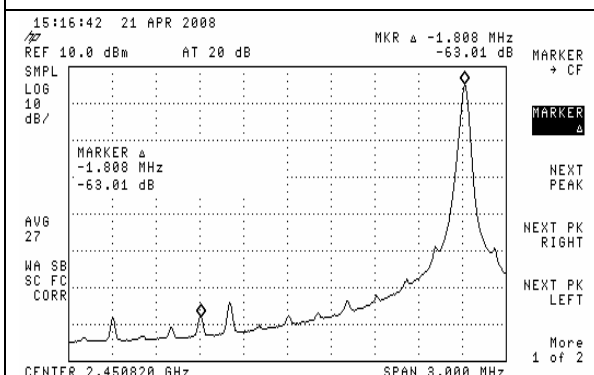


Figure C.37 Integer-N boundary spur with carrier frequency of 2451.80MHz and offset at 1.80MHz

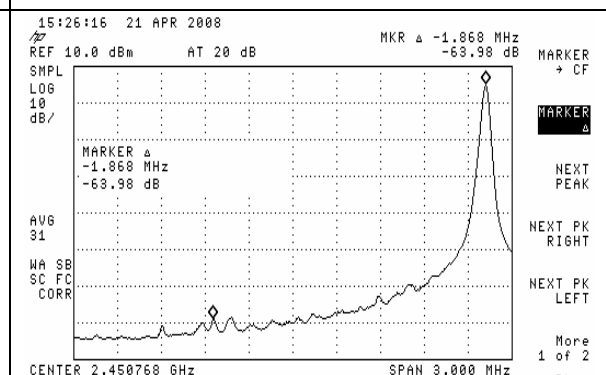


Figure C.38 Integer-N boundary spur with carrier frequency of 2451.85MHz and offset at 1.85MHz

Table C.2 Integer-N boundary spurious levels at carrier frequency of 2451MHz

| FN | Moduli | Spurious level (dBc) |         | Difference spurious level (dBc) |
|----|--------|----------------------|---------|---------------------------------|
|    |        | MASH= 3              | MASH= 4 |                                 |
| -  | 0      | -40.67               | -37.36  | 3.3                             |
| 1  | 25     | -40.60               | -37.43  | 3.2                             |
| 2  | 50     | -40.90               | -37.29  | 3.6                             |
| 3  | 75     | -40.44               | -38.05  | 2.4                             |
| 4  | 100    | -44.02               | -40.54  | 3.5                             |
| 5  | 125    | -45.98               | -41.38  | 4.6                             |
| 6  | 150    | -45.34               | -40.91  | 4.4                             |
| 7  | 175    | -45.66               | -41.95  | 3.7                             |
| 8  | 200    | -44.52               | -40.86  | 3.7                             |
| 9  | 225    | -45.04               | -41.60  | 3.4                             |
| 10 | 250    | -46.57               | -42.68  | 3.9                             |
| 11 | 275    | -44.89               | -39.99  | 4.9                             |
| 12 | 300    | -41.88               | -38.53  | 3.4                             |
| 13 | 325    | -42.63               | -38.78  | 3.9                             |
| 14 | 350    | -44.55               | -40.27  | 4.3                             |
| 15 | 375    | -42.79               | -39.07  | 3.7                             |
| 16 | 400    | -43.82               | -39.92  | 3.9                             |
| 17 | 425    | -41.95               | -37.95  | 4.0                             |
| 18 | 450    | -44.53               | -40.01  | 4.5                             |
| 19 | 475    | -45.76               | -42.22  | 3.5                             |

| FN | Moduli | Spurious level (dBc) |         | Difference spurious level (dBc) |
|----|--------|----------------------|---------|---------------------------------|
|    |        | MASH= 3              | MASH= 4 |                                 |
| 20 | 500    | -45.11               | -41.19  | 3.9                             |
|    | Max    | -40.44               | -37.29  | 4.9                             |
|    | Min    | -46.57               | -42.68  | 2.4                             |
|    | Delta  | 6.13                 | 5.39    | 2.5                             |

