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# On the absence of radio haloes in clusters with double relics

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## ABSTRACT

Pairs of radio relics are believed to form during cluster mergers, and are best observed when the merger occurs in the plane of the sky. Mergers can also produce radio haloes, through complex processes likely linked to turbulent re-acceleration of cosmic ray electrons. However, only some clusters with double relics also show a radio halo. Here, we present a novel method to derive upper limits on the radio halo emission, and analyse archival X-ray *Chandra* data, as well as galaxy velocity dispersions and lensing data, in order to understand the key parameter that switches on radio halo emission. We place upper limits on the halo power below the  $P_{1.4\text{ GHz}}-M_{500}$  correlation for some clusters, confirming that clusters with double relics have different radio properties. Computing X-ray morphological indicators, we find that clusters with double relics are associated with the most disturbed clusters. We also investigate the role of different mass-ratios and time-since-merger. Data do not indicate that the merger mass-ratio has an impact on the presence or absence of radio haloes (the null hypothesis that the clusters belong to the same group cannot be rejected). However, the data suggest that the absence of radio haloes could be associated with early and late mergers, but the sample is too small to perform a statistical test. Our study is limited by the small number of clusters with double relics. Future surveys with LOFAR, ASKAP, MeerKat and SKA will provide larger samples to better address this issue.

**Key words:** acceleration of particles – radiation mechanisms: non-thermal – galaxies: clusters: intracluster medium – techniques: interferometric – radio continuum: general.

## 1 INTRODUCTION

Cosmological simulations show that mergers between massive clusters produce shock waves that travel from the cluster cores out to the cluster periphery (Brüggen et al. 2012; Vazza et al. 2012; Skillman et al. 2013). Shock waves heat the thermal gas in the intracluster medium (ICM) and produce temperature and X-ray surface brightness discontinuities that have been observed in some clusters (e.g. Ogrean et al. 2013). At the same time, shock waves could amplify

the ICM magnetic field and (re)accelerate relativistic electrons, producing synchrotron emission in the radio band. Radio relics are arc-shaped radio sources found at the periphery of galaxy clusters that could result from shock-(re)acceleration of fossil electrons from active galactic nucleus (e.g. Bonafede et al. 2014b; van Weeren et al. 2017). Although the (re)acceleration process is not understood yet (Kang & Ryu 2011; Kang, Ryu & Jones 2012; Pinzke, Oh & Pfrommer 2013; Vazza & Brüggen 2014; Wittor, Vazza & Brüggen 2017), a connection between shock waves and radio relics is established. According to numerical and cosmological simulations, two symmetric relics can be visible when the merger axis is in the plane of the sky (e.g. Brüggen et al. 2012; van Weeren et al. 2011a).

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**Table 1.** Clusters with double relics.

| Cluster name      | Redshift | Cluster mass<br>$10^{14} M_{\odot}$ | Mass ref. | Radio halo    | Radio ref                 | <i>Chandra</i> |
|-------------------|----------|-------------------------------------|-----------|---------------|---------------------------|----------------|
| PSZ1 G096.89+24.1 | 0.3      | $4.7 \pm 0.3$                       | 1         | NO            | WSRT 1.4 GHz <sup>6</sup> |                |
| ZwCl0008.8+5215   | 0.104    | $3.4 \pm 0.3$                       | 1         | NO            | WSRT 1.4 GHz <sup>7</sup> | Y              |
| Abell 2345        | 0.1765   | $5.9 \pm 0.4$                       | 1         | NO            | VLA 1.4 GHz <sup>8</sup>  | Y              |
| Abell 1240        | 0.1948   | $3.7 \pm 0.4$                       | 1         | NO            | VLA 1.4 GHz <sup>8</sup>  | Y              |
| Abell 3376        | 0.0456   | $2.4 \pm 0.2$                       | 1         | NO            | GMRT 325 MHz <sup>9</sup> | Y              |
| MACSJ0025.4–1222  | 0.5857   | $8.4 \pm 3.2$                       | 2         | NO            | GMRT 325 MHz <sup>2</sup> | Y              |
| 8C 0212+703       | 0.0655   | $1.1 \pm 0.2$                       | 3         | RH            | 3                         | Y              |
| El Gordo          | 0.8700   | $10.8 \pm 0.5$                      | 1         | RH            | 10                        | Y              |
| PLCKG287.0+32.9   | 0.39     | $14.7 \pm 0.4$                      | 1         | RH            | 11                        |                |
| RXCJ1314.4–2515   | 0.24740  | $6.7 \pm 0.5$                       | 1         | RH            | 12                        |                |
| MACSJ1752.0+4440  | 0.366    | $6.7^{+0.4}_{-0.5}$                 | 1         | RH            | 13                        |                |
| PSZ1G108.18-11.53 | 0.336    | $7.7 \pm 0.6$                       | 1         | RH            | 14                        |                |
| CIZAJ2242.8+5301  | 0.1921   | $17.0 \pm 3.6$                      | 4         | RH            | 15                        | Y              |
| Abell 3365        | 0.0926   | $1.48 \pm 0.04$                     | 5         | DR[c] - NO    | 16                        |                |
| MACSJ1149.5+2223  | 0.5444   | $10.4 \pm 0.5$                      | 1         | DR[c] - RH    | 17                        | Y              |
| Abell 3667        | 0.0556   | $7.04 \pm 0.05$                     | 1         | Mini halo[c]  | 18                        |                |
| ZwCl2341.1+0000   | 0.27     | $5.2 \pm 0.4$                       | 1         | Controversial | 19                        |                |

Col. 1: Cluster name. Col. 2: cluster redshift. Col. 3: Cluster mass,  $M_{500}$  is given for all cluster except for 8C 0212+703 and A3365. Col. 4: Reference for the cluster mass in Col. 3. Col. 5: Radio emission from the cluster: RH for clusters with a radio halo, NO for clusters with no radio halo. Col 6: reference for the radio data in Col. 5. Col. 7: Archival Chandra data.

References: <sup>1</sup>Planck Union Catalog Planck Collaboration XXVII (2016), <sup>2</sup>Riseley et al. (2017), <sup>3</sup>the X-ray luminosity is taken from Brown et al. (2011), considering a mean between the total X-ray luminosity and the one in the halo region. The mass is derived using the correlation by Pratt et al. (2009). <sup>4</sup>Hoang et al., submitted, <sup>5</sup>ROSAT using Pratt et al. (2009) relation. <sup>6</sup>de Gasperin et al. (2014), <sup>7</sup>van Weeren et al. (2011b), <sup>8</sup>Bonafede et al. (2009a), <sup>9</sup>Kale et al. (2012), <sup>10</sup>Lindner et al. (2014), <sup>11</sup>Bonafede et al. (2014b), <sup>12</sup>Ferretti et al. (2005), <sup>13</sup>van Weeren et al. (2012), <sup>14</sup>de Gasperin et al. (2015), <sup>15</sup>van Weeren et al. (2010) <sup>16</sup>van Weeren et al. (2009a), <sup>17</sup>Bonafede et al. (2012), <sup>18</sup>Riseley et al. (2015), <sup>19</sup>van Weeren et al. (2009b) and Giovannini et al. (2010).

Mergers between massive galaxy clusters can also produce another type of Mpc-size radio source, named radio haloes (see reviews by Ferretti et al. 2012; Brunetti & Jones 2014, and reference therein). Radio haloes are extended radio sources, that appear to fill the central regions of clusters with linear sizes that range from  $\sim 500$  kpc up to more than 1 Mpc. Despite significant progress in recent years, the origin of radio haloes is not yet understood. They could be produced by the re-acceleration of a seed population of relativistic particles due to turbulent motions that develop in the ICM during mergers (Brunetti et al. 2001; Fujita, Takizawa & Sarazin 2003). Although data seem to fit the theoretical picture, many open issues remain, such as the origin of the seed electrons, the (re)acceleration mechanism and the role of the magnetic field. Since their first discovery, it has been noticed that radio haloes always occur in massive and merging clusters (e.g. Buote 2001; Venturi et al. 2008), and it has been suggested that the fraction of clusters with haloes increases with the cluster mass (e.g. Giovannini, Tordi & Ferretti 1999; Venturi et al. 2008). Using data from *Planck* catalogues, Cuciti et al. (2015) demonstrated that this conclusion can be statistically confirmed for clusters with masses  $M_{500} > 6 \times 10^{14} M_{\odot}$ .

