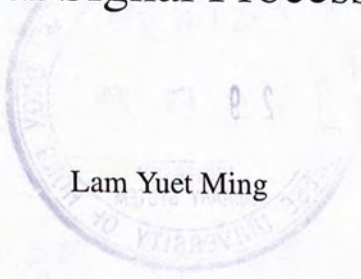


An Optimization Framework for Fixed-point Digital Signal Processing



Lam Yuet Ming

A Thesis Submitted in Partial Fulfillment
of the Requirements for the Degree of
Master of Philosophy
in
Computer Science and Engineering

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Abstract

Fixed-point hardware implementation of signal processing algorithms can often achieve higher performance with lower computational requirements than a floating-point implementation. However, the design of such systems is hard due to the difficulties of addressing quantization issues. This work presents an optimization approach to determining the wordlengths of signals in a fixed-point digital signal processing system which enables users to achieve a given quality criteria with minimum hardware resources, resulting in reduced cost and perhaps lower power consumption for VLSI implementation. These techniques lead to an automated optimization based design methodology for fixed-point based signal processing systems.

A framework involving a fixed-point class and an optimizer was developed. The object oriented class, called *Fixed*, consists of a fixed-point class to analyze fixed-point quantization effects. The *Fixed* class can simulate fixed-point operations such as addition, subtraction, multiplication and division where each operator uses wordlengths of arbitrary precision. Calculations are done using both fixed-point and floating-point formats and the floating-point calculations are used as a reference to determine the quantization error. An optimizer based on the simplex method and one-dimensional optimization approach was developed to minimize a user defined cost function, thus finding an implementation which balances hardware cost and user defined quality criteria.

This framework was applied to an isolated word recognition system based on a vector quantizer (VQ) and a hidden Markov model (HMM) decoder using linear predictive cepstral coefficients (LPCCs) as features. Utterances from the TIMIT TI 46-word database were used for both training and recognition. The isolated word recognition system was simulated using the fixed-point class, optimization of wordlengths was done using the optimizer. A 28.5% hardware cost reduction was achieved. Such an approach leads to clear advantages in both design effort and hardware resource utilization over the traditional approaches where the same wordlength is used for all operators.

定點數位信號處理的優化框架

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摘要

信號處理演算法的定點硬體實現通常比浮點實現達到較高的性能與較低的計算要求。然而，設計這樣的系統的艱難歸結於處理量化問題的困難。此論文提出一種優化方法去確定定點數位信號處理系統的信號詞長，使用戶達到一個指定的質量標準與最小硬體資源，以及在 VLSI 實現時，可以達到減少費用和可能比較低的功率消耗。這些技術為基於定點的信號處理系統提供一種基於自動優化的設計方法論。

此論文開發了一個包含了定點類和優化器 (optimizer) 的框架。這個物件導嚮的類，稱為 *Fixed*，包含了一個定點類用以分析定點量化作用。*Fixed* 能模仿定點運算，譬如加法，減法，乘法和除法，各種運算中的詞長是可以任意的。演算同時使用了定點和浮點格式，浮點演算被用作參考去計算量化錯誤。優化器使用單缸方法和一維優化方法去最小化一個用戶定義的成本函數，尋找平衡硬體費用和用戶定義質量標準的實現。

這個框架被應用到一個非連續單詞語音辨識系統，這個系統建構與向量量化器 (VQ) 和隱馬可夫模型 (HMM) 解碼器，線性可預測性頻譜係數 (LPCCs) 被用作語音辨識特徵。在這個應用中，TIMIT TI 46 詞匯數據庫被用來進行訓練和識別。定點類被用作模仿這個單詞語音辨識系統，優化器被用作詞長的優化。實驗結果表明，此框架降低了 28.5% 的硬體成本。相對與傳統方法在所有運算中使用相同的詞長，這個方法的好處在與設計工時的節省和硬體資源的充分運用

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Chapter 1

Introduction

1.1 Motivation

1.1.1 Difficulties of fixed-point design

The productivity of digital integrated circuit designers has been significantly improved by using high level synthesis techniques in recent times, these techniques can allow the designers concentrate more on high level issues, e.g. algorithm and architecture. Although higher productivity is obtained, the difficulties of addressing quantization effects in designing fixed-point system remain unchanged.

Because of the limited dynamic range of fixed-point representations of signals in a design, underflow and overflow problems may occur. When designing a fixed-point system, the designer needs to assign appropriate wordlength to each variable.

Simulation programs, typically constructed using high level languages are often used to develop and verify the algorithms. Unfortunately, up to now, there is no direct support for the representation of fixed-point arbitrary precision fractional numbers in high level programming languages and digital signal processing (DSP) chips. Fixed-point system design typically starts from a floating-point description which offers wider dynamic range and is hence less susceptible to quantization errors.

1.1.2 Why still fixed-point?

For signals with low dynamic range, fixed-point arithmetic offers advantages over floating-point in terms of performance, power consumption and hardware cost since fixed-point arithmetic is more efficient, a floating-point implementation may double or triple the hardware requirements compared with corresponding fixed-point implementation [Kai79]. Although there are some DSP chips support floating-point arithmetic, experimental results shows that using fixed-point arithmetic can reach higher clock rate [BM91], and lower cost, e.g. lower memory usage [FBM98]. Because of these benefits, fixed-point arithmetic is often used in a wide range of DSP applications where signals have relatively low dynamic ranges.

1.1.3 Difficulties of converting floating-point to fixed-point

Since fixed-point arithmetic is widely used in hardware implementations, the problem of converting an algorithmic description, which typically uses floating-point arithmetic in some high level programming language such as C, to a hardware efficient fixed-point description needs to be addressed. This process is tedious and error prone, because of the limited dynamic range of fixed-point representations. Some issues, e.g. overflow, underflow, rounding/truncation error, should be handled during transformation. Typical design analyzes the quantization effect manually by observing the ranges of variables and assign enough wordlength for each variable, but this is low efficiency and time consuming. As a result, bit-accurate simulation of the fixed-point design is necessary to analyze these quantization effects on an algorithmic level in order to be realized on hardware, in this way, the designer can concentrate on higher level design issues.

1.1.4 Why wordlength optimization?

Longer wordlengths will result in smaller quantization errors, but in order to reach a given error level, some intermediate variables, which will not contribute to the quantization error of final result, can be truncated in wordlengths. Wordlength optimization can be done based on this phenomenon. There are a number of advantages for wordlength optimization, such as lower cost and lower power consumption. These advantages can benefit some low power and small area designs, e.g. mobile devices, smart cards, PDAs, etc.

1.2 Objectives

The main objective of this research work was to develop a methodology for the design and optimization of fixed-point system. The detailed research aims were:

- Formulate a systematic methodology for addressing quantization issues in the fixed-point system.
- Explore the utility of this approach using isolated word recognition system as a realistic example.

1.3 Contributions

In this work, a framework was introduced to address the quantization issue in fixed-point systems. The main contributions of this dissertation are as follows:

- A C++ fixed-point class, called *Fixed*, was developed to simulate fixed-point arithmetic. All variables in an original floating-point description are changed to be of the *Fixed* type. Using overloading, the fixed-point description can be made to be very similar to the floating-point description, so minimal changes to the source code are required.

- An optimizer was developed to perform hardware cost/wordlength optimization, the optimizer can be used to minimize a cost function which is designed by the user. Since wordlength is monotonic decreasing with quantization error and monotonic increasing with hardware cost, if the cost function takes the error and hardware cost into account, optimal wordlengths can be found for all variables which can balance the hardware cost and error.
- This framework was applied to an isolated word recognition system, the system was simulated using the fixed-point class, optimization of wordlength was done using the optimizer. The design is very flexible, each part is developed independently, different experiments can be done easily. Optimal wordlengths were found which can balance the hardware cost and recognition accuracy.
- To the best of my knowledge, this is the first time an optimization of variable wordlengths has been applied to the isolated word recognition problem. This study has led to insights into the precision requirements in such systems.

1.4 Thesis Organization

In Chapter 2, a review of related work on fixed-point quantization issues and speech system implementation is given. Chapter 3 introduces background to fixed-point arithmetic and Chapter 4 presents the implementation of the fixed-point class. Chapter 5 introduces the background to an isolated word recognition system and Chapter 6 introduces the optimization background. In Chapter 7, the framework and word recognition system design methodology are presented. Some experimental results are given in Chapter 8. Finally, the conclusion is presented in Chapter 9.

Chapter 2

Review

2.1 Introduction

Fixed-point hardware implementations of signal processing algorithms can often achieve higher performance with lower computational requirements than corresponding floating-point implementations. However, the design of such systems is hindered by the difficulty of addressing quantization issues, which includes quantization effect analysis of fixed-point system and hardware cost/wordlength optimization.

Design of such systems center around analyzing and improving the quantization error of the fixed-point system, finding the wordlength requirements for fixed-point variables, and optimizing wordlengths for fixed-point variables which can reach specified quality criteria or balance the performance and hardware cost. In this chapter, some related work are reviewed. Since this work used an isolated word recognition system as an example, the implementations of speech systems are also reviewed.

This chapter is organized as follows. Section 2.2 presents the work using simulation approaches to address the quantization issue while Section 2.3 presents the work using analytical approaches. Section 2.4 introduces some implementations of speech systems. Section 2.5 and 2.6 are discussion and summary.

2.2 Simulation approach to address quantization issue

The simulation approach collects quantization information, e.g. quantization error, through simulation using realistic data. Wordlengths of variables are chosen heuristically while observing some quality criterion, this process is repeated with different configurations of wordlengths and stop when a specified quality criterion is met. One drawback using this approach is the long simulation time, especially for some complex systems. The other drawback is, the results obtained through simulation is dataset dependent and it is hard to choose a representative dataset.

Since manual fixed-point design is error prone, simulation of fixed-point design or transformation from floating-point descriptions to fixed-point implementations is required. The integer type in a high level programming language can be used to simulate a fixed-point format [RJ87]. C++ object classes have also been used to simulate a fixed-point format [WM94], a fixed-point format fraction number being represented using an object class, some information, e.g. the amplitude, wordlength, are stored in the object class and the calculation is handled by the class. The object class proposed by Jersák and Willems [MM98] used a similar approach.

Kim *et. al.* [SKW95] proposed C++ object classes to simulate fixed-arithmetic using operator overloading. Firstly, the floating-point type in the original code is replaced with a range estimating C++ class “fSig”, then a simulation-based approach is applied to determine the range of variables using realistic data. Another C++ object class, called “gFix”, is used to simulate fixed-point arithmetic and record the error. The wordlengths of variables were determined based on these collected information. Based on this work, Sung and Kum [WK95] proposed a searching-based approach to perform wordlength optimization. The fixed-point system is simulated using C++ object class, optimization is done to find minimum hardware cost implementation while meeting a specific error requirement. Wordlength optimization was done using two approaches, the heuristic and exhaustive approaches.

Firstly, the lower bound of wordlength of each variables are determined by setting the wordlength of other variables to very large. For the heuristic approach, each variable starts from the lower bound, and the wordlength of each variable is increased alternately until the error requirement is satisfied. For the exhaustive approach, wordlengths of all variables are increased simultaneously, until the error requirements are satisfied. The wordlength of each variable are then decreased until the error requirement test fails. A tool to transform a floating-point program into fixed-point implementation using ANSI-C integer types proposed by Kum *et. al.* [KJW00] was also based on the developed object class [SKW95]. Wordlengths of variables are determined based on the collected quantization information after simulation. Moreover, the number of shift operations in the transformed code is minimized, the minimization is done by minimize a cost function which take account of the number of shift operations. The number of shift operations is hardware dependent, for a DSP processor with a barrel shifter, like TMS320C25, TMS320C50 and TMS320C60, the cost of a shift operation is one cycle, for DSP processor without a barrel shift, like Motorola 56000, the cost of a n -bits shift operation is n cycles. Finally, the floating-point type is replaced by an integer type, and appropriate scaling codes are inserted.

Keding *et. al.* [HMMH98] proposed a system called FRIDGE to find the wordlength requirements of variables, an interpolative approach is introduced, and this approach depends much on human knowledge. Fixed-point variables are modeled as a C++ class. The designer should input some information to some fixed-point variables which are critical or already known in the system, such as wordlength, integer wordlength. Wordlengths of other variables are determined using propagation rules and the analysis of the data flow. Simulation is then applied to check if the accuracy constraints are fulfilled. If the requirement is not achieved, the designer needs to make adjustment to the inputted information. Another drawback of this work is the designer need to put much efforts during optimization.

The work proposed by Chang and Hauck [MS02] address on wordlength optimization in the *MATLAB* environment. A piece of code is appended into to original code to find the dynamic range of each variable, the dynamic range can be used to calculate the wordlengths of variables, these wordlengths are considered as lower bound. Propagation rules are used to find an upper bound for the wordlength of each variable. During optimization, for each variable, the wordlength is set to the lower bound, then the impact of that change over all variables is propagated and the change in hardware cost for that variable is recorded. This procedure is repeated for other variables and the change in hardware cost is sorted in decreasing order. This information is presented to the designer to decide which variables should be more tightly constrained in wordlength. One drawback with this approach is, the selection process is very much dependent on human experience.

2.3 Analytical approach to address quantization issue

Analytical approaches analyze the quantization error of computation based on a theoretical framework, an error expression often being derived [P. 91, SW98]. The wordlength of a fixed-point variable are usually derived from the signal-flow graph, local annotations, interpolation, and propagation of ranges of variables. This approach can give true upper bounds and achieve a faster run time than a simulation approach, but the result may be very conservative and lead to a gross overestimation of variable wordlengths [RLP⁺99].

Fiore [Pau98] addressed the quantization error of the addition of two uncorrelated values that are truncated/rounded prior to addition. Two methods were introduced for rounding which can reduce the hardware complexity and maintain a certain variance. The first method called LR, it basically ORing the most significant

bits of the parts to be truncated and input the result as carry input of the least significant bit of the adder chain. The second method called RLR, simply inputs 1 as carry input to the least significant bit of the adder chain. Some experiments shows that the variance using LR/RLR is close to the results using truncation/rounding.

Wadekar and Parker [SA98] proposed to reduce the wordlength of some variables that do not contribute significantly to the final result. A worse-case error estimation model is introduced, the error propagated from the input to output. Two examples, discrete cosine transform and 5×5 matrix determinant, were used and a genetic algorithm was applied to minimize the hardware cost and reach a specified error bound at the same time. In the genetic algorithm, the quality of the final result depends on the population size [Voj02], but the population size is bounded by the available computing resources, since the computational power is proportional to the population size.

The work proposed by Cmar *et. al.* [RLP⁺99] using both analytical and simulation approaches. The integer size of a fixed-point variable is determined by using a statistical method or propagation of dynamic range. But, as pointed out by the author, range propagation can become unstable and cause explosion when applied to feedback signals. To determine the fraction size of fixed-point variable, a simulation approach is used. An object class is introduced to represent a variable in fixed-point format, simulation is carried out to collect the error between a fixed-point and floating-point system, fraction size is determined by comparing the calculation results between fixed-point and floating-point arithmetic.

2.4 Implementation of speech systems

Optimizing recognition accuracy and real time performance are the major considerations of most previous approaches. Some popular DSP chips such as the TMS320 series [KGR97] have been widely used for implementing speech recognition systems [YY00, KJK95, NNS⁺99]. Kim *et. al.* [SIYS96] proposed a VLSI chip for

isolated speech recognition system which can recognize 1000 isolated words per second. Bliss and Scharf [WL89] proposed a ring architecture to perform hidden Markov model (HMM) decoding in parallel. In this architecture, each processing element will calculate predecessors serially. N processing elements can compute the score for all HMM states in parallel. Under the development of field-programmable gate array (FPGA) technique, FPGA chips have higher density and clock rate, implement more complicated systems on FPGA chip becomes realizable, it is often chosen to achieve high performance, Vargas *et. al.* [FRD01] proposed a FPGA implementation of a HMM decoder which is 500 times faster than a classic implementation. A speech recognition system proposed by Melnikoff *et. al.* [SSM02], can process speech 75 times real time using a Xilinx Virtex XCV1000 chip.

