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Observation of spin-exchange dynamics between itinerant and localized ^{171}Yb atoms

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We report on the observation of the spin-exchange dynamics of ^{171}Yb atoms in the ground state 1S_0 and in the metastable state 3P_0 . We implement the mixed-dimensional two-orbital system using near-resonant and magic-wavelength optical lattices, where the 1S_0 and 3P_0 atoms are itinerant in a one-dimensional tube and localized in three dimensions, respectively. By exploiting an optical Stern-Gerlach method, we observe the spin depolarization of the 1S_0 atoms induced by the spin-exchange interaction with the 3P_0 atom. Our work could pave the way to the quantum simulation of the Kondo effect.

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I. INTRODUCTION

Strongly correlated systems with orbital degrees of freedom exhibit interesting phenomena, with the Kondo effect [1], which is the many-body phenomenon arising from an antiferromagnetic interaction between a conduction electron and a localized magnetic moment, as a prominent example. It was originally studied in the context of the enhancement of the resistivity in magnetic alloys at low temperature, and it is now a ubiquitous problem in condensed-matter physics. Also, the Kondo lattice model, where the localized spins are aligned periodically, is a paradigmatic model of a heavy fermion system. Its phase diagram, called the Doniach phase diagram [2], contains the paramagnetic phase due to the Kondo screening in the strong-coupling regime and the Ruderman-Kittel-Kasuya-Yoshida (RKKY) ordered phase in the weak-coupling regime.

Although the Kondo effect has been intensively studied in solid-state and mesoscopic systems, by exploiting its novel possibilities in the control of system parameters and the detection, ultracold atomic gases in an optical lattice allow one to study the Kondo system in a unique manner, which is challenging to investigate in other systems [3]. In particular, alkaline-earth-like atoms have received much attention due to the presence of the metastable states 3P_0 and 3P_2 as well as the ground state 1S_0 . Taking advantage of the long-lived states, the quantum simulator with orbital degrees of freedom using the 1S_0 and 3P_0 or 3P_2 atoms has been proposed, and the Kondo system using the two-orbital system has been studied theoretically [4–11]. To implement the Kondo system with cold atoms, an antiferromagnetic spin-exchange interaction between mobile and immobile atoms is required. The clock transition spectroscopy in the state-independent optical lattice, called the magic-wavelength optical lattice, reveals that, in contrast to a ferromagnetic coupling of ^{173}Yb and ^{87}Sr [12–14], the fermionic isotope of ^{171}Yb has an antiferromagnetic coupling between the 1S_0 atom and the 3P_0 atom [15]. This suggests that the two-orbital system using ^{171}Yb is a

promising natural candidate for the quantum simulator of the Kondo effect in contrast to the tuning of the spin-exchange coupling via confinement-induced resonances [16]. Another feature of ^{171}Yb is the weak interatomic interaction of 1S_0 atoms, suggesting that the 1S_0 atoms in an optical lattice can be described as a noninteracting metallic state, which is suitable for the exploration of the Kondo physics. Motivated by these unique properties of the two-orbital system using ^{171}Yb , the numerical simulation of the dipole oscillation of the 1S_0 atoms in the presence of the localized 3P_0 atom is performed [11], showing that the Kondo effect manifests itself in such a way that the center-of-mass motion of 1S_0 atoms is suppressed as the temperature is lowered due to the antiferromagnetic spin-exchange interaction.

In this Letter, we report on the observation of the spin-exchange dynamics between ^{171}Yb atoms in the ground state $|g\rangle = |^1S_0\rangle$ and in the metastable state $|e\rangle = |^3P_0\rangle$. Using a two-orbital lattice system consisting of a two-dimensional (2D) magic-wavelength optical lattice and a 1D near-resonant optical lattice giving strong confinement to the $|e\rangle$ atom alone and no net effect to the $|g\rangle$ atom, the quasi-(0+1)D system is implemented, where the $|g\rangle$ atom behaves as the quasi-1D free fermion interacting with the $|e\rangle$ atom mimicking a localized magnetic moment. By exploiting the optical Stern-Gerlach method, we observe the relaxation of the spin polarization caused by the interorbital spin-exchange process and the suppression of the spin depolarization in a high magnetic field. The rate of spin-exchange dynamics is also controlled by the excited-state population. These observations are an important first step toward the quantum simulation of the Kondo effect.