A total of 17 clusters with double relics have been discovered so far (see Table 1 and references in the caption). Only in a fraction of these clusters, though, has a radio halo been detected. If both radio haloes and relics are produced during mergers, clusters with relics and without halo permit to investigate the merger parameters and the cluster properties that determine whether or not a radio halo develops during cluster mergers.

Here, we focus on clusters that host double relics, as they define a sample of objects where the merger is seen close to the plane of the sky. This minimizes projection effects and permits estimates of the time since merger.

Radio observations of clusters with double relics have different sensitivities and have been performed with different instruments. In addition, the radio power of haloes correlates with the cluster mass (e.g. Cassano et al. 2013), thus biasing against less massive systems. As a first step, one needs to establish whether present observations would have been able to detect a radio halo. Once a true upper limit on the radio halo emission is established, we analyse the cluster and merging properties using X-ray data and literature information. Our aim is to search for a parameter or a combination of parameters that determines the occurrence of radio haloes during mergers.

The paper is structured as follows. In Section 2, we present a new method to derive upper limits on the cluster radio emission. The dynamical status of the clusters is analysed in Section 3 using X-ray observations, and in Section 4, we discuss different parameters that could cause the radio emission. Finally, we present our conclusions in Section 5. Throughout this paper, we assume a  $\Lambda$  cold dark matter cosmological model with  $H_0 = 69.6 \text{ km s}^{-1} \text{ Mpc}^{-1}$ ,  $\Omega_M = 0.286$  and  $\Omega_{\Lambda} = 0.714$  (Bennett et al. 2014).

## 2 RADIO HALOES AND UPPER LIMITS

### 2.1 The cluster sample

From the literature, we have collected the data of all clusters known to date that host symmetric double radio relics. The main properties of these clusters are listed in Table 1. In total, there are six clusters that are known to host double relics and no halo (top of Table 1), seven clusters that host both double relics and a radio halo (mid-top of Table 1), two clusters that host one relic and one candidate counter-relic (mid-bottom of Table 1) and two controversial cases (bottom of Table 1). These clusters are Abell 3667 and ZwCl2341.1+0000. Abell 3667 hosts diffuse emission classified

as a ‘radio bridge connecting the NW relic of the galaxy cluster Abell 3667 to its central regions’ (Carretti et al. 2013), and more recently re-classified as a candidate mini halo (Riseley et al. 2015). For the cluster ZwCl2341.1+0000, different interpretations have been given (see e.g. Bagchi et al. 2002; van Weeren et al. 2009b; Giovannini et al. 2010) and the presence of a radio halo is uncertain. For these reasons, ZwCl2341 and A3667 have been excluded from our analysis. Hence, the final sample consists of 15 clusters. We note that the clusters span a wide range of redshifts (from  $z = 0.0456$  to  $z = 0.87$ ) and masses (from  $M_{500} = 1.2 \times 10^{14} M_{\odot}$  to  $M_{500} = 14 \times 10^{14} M_{\odot}$ ).

In this work, we use the calibrated data sets of clusters with double relics and no detected radio halo. Most of the observations were performed at 1.4 GHz. The only exceptions are A3376 and MACSJ0025 that have been observed at 325 MHz. Details about the observations and data reduction can be found in the papers listed in Table 1.

## 2.2 A new method to derive upper limits

Radio haloes have a low surface brightness at frequencies higher than few hundred MHz, and the observations that we analyse in this work have different sensitivities. Hence, we need to assess whether the observations of clusters with no halo are deep enough to detect it. Placing upper limits on the flux from extended structures in interferometric images is not a trivial task, and different methods have been used in the past. Venturi et al. (2008) have used the injection of mock radio haloes in the UV-plane. We have followed their approach, modifying the morphology of the mock radio haloes to resemble the observed ones.

### 2.2.1 Mock haloes: expected properties

The power of radio haloes is known to correlate with the mass of the host cluster (e.g. Cassano et al. 2013; Sommer & Basu 2014). More massive clusters host more powerful radio haloes, in line with the idea that the source of energy for the radio emission is the gravitational energy released in the ICM during mergers. To predict the expected power of radio haloes at 1.4 GHz ( $P_{1.4\text{GHz}}$ ), we have used the correlation between  $P_{1.4\text{GHz}}$  and  $M_{500}$  by Cassano et al. (2013). We note that this correlation has been derived using massive clusters only ( $M_{500} > 4 \times 10^{14} M_{\odot}$ ). A tighter correlation has been published by Martinez Aviles et al. (2016) while we were writing this paper. Although slightly steeper than the one by Cassano et al. (2013), the two are consistent within their  $1\sigma$  errors.

Another correlation exists between  $P_{1.4\text{GHz}}$  and the size of the radio halo (Giovannini & Feretti 2000). In particular, Cassano et al. (2007) have found a direct scaling between  $P_{1.4\text{GHz}}$  and  $R_{\text{H}} = \sqrt{R_{\text{min}} \times R_{\text{max}}}$ , where  $R_{\text{min}}$  and  $R_{\text{max}}$  are the minimum and maximum radii of the radio haloes, respectively.

Murgia et al. (2009) have analysed a sample of radio haloes and they have found that the azimuthally averaged brightness profile,  $I(r)$ , is well represented by an exponential law:

$$I(r) = I_0 e^{-r/r_e}, \quad (1)$$

where  $r_e$  and  $I_0$  are two independent fit parameters. We have compared the values of  $R_{\text{H}}$  and  $r_e$  found by Cassano et al. (2007) and Murgia et al. (2009) for the eight clusters in common in their samples. The median value of the ratio  $R_{\text{H}}/r_e$  is 2.6.

We used the  $P_{1.4\text{GHz}}-M_{500}$  correlation by Cassano et al. (2013) to predict the expected power of the radio haloes at 1.4 GHz. Then,

we used the correlations by Cassano et al. (2007) and Murgia et al. (2009) to predict the expected size of the radio haloes ( $R_{\text{H}}$  and  $r_e$ ).

Although the radio halo brightness can be described by azimuthally averaged profiles, the morphology of radio haloes is irregular and brightness fluctuations are present on a range of spatial scales. To account for this, we have modelled the mock haloes as 2D fields with power spectrum fluctuations. The power spectrum follows the form  $P(\Lambda) \propto \Lambda^n$ , where  $\Lambda$  is the spatial scale and ranges between 10 and 250 kpc, and  $n = 11/3$ . As discussed below, observations do not permit to constrain the range of  $\Lambda$  and the value of  $n$ . None the less, constraints about cluster magnetic fields indicate that the numbers we have adopted here are reasonable (Govoni et al. 2005, 2006; Bonafede et al. 2009b). Then, the radio profile has been normalized to follow equation (1). This way, we obtain models of the radio haloes with the radio power and size that obey known correlations and include fluctuations in the surface brightness distribution.

### 2.2.2 Imaging of mock haloes and determination of upper limits

Once the parameters of the model haloes are set, we have derived upper limits on the radio halo power as described below.

(1) To start with,  $I_0$  has been chosen such that the radio power within  $2.6 r_e$  (i.e.  $R_{\text{H}}$ ) follows the  $P_{1.4\text{GHz}}-M_{500}$  correlation. The flux density of the radio halo within  $R_{\text{H}}$  is referred as  $S_{R_{\text{H}}}^{\text{mock,tot}}$ .

(2) The images of the mock haloes have been Fourier-transformed and added to the visibilities of the observations. The positions of the mock haloes have been chosen to be close to the cluster centres and in regions devoid of radio sources. The new data sets have been imaged and deconvolved with the software package CASA 4.5 (McMullin et al. 2007), using the Briggs weighting scheme (Briggs 1995) with different robust parameters, and UV-tapers to achieve a beam of  $\sim 40-50$  arcsec.

