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<b>Authors</b>	Kirkpatrick, J. Davy; Martin, Emily C.; SMART, Richard Laurence; Cayago, Alfred J.; Beichman, Charles A.; et al.
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## Preliminary Trigonometric Parallaxes of 184 Late-T and Y Dwarfs and an Analysis of the Field Substellar Mass Function into the "Planetary" Mass Regime

J. DAVY KIRKPATRICK,<sup>1</sup> EMILY C. MARTIN,<sup>2</sup> RICHARD L. SMART,<sup>3</sup> ALFRED J. CAYAGO,<sup>4</sup> CHARLES A. BEICHMAN,<sup>1</sup> JACQUELINE K. FAHERTY,<sup>5</sup> FEDERICO MAROCCO,<sup>6,7</sup> CHRISTOPHER R. GELINO,<sup>6</sup> MICHAEL C. CUSHING,<sup>8</sup> ADAM C. SCHNEIDER,<sup>9</sup> GREGORY N. MACE,<sup>10</sup> CHRISTOPHER G. TINNEY,<sup>11,12</sup> EDWARD L. WRIGHT,<sup>2</sup> PATRICK J. LOWRANCE,<sup>13</sup> JAMES G. INGALLS,<sup>13</sup> FREDERICK J. VRBA,<sup>14</sup> AND IAN S. MCLEAN<sup>2</sup>

<sup>1</sup>*IPAC, Mail Code 100-22, Caltech, 1200 E. California Blvd., Pasadena, CA 91125, USA; davy@ipac.caltech.edu*

<sup>2</sup>*Department of Physics and Astronomy, University of California Los Angeles, 430 Portola Plaza, Box 951547, Los Angeles, CA, 90095-1547, USA*

<sup>3</sup>*Istituto Nazionale di Astrofisica, Osservatorio Astrofisico di Torino, Strada Osservatorio 20, 10025 Pino Torinese, Italy*

<sup>4</sup>*Department of Statistics, University of California Riverside, 900 University Avenue, Riverside, CA, 92521, USA*

<sup>5</sup>*Department of Astrophysics, American Museum of Natural History, Central Park West at 79th Street, New York, NY 10034, USA*

<sup>6</sup>*IPAC, Mail Code 100-22, Caltech, 1200 E. California Blvd., Pasadena, CA 91125, USA*

<sup>7</sup>*Jet Propulsion Laboratory, California Institute of Technology, MS 169-237, 4800 Oak Grove Drive, Pasadena, CA 91109, USA*

<sup>8</sup>*The University of Toledo, 2801 West Bancroft Street, Mailstop 111, Toledo, OH 43606, USA*

<sup>9</sup>*School of Earth and Space Exploration, Arizona State University, Tempe, AZ, 85282, USA*

<sup>10</sup>*McDonald Observatory and the Department of Astronomy, The University of Texas at Austin, Austin, TX 78712, USA*

<sup>11</sup>*School of Physics, University of New South Wales, NSW 2052, Australia*

<sup>12</sup>*Australian Centre for Astrobiology, University of New South Wales, NSW 2052, Australia*

<sup>13</sup>*IPAC, Mail Code 314-6, Caltech, 1200 E. California Blvd., Pasadena, CA 91125, USA*

<sup>14</sup>*US Naval Observatory, Flagstaff Station, P.O. Box 1149, Flagstaff, AZ 86002, USA*

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### ABSTRACT

To provide robust distance estimates for all T and Y dwarfs of type T6 or later believed to lie within 20 pc of the Sun, we present preliminary trigonometric parallax measurements of a sample of 184 of these objects. These 184 new measurements come from observations at *Spitzer*/IRAC 4.5 $\mu$ m (143), USNO *J*-band (18), NTT *J*-band (14), and UKIRT *J*-band (9). To complete the 20-pc census of the  $\geq$ T6 dwarfs, we use accurate trigonometric parallaxes previously published for another 44 objects in the census, along with spectrophotometric distance estimates for a final list of 7 believed to lie within 20 pc but lacking trigonometric parallaxes. Using the total sample of 235 objects, we compute the distances to which we are complete over five 150K-wide  $T_{\text{eff}}$  bins covering the range 300-1050K and compute space densities for each. To anchor the other end of the brown dwarf mass spectrum, we compile a list of early- to mid-L dwarfs within 20 pc using literature references and data from *Gaia* DR2. We likewise compute space densities for these objects, which cover four 150K-wide bins over the range 1500-2100K. We run simulations using various functional forms of the mass function passed through two different sets of evolutionary code to compute predicted distributions in  $T_{\text{eff}}$ . The best fit of our L, T, and Y observations to these predictions belongs to a simple power-law model with  $\alpha \approx 0.6$ , meaning that the slope of the field substellar mass function is in rough agreement with that found for brown dwarfs in nearby star forming regions and young clusters. Furthermore, we find that published versions of the log-normal form do not predict the steady rise seen in the space densities from 1050K to 350K. We also find that the low-mass cutoff to formation, if one exists, is no higher  $\sim 5 M_{\text{Jup}}$ , which corroborates findings in young, nearby moving groups and implies that extremely low-mass objects have been forming over the lifetime of the Milky Way. Shoring up the statistics in bins of lowest  $T_{\text{eff}}$  is necessary to determine whether the power law form applies to arbitrarily small masses. We discuss future plans that will allow us to explore this further.

*Keywords:* stars: luminosity function, mass function – brown dwarfs – parallaxes – stars: distances – solar neighborhood – catalogs

## 1. INTRODUCTION

Understanding the creation mechanisms for brown dwarfs has long been a stumbling block of star formation theory. Simplified arguments predicting the minimum Jeans mass fragment forming from a molecular cloud suggest a value of  $\sim 7 M_{Jup}$  (Low & Lynden-Bell 1976), although more complicated considerations such as the role of magnetic fields and rotation are thought to drive this value higher. Lower formation masses are possible via secondary mechanisms. For example, sites replete with high-mass stars can create lower-mass brown dwarfs through the ablation, via O star winds, of protostellar embryos that would otherwise have formed bona fide stars (e.g., Whitworth & Zinnecker 2004). Also, protostars in rich clusters with many high mass members may, via dynamical interactions, be stripped from their repository of accreting material, thus artificially stunting their growth (e.g., Reipurth & Clarke 2001). Star forming regions lacking higher mass stars will possess neither of these processes but still create low-mass objects down to at least  $\sim 3 M_{Jup}$ , as discoveries of low-mass brown dwarfs in nearby, sparse moving groups suggest (Liu et al. 2013; Gagné et al. 2015; Faherty et al. 2016; Best et al. 2017). Providing direct measurements on the frequency of low-mass formation and its low-mass limit are thus key parameters needed to inform modified predictions.

Field brown dwarfs – the well-mixed, low-mass by-products of star formation – can be used to derive the field substellar mass function. This function averages over any site-to-site differences and allows us to study the global efficiency of substellar formation integrated over the history of the Galactic disk. Does this field function suggest that low-mass star formation can be characterized by a simple form (Chabrier 2001) or only by a more complicated one (Kroupa et al. 2013)? What is the low-mass cutoff (Andersen et al. 2008)? Have these field objects, scattered from their stellar nurseries, been joined by other low-mass objects that escaped their birthplaces within a proto-planetary disk (Sumi et al. 2011; Mróz et al. 2017)? Is the formation efficiency of low-mass objects higher today than it was in the distant past (Bate 2005)?

Our ability to measure the low-mass cutoff is critically dependent on measuring the space density of objects with temperatures below 500K (Figure 12 of Burgasser 2004), which corresponds to late-T and Y dwarf spectral types believed to span a mass range of  $\sim 3$ - $20 M_{Jup}$  (Cushing et al. 2011; Luhman 2014b). The functional form of the mass function is also most easily discerned at these same temperatures (Figure 5 of Burgasser 2004). Both of these measurements can be accomplished by establishing a volume-limited sample of nearby brown dwarfs.

The recent spate of cold, field brown dwarf discoveries by the NASA *Wide-field Infrared Survey Explorer* (WISE) now

makes these measurements possible. The all-sky nature of WISE enables the creation of a sample of the closest, brightest brown dwarfs that exist, and these are the easiest brown dwarfs to characterize in detail. In this paper, we aim to use these discoveries to deduce the functional form and low-mass cutoff of the substellar mass function.

## 2. ESTABLISHING THE EMPIRICAL DATA SET

To reach the above goals, we define an empirical sample and a list of follow-up observations necessary to adequately characterize it. We consider the following four points:

(1) Accurate distances to these objects must be measured so that space densities can be calculated. These objects will have large parallactic signatures, but they are extremely faint in the optical and near-infrared wavelengths where ground-based astrometric monitoring takes place. For the faintest objects ( $J > 21$  mag), the Earth’s atmosphere and thermal environment preclude parallax measurements entirely. *Gaia* is unable to measure parallaxes for cold brown dwarfs because it observes only shortward of  $1.05 \mu\text{m}$ , a wavelength regime in which these sources emit very little flux. Observations are more easily done at wavelengths near  $5 \mu\text{m}$  where these objects are brightest. The InfraRed Array Camera (IRAC) onboard the *Spitzer Space Telescope* is therefore a natural choice, and accurate parallaxes can be measured using only a modest amount of *Spitzer* observing time.

(2) Objects must be characterized to the extent that unresolved binarity can be deduced. Unresolved binaries can lead to overestimates of the space density when spectrophotometric distance estimates are used, or underestimates if objects truly in the volume are not recognized as double. This is an inherent problem with any magnitude-limited sample. Although high-resolution imaging has been acquired for some of the nearest brown dwarfs (Gelino et al. 2011; Liu et al. 2012), very tight binaries or those with unfavorable orientations as seen from the Earth will go undetected. Measuring the absolute magnitude directly for each object is an excellent means of detecting unresolved doubles with small magnitude differences.

(3) The number of sources as a function of temperature must be known with sufficient resolution in mass to determine the low-mass cutoff to a few  $M_{Jup}$ . As Table 9 of Kirkpatrick et al. (2012) shows, a volume-limited sample with a distance limit of 20 pc provides between one dozen and four dozen stars in each half-subclass spectral type bin from T6 through early Y, although the magnitude limits of WISE restrict the T9 and later bins to somewhat smaller distances. This binning provides sufficient resolution to determine the low-mass cut-off to the precision required. Including objects as early as T6 allows us to properly measure the shape of the density distribution below  $\sim 1100\text{K}$  so that we can also place constraints on the overall functional form of the mass function, as Figure 14 of Kirkpatrick et al. (2012) illustrates.

(4) A sufficient sample size must be considered to robustly measure biases due to metallicity effects. At late-T and Y types, a higher percentage of old objects may be expected relative to field stars because the only young objects possible at these types are those that are exceedingly low in mass, although the percentage is critically dependent upon the low-mass cutoff of formation. (See, e.g., Figure 8 of [Burgasser 2004](#). Higher mass objects will not have time to cool to such low temperatures. In order to measure the spread in age, sufficient statistics is needed. Several late-T dwarfs identified spectroscopically as subdwarfs, believed to be older objects with lower-than-average metal content, are already recognized in the nearby sample. These can serve as metallicity calibrators with which to calibrate the absolute magnitude vs. spectral type relations as a function of metallicity and to provide the first evidence on the efficiency of low-mass formation at lower metallicities.

In conclusion, a volume-limited sample out to 20 pc that covers spectral types of T6 and later would fulfill our research goals. In the next section, we describe how we tabulated sources belonging to the sample itself.

### 3. TARGET SELECTION FOR THE 20-PC SAMPLE OF $\geq$ T6 DWARFS

Using the compilation of known T and Y dwarfs at Dwarf Archives<sup>1</sup> along with a listing of more recent additions that one of us (CRG) has compiled since the last Dwarf Archives update, we cataloged all published objects of type T6 and later ( $>350$  total), regardless of distance. We then used spectral types and  $H$ - and/or  $W2$ -band magnitudes to compute spectrophotometric distance estimates for those not already having measured parallaxes. Objects were retained in our list if their spectrophotometric distances placed them within 22 pc (to account for distance uncertainties) or if they had

published parallaxes good to 10% accuracy that placed them, within the measurement uncertainties, inside the 20-pc volume. This list of 235 objects is presented in Table 1. This table gives the discovery designation and reference in columns 1 and 2, the AllWISE designation in column 3, the measured infrared spectral type and its reference in columns 4 and 5, and the measured parallax and its reference in columns 6 and 7. For previously published parallax values in column 6, measurements of absolute parallax are commented with "(abs)" and those of relative parallax with "(rel)". In some cases, it is not clear whether the published value is an absolute or relative value, so those are left uncommented.

Of these 235 dwarfs in Table 1, 142 are being astrometrically monitored by our *Spitzer* program discussed further below, and 86 have high-accuracy parallax measurements from the ground and are either already published or are presented in this paper for the first time. Only seven objects lack astrometric monitoring, and these were not added to our *Spitzer* programs because they either do not have any prior *Spitzer* measurements – and thus may not have had a large time baseline to decouple proper motion from parallax had we observed them only in Cycle 13 – or were published after the Cycle 13 deadline. For these, the parallax values in column 6 are given in italics and are spectrophotometric estimates only. With one exception, these estimates take the apparent  $H$  and/or  $W2$  magnitudes in Table 2 together with the spectral types in column 4 to compute distance estimates via the equations (those than include the WISE 1828+2650 data point) from section 4.3 of [Kirkpatrick et al. \(2012\)](#). The sole exception is the parallax estimate of ULAS 0745+2332, which is calculated from the minimum and maximum distance estimates provided by [Burningham et al. \(2008\)](#).

**Table 1.** Dwarfs with Type  $\geq$ T6 and Distance or Distance Estimate  $\leq$ 20 pc

Discovery	Disc.	WISEA	Infrared	Type	Parallax	Parallax
Designation	Ref.	Designation	Sp. Type	Ref.	(mas)	Ref.
(1)	(2)	(3)	(4)	(5)	(6)	(7)
WISE J000517.48+373720.5	8	J000517.49+373720.4	T9	8	Table 4	1
WISE J001505.87–461517.6	2	J001505.88–461517.8	T8	2	Table 4	1
WISE J003231.09–494651.4	2	J003231.06–494651.9	T8.5	2	Table 4	1
ULAS J003402.77–005206.7	27	J003402.79–005208.2	T8.5	10	68.7±1.4 (abs)	67
	...	...	...	...	78.0±3.6 (abs)	70
2MASS J00345157+0523050	3	J003452.03+052306.9	T6.5	61	Table 4	1
	...	...	...	...	105.4±7.5 (abs)	66
WISE J003829.05+275852.1	8	J003829.06+275852.0	T9	8	Table 4	1
Gl 27B (0039+2115) <sup>a</sup>	28	<i>source not extracted</i>	T8	61	90.42±0.32 (abs)	73
WISE J004024.88+090054.8	8	J004024.88+090054.4	T7	8	Table 6	1

*Table 1 continued*

<sup>1</sup> See <http://www.DwarfArchives.org>.

Table 1 (continued)

Discovery	Disc.	WISEA	Infrared	Type	Parallax	Parallax
Designation	Ref.	Designation	Sp. Type	Ref.	(mas)	Ref.
(1)	(2)	(3)	(4)	(5)	(6)	(7)
WISE J004945.61+215120.0	8	J004945.65+215119.6	T8.5	8	Table 4	1
2MASS J00501994-3322402	29	J005021.05-332228.8	T7	61	94.6±2.4 (abs)	67
CFBDS J005910.90-011401.3	30	J005911.10-011401.1	T8.5	10	103.2±2.1 (abs)	67
	...	...	...	...	108.2±5.0 (abs)	70
WISEPA J012333.21+414203.9	4	J012333.25+414203.9	T7	4	Table 4	1
CFBDS J013302.27+023128.4	5	J013302.45+023128.8	T8.5	5	Table 4	1
WISE J014656.66+423410.0AB	2	J014656.66+423409.9	Y0	2	Table 4	1
WISEPC J014807.25-720258.7	4	J014807.34-720258.7	T9.5	4	91.1±3.4	21
ULAS J015024.37+135924.0	31	J015024.40+135923.6	T7.5	31	Table 6	1
WISEP J022105.94+384202.9	4	J022105.99+384203.0	T6.5	4	Table 4	1
WISEPC J022322.39-293258.1	4	J022322.38-293257.3	T7.5	4	Table 6	1
WISEPA J022623.98-021142.8AB	4	J022623.99-021142.7	T7	4	Table 4	1
WISE J023318.05+303030.5	8	J023318.06+303030.4	T6	8	Table 4	1
WISE J024124.73-365328.0	2	J024124.74-365328.0	T7	2	Table 4	1
2MASS J0243137-245329	32	J024313.47-245332.1	T6	61	93.62±3.63 (abs)	68
WISE J024512.62-345047.8	8	J024512.62-345047.8	T8	8	59	-
WISE J024714.52+372523.5	8	J024714.54+372523.4	T8	8	Table 4	1
WISEPA J025409.45+022359.1	4,33	J025409.55+022358.5	T8	4	Table 5	1
WISEA J030237.53-581740.3	6	J030237.53-581740.3	Y0:	6	Table 4	1
WISE J030449.03-270508.3	7	J030449.04-270508.1	Y0pec	7	Table 4	1
WISEA J030919.70-501614.2	6	J030919.70-501614.2	[T7] <sup>b</sup>	6	Table 4	1
WISEPA J031325.96+780744.2	4	J031326.00+780744.3	T8.5	4	Table 4	1
WISE J031624.35+430709.1	8	J031624.40+430708.7	T8	8	Table 4	1
WISEA J032309.12-590751.0	1	J032309.12-590751.0	[T6] <sup>c</sup>	1	Table 4	1
WISEPC J032337.53-602554.9	4	J032337.57-602554.5	T8.5	4	Table 4	1
WISE J032504.33-504400.3	9	J032504.52-504403.0	T8	9	Table 4	1
WISE J032517.69-385454.1	8	J032517.68-385453.8	T9	8	Table 4	1
WISE J032547.72+083118.2	8	J032547.73+083118.2	T7	8	Table 4	1
WISE J033515.01+431045.1	8	J033515.07+431044.7	T9	8	Table 4	1
WISE J033605.05-014350.4	8	J033605.04-014351.0	Y0	22	Table 4	1
2MASS J03480772-6022270	34	J034807.33-602235.2	T7	61	Table 6	1
WISE J035000.32-565830.2	2	J035000.31-565830.5	Y1	2	Table 4	1
WISE J035934.06-540154.6	2	J035934.07-540154.8	Y0	2	Table 4	1
WISE J040443.48-642029.9	9	J040443.50-642030.0	T9	9	Table 4	1
WISEPA J041022.71+150248.5	10	J041022.75+150247.9	Y0	10	Table 4	1
WISE J041358.14-475039.3	8	J041358.14-475039.4	T9	8	Table 4	1
2MASS J0415195-093506	32	J041521.26-093500.4	T8	61	175.2±1.7 (abs)	67
	...	...	...	...	174.34±2.76 (abs)	68
WISE J043052.92+463331.6	8	J043052.96+463331.7	T8	8	Table 4	1
WISEPA J045853.89+643452.9AB	11	J045853.91+643452.6	T8.5	10	Table 4	1
WISEPA J050003.05-122343.2	4	J050003.03-122343.1	T8	4	Table 4	1
WISE J051208.66-300404.4	8	J051208.67-300404.2	T8.5	8	Table 4	1
WISEPA J051317.28+060814.7	4	J051317.27+060814.5	T6.5	4	Table 5	1
WISE J052126.29+102528.4	35	J052126.30+102528.3	T7.5	35	171	-
UGPS J052127.27+364048.6	46	J052127.42+364043.6	T8.5	46	Table 6	1
WISEPA J052844.51-330823.9	4	J052844.52-330824.0	T7pec	4	Table 6	1
WISE J053516.80-750024.9	2	J053516.87-750024.6	≥Y1:	2	Table 4	1
WISE J054047.00+483232.4	8	J054047.01+483232.2	T8.5	8	Table 4	1
WISEPA J054231.26-162829.1	4	J054231.27-162829.1	T6.5	4	Table 6	1
GI 229B (0610-2152)	36	<i>source not extracted</i>	T7pec	61	173.81±0.99 (abs)	73
	...	...	...	...	172.66±0.29 (abs)	72

Table 1 continued

Table 1 (continued)

Discovery	Disc.	WISEA	Infrared	Type	Parallax	Parallax
Designation	Ref.	Designation	Sp. Type	Ref.	(mas)	Ref.
(1)	(2)	(3)	(4)	(5)	(6)	(7)
WISEPA J061213.93–303612.7AB	4	J061213.88–303612.1	T6	4	Table 6	1
WISEPA J061407.49+391236.4	4	J061407.50+391235.7	T6	4	Table 5	1
WISE J061437.73+095135.0	8	J061437.75+095135.2	T7	8	Table 4	1
WISEA J061557.21+152626.1	22	J061557.21+152626.1	T8.5	22	64	-
WISEPA J062309.94–045624.6	4	J062309.92–045624.5	T8	4	Table 6	1
WISEPA J062542.21+564625.5	4	J062542.23+564625.4	T6	4	Table 5	1
WISEPA J062720.07–111428.8	4	J062720.07–111427.9	T6	4	Table 6	1
WISE J062842.71–805725.0	6	J062842.74–805725.0	[T9] <sup>d</sup>	6	50	-
WISEA J064528.39–030247.9	6	J064528.39–030247.9	T6	6	Table 4	1
WISE J064723.23–623235.5	12	J064723.24–623235.4	Y1	12	Table 4	1
WISEA J071301.86–585445.2	6	J071301.86–585445.2	T9	6	Table 4	1
WISE J071322.55–291751.9	2	J071322.55–291752.0	Y0	2	Table 4	1
UGPS J072227.51–054031.2	37	J072227.27–054029.8	T9	10	242.8±2.4	40
WISE J072312.44+340313.5	8	J072312.47+340313.5	T9:	8	Table 4	1
2MASS J0727182+171001	32	J072719.15+170951.3	T7	61	112.5±0.9 (abs)	67
	...	...	...	...	110.14±2.34 (abs)	68
2MASS J07290002–3954043	24	J072859.49–395345.3	T8pec	24	126.3±8.3 (abs)	66
WISE J073444.02–715744.0	2	J073444.03–715743.8	Y0	2	Table 4	1
WISEPA J074457.15+562821.8	4	J074457.24+562820.9	T8	4	Table 4	1
ULAS J074502.79+233240.3	19	<i>source not extracted</i>	T8.5	19	63	-
WISEPA J075003.84+272544.8	4	J075003.75+272545.0	T8.5	4	Table 6	1
WISEPA J075108.79–763449.6	4	J075108.80–763449.3	T9	4	Table 6	1
WISEPC J075946.98–490454.0	4	J075946.98–490454.0	T8	4	Table 4	1
WD 0806–661B (0807–6618)	65	<i>source not detected</i>	[Y1] <sup>e</sup>	1	52.17±1.67 (abs)	69
WISE J081117.81–805141.3	8	J081117.95–805141.4	T9.5:	8	98.5±7.7	21
WISE J081220.04+402106.2	8	J081220.05+402106.2	T8	8	Table 4	1
DENIS J081730.0–615520	38	J081729.76–615503.8	T6	38	203±13	38
WISE J082507.35+280548.5	9	J082507.37+280548.2	Y0.5	9	Table 4	1
WISE J083337.83+005214.2	13	J083337.81+005213.8	(sd)T9	13	Table 4	1
WISEPC J083641.12–185947.2	4	J083641.13–185947.1	T8pec	4	Table 4	1
WISE J085510.83–071442.5	14,15,16	J085510.74–071442.5	[≥Y4] <sup>f</sup>	1	Table 4	1
WISEPA J085716.25+560407.6	4	J085716.21+560407.5	T8	4	Table 4	1
ULAS J085910.69+101017.1	64	J085910.62+101014.8	T7	64	Table 6	1
ULAS J090116.23–030635.0	39	J090116.20–030636.0	T7.5	39	62.6±2.6 (abs)	70
WISEPA J090649.36+473538.6	4	J090649.33+473538.2	T8	4	Table 4	1
WISE J091408.96–345941.5	17	J091408.99–345941.4	T8	6	Table 4	1
WISEPC J092906.77+040957.9	4	J092906.76+040957.6	T6.5	4	Table 6	1
2MASS J0937347+293142	32	J093735.63+293127.2	T6pec	61	162.84±3.88 (abs)	68
2MASS J09393548–2448279	29	J093935.93–244838.9	T8	61	196.0±10.4 (abs)	66
	...	...	...	...	187.3±4.6 (abs)	71
WISEA J094020.09–220820.5	6	J094020.09–220820.5	T8	6	Table 4	1
WISE J094305.98+360723.5	18	J094306.00+360723.3	T9.5	18	Table 4	1
ULAS J095047.28+011734.3 <sup>g</sup>	40,41	J095047.31+011733.1	T8	19,8	53.40±3.51	19
	...	...	...	...	Table 6	1
WISEPC J095259.29+195507.3	4	J095259.29+195508.1	T6	4	Table 4	1
WISEPC J101808.05–244557.7	4	J101808.03–244558.1	T8	4	Table 4	1
WISEPA J101905.63+652954.2	4	J101905.61+652954.0	T6	4	Table 5	1
WISE J102557.72+030755.7	8	J102557.67+030755.8	T8.5	8	Table 4	1
CFBDS J102841.01+565401.9	5	<i>source not extracted</i>	T8	5	Table 4	1
ULAS J102940.52+093514.6	19	J102940.51+093514.1	T8	20	Table 6	1
WISE J103907.73–160002.9	8	J103907.74–160002.9	T7.5	8	Table 4	1

Table 1 continued



Table 1 (continued)

Discovery	Disc.	WISEA	Infrared	Type	Parallax	Parallax
Designation	Ref.	Designation	Sp. Type	Ref.	(mas)	Ref.
(1)	(2)	(3)	(4)	(5)	(6)	(7)
WISEPC J104245.23–384238.3	4	J104245.24–384238.1	T8.5	4	64.8±3.4	21
ULAS J104355.37+104803.4	19	J104355.40+104802.4	T8	19	Table 4	1
2MASS J1047538+212423	43	J104752.35+212417.2	T6.5	61	94.73±3.81 (abs)	68
	...	...	...	...	110.8±6.6 (rel)	76
WISE J105047.90+505606.2	8	J105047.89+505605.9	T8	8	Table 4	1
WISE J105130.01–213859.7	8	J105130.02–213859.9	T8.5	22	Table 4	1
WISE J105257.95–194250.2	20	J105257.95–194250.1	T7.5	20	Table 4	1
WISEA J105553.62–165216.5	6	J105553.62–165216.5	T9.5	22	Table 4	1
WISE J111239.24–385700.7	6	J111239.25–385700.5	T9	6	56	-
2MASS J11145133–2618235	29	J111448.74–261827.9	T7.5	61	176.8±7.0 (abs)	66
	...	...	...	...	179.2±1.4 (abs)	67
WISE J111838.70+312537.9 <sup>b</sup>	2,44	J111838.69+312537.7	T8.5	44	113.2±4.6 (abs)	75
WISEPC J112254.73+255021.5	4	J112254.70+255021.9	T6	4	Table 5	1
WISE J112438.12–042149.7	8	J112438.10–042149.6	T7	8	Table 4	1
WISE J113949.24–332425.1	20	J113949.23–332425.4	T7	20	Table 4	1
WISEA J114156.67–332635.5	21	J114156.67–332635.5	Y0	6	Table 4	1
WISE J114340.22+443123.8	8	J114340.22+443124.0	T8.5	8	Table 4	1
WISEP J115013.88+630240.7	4	J115013.85+630241.3	T8	4	Table 4	1
ULAS J115239.94+113407.6	19	J115239.94+113406.9	T8.5	19	Table 4	1
WISE J120604.38+840110.6	9	J120604.25+840110.5	Y0	9	Table 4	1
2MASS J1217110–031113	43	J121710.27–031112.1	T7.5	61	110.36±5.88 (abs)	68
	...	...	...	...	90.8±2.2 (rel)	76
WISEPC J121756.91+162640.2AB	4	J121756.92+162640.3	T9	4	Table 4	1
WISEA J122036.38+540717.3	22	J122036.38+540717.3	T9.5	22	Table 4	1
WISE J122152.28–313600.8	8	J122152.28–313600.7	T6.5	8	Table 4	1
2MASS J12255432–2739466AB	43	J122554.66–273954.1	T6	61	74.20±3.47 (abs)	68
	...	...	...	...	75.1±2.5 (rel)	76
WISE J122558.86–101345.0	8	J122558.86–101345.2	T6	8	Table 4	1
2MASS J12314753+0847331	3	J123146.70+084722.1	T5.5 <sup>i</sup>	61	Table 4	1
2MASS J12373919+6526148	43	J123737.33+652608.0	T6.5	61	96.07±4.78 (abs)	68
ULAS J123828.51+095351.3	42	J123828.38+095352.0	T8	10	Table 6	1
WISE J124309.61+844547.8	20	J124309.40+844547.7	T9	20	Table 4	1
WISE J125015.56+262846.9	8	J125015.56+262846.8	T6.5	8	53	-
WISE J125448.52–072828.4	20	J125448.50–072828.3	T7	20	Table 4	1
WISE J125715.90+400854.2	8	J125715.91+400854.2	T7	8	Table 4	1
VHS J125804.89–441232.4	23	J125804.91–441232.6	T6	23	Table 4	1
Gl 494C (1300+1221) <sup>j</sup>	45	J130041.63+122114.5	T8	10	85.54±1.53 (abs)	73
WISE J130141.62–030212.9	8	J130141.63–030212.9	T8.5	8	Table 4	1
ULAS J130217.21+130851.2	31	J130217.07+130851.1	T8	10	65±5 (abs)	77
WISEPC J131106.24+012252.4	4	J131106.21+012253.9	T9:	4	Table 6	1
ULAS J131508.42+082627.4	64	J131508.40+082627.0	T7.5	64	42.8±7.7 (abs)	70
WISE J131833.98–175826.5	8	J131833.96–175826.3	T8	22	Table 4	1
WISEPC J132004.16+603426.2	4	J132004.16+603426.1	T6.5	4	Table 5	1
WISEPA J132233.66–234017.1	4	J132233.63–234017.0	T8	4	Table 5	1
WISEA J133300.03–160754.4	1	J133300.03–160754.4	[T7.5] <sup>k</sup>	1	Table 4	1
ULAS J133553.45+113005.2	42	J133553.41+113004.7	T8.5	10	99.9±1.6	67
	...	...	...	...	96.7±3.2 (abs)	70
SDSSp J134646.45–003150.4	47	J134646.05–003151.5	T6.5	61	68.3±2.3 (rel)	76
	...	...	...	...	72.74±5.02 (abs)	68
WISEPC J140518.40+553421.4	10	J140518.32+553421.3	Y0.5(pec?)	9,80	Table 4	1
ULAS J141623.94+134836.3	49	J141623.96+134836.0	(sd)T7.5	62	109.7±1.3 (abs) <sup>l</sup>	67

Table 1 continued

Table 1 (continued)

Discovery	Disc.	WISEA	Infrared	Type	Parallax	Parallax
Designation	Ref.	Designation	Sp. Type	Ref.	(mas)	Ref.
(1)	(2)	(3)	(4)	(5)	(6)	(7)
Gl 547B (1423+0116) <sup>m</sup>	50	J142320.84+011637.5	sdT8,T8	50,8	58.17±0.53 (abs)	73
VHS J143311.46–083736.3	23	J143311.41–083736.6	T8	23	Table 4	1
WISEPA J143602.19–181421.8	4	J143602.19–181422.0	T8pec	4	Table 4	1
WISE J144806.48–253420.3	20	J144806.48–253420.5	T8	20	Table 4	1
Gl 570D (1457–2121)	51	J145715.83–212208.0	T7.5	61	171.22±0.94 (abs)	73
WISEPC J145715.03+581510.2	4	J145715.01+581510.1	T7	4	Table 5	1
WISE J150115.92–400418.4	17	J150115.92–400418.2	T6	6	Table 4	1
2MASS J15031961+2525196	52	J150319.68+252525.7	T5	61	157.2±2.2 (abs)	67
SDSS J150411.63+102718.4	53	J150411.81+102715.4	T7	53	46.1±1.5 (abs)	67
	...	...	...	...	52.5±7.1 (abs)	66
Gl 576B (1504+0538) <sup>n</sup>	54	J150457.56+053759.8	T6pec	54	53.80±2.80 (abs)	73
	...	...	...	...	52.66±0.33 (abs)	72
WISEPC J150649.97+702736.0	4	J150649.92+702736.1	T6	4	Table 5	1
WISE J151721.13+052929.3	8	J151721.12+052929.3	T8	8	Table 4	1
WISEPC J151906.64+700931.5	4	J151906.63+700931.3	T8	4	Table 4	1
WISE J152305.10+312537.6	8	J152305.09+312537.3	T6.5pec	8	Table 4	1
WISEPA J154151.66–225025.2	10	J154151.65–225024.9 <sup>p</sup>	Y1	9	Table 4	1
WISE J154214.00+223005.2	8	J154214.00+223005.2	T9.5	8	Table 4	1
2MASS J1553022+153236AB	32	J155301.93+153238.8	T7	61	75.1±0.9 (abs)	67
WISEPA J161215.94–342027.1	4	J161215.92–342028.5	T6.5	4	Table 4	1
WISEPA J161441.45+173936.7	4	J161441.47+173935.4	T9	4	Table 4	1
2MASS J16150413+1340079	24	J161504.36+134004.0	T6	24	Table 4	1
	...	...	...	...	68.6±6.4 (abs)	66
WISEPA J161705.75+180714.3	4	J161705.73+180714.1	T8	4	Table 6	1
WISEPA J162208.94–095934.6	4	J162208.93–095934.6	T6	4	Table 4	1
SDSSp J162414.37+002915.6	55	J162414.07+002915.6	T6	61	90.9±1.2 (rel)	76
	...	...	...	...	86.85±3.85 (abs)	68
WISEPA J162725.64+325525.5	4	J162725.64+325524.5	T6	4	Table 5	1
SDSS J162838.77+230821.1	53	J162838.99+230817.9	T7	53	75.1±0.9 (abs)	67
WISE J163940.86–684744.6	17	J163940.84–684739.4	Y0pec	9	Table 4	1
WISEPA J165311.05+444423.9	4	J165311.03+444422.7	T8	4	Table 4	1
WISEPA J171104.60+350036.8AB	4	J171104.59+350036.7	T8	4	Table 4	1
WISEPA J171717.02+612859.3	4	J171717.04+612859.2	T8	4,8	Table 4	1
WISE J172134.46+111739.4	8	J172134.46+111739.5	T6	8	Table 4	1
WISEA J173551.56–820900.3	6	J173551.56–820900.3	T6	6	Table 4	1
WISEPA J173835.53+273258.9	10	J173835.52+273258.8	Y0	10	Table 4	1
WISEPA J174124.26+255319.5	4,33,56	J174124.22+255319.2	T9	4	Table 5	1
SDSS J175805.46+463311.9 <sup>q</sup>	57	J175805.45+463316.9	T6.5	61	70.99±1.86 (abs)	73
	...	...	...	...	71.44±0.30 (abs)	72
WISEPA J180435.40+311706.1	4	J180435.37+311706.2	T9.5:	4	Table 4	1
WISEPA J181210.85+272144.3	4	J181210.83+272144.2	T8.5:	10	Table 6	1
WISE J181243.14+200746.4	8	J181243.14+200746.2	T9	8	Table 4	1
WISE J181329.40+283533.3	8	J181329.40+283533.3	T8	8	Table 4	1
WISEPA J182831.08+265037.8	10	J182831.08+265037.6	≥Y2	2	Table 4	1
SCR J1845–6357B	58	<i>source not extracted</i>	T6	63	259.45±1.11 (abs)	78
WISEPA J185215.78+353716.3	4	J185215.82+353716.2	T7	4	Table 5	1
WISEPA J190624.75+450808.2	4	J190624.73+450807.0	T6	4	Table 5	1
WISE J192841.35+235604.9	8	J192841.39+235604.5	T6	8	Table 4	1
WISE J195500.42–254013.9	8	J195500.42–254013.5	T8	8	Table 4	1
WISEPA J195905.66–333833.7	4	J195905.64–333833.8	T8	4	Table 4	1
WISE J200050.19+362950.1	18	J200050.19+362950.1	T8	18	Table 4	1

Table 1 continued



Table 1 (continued)

Discovery	Disc.	WISEA	Infrared	Type	Parallax	Parallax
Designation	Ref.	Designation	Sp. Type	Ref.	(mas)	Ref.
(1)	(2)	(3)	(4)	(5)	(6)	(7)
WISE J200520.38+542433.9	25	J200520.35+542433.6	sdT8	25	Table 4	1
WISE J201546.27+664645.1	8	J201546.45+664645.2	T8	8	Table 4	1
WISEA J201748.74-342102.6	6	J201748.74-342102.6	[T7.5] <sup>f</sup>	6	Table 4	1
WISEPA J201824.96-742325.9	4	J201824.99-742327.9	T7	4	Table 6	1
WISE J201920.76-114807.5	8	J201920.75-114807.5	T8:	8	Table 4	1
WISEPC J205628.90+145953.3	10	J205628.88+145953.6	Y0	10	Table 4	1
WISE J210200.15-442919.5	2	J210200.14-442919.9	T9	2	92.3±1.9	21
WISEPA J213456.73-713743.6	4	J213456.79-713744.7	T9pec	4	109.1±3.7	21
ULAS J214638.83-001038.7 <sup>s</sup>	59	J214639.07-001039.3	T8.5	10	79.8±4.5 (abs)	79
WISE J214706.78-102924.0	8	J214706.79-102923.7	T7.5	8	Table 4	1
WISEPC J215751.38+265931.4	4	J215751.35+265931.2	T7	4	Table 4	1
WISEA J215949.54-480855.2	6	J215949.54-480855.2	T9	6	Table 4	1
WISEA J220304.18+461923.4	22	J220304.18+461923.4	T8	22	Table 4	1
Gl 845C (2204-5646) <sup>l</sup>	60	<i>source not extracted</i>	T6	61	276.06±0.28 (abs)	73
WISE J220905.73+271143.9	4	J220905.75+271143.6	Y0:	18	Table 4	1
WISEPC J220922.10-273439.5	4	J220922.09-273439.9	T7	4	Table 4	1
WISEA J221140.53-475826.7	6	J221140.53-475826.7	[T8] <sup>u</sup>	6	Table 4	1
WISE J221216.33-693121.6	9	J221216.27-693121.6	T9	9	Table 4	1
WISEPC J221354.69+091139.4	4	J221354.69+091139.3	T7	4	Table 5	1
WISE J222055.31-362817.4	2	J222055.34-362817.5	Y0	2	Table 4	1
WISEPC J222623.05+044003.9	4	J222623.06+044003.2	T8	4	Table 5	1
2MASS J22282889-4310262	34	J222829.01-431029.8	T6	61	92.1±2.6 (abs)	74
	...	...	...	...	94.02±7.0 (abs)	66
WISEA J223204.53-573010.4	6	J223204.53-573010.4	T9	6	Table 4	1
WISE J223720.39+722833.8	8	J223720.39+722833.9	T6	8	Table 4	1
WISEPC J225540.74-311841.8	4	J225540.75-311842.0	T8	4	Table 4	1
WISE J230133.32+021635.0	8	J230133.32+021635.0	T6.5	8	Table 4	1
WISEA J230228.66-713441.7	6	J230228.66-713441.7	[T4.5] <sup>v</sup>	6	Table 4	1
WISEPA J231336.40-803700.3	4	J231336.47-803700.4	T8	4	Table 4	1
WISEPC J231939.13-184404.3	4	J231939.14-184404.4	T7.5	4	Table 4	1
ULAS J232123.79+135454.9	26	J232123.82+135453.3	T7.5	31	Table 4	1
	...	...	...	...	84±4 (abs)	77
WISEPC J232519.54-410534.9	4	J232519.55-410535.1	T9pec	4	107.8±3.7	21
ULAS J232600.40+020139.2	19	J232600.44+020138.4	T8	19	Table 4	1
WISE J233226.49-432510.6	2	J233226.54-432510.9	T9:	2	Table 4	1
WISEPC J234026.62-074507.2	4	J234026.61-074508.4	T7	4	Table 5	1
ULAS J234228.96+085620.1	26	J234228.97+085619.9	T6.5	8	Table 6	1
	...	...	...	...	34.3±5.1 (abs)	74
WISEPA J234351.20-741847.0	4	J234351.28-741846.9	T6	4	Table 4	1
WISEPC J234446.25+103415.8	4	J234446.24+103415.8	T9	4,8	Table 4	1
WISEPC J234841.10-102844.4	4	J234841.11-102844.1	T7	4	Table 5	1
WISEA J235402.79+024014.1	9	J235402.79+024014.1	Y1	9	Table 4	1
WISE J235716.49+122741.8	8	J235716.49+122741.5	T6	8	Table 4	1

Table 1 continued

Table 1 (continued)

Discovery	Disc.	WISEA	Infrared	Type	Parallax	Parallax
Designation	Ref.	Designation	Sp. Type	Ref.	(mas)	Ref.
(1)	(2)	(3)	(4)	(5)	(6)	(7)

NOTE—References: (1) this paper, (2) Kirkpatrick et al. 2012, (3) Burgasser et al. 2004, (4) Kirkpatrick et al. 2011, (5) Albert et al. 2011, (6) Tinney et al., in press, (7) Pinfield et al. 2014, (8) Mace et al. 2013, (9) Schneider et al. 2015, (10) Cushing et al. 2011, (11) Mainzer et al. 2011, (12) Kirkpatrick et al. 2013, (13) Pinfield et al. 2014, (14) Luhman 2014a, (15) Kirkpatrick et al. 2014, (16) Luhman 2014b, (17) Tinney et al. 2012, (18) Cushing et al. 2014, (19) Burningham et al. 2013, (20) Thompson et al. 2013, (21) Tinney et al. 2014, (22) Martin et al., submitted, (23) Lodieu et al. 2012, (24) Looper et al. 2007, (25) Mace et al. 2013, (26) Scholz 2010, (27) Warren et al. 2007a, (28) Mugrauer et al. 2006, (29) Tinney et al. 2005, (30) Delorme et al. 2008, (31) Burningham et al. 2010, (32) Burgasser et al. 2002, (33) Scholz et al. 2011, (34) Burgasser et al. 2003, (35) Bihain et al. 2013, (36) Nakajima et al. 1995, (37) Lucas et al. 2010, (38) Artigau et al. 2010, (39) Lodieu et al. 2007, (40) Leggett et al. 2012, (41) Luhman et al. 2012, (42) Burningham et al. 2008, (43) Burgasser et al. 1999, (44) Wright et al. 2013, (45) Goldman et al. 2010, (46) Burningham et al. 2011, (47) Tsvetanov et al. 2000, (48) Cardoso et al. 2015, (49) Scholz 2010, (50) Pinfield et al. 2012, (51) Burgasser et al. 2000, (52) Burgasser et al. 2003, (53) Chiu et al. 2006, (54) Murray et al. 2011, (55) Strauss et al. 1999, (56) Gelino et al. 2011, (57) Knapp et al. 2004, (58) Biller et al. 2006, (59) Burningham et al. 2009, (60) Wright et al. 2003, (61) Burgasser et al. 2006, (62) Burgasser et al. 2010, (63) Kasper et al. 2007., (64) Pinfield et al. 2008, (65) Luhman et al. 2011, (66) Faherty et al. 2012, (67) Dupuy & Liu 2012, (68) Vrba et al. 2004, (69) Subasavage et al. 2009, (70) Marocco et al. 2010, (71) Burgasser et al. 2008, (72) Gaia Collaboration et al. 2016, (73) van Leeuwen 2007, (74) Smart et al. 2013, (75) van Altena et al. 1995, (76) Tinney et al. 2003, (77) Manjavacas et al. 2013, (78) Henry et al. 2006, (79) Harrington & Dahn 1980, (80) Cushing et al. 2016.

<sup>a</sup> 0039+2115: Also known as HD 3651B.

<sup>b</sup> 0309–5016: Type estimated from methane imaging.

<sup>c</sup> 0323–5907: The ch1–ch2 color of  $1.244 \pm 0.033$  mag (Table 2) suggests a type of T6 based on Figure 11 of Kirkpatrick et al. (2011).

<sup>d</sup> 0628–8057: Type estimated from methane imaging.

<sup>e</sup> 0807–6618: Given the fact that the absolute ch2 magnitude of this object ( $15.43 \pm 0.09$  mag) and ch1–ch2 color ( $2.81 \pm 0.16$  mag) are most like the Y1 dwarfs, this object has been assigned a temporary spectral type of Y1.

<sup>f</sup> 0855–0714: Given the fact that the absolute *H* and ch2 magnitudes of this object ( $27.04 \pm 0.24$  and  $17.13 \pm 0.02$  mag, respectively) are *much* fainter, and the *H*–W2 and ch1–ch2 colors ( $10.13 \pm 0.24$  and  $3.55 \pm 0.07$  mag, respectively) *much* redder, than that of the other Y dwarfs typed as late as  $\geq Y2$ , this object has been assigned a temporary spectral type of  $\geq Y4$ .

<sup>g</sup> 0950+0117: This is a common-proper-motion companion to LHS 6176.

<sup>h</sup> 1118+3125: Also known as the distant companion to  $\xi$  UMa (GI 423).

<sup>i</sup> 1231+0837: Object earlier in type than T6, but nonetheless included here because we obtained a parallax with *Spitzer*.

<sup>j</sup> 1300+1221: Also known as Ross 458C.

<sup>k</sup> 1333–1607: The Table 2 colors of ch1–ch2 =  $1.811 \pm 0.050$  mag and *H*–ch2 =  $3.369 \pm 0.132$  mag suggest, based on Figures 11 and 14 of Kirkpatrick et al. (2011), a type of T7.5.

<sup>l</sup> 1416+1348: The parallax of the sdL primary is quoted here for the (sd)T companion.

<sup>m</sup> 1423+0114: Also known as BD+01 2920B.

<sup>n</sup> 1504+0538: Also known as HIP 73786B.

<sup>p</sup> 1541–2250: Source not extracted in the AllWISE Source Catalog, so this designation is the one from the WISE All-Sky Source Catalog.

<sup>q</sup> 1758+4633: Also known as GJ 4040B

<sup>r</sup> 2017–3421: Type estimated from methane imaging.

<sup>s</sup> 2146–0010: Also known as Wolf 940B and GJ 1263B.

<sup>t</sup> 2204–5646: Also known as  $\epsilon$  Indi Bb.

<sup>u</sup> 2211–4758: Type estimated from methane imaging.

<sup>v</sup> 2302–7134: Type estimated from methane imaging. Object earlier in type than T6, but nonetheless included here because we obtained a parallax with *Spitzer*.

Photometry for these objects is given in Table 2. This table shows an abbreviated name from Table 1 in column 1, the *H*-band apparent magnitude and its reference in columns 2

and 3, and the *WISE* W1 through W3 magnitudes in columns 4 through 6. It should be noted that ground-based near-infrared photometry in both the *J* and *H* bands has been taken for many of these objects in one of two systems: either the

Mauna Kea Observatories filter set (MKO; Tokunaga et al. 2002) or the filter set established by the Two Micron All Sky Survey (2MASS; Skrutskie et al. 2006). Because the  $J$ -band filter profiles between the two systems are very different, and the  $H$ -band profiles are nearly the same, we list in Table 2 only the  $H$ -band magnitudes since those can be intercom-

pared regardless of the system used. Additional discussion on this point can be found in section 3.1 of Kirkpatrick et al. (2011). Discussion of the measurements of *Spitzer* magnitudes in columns 7-8 and the Astronomical Observation Requests (AORs) from which they were measured can be found in section 5.