# Appendix D Phase Noise

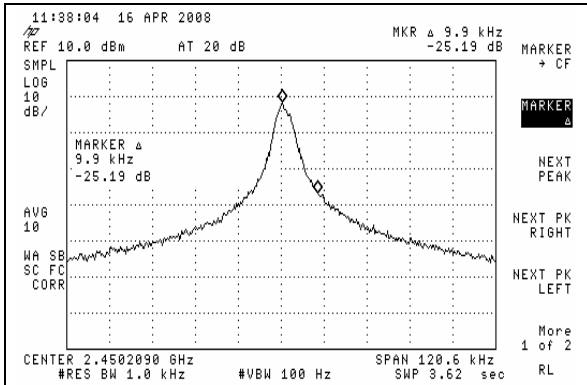


Figure D.1 #1 (LF 1kHz) phase noise performance at 2450MHz at 10kHz offset

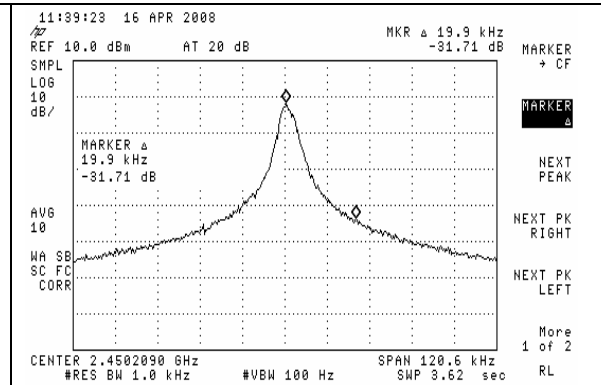


Figure D.2 #1 (LF 1kHz) phase noise performance at 2450MHz at 20kHz offset

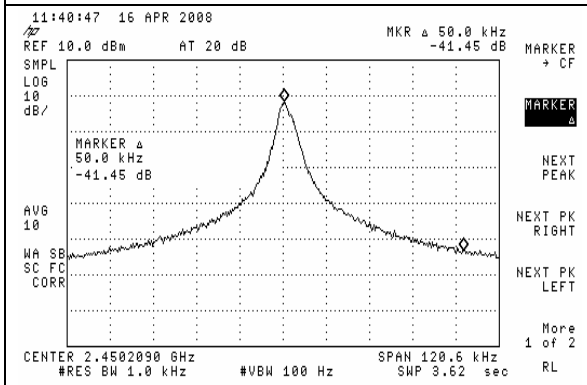


Figure D.3 #1 (LF 1kHz) phase noise performance at 2450MHz at 50kHz offset

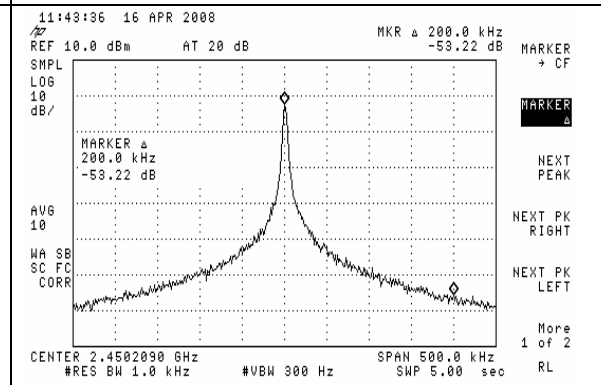


Figure D.4 #1 (LF 1kHz) phase noise performance at 2450MHz at 200kHz offset

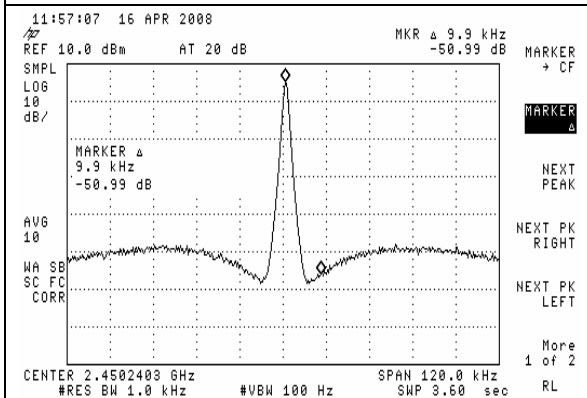