(3) The largest detectable size within a circle of radius  $R_{\text{H}}$  and above  $2\sigma$  has been measured ( $D_{2\sigma}^{\text{mock,meas}}$ ). We considered the mock halo as detected if  $D_{2\sigma}^{\text{mock,meas}} \geq R_{\text{H}}$ , i.e. if the largest detectable size above  $2\sigma$  is at least half of the expected halo size. We define  $S_{2\sigma}^{\text{mock,meas}}$  as the flux density measured within  $D_{2\sigma}^{\text{mock,meas}}$ .

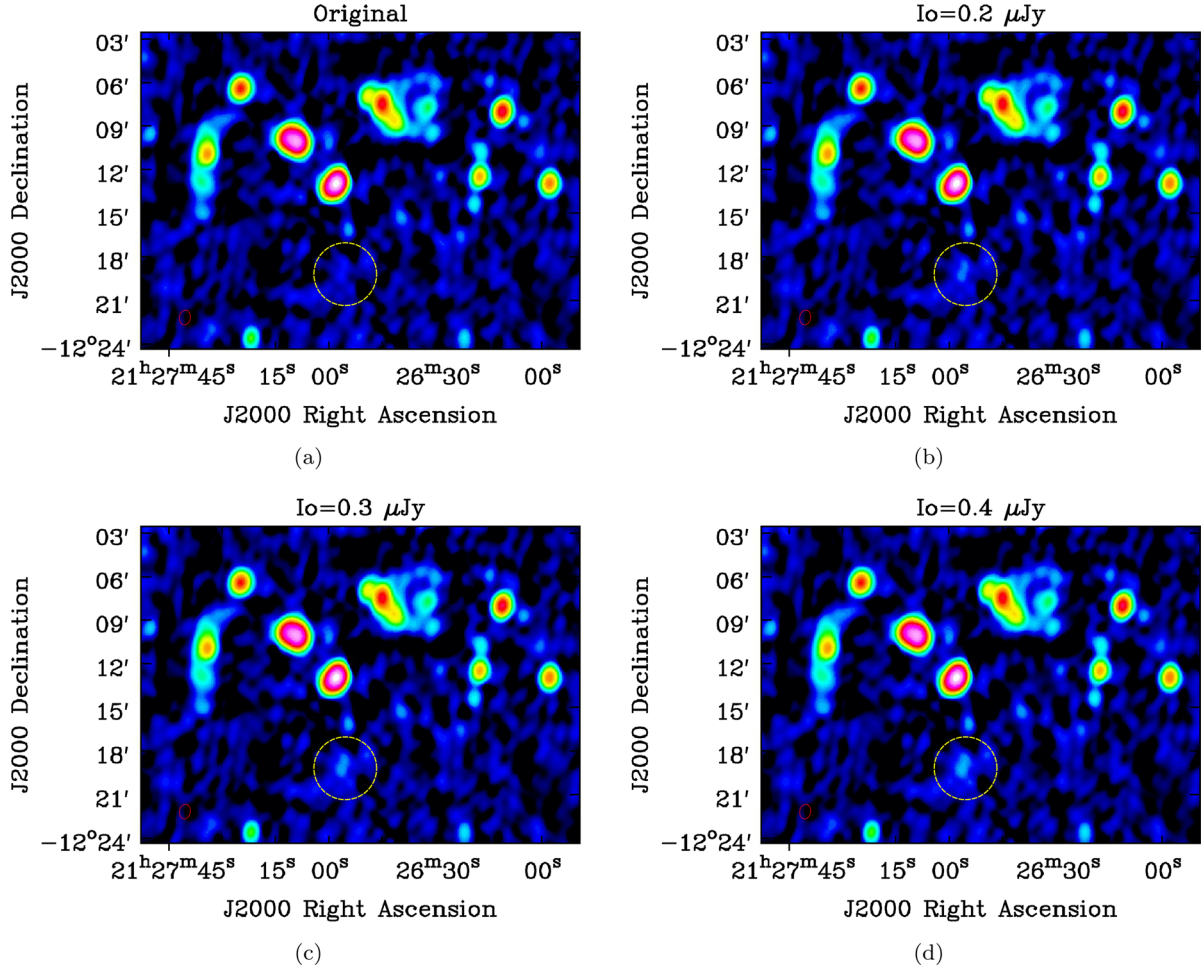
(4) If  $D_{2\sigma}^{\text{mock,meas}} \gg R_{\text{H}}$ , or  $S_{2\sigma}^{\text{mock,meas}} > 30$  per cent  $S_{R_{\text{H}}}^{\text{mock,tot}}$ , we have repeated the steps above decreasing the value of  $I_0$  by  $0.1 \mu\text{Jy arcsec}^{-2}$ , to see if we can achieve a more stringent limit. Conversely, if  $D_{2\sigma}^{\text{mock,meas}} < R_{\text{H}}$ , we have repeated steps above increasing the value of  $I_0$  by  $0.1 \mu\text{Jy arcsec}^{-2}$ .

(5) Steps 2–4 are repeated until the mock halo is considered detected, according to the conditions explained above. For the upper limits that we have computed, the measured  $S_{2\sigma}^{\text{mock,meas}}$  is 30–70 per cent of  $S_{R_{\text{H}}}^{\text{mock,tot}}$ .

We show in Fig. 1 a series of images of mock haloes with increasing brightness.

The upper limits for the clusters A3376 and MACSJ0025 have been derived using data at 325 MHz, assuming that the size of the radio halo would not change significantly between 325 MHz and 1.4 GHz, and assuming  $\alpha = 1.3$ .

As our main criterion is based on  $D_{2\sigma}^{\text{mock,meas}} \geq R_{\text{H}}$ , this approach is very conservative for clusters with  $M_{500} \geq 7.5 \times 10^{14} M_{\odot}$ . For these objects, the expected  $R_{\text{H}}$  is  $> 500$  kpc, while in reality a source larger than 500 kpc would already be classified as a radio halo. This is not critical for this study, as there is only one cluster in our sample with  $M_{500} > 7.5 \times 10^{14} M_{\odot}$ , but it will become important when larger samples become available.



**Figure 1.** Mock haloes in the cluster A2345. Images of the cluster (a): original data set, (b): mock halo with  $I_0 = 0.2 \mu\text{Jy arcsec}^{-2}$  (c) mock halo with  $I_0 = 0.3 \mu\text{Jy arcsec}^{-2}$  (d) mock halo with  $I_0 = 0.4 \mu\text{Jy arcsec}^{-2}$ . The yellow circle is centred on the halo and has a radius  $r = R_H$ . The images have been obtained with the same parameters, and displayed with the same colour scheme. The mock halo that fulfils the criteria for detection is the one in panel (c).

Similarly, the upper limits on  $P_{1.4\text{GHz}}$  for clusters with  $M_{500} \leq 3.4 \times 10^{14} M_\odot$  should be treated with caution. For these clusters, the estimated size of the radio haloes would be  $<500$  kpc, and the source would likely not be classified as a radio halo. As a consequence, the limits on the power of the radio haloes in A3365, A3376 and ZwCl0008 should be treated carefully. For our analysis, this is not crucial as the limits we have assumed are consistent with the  $P_{1.4\text{GHz}}-M_{500}$  correlation.

### 2.3 Upper limits and the $P_{1.4\text{GHz}}-M_{500}$ correlation

Clusters with and without radio haloes occupy separate regions of the  $P_{1.4\text{GHz}}-M_{500}$  correlation (Cassano et al. 2013; Sommer & Basu 2014). As mentioned before, most of the clusters with radio haloes are in merging systems, while most of the upper limits are found for non-merging clusters. However, not all massive merging clusters host a radio halo, and this raises questions about their origin.