Hidden Markov models (HMMs) are widely used in modern speech recognition systems because HMM-based speech recognition systems have proven to yield high recognition accuracy. Some speech systems focus on improving implementation of HMM to get better recognition accuracy. Zhang *et. al.* [YCR⁺94] proposed using multiple hidden Markov models, each word in the vocabulary contains three vector quantization methods and three hidden Markov models. Gholampour and Nayebi [IK99] introduced a cascade HMM/ANN model to improve the recognition accuracy.

2.5 Discussion

Analytical approaches require extensive knowledge of both the algorithm and hardware architecture, moreover, it is hard to develop an error model for complicated systems. Wordlength optimization is tedious, in the work proposed by Hui *et. al.* [GKZ98], in order to find an optimal allocation of a variable precision, the authors needed to implement several systems using different numerical formats, such as single fixed-point format, double fixed-point format and floating-point format. A

simulation-based approach seems to be a better choice, since it can reduce the burden of the designer, all jobs being done by computer. But some simulation approaches, e.g. [MS02], still require the designer to be involved in the optimization process, the designer should analyze the simulation result and make a decision to constrain which variables. Although some work has been done to optimize some fixed-point systems using a searching-based method, e.g. [WK95], the goal of this work is to provide a tool for assisting fixed-point system design and optimization, using this tool, designers can have a much clearer idea of the wordlength requirements of their hardware design.

Previous fixed-point implementations of speech recognition systems concentrated on optimizing recognition accuracy and real time performance, and quantization effects in fixed-point arithmetic were seldom directly addressed. With improvements in speech models and VLSI technology, speech recognition accuracy is much higher than in the past, and designing a speech recognition system with real time performance is not that difficult. However, quantization issues remain a problem when designing a fixed-point hardware system, this work performing wordlength/hardware cost optimization of an isolated word recognition system, it is more complicated than most of previous optimization work for filters.

2.6 Summary

In this chapter, we have reviewed some related work on fixed-point design and implementation, including the simulation of fixed-point arithmetic, analytical and simulation approaches to address the quantization effect and optimization. Some implementations of speech systems are also reviewed.

Chapter 3

Fixed-point arithmetic background

3.1 Introduction

Fixed-point arithmetic is widely used in digital signal processing systems, because it has a simpler implementation than floating-point arithmetic. A brief introduction to fixed-point arithmetic is given in this chapter.

This chapter is organized as follows. Section 3.2 introduces fixed-point number representations. In Section 3.3, fixed-point addition/subtraction is introduced. Fixed-point multiplication is introduced in Section 3.4 and fixed-point division is described in 3.5, the last section is the summary.

3.2 Fixed-point representation

There are several notations commonly used to represent a binary integer, such as sign-and-magnitude, one's complement and two's complement notations. Two's complement format is the most commonly used format [Amo94].

Figure 3.1 is an n -bit two's complement integer format, the first bit x_{n-1} is the sign bit. The absolute value of an n -bit two's complement integer is:

$$AbsoluteValue = -x_{n-1} \cdot 2^{n-1} + \sum_{i=0}^{n-2} x_i \cdot 2^i. \quad (3.1)$$

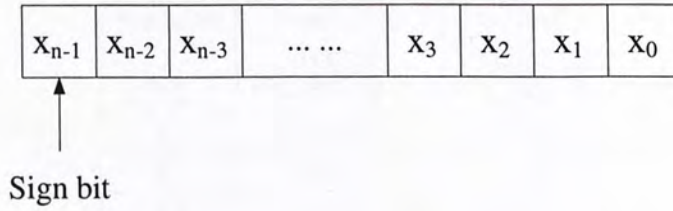


Figure 3.1: Two's complement integer format

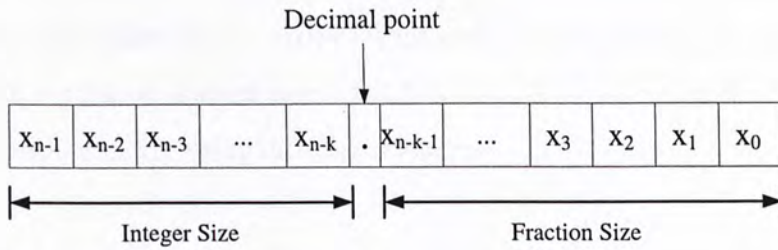


Figure 3.2: Fixed-point representation for fraction number

For an n -bit two's complement integer, the dynamic range it can represent is $[-2^{n-1}, 2^{n-1} - 1]$. Using the two's complement format, a negative integer can be represented by inverting all bits of the positive integer and adding one, as shown:

$$-X = \bar{X} + 1. \tag{3.2}$$

To represent a fraction number, a decimal point can be inserted into the integer format shown in Figure 3.1, as shown in Figure 3.2. The Integer Size is the number of bits used to represent the integer part, and the Fraction Size is the number of bits used to represent the fraction part. The absolute value of an n -bit fraction number with fraction size k is:

$$AbsoluteValue = (1/2^k)[-x_{n-1} \cdot 2^{n-1} + \sum_{i=0}^{n-2} x_i \cdot 2^i]. \tag{3.3}$$

The smallest non-zero fraction number it can represent is $\pm 1/2^k$, and the dynamic range is $[-2^{n-k-1}, 2^{n-k-1} - 1/2^k]$.

Notation	Fixed-point format	Decimal value
7.1	0000010.1	2.500
6.2	000010.11	2.750
5.3	00010.111	2.875
4.4	0010.1110	2.875

Table 3.1: Fixed-point representation of fractional number 2.875 using different notation

The decimal place can be varied for different integer size and fraction size. In Figure 3.2, a notation (integer size k , fraction size $n-k$) is used. Table 3.1 shows the representation of 2.875 using different notation.

3.3 Fixed-point addition/subtraction

Addition is straightforward, since all fraction numbers are represented in two's complement format. Using equation 3.2, subtraction can also be done as shown:

$$\begin{aligned}
 A - B &= A + (-B) \\
 &= A + \bar{B} + 1 \\
 &= A + \text{two's complement of } B.
 \end{aligned}
 \tag{3.4}$$

As a result, subtraction $A - B$ can be done by addition of A to the two's complement of B . The scaling issue must also be addressed. The fraction sizes of the two operands maybe different, and hence a shift operation must be done to align the decimal points before addition. Consider two numbers, $A = a_{n-1}a_{n-2}\dots a_1a_0$ with

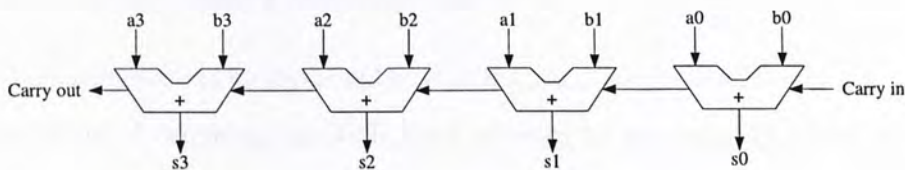


Figure 3.3: Parallel adder

fraction size k , and $B = b_{n-1}b_{n-2}\dots b_1b_0$ with fraction size m , when $m > k$,

$$\begin{aligned}
 A + B &= (1/2^k)[-a_{n-1} \cdot 2^{n-1} + \sum_{i=0}^{n-2} a_i \cdot 2^i] + (1/2^m)[-b_{n-1} \cdot 2^{n-1} + \sum_{i=0}^{n-2} b_i \cdot 2^i] \\
 &= (1/2^m)\{2^{m-k}[-a_{n-1} \cdot 2^{n-1} + \sum_{i=0}^{n-2} a_i \cdot 2^i] + \\
 &\quad [-b_{n-1} \cdot 2^{n-1} + \sum_{i=0}^{n-2} b_i \cdot 2^i]\} \tag{3.5}
 \end{aligned}$$

From equation 3.5, one can see that A should be shifted left by $m - k$ bits to align the decimal point with B . The result has an integer size $n - k$ and fraction size m , which are the maximum integer size and fraction size of the two input operands.

For the hardware implementation of addition/subtraction using a parallel architecture, all result bits are calculated at the same time. Figure 3.3 shows the block diagram of a 4-bit ripple-carry adder. The carry is propagated from the least significant bit to most significant bit, the result can be obtained within one cycle. Four 1-bit full adders are needed.

Although the result can be obtained within one cycle, the propagation delay required to propagate the carry from least significant bit to most significant bit is $O(n)$. Alternate implementations can be used to improve this delay, e.g. carry-look-ahead adders and carry-skip adders [Isr02] at the expense of increased hardware requirements. The number of 1-bit full adders required using parallel approach is $O(n)$ for an n -bit addition/subtraction.

3.4 Fixed-point multiplication

Let the multiplier and multiplicand be $A = a_{n-1}a_{n-2}\dots a_1a_0$ and $B = b_{n-1}b_{n-2}\dots b_1b_0$ respectively. A sequential multiplication operates by scanning the multiplier A bit by bit, and forming the product a_jB for the j th bit, a new partial product $P^{(j+1)}$ is obtained by summing a_jB and previous partial product $P^{(j)}$, a total of $n - 1$ iterations is required to calculate the final product. The expression for this recursive step is

$$P^{(j+1)} = P^{(j)} + a_j \cdot B \cdot 2^j; \quad (3.6)$$

where $P^{(0)} = 0$. One can see that product a_jB is aligned before added to previous partial product $P^{(j)}$, it is because the weight of a_{j+1} is double that of a_j . As a result, at step j , a_jB should shift to left j bits. Using this notation, $P^{(n-1)}$ can be calculated as

$$\begin{aligned} P^{(n-1)} &= P^{(n-2)} + a_{n-2} \cdot B \cdot 2^{n-2} \\ &= P^{(n-3)} + a_{n-3} \cdot B \cdot 2^{n-3} + a_{n-2} \cdot B \cdot 2^{n-2} \\ &= \dots \\ &= a_0 \cdot B \cdot 2^0 + a_1 \cdot B \cdot 2^1 + \dots + a_{n-3} \cdot B \cdot 2^{n-3} + a_{n-2} \cdot B \cdot 2^{n-2} \\ &= \sum_{j=0}^{n-2} a_j \cdot B \cdot 2^j \\ &= \left(\sum_{j=0}^{n-2} a_j \cdot 2^j \right) \cdot B \end{aligned} \quad (3.7)$$

Using the above result, if the multiplier A and multiplicand B are both positive, the product can be calculated as

$$\begin{aligned} Product = A \cdot B &= \left(\sum_{j=0}^{n-1} a_j \cdot 2^j \right) \cdot B \\ &= \left(\sum_{j=0}^{n-2} a_j \cdot 2^j \right) \cdot B \quad (\text{since } a_{n-1} = 0) \\ &= P^{(n-1)} \end{aligned} \quad (3.8)$$

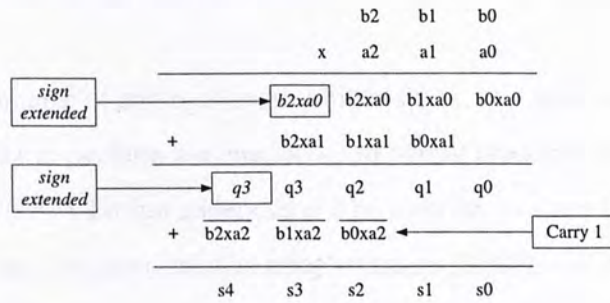


Figure 3.4: Two's complement multiplication

The above calculation result can also be used if applied to two's complement multiplication. When the multiplicand B is negative and the multiplier A is positive, the product calculation is same as above, except that partial product $P^{(j)}$ must be sign extended before the addition. When the multiplier is negative, using equation 3.1, the product can be calculated as follows where again, all partial products are sign extended before addition.

$$\begin{aligned}
 Product &= A \cdot B \\
 &= (-a_{n-1} \cdot 2^{n-1} + \sum_{i=0}^{n-2} a_i \cdot 2^i) \cdot B \\
 &= -a_{n-1} \cdot 2^{n-1} \cdot B + \sum_{i=0}^{n-2} a_i \cdot 2^i \cdot B \\
 &= P^{(n-1)} - B \cdot a_{n-1} \cdot 2^{n-1}
 \end{aligned} \tag{3.9}$$

To perform an $n \times n$ bits multiplication, from equation 3.7, $n - 2$ additions are required to calculate $P^{(n-1)}$, and from equation 3.9, extra one addition is required to calculate the final product, as a result, total number of addition is $n - 1$. Hardware implementation of parallel multiplication is performing all these additions in one cycle. Figure 3.4 shows an example of a 3×3 bits two's complement multiplication. In this figure, the partial product is sign extended. a_2B is inverted, addition is done with carry in 1. Since when A is negative, subtraction is performed instead, this process is shown by equation 3.9, as mentioned before, subtraction is equivalent to

addition of one operand to the two's complement of the other operand as shown by equation 3.4.

Since summing $P^{(j)}$ and $a_j B$ is an n -bit addition, and total number of iteration is $n - 1$, in order to perform summation of all partial products in one cycle, by approximation, $O(n^2)$ 1-bit full adders should be used for an $n \times n$ bits multiplication. Some parallel architectures, such as array structure [Isr02], can be used to perform this parallel addition.

3.5 Fixed-point division

Consider a division A/B , assume the quotient is Q and the remainder is R which are defined by

$$A = B \cdot Q + R. \quad (3.10)$$

Assuming that all variables are unsigned firstly, a sequence of subtractions and shifts is done to determine the quotient $Q = q_0 q_1 \dots q_{n-1}$. At iteration i , the remainder is compared to the divisor B , if the remainder is larger than B , the corresponding quotient bit is set to 1, otherwise, set to 0. The expression for this recursive step is

$$r_i = r_{i-1} - q_{i-1} \cdot B \cdot 2^{n-i}, \quad (3.11)$$

where r_i is the remainder at iteration i and $r_0 = A$. q_{i-1} is determined by comparing r_{i-1} to $B \cdot 2^{n-i}$. The final remainder can be obtained after n iterations as

$$\begin{aligned} r_n &= r_{n-1} - q_{n-1} \cdot B \cdot 2^0 \\ &= r_{n-2} - q_{n-2} \cdot B \cdot 2^1 - q_{n-1} \cdot B \cdot 2^0 \\ &= \dots \\ &= r_0 - q_0 \cdot B \cdot 2^n - q_1 \cdot B \cdot 2^{n-1} - \dots - q_{n-2} \cdot B \cdot 2^1 - q_{n-1} \cdot B \cdot 2^0 \\ &= r_0 - (q_0 \cdot 2^n + q_1 \cdot 2^{n-1} + \dots + q_{n-2} \cdot 2^1 + q_{n-1} \cdot 2^0) \cdot B \\ &= A - Q \cdot B, \end{aligned} \quad (3.12)$$

where $r_n = R$. For two's complement division, the process is similar, except that to determine the quotient bit, either subtraction or addition is used based on the signs of r_{i-1} and B , as shown below:

```

if  $r_{i-1}$  and  $B$  have the same sign, then {
     $r_i = r_{i-1} - q_{i-1} \cdot B \cdot 2^{n-i}$ ;
}
else {
     $r_i = r_{i-1} + q_{i-1} \cdot B \cdot 2^{n-i}$ ;
}

if  $r_i$  and  $r_{i-1}$  have the same sign, then {
    set  $q_{i-1}$  to 1;
}
else {
    set  $q_{i-1}$  to 0;
     $r_i = r_{i-1}$ ;
}

```

From the above algorithm, one can see that, when r_i and r_{i-1} have different signs, r_i is restored to the previous value r_{i-1} . This method is therefore called restoring division [CZS02]. In this method, the main arithmetic operations are addition and subtraction $r_i = r_{i-1} \pm q_{i-1} \cdot B \cdot 2^{n-i}$. As mentioned by previous section, subtraction can be done using addition, an n -bit adder is needed. Although B is left shifted $n - i$ bits, the lower bits are all zero, calculation of these lower $n - i$ bits can be ignored, an n -bit adder is enough.

Figure 3.5 shows the block diagram of the divider using restoring division. In this diagram, register Q and B are used to store dividend and divisor initially, an n -bit adder is used, which can be constructed by n 1-bit full adders. By approximation, the number of 1-bit full adders required for an n -bit division is $O(n)$.