**Table 2.** Photometry of Objects from Table 1

Object	$H$	$H$	W1	W2	W3	ch1	ch2	AOR
Name	(mag)	Ref.	(mag)	(mag)	(mag)	(mag)	(mag)	Used
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
WISE 0005+3737	17.98±0.02	2	16.764±0.089	13.291±0.031	11.785±0.236	15.431±0.024	13.282±0.018	44560128
WISE 0015-4615	17.91±0.07	43	16.960±0.101	14.218±0.043	>12.281	16.096±0.031	14.228±0.019	41490432
WISE 0032-4946	18.87±0.14	43	17.669±0.167	15.076±0.068	12.206±0.349	16.932±0.049	14.929±0.021	44698880
ULAS 0034-0052	18.49±0.04	3	17.007±0.133	14.544±0.062	>11.955	16.233±0.034	14.495±0.020	44747520
2MASS 0034+0523	15.55±0.03	4	15.088±0.037	12.552±0.025	11.780±0.313	14.095±0.019	12.580±0.017	44697856
WISE 0038+2758	18.92±0.04	40	17.448±0.145	14.363±0.043	12.379±0.332	16.454±0.037	14.410±0.020	44555776
Gl 27B (0039+2115)	16.72±0.03	5	...	...	...	15.38±0.04	13.62±0.02	— <sup>a</sup>
WISE 0040+0900	16.56±0.02	44	15.985±0.065	13.826±0.049	>11.819	15.067±0.022	13.757±0.018	44725504
WISE 0049+2151	16.72±0.02	1	15.920±0.060	13.030±0.028	11.583±0.191	15.009±0.022	13.043±0.017	44762368
2MASS 0050-3322	16.04±0.10	6	15.600±0.038	13.582±0.030	11.835±0.243	14.872±0.022	13.594±0.018	45074176
CFBDS 0059-0114	18.27±0.05	7	16.899±0.118	13.732±0.039	>11.630	15.771±0.028	13.715±0.018	44712448
WISE 0123+4142	17.20±0.13	8	16.842±0.084	14.946±0.066	>12.295	16.119±0.032	14.842±0.021	41730048
CFBDS 0133+0231	18.62±0.10	39	17.250±0.137	14.980±0.073	>12.662	16.789±0.044	15.053±0.023	45085696
WISE 0146+4234	22.69±0.14	42	>19.137	15.083±0.065	>12.447	17.500±0.070	15.072±0.022	41808128
WISE 0148-7202	19.22±0.04	8	18.260±0.200	14.592±0.039	>12.576	16.836±0.045	14.648±0.020	40830976
ULAS 0150+1359	18.11±0.02	44	17.505±0.165	15.235±0.088	>12.000	16.453±0.014	15.112±0.016	35261440
WISE 0221+3842	17.45±0.15	8	16.730±0.081	14.812±0.058	>12.073	15.926±0.029	14.860±0.021	41562880
WISE 0223-2932	17.30±0.11	8	16.870±0.083	14.021±0.035	12.647±0.393	15.810±0.028	14.013±0.019	40833792
WISE 0226-0211	18.88±0.10	1	17.413±0.131	14.518±0.047	>12.603	16.612±0.040	14.628±0.020	40824064
WISE 0233+3030	16.79±0.02	1	16.403±0.066	14.341±0.046	>12.025	15.629±0.026	14.352±0.019	44740096
WISE 0241-3653	17.04±0.07	1	16.863±0.078	14.352±0.039	12.514±0.330	15.739±0.027	14.348±0.019	41480704
2MASS 0243-2453	15.39±0.03	10	14.654±0.029	12.928±0.026	11.488±0.142	13.952±0.019	12.976±0.017	45105920
WISE 0245-3450	17.67±0.10	1	17.028±0.098	14.500±0.047	12.184±0.327	16.047±0.030	14.587±0.020	40825344
WISE 0247+3725	18.24±0.19	40	18.485±0.434	14.624±0.064	>12.354	16.698±0.042	14.553±0.020	41760512
WISE 0254+0223	16.29±0.02	44	15.807±0.048	12.758±0.026	11.357±0.139	14.689±0.021	12.703±0.017	40831488
WISE 0302-5817	...	-	>19.262	15.809±0.091	>12.940	18.187±0.092	15.844±0.019	52669440
WISE 0304-2705	21.02±0.16	12	>19.140	15.592±0.088	>12.775	17.706±0.033	15.494±0.016	50031872
WISE 0309-5016	17.43±0.04	43	16.465±0.057	13.631±0.031	12.755±0.455	15.528±0.025	13.633±0.018	41522688
WISE 0313+7807	17.63±0.06	8	15.953±0.045	13.263±0.026	12.045±0.264	15.310±0.024	13.267±0.017	41443840
WISE 0316+4307	19.70±0.09	40	17.790±0.221	14.640±0.054	>12.411	16.643±0.041	14.584±0.020	44590848
WISE 0323-5907	...	-	16.804±0.065	14.529±0.039	12.891±0.429	15.771±0.027	14.527±0.020	41508608
WISE 0323-6025	18.40±0.02	8	17.610±0.120	14.493±0.039	>12.146	16.570±0.039	14.505±0.020	40825856
WISE 0325-5044	19.42±0.03	15	18.430±0.258	16.209±0.145	>12.918	17.746±0.086	15.696±0.025	44562176
WISE 0325-3854	19.58±0.20	1	17.795±0.138	14.988±0.053	12.936±0.431	17.120±0.053	14.984±0.021	41746944
WISE 0325+0831	16.15±0.08	40	15.350±0.043	13.534±0.034	11.882±0.336	14.700±0.021	13.588±0.018	41797888
WISE 0335+4310	19.94±0.03	15	>18.652	14.515±0.055	>11.901	16.612±0.040	14.381±0.020	41838848
WISE 0336-0143	>20.2	41	18.449±0.470	14.557±0.057	>12.066	17.254±0.059	14.625±0.020	41462784
2MASS 0348-6022	15.56±0.14	46	15.024±0.028	12.550±0.022	11.220±0.082	14.166±0.019	12.538±0.017	44735488
WISE 0350-5658	22.26±0.14	15	>18.699	14.745±0.044	12.325±0.282	17.936±0.096	14.688±0.020	40834560
WISE 0359-5401	22.03±0.11	15	>19.031	15.384±0.054	>12.877	17.553±0.072	15.326±0.023	40819712
WISE 0404-6420	19.97±0.03	15	18.442±0.178	15.726±0.063	>12.977	17.633±0.082	15.418±0.022	44587264

Table 2 continued

Table 2 (continued)

Object	<i>H</i>	<i>H</i>	W1	W2	W3	ch1	ch2	AOR
Name	(mag)	Ref.	(mag)	(mag)	(mag)	(mag)	(mag)	Used
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
WISE 0410+1502	19.90±0.04	15	>18.170	14.113±0.047	12.314±0.500	16.636±0.042	14.166±0.019	40828160
WISE 0413-4750	20.20±0.03	14	19.084±0.351	15.587±0.068	>12.808	17.802±0.086	15.487±0.024	44572672
2MASS 0415-0935	15.70±0.03	10	15.140±0.036	12.292±0.025	11.093±0.125	14.256±0.019	12.374±0.017	44717824
WISE 0430+4633	19.24±0.12	1	>18.410	14.411±0.052	>12.014	16.130±0.032	14.216±0.019	44759296
WISE 0458+6434	17.41±0.06	8	16.439±0.074	13.022±0.027	12.084±0.281	15.079±0.022	12.984±0.017	40820736
WISE 0500-1223	18.13±0.12	8	17.447±0.151	13.979±0.038	>12.514	15.947±0.029	13.998±0.019	40832512
WISE 0512-3004	19.66±0.41	40	18.631±0.377	15.338±0.079	>12.583	17.641±0.076	15.583±0.024	41474048
WISE 0513+0608	16.13±0.08	8	15.841±0.056	13.899±0.040	>12.533	15.104±0.022	13.947±0.018	41741056
WISE 0521+1025	15.22±0.10	46	14.105±0.031	12.291±0.024	10.296±0.084	...	...	...
UGPS 0521+3640 <sup>b</sup>	17.28±0.04	45	14.398±0.034	13.004±0.029	11.153±0.151	14.937±0.022	...	32886784
...	...	...	...	...	...	...	13.577±0.017	32912896
WISE 0528-3308	16.97±0.14	8	17.231±0.109	14.517±0.046	12.565±0.416	16.308±0.034	14.590±0.020	40824320
WISE 0535-7500	23.34±0.34	2	17.940±0.143	14.904±0.047	>12.349	17.753±0.084	15.009±0.021	41033472
WISE 0540+4832	18.62±0.05	40	>18.730	14.988±0.076	>11.878	16.973±0.049	14.769±0.021	44737280
WISE 0542-1628	16.57±0.10	8	16.226±0.060	13.954±0.038	>12.121	15.264±0.023	13.967±0.018	41456896
Gl 229B (0610-2152)	14.36±0.05	17	...	...	...	...	...	...
WISE 0612-3036AB	17.06±0.11	8	16.402±0.061	14.038±0.038	>12.446	15.586±0.026	14.032±0.019	41455872
WISE 0614+3912	16.36±0.25	38	16.240±0.079	13.628±0.034	>11.901	15.188±0.023	13.596±0.018	41560320
WISE 0614+0951	16.83±0.03	45	16.623±0.107	14.237±0.053	>11.984	15.484±0.025	14.093±0.019	41446656
WISE 0615+1526	...	-	>18.454	15.324±0.117	>12.220	17.195±0.039	15.178±0.017	52669952
WISE 0623-0456	17.31±0.11	8	16.845±0.094	13.814±0.035	12.407±0.445	15.493±0.025	13.735±0.018	41772032
WISE 0625+5646	16.90±0.10	8	16.514±0.075	14.431±0.049	12.507±0.481	15.468±0.025	14.412±0.019	41561088
WISE 0627-1114	15.44±0.08	46	14.980±0.034	13.252±0.029	11.530±0.211	14.270±0.019	13.324±0.018	41823744
WISE 0628-8057	...	-	17.801±0.119	15.278±0.052	>12.765	16.845±0.046	15.247±0.023	44573952
WISE 0645-0302	17.33±0.02	45	17.990±0.325	14.862±0.078	>12.408	16.191±0.033	14.682±0.020	44771072
WISE 0647-6232	23.31±0.17	15	>19.539	15.224±0.051	>12.961	17.893±0.092	15.070±0.022	40829696
WISE 0713-5854	19.48±0.15	1	>18.977	15.267±0.050	>12.789	17.290±0.062	15.141±0.022	44556800
WISE 0713-2917	20.19±0.08	2	>18.776	14.462±0.052	12.294±0.355	16.673±0.043	14.223±0.019	44568064
UGPS 0722-0540	16.90±0.02	18	15.250±0.045	12.200±0.023	10.206±0.069	14.295±0.019	12.221±0.017	44721920
WISE 0723+3403	18.63±0.06	1	17.704±0.227	14.692±0.060	>11.920	16.767±0.044	14.684±0.021	40829440
2MASS 0727+1710	15.67±0.03	10	15.186±0.041	12.962±0.030	11.924±0.309	14.461±0.020	13.016±0.017	44748288
2MASS 0729-3954	15.98±0.18	46	15.292±0.033	12.972±0.024	11.366±0.119	14.555±0.020	12.997±0.017	44703744
WISE 0734-7157	21.07±0.07	15	18.749±0.281	15.189±0.050	>12.959	17.649±0.077	15.213±0.022	41754880
WISE 0744+5628	17.59±0.12	8	17.181±0.118	14.531±0.049	12.646±0.498	16.267±0.034	14.552±0.020	41697536
ULAS 0745+2332	...	-	...	...	...	...	...	...
WISE 0750+2725	19.00±0.06	8	18.434±0.423	14.552±0.061	>12.417	16.677±0.041	14.484±0.020	40837120
WISE 0751-7634	19.68±0.13	2	16.946±0.066	14.530±0.036	11.911±0.155	16.416±0.036	14.620±0.020	40821760
WISE 0759-4904	17.41±0.04	40	16.997±0.091	13.812±0.032	>12.228	15.619±0.026	13.757±0.018	40835072
WD 0806B (0807-6618)	25.29±0.14	14	...	16.82±0.09 <sup>c</sup>	...	19.65±0.15	16.84±0.06	— <sup>c</sup>
WISE 0811-8051	19.99±0.14	2	16.775±0.084	14.345±0.038	12.638±0.320	16.817±0.045	14.402±0.019	41498880
WISE 0812+4021	18.30±0.20	40	17.796±0.224	15.274±0.094	>12.279	16.932±0.048	15.299±0.024	40831744
DENIS 0817-6155	13.53±0.03	46	12.972±0.023	11.265±0.020	9.661±0.033	12.238±0.017	11.303±0.016	45119744
WISE 0825+2805	22.97±0.14	15	>18.444	14.578±0.060	>11.660	17.327±0.062	14.651±0.020	44588032
WISE 0833+0052	20.63±0.10	37	>18.342	14.973±0.079	>12.300	17.010±0.017	14.847±0.016	46068224
WISE 0836-1859	18.79±0.26	40	17.624±0.177	15.151±0.074	>12.573	16.865±0.047	15.084±0.022	40833536
WISE 0855-0714	23.83±0.24	14	19.805±0.424 <sup>d</sup>	13.704±0.033	11.143±0.126	17.470±0.066	13.923±0.016	48748032
WISE 0857+5604	17.49±0.14	8	17.120±0.103	14.095±0.040	>12.176	16.018±0.030	14.134±0.019	41543168
ULAS 0859+1010	18.58±0.06	19	17.751±0.232	15.158±0.084	>12.035	...	...	...
ULAS 0901-0306	18.46±0.13	20	17.188±0.129	14.557±0.054	>11.993	16.435±0.037	14.534±0.020	44792832
WISE 0906+4735	17.81±0.16	8	17.558±0.173	14.549±0.054	>11.793	16.472±0.037	14.549±0.020	40820224
WISE 0914-3459	...	-	17.613±0.159	15.055±0.057	>12.067	16.741±0.043	15.047±0.021	44719104

Table 2 continued

Table 2 (continued)

Object	$H$	$H$	W1	W2	W3	ch1	ch2	AOR
Name	(mag)	Ref.	(mag)	(mag)	(mag)	(mag)	(mag)	Used
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
WISE 0929+0409	17.37±0.07	44	16.543±0.083	14.254±0.048	12.379±0.519	15.715±0.027	14.237±0.019	41486080
2MASS 0937+2931	14.67±0.03	10	14.088±0.027	11.670±0.022	10.696±0.101	13.156±0.017	11.692±0.017	44708096
2MASS 0939-2448	15.96±0.09	21	14.906±0.030	11.640±0.022	10.667±0.086	13.773±0.018	11.620±0.016	44790784
WISE 0940-2208	...	-	16.870±0.084	14.639±0.056	>12.110	16.396±0.036	14.680±0.021	44739072
WISE 0943+3607	20.32±0.04	15	18.176±0.297	14.413±0.048	12.289±0.394	16.746±0.043	14.284±0.019	40827136
ULAS 0950+0117	18.40±0.05	22	17.635±0.182	14.507±0.051	>12.126	16.306±0.034	14.422±0.020	44564736
WISE 0952+1955	17.22±0.10	8	16.839±0.113	14.463±0.053	>12.387	15.812±0.028	14.498±0.020	41567488
WISE 1018-2445	18.00±0.23	40	17.267±0.139	14.128±0.039	>12.259	16.128±0.032	14.134±0.019	41510144
WISE 1019+6529	16.52±0.12	8	16.281±0.051	13.997±0.034	>12.196	15.309±0.024	14.002±0.019	40820992
WISE 1025+0307	18.36±0.05	40	17.487±0.194	14.136±0.052	>12.344	16.316±0.034	14.193±0.019	44547072
CFBDS 1028+5654	18.38±0.08	39	...	...	...	16.359±0.012	14.469±0.016	26686464
ULAS 1029+0935	17.63±0.02	1	16.780±0.117	14.376±0.074	>11.754	16.083±0.031	14.455±0.020	44772608
WISE 1039-1600	17.19±0.04	43	16.477±0.073	14.176±0.045	>11.846	15.868±0.028	14.206±0.019	44711936
WISE 1042-3842	19.21±0.02	14	18.281±0.299	14.556±0.048	>12.558	16.769±0.043	14.570±0.020	40833280
ULAS 1043+1048	18.53±0.07	44	18.435±0.475	15.687±0.142	>11.876	17.021±0.014	15.409±0.016	44144128
2MASS 1047+2124	15.83±0.03	17	15.377±0.036	13.004±0.030	11.864±0.312	14.409±0.020	12.998±0.017	44718848
WISE 1050+5056	18.31±0.03	40	17.941±0.227	14.858±0.060	>12.655	16.547±0.038	14.901±0.021	44580864
WISE 1051-2138	19.19±0.39	40	17.301±0.141	14.596±0.056	>12.132	16.419±0.036	14.598±0.020	41464320
WISE 1052-1942	17.06±0.12	1	16.585±0.084	14.111±0.044	>11.687	15.663±0.027	14.215±0.019	41486336
WISE 1055-1652	>20.1	41	>18.103	15.067±0.078	>12.238	17.296±0.062	15.048±0.022	44549632
WISE 1112-3857	20.40±0.25	1	17.478±0.169	14.404±0.048	>12.185	16.541±0.039	14.420±0.019	44578304
2MASS 1114-2618	15.82±0.05	6	15.251±0.038	12.271±0.024	11.346±0.179	14.185±0.019	12.354±0.017	44727040
WISE 1118+3125	18.15±0.06	23	16.158±0.053	13.341±0.028	12.241±0.330	15.600±0.026	13.366±0.018	41553920
WISE 1122+2550	16.64±0.11	8	16.087±0.061	14.096±0.044	>12.050	15.359±0.024	14.098±0.019	45537536
WISE 1124-0421	>17.0	1	16.446±0.083	14.049±0.045	>11.947	15.370±0.024	14.097±0.019	44728064
WISE 1139-3324	17.94±0.08	1	18.469±0.384	14.907±0.063	>12.722	16.891±0.047	14.996±0.022	44576256
WISE 1141-3326	...	-	17.079±0.117	14.611±0.055	11.728±0.213	16.414±0.036	14.659±0.020	44755200
WISE 1143+4431	19.04±0.06	40	18.722±0.380	15.188±0.064	>12.861	17.141±0.055	15.157±0.022	44590336
WISE 1150+6302	>18.0	8	16.958±0.089	13.405±0.028	12.375±0.303	15.612±0.026	13.429±0.018	40824576
ULAS 1152+1134	18.66±0.10	44	16.825±0.106	14.649±0.063	>11.681	16.278±0.034	14.778±0.021	45144320
WISE 1206+8401	21.06±0.06	15	>18.734	15.058±0.054	>12.536	17.339±0.061	15.220±0.022	40823808
2MASS 1217-0311	15.98±0.03	17	15.267±0.039	13.205±0.034	11.704±0.264	14.753±0.021	13.286±0.018	44770304
WISE 1217+1626	18.17±0.03	1	16.549±0.082	13.128±0.030	12.023±0.312	15.435±0.024	13.105±0.017	40822784
WISE 1220+5407	...	-	19.227±0.517	15.757±0.091	>12.988	18.005±0.078	15.715±0.018	52671232
WISE 1221-3136	16.06±0.18	40	15.884±0.049	13.870±0.037	12.116±0.327	15.090±0.023	13.891±0.018	44754944
2MASS 1225-2739	15.10±0.08	46	14.661±0.030	12.730±0.027	11.157±0.146	13.900±0.018	12.750±0.017	45141760
WISE 1225-1013	16.41±0.02	43	16.197±0.065	13.993±0.042	12.285±0.408	15.308±0.024	13.959±0.019	44726016
2MASS 1231+0847	15.31±0.11	46	15.067±0.035	13.083±0.031	12.227±0.391	14.268±0.019	13.079±0.017	44710144
2MASS 1237+6526	15.94±0.10	6	15.378±0.037	12.933±0.025	11.939±0.224	14.429±0.020	12.945±0.017	44781824
ULAS 1238+0953	19.20±0.02	25	18.534±0.455	15.340±0.122	>12.328	17.142±0.011	15.366±0.016	24979456
WISE 1243+8445	19.21±0.07	1	18.553±0.274	15.567±0.076	>13.045	17.355±0.063	15.402±0.023	44587520
WISE 1250+2628	16.74±0.02	44	16.412±0.071	14.587±0.053	>12.627	...	...	...
WISE 1254-0728	17.63±0.03	1	16.776±0.103	14.847±0.076	>12.278	16.334±0.035	14.823±0.021	44795136
WISE 1257+4008	16.96±0.13	40	16.672±0.079	14.431±0.045	>12.201	15.921±0.029	14.493±0.020	41475072
VHS 1258-4412	...	-	15.667±0.043	14.014±0.037	12.109±0.272	14.910±0.022	13.998±0.018	45162240
Gl 494C (1300+1221)	17.01±0.04	24	16.041±0.060	13.845±0.039	11.702±0.266	15.362±0.024	13.852±0.018	44698368
WISE 1301-0302	18.39±0.06	40	17.620±0.189	14.868±0.068	>11.995	16.636±0.040	14.894±0.021	44569088
ULAS 1302+1308	18.60±0.06	27	17.691±0.227	14.873±0.070	12.158±0.416	16.512±0.013	14.916±0.016	34784000
WISE 1311+0122	19.32±0.23	8	17.579±0.198	14.703±0.060	>12.645	16.817±0.045	14.676±0.020	40826368
ULAS 1315+0826	19.50±0.10	19	17.751±0.232	15.158±0.084	>12.571	...	...	...
WISE 1318-1758	17.71±0.23	40	17.513±0.160	14.666±0.058	>12.281	16.790±0.045	14.728±0.020	40824832

Table 2 continued

Table 2 (continued)

Object	$H$	$H$	W1	W2	W3	ch1	ch2	AOR
Name	(mag)	Ref.	(mag)	(mag)	(mag)	(mag)	(mag)	Used
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
WISE 1320+6034	16.56±0.13	8	16.715±0.066	14.519±0.042	>12.302	15.829±0.028	14.495±0.020	40823296
WISE 1322-2340	16.61±0.14	8	16.733±0.087	13.960±0.040	12.489±0.380	15.666±0.026	13.890±0.018	40834304
WISE 1333-1607	18.37±0.13	1	17.698±0.194	14.943±0.069	>12.409	16.812±0.045	15.001±0.022	41061888
ULAS 1335+1130	18.25±0.01	25	16.939±0.104	13.892±0.039	12.151±0.358	15.989±0.030	13.939±0.018	44755712
SDSS 1346-0031	15.84±0.05	26	15.398±0.038	13.632±0.034	11.921±0.239	14.667±0.020	13.672±0.018	44718080
WISE 1405+5534	21.50±0.07	15	18.765±0.396	14.097±0.037	12.204±0.263	16.876±0.046	14.058±0.019	40836864
ULAS 1416+1348	17.62±0.02	27	15.992±0.185	12.782±0.037	12.231±0.301	14.735±0.021	12.796±0.017	44771840
GI 547B (1423+0116)	18.96±0.07	40	17.988±0.255	14.850±0.065	>12.689	16.726±0.043	14.694±0.021	44577536
VHS 1433-0837	19.42±0.21	1	>18.914	15.240±0.091	>12.784	17.141±0.055	15.040±0.022	41751808
WISE 1436-1814	>17.62	40	16.887±0.108	14.603±0.063	12.596±0.436	15.985±0.030	14.717±0.021	41512704
WISE 1448-2534	18.91±0.12	1	18.086±0.345	14.958±0.090	>12.535	17.203±0.058	15.094±0.022	44590592
GI 570D (1457-2121)	15.28±0.05	28	14.932±0.038	12.129±0.024	10.784±0.086	13.877±0.018	12.150±0.017	44705536
WISE 1457+5815	16.64±0.29	46	16.661±0.059	14.417±0.037	13.068±0.505	15.848±0.028	14.441±0.019	40819968
WISE 1501-4004	16.38±0.04	1	16.091±0.060	14.233±0.043	>12.543	15.282±0.023	14.131±0.019	44722432
2MASS 1503+2525	13.86±0.03	46	13.436±0.024	11.720±0.021	10.709±0.071	12.792±0.017	11.744±0.017	45129472
SDSS 1504+1027	16.84±0.02	1	16.215±0.055	14.063±0.039	12.603±0.411	15.504±0.025	14.060±0.019	44731904
GI 576B (1504+0538)	17.02±0.03	1	15.999±0.050	14.234±0.043	>12.234	15.481±0.025	14.250±0.020	44734976
WISE 1506+7027	13.92±0.01	1	13.403±0.024	11.276±0.019	10.188±0.039	12.627±0.017	11.314±0.016	41557248
WISE 1517+0529	18.85±0.04	1	18.166±0.322	15.119±0.082	>12.648	16.846±0.046	15.102±0.023	44547328
WISE 1519+7009	18.28±0.07	8	17.084±0.069	14.138±0.031	13.264±0.495	16.192±0.033	14.087±0.019	40832768
WISE 1523+3125	18.69±0.18	40	17.664±0.167	14.385±0.038	>12.884	15.947±0.029	14.274±0.019	41496576
WISE 1541-2250 <sup>c</sup>	21.07±0.07	2	16.736±0.165	14.246±0.063	>12.312	16.658±0.042	14.228±0.019	41788672
WISE 1542+2230	20.52±0.05	15	18.846±0.425	15.043±0.061	>13.014	17.257±0.059	15.057±0.022	41058816
2MASS 1553+1532	15.94±0.16	46	15.291±0.037	13.033±0.028	12.059±0.330	14.509±0.020	13.131±0.017	44782080
WISE 1612-3420	16.96±0.03	40	17.415±0.199	13.984±0.045	>12.123	15.444±0.025	13.856±0.018	40825088
WISE 1614+1739	19.31±0.04	2	18.174±0.266	14.226±0.040	>12.244	16.425±0.036	14.217±0.019	40832256
2MASS 1615+1340	16.49±0.25	46	16.140±0.051	14.114±0.039	>12.063	15.388±0.024	14.143±0.019	44726528
WISE 1617+1807	18.23±0.08	8	16.936±0.091	14.063±0.036	12.378±0.388	15.961±0.029	14.095±0.019	40834048
WISE 1622-0959	16.05±0.05	8	16.240±0.073	14.162±0.049	>11.960	15.362±0.024	14.145±0.019	40830464
SDSS 1624+0029	15.48±0.05	31	15.163±0.040	13.088±0.029	12.163±0.394	14.408±0.020	13.101±0.017	44709120
WISE 1627+3255	16.40±0.05	8	16.195±0.050	13.584±0.029	>12.178	15.216±0.023	13.616±0.018	40825600
SDSS 1628+2308	16.63±0.03	4	16.267±0.052	13.922±0.035	11.802±0.250	15.441±0.025	13.941±0.019	44765440
WISE 1639-6847	20.75±0.03	15	17.266±0.187	13.544±0.059	>11.755	16.186±0.018	13.588±0.016	52672000
WISE 1653+4444	17.53±0.05	8	16.485±0.048	13.824±0.029	12.208±0.270	15.668±0.026	13.867±0.018	40828928
WISE 1711+3500	>18.1	8	17.800±0.159	14.634±0.044	12.844±0.460	16.455±0.037	14.622±0.020	40829184
WISE 1717+6128	18.91±0.09	8	17.760±0.108	15.008±0.045	13.422±0.460	17.071±0.053	15.138±0.022	40823040
WISE 1721+1117	16.41±0.10	1	15.815±0.050	14.316±0.047	12.463±0.498	15.237±0.023	14.352±0.020	45106432
WISE 1735-8209	16.68±0.03	1	15.570±0.036	13.723±0.029	>12.175	15.104±0.022	13.796±0.018	41799168
WISE 1738+2732	20.25±0.03	15	17.710±0.157	14.497±0.043	12.448±0.399	17.093±0.053	14.473±0.019	40828416
WISE 1741+2553	16.63±0.03	8	15.301±0.036	12.347±0.023	10.698±0.084	14.426±0.020	12.387±0.017	40820480
SDSS 1758+4633	16.20±0.03	10	15.648±0.034	13.802±0.029	12.351±0.289	14.838±0.021	13.856±0.018	45139712
WISE 1804+3117	19.21±0.11	8	18.184±0.278	14.590±0.046	>12.150	16.608±0.039	14.600±0.020	40836352
WISE 1812+2721	18.83±0.16	8	17.468±0.143	14.196±0.039	>12.095	16.323±0.034	14.173±0.019	41564160
WISE 1812+2007	18.95±0.06	40	>18.843	15.277±0.081	>12.676	16.956±0.049	15.024±0.022	41793536
WISE 1813+2835	17.27±0.02	1	15.583±0.042	14.040±0.035	12.384±0.366	15.820±0.028	14.186±0.019	45079296
WISE 1828+2650	22.73±0.13	2	>18.248	14.353±0.045	12.444±0.338	16.915±0.020	14.321±0.020	39526656
SCR 1845-6357B	13.19±0.03	33	...	...	...	...	...	...
WISE 1852+3537	16.76±0.01	1	15.946±0.047	14.139±0.040	12.229±0.323	15.582±0.026	14.186±0.019	40836096
WISE 1906+4508	16.32±0.09	8	16.033±0.045	13.815±0.033	12.876±0.469	15.030±0.023	13.816±0.018	41803520
WISE 1928+2356	14.29±0.01	45	13.574±0.027	12.023±0.023	10.802±0.094	13.139±0.017	12.063±0.017	45140480
WISE 1955-2540	18.00±0.05	40	17.986±0.305	14.963±0.089	>11.860	16.609±0.040	15.027±0.022	41800704

Table 2 continued

Table 2 (continued)

Object	$H$	$H$	W1	W2	W3	ch1	ch2	AOR
Name	(mag)	Ref.	(mag)	(mag)	(mag)	(mag)	(mag)	Used
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
WISE 1959-3338	17.18±0.05	8	16.152±0.065	13.838±0.039	>12.256	15.360±0.024	13.785±0.018	40823552
WISE 2000+3629	15.74±0.01	1	15.080±0.056	12.690±0.028	11.207±0.098	14.221±0.020	12.675±0.017	44792064
WISE 2005+5424	19.57±0.08	1	17.693±0.138	14.872±0.046	>12.430	15.870±0.028	14.625±0.020	41456640
WISE 2015+6646	16.50±0.09	40	16.472±0.046	14.700±0.041	>12.836	16.321±0.034	14.623±0.020	41442048
WISE 2017-3421	20.37±0.27	1	18.358±0.525	14.945±0.080	>12.520	16.729±0.043	14.874±0.022	41743616
WISE 2018-7423	17.17±0.04	40	16.490±0.068	13.607±0.031	>12.046	15.281±0.023	13.552±0.018	41561856
WISE 2019-1148	18.23±0.07	40	17.256±0.152	14.305±0.052	>11.959	16.028±0.031	14.251±0.020	41783296
WISE 2056+1459	19.64±0.03	15	16.480±0.075	13.839±0.037	11.731±0.249	16.031±0.030	13.923±0.018	40836608
WISE 2102-4429	18.58±0.07	1	16.951±0.111	14.139±0.043	>12.056	16.325±0.036	14.223±0.019	41704192
WISE 2134-7137	19.70±0.15	8	17.605±0.146	13.962±0.036	12.389±0.396	16.171±0.032	13.956±0.018	40827648
ULAS 2146-0010	18.77±0.03	36	15.819±0.056	14.085±0.043	>12.312	16.389±0.011	14.420±0.016	28830976
WISE 2147-1029	17.73±0.09	1	17.813±0.258	15.007±0.095	>12.143	16.551±0.039	14.959±0.021	41066240
WISE 2157+2659	17.45±0.04	8	16.990±0.107	14.493±0.048	>11.968	16.012±0.030	14.437±0.019	41046272
WISE 2159-4808	19.25±0.12	1	17.637±0.184	14.613±0.053	>11.523	16.841±0.046	14.579±0.020	41060608
WISE 2203+4619	...	-	>18.919	14.967±0.069	>12.267	16.365±0.014	14.642±0.016	50033152
Gl 845C (2204-5646)	13.27±0.02	32	...	...	...	...	...	...
WISE 2209+2711	22.39±0.15	15	>18.831	14.770±0.055	12.455±0.387	17.815±0.087	14.739±0.020	40821248
WISE 2209-2734	17.08±0.05	1	16.314±0.077	13.856±0.041	>11.945	15.478±0.025	13.899±0.018	40819456
WISE 2211-4758	17.79±0.04	43	17.470±0.143	14.607±0.051	12.508±0.476	16.380±0.035	14.618±0.020	44572160
WISE 2212-6931	20.23±0.04	15	17.259±0.122	14.873±0.061	>12.621	17.364±0.063	14.973±0.021	41770752
WISE 2213+0911	16.99±0.11	1	16.579±0.080	14.648±0.060	>12.261	15.790±0.028	14.564±0.020	41523712
WISE 2220-3628	20.86±0.04	15	>18.772	14.714±0.056	>12.292	17.200±0.057	14.736±0.021	44552448
WISE 2226+0440	17.32±0.02	1	16.864±0.112	14.505±0.055	>12.356	16.122±0.031	14.543±0.020	40837376
2MASS 2228-4310	15.36±0.12	46	15.235±0.040	13.326±0.030	11.748±0.273	14.453±0.020	13.353±0.018	45140736
WISE 2232-5730	19.20±0.10	1	17.592±0.178	15.201±0.079	11.900±0.315	17.435±0.066	15.176±0.022	41071616
WISE 2237+7228	15.94±0.21	40	15.563±0.037	13.592±0.029	12.333±0.332	14.607±0.020	13.557±0.018	44736000
WISE 2255-3118	17.70±0.11	8	16.550±0.079	14.161±0.045	>11.932	15.914±0.029	14.210±0.019	40835584
WISE 2301+0216	16.70±0.03	44	16.199±0.066	14.343±0.051	>12.104	15.601±0.026	14.367±0.019	44777728
WISE 2302-7134	17.79±0.12	1	16.846±0.081	14.240±0.040	>12.594	15.991±0.030	14.232±0.019	41723904
WISE 2313-8037	17.28±0.14	35	16.437±0.054	13.676±0.027	12.474±0.363	15.289±0.023	13.683±0.018	41530368
WISE 2319-1844	18.00±0.05	1	16.668±0.087	13.822±0.041	>11.779	15.919±0.029	13.949±0.018	41052928
ULAS 2321+1354	17.09±0.06	44	16.937±0.122	14.108±0.059	>12.337	15.860±0.028	14.191±0.019	44757504
WISE 2325-4105	19.22±0.11	8	17.064±0.114	14.108±0.040	>12.263	16.264±0.033	14.086±0.019	40827904
ULAS 2326+0201	18.46±0.12	44	17.959±0.293	15.531±0.127	>12.354	16.879±0.015	15.442±0.016	45060352
WISE 2332-4325	19.57±0.15	1	17.973±0.240	14.958±0.066	>12.210	17.271±0.059	15.012±0.021	40822272
WISE 2340-0745	16.19±0.06	8	15.934±0.058	13.600±0.036	>11.921	15.194±0.023	13.624±0.018	40830208
ULAS 2342+0856	16.73±0.03	44	15.969±0.059	13.951±0.042	>12.427	15.287±0.024	13.987±0.019	44765696
WISE 2343-7418	16.14±0.04	1	15.669±0.038	13.756±0.031	12.786±0.504	15.036±0.022	13.752±0.018	41727488
WISE 2344+1034	19.07±0.11	8	18.137±0.347	14.941±0.078	>12.345	16.733±0.042	14.907±0.021	41060352
WISE 2348-1028	16.93±0.12	8	16.647±0.093	14.381±0.051	>12.355	15.870±0.028	14.357±0.019	40831232
WISE 2354+0240	22.88±0.30	15	>18.263	15.007±0.085	>12.278	18.105±0.109	15.013±0.022	44790528
WISE 2357+1227	16.49±0.03	44	15.742±0.048	14.018±0.040	12.101±0.369	15.259±0.023	14.103±0.019	45154304

Table 2 continued



Table 2 (continued)

Object	<i>H</i>	<i>H</i>	W1	W2	W3	ch1	ch2	AOR
Name	(mag)	Ref.	(mag)	(mag)	(mag)	(mag)	(mag)	Used
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)

NOTE—For resolved photometry of binaries, see Table 5 of Leggett et al. (2015). For VHS *H*-band magnitudes, the hAperMag3 was chosen, per the recommendations given at <http://horus.roe.ac.uk/vsa/dboverview.html>. The AperMag3 values from ULAS and UGPS were also the ones used. References for *H*-band magnitudes: (1) this paper, (2) Leggett et al. 2015, (3) Warren et al. 2007a, (4) Chiu et al. 2006, (5) Liu et al. 2007, (6) Leggett et al. 2010, (7) Delorme et al. 2008, (8) Kirkpatrick et al. 2011, (9) UKIDSS - Lawrence et al. 2007, (10) Knapp et al. 2004, (11) Liu et al. 2011, (12) Pinfield et al. 2014, (13) Leggett et al. 2013, (14) Leggett et al. 2017, (15) Schneider et al. 2015, (16) Luhman & Esplin 2016, (17) Leggett et al. 2002, (18) Lucas et al. 2010, (19) Pinfield et al. 2008, (20) Lodieu et al. 2007, (21) Leggett et al. 2009, (22) Burningham et al. 2013, (23) Wright et al. 2013, (24) Goldman et al. 2010, (25) Burningham et al. 2008, (26) Tsvetanov et al. 2000, (27) Burningham et al. 2010, (28) Pinfield et al. 2012, (29) Geballe et al. 2001, (30) Scholz 2010, (31) Strauss et al. 1999, (32) McCaughrean et al. 2004, (33) Kasper et al. 2007, (34) Cushing et al. 2014, (35) Kirkpatrick et al. 2012, (36) Burningham et al. 2009, (37) Pinfield et al. 2014, (38) 2MASS Survey Point Source Reject Table - Skrutskie et al. 2006, (39) Albert et al. 2011, (40) Mace et al. 2013, (41) Martin et al., submitted, (42) Dupuy et al. 2015, (43) VHS - McMahon et al. 2013, (44) ULAS - Warren et al. 2007b, (45) UGPS - Lucas et al. 2008, (46) 2MASS All-Sky Point Source Catalog - Skrutskie et al. 2006.

<sup>a</sup> 0039+2115: *Spitzer* photometry is from Luhman et al. (2007).

<sup>b</sup> 0521+3640: AllWISE W1 photometry highly contaminated by the halo of a much brighter star.

<sup>c</sup> 0807–6618: W2 photometry is from a preliminary CatWISE detection (Meisner et al. 2018a). *Spitzer* photometry is from Luhman et al. (2012).

<sup>d</sup> 0855–0714: W1 magnitude is measured by ELW from a moving coadd using eleven epochs of *WISE* and *NEOWISE* data between early 2010 and mid 2018. The epochs themselves are comprised of 177 individual exposures. The software includes one moving source (*WISE* 0855–0714 itself) and a grid of 275 fixed background sources that model the fixed celestial pattern. The two known interfering sources in the 2010 epochs (see Wright et al. 2014) are measured, free of contamination by *WISE* 0855–0714, and are allowed for when using the 2010 data. The fit, which uses a scaled PSF for each source (moving or fixed) and a flat background for each frame, is in principle immune to confusion noise. The resulting W1 magnitude is much dimmer than the measurement made by Wright et al. (2014), which used only 1 epoch of *NEOWISE* Reactivation data. This new W1 measurement is a  $2.1\sigma$  detection (flux =  $1.896 \pm 0.905 \mu\text{Jy}$ ; most likely value is  $1.809 \mu\text{Jy}$ ).

<sup>e</sup> 1541–2250: *WISE* photometry is from the All-Sky Catalog.

#### 4. SPITZER OBSERVATIONS

A list of 142 objects from Table 1 was astrometrically monitored with *Spitzer*/IRAC. Most of the *Spitzer* data came from programs 70062, 80109, 90007, 11059, and 13012 (Kirkpatrick, PI). The earliest of these programs, 70062 and 80109, were primarily aimed at photometric characterization of *WISE*-selected brown dwarf candidates using the  $3.6 \mu\text{m}$  (hereafter, ch1) and  $4.5 \mu\text{m}$  (hereafter, ch2) bandpasses of IRAC. In these two programs, a cycling dither pattern of medium scale and a five-position dither were used with frame times of 30 s in both channels. However, candidates with the reddest *WISE* W1–W2 colors were also observed at subsequent epochs only in ch2 to provide early astrometric monitoring to supplement *Spitzer* astrometric programs planned for later. Additional photometric characterization of brown dwarf candidates selected later in the *WISE* mission was obtained in program 11059. In this program, ch1 and ch2 observations were obtained using a random dither pattern of medium scale and nine dither positions, again with frame times of 30 s. Our main astrometric monitoring campaigns were programs 90007 and 13012, which are described further below.

We chose ch2 for our astrometric follow-up for a variety of reasons, which are listed in Martin et al. (2018) but reiterated here. During *Spitzer* cryogenic operations, ch1 was more sensitive than ch2, but after cryogen depletion the deep image noise was found to be 12% worse in ch1 and 10% better in ch2, making the channels comparable in sensitivity for average field stars (ch1–ch2  $\approx 0$  mag; Carey et al. 2010).

Another change during warm operations was the behavior of latent images from bright objects. Whereas latents in ch2 decay rapidly (typically within ten minutes), ch1 latents decay on timescales of hours. Moreover, the ch2 intra-pixel sensitivity variation (aka, the pixel phase effect) is about half that of ch1. Given these points, the fact that the point response function (PRF) is less undersampled in ch2 than in ch1, and the fact that our cold brown dwarfs are also much brighter in ch2 than in ch1 ( $1.0 < \text{ch1} - \text{ch2} < 3.0$  mag), we choose to do our imaging in ch2.

Programs 90007 and 13012 were designed exclusively for astrometric monitoring, with program 90007 providing data to satisfy the minimum astrometric requirement and program 13012 extending the time baseline to improve the astrometric uncertainties. The Lutz-Kelker bias sets the fundamental requirement for the precision we targeted. The Lutz-Kelker effect, a systematic error inherent in the measurements of trigonometric parallax for a volume-limited set of stars, is induced as follows. Near the maximum distance,  $d_{\text{max}}$ , the volume of stars just inside, ( $d_{\text{max}} - \Delta d$ ), is smaller than that just outside, ( $d_{\text{max}} + \Delta d$ ), meaning that there are more stars able to scatter into the volume than can scatter outside. This means that the true average parallax is smaller than the average parallax that is measured. Figure 1 of Lutz & Kelker (1973) demonstrates that the astrometric error needed to correct this effect must be  $\leq 15\%$  or else the effect is uncorrectable. For our distance limit of 20 pc (a parallax of 50 mas), this sets the error floor at 7.5 mas. Ideally, we would like to have errors even smaller; for example, an error of 10% (5 mas) reduces

the bias on the absolute magnitude determination from 0.28 mag to 0.11 mag (see Table 1 of Lutz & Kelker 1973).

Our AORs for program 90007 were designed so targets were acquired with a signal-to-noise ratio (S/N) of  $\geq 100$  per epoch. Theoretically, the best astrometric precision we can expect from a single measurement (see equation 1 of Monet et al. 2010) is  $\text{FWHM}/(2 \times \text{S/N}) = 1''/7/(2 \times 100) = 8.5$  mas, where the full width at half maximum (FWHM) is the ch2 value from Table 2.1 of the IRAC Instrument Handbook. However, our ability to fully correct for astrometric distortion keeps us from reaching this theoretical floor. We conservatively estimated that we could achieve  $\sim 15$  mas precision after distortion is taken into account. Because we had already acquired earlier *Spitzer* epochs that would allow us to measure the proper motion and disentangle it from the parallax, we assumed that the error in the parallax would be roughly equal to the per-epoch-precision divided by the square root of the number of epochs measured in program 90007. For a per-epoch-precision of 15 mas and a final parallactic error of  $< 10\%$ , at least nine measurement epochs for each source were required. Hence, in program 9007, the per-epoch goal of  $\text{S/N} > 100$  per target was accomplished with a total ch2 integration time of 270 s acquired using a random dither pattern of medium scale, nine dither positions, and individual frame times of 30 s. This same procedure was used for program 13012.

Timing constraints were placed on the observations to optimize the measurement of parallax. The *Spitzer* viewing zone falls between  $82.5^\circ$  deg and  $120^\circ$  solar elongation, which encompasses the maximum parallax factor (at  $90^\circ$ ) critical

to our program. For targets having two *Spitzer* visibility windows per year, one Astronomical Observation Request (AOR) was placed within 3.5 days of each maximum parallax factor. The other two or three AORs were evenly spaced through the rest of the visibility period. For targets near, but not in, the Continuous Viewing Zone, five or six observations were obtained at roughly evenly spaced intervals within each window, with an AOR landing within  $\pm 3.5$  days of each available maximum parallax factor. For targets located within the Continuous Viewing Zone, ten to twelve observations were used each year, again with an AOR falling within 3.5 days of each available maximum parallax factor. Slight adjustments to these constraints had to be made to fit within the calendar dates of each cycle, and other post facto adjustments were included when the observed data were corrupted by (rarely occurring) coronal mass ejection events from the Sun. These timing constraints were determined using a program written by one of us (ELW) that calculates the time of maximum parallax factor for each target using the predicted *Spitzer* ephemerides available from JPL Horizons<sup>2</sup>.

Although program 13012 was granted a full two years of observation and is ongoing, this paper uses only those data taken by 2017 Oct 20 (UT). This date was chosen so that each target will have been observed through at least two maximum parallax factors in *Spitzer* Cycle 13. Future Cycle 13 observations will be included in a subsequent paper presenting our final parallactic measurements. A listing of the first and last observation date, total time baseline, and number of AORs per program for each target is given in Table 3.

**Table 3.** Objects on the IRAC ch2 *Spitzer* Parallax Program

Object	First Obs. Date	Last Obs. Date	Baseline	Program # (and # of Epochs)
Name	(UT)	(UT)	(yr)	with ch2 Coverage
(1)	(2)	(3)	(4)	(5)
WISE 0005+3737	2012 Sep 06	2017 Apr 22	4.6	80109(1), 90007(12), 13012(6)
WISE 0015-4615	2010 Dec 17	2017 Sep 10	6.7	70062(2), 90007(12), 13012(5)
WISE 0032-4946	2012 Jul 28	2017 Sep 12	5.1	80109(1), 90007(12), 13012(6)
2MASS 0034+0523	2012 Feb 15	2017 Apr 14	5.2	80109(2), 90007(12), 13012(6)
WISE 0038+2758	2012 Mar 22	2017 Apr 22	5.1	80109(2), 90007(14), 13012(6)
WISE 0049+2151	2012 Mar 22	2017 Apr 24	5.1	80109(2), 90007(12), 13012(6)
WISE 0123+4142	2011 Mar 25	2017 May 13	6.1	70062(1), 13012(6)
CFBDS 0133+0231	2012 Sep 13	2017 Apr 24	4.6	80109(1), 90007(12), 13012(6)
WISE 0146+4234AB	2011 Apr 05	2017 May 15	6.1	70062(1), 80109(2), 90007(12), 13012(6)
WISE 0221+3842	2011 Mar 31	2017 May 17	6.1	70062(1), 13012(6)
WISE 0226-0211AB	2010 Sep 18	2017 May 08	6.6	70062(2), 80109(1), 13012(6)
WISE 0233+3030	2012 Mar 22	2017 May 18	5.2	80109(2), 13012(6)
WISE 0241-3653	2011 Jan 19	2017 Apr 23	6.3	70062(1), 80109(2), 90007(12), 13012(6)
WISE 0247+3725	2011 Apr 12	2017 May 23	6.1	70062(1), 80109(1), 90007(12), 13012(6)

*Table 3 continued*

<sup>2</sup> See <https://ssd.jpl.nasa.gov/?horizons>.

Table 3 (continued)

Object	First Obs. Date	Last Obs. Date	Baseline	Program # (and # of Epochs)
Name	(UT)	(UT)	(yr)	with ch2 Coverage
(1)	(2)	(3)	(4)	(5)
WISE 0302–5817	2015 Feb 10	2017 Oct 02	2.6	11059(1), 13012(8)
WISE 0304–2705	2014 Oct 20	2017 May 09	2.6	10135(1), 13012(6)
WISE 0309–5016	2010 Dec 22	2017 May 05	6.4	70062(1), 80109(2), 13012(6)
WISE 0313+7807	2010 Dec 21	2017 Jun 16	6.5	70062(2), 80109(2), 13012(6)
WISE 0316+4307	2011 Nov 19	2017 Jun 02	5.5	80109(1), 90007(12), 13012(6)
WISE 0323–5907	2010 Dec 18	2017 Apr 23	6.3	70062(2), 13012(6)
WISE 0323–6025	2010 Sep 18	2017 Apr 23	6.6	70062(2), 80109(1), 90007(10), 13012(5)
WISE 0325–5044	2011 Nov 19	2017 May 09	5.5	80109(1), 90007(10), 13012(5)
WISE 0325–3854	2011 Jan 30	2017 May 03	6.3	70062(1), 80109(1), 13012(6)
WISE 0325+0831	2011 Apr 12	2017 May 23	6.1	70062(1), 90007(12), 13012(6)
WISE 0335+4310	2011 Apr 19	2017 Jun 05	6.1	70062(1), 80109(1), 90007(12), 13012(6)
WISE 0336–0143	2011 Apr 12	2017 May 29	6.1	70062(1), 80109(1), 90007(12), 13012(6)
WISE 0350–5658	2010 Sep 18	2017 May 13	6.6	70062(2), 80109(2), 90007(10), 13012(6)
WISE 0359–5401	2010 Sep 18	2017 May 19	6.7	70062(2), 80109(2), 90007(12), 13012(5)
WISE 0404–6420	2011 Nov 20	2017 May 05	5.5	80109(1), 90007(10), 13012(5)
WISE 0410+1502	2010 Oct 21	2017 Jun 05	6.6	70062(2), 80109(2), 90007(12), 13012(6)
WISE 0413–4750	2011 Nov 19	2017 May 28	5.5	80109(1), 13012(6)
WISE 0430+4633	2012 Apr 19	2017 Jun 16	5.2	80109(1), 13012(6)
WISE 0458+6434AB	2010 Oct 29	2017 Jun 22	6.6	70062(2), 80109(1), 13012(6)
WISE 0500–1223	2010 Oct 18	2017 Jun 19	6.7	70062(2), 80109(1), 13012(6)
WISE 0512–3004	2010 Dec 19	2017 Jun 20	6.5	70062(2), 80109(1), 90007(12), 13012(6)
WISE 0535–7500	2010 Oct 17	2017 Sep 12	6.9	70062(2), 80109(2), 90007(10), 13012(6)
WISE 0540+4832	2012 Apr 23	2017 Jun 02	5.1	80109(1), 90007(12), 13012(4)
WISE 0614+0951	2010 Dec 17	2017 Jul 05	6.5	70062(2), 80109(2), 90007(12), 13012(6)
WISE 0645–0302	2012 Jan 07	2017 Jul 20	5.5	80109(1), 13012(6)
WISE 0647–6232	2010 Sep 19	2017 Sep 10	7.0	70062(2), 80109(1), 90007(10), 13012(6)
WISE 0713–5854	2012 Mar 20	2017 Oct 13	5.6	80109(1), 13012(5)
WISE 0713–2917	2012 Jan 02	2017 Aug 01	5.6	80109(1), 90007(12), 13012(6)
WISE 0723+3403	2010 Nov 25	2017 Jul 24	6.7	70062(2), 80109(1), 13012(6)
WISE 0734–7157	2011 Apr 19	2017 Aug 19	6.3	70062(1), 80109(1), 90007(10), 13012(5)
WISE 0744+5628	2011 Jun 02	2017 Jul 18	6.1	70062(1), 80109(2), 90007(12), 13012(6)
WISE 0759–4904	2011 Jan 02	2017 Sep 15	6.7	70062(2), 80109(1), 90007(10), 13012(6)
WISE 0812+4021	2010 Dec 09	2017 Aug 02	6.6	70062(2), 80109(1), 90007(12), 13012(6)
WISE 0825+2805	2012 Jan 07	2017 Aug 04	5.6	80109(2), 90007(12), 13012(6)
WISE 0833+0052	2013 Jan 03	2017 Aug 13	4.6	80077(1), 13012(6)
WISE 0836–1859	2011 Jan 01	2017 Aug 24	6.6	70062(2), 80109(1), 13012(6)
WISE 0855–0714	2013 Jun 21	2017 Aug 24	4.2	90095(3), 10168(4), 13012(6)
WISE 0857+5604	2010 Dec 18	2017 Aug 03	6.6	70062(2), 80109(1), 90007(12), 13012(6)
WISE 0906+4735	2010 Dec 23	2017 Aug 04	6.6	70062(2), 80109(2), 13012(6)
WISE 0914–3459	2012 Jun 19	2017 Sep 10	5.2	80109(1), 13012(6)
WISE 0940–2208	2012 Feb 03	2017 Sep 10	5.6	80109(1), 13012(6)
WISE 0943+3607	2010 Dec 23	2017 Aug 19	6.7	70062(2), 80109(1), 90007(12), 13012(6)
WISE 0952+1955	2011 Jan 01	2017 Aug 26	6.7	70062(2), 80109(2), 13012(6)
WISE 1018–2445	2011 Jan 26	2017 Sep 19	6.6	70062(1), 80109(2), 13012(6)
WISE 1025+0307	2012 Jul 07	2017 Sep 13	5.2	80109(1), 90007(11), 13012(6)
CFBDS 1028+5654	2010 Dec 20	2017 Aug 19	6.7	70021(1), 90007(12), 13012(6)
WISE 1039–1600	2011 Jan 26	2017 Sep 19	6.6	70062(1), 80109(1), 90007(12), 13012(6)
ULAS 1043+1048	2012 Feb 01	2017 Sep 09	5.6	70058(1), 13012(6)
WISE 1050+5056	2012 Jun 12	2017 Aug 26	5.2	80109(1), 13012(6)
WISE 1051–2138	2011 Mar 13	2017 Sep 30	6.6	70062(1), 90007(11), 13012(6)
WISE 1052–1942	2011 Jan 31	2017 Sep 30	6.7	70062(1), 13012(6)

Table 3 continued

**Table 3** (*continued*)

Object	First Obs. Date	Last Obs. Date	Baseline	Program # (and # of Epochs)
Name	(UT)	(UT)	(yr)	with ch2 Coverage
(1)	(2)	(3)	(4)	(5)
WISE 1055–1652	2012 Jul 16	2017 Sep 30	5.2	80109(1), 90007(9), 13012(6)
WISE 1124–0421	2012 Jul 19	2017 Sep 30	5.2	80109(1), 90007(11), 13012(6)
WISE 1139–3324	2012 Aug 22	2017 Oct 13	5.1	80109(1), 13012(7)
WISE 1141–3326	2012 Aug 22	2017 Oct 13	5.1	80109(1), 13012(7)
WISE 1143+4431	2012 Mar 04	2017 Sep 10	5.5	80109(1), 13012(6)
WISE 1150+6302	2010 Dec 23	2017 Aug 23	6.7	70062(2), 80109(1), 90007(12), 13012(6)
ULAS 1152+1134	2012 Mar 18	2017 Sep 28	5.5	80109(1), 13012(5)
WISE 1206+8401	2010 Dec 09	2017 Aug 03	6.6	70062(2), 80109(1), 90007(12), 13012(6)
WISE 1217+1626AB	2011 Mar 12	2017 Sep 30	6.6	70062(1), 80109(2), 13012(6)
WISE 1220+5407	2015 Feb 10	2017 Sep 10	2.6	11059(1), 13012(6)
WISE 1221–3136	2012 Aug 12	2017 May 19	4.8	80109(1), 90007(12), 13012(5)
WISE 1225–1013	2012 Mar 18	2017 Oct 12	5.6	80109(1), 90007(12), 13012(6)
2MASS 1231+0847	2012 Sep 01	2017 Oct 09	5.1	80109(1), 13012(6)
WISE 1243+8445	2011 Nov 21	2017 Jul 29	5.7	80109(1), 13012(6)
WISE 1254–0728	2012 Mar 30	2017 Oct 20	5.6	80109(1), 13012(8)
WISE 1257+4008	2011 Jan 29	2017 Sep 25	6.7	70062(1), 13012(6)
VHS 1258–4412	2012 Apr 21	2017 Jun 06	5.1	80109(1), 13012(6)
WISE 1301–0302	2012 Aug 22	2017 Oct 20	5.2	80109(1), 13012(8)
WISE 1318–1758	2011 Apr 12	2017 May 27	6.1	70062(1), 80109(2), 90007(12), 13012(5)
WISE 1333–1607	2011 Apr 12	2017 May 31	6.1	70062(1), 13012(5)
WISE 1405+5534	2011 Jan 22	2017 Oct 10	6.7	70062(1), 80109(2), 90007(10), 13012(6)
VHS 1433–0837	2011 Apr 19	2017 Jun 07	6.1	70062(1), 80109(2), 13012(6)
WISE 1436–1814	2011 Apr 19	2017 Jun 10	6.1	70062(1), 80109(2), 90007(12), 13012(6)
WISE 1448–2534	2012 Apr 29	2017 Jun 17	5.1	80109(1), 90007(12), 13012(6)
WISE 1501–4004	2012 Apr 21	2017 Jun 28	5.2	80109(1), 13012(6)
WISE 1517+0529	2012 Apr 04	2017 Jun 19	5.2	80109(1), 13012(6)
WISE 1519+7009	2010 Dec 09	2017 Sep 25	6.8	70062(2), 80109(1), 90007(10), 13012(6)
WISE 1523+3125	2011 Apr 16	2017 Jun 28	6.2	70062(1), 80109(2), 13012(6)
WISE 1541–2250	2011 Apr 13	2017 Jun 26	6.2	70062(1), 80109(2), 90007(12), 13012(6)
WISE 1542+2230	2011 Apr 18	2017 Jun 26	6.2	70062(1), 80109(2), 13012(6)
WISE 1612–3420	2010 Sep 18	2017 Jul 05	6.8	70062(2), 80109(1), 13012(6)
WISE 1614+1739	2010 Sep 20	2017 Jul 07	6.8	70062(2), 80109(2), 13012(6)
2MASS 1615+1340	2012 Apr 28	2017 Jul 07	5.2	80109(2), 90007(12), 13012(6)
WISE 1622–0959	2010 Sep 18	2017 Jul 05	6.8	70062(2), 80109(2), 13012(6)
WISE 1639–6847	2012 May 12	2017 Aug 01	4.2 <sup>a</sup>	80109(1), 90007(12), 11059(1), 13012(6)
WISE 1653+4444	2010 Sep 20	2017 May 31	6.7	70062(2), 80109(2), 90007(10), 13012(4)
WISE 1711+3500AB	2010 Sep 18	2017 Aug 24	6.9	70062(2), 80109(1), 90007(12), 13012(6)
WISE 1717+6128	2010 Sep 19	2017 Jul 15	6.8	70062(2), 80109(1), 13012(6)
WISE 1721+1117	2012 May 12	2017 Jul 24	5.2	80109(1), 13012(6)
WISE 1735–8209	2011 Jun 17	2017 Sep 07	6.2	70062(1), 13012(6)
WISE 1738+2732	2010 Sep 18	2017 Aug 14	6.9	70062(2), 80109(2), 90007(12), 13012(6)
WISE 1804+3117	2010 Sep 26	2017 Sep 04	6.9	70062(2), 80109(2), 13012(6)
WISE 1812+2007	2011 Jun 11	2017 Aug 15	6.2	70062(1), 80109(1), 13012(6)
WISE 1813+2835	2012 May 19	2017 Sep 01	5.3	80109(1), 90007(12), 13012(6)
WISE 1828+2650	2010 Jul 10	2017 Aug 30	7.1	551(1), 70062(1), 80109(2), 90007(12), 13012(6)
WISE 1928+2356	2012 Jun 21	2017 Sep 14	5.2	80109(1), 90007(12), 13012(6)
WISE 1955–2540	2011 Jun 26	2017 Aug 24	6.2	70062(1), 90007(11), 13012(6)
WISE 1959–3338	2011 Jun 07	2017 Aug 24	6.2	70062(2), 80109(2), 90007(12), 13012(6)
WISE 2000+3629	2012 Jul 18	2017 Oct 17	5.2	80109(1), 90007(12), 13012(7)
WISE 2005+5424	2010 Dec 31	2017 Sep 10	6.7	70062(2), 80109(1), 13012(7)
WISE 2015+6646	2010 Dec 31	2017 May 19	6.4	70062(2), 90007(10), 13012(5)

*Table 3 continued*

Table 3 (continued)

Object	First Obs. Date	Last Obs. Date	Baseline	Program # (and # of Epochs)
Name	(UT)	(UT)	(yr)	with ch2 Coverage
(1)	(2)	(3)	(4)	(5)
WISE 2017–3421	2011 Jun 09	2017 Sep 01	6.2	70062(1), 13012(6)
WISE 2019–1148	2011 Jun 15	2017 Sep 01	6.2	70062(1), 80109(2), 13012(6)
WISE 2056+1459	2010 Dec 10	2017 Oct 01	6.8	70062(2), 80109(2), 90007(12), 13012(6)
WISE 2147–1029	2010 Dec 22	2017 Sep 25	6.8	70062(2), 13012(6)
WISE 2157+2659	2010 Dec 23	2017 Sep 20	6.7	70062(2), 80109(2), 90007(12), 13012(6)
WISE 2159–4808	2011 Jun 22	2017 Sep 21	6.2	70062(2), 80109(1), 90007(12), 13012(6)
WISE 2203+4619	2014 Sep 22	2017 Oct 01	3.0	10135(1), 13012(7)
WISE 2209+2711	2010 Dec 31	2017 Sep 23	6.7	70062(2), 80109(1), 90007(12), 13012(6)
WISE 2209–2734	2010 Dec 10	2017 Sep 23	6.8	70062(2), 80109(2), 90007(11), 13012(6)
WISE 2211–4758	2011 Nov 30	2017 Sep 19	5.8	80109(1), 13012(6)
WISE 2212–6931	2011 Jun 15	2017 Sep 22	6.3	70062(1), 80109(1), 90007(12), 13012(6)
WISE 2220–3628	2012 Jan 23	2017 Sep 24	5.7	80109(2), 90007(12), 13012(6)
WISE 2232–5730	2010 Nov 15	2017 Sep 24	6.9	70062(2), 13012(6)
WISE 2237+7228	2012 Apr 15	2017 Jun 02	5.1	80109(2), 90007(10), 13012(6)
WISE 2255–3118	2010 Dec 17	2017 Oct 06	6.8	70062(2), 80109(2), 13012(6)
WISE 2301+0216	2012 Jan 13	2017 Oct 16	5.8	80109(2), 90007(12), 13012(6)
WISE 2302–7134	2011 Jun 17	2017 Oct 07	6.3	70062(1), 13012(6)
WISE 2313–8037	2011 Jun 17	2017 Sep 22	6.3	70062(1), 80109(2), 90007(10), 13012(6)
WISE 2319–1844	2010 Dec 31	2017 Oct 12	6.8	70062(2), 80109(1), 90007(12), 13012(6)
ULAS 2321+1354	2009 Aug 19	2017 Oct 13	8.2	60093(1), 70021(1), 80109(2), 90007(12), 13012(7)
ULAS 2326+0201	2012 Jan 31	2017 Oct 09	5.7	80077(1), 13012(6)
WISE 2332–4325	2010 Dec 18	2017 Oct 12	6.8	70062(2), 80109(1), 90007(12), 13012(6)
WISE 2343–7418	2011 Jun 17	2017 Oct 07	6.3	70062(1), 80109(2), 90007(10), 13012(6)
WISE 2344+1034	2011 Jan 18	2017 Oct 04	6.7	70062(1), 80109(2), 13012(6)
WISE 2354+0240	2012 Sep 03	2017 Oct 04	5.1	80109(1), 13012(6)
WISE 2357+1227	2012 Sep 03	2017 Oct 07	5.1	80109(1), 13012(6)

<sup>a</sup> 1639–6847: In the observation from program 80109 and the first observation from program 90007, the object is blended with a background source. This reduces the usable time baseline for astrometric measurements from 5.2 to 4.2 yr because the first clean image was taken 2013 May 19 (UT).