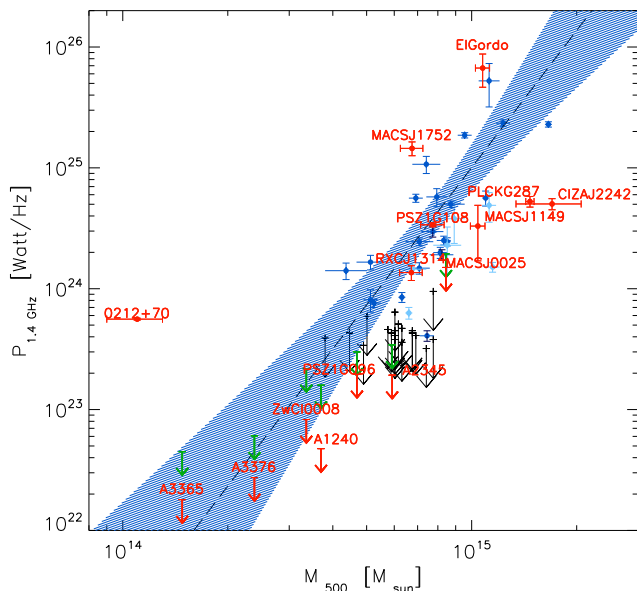
In Fig. 2, the  $P_{1.4\text{GHz}}-M_{500}$  correlation is shown, together with the upper limits derived here. Both, the upper limits corresponding to  $S_{2\sigma}^{\text{mock, meas}}$  and  $S_{R_H}^{\text{mock, tot}}$  are plotted in Fig. 2. If we assume that the power of the radio haloes on the  $P_{1.4\text{GHz}}-M_{500}$  correlation represents the whole radio emission in the cluster, i.e. that all the radio emission has been detected,  $S_{R_H}^{\text{mock, tot}}$  are the values that we have to consider.

It is more likely that a fraction of the halo flux has been missed by observations, and a more realistic value for the upper limit should lie in between  $S_{R_H}^{\text{mock, tot}}$  and  $S_{R_H}^{\text{mock, meas}}$ . We go here for a conservative approach and consider  $S_{R_H}^{\text{mock, tot}}$ .

From the analysis in the previous section, we conclude that three or four clusters with double relics and no previously detected radio halo do not host a radio halo that follows the  $P_{1.4\text{GHz}}-M_{500}$  correlation. They are PSZ1 G096.89+24.1, Abell 2345 and MACSJ0025.4–1222. For the cluster A1240, we can put an upper limit below the correlation only if we consider the flux density that is measured in the image ( $S_{R_H}^{\text{mock, meas}}$ ), while the corresponding flux density in the model halo ( $S_{R_H}^{\text{mock, tot}}$ ) would still be consistent with the correlation within 95 per cent confidence level (the shaded area in Fig. 2). For Abell 3376, ZwCl0008 and A3365, we can only place upper limits consistent with the  $P_{1.4\text{GHz}}-M_{500}$  correlation within 95 per cent confidence level.

As  $P_{1.4\text{GHz}} \propto M_{500}^{3.77}$  while  $P_{1.4\text{GHz}} \propto R_H^{4.18}$  (Cassano et al. 2007, 2013), the radio brightness is proportional to  $M_{500}^{1.97}$ . This explains why we are able to place lower upper limits for clusters with smaller  $M_{500}$  even if observations are not deeper (see values of  $I_0$  listed in Table 2).

Note that the limits that we have derived depend on the model that we have assumed for the radio haloes. The choice of some



**Figure 2.** Radio power at 1.4 GHz versus cluster mass within  $R_{500}$ . Filled dots are radio haloes: light blue dots mark haloes with a spectrum steeper than  $\alpha = 1.5$  (Venturi et al. 2007, 2008; Cassano et al. 2013; Bonafede et al. 2014a, 2015), red dots mark haloes in clusters with double relics. Black arrows are upper limits on  $P_{1.4\text{GHz}}$  (Venturi et al. 2008; Cassano et al. 2013, and reference therein). The dashed line is the  $P_{1.4\text{GHz}}-M_{500}$  correlation as derived by Cassano et al. (2013) excluding steep-spectrum haloes. The shaded area marks the 95 per cent CL of the correlation. Red and green arrows are upper limits on haloes in clusters with double relics derived in this work, computed from  $S_{RH}^{\text{mock,tot}}$  and  $S_{2\sigma}^{\text{mock,meas}}$ , respectively (see text for more details). Clusters analysed in this work are labelled.

parameters for the mock halo modelling is arbitrary, as present observations do not allow us to study the spectrum of the halo brightness fluctuations. None the less, the approach that we used has two improvements with respect to previous methods. (i) The fluctuations that we introduce in the halo brightness distribution make the mock halo appear more like the observed ones. (ii) The radial profiles follow the azimuthally averaged brightness profiles that have been observed.

## 2.4 Comparison with the previous method

The idea of injecting mock radio haloes in the UV-plane to derive limits on the radio halo power has been introduced by Venturi et al. (2008). Here, we compare our method to the one used by Venturi et al. (2008) to assess the impact on the upper limits. For this comparison, we take two clusters: Abell 2345 and Abell 3376.<sup>1</sup>

(i) A2345 is chosen because the images have the most uniform noise pattern among the clusters analysed here. Following Venturi et al. (2008), we have modelled mock haloes as concentric circles of increasing radius. The largest circle has a radius =  $R_H$ , and contains  $\sim 50$  per cent of the halo flux density. We have injected a radio halo with the same power at 1.4 GHz as the one listed in Table 2, corresponding to the upper limit we have derived for A2345. We found that the flux recovered in the two cases (concentric circles and exponential profile) measured above  $2\sigma$  is the same

<sup>1</sup> While this paper was in press, another work became publicly available, in which upper limits to the radio halo in the cluster A3667 are derived using yet another technique (Johnston-Hollitt & Praty 2017).

within the errors. Moreover, the largest linear size of the mock halo, measured above  $2\sigma$ , is  $\sim 6$  per cent smaller when concentric spheres are used. Hence, we can conclude that in this case differences are not significant.

This might indicate that the dominant factor is not the mock halo brightness distribution, but a combination of (i) the number of independent beams with which the halo is sampled, which depends on the full width at half-maximum of the restoring beam and on the angular size of the mock radio halo; (ii) the halo surface brightness, which depends on the observing frequency.

As haloes have a steep spectrum, their surface brightness decreases as the observing frequency increases. At 1.4 GHz, they are better imaged with large beams, which could smooth out the differences of the halo models. In the case of A2345, the data are taken at 1.4 GHz, the mock halo has a brightness of  $0.6 \text{ mJy beam}^{-1}$  and it is sampled by 18 beams (4 in the area above  $2\sigma$ ).

(ii) We have repeated the same comparison for the cluster Abell 3376, which has been observed at 325 MHz. The halo is sampled by 26 beams (8 in the area above  $2\sigma$ ), and it has a mean brightness of  $4.6 \text{ mJy beam}^{-1}$ , which is the highest among the clusters analysed here. As expected, the differences in this case are larger: the halo modelled with concentric spheres enables recovery of a higher flux density above  $2\sigma$ . Specifically, we recover 12 per cent more flux above  $2\sigma$ , and the halo angular size measured above  $2\sigma$  is  $\sim 7$  per cent smaller. This can be understood as the model with concentric spheres has a profile that is more peaked towards the centre with respect to the models with power-spectrum fluctuations and exponential profile (see Fig. 3).

Our analysis indicates that as the halo brightness increases (e.g. the halo is observed at lower frequencies), the upper limit to the radio power at 1.4 GHz depends on the modelling of the mock halo.

Analysing how the limits on  $P_{1.4\text{GHz}}$  are affected by observing frequency, halo angular size, models of the mock halo and many other parameters, goes beyond the aim of this work. However, instruments like LOFAR and the future SKA precursors in the coming years, are able to image extended emission at high angular resolution and sensitivity. Hence, we expect that upper limits derived from the observations of those instruments will depend on the modelling of the mock haloes, at which time a more thoughtful investigation of these parameters should be done.

## 2.5 Upper limit and halo model assumptions

### 2.5.1 Power spectrum brightness fluctuations

We investigate in this section the impact of models with and without power-spectrum fluctuations on the upper limits. As above, we have used the clusters A2345 and A3376. For A2345, we found that the flux density measured in the two cases is consistent within the errors, although higher when power spectrum fluctuations are not included. In the case of A3376, the flux measured is 6 per cent higher if power spectrum fluctuations are not included. Although negligible, these differences demonstrate that future observations at low frequency and high resolution will likely be sensitive to the modelling of the mock halo.