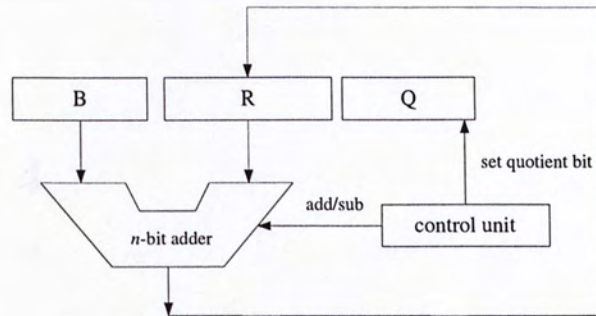


Figure 3.5: Block diagram of divider using restoring-division

3.6 Summary

In this chapter, background on fixed-point arithmetic was introduced. The two's complement representation was introduced and methods for implementing addition/subtraction, multiplication and division were discussed. Hardware cost for each arithmetic operation was estimated based on the arithmetic algorithms and their basic hardware implementations, the hardware cost was estimated in terms of 1-bit full adders.

Chapter 4

Fixed-point class implementation

4.1 Introduction

In order to analyze quantization effects of fixed-point arithmetic in fixed-point digital signal processing system, a fixed-point class, called *Fixed*, was developed to simulate fixed-point arithmetic in the C++ language. All operands are *Fixed* type, fixed-point calculated was handled internally by the fixed-point class. The detailed implementation of the fixed-point class will be described in this chapter.

This chapter is organized as follows. Section 4.2 introduce how to use overloading feature of the C++ language to simulate a fixed-point system. Some features and implementation of the fixed-point class are presented in Section 4.3. The last section is the summary.

4.2 Fixed-point simulation using overloading

In this work, we employ the simulation-based approach to analyze the quantization effects associated with each variable and collect statistical information from each variable during simulation. A fixed-point class, called *Fixed*, was developed to achieve this goal. All operands in a fixed-point system are defined as *Fixed*, some methods are implemented to handle the fixed-point arithmetic operations, such as

addition, subtraction, multiplication and division. In the following, an example will be given to show how to use this fixed-point class to simulate fixed-point arithmetic.

The overloading feature of the C++ language was used and the code for a fixed-point simulation is very similar to its floating-point one. It is possible to convert a floating-point program into fixed-point implementation by just changing the variable definitions, rest of the program being unchanged. Or using this class to develop system simulation description as using floating-point type. For example, the following floating-point program:

```
float a;  
float b;  
float c;  
  
a = 1.23;  
b = 4.56;  
c = a + b;
```

can be transformed into the fixed-point implementation:

```
Fixed a(4, 5); // integer size 4, fraction size 5  
Fixed b(5, 6); // integer size 5, fraction size 6  
Fixed c(5, 5); // integer size 5, fraction size 5  
  
a = 1.23;  
b = 4.56;  
c = a + b;
```

In the above fixed-point program, since the “=” operator is overloaded, fraction numbers 1.23 and 4.56 will be converted into fixed-point format and stored in *Fixed* objects *a* and *b*. The “*a + b*” statement will be handled by the overloaded operator “+” and the result will be a *Fixed* object. When assigned to *c*, the sum will be rounded to the precision of *c*.

```

#include <stdio.h>
#include <stdlib.h>

class Fixed
{
private:
    int IntegerSize;
    int FractionSize;

    MY_FLOAT SingleMax;
    MY_FLOAT SingleMin;

    MY_FLOAT ArrayMax;
    MY_FLOAT ArrayMin;
    int isArray;
    Fixed *arrayPtr;

    MY_INT FixedValue;
    MY_FLOAT FloatValue;

public:
    //// constructor ////
    Fixed(int, int, MY_FLOAT);
    //// end constructor ////

    //// return value////
    MY_FLOAT getQerr();
    int getIWL();
    //// end return value////

    //// for array use ////
    MY_INT setArray(Fixed *);
    //// end for array use ////

    //// overload operator ////
    Fixed operator = (Fixed);
    Fixed operator = (const MY_FLOAT);
    Fixed operator + (Fixed );
    Fixed operator - (Fixed );
    Fixed operator * (Fixed );
    Fixed operator / (Fixed );
    //// end overload operator ////

    //// calculate cos ////
    Fixed mcos(int, int);
    //// end calculate cos ////
}

```

Figure 4.1: Fixed-point class declaration

4.3 Fixed-point class implementation

Figure 4.1 shows the declaration of the fixed-point class. A fixed-point object is defined to represent two's complement fractions with arbitrary precision in fixed-point format. Detailed implementation is introduced as follows.

4.3.1 Fixed-point object declaration

A fixed-point variable can be declared as:

```
Fixed VariableName;
Fixed VariableName (IntegerSize, FractionSize);
Fixed VariableName (IntegerSize, FractionSize, FloatingPointValue);
```

The parameters *IntegerSize*/*FractionSize* are used to define the integer/fraction size of the fixed-point format in Figure 3.2 of the previous chapter. By defining different *IntegerSize* and *FractionSize* for each object, all variables in a fixed-point system can be of arbitrary wordlength. These two values are stored in the private variables *IntegerSize*/*FractionSize* of the object as shown in Figure 4.1. If *IntegerSize*/*FractionSize* is not specified when declaring a variable, default values will be used.

The parameter *FloatingPointValue* is stored in the private variable *FloatValue* of the object as shown in Figure 4.1 and *FixedValue* will store the corresponding fixed-point representation. In Figure 4.1, *MY_INT* is a *longlong* type, which is 64-bit integer, used to simulate fixed-point format. *MY_FLOAT* is a *double* type, it is used to simulate floating-point format. *Double* is IEEE 754 double-precision floating-point format, which is 64-bits in length [JD99] [Wil00]. From the most significant to least significant bit, a double has a sign bit, 11-bits exponent and 52-bits fraction as shown in Figure 4.2.

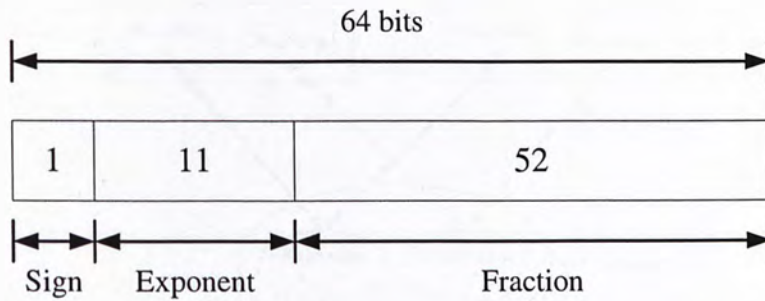


Figure 4.2: IEEE 754 double-precision format

4.3.2 Overload the operators

In order to overload the fixed-point operators, namely addition, subtraction, multiplication and division, corresponding methods were implemented in the fixed-point class. The following shows the method signatures:

```
Fixed Fixed::operator + (Fixed) { implementation }
Fixed Fixed::operator - (Fixed) { implementation }
Fixed Fixed::operator * (Fixed) { implementation }
Fixed Fixed::operator / (Fixed) { implementation }
Fixed Fixed::operator = (const MY_FLOAT) { implementation }
Fixed Fixed::operator = (Fixed) { implementation }
```

Where “::” is called scope resolution operator, the notation “ClassName::MethodName” means the method “MethodName” is belong to class “ClassName”. A mathematical expression

$$C = A \operatorname{operator} B \quad (4.1)$$

can be regarded as

$$C = A.\operatorname{operator}(B) \quad (4.2)$$

and handled by corresponding methods. One can see that, all methods take a *Fixed* object as input, and the returned result is also a *Fixed* object. Note that, the

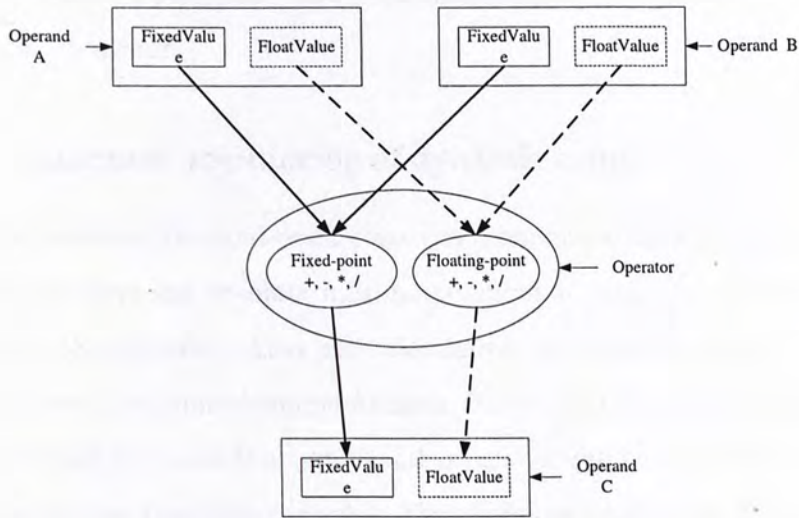


Figure 4.3: Arithmetic calculation using fixed-point object

assignment operator is also overloaded. If the input operand is a fraction number, this method will convert this fraction number into fixed-point format and stored in the *Fixed* object at a precision specified by the target object. If the input is a *Fixed* object, this method will round it to the target object's precision.

4.3.3 Arithmetic operations

The fixed-point class performs all calculations using both fixed-point and IEEE 754 double precision formats. The calculation result using fixed-point arithmetic is stored in *FixedValue*, and the calculation result using floating-point arithmetic is stored in *FloatValue*. This process can be shown by Figure 4.3. It is assumed throughout this work that calculations done in double precision floating-point are without error.

To avoid loss of precision during calculation, for addition, subtraction and division, the result use the maximum integer and fraction sizes of the two input operands. For multiplication, the product's wordlength is the summation of the two input operands' wordlengths minus one. This calculation result will be rounded to

the target operand's precision when performing assignment operation by the overloaded “ = ” operator.

4.3.4 Automatic monitoring of dynamic range

During calculation, the fixed-point class can monitor the dynamic range of each variable, and store the absolute maximum/minimum values in private variables *SingleMax*/*SingleMin*. After each calculation, the absolute result is compared with the existing maximum/minimum values. If it is larger than the maximum value, it will be stored in *SingleMax*, on the other hand, it will be stored in *SingleMin* if it is smaller than the minimum value. The minimum integer size of each variable which guarantees that overflow will not occur, can be calculated from *SingleMax* using the following equation

$$IntegerSize = int(\log_2 SingleMax) + 2; \quad (4.3)$$

The minimum integer size required to represent the positive number *SingleMax* is $int(\log_2 SingleMax) + 1$. Since all numbers are using two's complement format, additional one bit is needed for the sign bit. As a result, $int(\log_2 SingleMax) + 2$ bits are required. A method, called *getIWL()*, is provided by this fixed-point class to retrieve the minimum integer size.

4.3.5 Automatic calculation of quantization error

Since the fixed-point class performs operations using both fixed-point and floating-point arithmetic, the quantization effects between fixed-point and floating-point arithmetic are easily analyzed. Using the floating-point result as a reference, quantization error is computed as follows

$$Qerr = 20 * \log \left| \frac{FixedValue - FloatValue}{FloatValue} \right|. \quad (4.4)$$

A method, called *getQerr()*, is implemented to get the quantization error of a *Fixed* object.

4.3.6 Array supporting

The fixed-point class supports arrays, an array can be declared as follows

```
Fixed VariableName [NumberOfElements];
```

It can also be declared dynamically using *malloc* as follows

```
Fixed *VariableName;
VariableName = (Fixed *) malloc (sizeof(Fixed) * NumberOfElements);
```

In Figure 4.1, the private variable *isArray* is used to indicate whether this object is an element of an array. *ArrayMax/ArrayMin* are used to store the absolute maximum/minimum value of an array. Each array element has a pointer that point to a *Fixed* object, the pointer address is stored in the private variable *arrayPtr*. If any element's value is updated, *ArrayMax/ArrayMin* of the *Fixed* object, which is pointed by *arrayPtr*, will be updated if the updated value of this element is a new maximum/minimum value of the entire array. As a result, after finishing all fixed-point computation, *ArrayMax/ArrayMin* of the *Fixed* object pointed to by *arrayPtr* will store the absolute maximum/minimum value of the entire array. The method, *setArray(Fixed*)*, is used to save the pointer value to *arrayPtr*. The minimum integer size of an array can be calculated as follows

$$IntegerSize = \text{int}(\log_2 ArrayMax) + 2; \quad (4.5)$$

4.3.7 Cosine calculation

A method was implemented to compute the cosine function $\cos(2 * \pi * i/N)$. A set of results for *i* from 0 to *N* were calculated using double precision format, for a given input *i*, the double precision cosine result is converted into a fixed-point format and stored in the *Fixed* object, note that it is rounded to the target operand's precision during conversion. From the application program's point of view, it is a look up table implementation of the cosine function. The following is the simplified pseudo code:

```
Fixed Fixed::mcos(int i, int N)
{
    cosResult = cos(2.0 * PI * i / N);
    result = Fixed(this->IntegerSize, this->FractionSize, cosResult);

    return result;
}
```

4.4 Summary

A fixed-point class is developed to simulated fixed-point arithmetic, overloading is used, the fixed-point simulation program is very similar to a corresponding floating-point description. In this chapter, some features and implementation, which are convenient for quantization effect analysis, are introduced, e.g. automatic dynamic range monitoring, automatic quantization error calculation. A look up table implementation of an *cosine* function was presented. This class was used to simulate a fixed-point isolated word recognition system which will be introduced in a later chapter.

Chapter 5

Speech recognition background

5.1 Introduction

To analyze the quantization effects in a non-trivial example, an isolated word recognition system was studied. In this chapter, the isolated word recognition system is introduced.

This chapter is organized as follows. An overview of the isolated word recognition system is presented in Section 5.2, the system is constructed based on the linear predictive coding, vector quantization and hidden Markov model. Section 5.3 introduce the linear predictive coding model applied in speech. In Section 5.4, vector quantization is introduced while Section 5.5 explain the hidden Markov model used to calculate the score of input speech. The last section is a summary.

5.2 Isolated word recognition system overview

There are many hardware implementations of isolated word recognition systems, irrespective of the implementations, trade-offs between performance and complexity always exists. In order to get higher recognition accuracy, some complex models can be used, on the other hand, simple models can be used, but the recognition accuracy will be lower. In this section, the isolated word recognition system used in this work will be introduced.

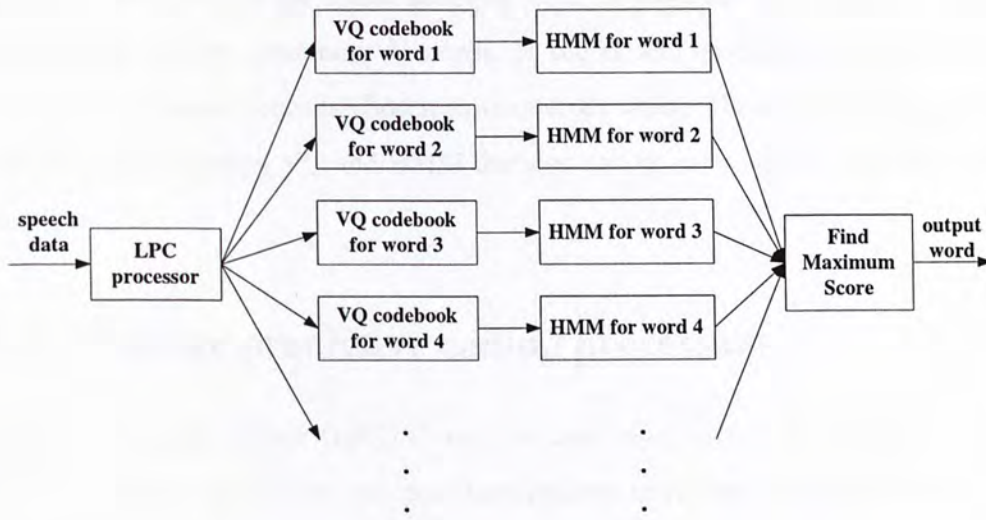


Figure 5.1: Isolated word recognition system

Figure 5.1 is the block diagram of the isolated word recognition system. The system contains three components: the linear predictive coding (LPC) processor, the vector quantizer (VQ) and the hidden Markov model (HMM) decoder. In the system, a common LPC processor was used for all word models, each word model has one VQ and one HMM decoder, hence for an N -word isolated word recognition system, N VQs and N HMM decoders are required. All states of the HMM decoder share the same VQ codebook.