For a few targets, the disentangling of proper motion from parallax benefited from using ch2 observations taken prior to our own:

1. WISE 0304–2705 and WISE 2203+4619: We supplemented our data with an earlier observation from program 10135 (D.J. Pinfield, PI) that used a sixteen-point spiral dither pattern with medium spacing, two frames at each dither position, and exposure times of 30 s per frame.
2. WISE 0833+0052 and ULAS 2326+0201: We used an earlier observation from program 80077 (S.K. Leggett, PI) that used a twelve-point Reuleaux dither pattern with medium spacing, four frames at each dither position, and exposure times of 30 s per frame.
3. WISE 0855–0714: We used earlier observations from programs 90095 and 10168 (K.L. Luhman, PI). Program 90095 acquired three separate epochs on the target object, using a 5-point Gaussian dither with small spacing and exposure times of 30 s per frame. Program 10168 acquired four separate epochs using a 9-point

random dither pattern of small spacing and exposure times of 30 s per frame.

4. CFBDS 1028+5654: An earlier observation from program 70021 (K.L. Luhman, PI) was used to extend our time baseline. This program acquired data using a 5-point Gaussian dither with small spacing, one frame per dither position, and exposure times of 30 s per frame.
5. ULAS 1043+1048: An observation from program 70058 (S.K. Leggett, PI) was used to extend the time baseline for this object. This program took data using a sixteen-point spiral dither pattern with medium spacing, six frames at each dither position, and exposure times of 30 s per frame.
6. WISE 1828+2650: Data from program 551 (A.K. Mainzer, PI) were the first taken as part of the WISE brown dwarf team’s follow-up of WISE color-selected objects. This program, which targeted only WISE 1828+2650 at a single epoch, used a twelve-point Reuleaux dither pattern with medium spacing, one

frame per dither position, and exposure times of 12 s per frame.

7. ULAS 2321+1354: Program 60093 (S.K. Leggett, PI) provided a supplemental data point for this object. Data were taken using a five-point Gaussian dither pattern with medium spacing, one frame per dither, and exposure times of 30 s per frame.

## 5. SPITZER REDUCTIONS

### 5.1. *Photometry in ch1 and ch2*

With the exception of Gl 27B (Luhman et al. 2007) and WD0806-661B (Luhman et al. 2012), the *Spitzer* photometry for all sources was measured by CRG and JDK as follows. For each object, we performed aperture photometry on an AOR that included both ch1 and ch2 data so that measurements were contemporaneous. These aperture measurements we done either on custom mosaics of the corrected basic calibrated data (CBCD) frames or on the post-basic calibrated data (pBCD) mosaics archived at the *Spitzer* Heritage Archive at IRSA<sup>3</sup> using the MOsaicker and Point Source EXtractor with point source extraction package (MOPEX/APEX), also available at IRSA. As mentioned in Kirkpatrick et al. (2011), for objects as bright as our targets, we have seen negligible difference in the photometry between the two methods. Our scripts used a 4-pixel aperture (aperture1) with a 24-to-40-pixel sky annulus. Resultant raw fluxes were then multiplied by the aperture corrections recommended in Table 4.7 of the IRAC Instrument Handbook, also available at IRSA – 1.208 for ch1 and 1.221 for ch2 – to obtain the flux in units of  $\mu\text{Jy}$ , and then converted to magnitudes using the flux zero points in the Handbook’s Table 4.1 ( $280.9 \pm 4.1$  Jy in ch1 and  $179.7 \pm 2.6$  in ch2), propagating the uncertainty in zero point and flux into the final measurement error. This resulting photometry, along with the AOR number from which the photometry was extracted, is given in columns 7-9 of Table 2.

### 5.2. *Astrometry in ch2*

Our basic astrometric reduction methodology is discussed in detail in Martin et al. (2018). Whereas ECM wrote python code for the reductions presented in that paper, JDK wrote independent IDL code and other wrappers for the reductions presented here, and those included one fundamental change to improve astrometric repeatability. We outline the basic steps below.

#### 5.2.1. *Identifying Gaia Astrometric Anchor Points*

For each AOR, we created a mosaic from the individual CBCD frames and extracted astrometry and photometry of detected sources using the MOPEX/APEX software. We examined the resulting mosaics at all epochs to ensure that the target object was near the center of the field, as expected.

(This step eliminated three AORs for WISE 2301+0216 – 46523392, 46523136, and 46522880 – from further use, due to a typographical error in the requested pointings for those epochs.) In addition to these per-epoch mosaics, we also created a supermosaic and associated source list by combining all available CBCD files for each object over the full time baseline. We then used the *tmatch2* routine in the Starlink Tables Infrastructure Library Tool Set (STILTS; Taylor 2006) and a 3-arcsec radius to match sources from each per-epoch mosaic source list to the supermosaic source list. Parameters were set so that we retained for each supermosaic source only the closest match in the per-epoch source list (*find = best1*) and listed only those supermosaic sources having a match (*join = 1and2*).

We then used the Interactive Data Language (IDL) to perform a preliminary re-registration on each per-epoch mosaic to place it on the same astrometric grid as the supermosaic. Only those objects with  $S/N \gtrsim 30$  on the per-epoch mosaics were used. After experimenting with full affine transformations for the re-registration, we found that a simple translation in RA and Dec provided the most robust results. The offsets were computed by performing a robust mean of the offsets and including a  $3\sigma$  clipping of outliers. We uploaded this list of high-S/N re-registration stars into IRSA and matched to the *Gaia* Data Release 1 (DR1) catalog using a 1 arcsec search radius. Most of these stars have *Gaia* matches, since they are bright at both *Gaia* G band and IRAC ch2 band, but we dropped any *Gaia* matches for which the *Gaia* DR1 astrometric uncertainties were  $\gtrsim 100$  milliarcsec.

Once the *Gaia* astrometric anchor stars had been identified in each field, more precise refinements to the astrometry can be performed, since the *Gaia* DR1 positions for these well detected objects typically have uncertainties of under a milliarcsec. Originally, we wrote code like that described in Martin et al. (2018), to do these refinements on the source lists derived from the per-epoch mosaics, but we found that this was degrading our final astrometric precision. After some experimentation, we concluded that the mosaicking step in MOPEX was responsible. Thus, the actual astrometric measurements for this paper use source positions as measured on the individual *frames*, not the per-epoch mosaics, as described below.

#### 5.2.2. *Astrometric Refinements to Frame Source Positions*

For each AOR, we ran scripts in MOPEX/APEX to measure the positions and photometry of our target and its association re-registration stars on each individual frame. These scripts used the CBCD, uncertainty (CBUNC), and mask (BIMSK) files available in the *Spitzer* Heritage Archive. Data were pulled from the *Spitzer* Heritage Archive after all image headers has been updated by the *Spitzer* Science Center to incorporate the new fifth-order correction to the array distortion<sup>4</sup> (Lowrance et al. 2014, 2016). Point response function (PRF) fitting was done using a set of PRFs measured by one

<sup>3</sup> See <http://irsa.ipac.caltech.edu>.

<sup>4</sup> See also [https://irachpp.spitzer.caltech.edu/page/dist\\_correct](https://irachpp.spitzer.caltech.edu/page/dist_correct)



of us (JGI) that are appropriate for use on *Spitzer* warm mission data and that sample the ch2 array on a  $5 \times 5$  grid. These PRFs are tabulated images of point sources at various sub-pixel offsets (Ingalls et al. 2012, 2014) and therefore strongly mitigate the astrometric bias caused by intrapixel distortion, which is a consequence of the fact that IRAC data are undersampled and the response function itself is not uniform across a pixel. Similar warm mission PRFs have been developed by Hora et al. (2012), but the resulting astrometric differences between the Hora PRFs and the ones used here are negligible.

The resulting, native astrometry of the re-registration stars on each frame was then compared to the *Gaia* DR1 positions of these same sources. Specifically, we used the  $(x, y)$  positions computed by APEX and translated these into (RA, Dec) using the World Coordinate System (WCS) information in the frame FITS header<sup>5</sup>. Naïvely, one would assume that the  $(x, y)$  positions reported by APEX would be true array coordinates, but through experimentation we determined that these positions are actually rubber-sheeted versions; i.e., ones with the fifth-order distortion correction already included. Hence, we were able to convert to (RA, Dec) using the WCS specifications only.

With the  $(x, y)$ -derived sky positions in hand for both the re-registration stars and the target, we converted all to tangent plane coordinates  $(\xi, \eta)$ , where we used the mean position of our target across all epochs as the tangent point itself; i.e.,  $(\xi, \eta) = (0, 0)$ . When then computed the  $(\Delta\xi, \Delta\eta)$  values between the  $(x, y)$ -derived sky positions for the re-registration stars and their *Gaia* reported positions, and computed a robust mean of the differences using  $3\sigma$  outlier clipping and a simple  $(\xi, \eta)$  translation. These mean differences were then used to place the  $(\xi, \eta)$  coordinates of the target object and re-registration stars onto the *Gaia* reference frame.

For most of our targets, we were able to find a sufficient number of *Gaia* DR1 stars above a single-frame S/N value of 100 to perform an adequate re-registration. For some targets in sparser fields, however, as few as three re-registration stars were found above S/N = 100. (For the two targets closest to the Galactic Center, WISE 1928+2356 and WISE 2000+3629, we had the opposite problem of too many potential re-registration stars, so we reset the selection threshold for re-registration stars to S/N > 500.) For any target having ten or more re-registration stars with S/N  $\geq$  100, we found that the inclusion of re-registration stars with  $30 < \text{S/N} < 100$  did not generally decrease the reduced  $\chi^2$  values in the final proper motion and parallax fits. For targets having fewer than ten re-registration stars with S/N  $\geq$  100, however, these reduced  $\chi^2$  values were generally much better. For these targets, a single-frame S/N floor of  $\sim 30$  was used for selection of the re-registration stars. With this adjustment, no fewer than 5 re-registration stars were used for each field.

<sup>5</sup> Note that FITS and APEX use the convention that the first pixel is located at (1,1), whereas IDL convention places this at (0,0).

For the target object, the robust mean of these per-frame adjusted positions (again using  $3\sigma$  clipping) was used as the measured position of the object for this AOR. For the astrometric uncertainty on each AOR position, we use a measurement of the positional repeatability for stars lying at a S/N value similar to the target. Figure 1 illustrates this repeatability. The plot demonstrates that our target T and Y dwarfs, which lie in the single-frame S/N range between 70 and 200, have per-axis astrometric precisions of  $\sim 15$  mas. There are some AORs for which, due to small number statistics, this measured repeatability falls below 10 mas. For these, we set a floor of 10 mas on the per-axis positional uncertainty of the target, since the broader analysis in Figure 1 shows this is the best we actually achieve. For each AOR, the mean  $(\xi, \eta)$  position of the target was then converted back to (RA, Dec). The FITS header of the middle frame in each AOR was then consulted for the UT date and barycentric (X,Y,Z) position of the *Spitzer* Space Telescope at the time of observation.

### 5.2.3. Fitting for Proper Motion and Parallax

For each target, our list of measured astrometry and its uncertainties along with the observation times and locations of the observing platform were fed into a least square fitting code to determine the proper motion, parallax, and position at a fiducial time. We supply two non-linear equations (see Smart 1977, Green 1985, Beichman et al. 2014) to the code:

$$\alpha_{\text{residual}} = \left( \alpha(t) - \alpha' \right) \cos \delta' - \pi_{\text{trig}} \left( X(t) \sin \alpha' - Y(t) \cos \alpha' \right) / 3600 \quad (1)$$

$$\delta_{\text{residual}} = \delta(t) - \delta' - \left( \pi_{\text{trig}} \left( X(t) \cos \alpha' \sin \delta' + Y(t) \sin \alpha' \sin \delta' - Z(t) \cos \delta' \right) \right) / 3600 \quad (2)$$

where

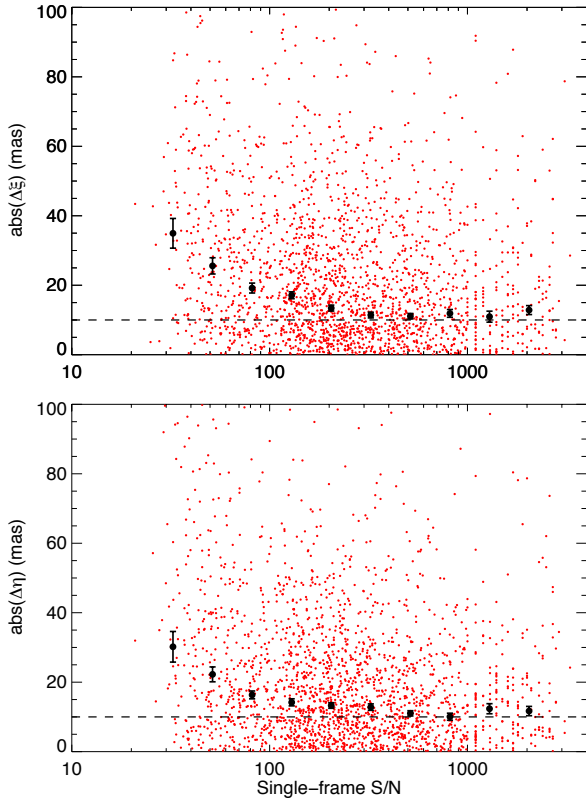
$$\alpha' = \alpha_0 + (\mu_\alpha(t - t_0) / \cos \delta') / 3600 \quad (3)$$

$$\delta' = \delta_0 + (\mu_\delta(t - t_0)) / 3600 \quad (4)$$

Here,  $\alpha(t)$  and  $\delta(t)$  are the RA and Dec positions (and their uncertainties) of the target in degrees;  $X(t)$ ,  $Y(t)$ , and  $Z(t)$  are the locations of the spacecraft in astronomical units;  $t_0$  is a fiducial time in years;  $\alpha_0$  and  $\delta_0$  are the RA and Dec in degrees at time  $t_0$ ;  $\mu_\alpha$  and  $\mu_\delta$  are the RA and Dec components of the proper motion in arcsec yr<sup>-1</sup>; and  $\pi_{\text{trig}}$  is the trigonometric parallax in arcsec. We employed the IDL module `mpfitfun` (Markwardt 2009), which uses the Levenberg-Marquardt least-squares algorithm to attempt to drive both  $\alpha_{\text{residual}}$  and  $\delta_{\text{residual}}$  simultaneously to zero, given the observational data and their uncertainties.

The fiducial time was chosen to be at a point in the middle of our observational data set, epoch 2014.0, since setting this to be within the timeframe of the observations minimizes





**Figure 1.** Astrometric repeatability as a function of the single-frame signal-to-noise ratio. Plotted in red are the per-axis differences in position ( $\xi$  in the top panel and  $\eta$  in the bottom) between our measurements and those of *Gaia* DR2. These are the mean position in the AOR determined from the (generally) nine independent measurements in each individual frame. Shown in the figure are sources from one representative AOR from each of our 142 targets, excepting nineteen with  $|\beta| < 15^\circ$  that have been removed since their higher source densities would otherwise dominate the plot. The black points are robust means – determined with a  $1\sigma$  clipping to remove outliers – that sample ten S/N bins over the range  $25 < S/N < 2500$ . As shown by the dashed black lines, an asymptotic floor of  $\sim 10$  mas is reached at very high S/N values.

the associated uncertainties. Choosing a much later or earlier time, say 2000.0, would result in larger positional uncertainties since the uncertainty from the proper motion compounds with the difference in the time interval between the observations and the chosen fiducial time.

Table 4 gives the best fitting solutions for each of our 142 targets. The abbreviated object name is in column 1 followed by the position of the object at epoch 2014.0 along with the positional uncertainties in column 2-5. The value of parallax obtained by the best-fit solution above is a measurement relative to the background stars and requires an adjustment to the absolute reference frame as described further below. The resulting value of the absolute parallax and the correction needed to convert from relative to absolute units are given

in columns 6 and 7. The best-fit proper motion per axis and its uncertainties are listed in columns 8 and 9. The  $\chi^2$  value of the best fit, the number of degrees of freedom, and the reduced  $\chi^2$  value are listed in columns 10-12. The number of Spitzer epochs used in the solution is shown in column 13. Finally, the number of re-registration stars used along with a flag value for the S/N floor used for registration star selection ("H" for the high S/N cut and "L" for the low S/N cut) is given in column 14.

**Table 4.** Parallax and Motion Fits for Objects on the Spitzer Parallax Program

Object	J2000 RA	RA	J2000 Dec	Dec	$\pi_{abs}$	$corr_{\pi}$	$\mu_{RA}$	$\mu_{Dec}$	$\chi^2$	Dof	Red.	# of	# of
Name	Ep. 2014.0	Unc.	Ep. 2014.0	Unc.	(mas)	(mas)	(mas yr <sup>-1</sup> )	(mas yr <sup>-1</sup> )			$\chi^2$	Ep.	Reg.
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
	(deg)	(mas)	(deg)	(mas)									Stars
WISE 0005+3737	1.324120	2.6	37.622066	2.5	127.0±2.4	1.3±0.4	998.9±1.4	-267.0±1.4	19.925	33	0.604	19	22H
WISE 0015-4615	3.775288	2.7	-46.255526	2.6	71.8±2.7	1.5±0.5	409.7±1.5	-682.9±1.3	30.137	33	0.913	19	15L
WISE 0032-4946	8.128906	3.3	-49.781951	3.0	63.6±2.9	1.4±0.3	-379.3±1.7	-858.1±1.7	28.256	33	0.856	19	13L
2MASS 0034+0523	8.717410	3.3	5.385402	3.7	120.1±3.0	1.6±0.4	672.6±1.7	184.7±1.9	17.909	35	0.512	20	16L
WISE 0038+2758	9.621136	2.5	27.981175	2.5	89.7±2.5	1.5±0.6	-15.4±1.6	96.3±1.5	37.107	39	0.951	22	12H
WISE 0049+2151	12.439742	2.5	21.855396	2.5	139.9±2.5	1.5±0.5	-483.2±1.4	-46.5±1.4	18.928	35	0.541	20	15L
WISE 0123+4142	20.889465	8.1	41.701367	5.6	44.0±4.1	1.3±0.3	601.7±2.6	91.5±1.9	5.439	9	0.604	7	10H
CFBDS 0133+0231	23.260890	3.7	2.524552	2.7	56.3±3.4	2.2±1.2	598.0±2.0	-113.9±1.5	44.910	33	1.361	19	8L
WISE 0146+4234AB	26.735580	2.4	42.569411	2.3	52.5±2.3	1.3±0.3	-452.0±1.2	-27.9±1.2	58.434	37	1.579	21	21H
WISE 0221+3842	35.275000	5.9	38.701001	5.6	36.0±4.1	1.5±0.5	139.6±1.9	-21.7±1.8	10.011	9	1.112	7	13H
WISE 0226-0211AB	36.599702	6.0	-2.195477	5.1	57.3±4.7	0.6±0.1	-294.9±2.1	-436.9±1.7	307.384	13	23.645	9	11L
WISE 0233+3030	38.325104	6.7	30.508434	6.2	31.3±4.2	1.6±0.4	-134.6±2.3	-29.5±2.2	11.591	11	1.054	8	16H
WISE 0241-3653	40.353413	2.4	-36.891001	2.6	52.4±2.7	1.6±0.2	242.0±1.5	148.4±1.4	26.606	37	0.719	21	8H
WISE 0247+3725	41.810711	2.4	37.422967	2.4	64.8±2.6	1.5±0.6	25.3±1.3	-83.2±1.3	23.715	33	0.719	19	21H
WISE 0302-5817	45.656121	14.5	-58.294668	15.9	56.1±4.4	1.3±0.3	41.2±4.9	-76.4±5.2	21.135	13	1.626	9	15L
WISE 0304-2705	46.204500	19.4	-27.085116	17.1	81.5±7.7	1.6±0.3	128.0±7.0	497.2±6.5	25.307	9	2.812	7	5L
WISE 0309-5016	47.332887	4.9	-50.270419	4.3	66.8±3.9	1.8±0.8	521.5±1.7	203.6±1.5	6.397	13	0.492	9	16L
WISE 0313+7807	48.358936	3.5	78.129054	3.6	134.3±3.6	1.0±0.3	71.1±1.2	54.8±1.2	19.065	15	1.271	10	46L
WISE 0316+4307	49.102234	3.0	43.118785	2.8	73.3±2.8	1.0±0.3	372.4±1.5	-225.9±1.5	28.850	27	1.069	16	33H
WISE 0323-5907	50.788921	4.9	-59.130369	5.9	71.5±4.3	1.5±0.6	519.1±1.6	499.6±2.0	16.304	11	1.482	8	18L
WISE 0323-6025	50.907543	2.7	-60.431966	2.8	71.4±2.9	1.5±1.0	506.7±1.3	-173.5±1.5	25.616	31	0.826	18	19L
WISE 0325-3854	51.324053	5.3	-38.915158	6.2	57.2±5.4	1.6±0.5	283.7±1.9	-107.0±1.8	3.098	11	0.282	8	13L
WISE 0325-5044	51.268421	2.9	-50.733514	3.1	36.7±2.7	1.5±0.4	84.6±1.5	-154.3±1.6	121.079	27	4.484	16	21L
WISE 0325+0831	51.449038	3.1	8.521650	3.4	78.5±3.0	1.4±0.3	116.2±1.8	-38.1±1.7	21.917	33	0.664	19	12L
WISE 0335+4310	53.813849	2.4	43.178366	2.3	72.1±2.4	1.0±0.2	825.7±1.2	-787.0±1.2	112.945	35	3.227	20	52H
WISE 0336-0143	54.020859	2.4	-1.732166	2.4	99.0±2.4	1.7±0.4	-257.8±1.2	-1212.3±1.2	55.719	35	1.592	20	20H
WISE 0350-5658	57.501000	2.7	-56.975637	2.7	174.6±2.6	1.4±0.4	-216.5±1.3	-579.0±1.4	28.501	35	0.814	20	20L
WISE 0359-5401	59.891824	2.5	-54.032512	2.6	75.8±2.5	1.5±0.4	-143.0±1.3	-774.8±1.5	92.938	37	2.512	21	16L
WISE 0404-6420	61.181138	3.0	-64.341730	2.9	45.7±2.7	1.8±0.6	-46.8±1.6	-50.2±1.6	38.537	27	1.427	16	11H
WISE 0410+1502	62.595853	2.3	15.044417	2.2	150.2±2.4	1.5±0.5	954.2±1.1	-2213.3±1.1	39.350	39	1.009	22	20H
WISE 0413-4750	63.492451	7.1	-47.843983	7.8	48.2±4.8	1.5±0.6	110.6±2.3	302.2±2.6	9.477	9	1.053	7	18L
WISE 0430+4633	67.721883	6.9	46.559111	6.7	93.9±4.1	0.4±0.1	879.7±2.3	383.8±2.2	2.835	9	0.315	7	63H
WISE 0458+6434AB	74.725158	3.7	64.581566	3.8	109.2±3.6	1.2±0.2	207.7±1.2	291.2±1.2	2.470	13	0.190	9	16H
WISE 0500-1223	75.012144	3.9	-12.394828	3.7	95.1±3.6	1.3±0.6	-536.5±1.3	493.1±1.2	6.578	13	0.506	9	26L
WISE 0512-3004	78.036948	2.4	-30.067509	2.5	48.9±2.6	1.2±0.4	614.2±1.2	187.6±1.3	72.645	37	1.963	21	23L
WISE 0535-7500	83.819481	2.4	-75.006736	2.4	66.4±2.4	1.4±0.5	-123.7±1.1	19.6±1.1	45.380	33	1.375	19	32H
WISE 0540+4832	85.196268	2.5	48.541582	2.5	70.0±2.6	0.8±0.1	246.0±1.5	-626.9±1.5	41.240	29	1.422	17	58H
WISE 0614+0951	93.657701	2.2	9.859608	2.2	65.6±2.2	0.6±0.1	387.0±1.1	-149.8±1.1	39.525	39	1.013	22	74H
WISE 0645-0302	101.368293	4.5	-3.047051	6.5	50.7±4.2	0.4±0.1	-0.8±1.2	-318.9±2.0	10.993	9	1.221	7	55H
WISE 0647-6232	101.846795	2.3	-62.542827	2.4	100.3±2.4	1.3±0.6	2.2±1.0	387.9±1.1	76.198	33	2.309	19	20H
WISE 0713-2917	108.344415	2.5	-29.298188	2.5	107.5±2.4	1.0±0.2	356.5±1.3	-413.8±1.3	28.123	33	0.852	19	87H

Table 4 continued

Table 4 (continued)

Object	J2000 RA	RA	J2000 Dec	Dec	$\pi_{abs}$	$corr_{\pi}$	$\mu_{RA}$	$\mu_{Dec}$	$\chi^2$	Dof	Red.	# of	# of
Name	Ep. 2014.0	Unc.	Ep. 2014.0	Unc.	(mas)	(mas)	(mas yr <sup>-1</sup> )	(mas yr <sup>-1</sup> )			$\chi^2$	Ep.	Reg.
	(deg)	(mas)	(deg)	(mas)									Stars
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
WISE 0713-5854	108.257861	6.7	-58.912164	7.5	78.2±4.6	1.6±0.6	82.2±2.1	358.2±2.3	12.659	7	1.808	6	20H
WISE 0723+3403	110.802009	3.8	34.053368	3.7	56.3±3.5	0.5±0.1	-5.0±1.2	-343.8±1.2	28.654	13	2.204	9	40L
WISE 0734-7157	113.681527	2.5	-71.962324	2.5	75.0±2.4	1.2±0.4	-565.5±1.3	-78.9±1.3	88.425	29	3.049	17	21H
WISE 0744+5628	116.238838	2.3	56.471738	2.4	67.1±2.5	1.8±0.6	153.6±1.2	-764.4±1.2	44.682	37	1.208	21	10H
WISE 0759-4904	119.945205	2.4	-49.081446	2.4	89.1±2.4	0.7±0.1	-367.0±1.1	244.3±1.1	21.246	33	0.644	19	55H
WISE 0812+4021	123.084041	2.6	40.351692	2.3	34.2±2.7	1.5±0.7	258.0±1.3	28.8±1.1	74.070	37	2.002	21	20L
WISE 0825+2805	126.280555	2.5	28.096544	2.4	155.8±2.4	1.4±0.2	-63.1±1.3	-232.8±1.2	34.192	35	0.977	20	14H
WISE 0833+0052	128.408480	8.8	0.869044	7.8	82.6±4.5	1.4±0.5	790.1±2.8	-1590.7±2.5	4.356	9	0.484	7	21H
WISE 0836-1859	129.171466	4.0	-18.996471	3.8	40.8±3.6	1.0±0.2	-47.6±1.3	-150.5±1.2	67.391	13	5.184	9	19H
WISE 0855-0714	133.787057	4.5	-7.244431	4.5	438.9±3.0	1.3±0.3	-8118.9±1.9	679.3±1.9	11.154	21	0.531	13	24H
WISE 0857+5604	134.316277	2.3	56.068512	2.5	87.2±2.4	1.3±0.2	-714.8±1.1	-233.5±1.2	43.297	37	1.170	21	12L
WISE 0906+4735	136.704848	3.5	47.593343	3.6	48.4±3.4	1.5±0.2	-545.9±1.2	-709.6±1.2	19.197	15	1.280	10	15L
WISE 0914-3459	138.537222	7.4	-34.994793	7.0	45.2±4.2	1.1±0.2	-19.7±2.2	175.9±2.2	12.900	9	1.433	7	30H
WISE 0940-2208	145.083635	7.3	-22.138988	7.7	38.1±4.7	1.3±0.3	-144.9±2.3	171.2±2.3	5.652	9	0.628	7	14H
WISE 0943+3607	145.775825	2.6	36.122729	2.7	93.8±2.8	1.8±0.9	675.1±1.3	-498.9±1.4	68.309	37	1.846	21	9L
WISE 0952+1955	148.247005	5.1	19.918980	3.7	41.1±3.9	1.4±0.2	-34.4±1.6	-32.1±1.2	18.487	15	1.232	10	13L
WISE 1018-2445	154.533566	4.0	-24.766900	4.0	83.6±3.6	1.0±0.3	54.3±1.3	-821.4±1.3	9.697	13	0.746	9	23L
WISE 1025+0307	156.489211	2.7	3.132060	2.7	85.4±2.5	1.7±0.5	-1199.3±1.4	-144.4±1.3	27.257	31	0.879	18	10H
CFBDS 1028+5654	157.171475	3.2	56.900364	2.8	45.0±2.9	1.4±0.2	200.8±1.5	-12.1±1.4	33.048	33	1.001	19	19L
WISE 1039-1600	159.782034	2.9	-16.000912	2.5	53.4±2.6	1.4±0.4	-189.1±1.5	-119.7±1.2	27.613	35	0.789	20	13H
ULAS 1043+1048	160.980791	9.7	10.800797	6.9	20.8±7.0	1.6±0.3	95.4±3.0	-105.1±2.1	11.428	9	1.270	7	11L
WISE 1050+5056	162.698915	8.0	50.934880	7.4	49.7±5.0	1.8±0.7	-427.5±2.5	-64.0±2.2	26.459	9	2.940	7	15L
WISE 1051-2138	162.875232	3.3	-21.650044	2.8	67.0±3.0	1.1±0.3	137.1±1.5	-156.4±1.3	27.284	31	0.880	18	19L
WISE 1052-1942	163.241771	7.0	-19.714310	5.9	62.3±4.4	1.3±0.4	326.2±2.1	-315.1±1.7	7.594	9	0.844	7	28L
WISE 1055-1652	163.972545	3.0	-16.870933	3.0	72.2±2.7	1.5±0.8	-991.3±1.4	414.9±1.4	28.055	27	1.039	16	13H
WISE 1124-0421	171.158218	3.4	-4.363736	3.2	61.6±3.1	1.5±0.2	-552.4±1.8	67.6±1.4	16.601	31	0.536	18	7H
WISE 1139-3324	174.955011	7.5	-33.407093	7.2	27.0±3.9	1.1±0.3	-97.5±2.3	-51.3±2.2	20.466	11	1.861	8	37L
WISE 1141-3326	175.485224	7.6	-33.443233	8.1	99.7±4.2	1.8±0.8	-904.4±2.3	-76.5±2.5	11.648	11	1.059	8	15H
WISE 1143+4431	175.917700	17.6	44.523342	16.6	38.1±6.5	1.9±0.8	76.9±5.1	-71.0±5.0	7.188	9	0.799	7	10L
WISE 1150+6302	177.558621	3.1	63.044318	2.6	124.5±3.0	1.7±0.5	410.4±1.8	-539.7±1.2	34.761	37	0.939	21	8L
ULAS 1152+1134	178.165841	12.5	11.568698	6.8	49.7±5.1	2.1±0.2	-492.4±3.6	-24.0±2.1	17.856	7	2.551	6	5H
WISE 1206+8401	181.512532	2.8	84.019282	2.4	81.9±2.5	1.3±0.3	-575.0±1.3	-255.7±1.1	44.711	35	1.277	20	19L
WISE 1217+1626AB	184.487872	5.0	16.443394	4.7	104.4±4.7	1.7±0.3	758.1±1.7	-1252.2±1.5	75.092	13	5.776	9	8L
WISE 1220+5407	185.151875	16.9	54.121108	24.9	42.7±7.1	1.6±0.3	192.2±5.6	-310.7±7.8	17.816	9	1.980	7	13L
WISE 1221-3136	185.468474	3.6	-31.599861	2.9	73.8±3.3	1.9±0.6	611.0±1.9	396.7±2.3	17.685	31	0.570	18	6H
WISE 1225-1013	186.495136	2.9	-10.229558	2.9	43.3±3.0	2.1±1.0	-156.6±1.8	-325.5±1.5	47.409	31	1.529	18	10H
2MASS 1231+0847	187.943521	10.3	8.788496	11.7	75.8±4.8	1.7±0.5	-1173.4±3.1	-1034.1±3.5	3.567	11	0.324	8	9L
WISE 1243+8445	190.783116	9.1	84.762718	8.8	48.6±4.5	1.8±0.4	-530.2±2.8	-524.1±2.7	11.855	9	1.317	7	11H
WISE 1254-0728	193.702040	12.0	-7.474752	7.8	47.2±4.4	1.7±1.0	9.0±3.6	-131.3±2.4	13.651	13	1.050	9	15L
WISE 1257+4008	194.316587	19.7	40.148440	15.3	45.7±8.2	1.8±0.8	320.0±5.7	176.5±4.5	7.465	9	0.829	7	10L
VHS 1258-4412	194.520589	6.7	-44.209184	6.7	63.8±4.0	1.3±0.3	143.6±2.3	-150.7±2.2	12.625	9	1.403	7	22H
WISE 1301-0302	195.423510	9.0	-3.037151	7.3	53.8±5.6	1.5±0.4	241.5±2.9	-295.5±2.2	16.300	13	1.254	9	18L
WISE 1318-1758	199.641069	2.6	-17.974000	2.5	57.8±2.7	1.5±0.4	-515.2±1.6	6.8±1.4	61.843	35	1.767	20	11H
WISE 1333-1607	203.249743	8.0	-16.131943	6.0	48.0±4.7	1.4±1.0	-315.3±2.5	-125.7±1.9	11.932	7	1.705	6	14L

Table 4 continued

Table 4 (continued)

Object	J2000 RA	RA	J2000 Dec	Dec	$\pi_{abs}$	$corr_{\pi}$	$\mu_{RA}$	$\mu_{Dec}$	$\chi^2$	Dof	Red.	# of	# of
Name	Ep. 2014.0	Unc.	Ep. 2014.0	Unc.	(mas)	(mas)	(mas yr <sup>-1</sup> )	(mas yr <sup>-1</sup> )			$\chi^2$	Ep.	Reg.
	(deg)	(mas)	(deg)	(mas)									Stars
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
WISE 1405+5534	211.322470	3.2	55.572792	2.7	157.9±3.1	2.0±1.1	-2326.5±1.7	236.1±1.3	19.758	33	0.599	19	10H
VHS 1433-0837	218.297357	7.0	-8.626956	4.8	50.9±4.5	1.7±0.6	-284.4±2.4	-204.6±1.8	13.113	13	1.009	9	10H
WISE 1436-1814	219.009079	2.4	-18.239528	2.4	48.3±2.4	1.2±0.3	-67.3±1.3	-86.3±1.3	40.342	37	1.090	21	14H
WISE 1448-2534	222.027086	2.6	-25.573128	2.6	52.5±2.5	1.1±0.3	142.5±1.4	-741.6±1.4	45.332	33	1.374	19	27H
WISE 1501-4004	225.317046	6.8	-40.072132	6.6	69.5±4.0	1.0±0.1	370.2±2.3	-337.3±2.2	22.436	9	2.493	7	39H
WISE 1517+0529	229.337884	6.8	5.491625	6.5	42.1±4.2	1.1±0.2	-55.5±2.3	194.9±2.2	11.812	9	1.312	7	23L
WISE 1519+7009	229.778548	3.0	70.158202	2.7	77.6±2.8	1.5±0.5	325.0±1.5	-501.4±1.2	28.582	33	0.866	19	10H
WISE 1523+3125	230.771352	4.9	31.426572	4.8	61.4±3.8	1.6±0.7	103.9±1.7	-509.2±1.7	10.595	13	0.815	9	15L
WISE 1541-2250	235.464060	2.4	-22.840555	2.3	167.1±2.3	1.1±0.4	-901.2±1.2	-82.4±1.2	42.714	37	1.154	21	31H
WISE 1542+2230	235.557193	6.5	22.501044	5.3	85.6±4.2	1.2±0.3	-974.3±2.2	-391.9±1.8	28.358	13	2.181	9	11L
WISE 1612-3420	243.066007	3.7	-34.341849	3.6	78.3±3.5	0.7±0.1	-289.4±1.2	-586.6±1.2	12.487	13	0.961	9	62H
WISE 1614+1739	243.673390	3.6	17.659388	3.5	97.6±3.4	1.7±0.5	554.5±1.2	-476.7±1.2	5.324	15	0.355	10	10H
2MASS 1615+1340	243.768480	2.5	13.667415	2.4	58.4±2.5	1.3±0.5	291.1±1.4	-325.5±1.3	30.952	35	0.884	20	18H
WISE 1622-0959	245.537284	3.9	-9.992961	3.4	40.2±3.5	1.0±0.2	44.2±1.4	-7.3±1.2	26.773	15	1.785	10	15H
WISE 1639-6847	249.921745	3.0	-68.797280	3.0	211.9±2.7	1.0±0.2	582.0±1.5	-3099.8±1.5	17.158	31	0.553	18	71H
WISE 1653+4444	253.295797	4.1	44.739248	3.9	78.0±4.2	1.4±0.5	-70.7±2.9	-387.3±2.2	12.774	31	0.412	18	13L
WISE 1711+3500AB	257.768950	2.2	35.010157	2.5	40.3±2.4	1.4±0.5	-156.3±1.1	-71.2±1.2	116.848	37	3.158	21	15H
WISE 1717+6128	259.320846	4.5	61.483138	4.0	48.0±3.8	1.6±0.6	81.7±1.4	-30.5±1.3	15.543	13	1.196	9	9H
WISE 1721+1117	260.393469	6.9	11.294412	9.0	42.0±4.0	1.0±0.2	-89.2±2.2	144.5±2.9	5.929	9	0.659	7	22H
WISE 1735-8209	263.963188	6.0	-82.150405	6.2	75.1±4.6	1.3±0.3	-250.2±1.9	-257.8±1.8	16.760	9	1.862	7	11H
WISE 1738+2732	264.648439	2.4	27.549315	2.3	131.0±2.4	1.2±0.4	337.3±1.1	-338.1±1.1	34.296	39	0.879	22	19H
WISE 1804+3117	271.147014	3.4	31.285122	3.5	62.7±3.4	1.5±0.5	-251.7±1.1	7.0±1.1	20.461	15	1.364	10	22H
WISE 1812+2007	273.179657	3.8	20.128953	4.5	47.8±4.0	0.9±0.1	0.7±0.6	-534.4±1.5	17.409	11	1.583	8	34H
WISE 1813+2835	273.372052	2.6	28.591745	2.6	74.9±2.5	1.0±0.2	-204.7±1.3	-462.4±1.3	22.237	33	0.674	19	31H
WISE 1828+2650	277.130718	2.2	26.844010	2.2	100.7±2.3	1.0±0.2	1017.5±1.0	174.5±1.0	32.475	39	0.833	22	38H
WISE 1928+2356	292.171905	2.5	23.934871	2.6	149.9±2.4	0.4±0.1	-241.5±1.3	243.1±1.3	77.458	33	2.347	19	374H
WISE 1955-2540	298.752056	2.5	-25.670762	2.5	36.6±2.4	1.1±0.3	349.8±1.2	-248.3±1.2	49.674	31	1.602	18	43H
WISE 1959-3338	299.773590	2.2	-33.642914	2.2	85.3±2.2	1.1±0.3	-8.6±1.0	-193.2±1.1	29.136	39	0.747	22	28H
WISE 2000+3629	300.209091	2.6	36.497627	2.7	133.1±2.5	1.2±0.3	9.4±1.3	377.9±1.2	16.485	35	0.471	20	343H
WISE 2005+5424	301.333016	3.7	54.408501	3.7	62.9±3.3	1.1±0.2	-1154.4±1.2	-900.4±1.2	16.282	15	1.085	10	41H
WISE 2015+6646	303.942603	2.7	66.779477	2.8	43.1±2.7	1.3±0.5	290.0±1.3	428.3±1.6	35.701	29	1.231	17	17H
WISE 2017-3421	304.453417	6.2	-34.350581	8.3	46.9±4.1	1.2±0.3	192.1±1.9	291.8±2.6	7.140	9	0.793	7	13H
WISE 2019-1148	304.836805	3.9	-11.802130	3.9	77.5±3.5	1.1±0.3	354.2±1.3	-48.3±1.3	11.785	13	0.907	9	16H
WISE 2056+1459	314.121286	2.2	14.998666	2.2	138.3±2.2	1.1±0.4	823.2±1.0	534.1±1.0	40.728	39	1.044	22	52H
WISE 2147-1029	326.778366	4.8	-10.490200	6.8	42.8±4.0	1.3±0.5	89.0±1.5	-135.0±2.0	25.841	11	2.349	8	22L
WISE 2157+2659	329.464040	2.2	26.991920	2.2	59.7±2.2	1.2±0.4	69.6±1.1	-92.2±1.1	32.509	39	0.834	22	31H
WISE 2159-4808	329.956825	2.7	-48.149927	2.5	75.7±2.7	1.2±0.4	316.6±1.4	-1229.8±1.3	36.665	37	0.991	21	22L
WISE 2203+4619	330.769173	12.8	46.322939	13.1	66.0±4.2	0.4±0.1	1284.9±4.4	-270.3±4.3	16.600	11	1.509	8	79H
WISE 2209-2734	332.341272	3.6	-27.578140	5.2	78.2±3.9	2.1±1.2	-781.0±2.4	-430.9±1.9	18.028	37	0.487	21	5L
WISE 2209+2711	332.275276	2.3	27.194171	2.3	161.6±2.4	1.4±0.5	1204.4±1.1	-1357.5±1.1	38.925	37	1.052	21	17H
WISE 2211-4758	332.918711	9.1	-47.974160	8.7	55.8±4.6	1.6±0.3	-117.6±2.8	-50.4±2.6	5.445	9	0.605	7	10H
WISE 2212-6931	333.070499	2.4	-69.522650	2.5	81.9±2.5	1.1±0.4	784.4±1.2	-54.6±1.2	84.780	35	2.422	20	39L
WISE 2220-3628	335.230876	2.4	-36.471641	2.5	97.0±2.4	2.0±0.6	286.8±1.2	-81.4±1.2	47.403	35	1.354	20	14H
WISE 2232-5730	338.019424	6.6	-57.503027	6.5	49.9±4.4	1.3±0.5	405.5±2.0	-102.6±1.9	12.625	11	1.148	8	15L

Table 4 continued

Table 4 (continued)

Object	J2000 RA	RA	J2000 Dec	Dec	$\pi_{abs}$	$corr_{\pi}$	$\mu_{RA}$	$\mu_{Dec}$	$\chi^2$	Dof	Red.	# of	# of
Name	Ep. 2014.0	Unc.	Ep. 2014.0	Unc.	(mas)	(mas)	(mas yr <sup>-1</sup> )	(mas yr <sup>-1</sup> )			$\chi^2$	Ep.	Reg.
	(deg)	(mas)	(deg)	(mas)									Stars
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
WISE 2237+7228	339.334691	2.6	72.476000	2.5	62.3±2.5	1.0±0.2	-80.2±1.3	-97.7±1.3	22.397	31	0.722	18	24H
WISE 2255-3118	343.920079	4.7	-31.311886	6.9	70.7±4.2	1.5±0.4	300.2±1.5	-162.1±2.2	16.157	15	1.077	10	11L
WISE 2301+0216	345.388795	3.4	2.276363	3.1	53.0±2.8	1.4±0.3	-82.6±1.6	-88.9±1.6	41.625	29	1.435	17	14L
WISE 2302-7134	345.619196	7.9	-71.578222	6.2	65.1±4.7	1.3±0.6	-106.3±2.4	30.7±2.0	7.049	9	0.783	7	35L
WISE 2313-8037	348.403564	2.8	-80.617175	2.6	93.5±2.7	1.0±0.2	275.1±1.3	-402.2±1.2	23.801	31	0.768	18	35L
WISE 2319-1844	349.913188	3.1	-18.734474	3.1	79.2±3.1	1.5±0.5	65.5±1.6	138.8±1.6	47.327	37	1.279	21	6L
ULAS 2321+1354	350.349333	2.4	13.914238	2.7	83.6±2.4	1.6±0.5	78.7±1.2	-561.6±1.4	25.489	39	0.654	22	12H
ULAS 2326+0201	351.502016	7.1	2.027545	7.8	49.5±4.6	1.5±0.6	299.8±2.2	80.4±2.4	13.197	9	1.466	7	22L
WISE 2332-4325	353.110751	2.4	-43.419959	2.7	65.3±2.6	2.0±0.6	249.7±1.2	-249.9±1.5	46.217	37	1.249	21	10H
WISE 2343-7418	355.965092	2.8	-74.312845	2.4	58.8±2.7	1.7±0.6	380.9±1.4	192.5±1.2	20.757	33	0.629	19	13H
WISE 2344+1034	356.193582	4.1	10.570956	3.9	64.7±3.7	1.6±0.6	942.1±1.4	-23.9±1.3	41.041	13	3.157	9	18L
WISE 2354+0240	358.512041	8.4	2.670263	8.8	124.1±4.9	1.9±0.9	491.1±2.8	-393.1±3.0	14.458	9	1.606	7	16L
WISE 2357+1227	359.318798	7.6	12.460976	9.9	59.5±4.1	1.5±0.4	24.0±2.6	-500.5±3.2	11.415	9	1.268	7	19L

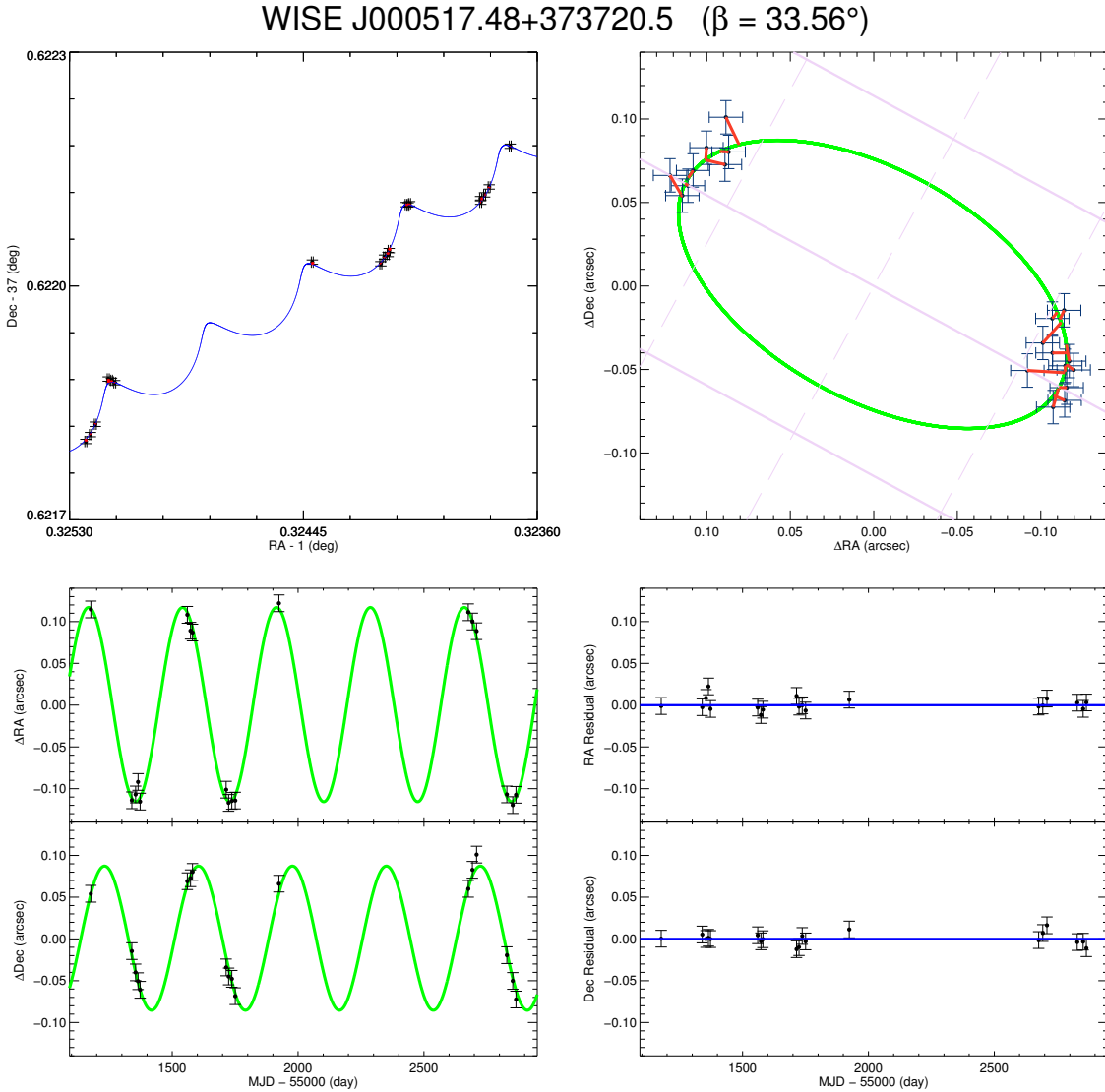
Because we are measuring parallaxes relative to re-registration stars in each field, we need to account for the fact that those re-registration stars themselves each have a small parallax that is partially damping the parallactic signal of our target. In order to correct for this, we need estimates of the mean distance to the re-registration stars. To do this, we tabulated the stars'  $J$ -band magnitudes measured from the 2MASS All-Sky Point Source Catalog, supplemented in some cases by the 2MASS Survey Point Source Reject Table. The distance to each object is then estimated by comparing that magnitude to a model prediction of Galactic structure for that region of sky, as provided by [Mendez & van Altena \(1996\)](#). For fields where 2MASS  $J$  magnitudes were available for all re-registration stars, we found that the correction was very small and varied from 0.4 to 2.2 mas. For some fields, not all of our re-registration stars were detected by 2MASS, so these stars were assigned a floor value for  $J = 16.5$ . To test whether this is a reasonable assumption, we chose WISE 0032-4946 because five of its thirteen re-registration stars have no 2MASS mags. Setting all five of these to have  $J = 17.0$  mag gives a correction of  $1.4 \pm 0.3$  mas. If we instead set all five to an absurdly faint value of  $J = 19.0$  mag, we find a correction of  $1.1 \pm 0.6$  mas. Because these two assumptions give corrections that are essentially identical within the error bars and the former is likely more realistic, we assumed a floor of  $J = 17.0$  mag (but slightly brighter in fields of higher source density) for all 2MASS undetected sources.

Plots of our astrometric measurements and their best fits are shown in Figure 2. **Fig. Set 2. Parallax and proper motion fits to the 142 objects in the Spitzer parallax program**

We note from Table 4 that most of our objects have values of reduced  $\chi^2$  near 1.0, meaning that our methodology for measuring the astrometric uncertainties per epoch is sound. This enables us to identify targets for which either our centroiding is poor because a slightly resolved companion creates a profile not well fit by our PRF, or our single-object solution is a poor assumption due to the presence of an unseen companion. Objects with fits having reduced  $\chi^2$  values  $>2$  have been placed on continued monitoring with *Spitzer* through the end of Cycle 14 to see if any cyclical variations in the residuals, indicative of an unseen astrometric companion, can be found. These and other targets of interest are discussed in Section 8.2.

By design, most of the T dwarfs in our parallax program were selected for observation because they were not being targeted by other ground- or space-based programs. On the other hand, *all* known Y dwarfs were targeted regardless of whether they had parallaxes measured elsewhere. As a result, only 31 of the 142 objects for which we have *Spitzer*-measured parallaxes have previously measured values. Figure 3 compares our values to those in the literature for these 31 objects. Three comparison data points fall outside of the boundaries of this plot, but those are attributed to poor measurements in the literature: WISE 0146+4234 and WISE 2220-3628 from [Beichman et al. \(2014\)](#), which are discrepant from our values by  $\sim 9\sigma$ , and WISE 1541-2250 from [Dupuy & Kraus \(2013\)](#), which is discrepant from our value by  $\sim 20\sigma$ . These values are also discrepant with other published values; see analysis of WISE 2220-3628 and WISE 1541-2250 in [Martin et al. \(2018\)](#) and of WISE 0146+4234 in [Leggett et al. \(2017\)](#).