### 2.5.2 Ellipsoidal haloes

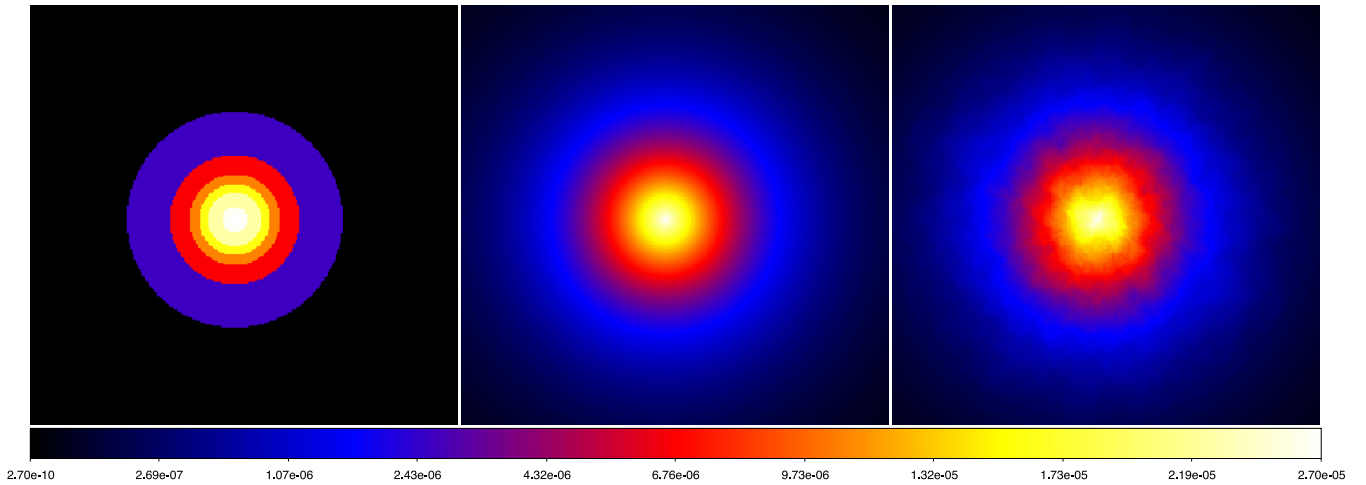
Some clusters with double relics have a radio halo that extends in-between the two relics. This is the case of CIZAJ2242, MACSJ1752 and El Gordo. For these clusters, the radio halo would be better

**Table 2.** Clusters with no halo.

| Cluster                       | Expected $P_{1.4\text{GHz}}$<br>(W Hz $^{-1}$ ) | $P_{1.4\text{GHz}}$ injected<br>(W Hz $^{-1}$ ) | $P_{1.4\text{GHz}}$ meas<br>(W Hz $^{-1}$ ) | $r_e$<br>(kpc) | $I_0$<br>( $\mu\text{Jy arcsec}^{-2}$ ) | $D_{2\sigma}^{\text{mock, meas}}$<br>(kpc) | $2 \times R_H$<br>(kpc) |
|-------------------------------|---|---|---|----------------|---|--|-------------------------|
| Abell 3365                    | $6.4 \times 10^{21}$                            | $4.5 \times 10^{22}$                            | $1.8 \times 10^{22}$                        | 45             | 1.5                                     | 170  | 230                     |
| Abell 3376 <sup>a</sup>       | $3.8 \times 10^{22}$                            | $6.8 \times 10^{22}$                            | $2.7 \times 10^{22}$                        | 69             | 3.0                                     | 210  | 360                     |
| ZwCl0008.8+5215               | $1.4 \times 10^{23}$                            | $2.4 \times 10^{23}$                            | $8.3 \times 10^{22}$                        | 94             | 0.7                                     | 365  | 490                     |
| Abell1240                     | $2.0 \times 10^{23}$                            | $1.6 \times 10^{23}$                            | $4.8 \times 10^{22}$                        | 103            | 0.3                                     | 300  | 530                     |
| PSZ1 G096.89+24.1             | $4.9 \times 10^{23}$                            | $3.8 \times 10^{23}$                            | $2.0 \times 10^{23}$                        | 127            | 0.3                                     | 400  | 660                     |
| Abell 2345                    | $1.2 \times 10^{24}$                            | $3.8 \times 10^{23}$                            | $1.9 \times 10^{23}$                        | 157            | 0.3                                     | 480  | 810                     |
| MACSJ0025.4–1222 <sup>a</sup> | $4.5 \times 10^{24}$                            | $1.9 \times 10^{24}$                            | $1.5 \times 10^{24}$                        | 216            | 1.5                                     | 800  | 1130                    |

Col. 1: cluster name; Col. 2: expected  $P_{1.4\text{GHz}}$  according to the  $P_{1.4\text{GHz}}-M_{500}$  correlation (Cassano et al. 2013); Col. 3:  $P_{1.4\text{GHz}}$  of the model injected in the UV-data (corresponding to  $S_{RH}^{\text{mock, tot}}$ ); Col. 4:  $P_{1.4\text{GHz}}$  measured in the image (corresponding to  $S_{2\sigma}^{\text{mock, meas}}$ ); Col. 5, 6: parameters of the mock halo corresponding to the upper limits. Col. 7: Size of the mock radio halo measured in the image above  $2\sigma$ ; Col. 8: expected size of the radio halo according to the  $P_{1.4\text{GHz}}-R_H$  correlation (Cassano et al. 2007).

<sup>a</sup>upper limit derived at 325 MHz,  $P_{1.4\text{GHz}}$  have been computed assuming  $\alpha = 1.3$ .



**Figure 3.** Models for the mock haloes used to derive upper limits. Left: models with concentric spheres (Venturi et al. 2008), middle: model with exponential profile, right: model with average exponential profile and power spectrum fluctuations. The three models have the same flux density within the same radius.

represented by an ellipsoid with the major axis equal to the distance between the two relics.

We have compared the value of  $R_H$  measured for the haloes in CIZAJ2242, MACSJ1752 and El Gordo with the one predicted by Cassano et al. (2007). For the clusters CIZAJ2242 and El Gordo, the values are consistent, while for MACSJ1752 the measured value of  $R_H$  is almost twice the predicted one.

In order to estimate how the upper limits change if the mock haloes are modelled as ellipsoids, we consider two scenarios in which the radio halo does not follow the  $M_{500}-R_H$  correlation and the exponential profile in equation (1).

(i) The mock halo surface brightness profile follows an exponential law of the form  $I = I_0 e^{-\epsilon/r_e}$ , with  $\epsilon = \frac{x^2}{a^2} + \frac{y^2}{b^2}$  for  $\epsilon \leq 1$ .

(ii) The mock radio halo has a constant surface brightness.

In both scenarios, the halo is modelled as an ellipsoid with the major axis equal to the distance between the two relics and the minor axis equal to the relics' size. We have assumed that the  $P_{1.4\text{GHz}}-M_{500}$  correlation holds, i.e. the total flux of the model halo is the same as the mode in Section 2.2.

Scenarios (i) and (ii) can be considered as the most extreme cases of haloes that follow the exponential fit, although not spherical but elliptical (i), and haloes that do not show any brighter part. We have derived the upper limits for the cluster Abell 2345 in both scenarios. It results that for model (i) the upper limit is consistent with the one

we put in Section 2.2, while for model (ii) the upper limit would be consistent with the  $P_{1.4\text{GHz}}-M_{500}$  correlation.

The analysis that follows in the next section will assume that haloes can be modelled as done in Section 2.2.

### 3 MERGING STATUS FROM X-RAY DATA

In this section, we analyse the X-ray properties of the clusters with double relics and compare them to other clusters – with and without radio haloes – analysed in the literature. In our sample, there are nine clusters with *Chandra* archival observations that can be suitable for a comparison with literature information. These clusters are listed in Table 1.