Figure D.5 #2 (LF 50kHz) phase noise performance at 2450MHz at 10kHz offset

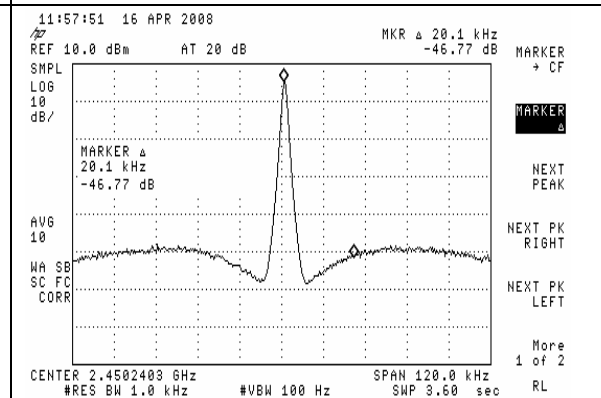


Figure D.6 #2 (LF 50kHz) phase noise performance at 2450MHz at 20kHz offset

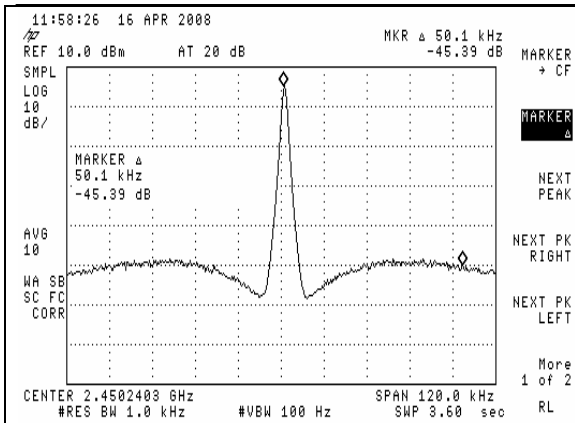


Figure D.7 #2 (LF 50kHz) phase noise performance at 2450MHz at 50kHz offset

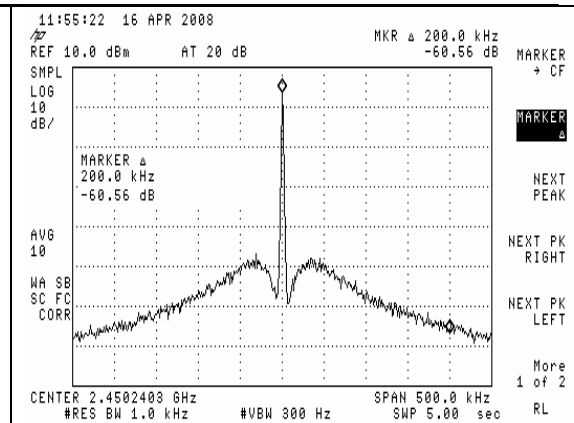


Figure D.8 #2 (LF 50kHz) phase noise performance at 2450MHz at 200kHz offset

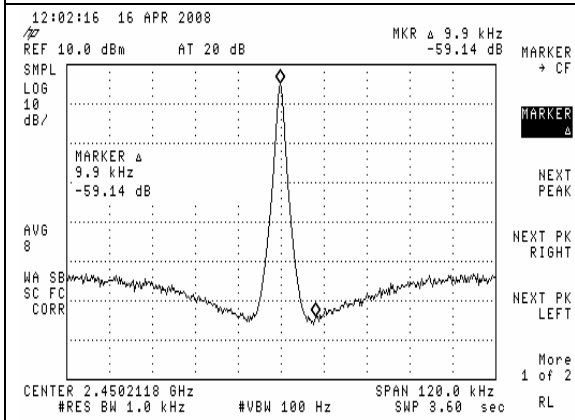


Figure D.9 #3 (LF 100kHz) phase noise performance at 2450MHz at 10kHz offset