II. METHODS

We first explain how we implement the quasi-(0+1)D system using a near-resonant optical lattice. An optical dipole potential $V(\mathbf{r})$ is proportional to the laser intensity $I(\mathbf{r})$:

$$V(\mathbf{r}) = -\frac{1}{4}\alpha I(\mathbf{r}). \quad (1)$$

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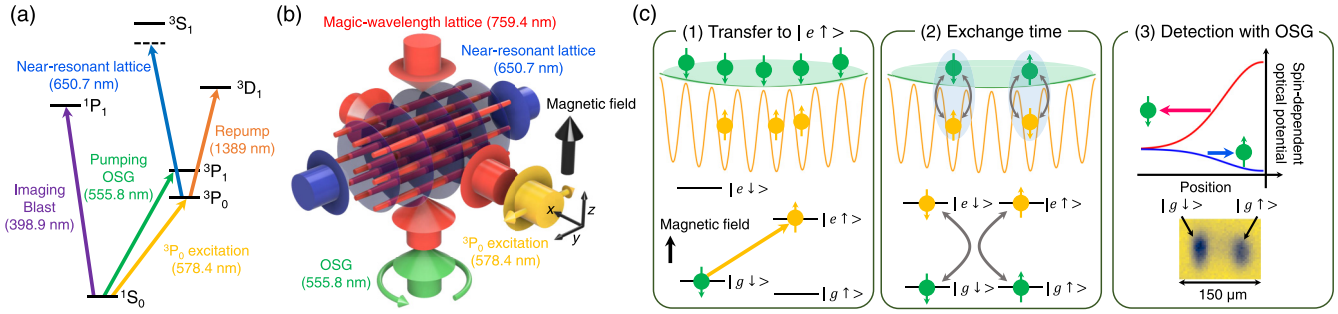


FIG. 1. Schematic diagram of experiment. (a) Relevant energy diagram of a Yb atom. (b) Schematic illustration of beam configuration. The polarization of the clock excitation light is perpendicular to the quantization axis defined by the magnetic field, and it amounts to an equal mixture of σ_+ and σ_- polarization. The circularly polarized OSG light propagates along the quantization axis. (c) Schematic illustration of the experimental procedure. (1) Initially, some fraction of the atoms in the $|g \downarrow\rangle$ state (a green ball) are excited to the $|e \uparrow\rangle$ state (a yellow ball) in a magnetic field of 30 G. The upper figure shows the schematic representation of the optical lattice potentials for the $|g\rangle$ atom (a green curve) and the $|e\rangle$ atom (a yellow curve). (2) After the excitation, a magnetic field is lowered to 0.5 G, and the spin-exchange dynamics is started. (3) After the hold time, the population of the atoms in $|g \uparrow\rangle$ and in $|g \downarrow\rangle$ is detected with an OSG technique. The upper figure shows the spin-dependent optical gradient potential to spatially separate the $|g \uparrow\rangle$ atom and the $|g \downarrow\rangle$ atom. The lower figure shows a typical example of the simultaneous observation of both spin states in the false color TOF image of the ^{171}Yb gas in the $|g\rangle$ state subjected to the OSG light.

The coefficient α is called polarizability:

$$\alpha = \sum_i \frac{6\pi c^2}{\omega_i^3} \left(\frac{\Gamma_i}{\omega_i - \omega} + \frac{\Gamma_i}{\omega_i + \omega} \right), \quad (2)$$