#### 3.1 X-ray morphological indicators

X-ray data can be used to assess the dynamical status of a cluster through three morphological indicators (e.g. Böhringer et al. 2010).

(i) The concentration parameter  $c$ , defined as

$$c = S_x(r < 100 \text{ kpc}) / S_x(r < 500 \text{ kpc}), \quad (2)$$

with  $S_x$  being the integrated X-ray surface brightness and  $r$  the radial coordinate from the cluster centre.

(ii) The power ratio  $P_3/P_0$ . The power ratio is a multipole decomposition of the projected mass distribution inside a given radius

(which we define as  $R_{\text{ap}} = 500$  kpc). As the gas is subject to the cluster gravitational potential, the idea behind the power ratio analysis is that the X-ray surface brightness can be used to trace the projected mass distribution.

Böhringer et al. (2010), found that  $P_3/P_0$  is the lowest power ratio moment that can give a measure of the cluster substructures.  $P_0$  is defined as

$$P_0 = S_x(r < R_{\text{ap}}) \ln(R_{\text{ap}}), \quad (3)$$

while

$$P_3 = \frac{1}{18R_{\text{ap}}^6} (a^2 + b^2), \quad (4)$$

with

$$a = \int_{r < R_{\text{ap}}} S_x(x') r'^3 \cos(3\phi') d^2x', \quad (5)$$

$$b = \int_{r < R_{\text{ap}}} S_x(x') r'^3 \sin(3\phi') d^2x'. \quad (6)$$

The higher the value of  $P_3/P_0$ , the more substructures are present in the X-ray surface brightness. Hence, high values of  $P_3/P_0$  indicate a merger cluster.

(iii) The centroid-shift parameter,  $w$ , measures the standard deviation of the projected separation between the X-ray peak and the centroid in units of  $R_{\text{ap}}$ , computed in  $N$  spheres of increasing radius. Specifically, it is defined as

$$w = \sqrt{\frac{1}{N-1} \sum (\Delta_i - \langle \Delta \rangle)^2} \times \frac{1}{R_{\text{ap}}}, \quad (7)$$

where  $\Delta_i$  is the distance between the cluster centre and the centroid of the  $i$ th circle. We start from  $R = 0.05R_{\text{ap}}$  and increase the radius at steps of  $0.05 \times R_{\text{ap}}$  until  $R = R_{\text{ap}}$ . As for  $P_3/P_0$ , high values of  $w$  indicate that the cluster is far from dynamical equilibrium. Using numerical simulations, Poole et al. (2006) has found that  $w$  is very sensitive to the cluster dynamical state.

Cassano et al. (2010) have computed these indicators for a mass-selected sample of clusters, and they found that clusters with and without radio haloes occupy different regions in the morphological diagrams. Although some outliers have been found later (Bonafede et al. 2014a, 2015; Sommer et al. 2017; Venturi et al. 2017), most of the haloes are in clusters with low  $c$ , high  $w$  and high  $P_3/P_0$ .

### 3.2 X-ray data reduction and analysis

*Chandra* observations have been reduced using the *Chandra Interactive Analysis of Observations* (CIAO) 4.7. The event files have been reprocessed to apply the latest calibration files as of 2016 February (v 4.7.2). Observations have been processed in the energy band 0.5–7 keV, to search for soft proton flares. Time periods affected by proton flares have been excluded (usually less than 10 per cent of the observing time) and clean event files have been created. The clean event files have been exposure corrected and images in the band 0.5–2.4 keV have been created. Exposure-corrected images have been binned to achieve a common resolution of 4 kpc pixel<sup>-1</sup>. This is necessary because we want to compare clusters at different redshifts with the sample analysed in Cassano et al. (2013) at  $z = 0.2$ – $0.3$ , and a different resolution may impact the value of  $P_3/P_0$  and  $w$ . Point sources have been detected using the *wavedetect* script in CIAO. This script correlates the images with wavelets of different scales, and searches the results for significant correlations. Results from *wavedetect* have been inspected visually and

corrected, when needed. Point sources have been excluded from the analysis.

The morphological parameters  $P_3/P_0$ ,  $w$  and  $c$  have been computed as described above. In Fig. 4, we show the positions of the clusters in the  $P_3/P_0 - c$ ,  $w - c$  and  $P_3/P_0 - w$  diagrams (taken from Bonafede et al. 2015, adapted from Cassano et al. 2013). Clusters with double relics are added with different symbols: red open triangles are clusters with double relics and no halo (MACSJ0025 and A2345), green open triangles are clusters with double relics and no halo, but with upper limits on  $P_{1.4\text{ GHz}}$  consistent with the  $P_{1.4\text{ GHz}} - M_{500}$  correlation (A1240, A3376 and ZWCI0008), blue triangles are clusters with double relics and halo (El Gordo, CIZA2242, J0212 and MACSJ1149). As expected – given the presence of double relics – the clusters we analyse in this work are all in the merging quadrant of the plots. In addition, we note that they are characterized by  $P_3/P_0$  and  $w$  values among the highest of the cluster sample. This indicates that the amount of substructures and asymmetries in the mass distribution are both very high. We also note that double relic clusters with and without radio halo occupy the same region of the plots, indicating that the merging status is similar. Projection effects could play a role, as double relics should be better observable when the merger takes place in the plane of the sky, and this is the most favourable configuration to detect as many substructures and asymmetries in the gas distribution as possible. None the less, it is interesting to note that clusters with double relics lie in the most disturbed region of the plots.

According to the X-ray substructure analysis, it remains unexplained why some of the clusters with double relics do not have a radio halo.

## 4 DISCUSSION

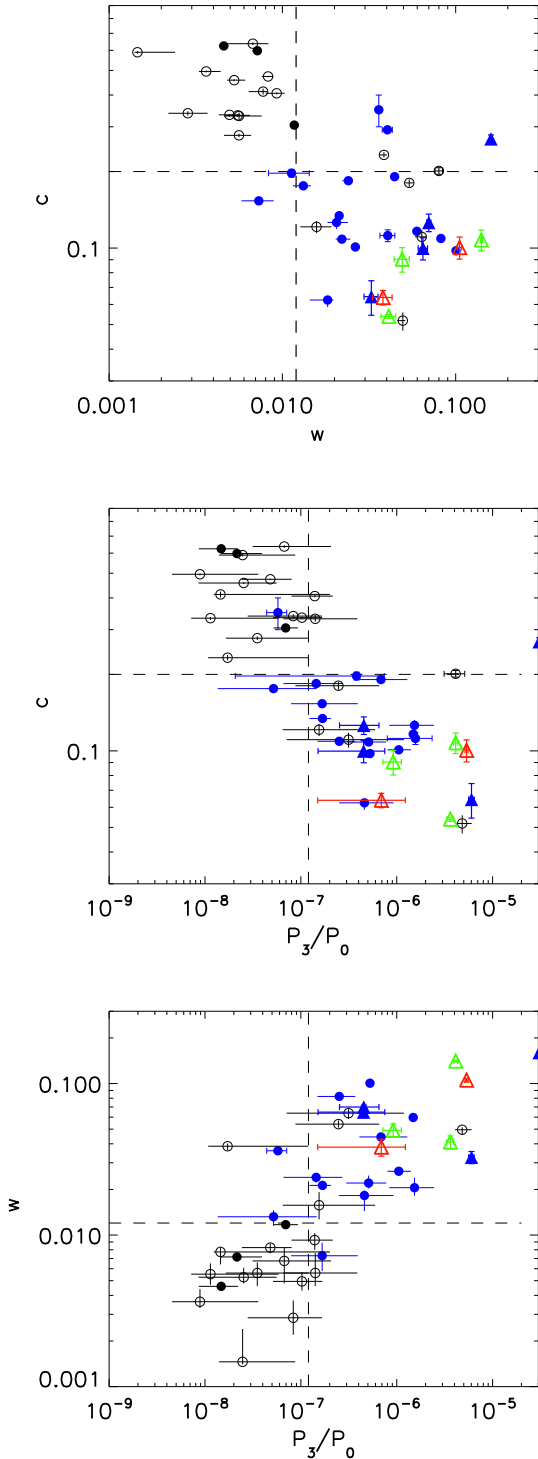
Our analysis shows that all clusters with double relics are merging clusters with similar dynamics and that is also similar to clusters with radio haloes. However, some of them do not have a radio halo that follows the  $P_{1.4\text{ GHz}} - M_{500}$  correlation. Although turbulent re-acceleration models make statistical predictions that are consistent with data so far, individual cases remain to be understood. This indicates that our understanding of the process is incomplete.