Vectors of the linear predictive cepstral coefficients (LPCCs) were extracted from the input speech data by an common LPC processor. One vector of the LPCC represents the spectrum of an all-pole model that can best model the speech spectrum over a certain period. The LPCC vectors were passed to a vector quantizer, which transforms the continuous data into a discrete representation. This process chooses the best codebook vector to represent an input LPCC vector, a sequence of codebook indices that specify the corresponding codebook vectors having minimum distances with the LPCC vectors is produced. A HMM decoder was used to

calculate the score for the vector quantizer's output sequence. For an isolated word recognition system containing N words, N scores will be obtained and the word with the maximum score is chosen as the output word. The detailed background of the LPC processor, VQ and HMM decoder will be introduced in the following sections.

5.3 Linear predictive coding processor

Linear predictive coding (LPC) theory has been used in speech recognition system for many years, a large number of recognizers were constructed based on LPC theory. It is because LPC has the following advantages:

1. LPC provides a good approximation to speech signal, it is more effective for voiced regions, and acceptable for unvoiced regions [LB93].
2. The mathematical calculation in LPC is simple, and is suitable for both software and hardware implementations.

In the past, due to the limitation of hardware technology, reaching real time performance was very difficult, and the second point made it easier to reach real time performance.

5.3.1 The LPC model

In an LPC model, speech sample $s(m)$ at time m can be approximated as a linear combination of the previous t speech samples:

$$s(m) = \sum_{n=1}^t a_n s(m-n) + Gu(m) \quad (5.1)$$

where $Gu(m)$ is an excitation term. Transformed into the z -domain, we obtain the transfer function:

$$H(z) = \frac{1}{1 - \sum_{n=1}^t a_n z^{-n}} \quad (5.2)$$

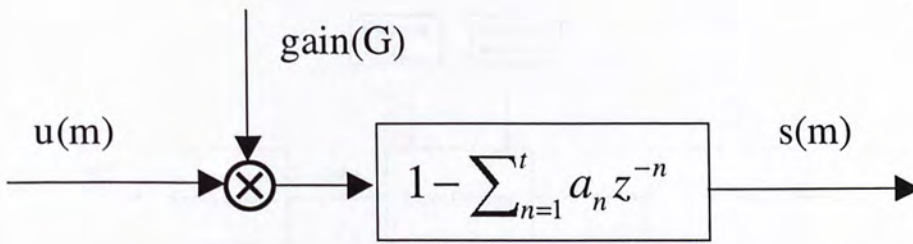


Figure 5.2: LPC model of speech

As shown in Figure 5.2, the normalized excitation source $u(m)$ is scaled by the gain G . In speech recognition, the LPC feature analysis finds the filter coefficients a_n that can best model the speech data, which are used for further processing in the recognition process. It is noted that, the higher the filter order, the better the spoken sounds it can model.

5.3.2 The LPC processor

The LPC processor is used to find the filter coefficients a_n , the processing, called the LPC feature analysis, contains six operations, which are preemphasis, frame blocking, windowing, autocorrelation, LPC analysis, conversion to cepstral coefficients. Figure 5.3 shows the block diagram of LPC feature analysis including the above operations. The following will introduce each part in detail.

1. Preemphasis: A low-order filter is used in this stage to flatten the input speech signal, typically, a fixed first-order system is widely used:

$$H(z) = 1 - \alpha z^{-1}, \quad 0.9 \leq \alpha \leq 1.0. \quad (5.3)$$

Using this fixed first-order filter, for the input speech signal $s(m)$, we have the output $p(m)$:

$$p(m) = s(m) - \alpha s(m-1), \quad \text{where } \alpha = 0.9375. \quad (5.4)$$

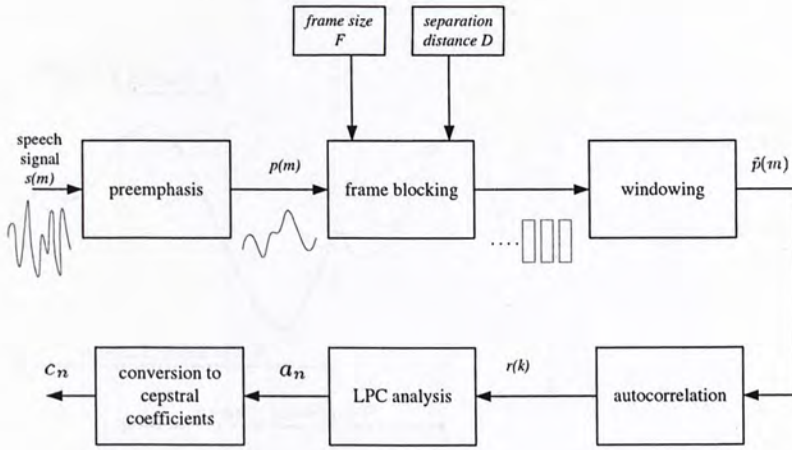


Figure 5.3: Block diagram of the LPC feature analysis

Although 0.95 is commonly used for α , a value of 0.9375 is often chosen in fixed-point implementations [LB93]. In this work, 0.9375 was used for α .

2. Frame blocking: By given the frame size F and separation distance D , the preemphasized speech signal, $p(m)$ is blocked into a number of frames in this stage. Figure 5.4 shows the blocking process, one can see that the continuous speech signal is being cut into pieces, each piece is called a frame. Each frame has frame size F , the next frame started at a distance, D samples, to the previous frame, and overlap $F - D$ samples.

Assume total number of samples is M for an input speech, the number of frames is $N = M/D$, the blocking process can be done by the following equation:

$$x_n(f) = p(nD + f), \quad \text{where } 0 \leq n \leq N - 1, \quad 0 \leq f \leq F. \quad (5.5)$$

3. Windowing: After frame blocking, a problem raised, there are discontinuities at the border of each frame, windowing is used to solve this problem. The most widely used method is the Hamming windowing:

$$\tilde{p}_n(f) = (0.54 - 0.46 \cos(\frac{2\pi f}{F-1}))x(f), \quad \text{where } 0 \leq f \leq F - 1. \quad (5.6)$$

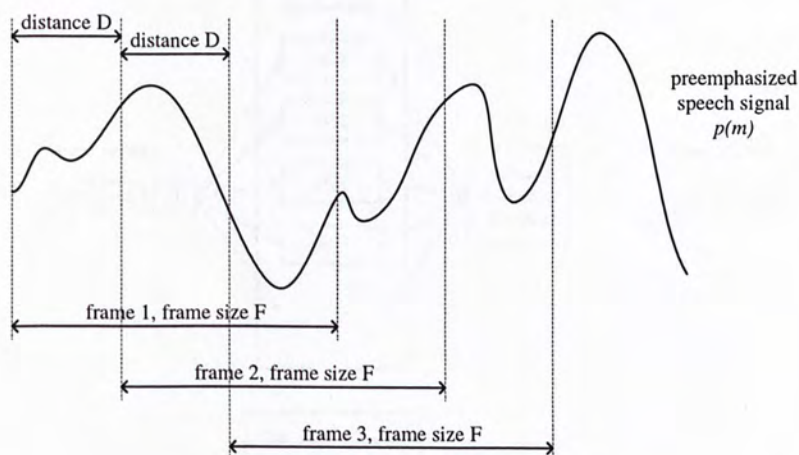


Figure 5.4: Frame blocking process

4. Autocorrelation analysis: The data after windowing is further autocorrelated using the following equation:

$$r_n(k) = \sum_{f=0}^{F-1-k} \tilde{p}_n(f) \tilde{p}_n(f+k), \quad \text{where } 0 \leq k \leq t. \quad (5.7)$$

5. LPC analysis: This process will calculate the filter coefficients a_n after autocorrelation, the Durbin's algorithm is usually used [LB93].

$$E^{(0)} = r_n(0) \quad (5.8)$$

$$k_i = \frac{r_n(i) - \sum_{j=1}^{i-1} \alpha_j^{(i-1)} r_n(|i-j|)}{E^{(i-1)}}, \quad 1 \leq i \leq t \quad (5.9)$$

$$\alpha_i^{(i)} = k_i \quad (5.10)$$

$$\alpha_j^{(i)} = \alpha_j^{(i-1)} - k_i \alpha_{i-j}^{(i-1)}, \quad 1 \leq j \leq i-1 \quad (5.11)$$

$$E^{(i)} = (1 - k_i^2) E^{(i-1)} \quad (5.12)$$

$$a_q = \alpha_q^{(t)}, \quad 1 \leq q \leq t \quad (5.13)$$

6. Conversion to cepstral coefficients: The LPC coefficients a_n were converted to cepstral coefficients. Using cepstral coefficients as features in speech recognition have been shown to be more reliable [LB93]. The conversion involves

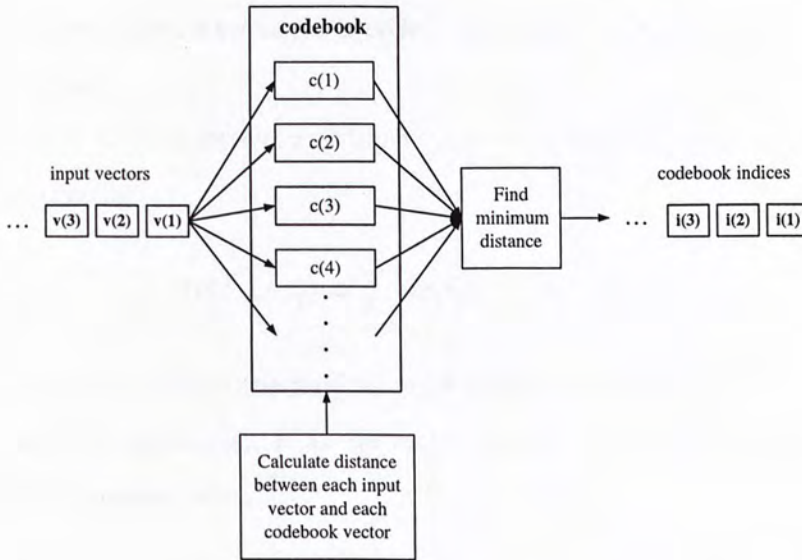


Figure 5.5: Vector quantization process

the following calculations:

$$c_n = a_n + \sum_{k=1}^{n-1} \left(\frac{k}{n}\right) c_k a_{n-k}, \quad \text{where } 1 \leq n \leq t. \quad (5.14)$$

5.4 Vector quantization

One advantage of using vector quantization is reducing the data rate, the high input speech data rate is transferred into a low data rate representation. The codebook of VQ is a discrete representation of continuous speech data. The VQ will find a codebook index specifying the codebook vector that best represents a given spectral vector. The codebook vectors can be obtained by clustering a set of training vectors, thus the codebook vectors representing the spectral variability observed in the training set [LB93], the K-means clustering algorithm is used in this work.

Figure 5.5 shows the vector quantization processing, for an input vector sequence $V\{v(1), v(2), v(3), \dots, v(N)\}$, VQ will calculate the vector distance between each vector in codebook $C\{c(1), c(2), c(3), \dots, c(P)\}$ and each input vector

$v(n)$, and the codebook index with minimum distance will be chosen as output. After vector quantization, a sequence of codebook indices $I\{i(1), i(2), i(3), \dots, i(N)\}$ will be produced.

The vector distance between an input vector $v(n)$ and each vector in codebook is calculated using:

$$d(v(i), c(j)) = \sum_{k=1}^K [v(i)(k) - c(j)(k)]^2, \quad (5.15)$$

where $v(i)(k)$ is the k th element of the input vector $v(i)$, $c(i)(k)$ is the k th element of the codebook vector $c(i)$, K is the vector length. The following is the pseudo code for vector quantization.

```

for p from 1 to codebook_size {
  distance(p) = 0;
  for k from 1 to vector_length {
    temp = (v(n)(k) - c(p)(k)) * (v(n)(k) - c(p)(k));
    distance(p) = distance(p) + temp;
  }
}
i(n) = arg min_p (distance(p));

```

In the above pseudo code, $i(n)$ is the n th element of the output codebook indices sequence as shown in Figure 5.5. Similar input vectors are clustered together in vector quantization, one can see that the data rate is reduced significantly. This advantage will benefit most HMM based speech recognition system using vector quantization, because HMM decoding is time consuming, lower data rate will make real time performance become realizable in the past. Furthermore, the storage size is reduced for spectral analysis data, only the codebook will be stored, as a result, it is more suitable for hardware implementation.

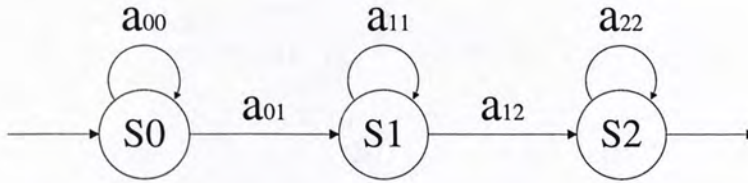


Figure 5.6: Left-to-Right HMM

5.5 Hidden Markov model

Hidden Markov models (HMMs) are widely used in modern speech recognition systems because HMM-based speech recognition systems have proven to yield high recognition accuracy. The Viterbi algorithm is used to find the most likely state sequence and likelihood score for a given observation sequence. In this section, the background theory of HMM and the Viterbi algorithm will be introduced.

Given an observation sequence $O = (o_1 o_2 \dots o_T)$, HMM decoding calculates $P(O|\lambda)$, which is the probability of the input observation sequence for a given model λ , the result means how much chance the utterance represented by model λ will produce the observation sequence O .

Figure 5.6 shows a basic three-state left-to-right HMM. A HMM is a probabilistic finite state machine (FSM) and has a set of state transaction and observation probabilities. The state transaction probability is the probability of state transaction from one to another, and the observation probability is the probability that a state emit a particular observation. In this figure, S_0, S_1, S_2 are the states, a_{ij} is the probability of state transaction from i to j . Figure 5.7 is the trellis representation showing all possible state transaction paths.

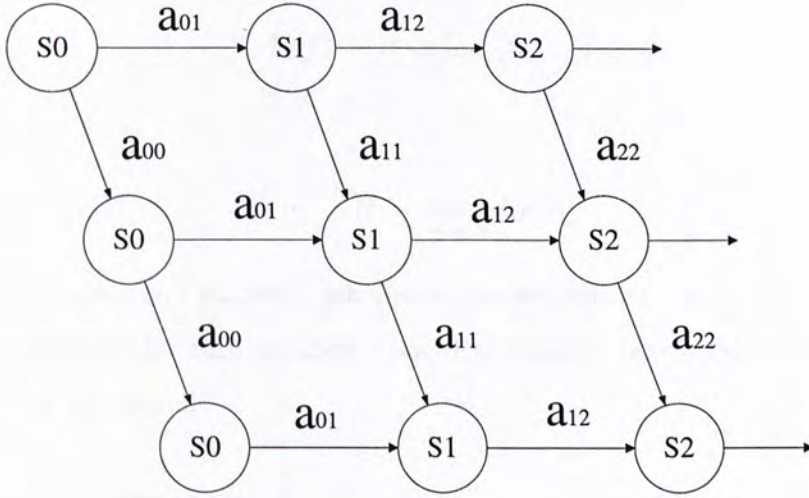


Figure 5.7: Trellis representation of Left-to-Right HMM

Traditional Viterbi algorithm

$P(O|\lambda)$ of course can be calculated by enumerating all possible paths in the trellis diagram (see Figure 5.7) over the entire observation sequence. Totally, there are N^T possible paths, where N is the number of HMM states and T is the length of the observation sequence. Assume $q = (q_1, q_2, q_3, \dots)$ is one of the state traversal path, the probability can be calculated as follow:

$$\begin{aligned}
 P(O|\lambda) &= \sum_{\text{all } q} P(O|q, \lambda)P(q|\lambda) \\
 &= \sum_{\text{all } q} P(O, q|\lambda)
 \end{aligned} \tag{5.16}$$

In practice, an alternative approach, called the Viterbi algorithm associated with a *max* function is used. Where $P(O|\lambda)$ is approximated by the probability associated with the best state sequence $q = (q_1, q_2, q_3, \dots)$ that maximizes $P(O, q|\lambda)$.