We find excellent agreement between our values and ground-based Magellan/FourStar measurements by [Tinney et al. \(2014\)](#), between our values and ground-based

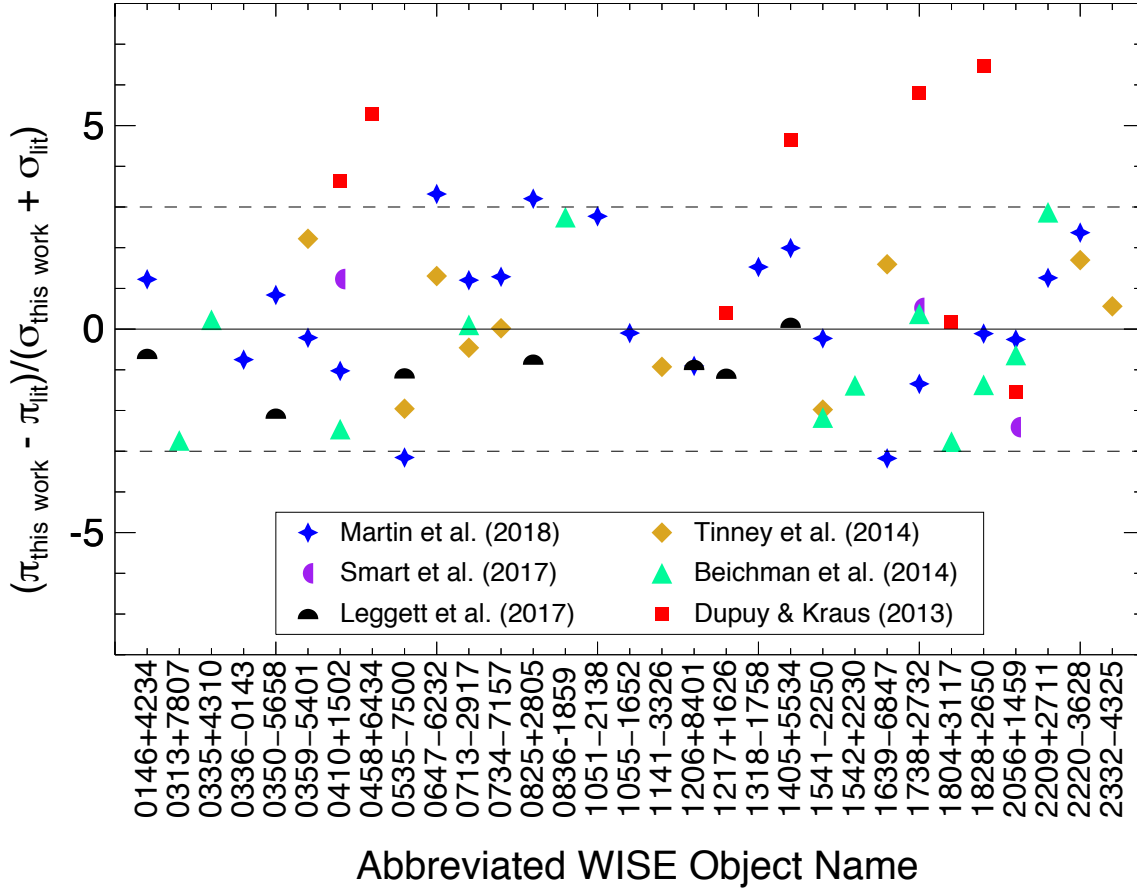


**Figure 2.** Plots of our astrometric measurements and their best fits, divided into four panels. (Upper left) The measured astrometry and its uncertainty at each epoch (black points with error bars) plotted in RA and Dec with the best fit model shown as the blue curve. Red lines connect each observation to its corresponding time point along the best-fit curve. (Upper right) A square patch of sky centered at the mean equatorial position of the target. The green curve is the parallactic fit, which is just the blue curve in the previous panel with the proper motion vector removed. In the background is the ecliptic coordinate grid, with lines of constant  $\beta$  shown in solid pale purple and lines of constant  $\lambda$  shown in dashed pale purple. Grid lines are shown at  $0''.1$  spacing. (Lower left) The change in RA and Dec as a function of time with the proper motion component removed. The parallactic fit is again shown in green. (Lower right) The overall RA and Dec residuals between the observations and the best fit model as a function of time. **The complete figure set contains these same plots for all 142 objects in the *Spitzer* parallax program.**

UKIRT/WFCAM measurements by Smart et al. (2017), and between our values and *Spitzer*/IRAC ch2 measurements by Leggett et al. (2017), some data for which had been published earlier in Luhman & Esplin (2016) and which uses a subset of the *Spitzer*/IRAC ch2 imaging taken by us. With the exception of the two objects noted above, we also find excellent agreement with a hybrid approach from Beichman et

al. (2014) that uses astrometry compiled from Keck/NIRC2, *HST*/WFC3, *WISE*, and *Spitzer*/IRAC.

We can also compare the parallax measurements for objects in common between this paper and Martin et al. (2018). The latter paper uses a subset of the same *Spitzer*/IRAC ch2 data used in the current paper, but there are a few differences to note: (1) the current paper uses measurements taken from individual frames as opposed to the Martin et



**Figure 3.** A comparison of the parallax determinations for thirty-one objects in common between this paper and those of other published works. Our results show excellent agreement with other values, with the exception of measurements from Dupuy & Kraus (2013). See text for discussion.

al. (2018) method of using measurements from the epochal coadds, (2) the current paper uses a different set of analysis code following the MOPEX frame extraction step, even though the guiding logic is very similar, and (3) the current paper benefits from the longer time baseline afforded by the additional data in Cycle 13. Four of the twenty-two objects in common between the two papers have differences exceeding three times the sum of the individual uncertainties. Two of these objects, WISE 0535–7500 and WISE 0647–6323, are located near the Continuous Viewing Zone of *Spitzer* and thus have frames taken at many different roll angles, where the aforementioned issue with the MOPEX mosaicking step (Section 5.2.1) is known to have problems. A comparison of the parallax-only plots for these two objects (Figure 2, upper right panels) show individual measurements with much smaller uncertainties and a more convincing overall fit than do similar plots in Martin et al. (2018) (their Figure 5). For the other two objects – WISE 0825+2805 and WISE 1639–6847 – the improved astrometry provided by individual frame measurements along with the added time baseline (an additional three years) appears to have vastly improved

the fits and as a consequence moved them significantly from the parallax values determined by Martin et al. (2018).

Just as both Smart et al. (2017) and Martin et al. (2018) found, we see a systematic offset between our values and the parallaxes measured by Dupuy & Kraus (2013), who used *Spitzer*/IRAC ch1 imaging. Martin et al. (2018) advanced three hypotheses to attempt to explain the discrepancy: (1) chromatic distortion in the ch1 data, (2) a fundamental error in the Dupuy & Kraus (2013) fitting analysis, or (3) an insufficient time baseline with which to beat down random errors and to disentangle proper motion and parallax. Despite testing each of these hypotheses, Martin et al. (2018) were unable to come to a firm conclusion.

## 6. USNO ASTROMETRY

A number of early *WISE* discoveries from Table 1 were astrometrically monitored at the US Naval Observatory (USNO) in Flagstaff. These objects were measured on the 1.55 m Strand Astrometric Reflector using the ASTROCAM infrared imager (Fischer et al. 2003), which was commissioned in Sep 2000. Sadly, the original ASTROCAM was



destroyed in a cryogenic explosion ultimately caused by a local forest fire in Jun 2006. In May 2011, a repaired version of ASTROCAM was commissioned, using the same basic setup as the old instrument. Observation and reductions procedures for these new targets are nearly identical to those described in Vrba et al. (2004), which presented preliminary parallaxes and proper motions of 40 L and T dwarfs using the first 1.7 years of data from the original instrument. The only difference is that these new reductions use a combined X+Y solution, rather than just using the X solution as was done in Vrba et al. (2004).

The eighteen objects in Table 5 were placed on the program over a number of years after recommissioning. The abbreviated object name is given in column 1, the relative parallax and its uncertainty in column 2, the proper motion along with its uncertainty and position angle (east of north) in columns 3

and 4, the total time baseline of the observations in column 5, the number of independent nights of observation in column 6, and the number of registration stars in column 7. Objects having smaller measurement errors are generally those that have been observed over a longer time baseline. As a case in point, WISE 2226+0440 has the poorest measurements because it was added much later into the program. (In fact, it is the only object in Table 5 not already listed in Table 3 of Vrba et al. 2015.) Given the typical magnitudes of the registration stars, the correction from relative to absolute parallax is  $\sim 1.6 \pm 0.3$  mas (Vrba et al. 2004). For subsequent analyses we have added this correction, and its uncertainty in quadrature, to the relative parallax to convert to near-absolute units.

**Table 5.** Parallax and Motion Fits for Objects on the USNO Parallax Program

Object Name	$\pi_{rel}$ (mas)	$\mu_{rel}$ (mas yr <sup>-1</sup> )	$\theta$ (deg)	Baseline (yr)	# of Ep.	# of Stars
(1)	(2)	(3)	(4)	(5)	(6)	(7)
WISE 0254+0223	144.49±1.45	2572.2±0.1	85.05±0.03	5.30	107	13
WISE 0513+0608	69.17±1.49	433.0±1.0	180.69±0.07	5.41	133	16
WISE 0614+3912	52.09±1.70	529.3±1.2	200.55±0.07	5.30	71	20
WISE 0625+5646	47.94±2.02	52.7±1.4	251.86±0.76	5.24	74	15
WISE 1019+6529	41.25±1.75	150.6±1.1	323.89±0.21	5.92	93	7
WISE 1122+2550	64.74±2.26	1028.6±1.2	252.34±0.04	5.98	88	8
WISE 1320+6034	59.00±2.54	561.3±1.4	264.80±0.08	6.05	50	10
WISE 1322-2340	75.86±4.22	524.1±1.9	318.35±0.11	5.92	56	9
WISE 1457+5815	53.43±2.30	502.0±1.1	262.75±0.07	6.08	107	12
WISE 1506+7027	191.91±0.51	1587.3±0.3	311.19±0.03	6.08	100	9
WISE 1627+3255	52.77±1.85	351.6±0.8	193.55±0.07	6.10	66	11
WISE 1741+2553	212.65±2.77	1556.9±1.3	198.94±0.04	5.10	56	14
WISE 1852+3537	70.41±1.88	381.5±1.1	138.82±0.09	5.29	63	15
WISE 1906+4508	59.04±0.72	473.0±0.4	111.74±0.04	5.35	53	16
WISE 2213+0911	52.88±2.45	128.0±1.2	256.46±0.27	5.37	133	9
WISE 2226+0440	49.13±8.85	542.8±10.0	210.39±0.53	1.21	26	9
WISE 2340-0745	46.19±3.11	293.1±1.4	148.58±0.14	5.32	61	9
WISE 2348-1028	56.77±3.46	642.5±1.5	75.96±0.08	5.24	62	7

## 7. NTT AND UKIRT ASTROMETRY

Twenty-three additional late-T dwarfs were monitored astrometrically at either the 3.5m New Technology Telescope (NTT) or at the 3.8m United Kingdom Infrared Telescope (UKIRT); one of these objects was observed at both facilities. Table 6 lists the results. An abbreviated name of the object from Table 1 is given in column 1, and the source of the measurement as either NTT or UKIRT is given in column

2. The J2000 equinox RA and Dec along with the epoch of the position are given in columns 3-5. The measured value of the absolute parallax and the correction from relative parallax is given in columns 6-7, and the measured proper motions per axis are given in columns 8-9. Columns 10-12 list the total time baseline, the number of registration stars, and the total number of observations.

Fourteen objects were targeted as part of the NTT Parallaxes of Southern Extremely Cool objects (NPARSEC) project. NPARSEC is a European Southern Observatory

long term program (186.C-0756) of 96 nights on the NTT’s infrared spectrograph and imaging camera Son Of ISAAC (SOFI; Moorwood et al. 1998). The main observational program ran from 01 Oct 2010 through 15 Sep 2013, although various ad-hoc requests were made to extend the temporal baseline through 2018. Target selection, observing methodology, and reduction procedures are explained in detail in Smart et al. (2013).

Ten objects were targeted as part of a UKIRT program primarily designed to follow-up T dwarfs from the UKIRT Infrared Deep Sky Survey (UKIDSS; Lawrence et al. 2007). This program, described in Marocco et al. (2010), used ser-

vice observations on the UKIRT Wide Field Camera (WFCAM; Casali et al. 2007), which is a large-field infrared imager. This program started as a director’s discretionary request in 2007 and continued under various proposals and target lists until 2016. As the UKIDSS discovery image was often used in the parallax determination, some targets also have observations starting as early as 2005. Scheduling, observing methodology, and reduction procedures are described in Smart et al. (2010) and Marocco et al. (2010).

The results in Table 6 are regarded as preliminary only. Final reductions on both data sets will be completed in the near future, once observations from the NTT program conclude.

**Table 6.** Parallax and Motion Fits for Objects on the NTT and UKIRT Parallax Programs

Object Name	Program	J2000 RA (deg)	J2000 Dec (deg)	Epoch	$\pi_{abs}$ (mas)	Abs. Corr. (mas)	$\mu_{RA}$ (mas yr <sup>-1</sup> )	$\mu_{Dec}$ (mas yr <sup>-1</sup> )	Baseline (yr)	# of Ref. Stars	# of Obs.
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
WISE 0040+0900	UKIRT	10.103778	9.0151823	2010.50	69.8±1.5	1.0	-52.3±0.9	-53.0±2.0	6.0	117	11
ULAS 0150+1359	UKIRT	27.601590	13.990027	2011.01	39.8±3.2	1.1	25.0±1.9	24.8±1.4	7.4	177	31
WISE 0223-2932	NPARSEC	35.844782	-29.550163	2016.79	80.7±2.6	0.6	780.2±1.1	-535.1±1.5	5.8	50	13
2MASS 0348-6022	NPARSEC	57.030457	-60.376464	2010.75	120.1±1.8	0.6	-279.7±0.6	-768.5±0.7	6.4	87	16
UGPS 0521+3640	UKIRT	80.364579	36.678113	2012.65	122.2±1.6	0.3	569.0±0.9	-1511.0±1.0	8.3	311	27
WISE 0528-3308	NPARSEC	82.185418	-33.140095	2011.93	49.4±3.9	0.7	1.0±1.2	-19.5±1.6	6.2	71	16
WISE 0542-1628	NPARSEC	85.629964	-16.474330	2015.89	61.5±2.7	0.7	-217.7±0.9	294.6±0.9	6.2	131	23
WISE 0612-3036AB	NPARSEC	93.057745	-30.603509	2011.12	41.1±1.6	0.6	-120.3±0.7	-258.5±1.7	6.2	274	18
WISE 0623-0456	NPARSEC	95.790440	-4.9403225	2012.98	87.4±2.9	0.6	-905.2±1.1	159.9±0.8	6.2	483	19
WISE 0627-1114	NPARSEC	96.837083	-11.242068	2015.92	74.8±3.6	0.4	-13.2±1.2	-337.8±1.1	6.2	361	23
WISE 0750+2725	UKIRT	117.51434	27.428690	2014.88	68.4±3.4	0.8	-755.7±2.0	-205.6±1.8	4.5	322	18
WISE 0751-7634	NPARSEC	117.78645	-76.580638	2013.23	97.9±6.7	0.6	-104.8±2.8	-189.7±4.5	5.3	187	18
ULAS 0859+1010	UKIRT	134.79402	10.170582	2012.27	50.3±1.7	1.2	-359.6±1.1	-615.3±1.1	6.3	93	44
WISE 0929+0409	UKIRT	142.27811	4.1660936	2009.92	41.0±2.2	0.9	513.8±1.0	-468.4±3.4	6.3	219	12
ULAS 0950+0117	NPARSEC	147.69721	1.2925019	2013.15	57.9±2.3	0.7	241.6±0.7	-360.7±1.1	6.2	40	24
ULAS 0950+0117	UKIRT	147.69729	1.292456	2011.87	55.4±3.2	0.9	234.3±1.9	-358.5±2.1	5.9	203	41
ULAS 1029+0935	UKIRT	157.41857	9.5873423	2012.98	66.8±4.2	1.0	-414.5±1.9	-138.2±2.6	6.3	115	14
ULAS 1238+0935	UKIRT	189.61832	9.8977247	2011.04	44.1±6.1	0.8	-445.8±2.7	48.4±2.9	9.0	223	30
WISE 1311+0122	NPARSEC	197.77626	1.3810927	2013.23	68.8±2.7	0.3	277.9±0.9	-813.9±0.9	5.1	99	18
ULAS 1315+0826	UKIRT	198.78501	8.4407566	2011.01	50.5±5.7	0.9	-61.4±2.1	-101.8±2.5	9.7	240	27
WISE 1617+1807	NPARSEC	244.27404	18.120548	2012.66	84.6±4.2	0.6	92.6±2.1	-40.0±2.1	5.7	48	17
WISE 1812+2721	NPARSEC	273.04510	27.362316	2012.66	98.5±4.4	0.5	140.3±4.1	-322.2±7.8	2.1	256	13
WISE 2018-7423	NPARSEC	304.60471	-74.391622	2012.64	83.2±1.9	0.5	307.7±1.0	-1008.4±1.6	5.9	99	19
ULAS 2342+0856	NPARSEC	355.62098	8.9388664	2012.66	39.9±2.8	0.5	260.1±1.7	-54.8±1.3	3.0	46	19

## 8. ANALYSIS OF THE MEAN TRENDS

In the following subsections, we amass the color, parallax, and proper motion data from Tables 1, 2, 4, 5, and 6 to study trends in spectral type, absolute magnitude, color, and tangential velocity for late-T to early-Y dwarfs. We also discuss objects that may be particularly interesting because of their

unusual placement relative to the means trends or their high reduced  $\chi^2$  values in the *Spitzer* parallax and proper motion fits.

Table 7 summarizes the adopted spectral types (column 2), the measured parallaxes and proper motions (columns 4 and 6), and the derived absolute magnitudes (columns 8-13) and tangential velocities (column 14) for all of the T6 and later objects for which we have newly measured parallaxes

or for which quality parallaxes have been published by other groups. Full designations for the abbreviated names listed in column 1 can be found in Table 1, and the spectral code in column 3 gives a conversion from the spectral type to a scale

running from 6 at T6.0 to 14 at Y4. Objects lacking spectral types are not shown on subsequent plots having spectral type along one axis, with the exception of WD 0806B and WISE 0855–0714, whose types are assumed to be Y1 and  $\geq$ Y4 (see footnotes to Table 1).

**Table 7.** Summary of Spectral Types, Parallaxes, Proper Motions, Absolute Magnitudes, and Tangential Velocities

Object	Spec.	Spec.	$\pi$	$\pi$	$\mu_{total}$	$\mu_{total}$	$M_H$	$M_{P1}$	$M_{W2}$	$M_{W3}$	$M_{d1}$	$M_{d2}$	$V_{tan}$
Name	Type	Code	(mas)	type*	(mas/yr)	Ref.	(mag)	(mag)	(mag)	(mag)	(mag)	(mag)	(km/s)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
WISE 0005+3737	T9	9	127.0±2.4	abs	1034.0±2.0	Table 4	18.50±0.05	17.28±0.10	13.81±0.05	12.30±0.24	15.95±0.05	13.80±0.04	38.6±0.7
WISE 0015-4615	T8	8	71.8±2.7	abs	796.4±2.0	Table 4	17.19±0.11	16.24±0.13	13.50±0.09	...	15.38±0.09	13.51±0.08	52.6±2.0
WISE 0032-4946	T8.5	8.5	63.6±2.9	abs	938.2±2.4	Table 4	17.89±0.17	16.69±0.19	14.09±0.12	11.22±0.36	15.95±0.11	13.95±0.10	69.9±3.2
ULAS 0034-0052	T8.5	8.5	68.7±1.4	abs	359.2±0.8	1	17.67±0.06	16.19±0.14	13.73±0.08	...	15.42±0.06	13.68±0.05	24.8±0.5
2MASS 0034+0523	T6.5	6.5	120.1±3.0	abs	697.5±2.5	Table 4	15.95±0.06	15.49±0.07	12.95±0.06	12.18±0.32	14.49±0.06	12.98±0.06	27.5±0.7
WISE 0038+2758	T9	9	89.7±2.5	abs	97.5±2.2	Table 4	18.68±0.07	17.21±0.16	14.13±0.07	12.14±0.34	16.22±0.07	14.17±0.06	5.2±0.2
Gl 27B	T8	8	90.4±0.3	abs	591.4±0.4	2	16.50±0.03	...	...	...	15.16±0.04	13.40±0.02	31.0±0.1
WISE 0040+0900	T7	7	69.8±1.5	abs	74.5±2.2	Table 6	15.78±0.05	15.20±0.08	13.05±0.07	...	14.29±0.05	12.98±0.05	5.1±0.2
WISE 0049+2151	T8.5	8.5	139.9±2.5	abs	485.4±2.0	Table 4	17.45±0.04	16.65±0.07	13.76±0.05	12.31±0.19	15.74±0.04	13.77±0.04	16.4±0.3
2MASS 0050-3322	T7	7	94.6±2.4	abs	1485.1±2.1	1	15.92±0.11	15.48±0.07	13.46±0.06	11.71±0.25	14.75±0.06	13.47±0.06	74.4±1.9
CFBDS 0059-0114	T8.5	8.5	103.2±2.1	abs	885.8±1.1	1	18.34±0.07	16.97±0.13	13.80±0.06	...	15.84±0.05	13.78±0.05	40.7±0.8
WISE 0123+4142	T7	7	44.0±4.1	abs	608.6±3.2	Table 4	15.42±0.24	15.06±0.22	13.16±0.21	...	14.34±0.20	13.06±0.20	65.6±6.1
CFBDS 0133+0231	T8.5	8.5	56.3±3.4	abs	608.8±2.5	Table 4	17.37±0.16	16.00±0.19	13.73±0.15	...	15.54±0.14	13.81±0.13	51.3±3.1
WISE 0146+4234	Y0	10	52.5±2.3	abs	452.9±1.7	Table 4	21.29±0.17	...	13.68±0.12	...	16.10±0.12	13.67±0.10	40.9±1.8
WISE 0148-7202	T9.5	9.5	91.1±3.4	rel	1269.3±4.1	3	19.02±0.09	18.06±0.22	14.39±0.09	...	16.63±0.09	14.45±0.08	66.0±2.5
ULAS 0150+1359	T7.5	7.5	39.8±3.2	abs	35.2±9.2	Table 6	16.11±0.18	15.50±0.24	13.23±0.20	...	14.45±0.18	13.11±0.18	4.2±1.1
WISE 0221+3842	T6.5	6.5	36.0±4.1	abs	141.3±2.6	Table 4	15.23±0.29	14.51±0.26	12.59±0.25	...	13.71±0.25	12.64±0.25	18.6±2.1
WISE 0223-2932	T7.5	7.5	80.7±2.6	abs	946.1±1.9	Table 6	16.83±0.13	16.40±0.11	13.56±0.08	12.18±0.40	15.34±0.08	13.55±0.07	55.6±1.8
WISE 0226-0211	T7	7	57.3±4.7	abs	527.1±2.7	Table 4	17.67±0.20	16.20±0.22	13.31±0.18	...	15.40±0.18	13.42±0.18	43.6±3.6
WISE 0233+3030	T6	6	31.3±4.2	abs	137.8±3.2	Table 4	14.27±0.29	13.88±0.30	11.82±0.29	...	13.11±0.29	11.83±0.29	20.9±2.8
WISE 0241-3653	T7	7	52.4±2.7	abs	283.8±2.1	Table 4	15.64±0.13	15.46±0.14	12.95±0.12	11.11±0.35	14.34±0.12	12.94±0.11	25.7±1.3
2MASS 0243-2453	T6	6	93.6±3.6	abs	354.8±4.1	4	15.25±0.09	14.51±0.09	12.78±0.09	11.34±0.16	13.81±0.09	12.83±0.09	18.0±0.7
WISE 0247+3725	T8	8	64.8±2.6	abs	87.0±1.8	Table 4	17.30±0.21	17.54±0.44	13.68±0.11	...	15.76±0.10	13.61±0.09	6.4±0.3
WISE 0254+0223	T8	8	144.5±1.5	rel	2572.2±0.1	Table 5	17.11±0.03	16.63±0.05	13.58±0.03	12.18±0.14	15.51±0.03	13.53±0.03	84.4±0.9
WISE 0302-5817	Y0:	10	56.1±4.4	abs	86.8±7.1	Table 4	...	...	14.55±0.19	...	16.93±0.19	14.59±0.17	7.3±0.8
WISE 0304-2705	Y0pec	10	81.5±7.7	abs	513.5±9.6	Table 4	20.58±0.26	...	15.15±0.22	...	17.26±0.21	15.05±0.21	29.9±2.8
WISE 0309-5016	[T7]	—	66.8±3.9	abs	559.8±2.3	Table 4	16.55±0.13	15.59±0.14	12.75±0.13	11.88±0.47	14.65±0.13	12.76±0.13	39.7±2.3
WISE 0313+7807	T8.5	8.5	134.3±3.6	abs	89.7±1.7	Table 4	18.27±0.08	16.59±0.07	13.90±0.06	12.69±0.27	15.95±0.06	13.91±0.06	3.2±0.1
WISE 0316+4307	T8	8	73.3±2.8	abs	435.6±2.1	Table 4	19.03±0.12	17.12±0.24	13.97±0.10	...	15.97±0.09	13.91±0.09	28.2±1.1
WISE 0323-5907	[T6]	—	71.5±4.3	abs	720.5±2.6	Table 4	...	16.08±0.15	13.80±0.14	12.16±0.45	15.04±0.13	13.80±0.13	47.8±2.9
WISE 0323-6025	T8.5	8.5	71.4±2.9	abs	535.6±2.0	Table 4	17.67±0.09	16.88±0.15	13.76±0.10	...	15.84±0.10	13.77±0.09	35.6±1.5
WISE 0325-5044	T8	8	36.7±2.7	abs	176.1±2.2	Table 4	17.24±0.16	16.25±0.30	14.03±0.22	...	15.57±0.18	13.52±0.16	22.7±1.7
WISE 0325-3854	T9	9	57.2±5.4	abs	303.2±2.6	Table 4	18.37±0.29	16.58±0.25	13.77±0.21	11.72±0.48	15.91±0.21	13.77±0.21	25.1±2.4
WISE 0325+0831	T7	7	78.5±3.0	abs	122.3±2.5	Table 4	15.62±0.12	14.82±0.09	13.01±0.09	11.36±0.35	14.17±0.09	13.06±0.08	7.4±0.3
WISE 0335+4310	T9	9	72.1±2.4	abs	1140.7±1.7	Table 4	19.23±0.08	...	13.80±0.09	...	15.90±0.08	13.67±0.07	75.0±2.5

*Table 7 continued*

Table 7 (continued)

Object	Spec.	Spec.	$\pi$	$\pi$	$\mu_{total}$	$\pi, \mu_{total}$	$M_H$	$M_{W1}$	$M_{W2}$	$M_{W3}$	$M_{d1}$	$M_{d2}$	$v_{tan}$
Name	Type	Code	(mas)	type*	(mas/yr)	Ref.	(mag)	(mag)	(mag)	(mag)	(mag)	(mag)	(km/s)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
WISE 0336-0143	Y0	10	99.0±2.4	abs	1239.4±1.7	Table 4	...	18.43±0.47	14.54±0.08	...	17.23±0.08	14.60±0.06	59.3±1.4
2MASS 0348-6022	T7	7	120.1±1.8	abs	817.8±0.9	Table 6	15.96±0.14	15.42±0.04	12.95±0.04	11.62±0.09	14.56±0.04	12.94±0.04	32.3±0.5
WISE 0350-5658	Y1	11	174.6±2.6	abs	618.2±1.9	Table 4	23.47±0.14	...	15.96±0.05	13.54±0.28	19.15±0.10	15.90±0.04	16.8±0.3
WISE 0359-5401	Y0	10	75.8±2.5	abs	787.9±2.0	Table 4	21.43±0.13	...	14.78±0.09	...	16.95±0.10	14.72±0.08	49.3±1.6
WISE 0404-6420	T9	9	45.7±2.7	abs	68.6±2.3	Table 4	18.27±0.13	16.74±0.22	14.03±0.14	...	15.93±0.15	13.72±0.13	7.1±0.5
WISE 0410+1502	Y0	10	150.2±2.4	abs	2410.2±1.6	Table 4	20.78±0.05	...	15.00±0.06	13.20±0.50	17.52±0.05	15.05±0.04	76.1±1.2
WISE 0413-4750	T9	9	48.2±4.8	abs	321.8±3.5	Table 4	18.62±0.22	17.50±0.41	14.00±0.23	...	16.22±0.23	13.90±0.22	31.6±3.2
2MASS 0415-0935	T8	8	175.2±1.7	abs	2278.2±1.2	1	16.92±0.04	16.36±0.04	13.51±0.03	12.31±0.13	15.47±0.03	13.59±0.03	61.6±0.6
WISE 0430+4633	T8	8	93.9±4.1	abs	959.8±3.2	Table 4	19.10±0.15	...	14.27±0.11	...	15.99±0.10	14.08±0.10	48.4±2.1
WISE 0458+6434	T8.5	8.5	109.2±3.6	abs	357.7±1.7	Table 4	17.60±0.09	16.63±0.10	13.21±0.08	12.28±0.29	15.27±0.07	13.18±0.07	15.5±0.5
WISE 0500-1223	T8	8	95.1±3.6	abs	728.7±1.8	Table 4	18.02±0.15	17.34±0.17	13.87±0.09	...	15.84±0.09	13.89±0.08	36.3±1.4
WISE 0512-3004	T8.5	8.5	48.9±2.6	abs	642.2±1.8	Table 4	18.11±0.43	17.08±0.39	13.78±0.14	...	16.09±0.14	14.03±0.12	62.3±3.3
WISE 0513+0608	T6.5	6.5	69.2±1.5	rel	433.0±1.0	Table 5	15.38±0.09	15.09±0.07	13.15±0.06	...	14.35±0.05	13.20±0.05	29.7±0.6
UGPS 0521+3640	T8.5	8.5	122.2±1.6	abs	1614.6±1.3	Table 6	17.72±0.05	14.83±0.04	13.44±0.04	11.59±0.15	15.37±0.04	14.01±0.03	62.6±0.8
WISE 0528-3308	T7pec	7	49.4±3.9	abs	19.5±2.0	Table 6	15.44±0.22	15.70±0.20	12.99±0.18	11.03±0.45	14.78±0.17	13.06±0.17	1.9±0.2
WISE 0535-7500	≥Y1:	11	66.4±2.4	abs	125.2±1.6	Table 4	22.45±0.35	17.05±0.16	14.01±0.09	...	16.86±0.11	14.12±0.08	8.9±0.3
WISE 0540+4832	T8.5	8.5	70.0±2.6	abs	673.4±2.1	Table 4	17.85±0.09	...	14.21±0.11	...	16.20±0.09	13.99±0.08	45.6±1.7
WISE 0542-1628	T6.5	6.5	61.5±2.7	abs	366.3±1.3	Table 6	15.51±0.14	15.17±0.11	12.90±0.10	...	14.21±0.10	12.91±0.10	28.2±1.2
Gl 229B	T7pec	7	172.7±0.3	abs	227.8±0.1	5	15.55±0.05	...	...	...	...	...	20.0±0.0
WISE 0612-3036AB	T6	6	41.1±1.6	abs	285.1±1.8	Table 6	15.13±0.14	14.47±0.10	12.11±0.09	...	13.66±0.09	12.10±0.09	32.9±1.3
WISE 0614+3912	T6	6	52.1±1.7	rel	529.3±1.2	Table 5	15.01±0.26	14.89±0.10	12.28±0.08	...	13.84±0.07	12.25±0.07	48.2±1.6
WISE 0614+0951	T7	7	65.6±2.2	abs	415.0±1.6	Table 4	15.91±0.08	15.71±0.13	13.32±0.09	...	14.57±0.08	13.18±0.08	30.0±1.0
WISE 0623-0456	T8	8	87.4±2.9	abs	919.2±1.4	Table 6	17.02±0.13	16.55±0.12	13.52±0.08	12.11±0.45	15.20±0.08	13.44±0.07	49.9±1.7
WISE 0625+5646	T6	6	47.9±2.0	rel	52.7±1.4	Table 5	15.37±0.13	14.99±0.12	12.90±0.10	10.98±0.49	13.94±0.09	12.89±0.09	5.2±0.3
WISE 0627-1114	T6	6	74.8±3.6	abs	338.1±1.6	Table 6	14.81±0.13	14.35±0.11	12.62±0.11	10.90±0.24	13.64±0.11	12.69±0.11	21.4±1.0
WISE 0645-0302	T6	6	50.7±4.2	abs	318.9±2.6	Table 4	15.86±0.18	16.52±0.37	13.39±0.20	...	14.72±0.18	13.21±0.18	29.7±2.6
WISE 0647-6232	Y1	11	100.3±2.4	abs	387.9±1.5	Table 4	23.32±0.18	...	15.23±0.07	...	17.90±0.11	15.08±0.06	18.3±0.4
WISE 0713-5854	T9	9	78.2±4.6	abs	367.5±3.1	Table 4	18.95±0.20	...	14.73±0.14	...	16.76±0.14	14.61±0.13	22.3±1.3
WISE 0713-2917	Y0	10	107.5±2.4	abs	546.2±1.8	Table 4	20.35±0.09	...	14.62±0.07	12.45±0.36	16.83±0.06	14.38±0.05	24.1±0.5
UGPS 0722-0540	T9	9	242.8±2.4	abs	970.2±2.1	6	18.83±0.03	17.18±0.05	14.13±0.03	12.13±0.07	16.22±0.03	14.15±0.03	18.9±0.2
WISE 0723+3403	T9:	9	56.3±3.5	abs	343.8±1.7	Table 4	17.38±0.15	16.46±0.26	13.44±0.15	...	15.52±0.14	13.44±0.14	28.9±1.8
2MASS 0727+1710	T7	7	112.5±0.9	abs	1296.2±0.9	1	15.93±0.03	15.44±0.04	13.22±0.03	12.18±0.31	14.72±0.03	13.27±0.02	54.6±0.4
2MASS 0729-3954	T8pec	8	126.3±8.3	abs	1738.3±7.6	7	16.49±0.23	15.80±0.15	13.48±0.14	11.87±0.19	15.06±0.14	13.50±0.14	65.2±4.3
WISE 0734-7157	Y0	10	75.0±2.4	abs	571.0±1.8	Table 4	20.45±0.10	18.12±0.29	14.56±0.09	...	17.02±0.10	14.59±0.07	36.1±1.2
WISE 0744+5628	T8	8	67.1±2.5	abs	779.7±1.7	Table 4	16.72±0.14	16.31±0.14	13.66±0.09	11.78±0.50	15.40±0.09	13.69±0.08	55.1±2.1
WISE 0750+2725	T8.5	8.5	68.4±3.4	abs	783.2±2.7	Table 6	18.18±0.12	17.61±0.44	13.73±0.12	...	15.85±0.12	13.66±0.11	54.3±2.7
WISE 0751-7634	T9	9	97.9±6.7	abs	216.7±5.3	Table 6	19.63±0.20	16.90±0.16	14.48±0.15	11.86±0.21	16.37±0.15	14.57±0.15	10.5±0.8
WISE 0759-4904	T8	8	89.1±2.4	abs	440.9±1.6	Table 4	17.16±0.07	16.75±0.11	13.56±0.07	...	15.37±0.06	13.51±0.06	23.5±0.6

Table 7 continued

Table 7 (continued)

Object	Spec.	Spec.	$\pi$	$\pi$	$\mu_{total}$	$\pi, \mu_{total}$	$M_H$	$M_{W1}$	$M_{W2}$	$M_{W3}$	$M_{d1}$	$M_{d2}$	$V_{tan}$
Name	Type	Code	(mas)	type*	(mas/yr)	Ref.	(mag)	(mag)	(mag)	(mag)	(mag)	(mag)	(km/s)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
WD 0806B	[Y1]	11	52.2±1.7	abs	446.8±1.8	8	23.88±0.16	...	15.41±0.11	...	18.24±0.17	15.43±0.09	40.6±1.3
WISE 0811-8051	T9.5:	9.5	98.5±7.7	rel	293.4±6.9	3	19.96±0.22	16.74±0.19	14.31±0.17	12.61±0.36	16.78±0.18	14.37±0.17	14.1±1.2
WISE 0812+4021	T8	8	34.2±2.7	abs	259.6±1.7	Table 4	15.97±0.26	15.47±0.28	12.94±0.20	...	14.60±0.18	12.97±0.17	36.0±2.9
DENIS 0817-6155	T6	6	203±13.	abs	1145.4±67.8	9	15.07±0.14	14.51±0.14	12.80±0.14	11.20±0.14	13.78±0.14	12.84±0.14	26.7±2.3
WISE 0825+2805	Y0.5	10.5	155.8±2.4	abs	241.2±1.8	Table 4	23.93±0.14	...	15.54±0.07	...	18.29±0.07	15.61±0.04	7.3±0.1
WISE 0833+0052	(sd)T9	9	82.6±4.5	abs	1776.1±3.8	Table 4	20.21±0.15	...	14.56±0.14	...	16.59±0.12	14.43±0.12	101.9±5.6
WISE 0836-1859	T8pec	8	40.8±3.6	abs	157.8±1.8	Table 4	16.84±0.32	15.68±0.26	13.20±0.21	...	14.92±0.20	13.14±0.19	18.3±1.6
WISE 0855-0714	[>Y4]	14	438.9±3.0	abs	8147.3±2.7	Table 4	27.04±0.24	23.02±0.42	16.92±0.04	14.35±0.13	20.68±0.07	17.13±0.02	88.0±0.6
WISE 0857+5604	T8	8	87.2±2.4	abs	752.0±1.6	Table 4	17.19±0.15	16.82±0.12	13.80±0.07	...	15.72±0.07	13.84±0.06	40.9±1.1
ULAS 0859+1010	T7	7	50.3±1.7	abs	712.7±1.6	Table 6	17.09±0.09	16.26±0.24	13.67±0.11	...	...	...	67.2±2.3
ULAS 0901-0306	T7.5	7.5	62.6±2.6	abs	264.0±3.6	10	17.44±0.16	16.17±0.16	13.54±0.11	...	15.42±0.10	13.52±0.09	20.0±0.9
WISE 0906+4735	T8	8	48.4±3.4	abs	895.3±1.7	Table 4	16.23±0.22	15.98±0.23	12.97±0.16	...	14.90±0.16	12.97±0.15	87.7±6.2
WISE 0914-3459	T8	8	45.2±4.2	abs	177.0±3.2	Table 4	...	15.89±0.26	13.33±0.21	...	15.02±0.21	13.32±0.20	18.6±1.8
WISE 0929+0409	T6.5	6.5	41.0±2.2	abs	695.3±3.5	Table 6	15.43±0.14	14.61±0.14	12.32±0.13	10.44±0.53	13.78±0.12	12.30±0.12	80.4±4.3
2MASS 0937+2931	T6pec	6	162.8±3.9	abs	1622.0±7.1	4	15.73±0.06	15.15±0.06	12.73±0.06	11.75±0.11	14.21±0.05	12.75±0.05	47.2±1.2
2MASS 0939-2448	T8	8	187.3±4.6	abs	1191.7±3.4	11	17.32±0.10	16.27±0.06	13.00±0.06	12.03±0.10	15.14±0.06	12.98±0.06	30.2±0.7
WISE 0940-2208	T8	8	38.1±4.7	abs	224.3±3.3	Table 4	...	14.77±0.28	12.54±0.27	...	14.30±0.27	12.58±0.27	27.9±3.5
WISE 0943+3607	T9.5	9.5	93.8±2.8	abs	839.4±1.9	Table 4	20.18±0.08	18.04±0.30	14.27±0.08	12.15±0.40	16.61±0.08	14.15±0.07	42.4±1.3
ULAS 0950+0117	T8	8	57.9±2.3	abs	434.1±1.3	Table 6	17.21±0.10	16.45±0.20	13.32±0.10	...	15.12±0.09	13.24±0.09	35.5±1.4
WISE 0952+1955	T6	6	41.1±3.9	abs	47.1±2.0	Table 4	15.29±0.23	14.91±0.24	12.53±0.21	...	13.88±0.21	12.57±0.21	5.4±0.6
WISE 1018-2445	T8	8	83.6±3.6	abs	823.2±1.8	Table 4	17.61±0.25	16.88±0.17	13.74±0.10	...	15.74±0.10	13.75±0.10	46.7±2.0
WISE 1019+6529	T6	6	41.3±1.8	rel	150.6±1.1	Table 5	14.68±0.15	14.44±0.10	12.16±0.10	...	13.47±0.09	12.16±0.09	17.3±0.8
WISE 1025+0307	T8.5	8.5	85.4±2.5	abs	1208.0±1.9	Table 4	18.02±0.08	17.14±0.20	13.79±0.08	...	15.97±0.07	13.85±0.07	67.0±2.0
CFBDS 1028+5654	T8	8	45.0±2.9	abs	201.2±2.1	Table 4	16.65±0.16	...	...	...	14.63±0.14	12.74±0.14	21.2±1.4
ULAS 1029+0935	T8	8	66.8±4.2	abs	436.9±3.2	Table 6	16.75±0.14	15.90±0.18	13.50±0.16	...	15.21±0.14	13.58±0.14	31.0±2.0
WISE 1039-1600	T7.5	7.5	53.4±2.6	abs	223.8±1.9	Table 4	15.83±0.11	15.11±0.13	12.81±0.11	...	14.51±0.11	12.84±0.11	19.9±1.0
WISE 1042-3842	T8.5	8.5	64.8±3.4	rel	93.7±6.2	3	18.27±0.12	17.34±0.32	13.61±0.12	...	15.83±0.12	13.63±0.12	6.9±0.6
ULAS 1043+1048	T8	8	20.8±7.0	abs	141.9±3.7	Table 4	15.12±0.73	15.03±0.87	12.28±0.74	...	13.61±0.73	12.00±0.73	32.3±10.
2MASS 1047+2124	T6.5	6.5	94.7±3.8	abs	1728.4±7.7	4	15.71±0.09	15.26±0.09	12.89±0.09	11.75±0.32	14.29±0.09	12.88±0.09	86.5±3.5
WISE 1050+5056	T8	8	49.7±5.0	abs	432.3±3.3	Table 4	16.79±0.22	16.42±0.32	13.34±0.23	...	15.03±0.22	13.38±0.22	41.2±4.2
WISE 1051-2138	T8.5	8.5	67.0±3.0	abs	207.9±2.0	Table 4	18.32±0.40	16.43±0.17	13.73±0.11	...	15.55±0.10	13.73±0.10	14.7±0.7
WISE 1052-1942	T7.5	7.5	62.3±4.4	abs	453.5±2.7	Table 4	16.03±0.19	15.56±0.17	13.08±0.16	...	14.64±0.16	13.19±0.15	34.5±2.4
WISE 1055-1652	T9.5	9.5	72.2±2.7	abs	1074.6±2.0	Table 4	...	...	14.36±0.11	...	16.59±0.10	14.34±0.08	70.6±2.6
2MASS 1114-2618	T7.5	7.5	179.2±1.4	abs	3043.2±1.1	1	17.09±0.05	16.52±0.04	13.54±0.03	12.61±0.18	15.45±0.03	13.62±0.02	80.5±0.6
WISE 1118+3125	T8.5	8.5	113.2±4.6	abs	745.4±2.8	18,12	18.42±0.11	16.43±0.10	13.61±0.09	12.51±0.34	15.87±0.09	13.64±0.09	31.2±1.3
WISE 1122+2550	T6	6	64.7±2.3	rel	1028.6±1.2	Table 5	15.75±0.13	15.19±0.10	13.20±0.09	...	14.47±0.08	13.21±0.08	75.4±2.7
WISE 1124-0421	T7	7	61.6±3.1	abs	556.5±2.3	Table 4	...	15.39±0.14	13.00±0.12	...	14.32±0.11	13.04±0.11	42.8±2.2
WISE 1139-3324	T7	7	27.0±3.9	abs	1102.2±3.1	Table 4	15.10±0.32	15.63±0.50	12.06±0.32	...	14.05±0.32	12.15±0.31	19.3±2.8

Table 7 continued

Table 7 (continued)

Object	Spec.	Spec.	$\pi$	$\pi$	$\mu_{total}$	$\pi, \mu_{total}$	$M_H$	$M_{W1}$	$M_{W2}$	$M_{W3}$	$M_{d1}$	$M_{d2}$	$V_{tan}$
Name	Type	Code	(mas)	type*	(mas/yr)	Ref.	(mag)	(mag)	(mag)	(mag)	(mag)	(mag)	(km/s)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
WISE 1141-3326	Y0	10	99.7±4.2	abs	907.6±3.4	Table 4	...	17.07±0.15	14.60±0.11	11.72±0.23	16.41±0.10	14.65±0.09	43.2±1.8
WISE 1143+4431	T8.5	8.5	38.1±6.5	abs	104.7±7.2	Table 4	16.94±0.38	16.63±0.53	13.09±0.38	...	15.05±0.37	13.06±0.37	13.1±2.4
WISE 1150+6302	T8	8	124.5±3.0	abs	678.0±2.2	Table 4	...	17.43±0.10	13.88±0.06	12.85±0.31	16.09±0.06	13.90±0.06	25.8±0.6
ULAS 1152+1134	T8.5	8.5	49.7±5.1	abs	493.0±4.2	Table 4	17.14±0.24	15.31±0.25	13.13±0.23	...	14.76±0.23	13.26±0.22	47.0±4.8
WISE 1206+8401	Y0	10	81.9±2.5	abs	629.3±1.7	Table 4	20.63±0.09	...	14.62±0.09	...	16.91±0.09	14.79±0.07	36.4±1.1
2MASS 1217-0311	T7.5	7.5	90.8±2.2	rel	1057.1±1.7	13	15.79±0.06	15.08±0.07	13.02±0.06	11.52±0.27	14.56±0.06	13.10±0.06	54.6±1.3
WISE 1217+1626	T9	9	104.4±4.7	abs	1463.8±2.3	Table 4	18.26±0.10	16.64±0.13	13.22±0.10	12.12±0.33	15.53±0.10	13.20±0.10	66.5±3.0
WISE 1220+5407	T9.5	9.5	42.7±7.1	abs	365.3±9.6	Table 4	...	17.38±0.63	13.91±0.37	...	16.16±0.37	13.87±0.36	40.6±6.8
WISE 1221-3136	T6.5	6.5	73.8±3.3	abs	728.5±3.0	Table 4	15.40±0.20	15.22±0.11	13.21±0.10	11.46±0.34	14.43±0.10	13.23±0.10	46.8±2.1
2MASS 1225-2739	T6	6	75.1±2.5	rel	736.8±2.9	13	14.50±0.11	14.07±0.08	12.13±0.08	10.56±0.16	13.30±0.07	12.15±0.07	46.0±1.5
WISE 1225-1013	T6	6	43.3±3.0	abs	361.2±2.3	Table 4	14.59±0.15	14.38±0.16	12.18±0.16	10.47±0.43	13.49±0.15	12.14±0.15	39.5±2.8
2MASS 1231+0847	T5.5	5.5	75.8±4.8	abs	1564.0±4.7	Table 4	14.71±0.18	14.47±0.14	12.48±0.14	11.63±0.41	13.67±0.14	12.48±0.14	97.8±6.2
2MASS 1237+6526	T6.5	6.5	96.1±4.8	abs	1131.4±8.9	4	15.85±0.15	15.29±0.11	12.85±0.11	11.85±0.25	14.34±0.11	12.86±0.11	55.8±2.8
ULAS 1238+0953	T8	8	44.1±6.1	abs	448.4±4.0	Table 6	17.42±0.30	16.76±0.55	13.56±0.32	...	15.36±0.30	13.59±0.30	48.2±6.7
WISE 1243+8445	T9	9	48.6±4.5	abs	745.5±3.9	Table 4	17.64±0.21	16.99±0.34	14.00±0.21	...	15.79±0.21	13.84±0.20	72.7±6.7
WISE 1254-0728	T7	7	47.2±4.4	abs	1311.6±4.7	Table 4	16.00±0.20	15.15±0.23	13.22±0.22	...	14.70±0.21	13.19±0.20	13.2±1.3
WISE 1257+4008	T7	7	45.7±8.2	abs	365.4±7.3	Table 4	15.26±0.41	14.97±0.40	12.73±0.39	...	14.22±0.39	12.79±0.39	37.9±6.8
VHS 1258-4412	T6	6	63.8±4.0	abs	208.2±3.2	Table 4	...	14.69±0.14	13.04±0.14	11.13±0.30	13.93±0.14	13.02±0.14	15.5±1.0
Gl 494C	T8	8	85.5±1.5	abs	616.5±1.8	2	16.67±0.06	15.70±0.07	13.50±0.05	11.36±0.27	15.02±0.05	13.51±0.04	34.2±0.6
WISE 1301-0302	T8.5	8.5	53.8±5.6	abs	381.6±3.6	Table 4	17.04±0.23	16.27±0.29	13.52±0.24	...	15.29±0.23	13.55±0.23	33.6±3.5
ULAS 1302+1308	T8	8	65.0±5.0	abs	67.2±8.6	14	17.66±0.18	16.76±0.28	13.94±0.18	11.22±0.45	15.58±0.17	13.98±0.17	4.9±0.7
WISE 1311+0122	T9:	9	68.8±2.7	abs	860.0±1.3	Table 6	18.51±0.25	16.77±0.22	13.89±0.10	...	16.00±0.10	13.86±0.09	59.3±2.3
ULAS 1315+0826	T7.5	7.5	50.5±5.7	abs	118.9±3.3	Table 6	18.02±0.26	16.27±0.34	13.67±0.26	...	...	...	11.2±1.3
WISE 1318-1758	T8	8	57.8±2.7	abs	515.2±2.2	Table 4	16.52±0.25	16.32±0.19	13.48±0.12	...	15.60±0.11	13.54±0.10	42.3±2.0
WISE 1320+6034	T6.5	6.5	59.0±2.5	rel	561.3±1.4	Table 5	15.47±0.16	15.63±0.11	13.43±0.10	...	14.74±0.09	13.41±0.10	45.1±1.9
WISE 1322-2340	T8	8	75.9±4.2	rel	524.1±1.9	Table 5	16.06±0.18	16.18±0.15	13.41±0.12	11.94±0.40	15.11±0.12	13.34±0.12	32.7±1.8
WISE 1333-1607	[T7.5]	—	48.0±4.7	abs	339.5±3.1	Table 4	16.78±0.25	16.10±0.29	13.35±0.22	...	15.22±0.22	13.41±0.21	33.5±3.3
ULAS 1335+1130	T8.5	8.5	99.9±1.6	abs	278.2±1.2	1	18.25±0.04	16.94±0.11	13.89±0.05	12.15±0.36	15.99±0.05	13.94±0.04	13.2±0.2
SDSS 1346-0031	T6.5	6.5	68.3±2.3	rel	516.0±3.3	13	15.04±0.09	14.60±0.08	12.83±0.08	11.12±0.25	13.87±0.07	12.87±0.07	35.3±1.2
WISE 1405+5534	Y0:spec?	10.5	157.9±3.1	abs	2338.4±2.1	Table 4	22.49±0.08	19.76±0.40	15.09±0.06	13.20±0.27	17.87±0.06	15.05±0.05	70.2±1.4
ULAS 1416+1348	(sd)T7.5	7.5	109.7±1.3	abs	163.5±1.4	1	17.82±0.03	16.19±0.19	12.98±0.05	12.43±0.30	14.94±0.03	13.00±0.03	7.1±0.1
Gl 547B	sdT8,T8	8	58.2±0.5	abs	527.3±0.6	2	17.78±0.07	16.81±0.26	13.67±0.07	...	15.55±0.05	13.52±0.03	42.9±0.4
VHS 1433-0837	T8	8	50.9±4.5	abs	350.3±3.0	Table 4	17.95±0.28	...	13.77±0.21	...	15.67±0.20	13.57±0.19	32.6±2.9
WISE 1436-1814	T8pec	8	48.3±2.4	abs	109.4±1.8	Table 4	...	15.31±0.15	13.02±0.12	11.02±0.45	14.40±0.11	13.14±0.11	10.7±0.6
WISE 1448-2534	T8	8	52.5±2.5	abs	755.2±2.0	Table 4	17.51±0.16	16.69±0.36	13.56±0.14	...	15.80±0.12	13.69±0.11	68.2±3.3
Gl 570D	T7.5	7.5	171.2±0.9	abs	2013.5±1.3	2	16.45±0.05	16.10±0.04	13.30±0.03	11.95±0.09	15.04±0.02	13.32±0.02	55.7±0.3
WISE 1457+5815	T7	7	53.4±2.3	rel	502.0±1.1	Table 5	15.34±0.30	15.36±0.11	13.12±0.10	11.77±0.51	14.55±0.10	13.14±0.09	44.6±1.9
WISE 1501-4004	T6	6	69.5±4.0	abs	500.8±3.2	Table 4	15.59±0.13	15.30±0.14	13.44±0.13	...	14.49±0.13	13.34±0.13	34.2±2.0

Table 7 continued



Table 7 (continued)