It has been suggested that the merger mass-ratio and/or a time-scale argument do not play a role (e.g. Cassano et al. 2016, and references therein). In the following analysis, we will use the Wilcoxon–Mann–Whitney statistical test to check whether clusters with and without radio haloes can be regarded as different groups. The Wilcoxon–Mann–Whitney test is a non-parametric test that checks whether two samples are consistent with the same population or not. Specifically, the test can check – given two independent samples – whether one variable tends to have values higher than the other. It is a good alternative to the t-test when data are not normally distributed, and can be used when the sample sizes is small. For more details, we refer to Neuhaeuser (2014). As independent samples, we have taken the masses of clusters with and without radio haloes, and tested the null hypothesis that the two populations are not statistically different.

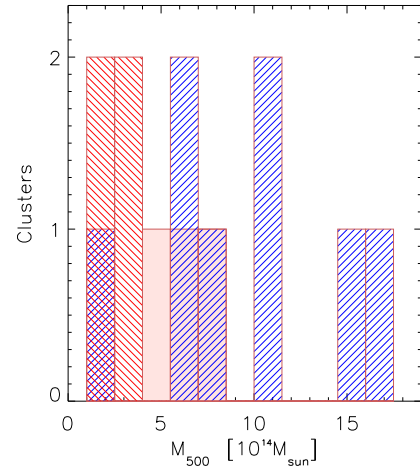
### 4.1 Total cluster mass

In Fig. 5, we show a histogram of the halo/no halo distribution versus the cluster mass. This plot hints at a mass trend, as clusters without radio halo tend to lie in the small mass region. For a quantitative test, we have run the Wilcoxon–Mann–Whitney statistical test. To start with, we have run the tests including in the ‘no-halo’ sample only the clusters for which we have put upper limits below the





**Figure 4.** Morphological estimators of cluster dynamical status from X-rays. Black filled dots are clusters with mini haloes, blue filled dots are clusters with radio haloes and no double relics (from Venturi et al. 2008; Cassano et al. 2010; Bonafede et al. 2014a, 2015), blue filled triangles are clusters with radio haloes and double relics, red open triangles are clusters with double relics and no radio halo (upper limit below the  $P_{1.4\text{GHz}}-M_{500}$  correlation), black spheres are clusters with no radio haloes and no double relics. Green triangle mark clusters where no radio halo has been detected but the upper limit is above the  $P_{1.4\text{GHz}}-M_{500}$  correlation. Dashed lines are the median of the parameters, that define radio-loud and radio-quiet quadrants (Cassano et al. 2010)



**Figure 5.** Histogram of the clusters with halo (blue diagonal lines), without halo (filled red) and with upper limit consistent with the  $P_{1.4\text{GHz}}-M_{500}$  correlation (red diagonal lines) versus the cluster mass.

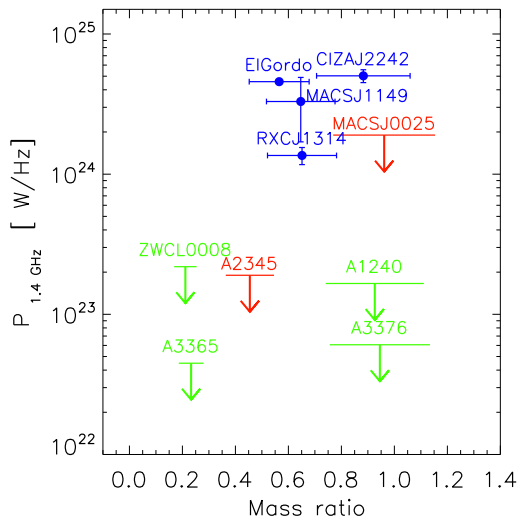
correlation. The null hypothesis that the clusters are drawn from the same population cannot be rejected at any of the confidence level tabulated. We have repeated the test including all the clusters with upper limits in the ‘no-halo’ sample, and found again that the null hypothesis cannot be rejected.

#### 4.2 Mass-ratio

Clusters with double relics and with or without radio haloes could trace mergers with different mass-ratios. Recently, Cassano et al. (2016) have analysed a sample of massive clusters and derived that the fraction of merger clusters is higher than the fraction of clusters with radio haloes. This could suggest that radio haloes trace mergers with larger mass-ratios. From the literature, we have collected the data about the masses of the clusters in our sample. Estimates come from strong and weak lensing analysis (ZwCl0008: Golovich et al. 2017, CIZAJ2242: Jee et al. 2015, ElGordo: Jee et al. 2014, MACSJ0025: Bradač et al. 2008), from dynamical analysis (MACSJ1149: Golovich et al. 2016), and from cluster members velocity dispersion (A2345 Barrena et al. 2011, RXCJ1314, A1240, A3376, A3365: Golovich et al., in preparation). We have defined the mass-ratio as  $M_{\min}/M_{\max}$ , where  $M_{\min}$  and  $M_{\max}$  are the minimum and maximum masses of the two main sub-clusters. In Fig. 6,  $P_{1.4\text{GHz}}$  is plotted versus the mass-ratio. Although the sample is small, data do not seem to support a different mass-ratio for clusters with and without radio haloes. To quantify this, we have run the Wilcoxon–Mann–Whitney statistical test. As independent samples, we have taken the mass-ratios derived for clusters with and without radio haloes. We have repeated the test twice, first considering in the sample of clusters without radio haloes, only the upper limits below the  $P_{1.4\text{GHz}}-M_{500}$  correlation (red arrows in Fig. 6) and then including also the upper limits that would be consistent with the  $P_{1.4\text{GHz}}-M_{500}$  correlation (green arrows in Fig. 6). In both cases, the null hypothesis that the clusters are drawn from the same population cannot be rejected. Hence, no indication is given by present data about a different radio behaviour for cluster mergers with different mass-ratios.

#### 4.3 Time since merger

If haloes are powered by turbulence injected in the ICM during mergers, we may expect that the cascade takes time to develop and



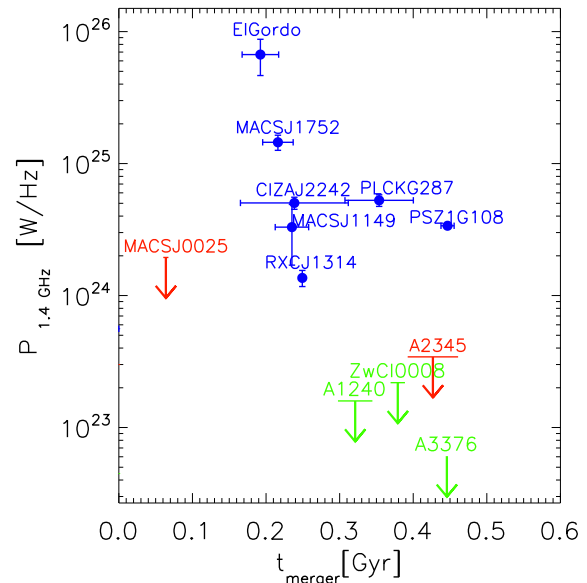
**Figure 6.**  $P_{1.4\text{GHz}}$  versus the merger mass-ratio. Blue points are detected haloes, red arrows are upper limits below the  $P_{1.4\text{GHz}}-M_{500}$  correlation, green arrows are upper limits above the  $P_{1.4\text{GHz}}-M_{500}$  correlation. As errors on the masses of the sub-clusters are not available for most objects, we assume a fiducial error of 20 per cent on the mass-ratios.

enter in the regime where it can accelerate particles. Hence, clusters with double relics and no radio haloes could be those undergoing a merger more recently than clusters with double relics and haloes.