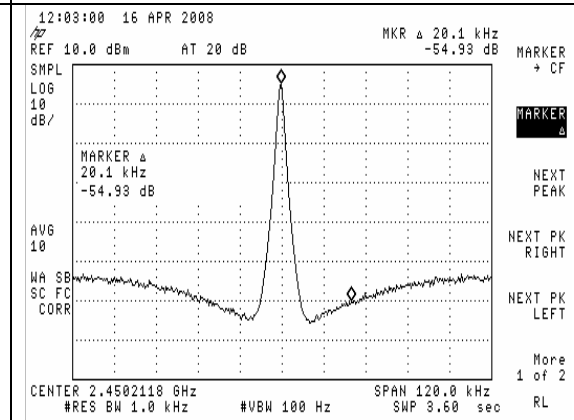


Figure D.10 #3 (LF 100kHz) phase noise performance at 2450MHz at 20kHz offset

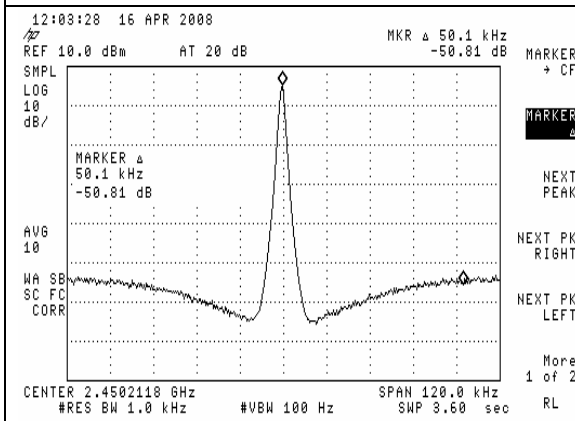


Figure D.11 #3 (LF 100kHz) phase noise performance at 2450MHz at 50kHz offset

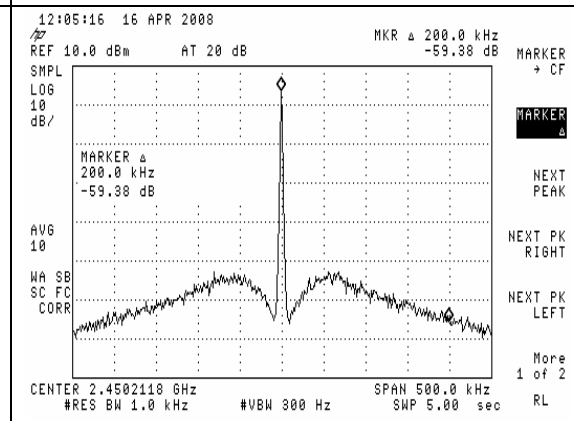


Figure D.12 #3 (LF 100kHz) phase noise performance at 2450MHz at 200kHz offset



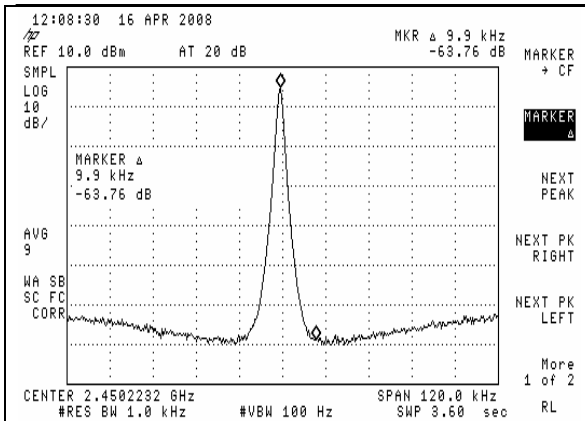


Figure D.13 #4 (LF 200kHz) phase noise performance at 2450MHz at 10kHz offset

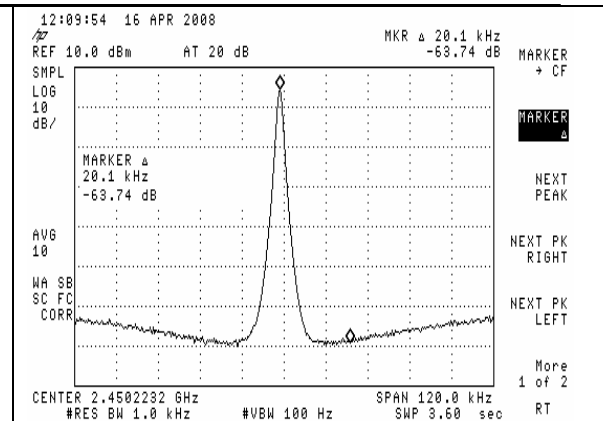