Object	Spec.	Spec.	$\pi$	$\pi$	$\mu_{total}$	$\pi, \mu_{total}$	$M_H$	$M_{W1}$	$M_{W2}$	$M_{W3}$	$M_{d1}$	$M_{d2}$	$V_{tan}$
Name	Type	Code	(mas)	type*	(mas/yr)	Ref.	(mag)	(mag)	(mag)	(mag)	(mag)	(mag)	(km/s)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
2MASS J503+2525	T5	5	157.2±2.2	abs	569.0±1.6	1	14.84±0.04	14.42±0.04	12.70±0.04	11.69±0.08	13.77±0.03	12.73±0.03	17.2±0.2
SDSS J504+1027	T7	7	46.1±1.5	abs	525.3±1.9	1	15.16±0.07	14.53±0.09	12.38±0.08	10.92±0.42	13.82±0.07	12.38±0.07	54.0±1.8
Gl 576B	T0pec	6	52.7±0.3	abs	840.4±0.3	5	15.63±0.03	14.61±0.05	12.84±0.04	...	14.09±0.03	12.86±0.02	75.6±0.4
WISE J506+7027	T6	6	191.9±0.5	rel	1587.3±0.3	Table 5	15.35±0.01	14.84±0.02	12.71±0.02	11.62±0.04	14.06±0.02	12.75±0.02	39.2±0.1
WISE J517+0529	T8	8	42.1±4.2	abs	202.6±3.2	Table 4	16.97±0.22	16.29±0.39	13.24±0.23	...	14.97±0.22	13.22±0.22	22.8±2.3
WISE J519+7009	T8	8	77.6±2.8	abs	597.5±1.9	Table 4	17.73±0.11	16.53±0.10	13.59±0.08	12.71±0.50	15.64±0.09	13.54±0.08	36.5±1.3
WISE J523+3125	T6.5pec	6.5	61.4±3.8	abs	519.7±2.4	Table 4	17.63±0.22	16.60±0.21	13.33±0.14	...	14.89±0.14	13.21±0.14	40.1±2.5
WISE J541+2250	Y1	11	167.1±2.3	abs	905.0±1.7	Table 4	22.18±0.08	17.85±0.17	15.36±0.07	...	17.77±0.05	15.34±0.04	25.7±0.4
WISE J542+2230	T9.5	9.5	85.6±4.2	abs	1050.2±2.8	Table 4	20.18±0.12	18.51±0.44	14.71±0.12	...	16.92±0.12	14.72±0.11	58.2±2.9
2MASS J553+1532	T7	7	75.1±0.9	abs	420.1±0.7	1	15.32±0.16	14.67±0.05	12.41±0.04	11.44±0.33	13.89±0.03	12.51±0.03	26.5±0.3
WISE J612+3420	T6.5	6.5	78.3±3.5	abs	654.1±1.7	Table 4	16.43±0.10	16.89±0.22	13.46±0.11	...	14.92±0.10	13.33±0.10	39.5±1.8
WISE J614+1739	T9	9	97.6±3.4	abs	731.2±1.7	Table 4	19.26±0.09	18.12±0.28	14.17±0.09	...	16.37±0.08	14.16±0.08	35.5±1.2
2MASS J615+1340	T6	6	58.4±2.5	abs	436.7±1.9	Table 4	15.32±0.27	14.97±0.11	12.95±0.10	...	14.22±0.10	12.98±0.09	35.4±1.5
WISE J617+1807	T8	8	84.6±4.2	abs	100.9±3.0	Table 6	17.87±0.13	16.57±0.14	13.70±0.11	12.01±0.40	15.60±0.11	13.73±0.11	5.7±0.3
WISE J622+0959	T6	6	40.2±3.5	abs	44.8±1.8	Table 4	14.07±0.20	14.26±0.20	12.18±0.20	...	13.38±0.19	12.17±0.19	5.3±0.5
SDSS J624+0029	T6	6	90.9±1.2	rel	373.0±1.6	13	15.29±0.06	14.98±0.05	12.90±0.04	11.98±0.40	14.22±0.03	12.92±0.03	19.3±0.3
WISE J627+3255	T6	6	52.8±1.9	rel	351.6±0.8	Table 5	15.08±0.09	14.87±0.09	12.26±0.08	...	13.89±0.08	12.29±0.08	31.6±1.1
SDSS J628+2308	T7	7	75.1±0.9	abs	605.2±0.8	1	16.01±0.04	15.65±0.06	13.30±0.04	11.18±0.25	14.82±0.04	13.32±0.03	38.2±0.5
WISE J639+6847	Y0pec	10	211.9±2.7	abs	3154.0±2.1	Table 4	22.38±0.04	18.90±0.19	15.17±0.07	...	17.82±0.03	15.22±0.03	70.6±0.9
WISE J653+4444	T8	8	78.0±4.2	abs	393.7±3.6	Table 4	16.99±0.13	15.95±0.13	13.28±0.12	11.67±0.29	15.13±0.12	13.33±0.12	23.9±1.3
WISE J711+3500	T8	8	40.3±2.4	abs	171.8±1.6	Table 4	...	15.83±0.20	12.66±0.14	10.87±0.48	14.48±0.13	12.65±0.13	20.2±1.2
WISE J717+6128	T8	8	48.0±3.8	abs	87.3±1.9	Table 4	17.32±0.19	16.17±0.20	13.41±0.18	11.83±0.49	15.48±0.18	13.54±0.17	8.6±0.7
WISE J721+1117	T6	6	42.0±4.0	abs	169.8±3.6	Table 4	14.53±0.23	13.93±0.21	12.43±0.21	10.58±0.54	13.35±0.21	12.47±0.21	19.2±1.9
WISE J735+8209	T6	6	75.1±4.6	abs	359.3±2.6	Table 4	16.06±0.14	14.95±0.14	13.10±0.14	...	14.48±0.13	13.17±0.13	22.7±1.4
WISE J738+2732	Y0	10	131.0±2.4	abs	477.6±1.6	Table 4	20.84±0.05	18.30±0.16	15.08±0.06	13.03±0.40	17.68±0.07	15.06±0.04	17.3±0.3
WISE J741+2553	T9	9	212.7±2.8	rel	1556.9±1.3	Table 5	18.29±0.04	16.96±0.05	14.00±0.04	12.35±0.09	16.08±0.03	14.04±0.03	34.7±0.5
SDSS J758+4633	T6.5	6.5	71.4±0.3	abs	578.4±0.1	5	15.47±0.03	14.92±0.04	13.07±0.03	11.62±0.29	14.11±0.02	13.12±0.02	38.4±0.2
WISE J804+3117	T9.5	9.5	62.7±3.4	abs	251.8±1.6	Table 4	18.20±0.16	17.17±0.30	13.58±0.13	...	15.59±0.12	13.59±0.12	19.0±1.0
WISE J812+2721	T8.5	8.5	98.5±4.4	abs	351.4±8.8	Table 6	18.80±0.19	17.44±0.17	14.16±0.20	...	16.29±0.10	14.14±0.10	16.9±0.9
WISE J812+2007	T9	9	47.8±4.0	abs	534.4±1.6	Table 4	17.35±0.19	...	13.67±0.20	...	15.35±0.19	13.42±0.18	53.5±4.2
WISE J813+2835	T8	8	74.9±2.5	abs	505.7±1.8	Table 4	16.64±0.08	14.96±0.08	13.41±0.07	11.76±0.37	15.19±0.08	13.56±0.07	32.0±1.1
WISE J828+2650	≥Y2	12	100.7±2.3	abs	1032.4±1.4	Table 4	22.75±0.14	...	14.37±0.07	12.46±0.34	16.93±0.05	14.34±0.05	48.6±1.1
SCR 1845-6357B	T6	6	259.5±1.1	abs	2664.4±1.7	15	15.26±0.03	...	...	...	...	...	48.7±0.2
WISE J852+3537	T7	7	70.4±1.9	rel	381.5±1.1	Table 5	16.05±0.06	15.23±0.07	13.43±0.07	11.52±0.33	14.87±0.06	13.47±0.06	25.7±0.7
WISE J906+4508	T6	6	59.0±0.7	rel	475.0±0.4	Table 5	15.23±0.09	14.95±0.05	12.73±0.04	11.79±0.47	13.94±0.04	12.73±0.03	38.0±0.5
WISE J928+2356	T6	6	149.9±2.4	abs	342.7±1.8	Table 4	15.17±0.04	14.45±0.04	12.90±0.04	11.68±0.10	14.02±0.04	12.94±0.04	10.8±0.2
WISE J955+2540	T8	8	36.6±2.4	abs	429.0±1.7	Table 4	15.82±0.15	15.80±0.34	12.78±0.17	...	14.43±0.15	12.84±0.14	55.6±3.6
WISE J959+3338	T8	8	85.3±2.2	abs	193.4±1.5	Table 4	16.83±0.08	15.81±0.09	13.49±0.07	...	15.01±0.06	13.44±0.06	10.7±0.3

Table 7 continued

Table 7 (continued)

Object	Spec.	Spec.	$\pi$	$\pi$	$\mu_{total}$	$\pi, \mu_{total}$	$M_H$	$M_{W1}$	$M_{W2}$	$M_{W3}$	$M_{d1}$	$M_{d2}$	$V_{tan}$
Name	Type	Code	(mas)	type*	(mas/yr)	Ref.	(mag)	(mag)	(mag)	(mag)	(mag)	(mag)	(km/s)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
WISE 2000+3629	T8	8	133.1±2.5	abs	378.0±1.8	Table 4	16.36±0.04	15.70±0.07	13.31±0.05	11.83±0.11	14.84±0.05	13.30±0.04	13.5±0.3
WISE 2005+5424	sdT8	8	62.9±3.3	abs	1464.0±1.7	Table 4	18.56±0.14	16.69±0.18	13.87±0.12	...	14.86±0.12	13.62±0.12	110.3±5.8
WISE 2015+6646	T8	8	43.1±2.7	abs	517.2±2.1	Table 4	14.67±0.16	14.64±0.14	12.87±0.14	...	14.49±0.14	12.80±0.14	56.9±3.6
WISE 2017-3421	[T7.5]	—	46.9±4.1	abs	349.4±3.2	Table 4	18.73±0.33	16.71±0.56	13.30±0.21	...	15.08±0.19	13.23±0.19	35.3±3.1
WISE 2018-7423	T7	7	83.2±1.9	abs	1054.3±1.9	Table 6	16.77±0.06	16.09±0.08	13.21±0.06	...	14.88±0.05	13.15±0.05	60.1±1.4
WISE 2019-1148	T8:	8	77.5±3.5	abs	357.5±1.8	Table 4	17.68±0.12	16.70±0.18	13.75±0.11	...	15.47±0.10	13.70±0.10	21.9±1.0
WISE 2056+1459	Y0	10	138.3±2.2	abs	981.3±1.4	Table 4	20.34±0.05	17.18±0.08	14.54±0.05	12.44±0.25	16.74±0.05	14.63±0.04	33.6±0.5
WISE 2102-4429	T9	9	92.3±1.9	rel	356.9±2.7	3	18.41±0.08	16.78±0.12	13.97±0.06	...	16.15±0.06	14.05±0.05	18.3±0.4
WISE 2134-7137	T9pec	9	109.1±3.7	rel	1381.4±6.2	3	19.89±0.17	17.79±0.16	14.15±0.08	12.58±0.40	16.36±0.08	14.15±0.08	60.0±2.1
ULAS 2146-0010	T8.5	8.5	79.8±4.5	abs	911.8±1.8	16	18.28±0.13	15.33±0.13	13.60±0.13	...	15.90±0.12	13.93±0.12	54.2±3.1
WISE 2147-1029	T7.5	7.5	42.8±4.0	abs	161.7±2.5	Table 4	15.89±0.22	15.97±0.33	13.16±0.22	...	14.71±0.21	13.12±0.20	17.9±1.7
WISE 2157+2659	T7	7	59.7±2.2	abs	115.5±1.6	Table 4	16.33±0.09	15.87±0.13	13.37±0.09	...	14.89±0.09	13.32±0.08	9.2±0.4
WISE 2159-4808	T9	9	75.7±2.7	abs	1269.9±1.9	Table 4	18.65±0.14	17.03±0.20	14.01±0.09	...	16.24±0.09	13.97±0.08	79.5±2.8
WISE 2203+4619	T8	8	66.0±4.2	abs	1313.0±6.2	Table 4	...	...	14.06±0.15	...	15.46±0.14	13.74±0.14	94.3±6.0
Gl 845C	T6	6	276.1±0.3	abs	4704.9±0.3	2	15.48±0.02	...	...	...	...	...	80.8±0.1
WISE 2209+2711	Y0:	10	161.6±2.4	abs	1814.8±1.6	Table 4	23.43±0.15	...	15.81±0.06	13.50±0.39	18.86±0.09	15.78±0.04	53.2±0.8
WISE 2209-2734	T7	7	78.2±3.9	abs	891.9±3.1	Table 4	16.55±0.12	15.78±0.13	13.32±0.12	...	14.94±0.11	13.37±0.11	54.1±2.7
WISE 2211-4758	[T8]	—	55.8±4.6	abs	128.0±3.8	Table 4	16.52±0.18	16.20±0.23	13.34±0.19	11.24±0.51	15.11±0.18	13.35±0.18	10.9±1.0
WISE 2212-6931	T9	9	81.9±2.5	abs	786.3±1.7	Table 4	19.80±0.08	16.83±0.14	14.44±0.09	...	16.93±0.09	14.54±0.07	45.5±1.4
WISE 2213+0911	T7	7	52.9±2.5	rel	128.0±1.2	Table 5	15.67±0.15	15.26±0.13	13.33±0.12	...	14.47±0.10	13.25±0.10	11.5±0.6
WISE 2220-3628	Y0	10	97.0±2.4	abs	298.1±1.7	Table 4	20.79±0.07	...	14.65±0.08	...	17.13±0.08	14.67±0.06	14.6±0.4
WISE 2226+0440	T8	8	49.1±8.9	rel	542.8±10.0	Table 5	15.85±0.38	15.39±0.40	13.03±0.39	...	14.65±0.38	13.07±0.38	52.4±9.5
2MASS 2228-4310	T6	6	92.1±2.6	abs	305.7±3.6	17	15.18±0.13	15.06±0.07	13.15±0.07	11.57±0.28	14.27±0.06	13.17±0.06	15.7±0.5
WISE 2232-5730	T9	9	49.9±4.4	abs	418.3±2.8	Table 4	17.69±0.22	16.08±0.26	13.69±0.21	10.39±0.37	15.93±0.20	13.67±0.19	39.7±3.5
WISE 2237+7228	T6	6	62.3±2.5	abs	126.4±1.8	Table 4	14.91±0.23	14.54±0.09	12.56±0.09	11.31±0.34	13.58±0.09	12.53±0.09	9.6±0.4
WISE 2255-3118	T8	8	70.7±4.2	abs	341.2±2.7	Table 4	16.95±0.17	15.80±0.15	13.41±0.14	...	15.16±0.13	13.46±0.13	22.9±1.4
WISE 2301+0216	T6.5	6.5	53.0±2.8	abs	121.4±2.3	Table 4	15.32±0.12	14.82±0.13	12.96±0.13	...	14.22±0.12	12.99±0.12	10.9±0.6
WISE 2302-7134	[T4.5]	—	65.1±4.7	abs	110.6±3.1	Table 4	16.86±0.20	15.91±0.18	13.31±0.16	...	15.06±0.16	13.30±0.16	8.0±0.6
WISE 2313-8037	T8	8	93.5±2.7	abs	487.3±1.8	Table 4	17.13±0.15	16.29±0.08	13.53±0.07	12.33±0.37	15.14±0.07	13.54±0.07	24.7±0.7
WISE 2319-1844	T7.5	7.5	79.2±3.1	abs	153.4±2.3	Table 4	17.49±0.10	16.16±0.12	13.32±0.09	...	15.41±0.09	13.44±0.09	9.2±0.4
ULAS 2321+1354	T7.5	7.5	83.6±2.4	abs	567.1±1.8	Table 4	16.70±0.09	16.55±0.14	13.72±0.09	...	15.47±0.07	13.80±0.07	32.2±0.9
WISE 2325-4105	T9pec	9	107.8±3.7	rel	837.0±6.7	3	19.38±0.13	17.23±0.14	14.27±0.08	...	16.43±0.08	14.25±0.08	36.8±1.3
ULAS 2326+0201	T8	8	49.5±4.6	abs	310.4±3.3	Table 4	16.93±0.23	16.43±0.36	14.00±0.24	...	15.35±0.20	13.92±0.20	29.7±2.8
WISE 2332-4325	T9:	9	65.3±2.6	abs	353.3±1.9	Table 4	18.64±0.17	17.05±0.26	14.03±0.11	...	16.35±0.10	14.09±0.09	25.6±1.0
WISE 2340-0745	T7	7	46.2±3.1	rel	293.1±1.4	Table 5	14.59±0.15	14.33±0.15	12.00±0.15	...	13.59±0.14	12.02±0.14	30.1±2.0
ULAS 2342+0856	T6.5	6.5	39.9±2.8	abs	265.8±2.1	Table 6	14.73±0.16	13.97±0.16	11.96±0.16	...	13.29±0.15	11.99±0.15	31.6±2.2
WISE 2343-7418	T6	6	58.8±2.7	abs	426.8±1.8	Table 4	14.99±0.11	14.52±0.11	12.60±0.10	11.63±0.51	13.88±0.10	12.60±0.10	34.4±1.6
WISE 2344+1034	T9	9	64.7±3.7	abs	942.4±1.9	Table 4	18.12±0.17	17.19±0.37	14.00±0.15	...	15.79±0.13	13.96±0.13	69.0±4.0

Table 7 continued

Table 7 (continued)

Object	Spec.	Spec.	$\pi$	$\pi$	$\mu_{total}$	$\pi, \mu_{total}$	$M_H$	$M_{W1}$	$M_{W2}$	$M_{W3}$	$M_{d1}$	$M_{d2}$	$v_{tan}$
Name	Type	Code	(mas)	type*	(mas/yr)	Ref.	(mag)	(mag)	(mag)	(mag)	(mag)	(mag)	(km/s)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
WISE 2348-1028	T7	7	56.8±3.5	rel	642.5±1.5	Table 5	15.76±0.18	15.48±0.16	13.21±0.14	...	14.70±0.13	13.19±0.13	53.6±3.3
WISE 2354+0240	Y1	11	124.1±4.9	abs	629.1±4.1	Table 4	23.35±0.31	...	15.48±0.12	...	18.57±0.14	15.48±0.09	24.0±1.0
WISE 2357+1227	T6	6	59.5±4.1	abs	501.1±4.1	Table 4	15.36±0.15	14.61±0.16	12.89±0.15	10.97±0.40	14.13±0.15	12.98±0.15	40.0±2.9

NOTE—References for parallax and total motions: (1) Dupuy & Liu 2012, (2) van Leeuwen 2007, (3) Tinney et al. 2014, (4) Vrba et al. 2004, (5) Gaia Collaboration et al. 2016, (6) Leggett et al. 2012, (7) Faherty et al. 2012, (8) Subasavage et al. 2009, (9) Artigau et al. 2010, (10) Marocco et al. 2010, (11) Burgasser et al. 2008, (12) Zacharias et al. 2012, (13) Tinney et al. 2003, (14) Manjavacas et al. 2013, (15) Henry et al. 2006, (16) Harrington & Dahn 1980, (17) Smart et al. 2013, (18) van Altena et al. 1995.

\* Denotes whether the listed parallax has been corrected to absolute ("abs") or is only relative ("rel"). For subsequent analyses and for the absolute magnitude and tangential velocity computations in this table, the relative parallaxes listed have been corrected to near-absolute parallaxes as follows: those from Tinney et al. (2003) have been adjusted upward by 0.9±0.3 mas, those from Tinney et al. (2014) have been adjusted upward by 0.6±0.3 mas, and those from Table 5 have been adjusted upward by 1.6±0.3 mas. See text for details.

Column 5 indicates whether the parallax value in column 4 is an absolute or a relative value. The only references with relative parallaxes are the USNO results from Table 5 and those from Tinney et al. (2003) and Tinney et al. (2014). As stated in section 6, the correction from relative to absolute parallax is expected to be  $\sim 1.6 \pm 0.3$  mas for the USNO results. The near-infrared results from Tinney et al. (2003) were done on a telescope of larger aperture (3.5m NTT) than that of the USNO program (1.55m Strand), so smaller corrections can be assumed based on the fact that stars in the reference frames are generally fainter and more distant. The corrections shown in Table 6 from both the 3.5m NTT and 3.8m UKIRT indicate that a correction of  $\sim 0.9 \pm 0.3$  mas is also appropriate here. The near-infrared results from Tinney et al. (2014) were obtained on the larger aperture Magellan Baade Telescope (6.5m), so even smaller corrections of  $\sim 0.6 \pm 0.3$  mas can be assumed. These mean relative-to-absolute parallax corrections have been applied to all parallaxes for these three sources prior to the calculation of the absolute magnitudes and tangential velocities in Table 7. These corrections have also been applied in the analyses of subsequent sections of this paper.

For the photometry, we list only  $H$ -band of the normal  $J$ ,  $H$ ,  $K$  complement because it is the only one of these three bands that is invariant between the two main near-infrared classification systems, 2MASS and MKO-NIR (see section 4.3 of Kirkpatrick et al. 2012). Photometry shortward of  $J$ -band is scarce due to a combination of non-universal filters (such as  $z$  and  $Y$ ) and the fact that these brown dwarfs are much fainter, and thus harder to detect, at even shorter wavelengths (e.g., at  $R$  or  $I$ ). Longward of  $K$ -band, we list the *WISE* W1, W2, and W3 photometry, although the last of these bands is generally not sensitive enough to detect these brown dwarfs well. In some cases, the object is sufficiently faint in the W1 band that it is not detected well there, either. We also list photometry in the *Spitzer*/IRAC ch1 and ch2 bands.

### 8.1. Identifying Outliers from the Mean Trends

Given the sheer number of objects with accurate parallaxes, motions, and photometry, we can now examine trends across the late-T and early-Y spectral types, particularly in relation to the 20-pc sample we are building for mass function analysis. The goal of this section is to examine these trends in an effort to identify outliers that may need special handling in section 9.3. In some cases, outliers may indicate unresolved binarity, and this is an issue because we want to have the most accurate accounting possible of the number of objects within our sample volume. In other cases, outliers may indicate unusual spectroscopic features which may be devil our translation of an observational parameter such as spectral type or color into a physical parameter such as effective temperature. In this subsection, we identify plots useful for identifying unusual objects, and in section 8.2 we discuss each of these objects in detail so that they will be properly handled during the mass function computation.

Shown in the leftmost panels of Figure 4 (blue points) are trends of  $H$ -W2 and  $H$ -ch2 color with spectral type. These colors are very similar because the W2 and ch2 bands sample a similar range in wavelength near the peak flux in cold brown dwarfs (see Figure 2 of Mainzer et al. 2011). A number of outliers stand out as having unusually red colors for their types between T6.5 and T8.

The middle panels of Figure 4 (green points) show the trends of W1-W2 and ch1-ch2 color with spectral type. Notable here are a handful of objects with significantly blue colors, especially on the ch1-ch2 plot.

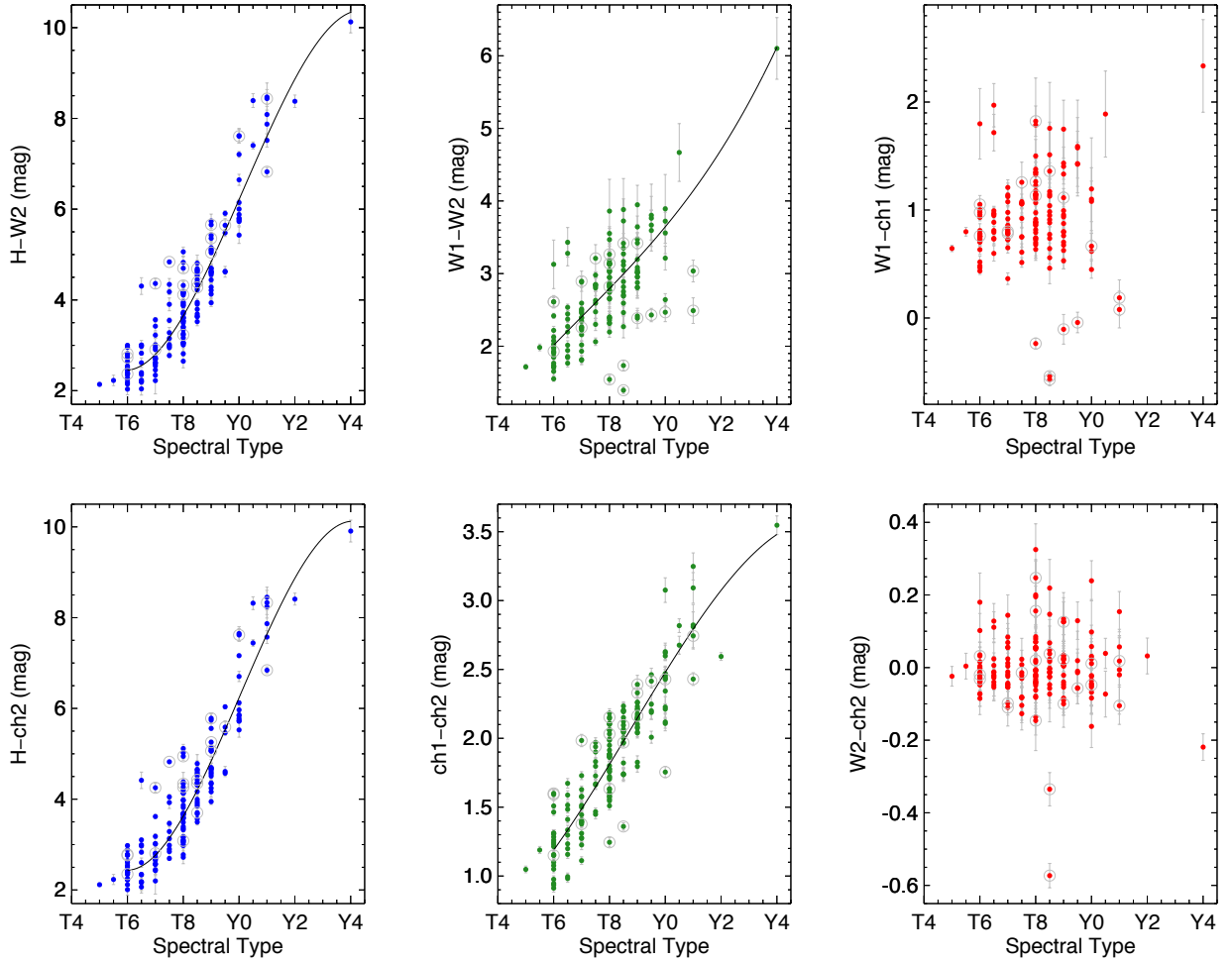
The rightmost panels in Figure 4 (red points) show the trends of W1-ch1 and W2-ch2 color with spectral type. Given the similarity of the W2 and ch2 filters, one would expect the W2-ch2 color to fall near zero, which it does. Objects falling significantly far from zero color likely have contamination by a background source in one of the two bands. The W1 and ch1 filters, on the other hand, sample slightly different wavelengths, with the W1 band centered squarely on the fundamental methane absorption feature near  $3.3 \mu\text{m}$  and the ch1 band lying somewhat redward of this and sampling more of the rise in the brown dwarf spectrum near  $4.0 \mu\text{m}$  (Figure 2 of Mainzer et al. 2011). As expected, objects are generally fainter in the W1 band than in the ch1 band, but the plot shows a few exceptions that again are likely to be objects with contaminated photometry in one of the bands.

Shown in Figure 5 are trends of absolute magnitude with spectral type. Despite the small uncertainties on these measurements, there is a surprisingly large scatter of absolute magnitude in all bands at each spectral subclass. At W2 and ch2, there is typically a magnitude of scatter at each late-T subclass, and this increases to two magnitudes at  $H$ , W1, and ch1. (The uncertainties at W3 are large enough that interpretation is more difficult.) At Y0, this scatter increases by roughly another magnitude in all bands. Despite this dispersion, we nonetheless can identify some objects that fall significantly further off the trends than the others.

On the absolute W1 and ch1 plots of Figure 5, we consider a T dwarf to be unusual if it is a clear outlier on *both* plots, since the T dwarfs in our sample generally have solid photometry in both bands. For the absolute W2 and ch2 plots, we consider an object to be unusual only if it appears as a significant outlier at both bands, and we can apply this strategy to T and Y dwarfs because both are easily detected at these wavelengths.

Figure 6 shows trends of absolute magnitudes with ch1-ch2 color. There is a linear trend of decreasing absolute magnitude with increasing ch1-ch2 color, but with a notable inflection point in most of the plots near ch1-ch2  $\approx 2.2$  mag, corresponding to the transition between types T and Y (see Figure 4).

Figure 7 shows the trend of absolute magnitudes with  $H$ -W2 color. These trends appear more linear than those with ch1-ch2 color above in that there is not a clear inflection point at the T/Y transition, corresponding to  $H$ -W2  $\approx 6.5$  mag, although data redder than this value are not plentiful. The plot of  $M_H$  vs.  $H$ -W2 color shows a tight correlation



**Figure 4.** Trends of color with spectral type for all objects from Table 7 that fall within 20 pc of the Sun ( $\pi_{abs} \geq 50$  mas). Shown as blue points in the two leftmost panels are trends with  $H-W2$  and  $H-ch2$  color. The two middle panels show trends of  $W1-W2$  and  $ch1-ch2$  color (green points). The two rightmost panels show trends of  $W1-ch1$  and  $W2-ch2$  color (red points). Polynomial fits to the relations in the four leftmost panels are shown by the black curves, and the functional forms are presented in Table 8. Points ignored by the fitting (see Section 8.3) are circled in gray.

between quantities, so we examine this plot in detail in Figure 8. The tight correlation allows us to identify close binary systems that may or may not already be known. Unresolved, equal-magnitude doubles would be expected to fall 0.75 mag above the canonical sequence, and there are a number of objects that appear to lie at roughly this level above the mean trend. For reference, we label and circle in red all of the known doubles. Other objects, not known to be doubles, exhibit the same overluminosity. We also label the locations of the known subdwarfs on this diagram with blue circles. This shows that – with the exception of ULAS 1416+1348, which may itself be an unresolved double – these objects fall on the main locus. There are a few objects that also inhabit an area below the main trend.

Finally, we plot a histogram of the measured tangential velocities in Figure 9 along with trends of  $v_{tan}$  as a function of

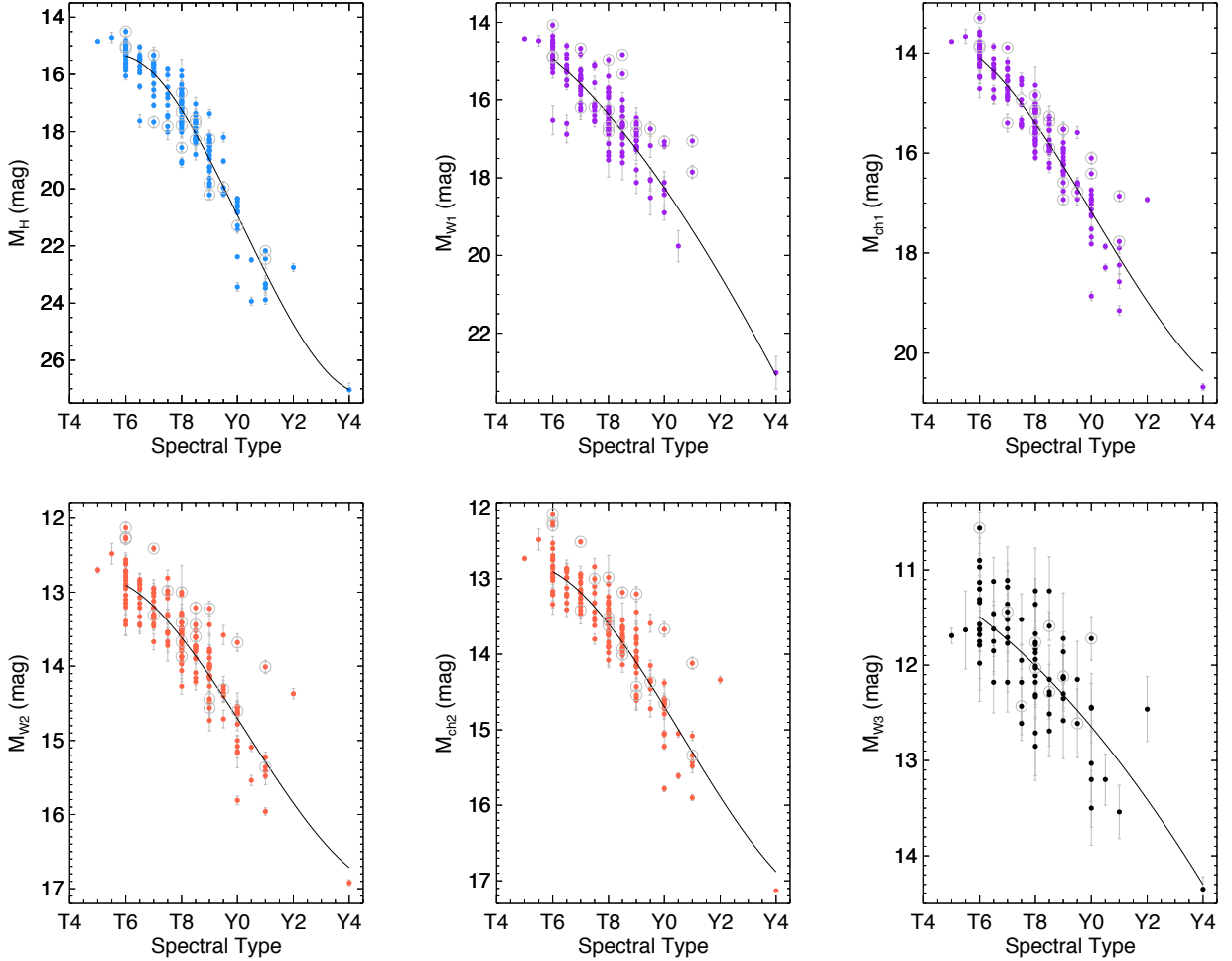
$H-W2$  color and  $M_H$ . Spectroscopically identified subdwarfs are circled in blue in the right-hand panels. The two highest  $v_{tan}$  values belong to the subdwarfs WISE 2005+5424 (110  $\text{km s}^{-1}$ ) and WISE 0833+0052 (102  $\text{km s}^{-1}$ ).

Objects appearing as outliers on any of these plots or having high reduced  $\chi^2$  values from our *Spitzer*-based astrometric fitting are discussed below.

## 8.2. Notes of Interest on Individual Objects within 20 pc

### 8.2.1. WISE 0146+4234AB

As noted by Dupuy et al. (2015), this is a tight binary of separation  $0.''0875 \pm 0.''0021$  with components believed to be of types T9 and Y0. The reduced  $\chi^2$  value of 1.579 for our *Spitzer* astrometric solution does not indicate any serious issue with the single-object fit despite the double nature of the system.

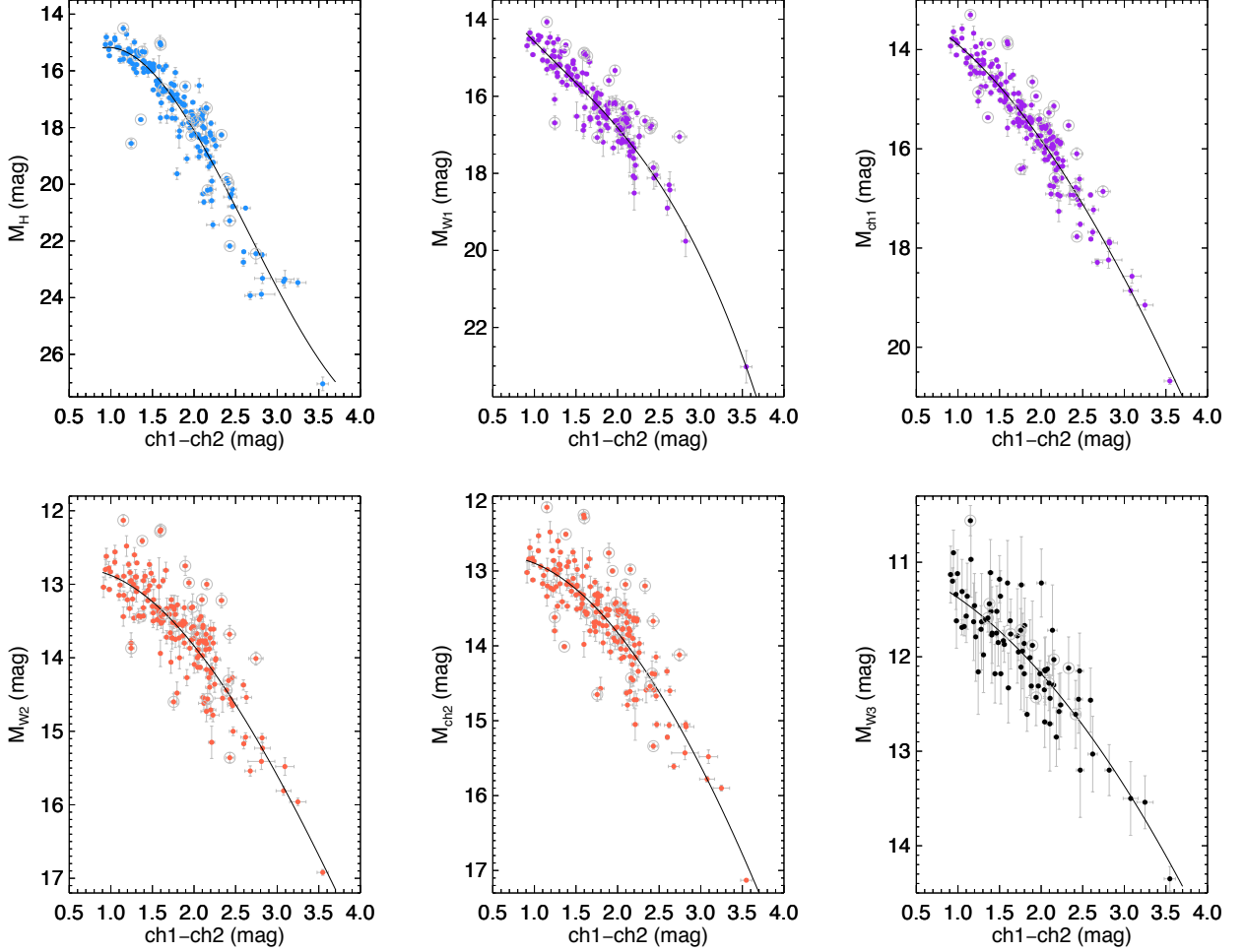


**Figure 5.** Trends of absolute magnitude with spectral type for all objects from Table 7 that fall within 20 pc of the Sun ( $\pi_{abs} \geq 50$  mas). The top row shows trends with absolute  $H$ -band magnitude (light blue) and the similar absolute W1 and ch1 magnitudes (purple). The bottom row shows trends with the similar absolute W2 and ch2 magnitudes (orange red) and the absolute W3 magnitude (black). Polynomial fits to the relations are shown by the black curves, and the functional forms are presented in Table 8. Points ignored by the fitting (see Section 8.3) are circled in gray.

### 8.2.2. WISE 0226–0211AB

This is a previously unreported common-proper-motion double with a separation of  $\sim 2''.1$  arcsec. This object has the worst reduced  $\chi^2$  value of any of our *Spitzer* targets (23.645) because the MOPEX/APEX software is unable to successfully centroid on either the A or the B component individually. Figure 10 shows the motion of the pair over a 6.6-yr baseline. This pair was observed with Keck/NIRC2 at  $J$  and  $H$  bands on dates 21 Sep 2013 and 22 Aug 2013 (UT), respectively, from which we measure PRF-fit magnitudes of  $J = 18.57 \pm 0.05$  and  $H = 18.88 \pm 0.10$  mag for the northern A component and  $J = 22.33 \pm 0.07$  and  $H = 22.33 \pm 0.12$  mag for the southern B component. Aperture photometry was measured on the first-epoch *Spitzer* AOR images (which had contemporaneous ch1 and ch2 images), and we obtained mea-

surements of ch1 =  $16.67 \pm 0.17$  and ch2 =  $14.86 \pm 0.05$  mag for A and ch1 =  $18.38 \pm 0.92$  and ch2 =  $15.59 \pm 0.08$  mag for B. The corresponding  $H$ –ch2 colors are  $4.02 \pm 0.11$  mag for A and  $6.74 \pm 0.14$  mag for B, suggesting types of  $\sim T8$ – $T8.5$  for A and  $\sim Y0$  for B (Figure 4). Using our measured parallax, which is somewhat suspect given our inability to properly centroid the pair, we find absolute magnitudes of  $M_H = 17.67$  and  $M_{ch2} = 13.65$  mag for A and  $M_H = 21.12$  and  $M_{ch2} = 14.38$  mag for B, suggesting types of  $\sim T8$ – $T8.5$  and  $\sim T9.5$ – $Y0$  for the two components (Figure 5), consistent with the type derived above from the measured colors. Despite the excellent agreement between the colors and the absolute magnitudes, the combined-light spectrum is that of a T7 dwarf (Kirkpatrick et al. 2011), when expectations would suggest a type closer to T8 or T9. This spectral type determination, based on a noisy  $H$ -band-only spectrum, should be



**Figure 6.** Trends of absolute magnitude with  $ch1-ch2$  color for all objects from Table 7 that fall within 20 pc of the Sun ( $\pi_{abs} \geq 50$  mas). The top row shows trends with absolute  $H$ -band magnitude (light blue) and the similar absolute W1 and  $ch1$  magnitudes (purple). The bottom row shows trends with the similar absolute W2 and  $ch2$  magnitudes (orange red) and the absolute W3 magnitude (black). Polynomial fits to the relations are shown by the black curves, and the functional forms are presented in Table 8. Points ignored by the fitting (see Section 8.3) are circled in gray.

revisited in light of the dual nature of the source. This source is the reddest T7 in  $H-W2$  color and is very faint in  $M_H$  for its spectral type despite being a binary, suggesting that the type itself is probably in error.

### 8.2.3. WISE 0254+0223

This T8 dwarf has a higher-than-average  $v_{tan}$  value of  $84.4 \pm 0.9$  km s $^{-1}$ , but it shows no oddities in the color and magnitude trends. High quality spectra from 0.8 to 2.5  $\mu$ m (Figure 22 of Kirkpatrick et al. 2011; Figure 3 of Liu et al. 2011) show it to be a normal T8 dwarf of presumably solar metallicity.

### 8.2.4. WISE 0304-2705

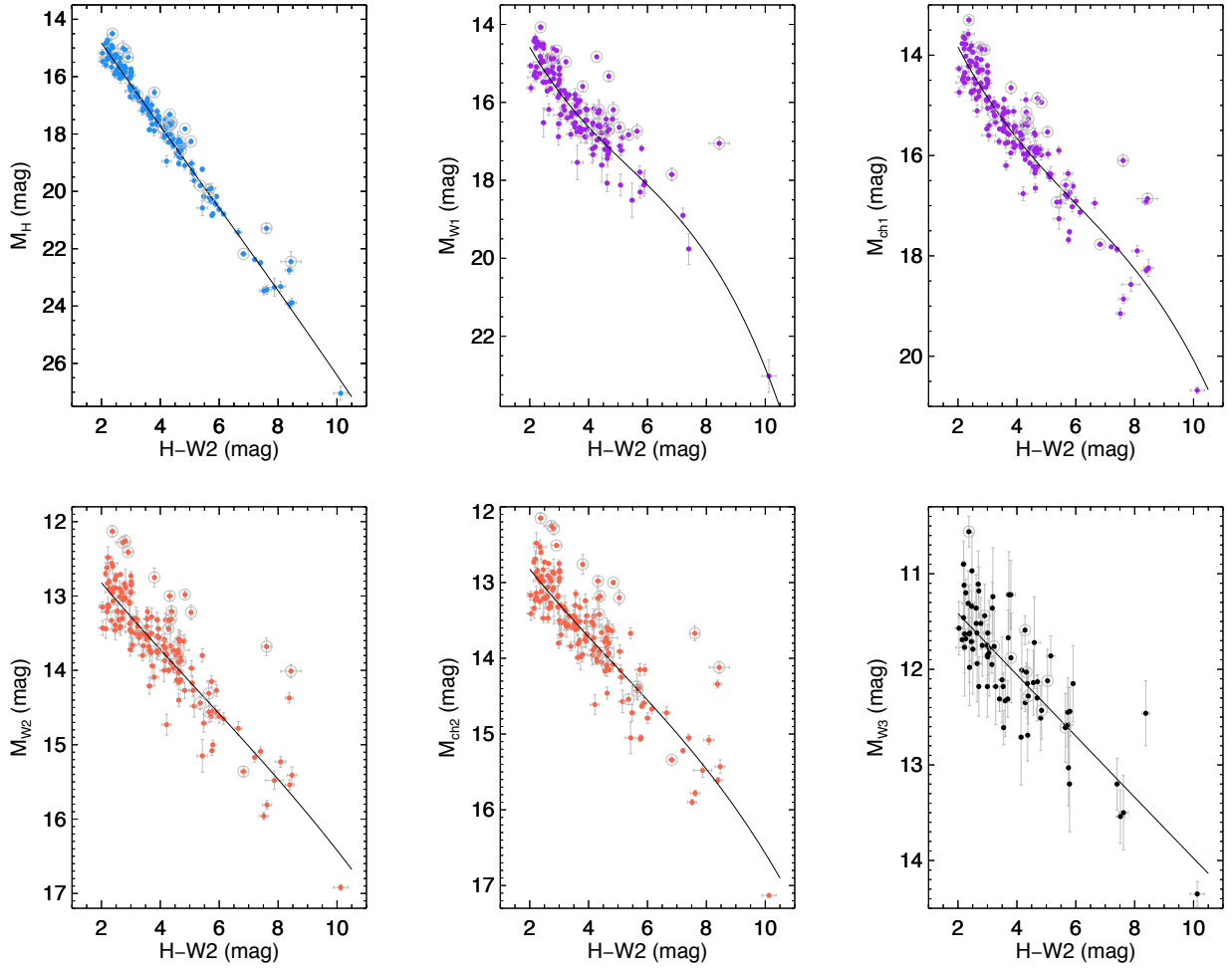
The *Spitzer* astrometric fit for this object has a reduced  $\chi^2$  value of 2.812. Additional observations of this object are

warranted, particularly since this is a peculiar Y0 dwarf. Pinfield et al. (2014) argued that the peculiar spectrum was most likely caused by an unusual metallicity and/or gravity. However, the fact that the object is too dim in  $M_H$  for its  $H-W2$  color (Figure 8) while other known subdwarfs do not share this effect may suggest that metallicity is not the sole cause. Continued astrometric monitoring is needed to determine if binarity may be complicating analysis, but in our subsequent analysis we consider this to be a single Y dwarf.

### 8.2.5. WISE 0309-5016

This source is much brighter in  $M_H$  than other objects of similar  $H-W2$  color, and also much brighter in  $M_{W1}$  and  $M_{ch1}$  than other objects of similar  $ch1-ch2$  color. This evidence points at WISE 0309-5016 being an unresolved double. There is no spectrum yet of this object, but methane





**Figure 7.** Trends of absolute magnitude with  $H-W2$  color for all objects from Table 7 that fall within 20 pc of the Sun ( $\pi_{abs} \geq 50$  mas). The top row shows trends with absolute  $H$ -band magnitude (light blue) and the similar absolute W1 and ch1 magnitudes (purple). The bottom row shows trends with the similar absolute W2 and ch2 magnitudes (orange red) and the absolute W3 magnitude (black). (Plots of absolute magnitude with  $H$ -ch2 color look virtually identical to the plots shown here.) Polynomial fits to the relations are shown by the black curves, and the functional forms are presented in Table 8. Points ignored by the fitting (see Section 8.3) are circled in gray.

on/off imaging suggests a spectral type of  $\sim T7$  (Tinney et al. 2018).

#### 8.2.6. WISE 0316+4307

In  $H-W2$  and  $H$ -ch2 colors, this is an abnormally red T8, and it is faint in  $M_H$  for its type. The spectral type is robust, since it is based on separate, high-quality spectra at  $J$  and  $H$  bands (Mace et al. 2013), so the reasons for these peculiarities are not known.

#### 8.2.7. WISE 0323-5907

This object is too faint in  $M_{W1}$  and  $M_{ch1}$  for its ch1-ch2 color. There is no spectrum yet of this object, but the ch1-ch2 color of  $1.244 \pm 0.034$  mag suggests a type of  $\sim T6$  (Figure 4), in agreement with the photometric type assigned

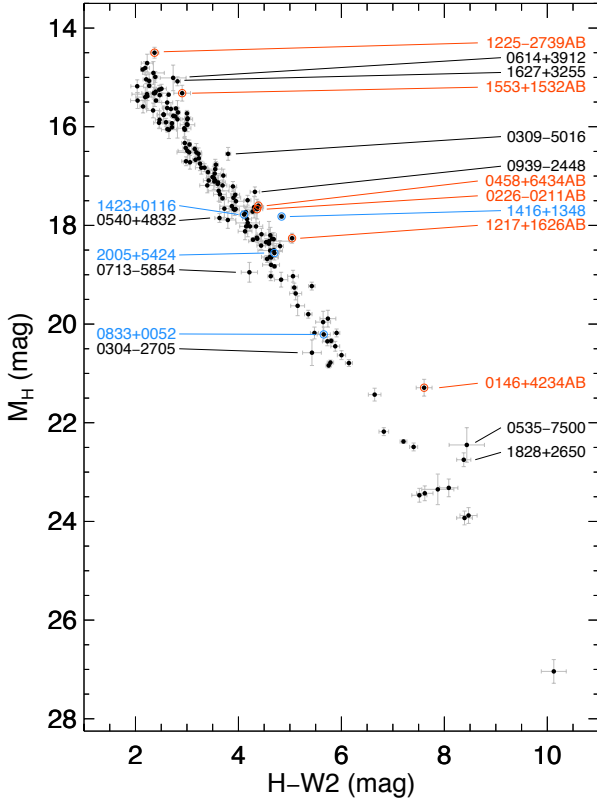
by Schneider et al. (2016) using 2MASS and AllWISE photometry.

#### 8.2.8. WISE 0335+4310

The poor reduced  $\chi^2$  value of 3.227 for this object's *Spitzer* astrometric fit is driven primarily by large residuals in the final year of data. For these later epochs, the T9 has moved within  $\sim 4''$  of a fainter background star that could possibly be complicating the astrometric measurement.

#### 8.2.9. WISE 0350-5658

This Y1 dwarf is too faint for its spectral type in both  $M_{W2}$  and  $M_{ch2}$ . It should be acknowledged, however, that there are very few Y dwarfs as late as this one, so judging observational trends at these late types is still difficult. Leggett et al. (2017) argue that this object's placement on the  $J$ -ch2



**Figure 8.** Trends of absolute  $H$ -band magnitude with  $H-W2$  color for all objects from Table 7 that fall within 20 pc of the Sun ( $\pi_{abs} \geq 50$  mas). Known binary systems are circled and labeled in red, and known subdwarfs are circled and labeled in blue. Other objects falling significantly above or below the mean trend are labeled in black.

vs.  $M_{ch2}$  diagram relative to model predictions suggest that it may be metal rich.

#### 8.2.10. *WISE 0359-5401*

This Y0 dwarf’s *Spitzer* astrometric fit has a reduced  $\chi^2$  value of 2.512, and our *Spitzer* images show no complications. [Opitz et al. \(2016\)](#) used adaptive optics imaging to rule out a binary nature for this object, but only for a companion of equal magnitude more distant than 1.9 AU from the primary. Given that this is one of the few Y dwarfs known, further astrometric monitoring might prove fruitful. Based on its location on the  $J$ -ch2 vs. ch1-ch2 plot and the trends shown by model atmosphere calculations, [Leggett et al. \(2017\)](#) argue that this object may be metal poor.

#### 8.2.11. *WISE 0430+4633*

In  $H-W2$  and  $H$ -ch2 colors, this is an abnormally red T8, and it is faint in  $M_H$  for its type. The spectral type is based on single  $J$ -band spectrum ([Mace et al. 2013](#)), but this type appears robust since these data have high S/N.

#### 8.2.12. *WISE 0458+6434AB*

Despite being a known binary with 0.5 separation ([Gelino et al. 2011](#)), this object has a *Spitzer* astrometric fit that is remarkably good. The reduced  $\chi^2$  value of 0.190 – the lowest of any of our targets – indicates either that our measurement uncertainties are inflated or that this is a statistical fluke. We note that this object is nonetheless clearly indicated as a binary because it is abnormally bright in  $M_{W1}$  and  $M_{ch1}$  for its ch1-ch2 color. Resolved spectroscopy of the two components gives spectral types of T8.5 and T9.5 ([Burgasser et al. 2012](#)).

#### 8.2.13. *UGPS 0521+3640*

This T8.5 dwarf appears as an outlier on a number of diagrams. It is unusually blue for a T8.5 in both  $W1-W2$  and ch1-ch2 color; it has a blue  $W1$ -ch1 color unlike that of most other late-T dwarfs and a  $W2$ -ch2 color significantly off zero; and it appears as an outlier on various absolute magnitude vs. color diagrams. As noted Table 2, the  $W1$  photometry for this source is contaminated by the halo of a much brighter star. Moreover, the only extant *Spitzer* imaging comes from the shallow GLIMPSE survey (program 61070; PI: B. Whitney). This object is located at a Galactic latitude of only  $b = -0.04$  deg, so source confusion in the Galactic Plane is likely an issue in bands other than just  $W1$ .

#### 8.2.14. *WISE 0535-7500*

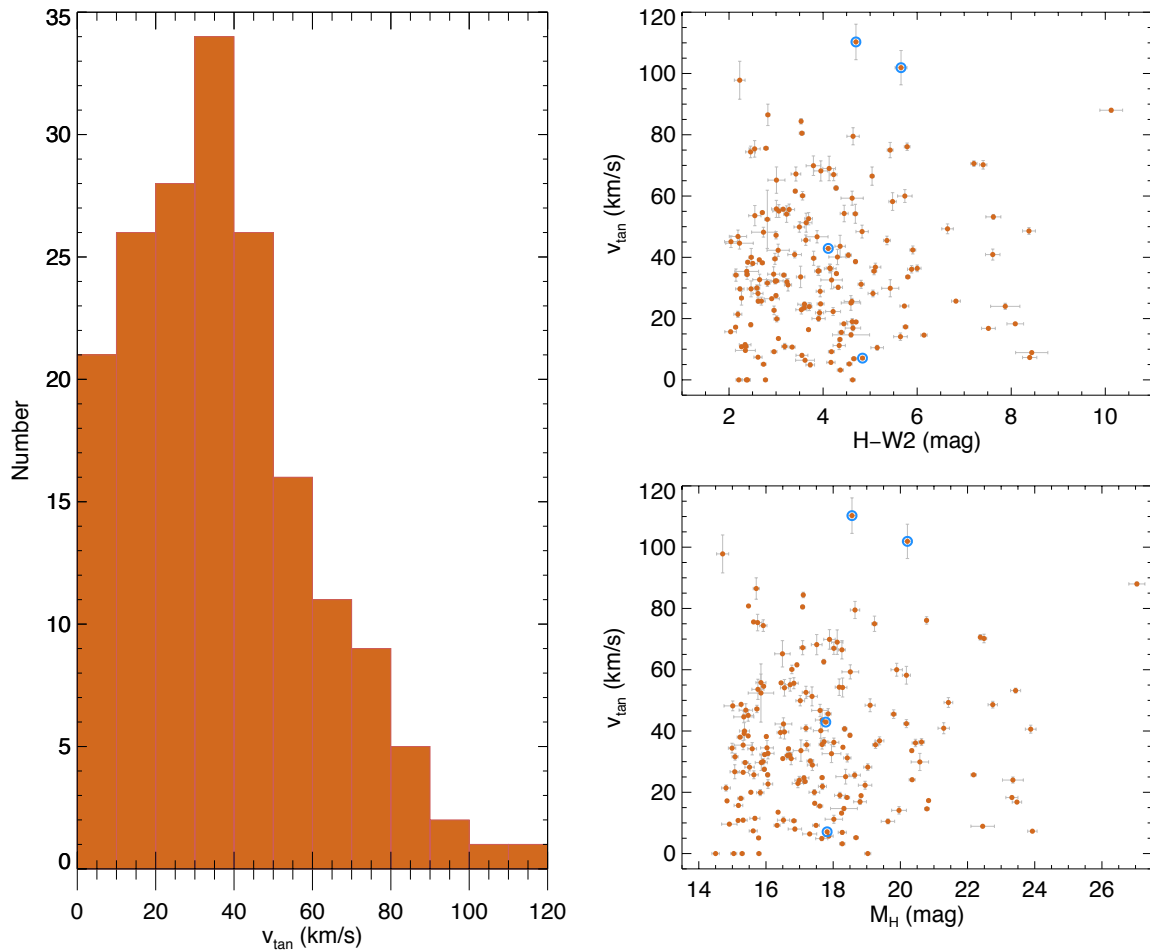
This  $\geq Y1$ : dwarf may be abnormally bright in  $M_H$ ,  $M_{W1}$ , and  $M_{W2}$  for its spectral type and  $H-W2$  and ch1-ch2 colors. However, there are very few Y dwarfs known that are as late as this one, so judging observational trends is still difficult. The overluminosity may indicate an unresolved double, as was pointed out by [Tinney et al. \(2014\)](#). [Opitz et al. \(2016\)](#) used high-resolution adaptive optics imaging in the near-infrared to rule out an equal-magnitude binary with a separation  $> 1.9$  AU. This source is located in a dense field at the outskirts of the Large Magellanic Cloud, so contamination of some of the filter measurements is a possibility. The small motion of this source ( $125.2 \pm 1.6$  mas yr $^{-1}$ ) means that the object has not yet moved significantly since its discovery to reveal whether a background source may have complicated earlier photometry. [Leggett et al. \(2017\)](#) favor the binary hypothesis, although [Tinney et al. \(2014\)](#) suggests that an unusual atmosphere with thick clouds might provide an alternative explanation.

#### 8.2.15. *WISE 0540+4832*

This T8.5 dwarf is abnormally dim in  $M_H$  for its  $H-W2$  color. The spectral type is based on a  $J$ -band spectrum from [Mace et al. \(2013\)](#), but it has high S/N. The reason for this peculiarity is unknown.

#### 8.2.16. *WISE 0614+3912*

This T6 dwarf shows overluminosity in  $M_H$ ,  $M_{W1}$ ,  $M_{ch1}$ ,  $M_{W2}$ , and  $M_{ch2}$  for its spectral type and  $H-W2$  and ch1-ch2 colors. In particular, see Figure 8. In subsequent analyses, we consider this to be an unresolved binary.