The iterative process to calculate the score for an observation sequence $O = (o_1 o_2 \dots o_T)$ is shown below. Assume the observation probability for an input symbol o_t at state j is $p_j(o_t)$, the score along the best state sequence at time t and ends in state j is $h_t(j)$, the number of HMM states is N .

1. Looping:

$$h_t(j) = \max_{1 \leq i \leq N} [h_{t-1}(i) a_{ij}] p_j(o_t) \quad (5.17)$$

2. Stop:

$$H = \max_{1 \leq i \leq N} [h_T(i)] \quad (5.18)$$

By using the *max* function, calculation can be reduced. But since multiplication is performed for each iteration, underflow problem may occur, an alternative approach is introduced.

Alternative Viterbi approach

To overcome the underflow problem, taking logarithms in Equation 5.17, results in the following procedures:

1. Looping:

$$\tilde{h}_t(j) = \max_{1 \leq i \leq N} [\tilde{h}_{t-1}(i) + \tilde{a}_{ij}] + \tilde{p}_j(o_t) \quad (5.19)$$

2. Stop:

$$\tilde{H} = \max_{1 \leq i \leq N} [\tilde{h}_T(i)] \quad (5.20)$$

Using this approach, computation is reduced since the main operations are addition rather than multiplication. This approach is very suitable for hardware implementation, and was adopted in this work.

5.6 Summary

Background of an isolated word recognition system was introduced in this chapter. The isolated word recognition consists of the LPC processor, VQ and HMM decoder using the Viterbi algorithm, the output of HMM decoder are the word scores, and the highest is taken to be the recognized word.

Chapter 6

Optimization

6.1 Introduction

To perform wordlength optimization of fixed-point system, one difficulty is that, the objective function cannot be stated as explicit functions of the design variables for most of implementations. For example, in speech recognition, the recognition accuracy cannot be stated in terms of wordlength. As a result, traditional analytical methods is difficult to be applied to all systems and a simulation searching-based method can be used. The cost is obtained through simulation, and a searching method is applied to find the optimal solution.

This chapter is organized as follows. In Section 6.2, the simplex method is introduced. Section 6.3 present the one-dimensional optimization approach, which significantly reduces the search space. Section 6.4 is a summary.

6.2 Simplex Method

The Nelder-Mead simplex method [JR65], published in 1965, is widely used in non-linear unconstrained optimization. The Nelder-Mead method attempts to minimize an object function of n variables, the minimization process depends on the function value, no derivative information is required, the Nelder-Mead thus was classed as

direct search method [Sin96]. Because of these features, it can be regarded as a general optimization method for wordlengths optimization in fixed-point systems.

In simplex method, a set of $n + 1$ initial point is formed for n -dimensional space, then reflection, expansion and contraction process are applied to find optimal solution.

6.2.1 Initialization

At the beginning, the user should supply a base point and guess scale. A set of $n + 1$ initial point is generated using the following equations:

$$X_0 = X_u \quad (6.1)$$

$$X_i = X_u + pu_i, \quad i = 1, 2, \dots, n \quad (6.2)$$

In the above equations, X_u is the base point and p is the guess scale, u_i is the unit vector along the i th coordinate axis. In the geometric figure's point of view, the $n + 1$ initial points formed is called a simplex.

For example, if $X_0 = [4, 5, 6]$ and $p = 2$, the initial points are:

$$X_0 = X_u = [4, 5, 6]$$

$$X_1 = X_u + pu_1 = [6, 5, 6]$$

$$X_2 = X_u + pu_2 = [4, 7, 6]$$

$$X_3 = X_u + pu_3 = [4, 5, 8]$$

6.2.2 Reflection

Among all the $n + 1$ points X_0, X_1, \dots, X_n in the simplex, if X_w is the point with worst value of the objective function, it is expected that X_r obtained by reflecting X_w to the opposite side, will yield a better value. Based on the above, a new simplex is formed by accepting the new point X_r and deleting X_w .

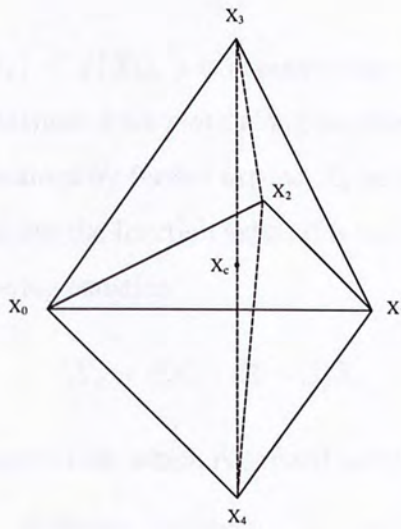


Figure 6.1: Reflection

The reflection process can be illustrated by Figure 6.1, in this figure, the old simplex is constructed by X_0, X_1, X_2, X_3 , assume that X_3 has the worst objective function value. After applying reflection, a new point X_4 is obtained, X_0, X_1, X_2, X_4 will form the new simplex. The following equation can be used to calculate the reflected point:

$$X_r = (1 + \alpha)X_c - \alpha X_w \quad (6.3)$$

where X_w is the point which has the worst objective function value and X_c is the centroid of all the points X_i for $i = 0, 1, 2 \dots n$, except $i = w$. In Figure 6.1, X_c is the centroid of X_0, X_1, X_2 . α is the reflection coefficient, which is defined as follows:

$$\alpha = \frac{\text{distance between } X_c \text{ and } X_r}{\text{distance between } X_c \text{ and } X_w} \quad (6.4)$$

For the standard Nelder-Mead method, a nearly universal choice for α is 1. Using reflection, if the function value $f(X_r) < f(X_w)$ and $f(X_r) > f(X_b)$, where X_b is the point yield best function value, X_w is replaced by X_r to form a new simplex.

6.2.3 Expansion

Using reflection, if $f(X_r) < f(X_b)$, it is expected that a point which has a better function value can be obtained if we move along the direction pointing from X_c to X_r . A new point X_e , obtained by further expand X_r in the direction pointing from X_c to X_r , will be used to test the function value, this is called expansion. X_e can be obtained using the following equation:

$$X_e = \beta X_r + (1 - \beta)X_c \quad (6.5)$$

β is the expansion coefficient, which is defined as follows:

$$\beta = \frac{\text{distance between } X_c \text{ and } X_e}{\text{distance between } X_c \text{ and } X_r} \quad (6.6)$$

One can see that β must be larger than 1, for standard Nelder-Mead method, a good choice is 2.

If the expansion point is a new best point, that means $f(X_e) < f(X_b)$, X_w is replaced by X_e and the reflection process will restart again. Otherwise, if $f(X_e) > f(X_b)$, X_w is replaced by X_r , and the reflection process is restarted.

6.2.4 Contraction

After reflection, X_w will be replaced by X_r if the following two conditions are satisfied for a reflection point X_r :

- (1) $f(X_r) > f(X_i)$, where $i = 0, 1, 2, \dots, n$, $i \neq w$
- (2) $f(X_r) < f(X_w)$

X_w will remain unchanged if only the following condition satisfy for a reflection point X_r :

$$f(X_r) > f(X_w)$$

Contraction is then applied to contract the simplex, a new point, generated using the following equation, will be used to test the objective function.

$$X_t = \gamma X_w + (1 - \gamma)X_c \quad (6.7)$$

where γ is the contraction coefficient, which is defined as follows:

$$\gamma = \frac{\text{distance between } X_c \text{ and } X_t}{\text{distance between } X_c \text{ and } X_w} \quad (6.8)$$

For standard Nelder-Mead method, γ is usually set to $\frac{1}{2}$. The reflection process will be restarted depending on the function value $f(X_t)$ as follows:

- $f(X_t) < \min[f(X_r), f(X_w)]$: That means the contraction was a success, replace X_w by X_t , and restart the reflection process.
- $f(X_t) \geq \min[f(X_r), f(X_w)]$: Contraction is a failure, for $i = 0, 1, 2, \dots, n$, replace X_i by $(X_i + X_b)/2$, and restart the contraction.

6.2.5 Stop

The reflection process will stop if the number of iterations reaches a maximum number, or if the following condition is satisfied:

$$2 \times \frac{|f(X_w) - f(X_b)|}{|f(X_w)| + |f(X_b)|} < \varepsilon \quad (6.9)$$

where ε is an user defined tolerance.

6.3 One-dimensional optimization approach

When performing wordlength optimization, one difficulty is that, the search space is very large. To overcome this problem, instead of optimizing global system, each variable is exhaustively searched between given bounds independently, which will

result in search space reduction. This is a trade-off between accuracy and execution time. The one-dimensional optimization approach may get trapped in a local minima.

6.3.1 One-dimensional optimization approach

Detailed implementation of one-dimensional optimization approach can be summarized as the following pseudo code, for a system consist of n variables $X_1, X_2, X_3, \dots, X_n$, each variable has a wordlength search space bound $[L(i), U(i)]$ for $i = 1, 2, 3, \dots, n$, where $L(i)$ is the lower bound of X_i and $U(i)$ is the upper bound of X_i .

```

\\ Initialization
For i = 1 to n {
  WordLength(i) = U(i);
}

MinFunctionValue = f(U(1), U(2), U(3), ..., U(n));
\\ Minimize each variable alternatively
For i = 1 to n {
  \\ Sweep wordlength of  $X_i$ 
  For WordLength(i) = U(i) to L(i) {
    CurrentFunctionValue = f(WordLength(1), WordLength(2), ..., WordLength(n));
    \\ Store the minimum wordlength
    if CurrentFunctionValue < MinFunctionValue then {
      MinFunctionValue = CurrentFunctionValue;
      MinWordLength(i) = WordLength(i);
    }
  }
  WordLength(i) = MinWordLength(i);
}

```

In the above pseudo code, $MinWordLength(i)$ is the minimum wordlength of X_i .

The one-dimensional optimization can be illustrated by Figure 6.2, assume a system consist of three variables X_1, X_2, X_3 , the optimization process is broken into three parts. From the left to the right, suboptimize the wordlength of X_1, X_2 and X_3 in sequence. When optimizing the wordlength of one variable, the others are

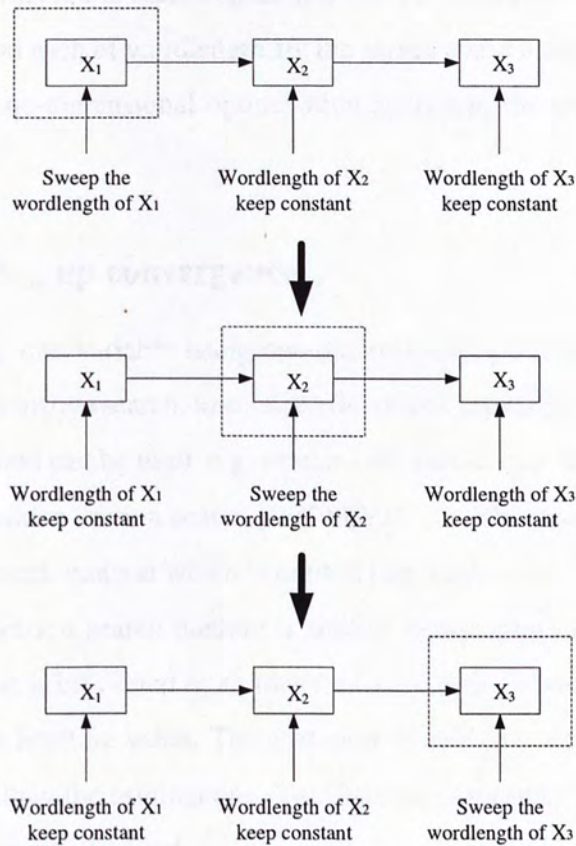


Figure 6.2: One-dimensional optimization

keep constant. Exhaustive search is used to sweep the wordlength in each dimension as shown in the pseudo code.

6.3.2 Search space reduction

Using the one-dimensional optimization approach, the search space is reduced significantly. Assume a system consists of n variable $X_1, X_2, X_3, \dots, X_n$, each has uniform distance b between $L(i)$ and $U(i)$, that means:

$$\text{constant} = b = U(i) - L(i), \quad \text{where } i = 1, 2, 3, \dots, n. \quad (6.10)$$

Original, using exhaustive search, the search space is b^n . Using the one-dimensional

optimization approach, the search space is $b \times n$. For example, a system consisting of 20 variables and each of wordlength 16, the search space using exhaustive search is 20^{16} . Using one-dimensional optimization approach, the search space is only 20×16 .

6.3.3 Speeding up convergence

When optimizing one variable using one-dimensional optimization approach, instead of using exhaustive search, to enhance the search convergence, some less brute force search method can be used, e.g. search with accelerated step size [Sin96], bisection search, golden section search [WSWB92], etc. This section introduces the golden section search method which is used in this work.

The golden section search method is similar to bisection method [WSWB92], where the solution is bracketed in an interval (a, c) , then an intermediate point b is chosen to test the function value. The next interval will converge to (a, b) or (b, c) , which is smaller than the original one. This process is repeated until the interval is smaller than an specified bound.

Instead of keeping track of two points in the bisection method, the golden section search method keeps track of three point in each iteration. As illustrated in Figure 6.3, originally, the minimum is bracketed by (X_1, X_2) , and X_3 is the intermediate point. The function is evaluated at X_4 , which is the intermediate point of (X_1, X_2) , since $f(X_4) < f(X_1)$, $f(X_1)$ is replaced by X_4 , the minimum is bounded by (X_4, X_2) . The function is then evaluated at X_5 , which is the intermediate point of (X_3, X_2) , since $f(X_5) < f(X_2)$, X_2 is replaced by X_5 , the minimum is bracketed by (X_4, X_5) . This process continues until the bracket is small than an specified interval.

Assume the initial three points are a, b, c , the golden section search method can be summarized as follows:

$$X_0 = a;$$

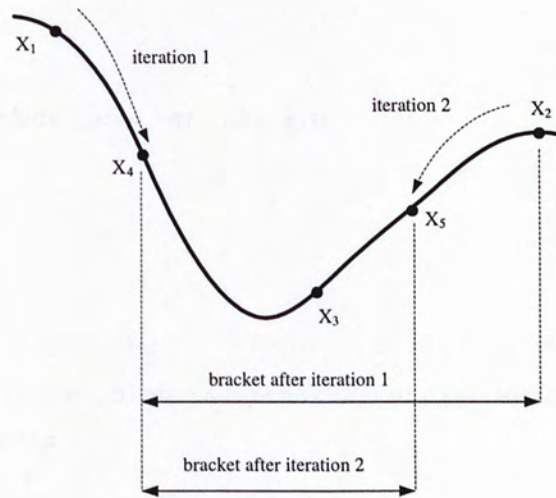


Figure 6.3: Golden section search

```

 $X_3 = c;$ 
if interval  $(b, c)$  smaller than interval  $(a, b)$  then {
   $X_2 = b;$ 
   $X_1 =$  intermediate point of  $(a, b);$ 
} else {
   $X_1 = b;$ 
   $X_2 =$  intermediate point of  $(b, c);$ 
}

```

```

\\ Evaluate the two intermediate points
 $f1 = f(X_1);$ 
 $f2 = f(X_2);$ 
\\ Execute iteratively
while interval  $(X_0, X_3)$  larger than a constant {
  if  $f2 > f1$  then {
     $X_3 = X_2;$ 
     $X_2 = X_1;$ 
     $X_1 =$  intermediate point of  $(X_0, X_3);$ 
     $f2 = f1;$ 
     $f1 = f(X_1);$ 
  }
}

```

```

    } else {
       $X_0 = X_1;$ 
       $X_1 = X_2;$ 
       $X_2 = \text{intermediate point of } (X_0, X_3);$ 
       $f1 = f2;$ 
       $f2 = f(X_2);$ 
    }
  }

  \\ Now, the minimum point is either  $X_1$  or  $X_2$ , which are the two
intermediate points
  if  $f2 < f1$  then {
    Minimum point is  $X_2;$ 
  } else {
    Minimum point is  $X_1;$ 
  }
}

```

In the above pseudo code, $f1$ and $f2$ is used to store the function value of the two intermediate points. Finally, when the outer bound (X_0, X_3) smaller than a specified interval, the looping is terminated. The minimum point is either X_1 or X_2 , after comparing their function values, the minimum point can be obtained.