Alternatively, clusters with relics and no halo on the  $P_{1.4\text{GHz}}-M_{500}$  relation could be those that have undergone a merger a longer time ago. While shock acceleration takes place at relics, the halo emission at 1.4 GHz is fading quickly due to synchrotron and inverse Compton losses. In both cases (earlier or later merger), the two classes of clusters should be divided by a characteristic time since the merger took place. Obtaining an estimate of the time since the merger started is difficult and little data are available in the literature. However, we can take the distance between the two relics ( $d_{r,\text{max}}$ ) as a proxy of the time since the merger happened. To do this, we made the following assumptions.

- (i) The ICM is isothermal.
- (ii) Relics trace two symmetric shock waves injected in the ICM at a given time.
- (iii) Radio relics are powered by Diffusive Shock Acceleration (DSA).
- (iv) The Mach number of the shock wave has a shallow radial dependence  $M \propto r^{1/2}$  (Vazza, Brunetti & Gheller 2009; Vazza, Gheller & Brunetti 2010; Hong et al. 2014, and reference therein).
- (v) The merger is taking place in the plane of the sky (i.e. projection effects are minimal), and both shocks travelled the same distance equal to half of the distance of the two relics.

We have estimated the cluster temperature,  $T$ , and the sound speed,  $c_s$ , in the ICM using the  $M_{500}-T$  correlation by Pratt et al. (2009). Assuming (iii), we can derive the Mach number ( $M_{\text{shock}}$ ) of the shock wave from the radio spectral index ( $\alpha$ , Drury 1983). From  $M_{\text{shock}}$  and  $c_s$ , we derived the shock velocity  $v_{\text{shock}}$  as the shock wave propagated outwards, and the time that the shock wave spent to arrive at the position of the relic ( $t_{\text{merger}}$ ). Values of  $d_{r,\text{max}}$  and  $\alpha$  have been taken from de Gasperin et al. (2014, 2015); Riseley et al. (2017). We refer to Table 1 for references on single objects. Unfortunately, no information of  $\alpha$  is available for the clusters A3365, 0212+70 and PSZ1 G096.89+24.1. When  $\alpha \leq 1$ , we have assumed that the spectral index is the injection spectral index. Otherwise, we have



**Figure 7.**  $P_{1.4\text{GHz}}$  versus estimate of the time-since-merger. Blue points are detected haloes, red arrows are upper limits below the  $P_{1.4\text{GHz}}-M_{500}$  correlation, green arrows are upper limits above the  $P_{1.4\text{GHz}}-M_{500}$  correlation.

assumed that the injection spectral index can be derived by flattening the integrated spectral index by 0.5.

We have computed  $t_{\text{merger}}$  independently for each relic. In Fig. 7, we plot the mean of  $t_{\text{merger}}$  for each cluster versus radio halo power. If the time since the merger started is the key quantity to switch on the radio emission in merging clusters, clusters with and without radio haloes should lie in different regions of the plot. We note that A2345 and MACSJ0025 (red arrows in Fig. 7) lie at early and late merger with respect to clusters with double relics and a radio halo. Also clusters with double relics for which we put an upper limit to  $P_{1.4\text{GHz}}$  consistent with the correlation (green arrows in Fig. 7) seem associated with late mergers. However, the sample is too small to draw any conclusions, and no suitable statistical test can help us assessing whether  $t_{\text{merger}}$  plays a role in the formation of the radio halo.<sup>2</sup>

It must be noted that the time-scale  $t_{\text{merger}}$  that we derive here is not the time after core passage ( $t_{\text{cross}}$ ) that is derived through more accurate modelling (see e.g. Golovich et al. 2017). Unfortunately, data do not allow us to derive estimates of  $t_{\text{cross}}$  for all the clusters in the sample. The  $t_{\text{merger}}$  estimates that we have derived are the best estimate that current data can provide, but could be affected by the assumptions (i)–(iv). Once more data are available, the analysis should be repeated using estimates of  $t_{\text{cross}}$  from lensing analysis, to better evaluate the role of the time since core passage.

It must be noted that we are dealing with very small samples. Although non-parametric statistical tests can deal with samples as small as those we have here, our hope is that future radio surveys will increase the sample of clusters with double relics and enable lower upper limits in order to investigate the role of time-scale, mass and mass-ratio.

<sup>2</sup> The Wilcoxon–Mann–Whitney test cannot be used in this case, because we do not want to test whether one variable tends to have values higher than the other, but we want to test whether one variable has a different distribution. Other tests exist in this case, but to our knowledge none of them can be used for small samples.

## 5 CONCLUSIONS

In this work, we have analysed all clusters with double relics known to date, in order to understand why radio halo emission is found in only a fraction of them. Our results can be summarized as follows.

(i) We have developed a new procedure to derive upper limits on the halo emission. We have modelled the radio haloes as exponential functions, as observed by Murgia et al. (2009), and with sizes that follow the observed correlation between  $P_{1.4\text{GHz}}$  and  $R_H$  (Cassano et al. 2007). We also added brightness fluctuations in a range of spatial scales (10–250 kpc) to resemble observed radio haloes. With our method, we have placed upper limits below the  $P_{1.4\text{GHz}}-M_{500}$  correlation for three or four clusters.

(ii) We have recomputed the upper limits to  $P_{1.4\text{GHz}}$  assuming that clusters with double relics do not follow the observed properties of radio haloes, to test the robustness of our limit. In particular, we have modelled the haloes as ellipsoids with sizes much larger than expected from the  $P_{1.4\text{GHz}}$ –halo size correlation. We found that if haloes have a constant brightness, no upper limit can be put below the  $P_{1.4\text{GHz}}-M_{500}$  correlation. Instead, our limits still hold if the brightness distribution is exponential.

(iii) Our analysis indicates that the large beams needed to recover the diffuse emission in data published so far are likely to smooth out the differences in the halo models. However, differences between this new method and previous ones become significant if clusters are observed at low frequency, high resolution and sensitivity. Hence, this method is promising to derive deep upper limits with the new generation of radio instruments, such as LOFAR and the SKA pathfinders.

(iv) Using the *Chandra* archival data, we have computed the cluster morphological parameters. As expected, clusters are placed in the *merger region* of the morphological diagrams, irrespective of the presence or absence of radio haloes. Although projection effects could play a role, clusters with double relics show the highest levels of disturbances in the X-rays. Hence, we conclude that based on the X-ray analysis it remains unexplained why only some clusters with double relics have a radio halo.

(v) Using literature information and under simple assumptions on the clusters properties, we have investigated whether the presence/absence of a radio halo depends on different time-scales since the merger happened ( $t_{\text{merger}}$ ) or on different mass-ratios of the merger sub-clusters. Although the sample of clusters is small, data do not suggest a dependence on the mass-ratio: the null hypothesis that clusters with and without radio haloes can be interpreted as different samples depending on the merger mass-ratio cannot be rejected. We note that clusters without haloes tend to be associated with late and early mergers, but data are too scarce to perform a statistical test.

A different magnetic field in clusters with and without radio haloes could also explain the presence/absence of radio emission. Data are scarce, but do not support this scenario (Bonafede et al. 2011). In addition, it would be hard to understand from a theoretical point of view why clusters with similar masses and merging status should have different magnetic field properties.

According to re-acceleration models, clusters with  $M_{500} \sim 5-7 \times 10^{14} M_{\odot}$  could host radio haloes that become visible only at low radio frequencies (around 150 MHz, see Cassano et al. 2013). These radio haloes should be produced by less-energetic mergers, that cannot inject enough energy to accelerate particles up to  $\sim$  GeV. The upper limits that we have derived are computed from observations at 300 MHz and 1.4 GHz, and these clusters could

host a radio halo at lower frequencies. On going LOFAR and MWA surveys – together with follow-up X-ray and lensing studies – will shed light on this issue, as they are expected to detect more clusters with double relics, increasing the poor statistics we have now, and possibly revealing that either the mass-ratio and/or the time-since-merger play a role in understanding the absence of radio haloes in merging clusters.

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