**Figure 9.** Distributions in number, color, and absolute magnitude for our tangential velocity measurements for objects in Table 7 that fall within 20 pc of the Sun ( $\pi_{abs} \geq 50$  mas). On the left is the histogram of the  $v_{tan}$  values. At upper right is the distribution with respect to  $H-W2$  color, and at bottom right is the distribution with respect to  $M_H$ . In these rightmost panels, spectroscopically identified subdwarfs (WISE 0833+0052, ULAS 1416+1348, Gl 547B, and WISE 2005+5424) are circled in blue.

#### 8.2.17. WISE 0647–6232

The *Spitzer* astrometric fit for this Y1 dwarf has a reduced  $\chi^2$  value of 2.309. Given that this is one of the coolest Y dwarfs currently known, continued astrometric monitoring would be instructive.

#### 8.2.18. WISE 0713–5854

This T9 dwarf is abnormally dim in  $M_H$  for its  $H-W2$  color. The spectral type is based on a high-quality 0.95–1.65  $\mu\text{m}$  spectrum from Tinney et al. (2018) and shows no peculiarities with respect to a standard T9 spectrum. The reason for this underluminosity is unknown.

#### 8.2.19. WISE 0723+3403

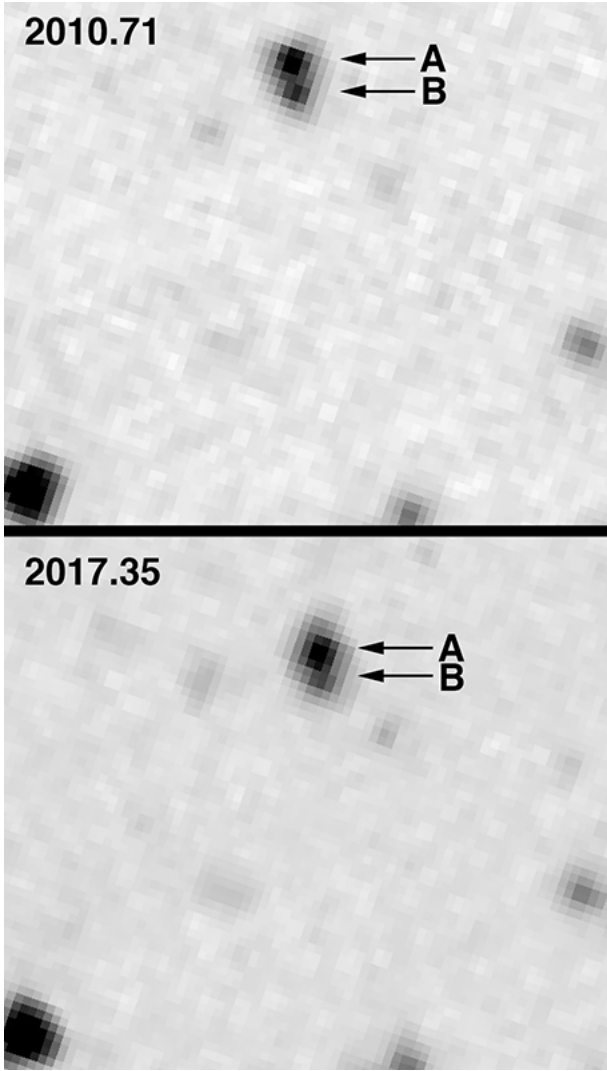
Very little follow-up has been done on this T9: dwarf, whose plot of the *Spitzer* astrometric fit residuals (Figure 2)

and reduced  $\chi^2$  value of 2.204 may be suggestive of a companion. The possible cyclical variation in the residuals is, however, based on only nine data points. We note, however, that there is other evidence for binarity given its overluminosity in  $M_H$  for its spectral type.

#### 8.2.20. WISE 0734–7157

This Y0 dwarf has a *Spitzer* astrometric fit with a reduced  $\chi^2$  value of 3.049. As pointed out by Martin et al. (2018), this is likely one of the warmest Y0 dwarfs known, based on colors and its absolute  $J$ -band magnitude. Even though *HST*/WFC2 images at F105W and F125W show no evidence for binarity (Schneider et al. 2015), more detailed analysis into the possibility of its being a tighter double is warranted.

#### 8.2.21. WISE 0751–7634



**Figure 10.** A  $33'' \times 38''$  section of the IRAC ch2 mosaics from AOR 40824064 (epoch 2010.71, top) and 61480192 (epoch 2017.35, bottom) illustrating the common proper motion and binary nature of the WISE 0226–0211AB system

This T9 dwarf is underluminous in  $M_H$ ,  $M_{W1}$ , and  $M_{ch1}$  for its ch1–ch2 color. Another object that shows this same behavior is the sdT8 WISE 2005+5424, which might indicate that WISE 0751–7634 is also metal poor. On the other hand, the three other T subdwarfs in the 20-pc sample do not share these traits. Leggett et al. (2017) also argue that a metal poor explanation would better explain this object’s location on the  $J$ –ch2 vs. ch1–ch2 diagram based on atmospheric model trends.

#### 8.2.22. WD 0806–661B

This object is a very cold companion to a white dwarf, and its spectral type is currently an educated guess. This object is sufficiently faint ( $H = 25.29 \pm 0.14$  mag) that no spectrum has yet been acquired. Leggett et al. (2017) argue that the

object may be metal poor based on its location on the  $J$ –ch2 vs. ch1–ch2 diagram.

#### 8.2.23. WISE 0811–8051

This T9.5: dwarf is one of the objects with a strangely blue W1–ch1 color, which is almost certainly indicative of a corrupted measurement, most likely through contamination by a background source in W1. The object, however, does not distinguish itself as an outlier on any other plots.

#### 8.2.24. WISE 0825+2805

This Y0.5 dwarf may be underluminous in  $M_H$  for its spectral type, but there are very few known Y dwarfs with types this late, so accurately gauging trends is difficult.

#### 8.2.25. WISE 0833+0052

This is an (sd)T9 with a high  $v_{tan}$  value of  $101.9 \pm 5.6$  km  $s^{-1}$ . It does not appear as an outlier on any of our color or absolute magnitude plots.

#### 8.2.26. WISE 0855–0714

This, the least luminous brown dwarf known, has a relatively high tangential velocity of  $88.0 \pm 0.6$  km  $s^{-1}$ . The only extant spectra of this object are low-resolution data at  $L$  and  $M$  bands from Skemer et al. (2016) and Morley et al. (2018). Fits to model atmospheres by Morley et al. (2018) indicate that the object may have slightly subsolar abundance.

#### 8.2.27. 2MASS 0939–2448

Our analysis indicates that this T8 dwarf is overluminous in  $M_H$  for its  $H$ –W2 color (Figure 8) and overluminous in  $M_{W1}$  and  $M_{ch1}$  for its ch1–ch2 color. This has been a suspected binary for a decade: Burgasser et al. (2008) noted its overluminosity early and favored a binary hypothesis and slightly subsolar metallicity, and Leggett et al. (2009) reached the same conclusion in analyzing the same data set. Line et al. (2017) note that the object appears to be single in the near-infrared with adaptive optics imaging, and their own analysis reaches the same conclusion of binarity and slightly subsolar abundance. For subsequent analyses, we consider this object to be an unresolved double.

#### 8.2.28. 2MASS 1047+2124

This T6.5 has a higher-than-average  $v_{tan}$  value of  $86.5 \pm 3.5$  km  $s^{-1}$ , but it appears to be a normal, solar metallicity T dwarf (Burgasser et al. 2002). Its claim to fame is that it is the first T dwarf with detected bursts in the radio (Williams & Berger 2015 and references therein).

#### 8.2.29. WISE 1050+5056

The reduced  $\chi^2$  value for this object’s *Spitzer* astrometric fit is 2.940, but this is based on only seven epochs of information. Additional astrometric measurements of this object are needed not only to further study the residuals but also to determine whether or not this object falls inside of or outside of the 20-pc sample, as our current fit gives  $\pi_{abs} = 49.7 \pm 5.0$  mas. For subsequent analyses, this object is assumed to fall beyond 20 pc.

8.2.30. *2MASS 1114–2618*

This T7.5 dwarf has a relatively high  $v_{tan}$  value of  $86.5 \pm 3.5$  km s<sup>-1</sup>. Both [Burgasser et al. \(2006\)](#) and [Leggett et al. \(2007\)](#) agree that this object’s near-infrared spectrum is best explained by slightly subsolar metallicity ( $[M/H] \approx -0.3$ ).

8.2.31. *WISE 1141–3326*

This Y0 dwarf is anomalously blue in ch1–ch2 color for its type, and has a W2–ch2 color that’s distinctly non-zero. Moreover, it is anomalously blue in W1–ch2 color, is too bright in  $M_{W1}$  for its  $H$ –W2 color, is too faint in both  $M_{W2}$  and  $M_{ch2}$  for its ch1–ch2 color, and is an outlier on the  $M_H$  vs. ch1–ch2 diagram. It is quite likely that most, if not all, of these anomalies can be attributed to confusion at early epochs by a background galaxy (see Figure 2 of [Tinney et al. 2018](#)). A new round of photometry, now that the Y dwarf has moved clear of the background source, would be informative.

8.2.32. *ULAS 1152+1134*

The fit to this object’s *Spitzer* astrometry has a reduced  $\chi^2$  value of 2.551, but this is based on only six data points. Additional astrometric measurements of this object are needed not only to further study the residuals but also to determine whether or not this object falls within the 20-pc sample. Our current fit gives  $\pi_{abs} = 49.7 \pm 5.1$  mas. For subsequent analyses, this object is assumed to fall beyond 20 pc.

8.2.33. *WISE 1217+1626AB*

This T9 dwarf is overluminous in  $M_{W1}$  and  $M_{ch1}$  for its ch1–ch2 color and clearly sits above the standard sequence in the  $M_H$  vs.  $H$ –W2 plot (Figure 8). This object was found to be a 0<sup>h</sup>8 binary with component spectral types of T9 and Y0 by [Liu et al. \(2012\)](#). Our *Spitzer* astrometric fit for this object has a reduced  $\chi^2$  value of 5.776, which also strongly hints at its binary nature.

8.2.34. *2MASS 1225–2739*

This T6 dwarf is overluminous in all measured bands for its spectral type and colors. [Burgasser et al. \(2003\)](#) showed that the source was a binary with separation of 0<sup>h</sup>28 on *HST*/WFPC2 images at F814W and F1042M. Using the parallax of the system and photometry from the *HST* images, [Vrba et al. \(2004\)](#) estimate spectral types of T6: and T8: for the pair. This was later revised with additional photometric data to T5.5 and T8 by [Dupuy & Liu \(2012\)](#).

8.2.35. *2MASS 1231+0847*

This T5.5 dwarf has a relatively high  $V_{tan}$  value of  $97.8 \pm 6.3$  km s<sup>-1</sup>. [Burgasser et al. \(2004\)](#) noted that this object has broad K I lines, indicating that it is either rapidly rotating or has a higher photospheric pressure, the latter of which could point to a higher surface gravity that is the consequence of somewhat subsolar metallicity. However, this object, which was originally given a spectral type of T6 by

[Burgasser et al. \(2004\)](#), was revised to T5.5 by [Burgasser et al. \(2006\)](#) and thus falls outside of the spectral type sample we consider in further analyses.

8.2.36. *WISE 1322–2340*

This is an abnormally blue T8 in both  $H$ –W2 and  $H$ –ch2 color, but it is not noted as peculiar on any other plots. [Gelino et al. \(2011\)](#) did not find any evidence for binarity using adaptive optics near-infrared imaging, ruling out any companions with  $\Delta H < 4$  mag outside of 0<sup>h</sup>2. No peculiarities were noted in the 0.8–2.5  $\mu$ m spectrum by [Kirkpatrick et al. \(2011\)](#).

8.2.37. *WISE 1405+5534*

This object is an outlier in  $M_{W1}$  for its type, but it is known to have an unusual spectrum for an early-Y dwarf. Its  $H$ -band emission peak is shifted to longer wavelengths by  $\sim 60\text{\AA}$  relative to other late-T and early-Y dwarfs ([Cushing et al. 2011](#)).

8.2.38. *ULAS 1416+1348*

This is the reddest T7.5 dwarf in  $H$ –W2 and  $H$ –ch2 color. It is also overluminous in  $M_{W1}$  and  $M_{ch1}$  for its ch1–ch2 color and in  $M_H$  for its  $H$ –W2 color. This object is a common-proper-motion companion to SDSS J141624.08+134826.7, which is often regarded as an sdL7 or d/sdL7 ([Kirkpatrick et al. 2011](#), [Burningham et al. 2010](#)). ULAS 1416+1348 has somewhat conflicting spectral types of T7.5 (blue), T7.5 pec, and sdT7.5 ([Burgasser et al. 2010](#), [Burningham et al. 2010](#), [Kirkpatrick et al. 2011](#)), all of which highlight its unusual spectrum. Given that its peculiarities and those of its primary are often attributed to subsolar metallicity, a designation of sdT7.5 seems appropriate. Whereas the three other late-T subdwarfs known (WISE 0833+0052, Gl 547B, and WISE 2005+5424) show no overluminosity relative to normal dwarfs, ULAS 1416+1348 very clearly does. We therefore conclude that this object is a close, unresolved double and consider it as such in subsequent analyses.

8.2.39. *WISE 1501–4004*

The *Spitzer* astrometric fit for this T6 dwarf has a reduced  $\chi^2$  value of 2.493, but that is based on only seven epochs of data. Continued monitoring is indicated to see if this may indicate the presence of a lower-mass companion. The object does not, however, appear as an outlier in any of our color/magnitude/type plots.

8.2.40. *WISE 1523+3125*

This T6.5pec dwarf is the reddest T6.5 in  $H$ –W2 and  $H$ –ch2 colors. It is also underluminous in  $M_H$  for its spectral type. [Mace et al. \(2013\)](#) showed that the  $J$ -band flux best matched that of a T7 standard whereas the  $H$ -band flux best matched that of a T6 standard, which is similar to the spectral behavior of 2MASS 0937+2931, which may be slightly metal poor itself ([Burgasser et al. 2002](#)). However, this same spectral behavior is not seen in the true T subdwarfs such as Gl 547B, and 2MASS 0937+2931 does not stand out as an



outlier on any of our plots. The cause for the peculiar spectra and photometry of WISE 1523+3125 is unknown.

#### 8.2.41. WISE 1541–2250

This Y1 dwarf is another of the objects with a strangely blue W1–ch1 color. This is almost certainly due to an erroneous W1 measurement (see discussion in Kirkpatrick et al. 2012) caused by its passage near a brighter background source.

#### 8.2.42. WISE 1542+2230

The reduced  $\chi^2$  value for this T9.5 object’s *Spitzer* astrometric fit is 2.181. The only high-resolution imaging reported for this object is from *HST*/WFC2 by Schneider et al. (2015) at F105W, F125W, and F140W. No evidence of a companion is seen. Continued monitoring is again indicated.

#### 8.2.43. 2MASS 1553+1532

This T7 dwarf is overluminous in  $M_{W2}$  and  $M_{ch2}$  for its spectral type. This object was confirmed as a close binary by Burgasser et al. (2002) using *HST*/NICMOS imaging. Using available photometry and combined-light spectroscopy, Dupuy & Liu (2012) estimate spectral types for the individual components of T6.5 and T7.5.

#### 8.2.44. WISE 1627+3255

This T6 dwarf is consistently overluminous in all bands for its colors. It is a dramatic outlier, for example, on the  $M_H$  vs.  $H$ –W2 plot of Figure 8. Gelino et al. (2011) found no evidence for a companion down to  $\Delta H \approx 5$  mag for separations larger than  $0''.2$ . Because of the strong evidence favoring binarity, we consider this object to be a tight, unresolved double in subsequent analyses.

#### 8.2.45. WISE 1804+3117

This T9.5: dwarf is overluminous in  $M_H$ ,  $M_{W2}$ , and  $M_{ch2}$  for its spectral type. Because the type is uncertain, this discrepancy would disappear if a slightly earlier spectral type were indicated. We note that the object is not overluminous on the absolute magnitude vs. color plots, so we will assume this object is single for subsequent analyses.

#### 8.2.46. WISE 1813+2835

This T8 is unusually blue in both W1–W2 and W1–ch1 color. This may simply indicate that the W1 measurement from WISE is contaminated (made too bright) by a background object. Mace et al. (2013) do not note anything peculiar about the spectrum.

#### 8.2.47. WISE 1828+2650

This  $\geq Y2$  dwarf is overluminous for its spectral type in  $M_{W2}$  and  $M_{ch2}$  and is also overluminous in  $M_H$  for its  $H$ –W2 color (Figure 8). On the  $M_{W2}$  vs.  $H$ –W2 plot, it falls  $\sim 1$  mag above the trend, and in the  $M_{ch1}$  vs.  $H$ –W2 plot, it falls at least 1 mag above the trend. However, WISE

1828+2650 falls in line with other Y dwarfs on the plot of  $M_H$  vs. ch1–ch2. This Y dwarf has been an object of much speculation since its broad-band colors cannot be fit by any of the current suite of models (e.g., Beichman et al. 2013). Leggett et al. (2017) speculate that the object may be an equal-magnitude binary (which explains only 0.75 mag worth of overluminosity) as well as having a subsolar metallicity ( $[M/H] \approx -0.5$ ), the latter based on model atmosphere trends seen in the  $M_{ch2}$  vs.  $J$ –ch2 diagram. Inexplicably, though, their best fitting atmospheric model suggests a young system ( $\sim 1.5$  Gyr). Such a young age is hard to reconcile with the subsolar metallicity, so the more likely explanation is that the current suite of atmospheric models simply fails to contain the physics necessary to explain this object’s near-infrared spectrum and broadband colors.

#### 8.2.48. WISE 1928+2356

This T6 dwarf lies near the Galactic Plane at  $l = 58.3$  deg and  $b = +3.1$  deg, and our *Spitzer* astrometric fit has a reduced  $\chi^2$  value of 2.347. The motion over our 5.2 yr of *Spitzer* observations shows that there are no background sources that might be confusing the astrometric measurements. Continued monitoring is suggested to test for the presence of an unseen companion.

#### 8.2.49. WISE 2005+5424

This object has a relatively high  $v_{tan}$  value of  $110.3 \pm 5.8$  km  $s^{-1}$ , and appears as an outlier on some of our other plots. This is a known sdT8 (Mace et al. 2013) and is a distant, common-proper-motion companion to the Wolf 1130 (Gl 781) system.

#### 8.2.50. ULAS 2146–0010

This object is also known as Wolf 940B, so the near-solar metallicity of the primary star can be assumed to apply to the companion as well (Bunningham et al. 2009, Leggett et al. 2010). Surprisingly, this T8 dwarf is an outlier on many of our plots. Because of the high proper motion of this late-T dwarf, we now know that during the time of its *Spitzer*/IRAC observations in 2008 (see the *Spitzer* Heritage Archive), it was contaminated by a background object now clearly visible in later NEOWISE images at these same wavelengths (see NEOWISE data at IRSA). Thus, we conclude that the odd placement of this object on many of our diagrams is simply due to contaminated measurements.

#### 8.2.51. WISE 2209+2711

This is the faintest Y0 dwarf in  $M_H$ ,  $M_{ch1}$ ,  $M_{ch2}$ , and  $M_{W2}$ . Its spectral type is uncertain, though. Schneider et al. (2015) suggests that the noisy *HST*/WFC3 spectrum on which the type is based may be, despite its poor signal, hinting at sharper  $Y$ -,  $J$ -, and  $H$ -band peaks that point to a type closer to Y1. A later spectral type would solve the discrepancy.

#### 8.2.52. WISE 2212–6931

The reduced  $\chi^2$  value for the *Spitzer* astrometric fit of this T9 dwarf is 2.422. High-resolution *HST*/WFC3 imaging at F105W and F125W by [Schneider et al. \(2015\)](#) shows no evidence of binarity. However, this object also shows an abnormally blue W1–ch1 color. This suggests possible contamination by a background object in the W1 photometry, which later NEOWISE imaging strongly suggests. This contamination at W1 should not, however, effect the ch2 astrometry, so continued monitoring is still warranted.

### 8.2.53. WISE 2226+0440

This T8 is abnormally blue in  $H$ -W2 and  $H$ -ch2 color and overluminous in  $M_H$  for its type. It does not, however, appear overluminous in  $M_H$  for its  $H$ -W2 color. We consider this to be a single object. The USNO measurement of the parallax is  $49.13 \pm 8.85$  mas, and it is removed from subsequent analyses since it is considered to be more distant than 20 pc.

### 8.2.54. WISE 2344+1034

The reduced  $\chi^2$  value for this T9 dwarf's *Spitzer* astrometric fit is 3.157. No high-resolution imaging has been published for this source. Astrometric monitoring will continue

in an attempt to determine whether the poor fit is due to an unseen companion.

### 8.3. Fits to the Trends

With the examination of the outliers complete, we fit polynomial relations to trends seen in Figures 4, 5, 6, and 7. Removed from consideration from the fits, and shown by the circled points in each of the four figures, are known binaries (WISE 0146+4324AB, WISE 0226–0211AB, WISE 0458+6434AB, WISE 1217+1626AB, 2MASS 1225–2739AB, and 2MASS 1553+1532AB), objects with strong indication of binarity even if this is not yet proven (WISE 0309–5016, WISE 0614+3912, 2MASS 0939–2448, ULAS 1416+1348, and WISE 1627+3255), subdwarfs (WISE 0833+0052, Gl 547B, and WISE 2005+5424), and objects proven to have poor photometry in any band (UGPS 0521+3640, WISE 0535–7500, WISE 0811–8051, WISE 1141–3326, WISE 1541–2250, WISE 1813+2835, ULAS 2146–0010, WISE 2212–6931). The coefficients for the resulting fitted polynomials are given in Table 8.

**Table 8.** Coefficients for the Fitted Relations in Figures 4, 5, 6, 7, and 14

$x$	$y$	$c_0$	$c_1$	$c_2$	$c_3$	Valid Range	Fig. No.
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
SpT	H–W2	$19.7444 \pm 3.43923$	$-6.76528 \pm 1.18653$	$0.806149 \pm 0.132423$	$-0.0264937 \pm 0.00477809$	$6 \leq \text{SpT} \leq 14$	4
SpT	W1–W2	$-1.29441 \pm 3.12275$	$0.812400 \pm 1.08525$	$-0.0609403 \pm 0.121097$	$0.00290939 \pm 0.00431632$	$6 \leq \text{SpT} \leq 14$	4
SpT	H–ch	$21.3744 \pm 3.46898$	$-7.36894 \pm 1.19729$	$0.876955 \pm 0.133654$	$-0.0291438 \pm 0.00482272$	$6 \leq \text{SpT} \leq 14$	4
SpT	ch1–ch2	$0.769877 \pm 1.27185$	$-0.229115 \pm 0.438774$	$0.0645336 \pm 0.0489775$	$-0.00245289 \pm 0.00176859$	$6 \leq \text{SpT} \leq 14$	4
SpT	$M_H$	$36.9823 \pm 4.52559$	$-8.67412 \pm 1.56407$	$1.05192 \pm 0.174819$	$-0.0345062 \pm 0.00631589$	$6 \leq \text{SpT} \leq 14$	5
SpT	$M_{W1}$	$13.8233 \pm 4.02261$	$-0.280335 \pm 1.39798$	$0.0849970 \pm 0.155993$	$-0.00126205 \pm 0.00556011$	$6 \leq \text{SpT} \leq 14$	5
SpT	$M_{ch1}$	$17.0846 \pm 2.63109$	$-1.78683 \pm 0.907701$	$0.267542 \pm 0.101321$	$-0.00879858 \pm 0.00365872$	$6 \leq \text{SpT} \leq 14$	5
SpT	$M_{W2}$	$16.3566 \pm 1.97250$	$-1.59982 \pm 0.680223$	$0.211779 \pm 0.0759126$	$-0.00683350 \pm 0.00274110$	$6 \leq \text{SpT} \leq 14$	5
SpT	$M_{ch2}$	$16.3313 \pm 1.90378$	$-1.56291 \pm 0.656784$	$0.203565 \pm 0.0733125$	$-0.00636583 \pm 0.00264733$	$6 \leq \text{SpT} \leq 14$	5
SpT	$M_{W3}$	$10.7028 \pm 0.855644$	$0.0373974 \pm 0.201161$	$0.0156912 \pm 0.0115047$	...	$6 \leq \text{SpT} \leq 14$	5
ch1–ch2	$M_H$	$18.9265 \pm 1.86956$	$-8.42821 \pm 2.95676$	$5.35110 \pm 1.47305$	$-0.671764 \pm 0.231385$	$0.9 \leq \text{ch1–ch2} \leq 3.7$	6
ch1–ch2	$M_{W1}$	$11.9474 \pm 1.04382$	$3.34232 \pm 1.67324$	$-0.961963 \pm 0.840256$	$0.253873 \pm 0.132210$	$0.9 \leq \text{ch1–ch2} \leq 3.7$	6
ch1–ch2	$M_{ch1}$	$12.9955 \pm 0.774422$	$0.338479 \pm 1.23058$	$0.589613 \pm 0.615497$	$-0.0261095 \pm 0.0971189$	$0.9 \leq \text{ch1–ch2} \leq 3.7$	6
ch1–ch2	$M_{W2}$	$13.0317 \pm 0.771663$	$-0.810665 \pm 1.22622$	$0.708750 \pm 0.613162$	$-0.0509940 \pm 0.0967195$	$0.9 \leq \text{ch1–ch2} \leq 3.7$	6
ch1–ch2	$M_{ch2}$	$12.9798 \pm 0.773265$	$-0.636228 \pm 1.22874$	$0.577744 \pm 0.614577$	$-0.0244403 \pm 0.0969738$	$0.9 \leq \text{ch1–ch2} \leq 3.7$	6
ch1–ch2	$M_{W3}$	$10.9597 \pm 0.332495$	$0.222754 \pm 0.352291$	$0.193301 \pm 0.0874473$	...	$0.9 \leq \text{ch1–ch2} \leq 3.7$	6
H–W2	$M_H$	$11.8395 \pm 0.422339$	$1.52105 \pm 0.276539$	$-0.0169462 \pm 0.0553281$	$0.00105926 \pm 0.00337858$	$2.0 \leq \text{H–W2} \leq 10.5$	7
H–W2	$M_{W1}$	$11.1176 \pm 0.735170$	$2.22837 \pm 0.494409$	$-0.283438 \pm 0.100149$	$0.0177630 \pm 0.00597848$	$2.0 \leq \text{H–W2} \leq 10.5$	7
H–W2	$M_{ch1}$	$10.9971 \pm 0.551329$	$1.76116 \pm 0.361104$	$-0.191714 \pm 0.0722079$	$0.0106388 \pm 0.00440667$	$2.0 \leq \text{H–W2} \leq 10.5$	7
H–W2	$M_{W2}$	$11.8351 \pm 0.422522$	$0.524627 \pm 0.276660$	$-0.0178469 \pm 0.0553522$	$0.00112382 \pm 0.00338004$	$2.0 \leq \text{H–W2} \leq 10.5$	7
H–W2	$M_{ch2}$	$11.7379 \pm 0.424309$	$0.611981 \pm 0.277910$	$-0.0402293 \pm 0.0555720$	$0.00274103 \pm 0.00339142$	$2.0 \leq \text{H–W2} \leq 10.5$	7

Table 8 continued



Table 8 (continued)

$x$	$y$	$c_0$	$c_1$	$c_2$	$c_3$	Valid Range	Fig. No.
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
H–W2	$M_{W3}$	$10.7731 \pm 0.275922$	$0.321823 \pm 0.122970$	$-0.000147914 \pm 0.0117518$	...	$2.0 \leq \text{H–W2} \leq 10.5$	7
	$M_H$	$11610.9 \pm 1165.61$	$-1424.48 \pm 177.512$	$61.2423 \pm 8.88772$	$-0.892386 \pm 0.146389$	$14.5 \leq M_H \leq 27.0$	14
	$M_{W2}$	$40669.7 \pm 16715.8$	$-7272.51 \pm 3476.93$	$440.398 \pm 240.300$	$-8.96515 \pm 5.51811$	$12.5 \leq M_{W2} \leq 17.0$	14
	$M_{ch2}$	$35476.5 \pm 15647.4$	$-6198.65 \pm 3231.62$	$366.839 \pm 221.694$	$-7.29548 \pm 5.05173$	$12.5 \leq M_{ch2} \leq 17.2$	14
H–W2	$T_{\text{eff}}$	$1821.84 \pm 109.420$	$-490.635 \pm 68.2886$	$59.1937 \pm 12.9725$	$-2.55531 \pm 0.760092$	$2.0 \leq \text{H–W2} \leq 10.5$	14
	SpT	$2335.64 \pm 139.416$	$-286.401 \pm 31.8992$	$9.89240 \pm 1.78104$	...	$6 \leq \text{SpT} \leq 14$	14
	ch1–ch2	$1603.55 \pm 94.2015$	$-658.290 \pm 94.2278$	$79.4503 \pm 22.5429$	...	$0.9 \leq \text{ch–ch2} \leq 3.6$	14

NOTE—These are simple polynomial equations of the form

$$y = \sum_{i=0}^n c_i x^i.$$

For spectral types, SpT = 6 for T6, SpT = 7 for T7,... SpT = 14 for Y4.

## 9. ANALYSIS OF THE UNDERLYING MASS FUNCTION

### 9.1. Transforming from the Theoretical to the Observational Plane

Determining the form of the stellar mass function enlightens us about the physical mechanisms underlying star formation and the creation efficiency for objects of all masses. For hydrogen-burning stars in a well-defined observational sample, this is a relatively straightforward measurement: the spectral type or broadband color of each star determines its location on the HR diagram’s main sequence, which in turn determines its mass.

The lowest mass end of the mass function, which is comprised solely of brown dwarfs, is, however, much more difficult to measure. Unlike stars, brown dwarfs lack a simple relationship between spectral type/color and mass because they never settle onto a main sequence. Instead, they cool constantly with time, so mass cannot be deduced without some determination of the age, which is a notoriously difficult measurement for field objects.

For brown dwarfs, an alternate method is to assume various functional forms of the mass function and to draw objects from those distributions according to an assumed rate of star formation. Using an assigned birth time, each brown dwarf is allowed to cool to the present time as predicted from an assumed suite of evolutionary models. Then the distribution of these objects as a function of color, spectral type, or other quantity is compared to the empirical distribution.

Burgasser (2004) undertook this kind of analysis to produce predicted empirical distributions assuming several different power-law mass functions and a single version of the log-normal function favored by Chabrier (2001). For evolutionary models, Burgasser (2004) employed models by Burrows et al. (1997) and the new (at the time) models of Baraffe et al. (2003). Here we attempt to expand that formalism and

to produce empirical distributions over a wider range of assumed mass function models. We also include a newer suite of evolutionary models from Saumon & Marley (2008) that better predicts behavior across the L/T transition.

#### 9.1.1. Formalism

Each assumed mass function, once properly normalized, can be thought of as a probability distribution function (PDF) describing the likelihood of finding a randomly selected object of mass  $M$  (in units of  $M_{\odot}$ ). Integrating the area under this PDF gives the cumulative distribution function (CDF), which gives the probability of a randomly selected object having a mass less than or equal to  $M$ . In order to sample from this distribution, one can use the inverse transform sampling method, which is done by switching the dependent and independent variables in the CDF and re-solving for the dependent variable, thus giving the inverse CDF. Random seeds can then be generated from a uniform distribution over the interval  $[0,1]$  and passed through the inverse CDF to produce samples of objects whose mass distribution is described by the assumed mass function.

As an example, consider a power-law mass function with an exponent of  $\alpha$ :

$$f(M) = \text{PDF} = CM^{-\alpha},$$

where  $C$  is a constant and  $M$  is the mass. If we wish to sample this distribution over the range of masses  $m_1 < M < m_2$ , then the cumulative distribution function would be

$$\begin{aligned} \text{CDF} &= C \int_{m_1}^{m_2} M^{-\alpha} dM \\ &= \begin{cases} \frac{M^{1-\alpha} - m_1^{1-\alpha}}{m_2^{1-\alpha} - m_1^{1-\alpha}}, & \text{for } \alpha \neq 1 \\ \frac{\ln(M) - \ln(m_1)}{\ln(m_2) - \ln(m_1)}, & \text{for } \alpha = 1 \end{cases} \end{aligned}$$

Note that at the low-mass limit of  $M = m_1$  we have  $CDF = 0$ , and at the high-mass limit of  $M = m_2$  we have  $CDF = 1$ . The inverse CDF would then be

$$CDF^{-1} = \begin{cases} [x(m_2^{1-\alpha} - m_1^{1-\alpha}) + m_1^{1-\alpha}]^{\frac{1}{1-\alpha}}, & \text{for } \alpha \neq 1 \\ e^{x[\ln(m_2) - \ln(m_1)] + \ln(m_1)}, & \text{for } \alpha = 1 \end{cases}$$

Note that at  $x = 0$  we have  $CDF^{-1} = m_1$  and at  $x = 1$  we have  $CDF^{-1} = m_2$ .

### 9.1.2. Functional Forms

We considered several different forms of the mass function, as summarized in Table 9: (1) a single power law, (2) a log-normal distribution, and (3) a bi-partite power law:

1. For the single power law, we ran simulations with six different values of the exponent ranging from  $\alpha = -1.0$  to  $\alpha = 1.5$  in half-integer increments.
2. For the log-normal function shown in Table 9, we chose three different values of the mean,  $\mu$ , and standard deviation,  $\sigma$ , corresponding to published values in the literature<sup>6</sup>:  $(\mu, \sigma) = (\ln(0.079), 0.69\ln(10))$  from Chabrier (2003),  $(\ln(0.10), 0.627\ln(10))$  from Chabrier (2001), and  $(\ln(0.22), 0.57\ln(10))$  from Chabrier (2003). The first two of these are applicable to the single-object mass function, and the third is applicable to the system mass function (which includes unresolved binaries).
3. For the bi-partite power law, we took the functional form shown in Table 9 and taken from equation 55 of Kroupa et al. (2013). The two power laws overlap in the mass range  $0.07 < M < 0.15M_{\odot}$ , with the high-mass component having  $\alpha_1 = 1.3 \pm 0.3$  and the low-mass component having  $\alpha_2 = 0.3 \pm 0.4$ . We have taken three versions of this bi-partite law, the first of which is taken at the canonical values of  $\alpha_1$  and  $\alpha_2$ . We have also considered two other versions: one in which the contribution from the lower-mass portion is increased (to  $\alpha_2 - \sigma_{\alpha_2}$ ) while the higher-mass portion is decreased (to  $\alpha_1 + \sigma_{\alpha_1}$ ), and another for which we did the opposite (using  $\alpha_1 - \sigma_{\alpha_1}$  and  $\alpha_2 + \sigma_{\alpha_2}$ ).

### 9.1.3. Evolutionary Models

Objects with a variety of birth times are randomly selected from the above mass functions and allowed to evolve to the present day. This latter step requires that we use evolutionary models to predict the object's current effective temperature and luminosity. For each form of the mass function, we

considered two different sets of evolutionary models, both of which are for objects of solar metallicity. The first is the set of COND models from Baraffe et al. (2003), which neglect dust opacity and are most applicable in the spectral ranges (mid-M and mid- to late-T) where atmospheres are believed to be largely cloud-free. The second set is from Saumon & Marley (2008) – specifically, their hybrid suite of models. These hybrid models should be applicable to our full range of  $T_{\text{eff}}$  because they include clouds for objects warmer than the L/T transition region (a zone in which rapid cloud growth and subsequent clearing are believed to occur; Burrows et al. 2006) and are cloudless for temperatures cooler than this.

Both sets of models have restrictions that need to be taken into account when drawing object samples. The model grids of Baraffe et al. (2003) are presented at five different ages (0.1, 0.5, 1, 5, and 10 Gyr) and fully sample the range  $125K \lesssim T_{\text{eff}} \lesssim 2800K$ , corresponding roughly to masses  $0.01M_{\odot} < M < 0.10M_{\odot}$ . Objects younger than 100 Myr were not included. Values of  $T_{\text{eff}}$  were obtained through linear interpolation of grid points.

The models of Saumon & Marley (2008) are presented at twenty-six different ages covering 3 Myr < age < 10 Gyr and cover the temperature range  $300K \lesssim T_{\text{eff}} \lesssim 2400K$  for objects with masses  $M > 0.002M_{\odot}$ . As with the Baraffe models, values of  $T_{\text{eff}}$  for our sample objects were obtained through linear interpolation of grid points.

### 9.1.4. Birthrates

Both Allen et al. (2005) and Burgasser et al. (2006) have studied the effect of differing birthrates on the shape of the resulting luminosity function. Allen et al. (2005) noted that most empirically derived birthrate distributions derived for field stars are roughly consistent with a constant formation rate over the past 10 Gyr. They found that differences in the assumed birthrate produced small variations in the shape of the resulting luminosity function, but these were much smaller than the effects produced by the assumed functional form of the mass function itself. Burgasser et al. (2006) expanded this discussion to more extreme birthrate scenarios and found that the resulting empirical luminosity function in the T dwarf regime is relatively insensitive to the assumed star formation rate, whereas the L dwarf regime is not. Nonetheless, we will simply assume constant star formation over the last 10 Gyr and leave analysis of other star formation rates to a future study.

### 9.1.5. Sampling Method

Using the above assumptions, one of us (AJC) wrote code in the *R* software environment<sup>7</sup> to produce simulated versions of the  $T_{\text{eff}}$  distributions. A random number generator was used to draw  $3 \times 10^6$  values in the interval  $[0,1]$ , and each was assigned an age depending upon the order of its selection. The  $n$ th draw was given an age of  $n \times 3333.\bar{3}$  yr so that the full sample covered an age spread of 0-10 Gyr uniformly. Its

<sup>6</sup> We quote these values for the natural (base  $e$ ) logarithmic version of the log-normal function that the *R* software environment uses.

<sup>7</sup> See <https://www.r-project.org/>.

**Table 9.** Mass Functions Considered for Masses  $< 0.1M_{\odot}$ 

Name	Functional Form	Parameters Used	Notation in Figures
(1)	(2)	(3)	(4)
Power law	$CM^{-\alpha}$	$\alpha = -1.0$	A
...	...	$\alpha = -0.5$	B
...	...	$\alpha = 0.0$	C
...	...	$\alpha = 0.5$	D
...	...	$\alpha = 1.0$	E
...	...	$\alpha = 1.5$	F
Log-normal	$Ce^{-(\ln(M)-\mu)^2/2\sigma^2}$	$\mu = \ln(0.079), \sigma = 0.69\ln(10)$	G
...	...	$\mu = \ln(0.10), \sigma = 0.627\ln(10)$	H
...	...	$\mu = \ln(0.22), \sigma = 0.57\ln(10)$	I
Bi-partite power law	$C\left(\frac{M}{0.07}\right)^{-\alpha_1}$ for $M > 0.07M_{\odot}$ , $\frac{C}{3}\left(\frac{M}{0.07}\right)^{-\alpha_2}$ for $M < 0.15M_{\odot}$	$\alpha_1 = 1.3, \alpha_2 = 0.3$	J
...	...	$\alpha_1 = 1.0, \alpha_2 = 0.7$	K
...	...	$\alpha_1 = 1.6, \alpha_2 = -0.1$	L

random seed value in the [0,1] interval was passed through the inverse CDF to provide a mass. This mass and age were then compared to the evolutionary model grids to determine the present-day effective temperature of the object.

### 9.2. Simulation Results

Results are shown in the following figures. Figure 11 shows the twelve forms of the mass function from Table 9. Overplotted on each panel are three different versions, one for each of three different low-mass cutoffs assumed:  $10M_{\text{Jup}}$ ,  $5M_{\text{Jup}}$ , and  $1M_{\text{Jup}}$ . Subsequent figures show the resulting  $T_{\text{eff}}$  histograms for each of these mass functions when paired with evolutionary code of Baraffe et al. (2003) in Figure 12 or Saumon & Marley (2008) in Figure 13.

The simulations in Figure 12 probe sufficiently low masses that the effects of varying the low-mass cutoff can be studied. This has already been explored by Burgasser (2004), but we reiterate here that the lowest  $T_{\text{eff}}$  bins, particularly the one from 150-300K, is very sensitive to the mass cutoff. In Model D (power law of  $\alpha = 0.5$ ), for example, the space densities vary wildly between the 450-300K and 150-300K bins depending upon the cutoff mass. From the 450-300K bin to the 150-300K bin, the space density drops by  $\sim 16\times$  for the  $10M_{\text{Jup}}$  cutoff, by  $\sim 2\times$  for the  $5M_{\text{Jup}}$  cutoff, and is roughly identical for the  $1M_{\text{Jup}}$  cutoff. This is a consequence of the fact that for the  $10M_{\text{Jup}}$  cutoff, there has not been enough time in the 10 Gyr allotted for any but the lowest mass, oldest objects to cool to these temperatures. For lower-mass cutoffs, there are larger populations of low-mass objects capable of cooling to these values. Measuring the space density of these coldest objects thus provides a powerful tool in determining the cutoff mass itself.

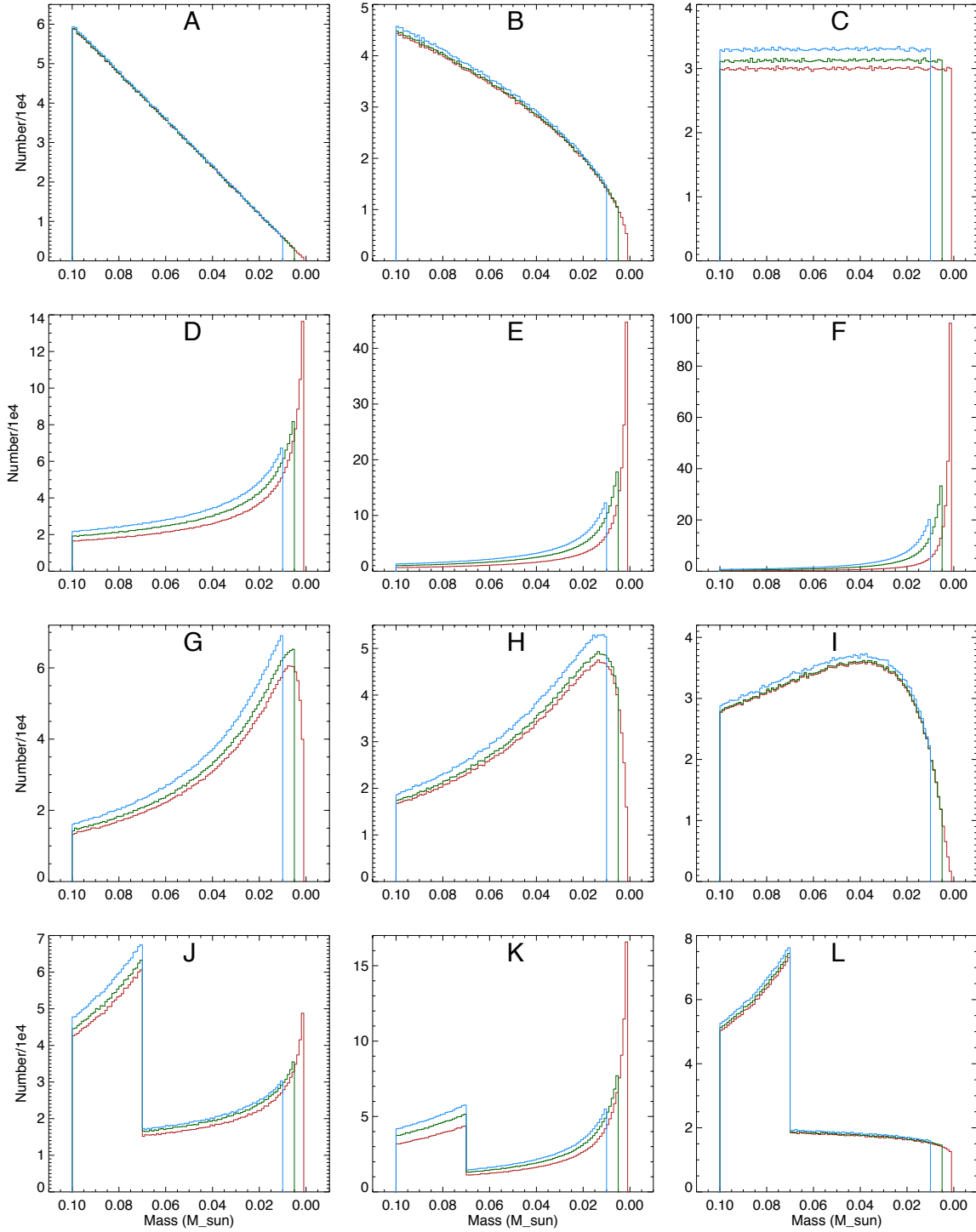
Note also that the  $T_{\text{eff}}$  simulations using the Baraffe et al. (2003) models are generally smooth where as those from Saumon & Marley (2008) show substructure along the run

of  $T_{\text{eff}}$ . Namely, all simulations show a bump in the number counts in the 1200-1350K bin. This was noted in Figure 13 of Saumon & Marley (2008) and is a consequence of the hybrid models in which the cooling timescale increases from 1400K to 1200K, at the transition between L and T dwarfs. This is the  $T_{\text{eff}}$  zone at which objects are transitioning from cloudy to clear photospheres. It is worth noting that the 1050-1500K range over which this overdensity is seen corresponds to  $\sim$ L6 to  $\sim$ T6, a wide spectral type range that itself reflects the breadth of change in spectral morphology as the clouds clear.

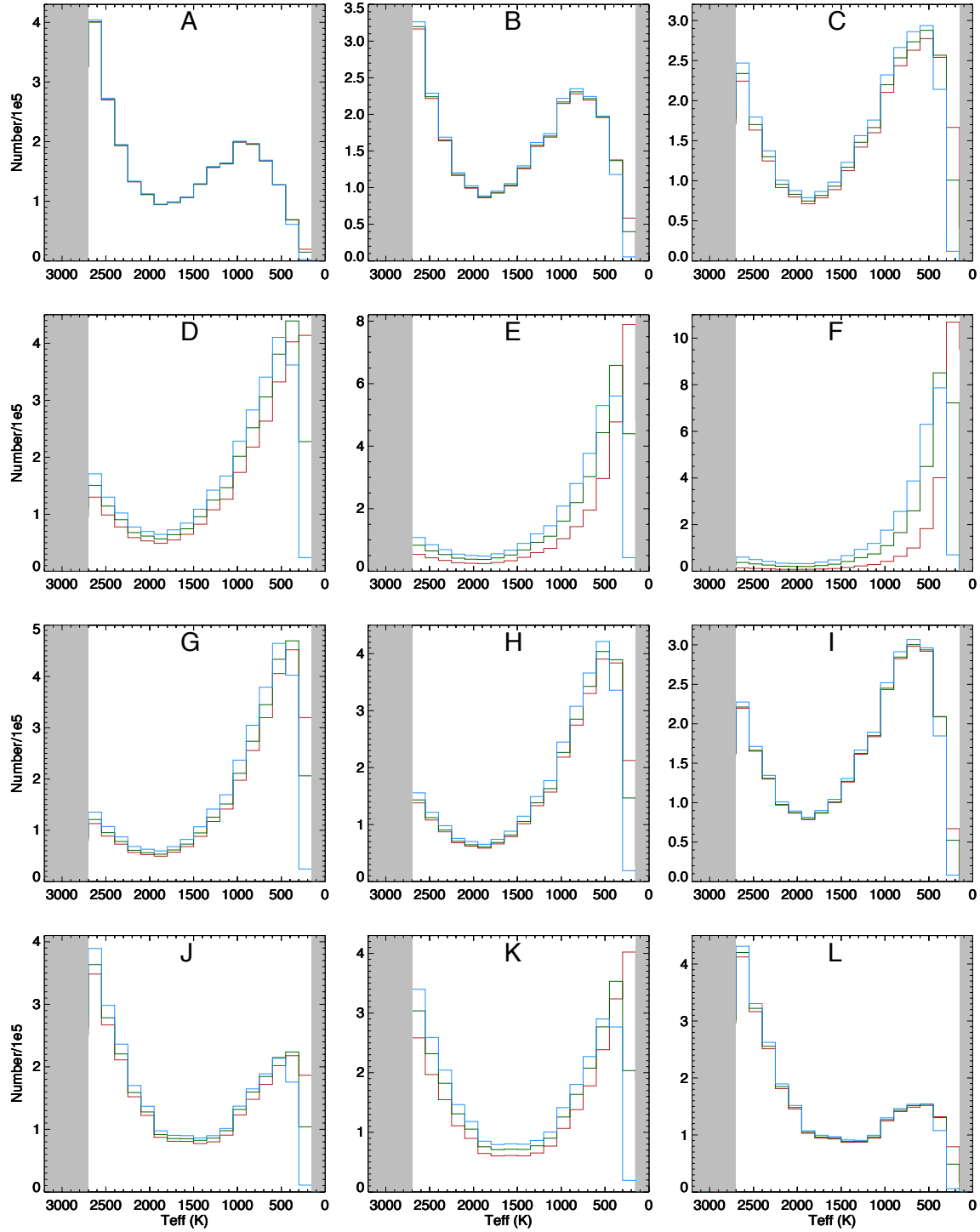
### 9.3. Comparison to Empirical Data

#### 9.3.1. Late-T and Y Dwarfs

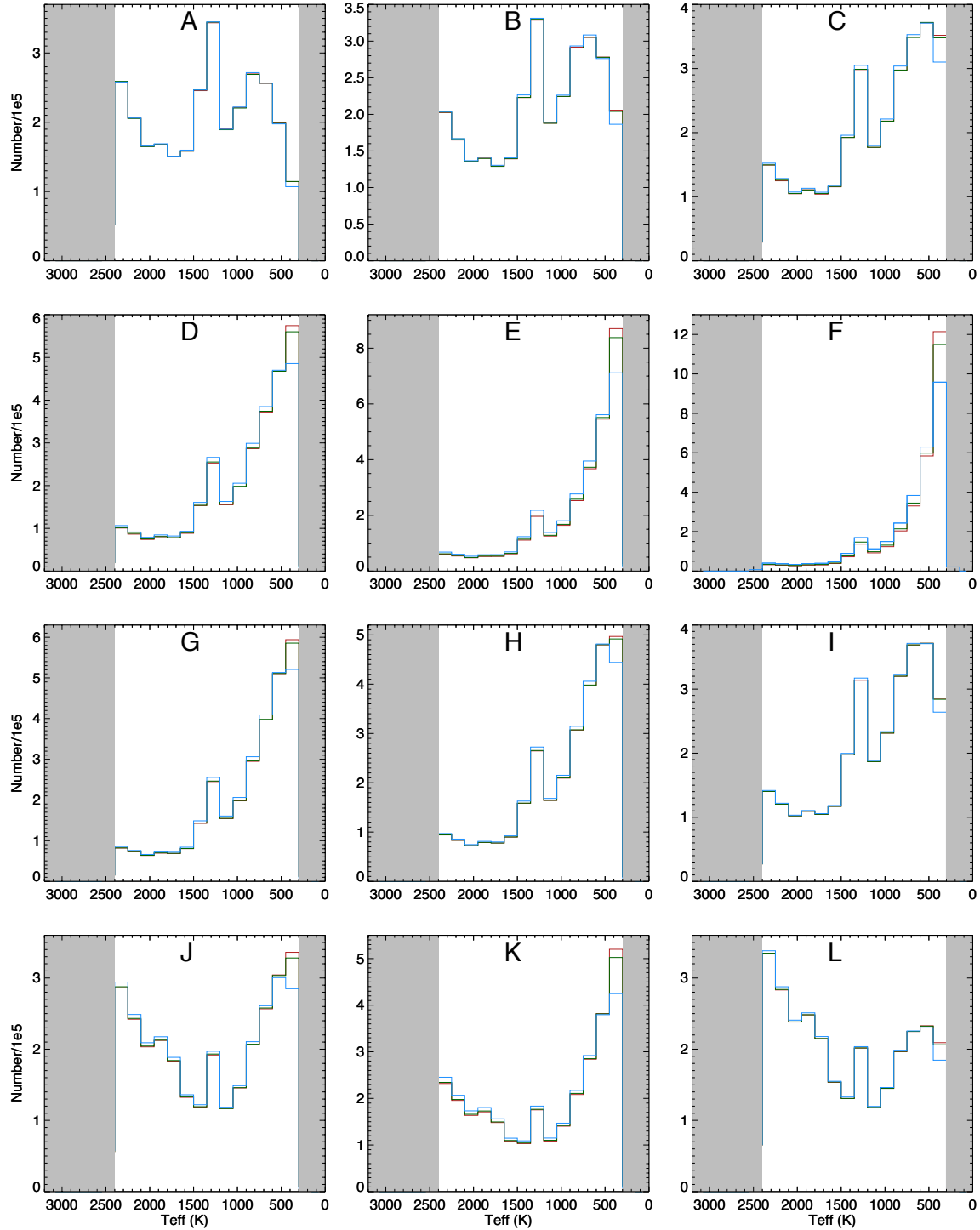
To compare the output from our mass function simulations to our observational sample, we need to determine the effective temperature for each object within the 20-pc volume. Using the subset of objects from Table 7 that have effective temperature estimates in the literature (Table 10), we can estimate  $T_{\text{eff}}$  values for the entire set.



**Figure 11.** Simulated mass functions. Each panel is labeled with a capital letter that refers back to the code in column 4 of Table 9 and specifies the functional form assumed. Each panel shows the results of three different assumed values of the low-mass cutoff:  $10 M_{\text{Jup}}$  (blue),  $5 M_{\text{Jup}}$  (green), and  $1 M_{\text{Jup}}$  (red). Bins are  $0.001 M_{\odot}$  wide.



**Figure 12.** The distribution of our simulated sample in  $T_{\text{eff}}$  for each of the mass function and low-mass cutoff assumptions shown in Figure 11 and passed through the evolutionary models of Baraffe et al. (2003). Color coding is the same as in Figure 11. Grey zones mark areas in  $T_{\text{eff}}$  that are not covered by the Baraffe et al. (2003) models. Bins are 150K wide.



**Figure 13.** The distribution of our simulated sample in  $T_{\text{eff}}$  for each of the mass function and low-mass cutoff assumptions shown in Figure 11 and passed through the evolutionary models of Saumon & Marley (2008). Color coding is the same as in Figure 11. Grey zones mark areas in  $T_{\text{eff}}$  that are not covered by the Saumon & Marley (2008) models. Bins are 150K wide.