6.4 Summary

Optimization background was introduced in this chapter. Two optimization approaches, the simplex method and one-dimensional optimization approach, were introduced. The search space is reduced by using a one-dimensional optimization approach. Furthermore, the golden section method can be used to speed up the optimization.

Chapter 7

Word Recognition System Design

Methodology

7.1 Introduction

A framework was introduced to address the quantization issues of fixed-point systems, flexibility and easy to be extensible are the major consideration of this framework. It is applied to an isolated word recognition system to explore the utility of this approach. In this chapter, detailed design of the framework is introduced.

This chapter is organized as follows. In Section 7.2, the architecture of framework is introduced. Section 7.3 present how to apply this framework to an isolated word recognition system. The last section is a summary.

7.2 Framework design

Figure 7.1 shows the block diagram of the framework, which consists of a fixed-point class and an optimizer. Fixed-point application is simulated using the fixed-point class, and the optimizer is used to find optimal wordlength.

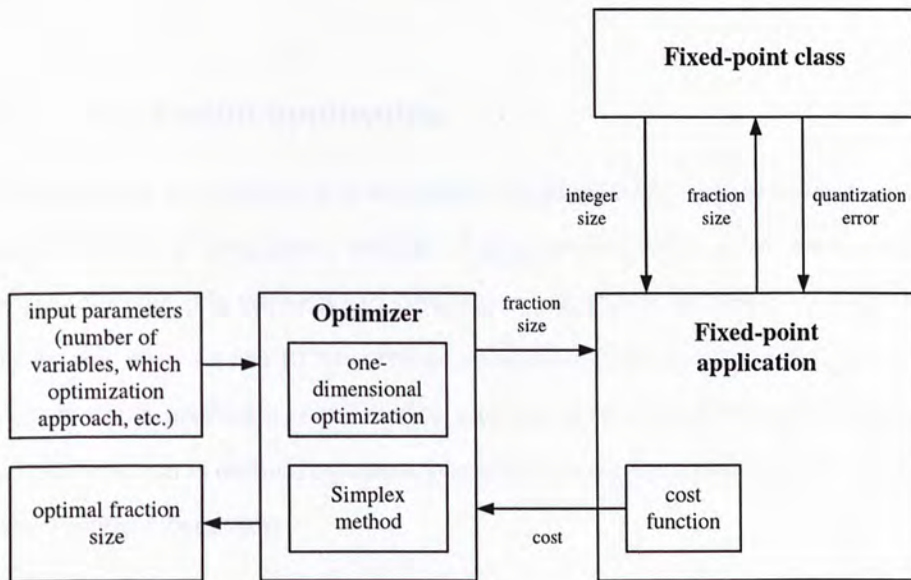


Figure 7.1: Block diagram of the framework

7.2.1 Fixed-point class

As introduced in the previous chapter, the fixed-point class was developed using the C++ language. Currently, it can simulate fixed-point arithmetic including addition, subtraction, multiplication and division, cosine operation is implemented using a look up table.

The fixed-point class can simulate fixed-point arithmetic at a precision specified by the user, i.e. the user can specify the fraction size for each variable. Quantization error, which is calculated using floating-point calculation result as a reference, can be obtained by the class automatically.

Furthermore, the fixed-point class can monitor the dynamic range of each variable during calculation, integer size is calculated using the range information obtained by the class during simulation.

Using an object oriented concept and overloading, the fixed-point class is extensible, new overloading of operators can be appended by adding new methods in

the fixed-point class and do not affect the design of the optimizer and application program.

7.2.2 Fixed-point application

The fixed-point application is a simulation program which implements the desired functionality of a fixed-point system. Using overloading, it has been shown by previous chapter, it is very easy to simulate an algorithm and the fixed-point implementation is very similar to its corresponding C++ floating-point description.

Users can construct a cost function and return the cost as shown in Figure 7.1. The cost function is defined by users, because the cost function may vary depending on the system's behaviors.

7.2.3 Optimizer

The optimizer is developed using the Perl language, which can perform wordlength optimization using two approaches, the one-dimensional optimization approach and simplex method, both optimization methods process based on a user defined cost function.

Some parameters, e.g. using which optimization approach, number of variable and initial guesses, should be provided by the user. The optimizer executes the fixed-point application iteratively with different configurations of fraction size and costs are determined.

Figure 7.2 illustrates how the optimizer executes the fixed-point application iteratively. The optimizer reads in a function handler, and call this function iteratively, within the function, the fixed-point application will be executed and the cost will be calculated.

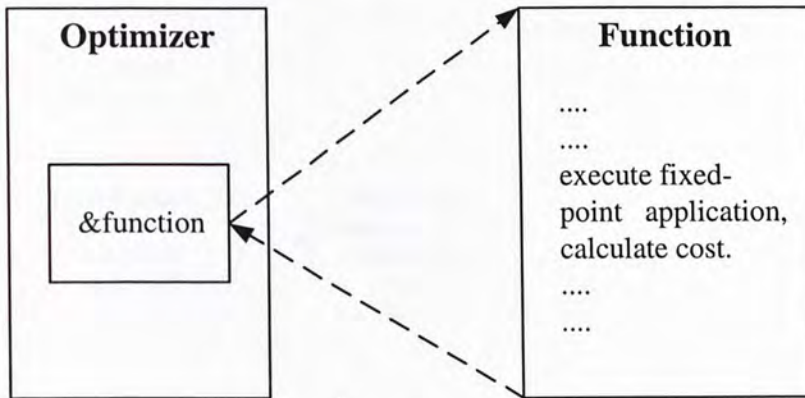


Figure 7.2: Optimizer executes fixed-point application iteratively

7.3 Speech system implementation

This framework was applied to an isolated word recognition system which was introduced in the previous chapter. The isolated word recognition system consists of three parts, the LPC processor, the vector quantizer and HMM decoder. A user application program was developed to simulate the isolated word recognition system, all arithmetic operations were handled by the fixed-point objects. Minimum integer size can be obtained by the fixed-point class through simulation, optimization was done to minimize the fraction size. The optimization proceed based on a cost function which take recognition accuracy and hardware cost into account. By minimize the integer size and fraction size, minimum hardware cost implementation can be found. The above process is illustrated in Figure 7.3.

7.3.1 Model training

The VQ codebook and HMM parameters need to be trained, the trained model will be used during recognition. One set of utterances from the TIMIT TI 46-word database [LDC] containing 20 words from 8 males and 8 females were used for both training and recognition. There were 26 utterances for each word, 10 utterances

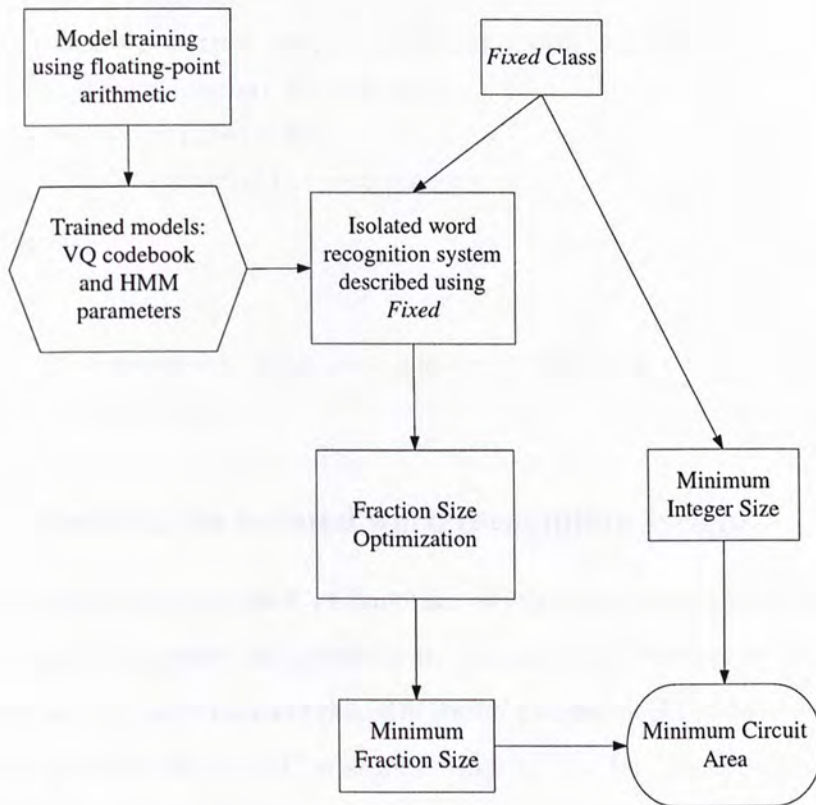


Figure 7.3: Overview of isolated word recognition system optimization flow

were used for training and 16 utterances were used for recognition.

A frame size of 30ms was chosen for the frame blocking process in the LPC processor and 12th order LPCCs were used. The sampling frequency for this set of TIMIT utterances was 12.5KHz. Thus the number of samples in each frame is:

$$12500 \text{ samples/second} \times 30 \text{ ms} = 375 \text{ samples.} \quad (7.1)$$

The VQ codebook and HMM parameter training was done using floating-point arithmetic. To choose the codebook size and number of HMM states, different configurations of codebook size and number of states were tested. The configuration with maximum recognition accuracy was selected. The selection process can be described by the following pseudo code.

```
for different codebook size {
```

```

train VQ codebook;
calculate VQ output sequence using trained codebook;
for different number of HMM states {
    train HMM parameters;
    calculate recognition accuracy;
}
}

```

choose the codebook size and number of HMM states yield highest recognition accuracy;

7.3.2 Simulate the isolated word recognition system

A user program written in the C++ language was developed to simulate the isolated word recognition system. All operands are represented in fixed-point object, overloading was used, the following program shows a segment of the codes to simulate the autocorrelation step in LPC processor which is described by previous chapter.

```

...
...

int m , n;

...
...

for (m = 0; m <= p_order; m++)
{
    autosum = 0.0;
    for (n = 0; n < win_size-m; n++) {

        wswsF = cwsF[n] * cwsF[n+m];

```

```

        autosum = autosum + wswsF;
    }
    R[m] = autosum;
}
...
...

```

In the above codes, *autosum* and *wswsF* are fixed-point object type *Fixed*, *cwsF* and *R* are array of *Fixed*. One can see that using overloading, the program is similar to a normal floating-point implementation, and it is very easy for a user to simulate the algorithm using the *Fixed* class.

7.3.3 Hardware cost model

In the calculation of hardware costs, only arithmetic components are taken into account. Since this work focus on wordlength optimization, the change in wordlength will mostly affect the size of arithmetic components, and it is assumed that other components, e.g. registers, memories, interfaces, do not occupy significant resources.

When estimating the arithmetic circuit area, since addition, subtraction, multiplication and division can be implemented using adders, circuit area is counted as the number of one-bit full adders used for each arithmetic operation. The following descriptions detail the arithmetic circuit size estimation for each operation.

- *addition/subtraction*: Assume parallel adder/subtractor is used, and the result chooses the maximum integer and fraction size of the two input operands, the number of full one-bit full adders (i.e. the circuit size) used is:

$$\text{Circuit size} = \text{Max}(I1, I2) + \text{Max}(F1, F2), \quad (7.2)$$

where (*I1* and *F1*)/(*I2* and *F2*) are the integer size and fraction size for the first/second operand.

- *multiplication*: Assume parallel multiplier is used. The circuit size of an n bit \times m bit multiplier is:

$$\text{Circuit size} = n \times m. \quad (7.3)$$

- *division*: Assume restoring-division is used. As introduced in the previous chapter, the main operation involved in this algorithm is addition, and the circuit size is same as addition/subtraction:

$$\text{Circuit size} = \text{Max}(I1, I2) + \text{Max}(F1, F2), \quad (7.4)$$

where $(I1$ and $F1)/(I2$ and $F2)$ are the integer size and fraction size for the two input operands.

The total arithmetic circuit size is calculated by summing the circuit size of all operators for the entire isolated word recognition system. For example, to calculate the circuit size for the autocorrelation, pseudo code shown by Section 7.3.2. Assume integer size for $cwsF$, $wswsF$ and $autosum$ are I_c , I_w and I_a respectively, fraction size for $cwsF$, $wswsF$ and $autosum$ are F_c , F_w and F_a respectively. Circuit size for multiplication $cwsF[n] \times cwsF[n + m]$ is:

$$s_1 = (I_c + F_c) \times (I_c + F_c), \quad (7.5)$$

circuit size for addition $autosum + wswsF$ is:

$$s_2 = \text{Max}(I_a, I_w) + \text{Max}(F_a, F_w), \quad (7.6)$$

the total circuit size for the autocorrelation is $s_1 + s_2$.

7.3.4 Cost function

Since this work focuses on how to reach certain recognition accuracy with minimum hardware cost, the cost function will take the circuit size and recognition accuracy into account. The following cost function was used:

$$\text{cost} = \alpha * \text{CircuitSize} + \beta * \text{RegAcy} \quad (7.7)$$

where *RegAcy* is the recognition accuracy calculated using fixed-point arithmetic, and α and β are the weightings of circuit area and recognition accuracy respectively. Note that α and β can be adjusted for different weightings of circuit area and recognition accuracy.

In this work, the following condition was added to compute the cost:

```
if (RegAcy < expectRegAcy) {
    penalty = expectRegAcy - RegAcy;
    cost = cost + VeryLargeValue * penalty;
}
```

where *expectRegAcy* is a user defined expected recognition accuracy. In this work, it is the recognition accuracy of a floating-point system. A penalty is added to the cost when the recognition accuracy is smaller than the expected recognition accuracy, because we want to reach the same recognition accuracy as the floating-point system.

7.3.5 Fraction size optimization

The minimum integer size for each operand can be obtained by the fixed-point class after simulation. The optimization stage will find the minimum fraction size for each operand using the optimizer, which will result in minimum circuit size while achieving the same recognition accuracy as that of a floating-point system.

The optimization process is divided into two stages. In the first stage, it optimizes the fraction size from the entire system's point of view, and then in the second stage, it further optimizes the fraction size of the LPC processor. The Nelder-Mead simplex method [JR65] was used to minimize the hardware cost based on a user defined cost function which takes recognition accuracy and hardware cost into account, finding an implementation which balances hardware cost and recognition accuracy.

System level optimization

To perform optimization, a technique, called variable grouping, was used to reduce the search space. In this stage, the isolated word recognition system is divided into three parts, namely the LPC processor, VQ and HMM decoder, all operands in each part use uniform fraction size, the optimization steps are shown in Figure 7.4, the optimizer was used to find optimal wordlength of each part.

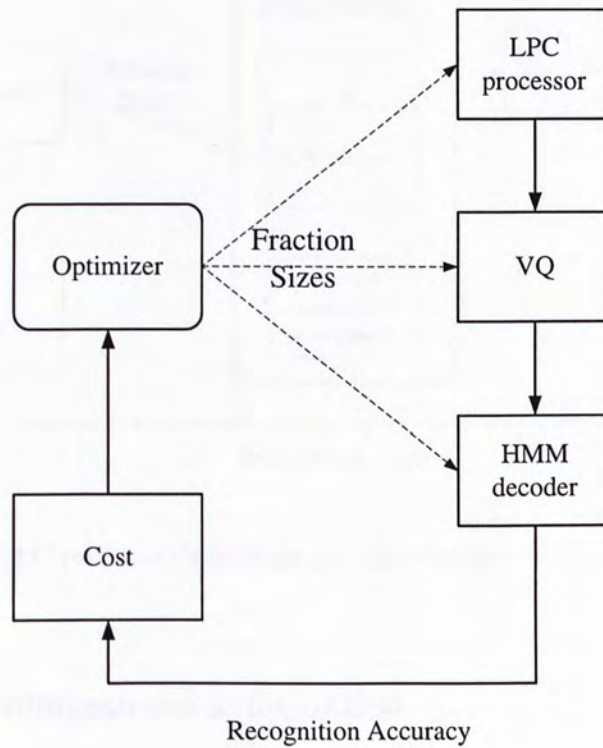


Figure 7.4: System level optimization using simplex method

LPC processor's fraction size optimization

Since the LPC processor occupies most of the hardware resources, using variable grouping, the LPC processor was further divided into four parts, namely preemphasis and windowing, autocorrelation analysis, LPC analysis, and cepstral coefficient

conversion. All operands in each part use uniform fraction size, optimization was done to minimize these four fraction sizes as shown in Figure 7.5.