Figure D.14 #4 (LF 200kHz) phase noise performance at 2450MHz at 20kHz offset

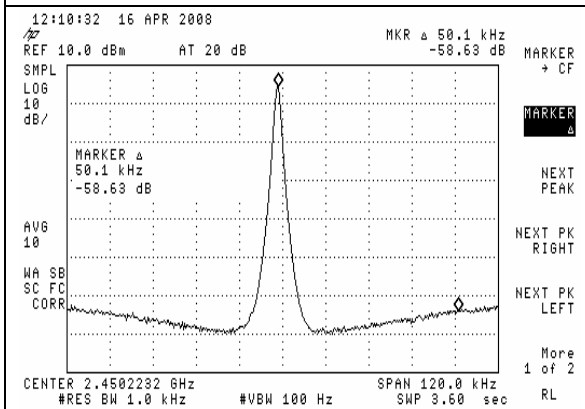


Figure D.15 #4 (LF 200kHz) phase noise performance at 2450MHz at 50kHz offset

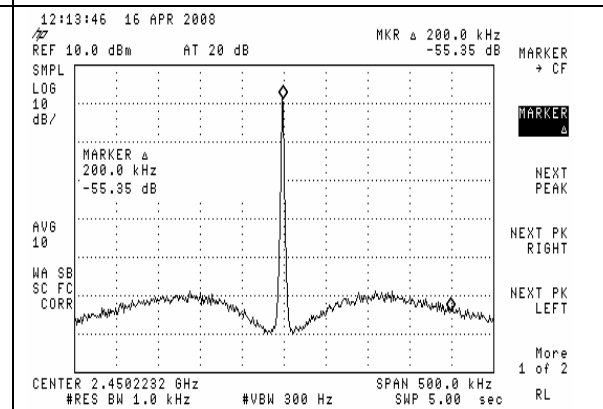


Figure D.16 #4 (LF 200kHz) phase noise performance at 2450MHz at 200kHz offset

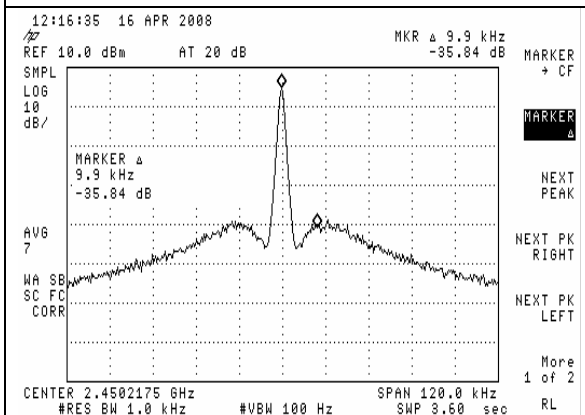


Figure D.17 #5 (LF 20kHz) phase noise performance at 2450MHz at 10kHz offset

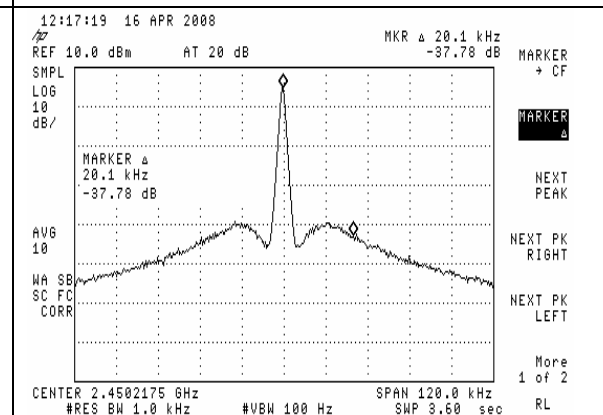


Figure D.18 #5 (LF 20kHz) phase noise performance at 2450MHz at 20kHz offset