**Table 10.** Effective Temperature Determinations for Objects from Table 7

Name	Spec. Type	$T_{\text{eff}}$ (K) from Forward Modeling (Ref.)	$T_{\text{eff}}$ (K) from Retrieval Analysis (Ref.)	$T_{\text{eff}}$ (K) from Stefan-Boltzmann (Ref.)	Adopted $T_{\text{eff}}$ (K)
(1)	(2)	(3)	(4)	(5)	(6)
ULAS 0034-0052	T8.5	625, 540 (5,10)	...	...	583
2MASS 0034+0523	T6.5	840 (11)	...	899 (4)	870
Gl 27B	T8	...	719 (3)	...	719
2MASS 0050-3322	T7	980 (11)	815 (3)	836 (4)	836
CFBDS 0059-0114	T8.5	573, 520 (5,10)	...	...	547
WISE 0146+4234AB	Y0	570 (7)	...	...	570
WISE 0146+4234A	T9	333 (16)	...	...	330
WISE 0146+4234B	Y0	415, 320 (2,16)	...	...	368
WISE 0148-7202	T9.5	600 (5)	...	...	600
ULAS 0150+1359	T7.5	775 (6)	...	...	775
2MASS 0243-2453	T6	1070 (11)	...	972 (4)	1021
WISE 0254+0223	T8	690 (5)	...	621 (4)	656
WISE 0304-2705	Y0pec	475 (2)	...	...	475
WISE 0313+7807	T8.5	662 (7)	...	...	662
WISE 0325-5044	T8	575 (1)	...	...	575
WISE 0335+4310	T9	525, 605 (1,7)	...	...	565
2MASS 0348-6022	T7	950 (8)	...	...	950
WISE 0350-5658	Y1	325, 325, 253 (1,2,5)	...	...	325
WISE 0359-5401	Y0	400, 435, 268 (1,2,5)	...	...	400
WISE 0404-6420	T9	575 (1)	...	...	575
WISE 0410+1502	Y0	400, 425, 415, 491 (1,2,5,7)	...	...	420
2MASS 0415-0935	T8	704, 750 (5,11)	680 (3)	677 (4)	692
WISE 0458+6434A	T8.5	765 (5)	...	...	765
WISE 0458+6434B	T9.5	615 (5)	...	...	615
UGPS 0521+3640	T8.5	625 (9)	...	...	625
WISE 0535-7500	>=Y1:	475, 375, 595 (1,2,5)	...	...	475
Gl 229B	T7pec	...	...	927 (4)	927
WISE 0647-6232	Y1	375, 335 (1,2)	...	...	355
WISE 0713-2917	Y0	450, 513 (2,7)	...	...	482
UGPS 0722-0540	T9	521 (5)	...	569 (4)	545
2MASS 0727+1710	T7	920 (11)	807 (3)	845 (4)	845
2MASS 0729-3954	T8pec	755 (5)	737 (3)	752 (4)	752
WISE 0734-7157	Y0	450, 450 (1,2)	...	...	450
WD 0806B	[>=Y3]	338, 353 (2,5)	...	...	346
DENIS 0817-6155	T6	...	...	1004 (4)	1004
WISE 0825+2805	Y0.5	400, 325 (1,2)	...	...	363
WISE 0836-1859	T8pec	765 (7)	...	...	765
WISE 0855-0714	[>=Y4]	250 (2)	...	...	250
ULAS 0901-0306	T7.5	670 (10)	...	...	670
2MASS 0937+2931	T6pec	810 (11)	...	881 (4)	846
2MASS 0939-2448	T8	709 (5)	611 (3)	686 (4)	686
WISE 0943+3607	T9.5	475 (1)	...	...	475
2MASS 1047+2124	T6.5	...	...	880 (4)	880

*Table 10 continued*



**Table 10** (*continued*)

Name	Spec. Type	$T_{\text{eff}}$ (K) from Forward Modeling (Ref.)	$T_{\text{eff}}$ (K) from Retrieval Analysis (Ref.)	$T_{\text{eff}}$ (K) from Stefan-Boltzmann (Ref.)	Adopted $T_{\text{eff}}$ (K)
(1)	(2)	(3)	(4)	(5)	(6)
2MASS 1114-2618	T7.5	...	678 (3)	669 (4)	674
WISE 1118+3125	T8.5	560 (5)	...	...	560
WISE 1141-3326	Y0	425 (2)	...	...	425
WISE 1206+8401	Y0	425, 435 (1,2)	...	...	430
2MASS 1217-0311	T7.5	870 (11)	726 (3)	885 (4)	870
WISE 1217+1626A	T9	575, 583 (5,13)	...	...	579
WISE 1217+1626B	Y0	435, 435, 401 (2,5,13)	...	...	435
2MASS 1225-2739B	T8	850 (5)	...	...	850
2MASS 1231+0847	T5.5	1070 (11)	...	...	1070
2MASS 1237+6526	T6.5	...	...	851 (4)	851
Gl 494C	T8	671 (5)	...	721 (4)	696
WISE 1311+0122	T9:	672 (7)	...	...	672
ULAS 1315+0826	T7.5	580 (10)	...	...	580
ULAS 1335+1130	T8.5	565, 550 (5,10)	...	...	558
SDSS 1346-0031	T6.5	990 (11)	...	1011 (4)	1001
WISE 1405+5534	Y0.5pec?	375, 385, 415 (1,2,5)	...	...	385
ULAS 1416+1348	(sd)T7.5	...	605 (3)	656 (4)	631
Gl 547B	sdT8,T8	618 (5)	...	...	618
Gl 570D	T7.5	800 (11)	715 (3)	759 (4)	759
2MASS 1503+2525	T5	...	...	1016 (4)	1016
SDSS 1504+1027	T7	...	...	992 (4)	992
WISE 1541-2250	Y1	400, 375, 550, 441 (1,2,5,7)	...	...	421
WISE 1542+2230	T9.5	475, 563 (1,7)	...	...	519
2MASS 1553+1532AB	T7	...	803 (3)	...	803
2MASS 1615+1340	T6	...	...	906 (4)	906
WISE 1617+1807	T8	600 (12)	...	...	600
SDSS 1624+0029	T6	1010 (11)	...	936 (4)	973
WISE 1639-6847	Y0pec	400, 375, 255 (1,2,5)	...	...	375
WISE 1711+3500A	T8	761 (13)	...	...	761
WISE 1711+3500B	T9.5	465 (13)	...	...	465
WISE 1738+2732	Y0	400, 425, 440, 514 (1,2,5,7)	...	...	433
WISE 1741+2553	T9	615 (5)	...	...	615
SDSS 1758+4633	T6.5	980 (11)	...	...	980
WISE 1804+3117	T9.5:	620, 706 (5,7)	...	...	663
WISE 1812+2721	T8.5:	620 (12)	...	...	620
WISE 1828+2650	>=Y2	325, 540, 400 (2,5,7)	...	...	400
SCR 1845-6357B	T6	1000 (14)	...	...	1000
WISE 2005+5424	sdT8	750 (15)	...	...	750
WISE 2018-7423	T7	710 (12)	...	...	710
WISE 2056+1459	Y0	425, 425, 425, 488 (1,2,5,7)	...	...	425
ULAS 2146-0010	T8.5	554, 560 (5,12)	...	...	557
Gl 845C	T6	952 (17)	...	...	952
WISE 2209+2711	Y0:	525, 325, 400 (1,2,7)	...	...	400
WISE 2212-6931	T9	550 (1)	...	...	550
WISE 2220-3628	Y0	425, 425, 525 (1,2,7)	...	...	425

*Table 10 continued*

**Table 10** (*continued*)

Name	Spec. Type	$T_{\text{eff}}$ (K) from Forward Modeling (Ref.)	$T_{\text{eff}}$ (K) from Retrieval Analysis (Ref.)	$T_{\text{eff}}$ (K) from Stefan-Boltzmann (Ref.)	Adopted $T_{\text{eff}}$ (K)
(1)	(2)	(3)	(4)	(5)	(6)
2MASS 2228-4310	T6	891, 1110 (4,11)	...	...	1001
WISE 2313-8037	T8	600 (12)	...	...	600
ULAS 2321+1354	T7.5	800 (6)	...	...	800
WISE 2354+0240	Y1	350, 350 (1,2)	...	...	350

NOTE—References to discovery and spectral classification papers: (1) Schneider et al. 2015, (2) Leggett et al. 2017, (3) Line et al. 2017, (4) Filippazzo, et al. 2015, (5) Dupuy & Kraus 2013, (6) Leggett et al. 2010, (7) Beichman et al. 2014, (8) Manjavacas et al. 2016, (9) Burningham et al. 2011, (10) Marocco et al. 2010, (11) Burgasser et al. 2006, (12) Burgasser et al. 2010, (13) Liu et al. 2012, (14) Vigan et al. 2012, (15) Mace et al. 2013, (16) Dupuy et al. 2015, (17) King et al. 2010.

NOTE—The  $T_{\text{eff}}$  values taken from Beichman et al. (2014) are those using the models of Morley et al. (2012).

As the division in Table 10 shows, three main methods have been used in the determinations. Method 1 is forward modeling, which has been the traditional method for determining temperatures. In this method, a grid of model atmospheres is calculated using a complete theoretical description wherein a few vital physical parameters are varied to simulate those likely to be encountered in real atmospheres. Observational spectrophotometric data are then compared to the grid to find the model that best reproduces the observations. Method 2 is inverse modeling, which is also referred to as retrieval analysis. This method strives to deduce physical parameters directly from the data. As explained in Line et al. (2014), this method uses fewer assumptions than forward modeling and has the potential of discerning physical processes (e.g., non-equilibrium chemistry) missing from the forward models, or revealing poor assumptions (e.g., solar elemental abundances) made in those models. Method 3 uses the Stefan-Boltzmann Law to compute the value of  $T_{\text{eff}}$  directly. In this method, the absolute bolometric luminosity – computed using a measured parallax and spectrophotometry over a wide range of wavelengths – is used with an assumed radius ( $\sim 1 R_{\text{Jup}}$  for old brown dwarfs) to determine the temperature directly from  $T_{\text{eff}} = (L/(4\pi R^2\sigma))^{0.25}$ .

For objects in Table 7, we have searched for  $T_{\text{eff}}$  measures in the literature. If an object from Table 7 is not listed in Table 10, that indicates that no  $T_{\text{eff}}$  measures were readily found for that source. However, if measurements were found, only a sample of the measurements from forward modeling are reproduced in the table, since some of the brighter objects and most of the Y dwarfs have many such references. However, we have listed all instances of the  $T_{\text{eff}}$  measures from retrieval analysis (all from Line et al. 2017) and from the Stefan-Boltzmann method (all from Filippazzo, et al. 2015<sup>8</sup>). Many

of the  $T_{\text{eff}}$  measures from forward modeling lack quoted uncertainties, partly due to the fact that the sparse sampling of the model grids makes interpretation of the actual uncertainty difficult, particularly when the perceived uncertainty is comparable to the  $T_{\text{eff}}$  step size in the grid itself. For uncertainties in the other values, the reader is referred to the cited paper.

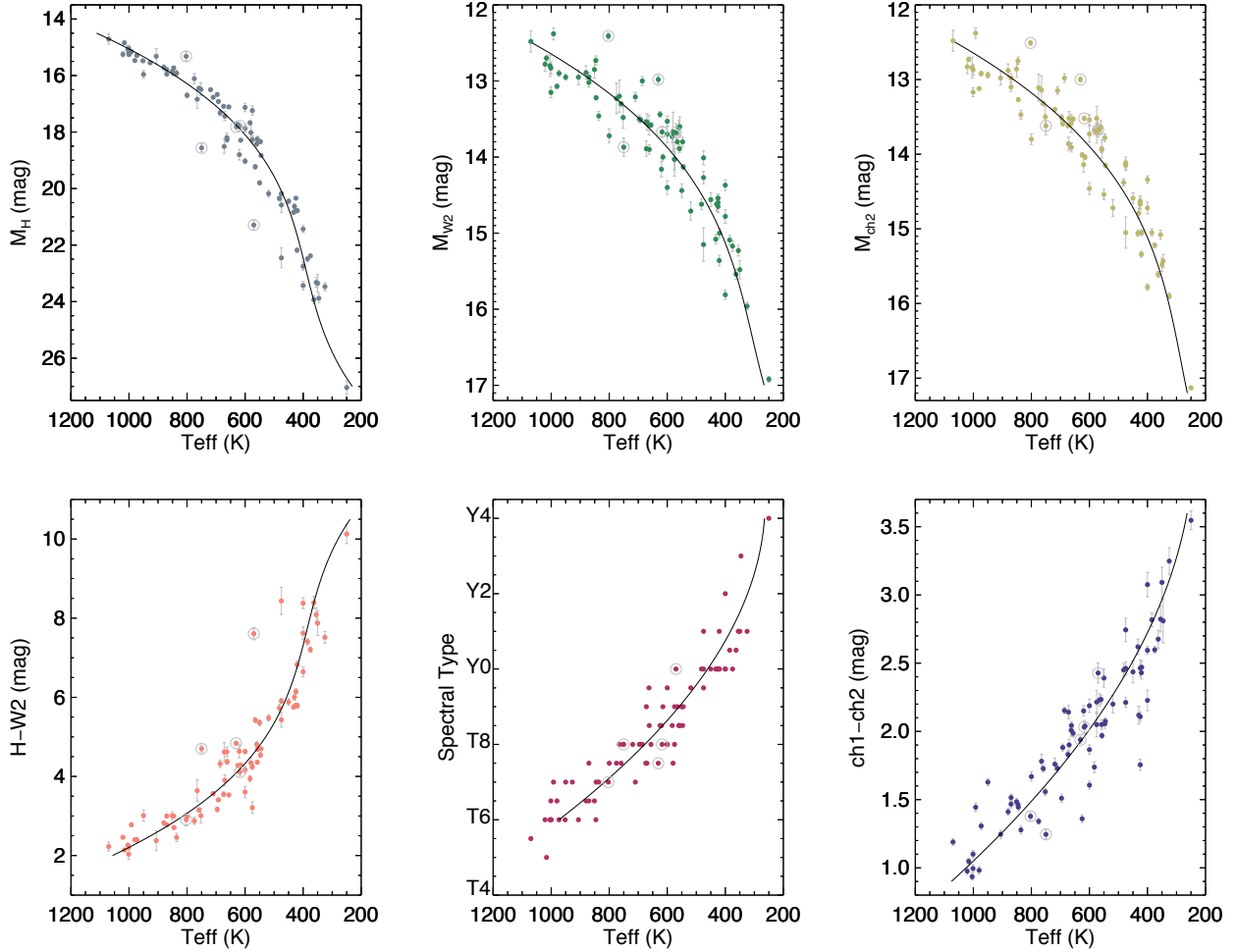
For the nine objects having  $T_{\text{eff}}$  measures from both retrieval analysis and the Stefan-Boltzmann method, the retrieval values tend to run cooler by  $\sim 40\text{K}$  on average. For the seven objects having  $T_{\text{eff}}$  measures from both forward modeling and retrieval analysis, the retrieval values tend to run cooler by  $\sim 90\text{K}$  on average. Indeed, Line et al. 2017 has noted that the retrieval values generally run cooler than the values obtained by other methods. Finally, for the fifteen objects having  $T_{\text{eff}}$  measures from both forward modeling and Stefan-Boltzmann, nine are warmer in the forward modeling value and six are warmer in the Stefan-Boltzmann value. The mean offset for these is  $\sim 25\text{K}$  on average, with the  $T_{\text{eff}}$  measure from forward modeling generally being the warmer one. Because of the sparseness of these comparison data, we have not attempted a correction from one method to the other since there are likely to be correlations with spectral type and/or color as well. So, for each object we merely take a median of all available measures and list that as the adopted  $T_{\text{eff}}$  value in Table 10. These adopted values are the ones used in the analysis below.

Figure 14 shows the adopted  $T_{\text{eff}}$  values from Table 10 and the collected photometry and parallax information from Table 7 to illustrate the trend of temperature with absolute magnitudes, colors, and spectral type. Fits to the relations, excluding known binaries and subdwarfs, are shown in the figure and described in Table 8.

Using these polynomial relations, we can assign  $T_{\text{eff}}$  values to all objects in the 20-pc sample. Table 11 gives these values

<sup>8</sup> In actuality, Filippazzo, et al. (2015) do not assume  $1R_{\text{Jup}}$  radius for all of their T dwarfs but use the radius predicted by evolutionary models matching their age estimates. They use gravity diagnostics, or knowledge of the primary if the T dwarf is a companion, to rule out youth for these T

dwarfs, which generally sets the ages to a very large range of 0.5-10 Gyr. However, brown dwarfs at these ages are predicted to have contracted to their final radii, so all of the Filippazzo, et al. 2015 sources in Table 10 were found to have radii of essentially  $1R_{\text{Jup}}$  anyway (0.94 to  $1.06R_{\text{Jup}}$ ).



**Figure 14.** Trends of adopted  $T_{\text{eff}}$  with  $M_H$ ,  $M_{W2}$ , and  $M_{ch2}$  magnitudes,  $H-W2$  color, spectral type, and  $ch1-ch2$  color, as taken from the data in Table 7 and Table 10. Polynomial fits to the data are shown on the plots and described in Table 8. Open circles in these three panels indicate data points that were excluded from the fits because the objects are binary or known to be of low metallicity.

and the method used in their determination. We use all relations if the supporting data have been measured, and take the median of the individual results as the adopted  $T_{\text{eff}}$  value. Table 11 lists which of the relations were used for each source.

In the case of two of the subdwarfs, measured values from the literature were used instead.

**Table 11.** Effective Temperature Determinations for the 20-pc Census of T6 and Later Dwarfs

Name	Adopted Spec. Type	Parallax (mas)	$T_{\text{eff}}$ (K)	$T_{\text{eff}}$ Methods <sup>a</sup>	( $l, b$ ) (deg)
(1)	(2)	(3)	(4)	(5)	(6)
Warmer objects (>1050K)					
2MASS 1231+0847	5.5	75.8±4.8	1064	1,2,3,4,5,6	287.8 71.1

Table 11 continued

**Table 11** (*continued*)

Name	Adopted Spec. Type	Parallax (mas)	$T_{\text{eff}}$ (K)	$T_{\text{eff}}$ Methods <sup>a</sup>	( <i>l, b</i> ) (deg)
(1)	(2)	(3)	(4)	(5)	(6)
2MASS 1225-2739A	5.5	76.0±2.5	1060	5	296.0 34.9
900-1050K					
WISE 2237+7228	6.0	62.3±2.5	1014	1,2,3,4,5,6	113.1 12.2
2MASS 1503+2525	5.0	157.2±2.2	1009	1,2,3,4,5,6	37.2 60.5
WISE 0627-1114	6.0	74.8±3.6	1008	1,2,3,4,5,6	220.3 -10.4
WISE 2343-7418	6.0	58.8±2.7	993	1,2,3,4,5,6	309.0 -42.0
DENIS 0817-6155	6.0	203.0±13.0	979	1,2,3,4,5,6	276.1 -14.4
WISE 1928+2356	6.0	149.9±2.4	977	1,2,3,4,5,6	58.3 3.1
2MASS 2228-4310	6.0	92.1±2.6	974	1,2,3,4,5,6	354.4 -57.0
WISE 1627+3255A	[6.0]	54.4±1.9	973	5	53.8 43.4
WISE 1627+3255B	[6.0]	54.4±1.9	973	5	53.8 43.4
WISE 0614+3912A	[6.0]	53.7±1.7	973	5	173.9 10.2
WISE 0614+3912B	[6.0]	53.7±1.7	973	5	173.9 10.2
SCR 1845-6357B	6.0	259.5±1.1	968	1,5	331.5 -23.5
WISE 1906+4508	6.0	60.6±0.8	964	1,2,3,4,5,6	75.7 16.4
SDSS 1346-0031	6.5	69.2±2.3	961	1,2,3,4,5,6	330.9 59.3
2MASS 0243-2453	6.0	93.6±3.6	954	1,2,3,4,5,6	214.2 -64.8
WISE 1250+2628	6.5	[53]	953	4,5	280.8 89.3
WISE 1506+7027	6.0	193.5±0.6	952	1,2,3,4,5,6	108.3 42.6
GI 845C	6.0	276.1±0.3	949	1,5	336.1 -48.1
WISE 2357+1227	6.0	59.5±4.1	939	1,2,3,4,5,6	102.8 -48.3
2MASS 1615+1340	6.0	58.4±2.5	930	1,2,3,4,5,6	27.7 40.8
WISE 1501-4004	6.0	69.5±4.0	929	1,2,3,4,5,6	328.3 16.3
SDSS 1624+0029	6.0	91.8±1.2	924	1,2,3,4,5,6	14.6 32.5
2MASS 0937+2931	6.0	162.8±3.9	920	1,2,3,4,5,6	197.9 47.6
WISE 0513+0608	6.5	70.8±1.5	917	1,2,3,4,5,6	195.5 -18.6
VHS 1258-4412	6.0	63.8±4.0	914	2,3,5,6	304.2 18.6
GI 576B	6.0	52.7±0.3	914	1,2,3,4,5,6	4.9 51.7
WISE 1221-3136	6.5	73.8±3.3	910	1,2,3,4,5,6	295.6 30.9
SDSS 1758+4633	6.5	71.4±0.3	909	1,2,3,4,5,6	73.5 28.2
WISE 2301+0216	6.5	53.0±2.8	902	1,2,3,4,5,6	76.6 -50.4
750-900K					
WISE 0542-1628	6.5	61.5±2.7	895	1,2,3,4,5,6	220.6 -22.5
2MASS 1553+1532A	6.5	75.1±0.9	892	5	27.1 46.4
WISE 1122+2550	6.0	66.3±2.3	890	1,2,3,4,5,6	211.6 70.2
2MASS 1047+2124	6.5	94.7±3.8	890	1,2,3,4,5,6	217.7 61.3
WISE 1320+6034	6.5	60.6±2.5	879	1,2,3,4,5,6	116.6 56.2
WISE 0241-3653	7.0	52.4±2.7	879	1,2,3,4,5,6	242.7 -64.8
2MASS 1237+6526	6.5	96.1±4.8	878	1,2,3,4,5,6	125.2 51.6
WISE 0325+0831	7.0	78.5±3.0	876	1,2,3,4,5,6	174.8 -38.3
WISE 0040+0900	7.0	69.8±1.5	870	1,2,3,4,5,6	118.3 -53.8
GI 229B	7.0	172.7±0.3	864	1,5	228.6 -18.4
2MASS 0034+0523	6.5	120.1±3.0	859	1,2,3,4,5,6	115.3 -57.2
WISE 2213+0911	7.0	54.5±2.5	855	1,2,3,4,5,6	71.0 -37.3
WISE 1124-0421	7.0	61.6±3.1	853	2,3,5,6	266.0 52.2
WISE 2226+0440	8.0	50.7±8.9	842	1,2,3,4,5,6	69.6 -42.7

*Table 11 continued*

Table 11 (continued)

Name	Adopted Spec. Type	Parallax (mas)	$T_{\text{eff}}$ (K)	$T_{\text{eff}}$ Methods <sup>a</sup>	( <i>l, b</i> ) (deg)
(1)	(2)	(3)	(4)	(5)	(6)
WISE 1039-1600	7.5	53.4±2.6	839	1,2,3,4,5,6	262.4 36.2
2MASS 1217-0311	7.5	91.7±2.2	839	1,2,3,4,5,6	286.4 58.6
2MASS 0050-3322	7.0	94.6±2.4	835	1,2,3,4,5,6	305.0 -83.7
2MASS 0348-6022	7.0	120.1±1.8	832	1,2,3,4,5,6	273.6 -45.4
WISE 0614+0951	7.0	65.6±2.2	829	1,2,3,4,5,6	199.9 -3.6
WISE 1735-8209	6.0	75.1±4.6	828	1,2,3,4,5,6	311.1 -24.4
WISE 0645-0302	6.0	50.7±4.2	827	1,2,3,4,5,6	215.0 -2.7
WISE 1852+3537	7.0	72.0±1.9	825	1,2,3,4,5,6	65.5 15.2
WISE 1457+5815	7.0	55.0±2.3	825	1,2,3,4,5,6	96.5 51.9
WISE 1052-1942	7.5	62.3±4.4	821	1,2,3,4,5,6	268.3 35.1
2MASS 0727+1710	7.0	112.5±0.9	817	1,2,3,4,5,6	201.3 15.5
WISE 0309-5016A	[7.0]	66.8±3.9	816	5	263.8 -55.0
WISE 0309-5016B	[7.0]	66.8±3.9	816	5	263.8 -55.0
WISE 2348-1028	7.0	58.4±3.5	806	1,2,3,4,5,6	78.4 -67.7
SDSS 1628+2308	7.0	75.1±0.9	805	1,2,3,4,5,6	40.9 41.0
WISE 0521+1025	7.5	[171]	786	4,5	192.8 -14.6
WISE 0245-3450	8.0	[59]	780	4,5,6	237.6 -64.5
WISE 2157+2659	7.0	59.7±2.2	779	1,2,3,4,5,6	81.7 -21.7
WISE 1612-3420	6.5	78.3±3.5	770	1,2,3,4,5,6	343.4 12.3
WISE 2000+3629	8.0	133.1±2.5	768	1,2,3,4,5,6	72.7 3.3
WISE 2209-2734	7.0	78.2±3.9	764	1,2,3,4,5,6	22.6 -54.2
WISE 2018-7423	7.0	83.2±1.9	761	1,2,3,4,5,6	320.0 -31.9
GI 570D	7.5	171.2±0.9	755	1,2,3,4,5,6	338.2 32.7
WISE 0628-8057	[9.0]	[50]	754	6	292.8 -27.7
600-750K					
WISE 2005+5424	8.0	62.9±3.3	750	7	88.6 11.9
WISE 2211-4758	[8.0]	55.8±4.6	746	1,2,3,4,6	348.1 -52.7
ULAS 1416+1348A	[7.5]	109.7±1.3	744	5	3.3 66.1
ULAS 1416+1348B	[7.5]	109.7±1.3	744	5	3.3 66.1
2MASS 1553+1532B	7.5	75.1±0.9	744	5	27.1 46.4
2MASS 0729-3954	8.0	126.3±8.3	736	1,2,3,4,5,6	252.6 -10.4
WISE 1523+3125	6.5	61.4±3.8	735	1,2,3,4,5,6	49.6 56.8
WISE 1322-2340	8.0	77.5±4.2	735	1,2,3,4,5,6	312.1 38.6
ULAS 2321+1354	7.5	83.6±2.4	735	1,2,3,4,5,6	92.1 -43.5
WISE 1813+2835	8.0	74.9±2.5	731	1,2,3,4,5,6	55.5 20.3
WISE 2302-7134	[4.5]	65.1±4.7	726	1,2,3,4,6	314.3 -43.1
WISE 1959-3338	8.0	85.3±2.2	724	1,2,3,4,5,6	7.3 -27.9
GI 494C	8.0	85.5±1.5	724	1,2,3,4,5,6	311.7 75.1
ULAS 1029+0935	8.0	66.8±4.2	718	1,2,3,4,5,6	233.8 52.3
ULAS 0859+1010	7.0	50.3±1.7	716	1,2,4,5	218.4 32.9
WISE 2255-3118	8.0	70.7±4.2	713	1,2,3,4,5,6	16.5 -64.5
GI 27B	8.0	90.4±0.3	711	1,3,5,6	119.2 -41.5
WISE 0223-2932	7.5	80.7±2.6	709	1,2,3,4,5,6	225.2 -69.7
WISE 1653+4444	8.0	78.0±4.2	699	1,2,3,4,5,6	70.0 39.3
WISE 0623-0456	8.0	87.4±2.9	699	1,2,3,4,5,6	214.1 -8.5
WISE 1318-1758	8.0	57.8±2.7	696	1,2,3,4,5,6	312.0 44.4

Table 11 continued

**Table 11** (*continued*)

Name	Adopted	Parallax	$T_{\text{eff}}$	$T_{\text{eff}}$	( <i>l, b</i> )
	Spec. Type	(mas)	(K)	Methods <sup>a</sup>	(deg)
(1)	(2)	(3)	(4)	(5)	(6)
WISE 1301-0302	8.5	53.8±5.6	694	1,2,3,4,5,6	308.0 59.7
WISE 0744+5628	8.0	67.1±2.5	693	1,2,3,4,5,6	161.1 29.6
WISE 2313-8037	8.0	93.5±2.7	692	1,2,3,4,5,6	307.7 -35.6
2MASS 1114-2618	7.5	179.2±1.4	692	1,2,3,4,5,6	277.4 31.7
WISE 2319-1844	7.5	79.2±3.1	688	1,2,3,4,5,6	49.8 -67.3
WISE 0015-4615	8.0	71.8±2.7	688	1,2,3,4,5,6	321.2 -69.6
WISE 0759-4904	8.0	89.1±2.4	685	1,2,3,4,5,6	263.5 -10.0
WISE 0254+0223	8.0	146.1±1.5	685	1,2,3,4,5,6	172.8 -48.2
2MASS 0415-0935	8.0	175.2±1.7	685	1,2,3,4,5,6	202.9 -38.9
ULAS 0950+0117	8.0	57.9±2.3	682	1,2,3,4,5,6	236.0 39.6
WISE 0226-0211A	[8.0]	57.3±4.7	678	5	169.3 -56.3
2MASS 1225-2739B	8.0	76.0±2.5	678	5	296.0 34.9
2MASS 0939-2448A	[8.0]	187.3±4.6	678	5	256.9 20.5
2MASS 0939-2448B	[8.0]	187.3±4.6	678	5	256.9 20.5
WISE 0247+3725	8.0	64.8±2.6	674	1,2,3,4,5,6	147.1 -20.0
ULAS 0901-0306	7.5	62.6±2.6	673	1,2,3,4,5,6	232.1 26.9
WISE 0857+5604	8.0	87.2±2.4	661	1,2,3,4,5,6	161.1 39.6
WISE 0723+3403	9.0	56.3±3.5	660	1,2,3,4,5,6	184.4 20.9
ULAS 1302+1308	8.0	65.0±5.0	659	1,2,3,4,5,6	313.7 75.8
WISE 2203+4619	8.0	66.0±4.2	658	1,2,3,4,5,6	95.1 -7.3
WISE 1519+7009	8.0	77.6±2.8	652	1,2,3,4,5,6	107.0 42.1
WISE 1448-2534	8.0	52.5±2.5	652	1,2,3,4,5,6	333.5 30.3
CFBDS 0133+0231	8.5	56.3±3.4	652	1,2,3,4,5,6	143.2 -58.7
WISE 2019-1148	8.0	77.5±3.5	651	1,2,3,4,5,6	32.0 -24.8
ULAS 0034-0052	8.5	68.7±1.4	645	1,2,3,4,5,6	113.2 -63.4
WISE 1617+1807	8.0	84.6±4.2	641	1,2,3,4,5,6	33.4 42.0
WISE 1018-2445	8.0	83.6±3.6	640	1,2,3,4,5,6	264.0 26.3
WISE 0323-6025	8.5	71.4±2.9	629	1,2,3,4,5,6	275.9 -47.9
WISE 0049+2151	8.5	139.9±2.5	629	1,2,3,4,5,6	122.4 -41.0
ULAS 1315+0826	7.5	50.5±5.7	628	1,2,4,5	320.7 70.5
WISE 1051-2138	8.5	67.0±3.0	625	1,2,3,4,5,6	269.2 33.2
UGPS 0521+3640	8.5	122.2±1.6	625	1,2,3,4,5,6	170.7 -0.0
WISE 0323-5907	[6.0]	71.5±4.3	623	2,3,6	274.4 -48.7
VHS 1433-0837	8.0	50.9±4.5	622	1,2,3,4,5,6	341.1 46.6
GI 547B	8.0	58.2±0.5	618	7	347.2 56.0
WISE 0458+6434A	8.5	109.2±3.6	616	5	145.8 13.4
ULAS 0745+2332	8.5	[63]	616	5	196.8 21.8
WISE 0500-1223	8.0	95.1±3.6	614	1,2,3,4,5,6	211.8 -30.3
WISE 1025+0307	8.5	85.4±2.5	612	1,2,3,4,5,6	241.2 47.8
WISE 0032-4946	8.5	63.6±2.9	610	1,2,3,4,5,6	310.8 -67.1
WISE 0615+1526	8.5	[64]	607	5,6	195.2 -0.6
WISE 0750+2725	8.5	68.4±3.4	605	1,2,3,4,5,6	193.2 24.2
ULAS 2146-0010	8.5	79.8±4.5	604	1,2,3,4,5,6	56.4 -38.1
WISE 1042-3842	8.5	65.4±3.4	601	1,2,3,4,5,6	277.1 17.6
CFBDS 0059-0114	8.5	103.2±2.1	601	1,2,3,4,5,6	127.4 -64.0

450-600K

*Table 11 continued*

**Table 11** (*continued*)

Name	Adopted Spec. Type	Parallax (mas)	$T_{\text{eff}}$ (K)	$T_{\text{eff}}$ Methods <sup>a</sup>	( <i>l, b</i> ) (deg)
(1)	(2)	(3)	(4)	(5)	(6)
WISE 1150+6302	8.0	124.5±3.0	599	2,3,5,6	134.3 52.7
WISE 0540+4832	8.5	70.0±2.6	598	1,2,3,4,5,6	162.7 9.4
WISE 1804+3117	9.5	62.7±3.4	597	1,2,3,4,5,6	57.5 23.0
WISE 1118+3125	8.5	113.2±4.6	595	1,2,3,4,5,6	195.4 69.4
WISE 0313+7807	8.5	134.3±3.6	595	1,2,3,4,5,6	130.1 17.3
ULAS 1335+1130	8.5	99.9±1.6	593	1,2,3,4,5,6	338.8 71.2
WISE 2344+1034	9.0	64.7±3.7	592	1,2,3,4,5,6	97.5 -49.0
WISE 0316+4307	8.0	73.3±2.8	582	1,2,3,4,5,6	149.1 -12.3
WISE 1741+2553	9.0	214.3±2.8	578	1,2,3,4,5,6	50.1 26.1
WISE 0325-3854	9.0	57.2±5.4	574	1,2,3,4,5,6	243.1 -56.0
WISE 2102-4429	9.0	92.9±1.9	573	1,2,3,4,5,6	356.2 -41.5
WISE 1311+0122	9.0	68.8±2.7	567	1,2,3,4,5,6	314.1 63.8
WISE 0005+3737	9.0	127.0±2.4	564	1,2,3,4,5,6	112.9 -24.4
WISE 2159-4808	9.0	75.7±2.7	562	1,2,3,4,5,6	348.8 -50.8
WISE 2332-4325	9.0	65.3±2.6	559	1,2,3,4,5,6	342.2 -67.2
WISE 1217+1626A	9.0	104.4±4.7	559	5	265.2 76.8
WISE 1112-3857	9.0	[56]	559	4,5,6	282.7 20.0
WISE 0146+4234A	9.0	52.5±2.3	559	5	133.7 -19.1
WISE 0038+2758	9.0	89.7±2.5	557	1,2,3,4,5,6	119.4 -34.8
WISE 0430+4633	8.0	93.9±4.1	553	1,2,3,4,5,6	157.2 -1.2
WISE 1812+2721	8.5	98.5±4.4	552	1,2,3,4,5,6	54.2 20.1
UGPS 0722-0540	9.0	242.8±2.4	552	1,2,3,4,5,6	221.5 4.3
WISE 0713-5854	9.0	78.2±4.6	546	1,2,3,4,5,6	269.7 -20.3
WISE 0335+4310	9.0	72.1±2.4	545	1,2,3,4,5,6	152.0 -10.3
WISE 2134-7137	9.0	109.7±3.7	538	1,2,3,4,5,6	320.5 -38.0
WISE 1614+1739	9.0	97.6±3.4	538	1,2,3,4,5,6	32.6 42.4
WISE 2325-4105	9.0	108.4±3.7	523	1,2,3,4,5,6	349.1 -67.5
WISE 0148-7202	9.5	91.7±3.4	520	1,2,3,4,5,6	296.9 -44.4
WISE 1055-1652	9.5	72.2±2.7	509	2,3,5,6	267.1 37.8
WISE 0458+6434B	9.5	109.2±3.6	508	5	145.8 13.4
WISE 0226-0211B	[9.5]	57.3±4.7	508	5	169.3 -56.3
WISE 0751-7634	9.0	97.9±6.7	507	1,2,3,4,5,6	288.8 -23.0
WISE 0811-8051	9.5	99.1±7.7	493	1,2,3,4,5,6	293.5 -23.7
WISE 2212-6931	9.0	81.9±2.5	489	1,2,3,4,5,6	320.4 -41.8
WISE 0943+3607	9.5	93.8±2.8	489	1,2,3,4,5,6	188.1 49.3
WISE 0833+0052	9.0	82.6±4.5	486	1,2,3,4,5,6	224.4 23.0
WISE 1542+2230	9.5	85.6±4.2	481	1,2,3,4,5,6	35.8 51.2
WISE 0302-5817	10.0	56.1±4.4	471	2,3,5,6	275.8 -51.4
WISE 2056+1459	10.0	138.3±2.2	467	1,2,3,4,5,6	62.0 -19.2
WISE 0734-7157	10.0	75.0±2.4	466	1,2,3,4,5,6	283.7 -22.4
WISE 0713-2917	10.0	107.5±2.4	466	1,2,3,4,5,6	241.5 -8.6
WISE 0336-0143	10.0	99.0±2.4	464	2,3,5,6	187.3 -43.1
WISE 1141-3326	10.0	99.7±4.2	463	2,3,5,6	286.7 27.2
WISE 1217+1626B	10.0	104.4±4.7	461	5	265.2 76.8
WISE 0146+4234B	10.0	52.5±2.3	461	5	133.7 -19.1
WISE 1206+8401	10.0	81.9±2.5	459	1,2,3,4,5,6	124.3 33.0

*Table 11 continued*



**Table 11** (*continued*)

Name	Adopted Spec. Type	Parallax (mas)	$T_{\text{eff}}$ (K)	$T_{\text{eff}}$ Methods <sup>a</sup>	( <i>l, b</i> ) (deg)
(1)	(2)	(3)	(4)	(5)	(6)
WISE 2220-3628	10.0	97.0±2.4	458	1,2,3,4,5,6	7.0 -56.9
WISE 0304-2705	10.0	81.5±7.7	458	1,2,3,4,5,6	220.6 -60.4
WISE 0410+1502	10.0	150.2±2.4	454	1,2,3,4,5,6	177.9 -25.9
300-450K					
WISE 0359-5401	10.0	75.8±2.5	445	1,2,3,4,5,6	264.3 -46.5
WISE 1738+2732	10.0	131.0±2.4	435	1,2,3,4,5,6	51.6 27.2
WISE 1828+2650	12.0	100.7±2.3	412	1,2,3,4,5,6	55.1 16.6
WISE 1639-6847	10.0	211.9±2.7	403	1,2,3,4,5,6	321.2 -14.5
WISE 1405+5534	10.5	157.9±3.1	402	1,2,3,4,5,6	102.8 58.6
WISE 0535-7500	11.0	66.4±2.4	398	1,2,3,4,5,6	286.3 -31.0
WISE 1541-2250	11.0	167.1±2.3	395	1,2,3,4,5,6	346.5 25.3
WISE 0647-6232	11.0	100.3±2.4	381	1,2,3,4,5,6	272.5 -24.3
WISE 2354+0240	11.0	124.1±4.9	374	1,2,3,4,5,6	95.8 -57.1
WD 0806B	[11.0]	52.2±1.7	369	1,2,3,4,6	279.4 -17.5
WISE 0825+2805	10.5	155.8±2.4	364	1,2,3,4,5,6	195.2 31.8
WISE 2209+2711	10.0	161.6±2.4	360	1,2,3,4,5,6	83.9 -23.1
WISE 0350-5658	11.0	174.6±2.6	355	1,2,3,4,5,6	269.0 -46.7
150-300K					
WISE 0855-0714	[14.0]	438.9±3.0	250	0	235.0 23.4

<sup>a</sup>These are the methods used in determining the  $T_{\text{eff}}$  value for the source: 1 =  $M_H$  relation, 2 =  $M_{W2}$  relation, 3 =  $M_{ch2}$  relation, 4 =  $H-W2$  relation, 5 = spectral type relation, 6 = ch1–ch2 relation, 7 = value taken from Table 10. All relations are those shown in Figure 14 and described in the last six lines of Table 8

NOTE—Spectral types and parallaxes in brackets are estimates, not actual measures.

The objects in Table 11 represent all of the T and Y dwarfs in Table 1 that have parallax values  $\geq 50$  mas. Binaries are listed as separate objects, with individual spectral types being those discussed in Section 8.2. (For suspected binaries with no other corroborating information, equal-magnitude binaries were assumed for which the individual components have the same spectral type as the component system.) Objects are ordered by our  $T_{\text{eff}}$  determinations and grouped into 150K bins to coincide with the binning given in Figures 12 and 13. There are six such bins running from 150K to 1050K. The hottest of these bins, from 900-1050K, primarily includes T6 and T6.5 dwarfs. We note that of the 29 objects in this bin, 12 fall in the 50K range from 900-950K, 14 fall in the range 950-100K, and only 3 fall in the range 100-1050K. By performing a spectral type cut of  $\geq T6$ , we have removed some earlier type objects that should otherwise be counted here. In fact, one such object that inadvertently was added to the sample – the T5 dwarf 2MASS 1503+2525 – has a temperature determination of 1009K. Thus, we should consider this bin to be incomplete.

A similar analysis shows that the two low-temperature bins are also incomplete. The 150-300K bin contains only WISE 0855–0714, at  $d=2.3$  pc and  $T_{\text{eff}}=250$ K. Cooler and/or more

distant brown dwarfs are expected to be missing from this bin because of their extreme faintness. The 300-450K bin contains 13 objects, but none of these fall in the 50K bin from 300-350K. Objects in this temperature range have also likely eluded detection.

In addition to incompletenesses related to spectral type and intrinsically dim magnitudes, we need to determine if our goal of identifying a complete 20-pc sample has been successful. The standard analysis used for this is the  $V/V_{\text{max}}$  test of Schmidt (1968), which checks the distribution of objects in space. In each 150K bin, each object is assigned a value  $V$  that is the volume of space interior to object at the distance corresponding to its parallax. The value  $V_{\text{max}}$  is the full volume of space contained within the distance limit being considered. For a uniform sample, the average value,  $\langle V/V_{\text{max}} \rangle$ , should be  $\sim 0.5$  because half of the sample should lie in the closer half of the volume and the rest should lie in the more distant half. If the value of  $\langle V/V_{\text{max}} \rangle$  is significantly different from 0.5, then the sample is either non-homogeneous or incomplete. Given that we expect old, solivagant brown dwarfs to be isotropically distributed in space, this would indicate incompleteness to the distance limit being considered.

Using the parallaxes listed in Table 11, we can measure the value of  $\langle V/V_{\text{max}} \rangle$  for many different assumed limiting

distances. These results are shown in Figure 15, for five of our six 150K bins. (The coldest bin, from 150-300K, is not shown since it contains only one known object.) At distances of only a few parsec, for which there are only a handful of objects, the values of  $\langle V/V_{max} \rangle$  vary wildly. For most bins, however, this value stabilizes near 0.5 as larger distances and larger number of objects are considered. At distances beyond 20 pc, the value of  $\langle V/V_{max} \rangle$  drops steadily since the list in Table 11 contains no objects more distant than this limit.

Given that there are, at most, only a few dozen objects in each 150K temperature bin, random fluctuations due to poor statistics can naturally cause the value of  $\langle V/V_{max} \rangle$  to deviate from 0.5. What value of  $\langle V/V_{max} \rangle$  should we take to indicate true incompleteness? To answer this question, we assume a perfectly uniform sample and examine the scale of deviations from  $\langle V/V_{max} \rangle = 0.5$  that can be imparted due to sample size. For instance, consider a sample of two marbles for which each marble is equally likely to fall in bucket A (representing the nearer half of the sky) or bucket B (representing the more distant half). There is a 50% probability that two marbles will fall into different buckets, a 25% probability that both will fall in bucket A, and a 25% probability that both will fall in bucket B. By analogy with a sky distribution of brown dwarfs,  $\langle V/V_{max} \rangle$  values can thus range as low as 0.0 and as high as 1.0, with only half of the values falling at or near 0.5.

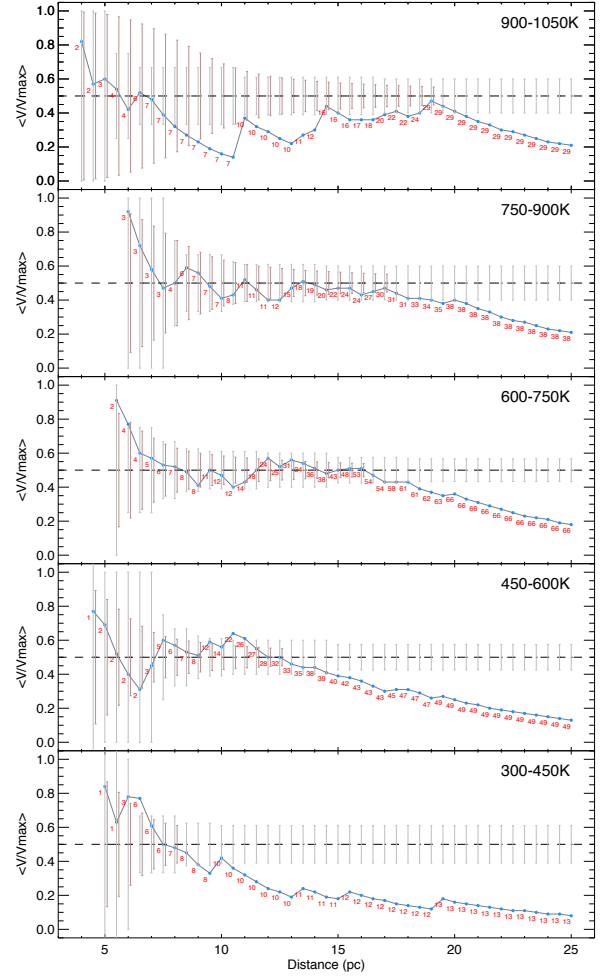
We can generalize this argument to any number of marbles, although we consider only even numbers so that the average value becomes the same number of marbles in each bucket (roughly equivalent to  $\langle V/V_{max} \rangle = 0.5$ ). The likelihood that the same number of marbles,  $n$ , falls in each bucket is given by

$$\frac{n!}{\left(\frac{n}{2}\right)! \left(\frac{n}{2}\right)! 2^n}. \quad (5)$$

The likelihood that we find a different number of marbles, differing by the integer  $a$ , is twice the following value (with the additional factor of two coming from the fact that the number in bucket A can be larger by  $a$  than that in bucket B or vice versa)

$$\frac{n!}{\left(\frac{n}{2}-a\right)! \left(\frac{n}{2}+a\right)! 2^n}. \quad (6)$$

We can determine the value of  $a_{max}$  at which we reach a cumulative probability, summed over all values of  $a$  from  $a_{min} = 0$  (the case of equal numbers in both buckets) to  $a_{max}$ , of  $\sim 68\%$ . This will allow us to determine a "most likely" range analogous to the Gaussian statistical concept of a  $1\sigma$  likelihood. Because marbles, and thus brown dwarfs, are quantized, so are the cumulative probabilities, so we consider the value of  $a_{max}$  for which the cumulative probability first exceeds 68%. We then take  $0.5 - ((n/2) - a_{max})/n$  as the approximation for the  $1\sigma$  range on  $\langle V/V_{max} \rangle$  for a uniformly distributed set of  $n$  objects. We find that for  $n = 100$ , the  $1\sigma$  value for  $\langle V/V_{max} \rangle$  is  $\sim 0.050$ ; for  $n = 50$  it is  $\sim 0.075$ ; and for  $n = 30$  it is  $\sim 0.100$ . For smaller values of  $n$  this  $1\sigma$  value dramatically jumps: 0.11 for  $n = 10$ , 0.125 for  $n = 8$ , 0.167



**Figure 15.** The average  $V/V_{max}$  value in 0.5-pc intervals for five of the six 150-K bins encompassing our 20-pc T6-Y4 sample. (The sixth bin, from 150-300K, is not shown because it contains only one object, WISE 0855-0714.) Blue dots represent our empirical sample. Red labels mark the number of objects in the computation at each 0.5-pc interval. The grey dotted line shows the  $V/V_{max} = 0.5$  level indicating a complete sample. The grey error bars show the approximate  $1\sigma$  range around  $V/V_{max} = 0.5$  that a complete sample of the size indicated by the red number would exhibit, given random statistics. The brown error bars, offset by +0.05 pc from the grey error bars for clarity, show the  $1\sigma$  variation around 0.5 obtained by 10,000 Monte Carlo simulations having the same number of objects and the same completeness limit listed in Table 12. See text for details.

for  $n = 6$ , and 0.25 for  $n = 4$ . These  $1\sigma$  values are the ones shown as the grey probability intervals around the  $\langle V/V_{max} \rangle = 0.5$  line on Figure 15. The  $1\sigma$  value chosen is the one corresponding to the number of objects (in red on the plot and denoted as  $n$  here) being used in the computation at that dis-

tance. (When  $n$  is odd, we use the  $1\sigma$  value measured for  $n-1$ .)

With these likelihoods in mind, we can now better interpret the curves shown in Figure 15. For the 900-1050K bin, we last reach a  $\langle V/V_{max} \rangle$  value of  $\sim 0.5$  at  $d = 19.0$  pc (29 objects; space density  $> 1.01 \times 10^{-3} \text{ pc}^{-3}$ ), although the numbers are still within the  $1\sigma$  envelope at  $d = 20.0$  pc for a sample of 29 objects (space density  $> 0.865 \times 10^{-3} \text{ pc}^{-3}$ ). For the 750-900K bin, we last reach  $\langle V/V_{max} \rangle \approx 0.5$  at  $d = 17.0$  pc (30 objects; space density  $= 1.46 \times 10^{-3} \text{ pc}^{-3}$ ), although the numbers are still within the  $1\sigma$  envelope at  $d = 18.0$  pc for a sample of 30 objects (space density  $= 1.23 \times 10^{-3} \text{ pc}^{-3}$ ). For the 600-750K bin, we last reach  $\langle V/V_{max} \rangle \approx 0.5$  at  $d = 16.0$  pc (53 objects; space density  $= 3.09 \times 10^{-3} \text{ pc}^{-3}$ ), although the numbers are still within the  $1\sigma$  envelope at  $d = 17.0$  pc for a sample of 53 objects (space density  $= 2.58 \times 10^{-3} \text{ pc}^{-3}$ ). For the 450-600K bin, we last reach  $\langle V/V_{max} \rangle \approx 0.5$  at  $d = 12.5$  pc (32 objects; space density  $= 3.91 \times 10^{-3} \text{ pc}^{-3}$ ), although the numbers are still within the  $1\sigma$  envelope at  $d = 13.5$  pc for a sample of 32 objects (space density  $= 3.10 \times 10^{-3} \text{ pc}^{-3}$ ). For the 300-450K bin, we last reach  $\langle V/V_{max} \rangle \approx 0.5$  at  $d = 8.0$  pc (7 objects; space density  $> 3.26 \times 10^{-3} \text{ pc}^{-3}$ ), although the numbers are still within the  $1\sigma$  envelope at  $d = 9.0$  pc for a sample of 7 objects (space density  $> 2.29 \times 10^{-3} \text{ pc}^{-3}$ ). We make no claims about the completeness limits of the 150-300K bin since it has only one known object in it. Hereafter, we will take the values determined from the last crossing of  $\langle V/V_{max} \rangle \approx 0.5$  to be the measured space density, and we will use the difference between that number and the space density derived from the  $1\sigma$  envelope to be the  $1\sigma$  uncertainty.

We can also use another method to determine when our measured value of  $\langle V/V_{max} \rangle$  is significantly different from 0.5, given the size of our sample. We take the completeness limit and sample size judged from our analysis above and determine what the  $1\sigma$  variation in  $\langle V/V_{max} \rangle$  would be for a uniform but randomly distributed population of the same size simulated via 10,000 Monte Carlo trials (see Smart et al., in prep.) We measure the  $1\sigma$  variation in 0.5-pc steps up to the distance corresponding to our distance limit, and plot these in brown on Figure 15. In general, these variations are smaller than the ones determined by our method above. However, this method assumes a completeness at a set distance and predicts the variations likely to be seen at smaller distances. The previous method, on the other hand, predicts the likelihood of a uniform sample at each distance interval given the number of objects internal to that distance. Because it is a more direct measurement, we will continue to use the previous method to judge our completeness limits, and we further note that it also gives us more conservative estimates on our uncertainties.

Now that we have judged completeness in distance, we must further judge whether the sky distribution itself indicates a deficiency of objects toward the Galactic Plane. If we divide the hemisphere into eight equal-area slices cut along lines of constant  $b = 0^\circ 00, \pm 14^\circ 47, \pm 30^\circ 00, \text{ and } \pm 48^\circ 59$ , we find 23, 24, 23, 10, 11, 17, 23, and 21 objects starting with the northernmost piece and ending with the southern-

**Table 12.** Space Density Measurements for Early-L through Early-Y Dwarfs

$T_{\text{eff}}$	Completeness	No. of	Adjustment	Adopted
Range	Limit	Objects	Factor	Space Density
(K)	(pc)			( $\times 10^{-3} \text{ pc}^{-3}$ )
(1)	(2)	(3)	(4)	(5)
1950-2100	20.0	19	1.00	$0.57 \pm 0.20$
1800-1950	20.0	16	1.00	$0.48 \pm 0.12$
1650-1800	20.0	21	1.00	$0.63 \pm 0.09$
1500-1650	20.0	26	1.00	$0.78 \pm 0.11$
1350-1500	...	...	...	...
1200-1350	...	...	...	...
1050-1200	...	...	...	...
900-1050	19.0	29	1.15	$> 1.16$
750-900	17.0	30	1.15	$1.68 \pm 0.23$
600-750	16.0	53	1.15	$3.55 \pm 0.51$
450-600	12.5	32	1.15	$4.50 \pm 0.81$
300-450	8.0	7	1.15	$> 3.75$
150-300	—	1	—	—

most. Indeed, there is a clear deficit concentrated toward the Galactic Plane. To account for this deficit, we multiply our derived space density values by  $(4/3)(\text{total number with } |b| > 14^\circ 47) / (\text{total number at all } b \text{ values}) = (4/3)(131)/152 = 1.15$  to account for the missing objects toward the Plane. With this correction factor in hand, we derive our adopted space densities and their uncertainties as listed in Table 12.

### 9.3.2. Early- to Mid-L Dwarfs

Because our mass function simulations predict only relative space densities, our best metric for determining which simulation  $T_{\text{eff}}$  distributions best fit the data would be to have another set of space densities measured in a temperature range far removed from the late-T and Y dwarfs. The Baraffe et al. (2003) and Saumon & Marley (2008) models are both valid between 300K and 2500K, so we will determine space densities for objects at the upper end of this  $T_{\text{eff}}$  range.

Objects at 2500K land near the boundary between late-M dwarfs and early-L dwarfs (see Figure 9.19 of Gray & Corbally 2009). Fortunately, we can create a complete, volume-limited census of early- to mid-L dwarfs with reasonable ease, in no small part because these objects are much rarer than their late-T and Y brethren. One of us (CRG) has recently updated the data underlying the DwarfArchives<sup>9</sup> com-

<sup>9</sup> See <http://DwarfArchives.org>

pilation of published L, T, and Y dwarfs, so we used this to extract the list. All objects having either an optical or a near-infrared type from L0 to L5 were retained. Those with pre-*Gaia* parallaxes placing them within 20 pc of the Sun were kept. For the rest, we used the compiled *J*, *H*, and *W2* magnitudes along with their spectral types to compute spectrophotometric distance estimates using the spectral type to absolute magnitude relations presented in [Filippazzo, et al. \(2015\)](#) for field dwarfs and in [Faherty et al. \(2016\)](#) for low-gravity (young) dwarfs, whichever was applicable based on the spectral type. In order to ensure a complete 20-pc sample, we retained all objects having distance estimates of  $<23$  pc. We then consulted *Gaia* DR2 to obtain parallaxes of these

objects and dropped any whose *Gaia* data ruled out membership in the 20-pc sample. Of the ninety-one objects, only six lacked parallaxes from either *Gaia* DR2 or another published source.