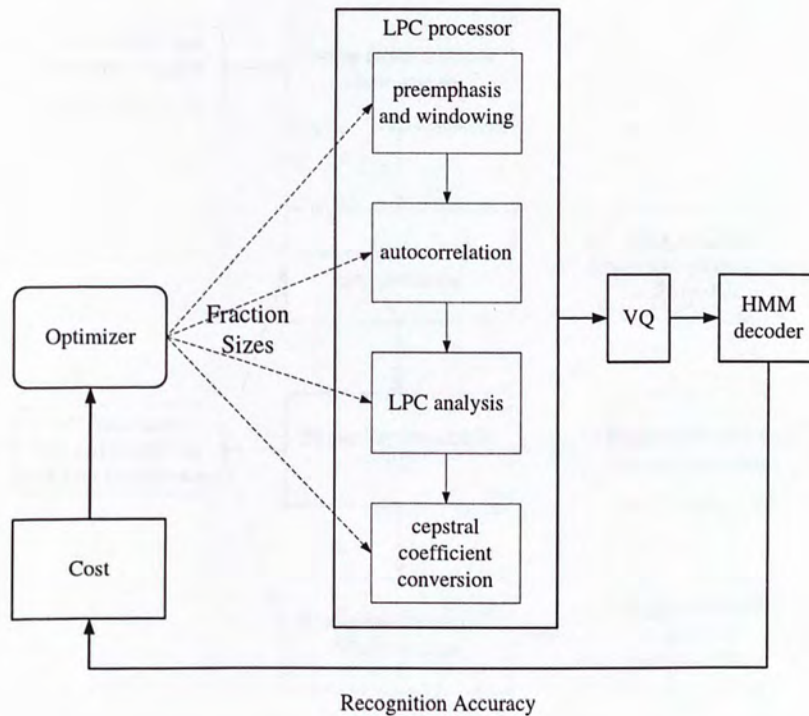


Figure 7.5: LPC processor's fraction size optimization using simplex method

7.3.6 One-dimensional optimization

In order to analyze the optimization behaviors of the simplex method and one-dimensional optimization approach, one-dimensional optimization was applied to system level optimization. Using one-dimensional optimization and variable grouping, the search space is reduced significantly. The isolated word recognition system consists of 48 variables, assume wordlength of each variable is b bits, the search space is $48 * b$ without variable grouping. This becomes $3 * b$ after applying variable grouping. Using variable grouping, the number of wordlength conversion operations in the resulting fixed-point hardware implementation can be reduced, since

the number of distinct wordlengths is reduced. The optimization steps are shown in Figure 7.6.

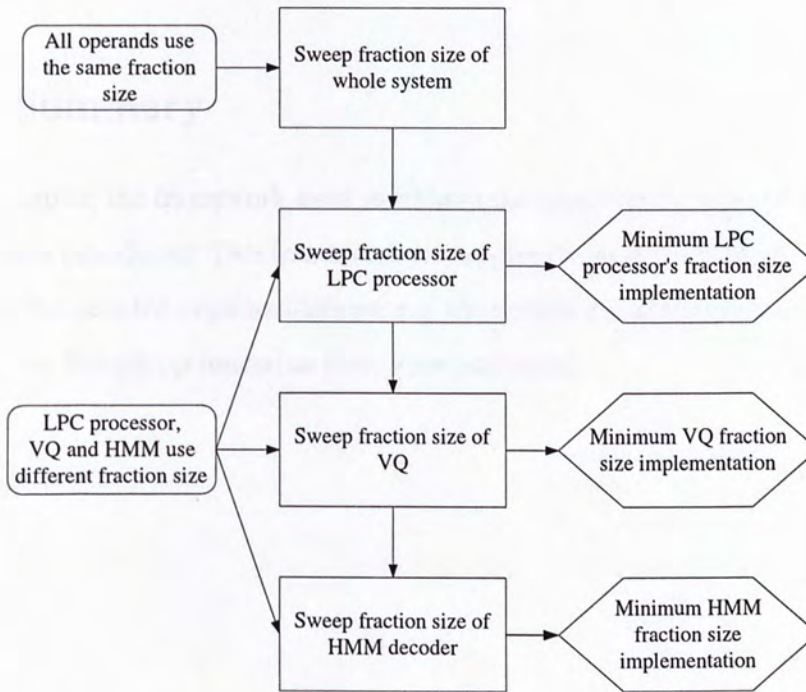


Figure 7.6: System level optimization using one-dimensional optimization

1. Optimizing whole speech system's fraction size: The whole system uses a uniform fraction size, which is varied to find a configuration which yield minimum cost.
2. Optimizing the LPC processor's fraction size: Fix the fraction size of the VQ and HMM decoder, vary the fraction size of the LPC processor to find a configuration which yields minimum cost.
3. Optimizing the VQ's fraction size: Fix the fraction size of the LPC processor and HMM decoder, vary the fraction size of the VQ to find a configuration which yields minimum cost.

4. Optimizing the HMM decoder's fraction size: Fix the fraction size of the LPC processor and VQ, vary the fraction size of the HMM decoder to find a configuration which yields minimum cost.

7.4 Summary

In this chapter, the framework used to address the quantization issue of fixed-point system was introduced. This framework was applied to an isolated word recognition system. The detailed implementations, e.g. the speech model training, cost function design, wordlength optimization flow, were presented.

Chapter 8

Results

8.1 Model training

One set of utterances from the TIMIT TI 46-word database [LDC] containing 20 words from 8 males and 8 females were used, there were 26 utterances for each word, 10 were used for training and 16 were used for recognition.

The isolated word recognition system uses 12th order LPCCs, in order to choose the VQ codebook size and number HMM state, using the method introduced in previous chapter, different configurations of codebook size and number of state were tested, the configuration with maximum recognition accuracy was selected.

Figure 8.1 shows the recognition accuracy for different configurations of VQ codebook size and number of HMM states. In principle, the smaller codebook size and number of states, the better, since the hardware cost can be reduced. In this figure, one can see that the improvement of recognition accuracy becomes insignificant when number of HMM states and codebook size increased. Practically, codebook size 64 and 12 HMM states were used, this configuration doesn't yield maximum recognition, but this configuration can reach a certain level of recognition accuracy with relative low cost.

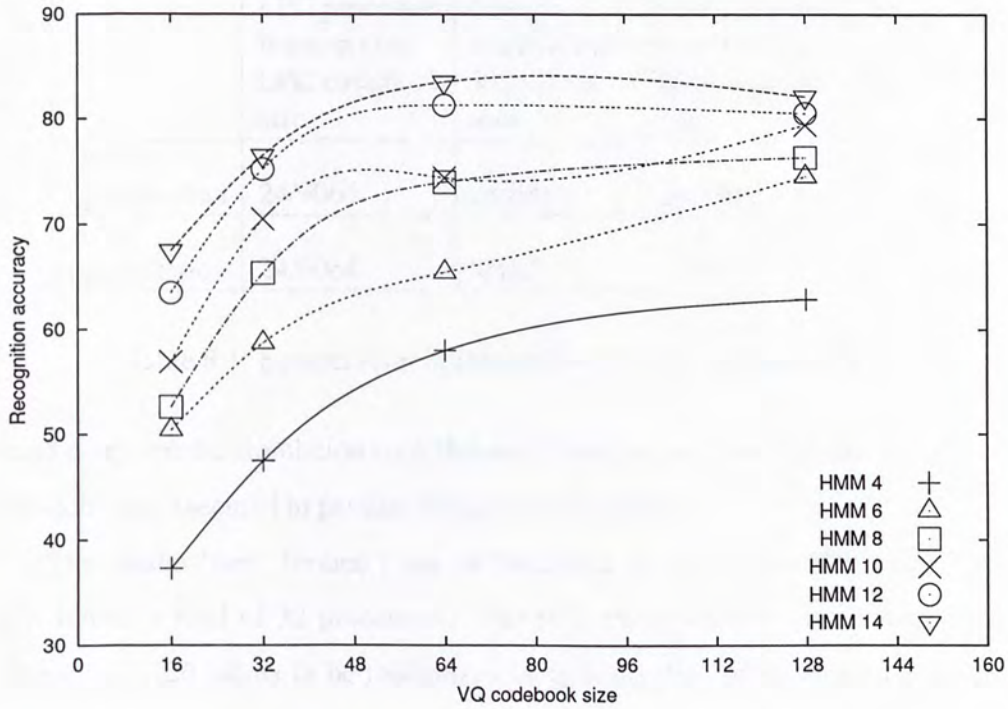


Figure 8.1: Recognition accuracy for different configurations of VQ codebook size and number of HMM states

8.2 Simplex method optimization

Using a VQ codebook size of 64 and 12 HMM states, the recognition accuracy using floating-point arithmetic is 81.3%. This recognition accuracy was used as reference during hardware cost optimization.

8.2.1 Simulation platform

The isolated word recognition system was developed using the *Fixed* class. Since fixed-point arithmetic was simulated using objects, the execution time is much longer than a floating-point implementation using primitive C++ *float* type. Specifically, 7.35 hours were required to perform recognition for all words using fixed-point simulation on an Intel Pentium 4 2.2GHz processor. Parallel computing was

	LPC processor fraction size/ LPC circuit size	VQ fraction size/ VQ circuit size	HMM decoder fraction size/ HMM circuit size	Total Circuit Size
Before optimization	24/9064	24/841	24/195	10100
After optimization	24/9064	8/185	21/177	9426

Table 8.1: System level optimization using the simplex method

used carry out the simulation such that each iteration was divided into a number of sub-jobs and executed in parallel using a Linux cluster.

The cluster [mm] formed from 16 Dual Intel Xeon 2.2GHz PCs, each with 1 GB RAM, a total of 32 processors. The PCs are networked via Myrinet [Myr]. There are 5120 words to be recognized in each iteration of optimization process. These were divided into 10 sub-jobs and executed in parallel, there are 512 words to be recognized in each sub-jobs and each sub-job is executed on a single PC. The execution time for each iteration is 0.76 hour, which is 9.5 times faster than using single PC. The performance cannot reach 10 times faster because of the overheads of submitting jobs to the cluster and collecting results.

8.2.2 System level optimization

The isolated word recognition system was divided into the LPC processor, the VQ and HMM decoder, the simplex method is used to find optimal wordlengths for each part which can reach the same recognition accuracy of a floating-point system. After optimization, the wordlengths found for these three parts are 24 bits, 8 bits and 21 bits respectively, the circuit size is 9426, compared with a system using uniform fraction size of 24 bits, a 6.67% circuit size reduction is obtained. These results are illustrated in Table 8.1.

	Before LPC optimization	After LPC optimization
Preemphasis and windowing fraction size	24	20
Autocorrelation fraction size	24	31
LPC analysis fraction size	24	20
Cepstral conversion fraction size	24	19
LPC processor circuit size	9064	6857
Total circuit size	9426	7219

Table 8.2: LPC processor optimization using the simplex method

8.2.3 LPC processor optimization

From table 8.1, one can see that the circuit size of the LPC processor is the largest. Further optimization was done to reduce the hardware cost of the LPC processor, as introduced in previous chapter, the LPC processor is divided into four parts, they are preemphasis and windowing, autocorrelation analysis, the LPC analysis and cepstral coefficient conversion, simplex method was used to find minimum fraction size for each part.

Table 8.2 shows the circuit size before and after the LPC processor's fraction size optimization. Before optimization, the LPC processor uses a uniform fraction size of 24 bits, and circuit size of LPC processor is 9064. After optimization, fraction sizes of 20 bits, 31 bits, 20 bits and 19 bits were found for the preemphasis and windowing, autocorrelation analysis, LPC analysis and cepstral coefficient conversion respectively. The LPC processor's circuit size after optimization is 6857, and the total circuit size after optimization is 7219.

Before any optimization, for a uniform fraction size of 24 bits, the circuit size is 10100 for the isolated word recognition system. After performing system level

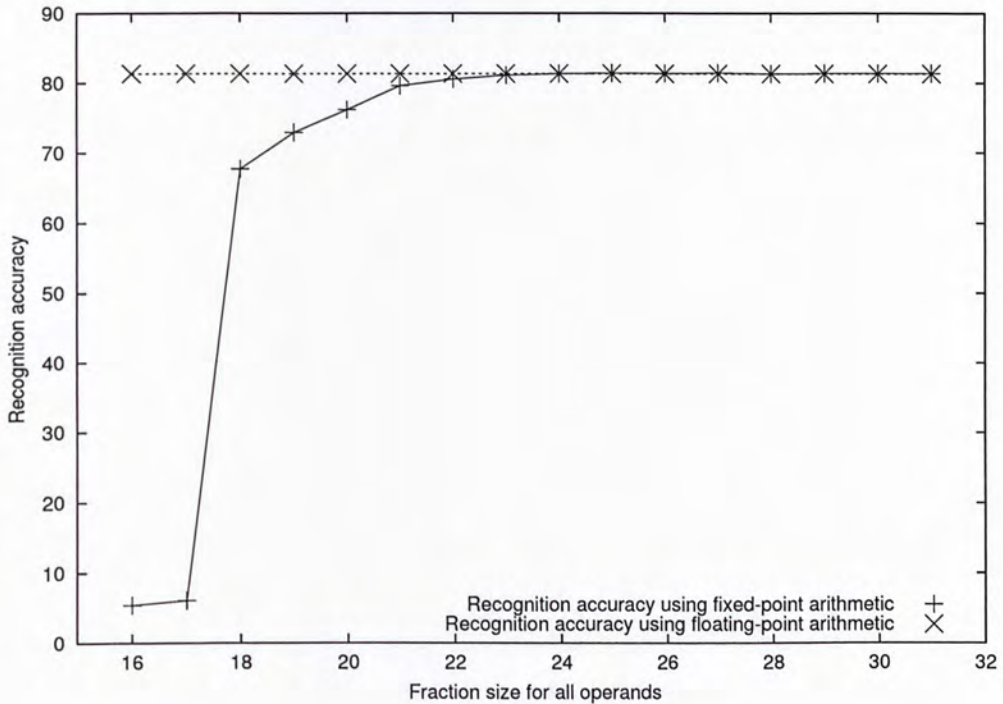


Figure 8.2: Recognition accuracy when sweep the fraction size of the whole system optimization and LPC processor optimization, the circuit size is 7219. Thus an overall improvement of 28.5% was achieved.

8.2.4 One-dimensional optimization

One-dimensional optimization was applied to system level optimization, Figure 8.2 shows the recognition accuracy when performing optimization step 1, where all operands use the same fraction size. In this diagram, the line with markers “x” represents the recognition accuracy using floating-point arithmetic, and the line with markers “+” represents the recognition accuracy using fixed-point arithmetic. It can be seen when all operands use a fraction size of 24 bits, the fixed-point calculation reaches the same recognition accuracy as floating-point arithmetic.

The line with markers “+” in Figure 8.3 represents the recognition accuracy

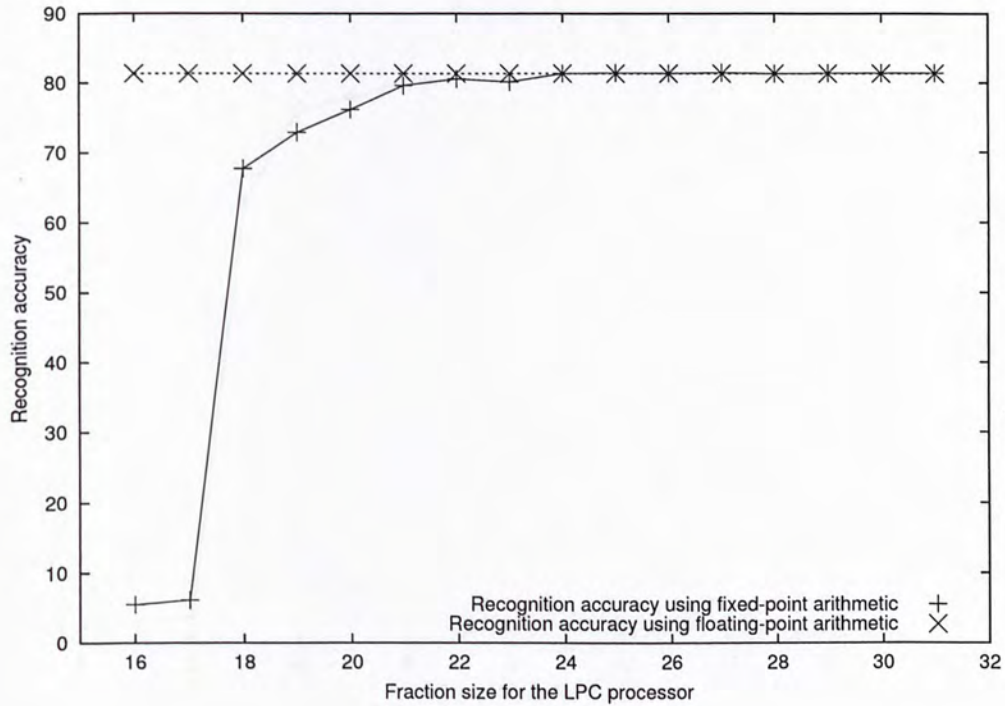


Figure 8.3: Recognition accuracy when sweep the fraction size of the LPC processor

obtained using fixed-point arithmetic after system level optimization step 2, the line with markers “x” is the recognition accuracy using floating-point arithmetic. In this step, the VQ and HMM decoder have fraction size of 24 bits, and the LPC processor’s fraction size is varied. It can be seen that when the LPC processor uses a fraction size of 24 bits, the fixed-point calculation can reach the floating point calculation’s recognition accuracy.

Figure 8.4 shows the recognition accuracy when performing system level optimization step 3, in this step, the LPC processor and HMM decoder have a fraction size of 24 bits, and the fraction size of VQ is varied. The line with markers “+” and “x” represent the recognition accuracy using fixed-point and floating-point arithmetic respectively. It shows that, at a VQ fraction size of 8 bits, the fixed-point calculation has the same recognition accuracy as floating-point arithmetic.

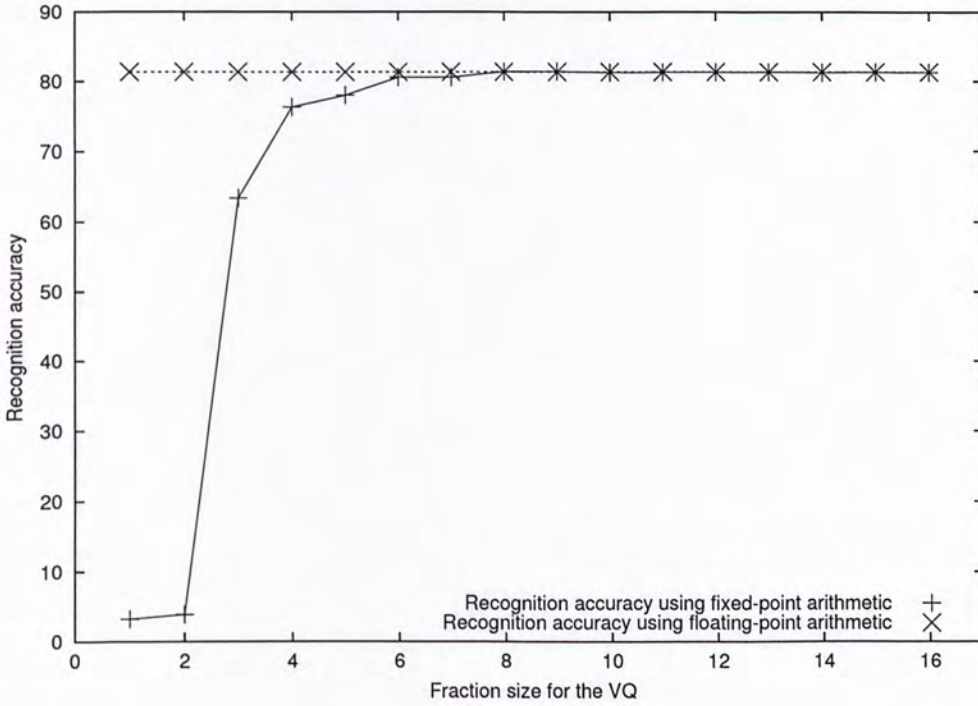


Figure 8.4: Recognition accuracy when sweep the fraction size of the VQ

Figure 8.5 shows the recognition accuracy when performing system level optimization step 4, in this step, the LPC processor's fraction size is fixed at 24 bits, VQ fraction size fixed at 8 bits, and the HMM decoder's fraction size is varied. The line with markers “+” and “x” represent the recognition accuracy using fixed-point and floating-point arithmetic respectively. It can be seen that fraction size 1 bit is sufficient for the HMM decoder.

Table 8.3 shows the circuit size before and after system level fraction size optimization using one-dimensional optimization approach. After optimization, optimal fraction sizes of 24 bits, 8 bits and 1 bit were found for the LPC processor, the VQ and HMM decoder respectively. Circuit size before optimization was 10100. After optimization, it is reduced to 9306, a 7.86% improvement.

A fraction size of 1 bit was sufficient for the HMM decoder. It is because in

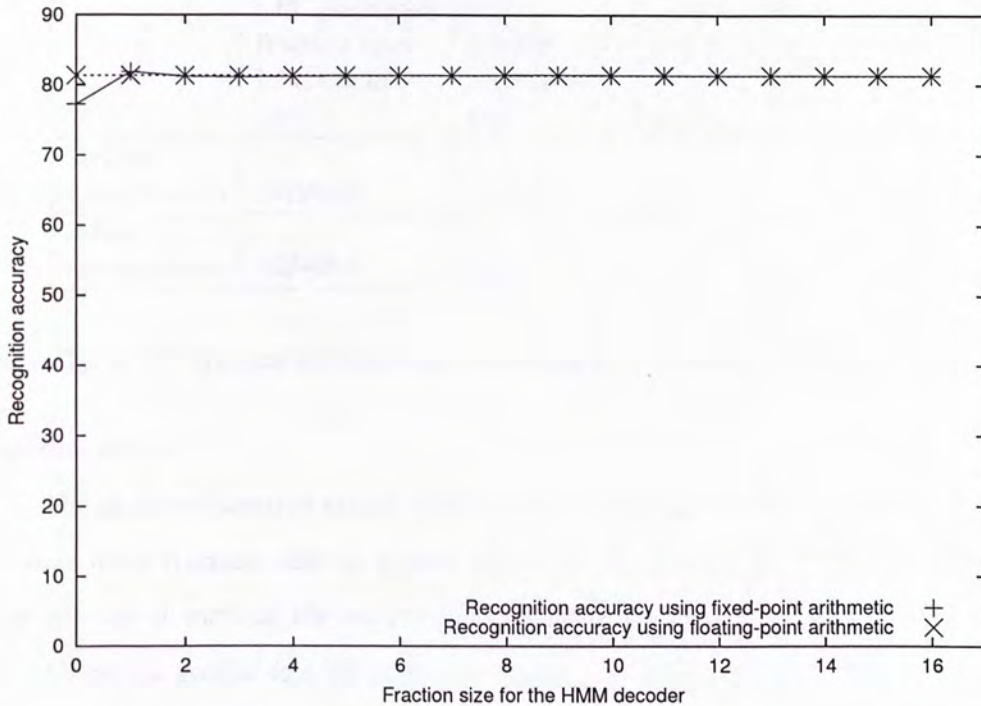


Figure 8.5: Recognition accuracy when sweep the fraction size of the HMM decoder

HMM decoding, the scores for all words are sorted and the word with highest score will be chosen as the recognized word. Although there are some errors for smaller fraction sizes, using fixed-point arithmetic can still obtain the same score sequence as using floating-point arithmetic. Furthermore, since the HMM state transition probabilities are computed in the logarithmic domain when using the Viterbi algorithm, the integer part is the most important factor that affects the scores.

8.3 Speeding up the optimization convergence

Table 8.4 shows a comparison between different optimization approaches applied to system level optimization, which are the simplex method, one-dimensional optimization with exhaustive search and one-dimensional optimization with the golden

	LPC processor fraction size/ LPC circuit size	VQ fraction size/ VQ circuit size	HMM decoder fraction size/ HMM circuit size	Total Circuit Size
Before optimization	24/9064	24/841	24/195	10100
After optimization	24/9064	8/185	1/57	9306

Table 8.3: System level optimization using one-dimensional optimization

section search.

Using the exhaustive search method, the number of iterations required to optimize three fraction sizes in system level optimization is 107. Using the golden section search method, the number of iterations required is 35 (3 times faster).

Using the golden section search, the fraction sizes found for the LPC processor, VQ and HMM decoder are 24 bits, 8 bits and 5 bits, and the total circuit size is 9330. It is a little bit worse than the result found using exhaustive search, which are 24 bits, 8 bits and 1 bit, and the total circuit size is 9306. It is because of the drawback of the golden section search, the searching may get trapped into a local optimum. However, the searching converges very quickly compared with exhaustive search, it can be considered as a quick wordlength estimation method when designing fixed-point systems.

Using the simplex method, the number of iterations is 84, the optimized cost is worse than using exhaustive search. As introduced in previous chapter, a penalty is added to the cost when recognition accuracy smaller than the reference value, because we want to reach the same recognition accuracy as a floating-point system. As a result, the cost will be very large when recognition accuracy smaller than the reference value. This design of the cost function will affect the reflection process of the simplex method, where three dimensions are reflected at the same time. If the reflection point has a LPC processor fraction size smaller than 24 bits, since

	Exhaustive search	Golden section search	Simplex method
LPC processor fraction size	24	24	24
VQ fraction size	8	8	8
HMM decoder fraction size	1	5	21
Total circuit size	9306	9330	9426
Percentage of cost improvement	7.86 %	7.62 %	6.67 %
Number of iteration	107	35	84

Table 8.4: Result comparison between applying exhaustive search, the golden section search and simplex method in system level optimization

the recognition accuracy is smaller than the reference value, the cost becomes very large. Although this reflection point may contains a smaller fraction size for the HMM decoder, this reflection is regarded as unsuccessful. Because of this reason, the HMM decoder's fraction size may not be able to converge to global optimum.

8.4 Optimization criteria

The optimizations done above used recognition accuracy and circuit size as optimization criteria. It is possible to use any criteria, quantization error being a possible alternative. Table 8.5 shows the LPC processor's optimization result using different optimization criteria, both results were obtained using the simplex method.

The average quantization error of the LPC processor is -60.5dB at fraction size of 24 bits, which is calculated as follows:

Optimization criteria	Recognition accuracy and Circuit size	Quantization error of LPC and Circuit size
Preemphasis and windowing fraction size	20	20
Autocorrelation fraction size	31	31
LPC analysis fraction size	20	20
Cepstral conversion fraction size	19	22
LPC processor circuit size	6857	7075
Improvement	24.3%	21.9%
Recognition accuracy	81.3%	81.3%

Table 8.5: Results using different optimization criteria in LPC processor optimization

$$avgQerr = \frac{\sum_{i=1}^W \left(\frac{\sum_{j=1}^{N \times P} \sum_{k=1}^P Qerr[j][k]}{N} \right)}{W} \quad (8.1)$$

where $Qerr[j][k]$ is the quantization error of the k th element of the j th LPCCs, P is the LPC order, N is the total number of LPCC vectors in each word, W is the total number of words used in recognition.

Optimization was done based on the cost function using circuit size and average quantization error as criteria, a penalty is added when the average quantization is error less than -60.5 dB. The circuit size of the LPC processor before optimization is 9064 with a uniform fraction size of 24 bits. Using recognition accuracy and circuit size as optimization criteria, the circuit size of the LPC processor is 6857 after optimization, the improvement is 24.3%. Using the average quantization error and circuit size as optimization criteria, the circuit size of the LPC processor is 7075 after optimization, a 21.9% reduction. Using average quantization error of the LPC

processor and circuit size as criteria, the result is similar to that using recognition accuracy and circuit size as criteria.

8.5 Summary

This chapter presented the results for the optimization of an isolated word recognition system. An overall circuit size reduction of 28.5% was achieved. The golden section search method can be used to speed up the searching and was shown to be 3 times faster than an exhaustive search. The results using different optimization criteria were also analyzed. Using average quantization error of the LPC processor as criteria, a 21.9% circuit size reduction of the LPC processor was obtained, while a 24.3% reduction was achieved using recognition accuracy as criteria.

Chapter 9

Conclusion

A framework was introduced to address the quantization issues of fixed-point system, an isolated word recognition system was used to explore the utility of the framework. The isolated word recognition system uses 12th order LPCCs, codebook size 64 and 12 HMM states, the recognition accuracy is 81.3% using floating-point arithmetic, this recognition accuracy was used as reference during hardware cost optimization. An application program was developed to simulate the speech system using the fixed-point class, when all operands use a uniform fraction size of 24 bits, the circuit size is 10100. After performing hardware cost optimization using the optimizer, the circuit size is 7219, a 28.5% reduction was obtained. The problems addressed are stated below:

9.1 Search space reduction

One-dimensional optimization and variable grouping were used to reduce the search space. The isolated word recognition system contains 48 variables, each variable has fraction size 32 bits, the search space is 48^{33} , after applying the one-dimensional optimization, the search space becomes 48×33 . Using variable grouping, the speech system was divided into three components, the LPC processor, the VQ and HMM decoder, each part uses uniform fraction size, the search space becomes

3×33 . Variable grouping was used to further optimize the cost of the LPC processor, where the LPC processor is divided into the preemphasis and windowing, the autocorrelation, the LPC analysis and the cepstral coefficient conversion. After applying the one-dimensional optimization to optimize the speech system in system level optimization, a 7.86% circuit size reduction was obtained, which is a little bit better than the simplex method, where a 6.67% reduction was achieved.

9.2 Speeding up the searching

The golden section search method was used to speed up searching. Using this approach, the searching can be 3 times faster than exhaustive search and achieve similar results. In the system level optimization, the difference between the final costs was only 0.24%. Using exhaustive search, the fraction sizes of the LPC processor, VQ and HMM decoder were 24 bits, 8 bits and 1 bit respectively, however, fraction sizes of 24 bits, 8 bits and 5 bits were obtained using the golden section search. Since the searching converges very quickly using the golden section search, the one-dimensional optimization with the golden section search can be considered as a quick wordlength estimation method.

9.3 Optimization criteria

The cost function used in this work was based primarily on recognition accuracy, since this is a direct measure of the system's performance. However, as described in Section 8.4, other optimization criteria such as quantization error could be used, and in fact may be more suitable for other applications with real valued outputs such as filtering etc.

When optimizing the cost of the LPC processor, the results obtained using different optimization criteria were compared. Using recognition accuracy as a criteria, a cost of 6857 was obtained for the LPC processor, which is a 24.3% improvement, while a cost of 7075 was obtained using average quantization error of the LPCCs as criteria, the improvement is 21.9%, the simplex method was applied to do the experiments, the difference of the optimized cost is 2.4%.

9.4 Flexibility of the framework design

Using object oriented concept, each part of the framework can be developed independently, modification to one part will not affect the design of other parts. Using overloading, the fixed-point simulation description can be developed easily. Since optimization was done based on a cost function, by modifying the attributes of the cost function, different optimization results can be analyzed easily.

The fixed-point class can automatically trace the range information of each variable and determine the integer size, moreover, it can perform calculations using both floating-point and fixed-point arithmetic simultaneously and calculate the quantization error automatically. Quantization effect of the fixed-point system can be analyzed conveniently.

9.5 Further development

Currently, the cost model only considers the hardware cost of arithmetic components, other components, e.g. memories, interfaces, were assumed occupying insignificant resources. A more accurate model can be developed, which will take these factors into account. Moreover, timing constraint can also be considered, e.g. logic delay, clock cycles can be added into the cost.

A more robust error reporting mechanism can be used. For example, each object can be associated with a flag, which can indicate arithmetic error, such as overflow

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