The full list is presented in [Table 13](#). We list the discovery name and coordinates in column 1, the discovery reference in column 2, the adopted parallax and reference in columns 3 and 4, the optical spectral type and reference in columns 5 and 6, the near-infrared spectral type and reference in columns 7 and 8, approximate Galactic coordinates in column 9, and the final adopted type (for use in the discussion below) in column 10.

**Table 13.** The 20-pc Census of L0 to L5.5 Dwarfs

Name and J2000 Coords.	Disc. Ref.	Parallax <sup>a</sup> (mas)	Par. Ref.	Opt. Sp. Ty.	Opt. Ref.	NIR Sp. Ty.	NIR Ref.	( <i>l</i> , <i>b</i> ) (deg)	Adopt. Type
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)
GJ 1001B (J0004-4044B)	1	82.0946±0.3768	68	...	...	L5	2	335.3 -73.3	5
GJ 1001C (J0004-4044C)	16	82.0946±0.3768	68	...	...	L5	2	335.3 -73.3	5
2MASS J00145575-4844171	3	50.1064±0.3898	68	L2.5 pec	3	L2.5±1	4	318.6 -67.2	2.5
2MASSW J0015447+351603	5	58.6085±0.3664	68	L2	5	L1.0	6	114.7 -27.0	1.5
2MASSW J0036159+182110	7	114.4167±0.2088	68	L3.5	7	L4±1	8	117.8 -44.3	3.5
2MASSW J0045214+163445	9	65.0151±0.2274	68	L2 $\beta$	10	L2 $\gamma$	18,75	120.8 -46.2	2 yng
2MASS J01282664-5545343	11	54.0168±0.2345	68	L2	12	L1	11	292.3 -60.5	1.5
2MASS J01443536-0716142	13	79.0319±0.6240	68	L5	13	L6.5	14	157.7 -66.4	5.5
2MASSI J0213288+444445	15	51.6812±0.3832	68	L1.5	15	...	...	137.9 -15.7	1.5
2MASSI J0251148-035245	15	90.62±3.02	69	L3	15	L1	9	179.0 -53.1	2
2MASS J03140344+1603056	17	73.4296±0.2757	68	L0	17	M9.4	6	165.8 -34.6	0
2MASS J03552337+1133437	17	109.6451±0.7368	68	L5 $\gamma$	10	L3-L6 $\gamma$	75	178.1 -30.9	5 yng
WISE J040137.21+284951.7	19	80.2894±0.2615	68	L3	19	L2.5	19	165.6 -17.8	3
WISE J040418.01+412735.6	19	61.7516±0.4163	68	L2	19	L2 pec (red)	19	157.3 -08.1	2
2MASSI J0445538-304820	15	61.9685±0.1843	68	L2	15	...	...	231.8 -39.1	2
2MASS J05002100+0330501	17	76.2093±0.3565	68	L4	17	L4.1	6	196.1 -22.7	4
2MASSI J0512063-294954	15	54	74	L5 $\gamma$	75	L5 $\beta$	75	232.2 -33.4	5 yng
2MASSI J0523382-140302	15	78.3632±0.1855	68	L2.5	15	L5	9	216.1 -25.6	3.5
SDSSp J053951.99-005902.0	21	78.5318±0.5707	68	L5	21	L5	22	205.4 -16.3	5
LSR J0602+3910	23	85.6140±0.1663	68	L1	23	L2 $\beta$	75	172.8 +08.1	1.5 yng
2MASS J06244595-4521548	17	81.6233±0.4986	68	L5	17	L5	24	253.4 -23.3	5
2MASS J06411840-4322329	12	51.2819±0.1930	68	L1.5	12	L2.4:	6	252.3 -19.9	2
2MASSI J0652307+471034	15	109.6858±0.4380	68	L4.5	15	...	...	169.1 +19.7	4.5
2MASS J07003664+3157266A	25	88.2790±0.3479	68	L3.5	17	L3±1	2	184.6 +15.7	3.5
WISEA J071552.38-114532.9	26	55.5855±0.3446	68	...	...	L4 pec (blue)	26	226.1 -00.0	4
2MASS J07414279-0506464A	77	53	77	...	...	L5	77,78	223.3 +08.7	5
2MASS J07414279-0506464B	77	53	77	...	...	L5	77,78	223.3 +08.7	5
2MASSI J0746425+200032A	7	81.9±0.3	70	L0	28	...	...	200.4 +20.8	0
2MASSI J0746425+200032B	27	81.9±0.3	70	L1.5	28	...	...	200.4 +20.8	1.5
DENIS-P J0751164-253043	29	56.5689±0.1555	68	L1.5	29	L1.1	6	242.2 +00.6	1.5
SSSPM J0829-1309	30	85.5438±0.1720	68	L2	30	...	...	236.3 +14.6	2

Table 13 continued

Table 13 (continued)

Name and J2000 Coords.	Disc. Ref.	Parallax <sup>a</sup> (mas)	Par. Ref.	Opt. Sp. Ty.	Opt. Ref.	NIR Sp. Ty.	NIR Ref.	( <i>l</i> , <i>b</i> ) (deg)	Adopt. Type
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)
2MASS J0847287-153237	15	56.9235±0.3167	68	L2	15	...	...	241.1 +17.0	2
SIPS J0921-2104	17,31	79.3128±0.2253	68	L2	17	L4: (blue)	32,33	250.9 +19.9	3
2MASSW J1004392-333518 <sup>b</sup>	35	53.2798±0.5684	68	L4	35	...	...	267.4 +17.5	4
2MASS J10224821+5825453	12	54.3331±0.3143	68	L1 $\beta$	10	L1	12	152.0 +49.4	1 yng
2MASS J1029216+162652	5	52.3361±0.7414	68	L2.5	5	L2.8	6	223.4 +55.4	2.5
SDSS J104523.98-014957.7	36	58.6576±0.2384	68	L1	36	L1	12	251.5 +48.0	1
SDSS J104842.84+011158.5	36	66.4589±0.2143	68	L1	36	L4	37	249.1 +50.7	2.5
2MASS J10511900+5613086	17	63.9956±0.1886	68	L2	17	L0.8	6	151.0 +53.8	1.5
DENIS-P J1058.7-1548	38	54.6468±0.5213	68	L3	39	L3	22	267.1 +39.1	3
2MASS J1104012+195921	40	55.9160±0.4448	68	L4.5	40	L4	41	223.3 +64.4	4.5
2MASSW J1108307+683017	42	61.3537±0.1985	68	L1 $\gamma$	75	L1 $\gamma$	75	136.1 +45.8	1 yng
2MASS J11263991-5003550	43	59.38±1.64	71	L4.5	32	L6.5± pec	32	289.2 +10.5	5.5
2MASSW J1155395-372735	35	84.5693±0.1867	68	L2	35	L2.3	6	290.8 +24.0	2
SDSSp J120358.19+001550.3	21	67.2362±0.5553	68	L3	21	L5.0	6	277.9 +60.8	4
2MASS J1213033-043243	15	59.4765±1.0156	68	L5	15	L4.2	6	285.1 +56.9	4.5
2MASS J12212770+0257198	17	53.9501±0.2528	68	L0	17	L0.5	14	285.1 +64.7	0
DENIS-P J1253108-570924	29	60.0190±0.2612	68	L0.5	29	...	...	303.1 +05.7	0.5
2MASSW J1300425+191235	42	71.6755±0.2012	68	L1	42	L3 (blue)	32	318.4 +81.8	2
Kelu-1A (J1305-2541A)	44	53.8492±0.7107	68	L3	46	L1.5-L3	45	306.9 +37.0	2.5
Kelu-1B (J1305-2541B)	45	53.8492±0.7107	68	L3	46	L3-L4.5	45	306.9 +37.0	3
Gl499C (J1305+2046)	15	50.4348±0.8447	68	L5	47	L6.5	6	330.8 +82.8	5.5
DENIS-P J142527.97-365023.4	37	84.5181±0.3435	68	L3	50	L4 $\gamma$	75	323.1 +22.3	3.5 yng
2MASSW J1439284+192915	39	69.6±0.5	70	L1	39	L1	14	021.5 +64.1	1
G 239-25B	16	91.7062±0.2434	68	...	...	L0	51	106.7 +47.4	0
2MASSW J1448256+103159	9	71.2548±0.7233	68	L5	17	L3.5	24	007.4 +57.8	4.5
Gl 564B (J1450+2354B)	52	54.9068±0.0684	68	...	...	L4	53	032.7 +63.0	4
Gl 564C (J1450+2354C)	52	54.9068±0.0684	68	...	...	L4	53	032.7 +63.0	4
DENIS-P J1454078-660447	29	93.2242±0.3013	68	L3.5	29	...	...	314.9 -06.1	3.5
2MASSW J1506544+132106	42	85.5810±0.2883	68	L3	42	L4	24	016.2 +55.5	3.5
2MASSW J1507476-162738	7	135.2332±0.3274	68	L5	7	L5.5	8	344.1 +35.2	5
2MASS J15200224-4422419A	11	54.4581±0.2465	68	...	...	L1.5	54	329.0 +10.8	1.5
2MASS J15200224-4422419B	11	53.6580±0.6308	68	...	...	L4.5	54	329.0 +10.8	4.5
DENIS-P J153941.96-052042.4	37	58.8245±0.4213	68	L3.5	12	L4.0	24	000.7 +37.9	3.5
2MASSW J1555157-095605	35	73.6519±0.1870	68	L1	35	L1.6	6	359.5 +32.0	1
2MASSW J1615441+355900	5	50.0611±0.3713	68	L3	5	L3.6	6	057.7 +46.0	3
2MASSW J1645221-131951	35	88.8220±0.1444	68	L1.5	35	...	...	005.1 +20.3	1.5
2MASSW J1658037+702701	42	54.1172±0.2058	68	L1	42	...	...	101.9 +34.8	1
DENIS-P J170548.38-051645.7	37	52.6734±0.3516	68	L0.5	17	L1.0	24	015.2 +20.6	0.5
2MASS J17065487-1314396	76	51.4814±0.5128	68	...	...	L5 pec	76	008.3 +16.0	5
2MASS J17072343-0558249B	56	85.0112±0.4386	68	...	...	L3	56	014.8 +19.9	3
2MASS J1721039+334415	15	61.3203±0.2050	68	L3	15	L5±1 (blue)	32	057.3 +32.5	4
VVV J172640.2-273803	57	53.9938±0.3612	68	...	...	L5±1 (blue)	57	358.8 +04.2	5
2MASS J17312974+2721233	17	83.7364±0.1182	68	L0	17	L0	12	050.8 +28.6	0
DENIS-P J1733423-165449	29	55.3156±0.3564	68	L1.0	29	L0.9	6	008.8 +08.6	1
DENIS-P J1745346-164053	29	51.0274±0.2957	68	L1.5	29	L1.3	6	010.4 +06.3	1.5
2MASS J17502484-0016151	11	108.2676±0.2552	68	L5.0	59	L5.5	11	025.5 +13.4	5

Table 13 continued



Table 13 (continued)

Name and J2000 Coords.	Disc. Ref.	Parallax <sup>a</sup> (mas)	Par. Ref.	Opt. Sp. Ty.	Opt. Ref.	NIR Sp. Ty.	NIR Ref.	( <i>l, b</i> ) (deg)	Adopt. Type
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)
2MASS J17534518-6559559	17	63.8219±0.3244	68	L4	17	...	...	327.5 -19.0	4
WISE J180001.15-155927.2	60	89	74	L4.5	55	L4.3	6	012.8 +03.7	4.5
2MASS J1807159+501531	9	68.3317±0.1280	68	L1.5	15	L1	9	077.9 +27.3	1.5
2MASS J18212815+1414010	61	106.8740±0.2518	68	L4.5	61	L5 pec (red)	61	042.4 +12.9	4.5
WISEP J190648.47+401106.8	62	59.5710±0.1363	68	...	...	L1	62	071.0 +14.4	1
GI 779B (J2004+1704B)	63	56.28±0.35	73	...	...	L4.5±1.5	63	056.5 -07.5	4.5
DENIS-P J205754.1-025229	64	64.4710±0.2365	68	L1.5	15	L2 $\beta$	75	045.7 -29.2	1.5 yng
2MASS J2104149-103736	15	58.1658±0.4051	68	L2.5	3	L2.0	24	038.5 -34.2	2.5
2MASS J21373742+0808463	12	66.0620±0.8664	68	L5:	12	L5.0	24	062.8 -31.3	5
2MASS J21580457-1550098	65	52	74	L4:	3	L5.0	24	039.5 -48.3	4.5
2MASSW J2224438-015852	5	86.6169±0.7080	68	L4.5	5	L4.5 pec (red)	66	062.2 -46.8	4.5
2MASS J22551861-5713056A	11	58.8576±0.5866	68	...	...	L5.5:	67	329.2 -53.5	5.5
2MASS J23174712-4838501	12	62	74	L4 pec	33	L6.5 pec (red)	33	336.7 -61.8	5
2MASS J23224684-3133231	12	50.3213±0.5576	68	L0 $\beta$	12	L2 $\beta$	18,75	014.6 -70.2	0 yng

<sup>a</sup> Values in italics are spectrophotometric distance estimates, derived as explained in the text.

<sup>b</sup> This object is a possible common proper motion companion to LP 903-20 (LHS 5166).

NOTE—References to discovery and spectral classification papers: (1) EROS Collaboration, et al. 1999, (2) Dupuy & Liu 2012, (3) Kirkpatrick, et al. 2008, (4) Marocco, et al. 2013, (5) Kirkpatrick, et al. 2000, (6) Bardalez Gagliuffi, et al. 2014, (7) Reid, et al. 2000, (8) Knapp et al. 2004, (9) Wilson, et al. 2003, (10) Cruz et al. 2009, (11) Kendall et al. 2007, (12) Reid et al. 2008, (13) Liebert, et al. 2003, (14) Schneider, et al. 2014, (15) Cruz, et al. 2003, (16) Golimowski et al. 2004, (17) Reid, et al. 2006, (18) Allers & Liu 2013, (19) Castro et al. 2013, (20) Cruz, et al. 2007, (21) Fan, et al. 2000, (22) Geballe, et al. 2002, (23) Salim, et al. 2003, (24) Burgasser, et al. 2010, (25) Thorstensen & Kirkpatrick 2003, (26) Kirkpatrick et al. 2014, (27) Reid, et al. 2001, (28) Bouy, et al. 2004, (29) Phan-Bao, et al. 2008, (30) Scholz & Meusinger 2002, (31) Deacon, et al. 2005, (32) Burgasser, et al. 2008, (33) Kirkpatrick, et al. 2010, (34) Schmidt, et al. 2010, (35) Gizis 2002, (36) Hawley, et al. 2002, (37) Kendall, et al. 2004, (38) Delfosse et al. 1997, (39) Kirkpatrick, et al. 1999, (40) Bouy, et al. 2003, (41) Geiβler, et al. 2011, (42) Gizis, et al. 2000, (43) Folkes, et al. 2007, (44) Ruiz et al. 1997, (45) Liu & Leggett 2005, (46) Koen, et al. 2017, (47) Gomes, et al. 2013, (48) Luhman 2014a, (49) Kirkpatrick, et al. 2016, (50) Schmidt, et al. 2007, (51) Forveille, et al. 2004, (52) Potter, et al. 2002, (53) Goto, et al. 2002, (54) Burgasser, et al. 2007, (55) West, et al. 2008, (56) Burgasser et al. 2004, (57) Beamín, et al. 2013, (58) Schneider et al. 2017, (59) Metodieva, et al. 2015, (60) Folkes, et al. 2012, (61) Looper, et al. 2008, (62) Gizis, et al. 2011, (63) Liu, et al. 2002, (64) Ménard, et al. 2002, (65) Gizis, et al. 2003, (66) Cushing, et al. 2005, (67) Reid, et al. 2008, (68) Gaia Data Release 2: Gaia Collaboration et al. 2016 and Gaia Collaboration et al. 2018, (69) Bartlett, et al. 2017, (70) Dahn, et al. 2002, (71) Dieterich, et al. 2014, (72) Dahn et al. 2017, (73) Hipparcos: van Leeuwen 2007, (74) This paper, (75) Faherty et al. 2016, (76) Gagné, et al. 2015, (77) Scholz & Bell 2018, (78) Cushing et al. 2018.

The adopted spectral types were determined as follows. For field objects, we averaged the optical and near-infrared types, but rounded any decimal type from Bardalez Gagliuffi, et al. (2014) to its nearest half-type beforehand. For those averages landing at a quarter or three-quarters type, we chose the closest half type that fell in the direction of the optical value. For young objects, the optical type is used as the adopted type, unless only the near-infrared type is noted as low-gravity, in which case the averaging used above for the field objects is employed.

As was done with the late-T and Y dwarfs in the last section, we need to place these objects on a  $T_{\text{eff}}$  scale. Faherty et al. (2016) provide a mapping from spectral type to  $T_{\text{eff}}$  for the L dwarfs. They find that this mapping depends upon the age of the L dwarf. In the early- to mid-L dwarf range, young (low-gravity), higher mass L dwarfs have slightly colder  $T_{\text{eff}}$  values compared to old field L dwarfs of the same spectral subclass (see their Figure 33). We note that the Faherty et al. (2016) spectral type relation (which is the same one deter-

mined in Filippazzo, et al. (2015)) for field L dwarfs gives a  $\sim 150\text{K}$  range for each full spectral class at early L, but this shrinks to  $\sim 100\text{K}$  per full spectral class by mid-L. As shown in Table 14, we thus map field spectral types into  $T_{\text{eff}}$  as follows: L1-L1.5 is mapped to the 1950-2100K bin, L2-L2.5 to 1800-1950K, L3-L3.5-L4 to 1650-1800K, and L4.5-L5-L5.5 to 1500-1650K.

The adopted types of the young, low-gravity L dwarfs are mapped to  $T_{\text{eff}}$  using the "YNG" relations of Faherty et al. (2016)<sup>10</sup> Specifically, the mapping into our 150K bins is L0-L0.5-L1 for 1950-2100K, L1.5-L2-L2.5 for 1800-1950K, L3-L3.5 for 1650-1800K, and L4 for 1500-1650K. Note that the young L dwarfs of type L4.5 and later from Table 13 fall in a cooler bin for which later-type field L dwarfs ( $\geq L6$ ) are expected to have poorer coverage out to 20 pc by Gaia. Like-

<sup>10</sup> Note that in Table 19 of Faherty et al. (2016), the coefficients of the  $T_{\text{eff}}$  YNG relation are accidentally listed in reverse order. Coefficient  $c_0$  is actually  $c_4$ ,  $c_1$  is actually  $c_3$ , etc.

**Table 14.** Analysis of the 20-pc Census for  $1500 < T_{\text{eff}} < 2100\text{K}$ 

$T_{\text{eff}}$ range	Type range	Type range	Total	Completeness
(K)	Field obj.	Young obj.	Number	of Gaia DR2 <sup>a</sup>
(1)	(2)	(3)	(4)	(5)
1950-2100	L1, L1.5	L0, L0.5, L1	19	89%
1800-1950	L2, L2.5	L1.5, L2, L2.5	16	94%
1650-1800	L3, L3.5, L4	L3, L3.5	21	100%
1500-1650	L4.5, L5, L5.5	L4	26	73%

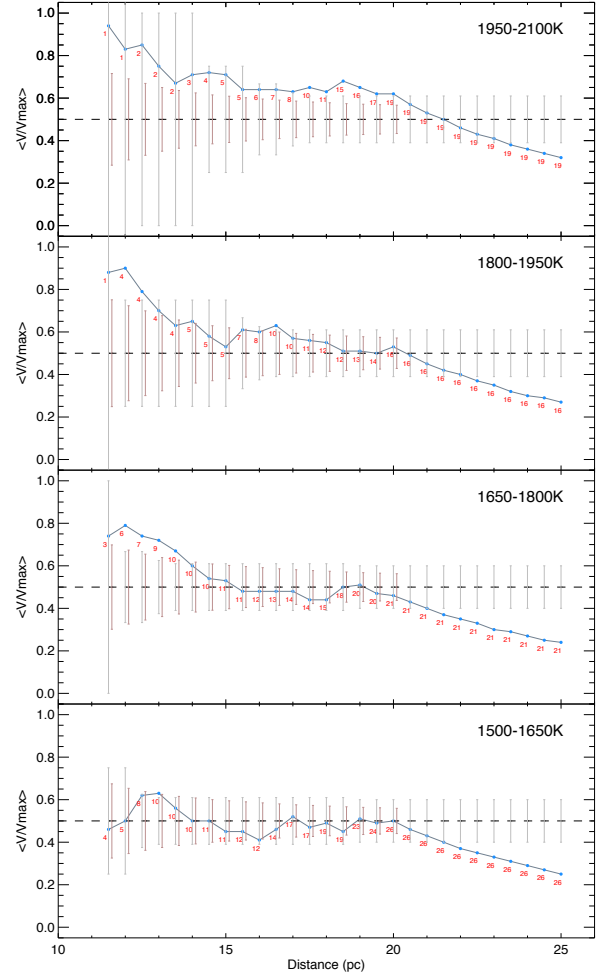
<sup>a</sup> This is the percentage of objects with parallaxes listed in the Second Data Release from Gaia.

wise, old field objects in Table 13 that are earlier in type than L0 share a temperature bin containing low-gravity late-M dwarfs, which we have not tabulated because DwarfArchives does not track objects with M dwarf types. Hence, not all objects in Table 13 were used in the space density arguments that follow.

In Table 14 we list the aforementioned mapping of types into each 150K bin along with the number of objects found in each range. Because these objects were drawn from the literature using ground-based parallaxes and spectrophotometric distance estimates, we can use them to check the completeness of the *Gaia* DR2 sample over our spectral type and distance range. Overall we find that DR2 is 88% complete for early- to mid-L dwarfs within 20 pc, with the completeness dropping at later types as expected, given *Gaia*'s reduced sensitivity to those fainter objects.

Figure 16 shows the results of our  $\langle V/V_{\text{max}} \rangle$  test on this L dwarf sample. In all four temperature bins, we are within  $1\sigma$  of the expected  $\langle V/V_{\text{max}} \rangle$  value of 0.5 at  $d = 20.0$  pc, giving space densities of  $0.57 \times 10^{-3} \text{ pc}^{-3}$  (19 objects) for the 1950-2100K bin,  $0.48 \times 10^{-3} \text{ pc}^{-3}$  (16 objects) for the 1800-1950K bin,  $0.63 \times 10^{-3} \text{ pc}^{-3}$  (21 objects) for the 1650-1800K bin, and  $0.78 \times 10^{-3} \text{ pc}^{-3}$  (26 objects) for the 1500-1650K bin. The values of  $\langle V/V_{\text{max}} \rangle$  are still within the  $1\sigma$  envelope at 23.0, 22.0, 21.0, and 21.0 pc for the four bins, giving densities of  $0.37 \times 10^{-3} \text{ pc}^{-3}$ ,  $0.36 \times 10^{-3} \text{ pc}^{-3}$ ,  $0.54 \times 10^{-3} \text{ pc}^{-3}$ , and  $0.67 \times 10^{-3} \text{ pc}^{-3}$ . We use the differences between these latter densities and the ones at our 20-pc limit as the  $1\sigma$  uncertainties in our measurements. These values are listed in Table 12 along with the ones measured earlier for the late-T and Y dwarfs.

Unlike for the late-T and Y dwarfs, we find that this sample has no obvious incompleteness along the Galactic Plane. Because of the poorer statistics, we divide the celestial sphere into only four equal-area pieces sliced along lines of constant  $b$  values of  $+30^\circ$ ,  $0^\circ$ , and  $-30^\circ$ . We find 25, 25, 14, and 16 objects starting with the northernmost piece and ending with



**Figure 16.** The average  $V/V_{\text{max}}$  value in 0.5-pc intervals for the four 150-K bins encompassing our 20-pc early- to mid-L sample. See the caption to Figure 15 for more details.

the southernmost. This shows that our 20-pc sample of early-L dwarfs lacks an obvious zone of avoidance in the Galactic Plane because  $39/80 = 49\%$  of the sources are concentrated in the 50% of the sky closest to the Plane itself. We can thus assume that the 20-pc sample of 1500-2100K dwarfs is reasonably complete both sky-wide and to the full 20-pc distance limit. Therefore, no adjustment factor (see Table 12) to the measured space densities is needed.

### 9.3.3. A Uniform Distribution of the Nearest Brown Dwarfs

Bihain & Scholz (2016) have posited that the distribution of nearby brown dwarfs on the sky is astonishingly non-uniform. Those authors claim that most of the brown dwarfs with the 6.5-pc volume (21 out of 26 objects) are leading the Sun in its Galactic orbit, with only a handful (the remaining 5) trailing the Sun. They further state that the probability of such a distribution occurring by chance is 0.098%, although the  $2\sigma$  error bar on this quantity pushes it as high as 11%.



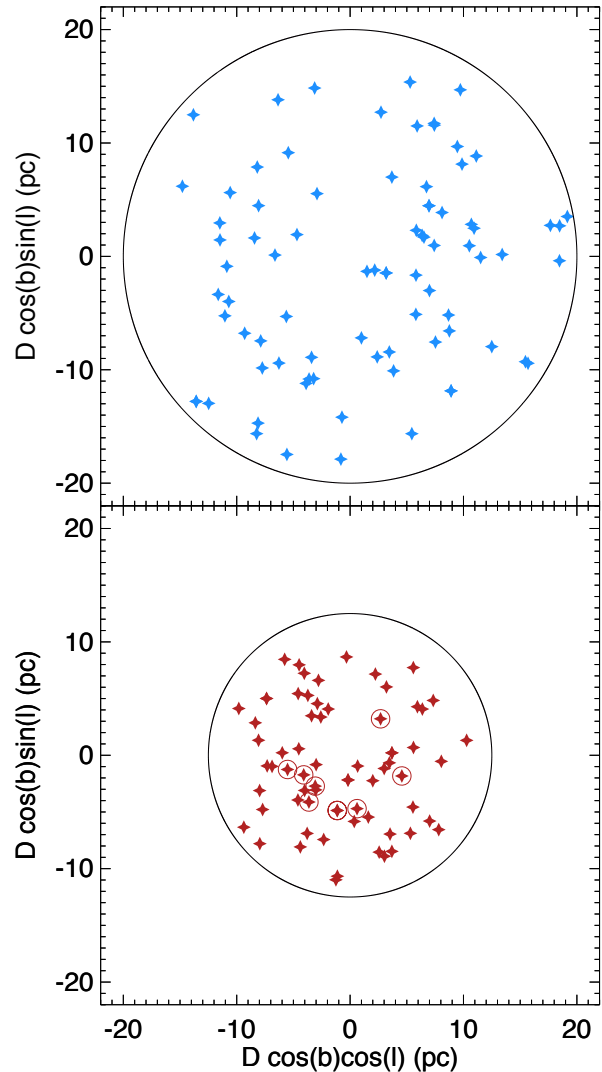
They conjecture that the literature sample of brown dwarfs within 6.5 pc is incomplete due to biases in the methodology being employed to search the all-sky 2MASS and *WISE* data sets, although the ways in which the search criteria might have created such an odd bias are not clearly specified. Alternatively, they suggest that if the sample is complete, or nearly so, it is either caused by some "random inhomogeneity" or an unknown dynamical mechanism causing brown dwarfs to segregate from stars in this manner, as the stellar sample (136 objects within 6.5 pc) shows no such asymmetric distribution.

We show here, using a sample  $\sim 6$  times larger, that nearby brown dwarfs are distributed uniformly and that the Bihain & Scholz (2016) observation is solely the result of the statistics of small numbers. To demonstrate this, we employ our sample of 1500-2100K and 450-900K objects used in the space density measurements of Table 12. The warmer group of objects is comprised of early- to mid-L dwarfs, which includes some low-mass stars as well as brown dwarfs, and the cooler group is comprised of late-T to Y dwarfs, all of which are brown dwarfs. We note also that we have not added any new objects to these samples that weren't already in the 6.5-pc accounting of Bihain & Scholz (2016), with the exception of considering 2MASS 0939–2448 to be an unresolved double (see Section 8.2). Figure 17 shows the sky distribution of these objects on a Galactic projection identical to that used in Figure 1 of Bihain & Scholz (2016). For the 1500-2100K objects, we use the entire sample out to 20 pc since we believe that to be relatively complete, and for the 450-900K objects we use only the subsample out to 12.5 pc since the coolest sub-bin (450–600K) is complete only out to that distance.

Both sets of objects are distributed so that roughly equal numbers are seen in the upper and lower halves of the diagram. We circle objects falling within the same 6.5-pc distance used by Bihain & Scholz (2016) to show that these objects appear, as those authors noted, primarily in the lower half of the diagram. (Note that *none* of the objects in the 1500-2100K range falls within 6.5 pc.) However, this is a result of random statistics on a small sample, as the larger sample shows no such effect. It is very difficult to imagine a selection effect or a dynamical process at work within the 6.5-pc distance that would not also be operating in the distance range from 6.5 to 12.5 pc.

#### 9.3.4. Best Fits to the Space Densities

We can now test which of the seventy-two models in Figures 12 and 13 best match our measured space densities. We use the IDL routine `mpfit` (Markwardt 2009) to perform a weighted least-squares fit between the data and the model where the only adjustable parameter is the scaling between the arbitrary number counts in the models and our measured space densities. For the calculation, we use only the seven values in Table 12 with measured uncertainties (four in the 1500-2100K range and three in the 450-900K range) and ignore the ranges in which we have only lower limits (900-1050K and 300-450K) and the range in which we have only one data point and no measurable space density (150-300K).



**Figure 17.** A Galactic projection plot identical to that in Figure 1 of Bihain & Scholz (2016) showing the distributions of our two samples. The upper panel shows the 1500-2100K sample (82 objects) out to our completeness limit of 20 pc, and the lower panel shows the 450-900K sample (69 objects) out to our completeness limit of 12.5 pc. Objects within 6.5 pc of the Sun are circled individually; no such objects appear in the upper panel.

The best fit to each model produces a reduced  $\chi^2$  value, and we illustrate in Figure 18 the fits for which this value is minimized. For mass functions paired with the evolutionary code of Baraffe et al. (2003), the best fits are given by the power law mass function with  $\alpha = 0.5$  (model D). The single-object log-normal mass function of Chabrier (2001) (model H) is the next best model, although it consistently un-

derpredicts the space densities seen in the 300-750K range. If we consider the lower limit to the space density in the 300-450K bin, we find that for the power-law model there is a preference for the lower-mass cutoffs, with the current data favoring a cutoff no higher than  $\sim 5M_{Jup}$ . The other power law mass functions produced poorer reduced  $\chi^2$  values of  $\sim 7.8$ ,  $\sim 5.2$ ,  $\sim 3.0$ ,  $\sim 3.0$ , and  $\sim 6.2$  for  $\alpha$  values of  $-1.0$ ,  $-0.5$ ,  $0.0$ ,  $+1.0$ , and  $+1.5$  (models A, B, C, E, and F), respectively. The other log-normal mass functions give reduced  $\chi^2$  values of  $\sim 3.8$  and  $\sim 3.2$  for models G and I, respectively. The bi-partite power law mass functions of Kroupa et al. (2013) give much larger reduced  $\chi^2$  values of  $\sim 7.2$ ,  $\sim 4.1$ , and  $\sim 10.2$  for models J, K, and L, respectively.

For mass functions paired with the evolutionary code of Saumon & Marley (2008), we find even better fits. As with the Baraffe et al. (2003) models, the best fits are given by the power law mass function with  $\alpha = 0.5$  (model D), with the single-object log-normal mass function of Chabrier (2001) (model H) being only slightly worse. The log-normal function again underpredicts the space densities in the 300-750K range. The  $\alpha = 0.5$  power law suggests that the cutoff mass is likely no higher than  $\sim 5M_{Jup}$  given our measured lower limit to the space density in the 300-450K bin. The other power law mass functions produced poorer reduced  $\chi^2$  values of  $\sim 8.7$ ,  $\sim 5.7$ ,  $\sim 3.1$ ,  $\sim 2.4$ , and  $\sim 5.6$  for  $\alpha$  values of  $-1.0$ ,  $-0.5$ ,  $0.0$ ,  $+1.0$ , and  $+1.5$  (models A, B, C, E, and F), respectively. The other log-normal mass functions give reduced  $\chi^2$  values of  $\sim 2.0$  and  $\sim 3.1$  for models G and I, respectively, showing that the log-normal function of Chabrier (2003) (model G) produces almost as good a match to the observed data as that from Chabrier (2001) (model H). The bi-partite power law mass functions of Kroupa et al. (2013) give much larger reduced  $\chi^2$  values of  $\sim 12.0$ ,  $\sim 8.8$ , and  $\sim 14.6$  for models J, K, and L, respectively.

Two other points should be noted regarding these preliminary results:

1. As mentioned earlier, there is a clear discriminator present in the 1050-1500K range of the simulations that will determine whether the Baraffe et al. (2003) or Saumon & Marley (2008) evolutionary models are preferred, from the point of view of the mass function. In the six lower panels of Figure 18 based on the Saumon & Marley (2008) models, there is a clear overdensity relative to a simple interpolation between the space densities seen in the 750-900K and 1500-1650K bins that is not present in the six upper panels based on the Baraffe et al. (2003) models. Using a literature update by CRG to the known L and T dwarfs archived at DwarfArchives along with spectrophotometric distance estimates to those still lacking parallax determinations, we find strong evidence that this overdensity is, indeed, present. This can be tested with a large, volume-limited sample of objects in this temperature range, which both the ground-based parallax program of Best et al. (2018) and the Cycle 14 *Spitzer* program 14000 (PI: Kirkpatrick) are currently aiming to do.

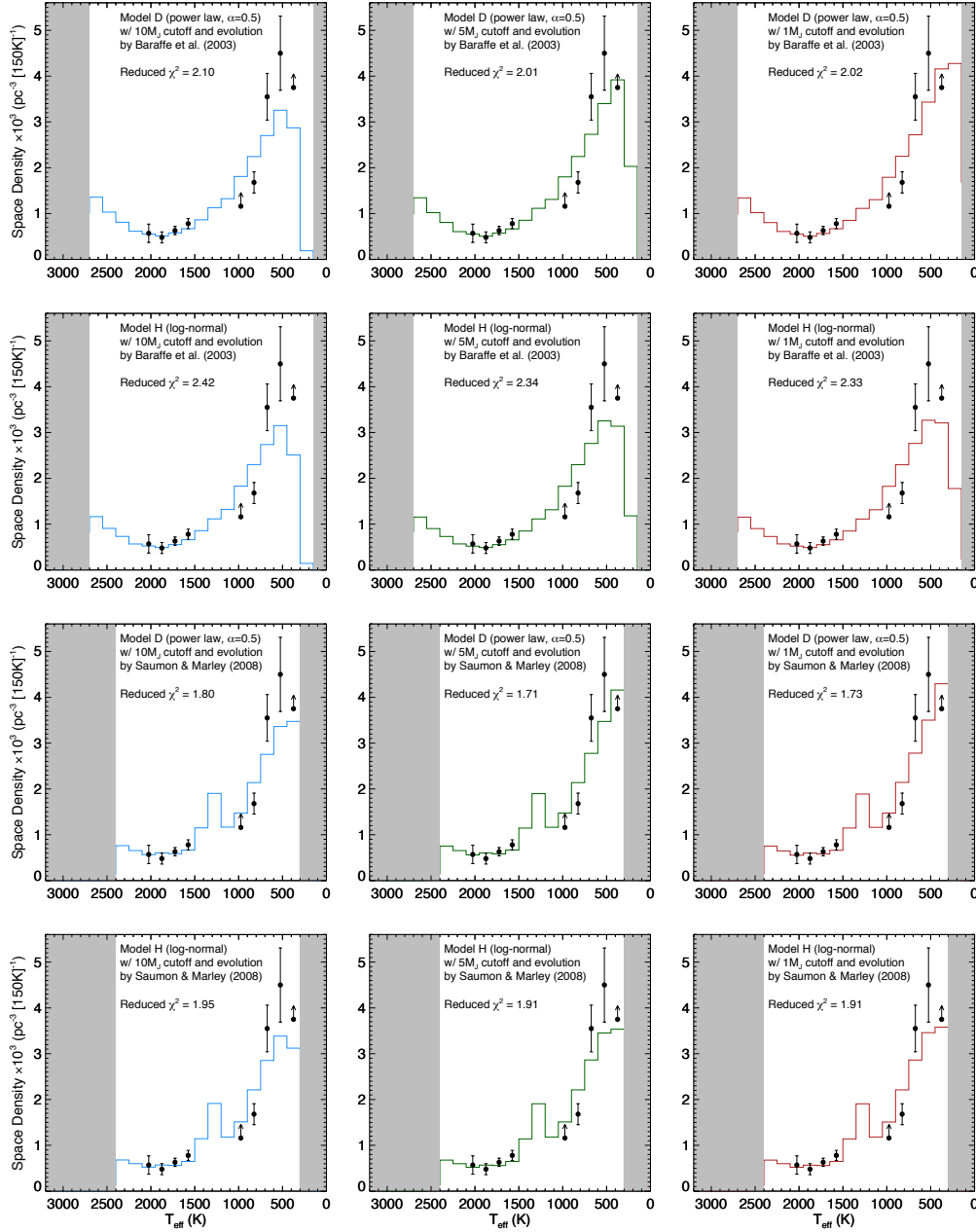
2. As the three panels in the top row of Figure 18 indicate, improving the space density measurement in the 300-450K bin as well as providing a robust lower limit to the density in the 150-300K bin would better help determine the low-mass cutoff of the mass function as the simulations show vast differences in the predicted numbers in these ranges. Current work to find more of these Y dwarfs, which at these temperatures are typically those classified as Y1 and later, is currently underway using proper motion searches afforded by the long time baseline (7+ years) now available between the classic *WISE* and *NEOWISE* Reactivation missions. The prospect for discovering more of these objects looks promising based on early results from the Backyard Worlds Citizen Science project (Kuchner et al. 2017) and CatWISE (Meisner et al. 2018a), but characterizing the spectra of such discoveries and measuring accurate distances will be challenging given the extreme faintness of these objects. (See Section 11 for more discussion on this point.)

Given the success of fitting our observational data to the power law model with  $\alpha = 0.5$ , we searched for even better fits using a smaller grid spacing (increments of 0.1) for  $\alpha$ . We find that the  $\alpha = 0.6$  version using the evolutionary models of Saumon & Marley (2008) results in the lowest overall reduced  $\chi^2$ , as illustrated in Figure 19. The fits to the 1 and 5  $M_{Jup}$  cutoffs are slightly better than the one for the 10  $M_{Jup}$  cutoff. If we assume, based on the  $T_{eff}$  determinations in Table 11, that our coldest bin on Figure 19 is reasonably complete to  $T_{eff} \approx 350K$ , then the simulations predict a mean mass of 16  $M_{Jup}$  with standard deviation of 5  $M_{Jup}$ . (See the figure for the mean mass and age in each  $T_{eff}$  bin.) It should also be stated again that the next coldest bin – the 150-300K bin just off the right side of the plot – has only one known object, WISE 0855–0714, whose mass has been estimated at 3-10  $M_{Jup}$  (Luhman 2014b). Thus, our observations are already beginning to measure the field mass function in the regime below the deuterium-burning limit of  $\sim 13M_{Jup}$ .

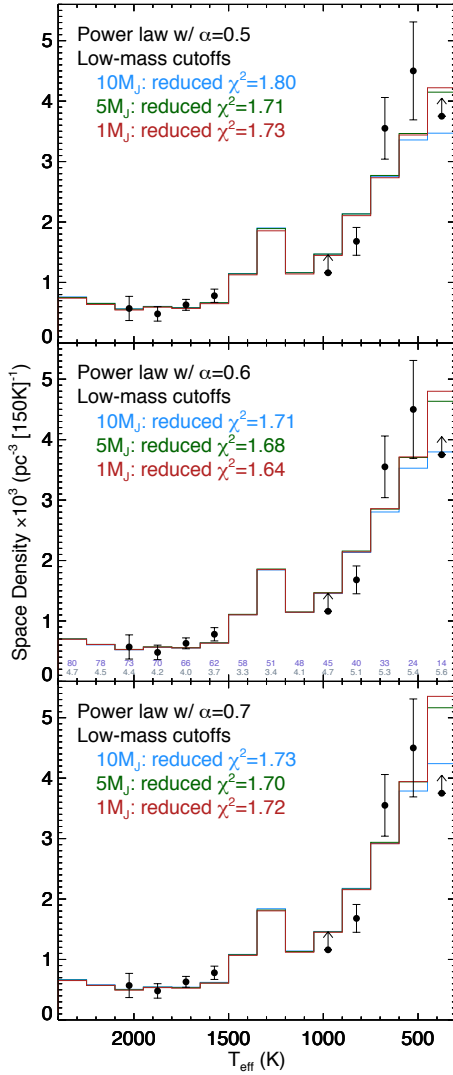
## 10. DISCUSSION

The fitting of our measured space densities to the suite of simulated  $T_{eff}$  distributions in Section 9.3.4 was focused solely on the substellar regime. Here we place these results in context with efforts that have attempted to describe the mass function across the entirety of star formation’s mass spectrum, from  $\sim 100M_{\odot}$  to  $\sim 1M_{Jup}$ .

Specifically, early work by Salpeter (1955) suggested that the stellar mass function at very high masses could be adequately described by a power law with exponent  $\alpha = 2.35$ . Miller & Scalo (1979) found this same power law for  $M > 10M_{\odot}$ , but at lower masses favored a two-piece power law with exponents of  $\alpha = 1.5$  for  $1M_{\odot} < M < 10M_{\odot}$  and  $\alpha = 0.4$  for  $0.1M_{\odot} < M < 1M_{\odot}$ . Kroupa (2001) prefers a three-piece power law in the stellar regime having segments with  $\alpha \approx 2.3$  for  $M > 1.0M_{\odot}$ ,  $\alpha \approx 2.7$  for  $0.5M_{\odot} < M < 1.0M_{\odot}$ , and  $\alpha \approx 1.8$  for  $0.08M_{\odot} < M < 0.5M_{\odot}$ , once the hidden



**Figure 18.** The best fits between the simulations of Figures 12 and 13 and our measured space densities in Table 12. The top two rows show the two mass functions using the Baraffe et al. (2003) evolutionary code that provide the smallest reduced  $\chi^2$  values: the power law with  $\alpha = 0.5$  (top row; Model D) and the single-object log-normal from Chabrier (2003) (second row; Model G). Similarly, the bottom two rows show the two mass functions using the Saumon & Marley (2008) evolutionary code that provide the smallest reduced  $\chi^2$  values: the power law with  $\alpha = 0.5$  (third row; Model D) and the single-object log-normal from Chabrier (2003) (bottom row; Model H). In each row the mass functions are shown with assumed low-mass cutoffs of  $10M_{\text{Jup}}$  (blue, left panels),  $5M_{\text{Jup}}$  (dark green, middle panels), and  $1M_{\text{Jup}}$  (red, right panels). Our measured spaced densities and their uncertainties are show in black on each panel.



**Figure 19.** Fits of power laws with  $\alpha$  values of 0.5 (top panel), 0.6 (middle panel), and 0.7 (bottom panel) to our observational data (black points). These predicted  $T_{\text{eff}}$  distributions have been passed through the evolutionary models of Saumon & Marley (2008). Each panel shows simulations for each of three low-mass cutoffs:  $10 M_{\text{Jup}}$  (blue),  $5 M_{\text{Jup}}$  (green), and  $1 M_{\text{Jup}}$  (red). The minimum reduced  $\chi^2$  value is found for the  $\alpha = 0.6$  model. The numbers in each bin of the middle panel indicate the mean mass (in units of  $M_{\text{Jup}}$ ; upper value in purple) and the mean age (in units of Gyr; lower value in grey) for each  $T_{\text{eff}}$  bin for the model with the  $5 M_{\text{Jup}}$  cutoff.

members of unresolved binaries are properly accounted for. Chabrier (2003) have suggested that over the entire stellar mass range ( $\sim 100 M_{\odot}$  to  $\sim 0.1 M_{\odot}$ ), the mass function can be adequately described by either a log-normal or a two-segment power law.

With the discovery of brown dwarfs in both the field and young clusters, researchers have attempted to describe the mass function into the substellar regime. Kroupa et al. (2013) suggest that brown dwarfs form in a fundamentally differ-

ent way from stars and that the mass function of brown dwarfs is a power law with  $\alpha \approx 0.3$ . However, they state that there is significant overlap in mass between the normal “stellar” portion (a power law with  $\alpha \approx 1.3$ ) of the mass function and the “substellar” part but that the two pieces are discontinuous. Chabrier (2001), on the other hand, prefers a log-normal form, with values<sup>11</sup> of  $\mu = \ln(0.10)$  and  $\sigma = 0.627 \ln(10)$ . These values were later revised to  $\mu = \ln(0.079)$  and  $\sigma = 0.69 \ln(10)$  by Chabrier (2003) and later, as stated by Chabrier et al. (2014), to  $\mu = \ln(0.25)$  and  $\sigma = 0.55 \ln(10)$  by Chabrier (2005).

We find, however, that neither the Kroupa bi-partite power law or the Chabier log-normal forms adequately fit the data even when we allow for the vertical axis scaling (the space density) to be adjusted as a free parameter. Specifically, the Chabier log-normal forms underpredict the number of objects below 650K. Indeed, as Chabrier et al. (2014) note, their preferred values of  $\mu$  and  $\sigma$  from Chabrier (2005) behaves like a power law with a negative  $\alpha$  value below  $T_{\text{eff}} \approx 1300\text{K}$ . Using the two  $\alpha$  values and their break points in mass as suggested by Kroupa et al. (2013), the bi-partite power laws fare even worse; however, these still hold promise, as the individual mass break points and  $\alpha$  values can be fine tuned to provide better fits. This should be possible since our best-fit value of  $\alpha \approx 0.6$  seems to describe the 350-2100K portion of the  $T_{\text{eff}}$  distribution very well. As predicted by Hoffmann et al. (2018), the difference between a log-normal and power-law representation of the mass function at the smallest masses provides a powerful discriminant in distinguishing between formation theories.

Based on a theoretical perspective, Hennebelle & Chabrier (2008) argue that the full stellar + substellar mass function should be described as a power law at the highest masses and a single log-normal form at the lower masses. The same conclusion is reached via a somewhat different formalism by Hopkins (2012), although more recent theoretical considerations by Guszejnov et al. (2018) have raised questions about how both of these methods treated formation at the smallest masses. For these lowest mass objects, the log-normal form implies a single “characteristic” mass governing their formation. Chabrier (2003) argues that using multi-part power laws instead of a log-normal form to describe the mass function necessarily implies that multiple characteristic masses determine the processes of formation for low-mass objects. Multiple (or at least two) characteristic masses may, in fact, be necessary to describe the observational results for low-mass stars and brown dwarfs, as Kroupa et al. (2013) argue. A theoretical formalism for this alternate scenario has been described by Thies et al. (2010).

Finally, we caution that the *field* mass function is the result of formation processes that have occurred in different environments over the last  $\sim 10$  Gyr. If the physics governing star formation in one environment is found to differ substantially

<sup>11</sup> See the footnote in Section 9.1.2 regarding our translation of these  $\mu$  and  $\sigma$  values into a natural logarithm form.



from that in another, disentangling the physics from the resulting mixture may be extremely difficult. For example, the formation of brown dwarfs could be fundamentally different in a low-mass moving group such as the TW Hydrae Association than it is from that operating in a high-mass region such as the Orion Nebula Cluster, where oblation from O star winds and the higher potential for gravitational disruption of forming pre-stellar cores may play critical roles. (If so, such effects are likely to be seen only below  $\sim 30M_{Jup}$  because Andersen et al. (2008) do not see strong evidence for environment-specific effects at higher masses.) The field mass function may, therefore, have utility only in predicting the outcome of galaxy-wide star formation, although it may eventually be used in determining the relative roles that each environmentally dependent process plays in the overall picture.

## 11. CONCLUSIONS AND FUTURE PLANS

We have presented preliminary trigonometric parallaxes for 184 dwarfs with spectral types from T6 through early-Y. The vast majority of these, 142, come from a dedicated *Spitzer*/IRAC ch2 program, with the rest coming from dedicated programs at the USNO, NTT, and UKIRT. We use these parallaxes to produce a 20-pc sample with which we fits trends to various relationships between colors, spectral types, absolute magnitudes, and effective temperatures. We use these parallaxes to determine the distance limits at which our sample is complete for each of five 150K-wide bins ranging over  $300K < T_{\text{eff}} < 1050K$ . We also take a sample of early- to mid-L dwarfs from the literature, supplemented with recent *Gaia* data, to produce a complete 20-pc sample across four hotter 150K-wide bins in the range  $1500K < T_{\text{eff}} < 2100K$ . We compute the observed space densities in these bins and compare to simulations using various forms of the mass function passed through different evolutionary code – either Baraffe et al. (2003) or Saumon & Marley (2008) – to produce predicted distributions as a function of  $T_{\text{eff}}$ . Fits of our observations to these simulations show that a power law with  $\alpha = 0.6$  provides the best match. Functions involving log-normal forms do not fit the observed space densities well at the lowest temperatures and lowest masses. We find that simulations with low-mass cutoffs of  $10 M_{Jup}$  underpredict the number of objects in these same bins, with which we conclude that the low mass cutoff for star formation, if there is one, must be lower than  $\sim 5 M_{Jup}$ , a result corroborated by analysis of the low-mass constituents in nearby young clusters (e.g., Luhman et al. 2016). Obtaining this result for the *field* substellar distribution, however, confirms that the formation of objects this low in mass is not a recent phenomenon but has been occurring over the lifetime of the Milky Way. The predicted mean age (see Figure 19) of objects in the 300-450K, for example, is 5.6 Gyr for a mean mass of  $14 M_{Jup}$ .

These new results represent a vast improvement upon our previous attempt (Kirkpatrick et al. 2012) to derive the shape of the low-mass end of the mass function for several reasons: (1) There have been six additional years of follow-up

by the entire community of brown dwarf researchers to uncover late-T and Y dwarfs in the Solar Neighborhood, so we have benefited in this paper from a larger sample of objects. (2) Rather than using measured parallaxes for a handful of objects and extending those via spectrophotometric distance estimates to the others, we now have actual trigonometric parallaxes for (almost) the entire sample. (3) With actual parallaxes in hand, we can eliminate unresolved interlopers that would fall within our volume based on their spectrophotometric distances, and for objects still within the volume, we can better access which objects are likely to be unresolved binaries themselves. (4) We have created a new suite of mass function simulations, some tied to newer and more realistic evolutionary models, that better incorporate the complexities of cooling across the brown dwarf sequence. In Kirkpatrick et al. (2012), we concluded that the brown dwarf segment of the mass function most closely approximated a power-law with  $\alpha \approx 0.0$ , but if we used a normalization based on the space density of low-mass *stellar* objects, this power law overpredicted our counts by a factor of 2-3. In this paper, we fit the brown dwarf segment independently and find that much steeper power-law is indicated, with  $\alpha \approx 0.6$ . This number is much closer to the  $\alpha$  values of the brown dwarf mass function found in the Pleiades ( $\sim 0.6$ ; Bouvier et al. 1998; Casewell et al. 2007) as well as other young clusters (typically  $\sim 0.5$ ; see review by Luhman 2012) and star forming regions ( $\lesssim 0.5$ ; see review by Bastian et al. 2010).

We will be able to improve upon the results in this paper in several ways. The tabulated parallaxes and their uncertainties should continue to improve for our *Spitzer* sample of 142 targets as there is a final year of Cycle 13 observations currently underway. The measured parallaxes for objects in the USNO, NTT, and UKIRT parallax programs will also continue to improve, as those results presented here are also regarded as preliminary. For our *Spitzer* targets with large ( $> 2$ ) reduced  $\chi^2$  values in their astrometric fits, we will obtain an additional year of data in Cycle 14 to monitor whether the residuals in the fits show signs of periodicity related to unseen companions. In Cycle 14, we will also be acquiring astrometric data in IRAC ch2 of the 20-pc L dwarf sample in the missing 1050-1500K  $T_{\text{eff}}$  interval of Table 12 as well as obtaining astrometry for those T dwarfs in Table 11 lacking parallax measurements. Other improvements for our continued analysis includes the use of *Gaia* DR2 data to tie directly to the absolute astrometric reference frame for the individual *Spitzer* exposures, as parallactic solutions for most of our reference stars are available; this will obviate the need for a correction from relative to absolute astrometry at a later step. Moreover, as the community of nearby star researchers continues to scour the *Gaia* DR2 data, volume-limited samples of the omnipresent M dwarfs will finally become published out to  $\sim 20$  pc or more, enabling us to check how the brown dwarf power law segment found in this paper dovetails with the low-mass end of the field stellar mass function.

Most pressing, however, is the need to uncover even colder objects that will enable us to determine more accurately the low-mass cutoff of star formation and to discern if the power-

law form continues to describe the observed space density at the coldest temperatures. In this regard, we need to complete the census of the coldest members in the 300–450K bin, and find more objects that occupy the 150–300K bin with WISE 0855–0714 (see Table 12). For this we need an all-sky data set probing wavelengths where these objects are brightest, and  $\sim 5\mu\text{m}$  images from *WISE* will likely be the only ones capable of providing that info for many years to come. Presently, two efforts are underway to discover more Y dwarfs using these data. The first is the Citizen Scientist project Backyard Worlds (Faherty et al. 2018) and the second is a NASA-funded ADAP proposal led by Peter Eisenhardt called CatWISE. Backyard Worlds is taking the unWISE coadds (Lang 2014; Meisner et al. 2017a,b) spanning several years of the *WISE* and *NEOWISE* missions and creating blinking coadds on which members of the public can identify moving objects. CatWISE is taking epochal versions of the unWISE coadds (Meisner et al. 2018b) and running an AllWISE-style processing (Cutri et al. 2013; Kirkpatrick et al. 2014) on them to measure proper motions for all detected sources. For both, the main advantage over previous *WISE* data sets is that motions over a long,  $\sim 7$ -year time baseline can now be used to uncover nearby objects, freeing selections from relying on color to identify cold objects that may be detected only weakly at W2 and undetected in W2. (Previous motion searches with *WISE* data by Luhman 2014a; Luhman & Sheppard 2014; Kirkpatrick et al. 2014; Kirkpatrick, et al. 2016 and Schneider et al. 2016 were limited by a small 0.5-yr time baseline, shallow individual frame depths, or both.) Obtaining imaging and spectroscopic characterization of cold discoveries from both programs will be possible using current ground-based and space-based assets, although for the coldest discoveries, given their extreme faintness, obtaining spectra will likely have to wait for the launch of the *James Webb Space Telescope*. Sadly, once *Spitzer* ceases operations there will be no obvious instrumentation with which to obtain the much needed parallaxes for these discoveries. The astronomical community, and brown dwarf researchers in particular, will be left with a need that no planned future mission fulfills.

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*Facilities:* Spitzer(IRAC), USNO:61in(ASTROCAM), NTT (SOFI), UKIRT(WFCAM), WISE, Gaia, IRSA

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