where ω is the laser angular frequency and c is the speed of light. Here ω_i and Γ_i correspond to the resonant angular frequency and the natural linewidth of the i th state, respectively. The wavelength of the near-resonant optical lattice is chosen to be 650.7 nm, which is close to the 3P_0 - 3S_1 transition wavelength of 649.1 nm, resulting in the large polarizability for the $|e\rangle$ atom α_e [see Fig. 1(a) for relevant energy levels]. Using Eq. (2), the polarizability is obtained as $\alpha_e/h = 1.4$ kHz/(mW/cm²), h being the Planck constant. In this calculation, we assume that the 3P_0 - 3S_1 transition makes the dominant contribution and the other transitions are negligible. Similarly, the polarizability for the $|g\rangle$ atom α_g due to the 650.7 nm light is also calculated as $\alpha_g/h = 39$ Hz/(mW/cm²). As a result, the near-resonant optical lattice has the large polarizability ratio $\alpha_e/\alpha_g = 36$, while a similar experiment in Ref. [16] uses a state-dependent lattice with $\alpha_e/\alpha_g = 3.3$. In our experiment, the $|e\rangle$ atom is deeply confined by the near-resonant lattice while the lattice potential is regarded as the continuum system for the $|g\rangle$ atom. A natural concern of using near-resonant light is the possibly non-negligible photon scattering loss rate γ_{sc} of the $|e\rangle$ atoms. By using narrow-linewidth band-pass filters with less than 0.1 nm to suppress the 649.1 nm resonant frequency component in the single-mode narrow-linewidth 650.7 nm laser, we obtain the loss rate of the $|e\rangle$ atom in the absence of the $|g\rangle$ atom $\gamma_{sc} = 5.0$ Hz. Although this is larger than the theoretically estimated value of 0.59 Hz obtained by assuming only the off-resonant excitation, the corresponding lifetime is long enough to clearly observe the spin-exchange dynamics (see Sec. III). A state-independent optical lattice is obtained with the magic wavelength of 759.4 nm.

Figure 1(b) illustrates the schematic diagram of the beam configuration. The 2D array of the tube traps is produced using the 2D magic-wavelength lattice (x and z), and the 1D near-resonant optical lattice is superimposed along the axis

of the tubes (y). As a result, the $|e\rangle$ atom is localized by the 3D confinement while the $|g\rangle$ atom is mobile along the y direction in the tube potential. The maximum potential depth for the $|e\rangle$ atom due to the near-resonant lattice amounts to $27E_R$, with $E_R = k_B \times 96$ nK being the recoil energy for the magic wavelength. Here k_B is the Boltzmann constant. The corresponding trap frequency of the lattice site at the trap center is 24 kHz, and the residual harmonic trap frequency due to the Gaussian beam shape is estimated as 24 Hz from the beam radius.

The near-resonant lattice depth is calibrated using diffraction of the $|e\rangle$ atoms by a pulsed optical lattice technique with the near-resonant lattice [17]. We use the ^{171}Yb atom for the calibration of the lattice depth since the bosonic isotopes would suffer from the severe inelastic loss in the 3P_0 states, in addition to another technical merit that the Rabi frequency of the clock transition for the fermionic isotopes is larger than that for bosonic isotopes. After the excitation to the $|e\rangle$ state in the 3D magic-wavelength lattice, the remaining atoms in the $|g\rangle$ state are blasted with the resonant light with the 1S_0 - 1P_1 transition. Then the magic-wavelength lattice potential along the y axis is ramped down in 1 ms, and the pulsed lattice is irradiated along the y axis immediately after switching off the remaining magic-wavelength lattice potentials along the x and z axes. During the time-of-flight (TOF), the atoms are repumped into the $|g\rangle$ state using the resonant light with the 3P_0 - 3D_1 transition, and the diffraction pattern is probed by absorption imaging with the 1S_0 - 1P_1 transition. From the oscillatory behavior of the diffraction pattern, we can calibrate the near-resonant lattice depth.

Our experiments start with the preparation of the quantum degenerate gas of ^{171}Yb using the sympathetic evaporative cooling with ^{173}Yb [15]. During the evaporative cooling, the optical pumping into the $|g \downarrow\rangle$ state is performed with the 1S_0 - 3P_1 ($F' = 1/2$) transition, where $|\uparrow\rangle = |m_F = +1/2\rangle$, $|\downarrow\rangle = |m_F = -1/2\rangle$ denote the projections of the nuclear spin F onto the quantization axis defined by a magnetic field. The number of atoms N and the temperature scaled by the Fermi temperature T/T_F are $N \simeq 2 \times 10^4$ and $T/T_F \simeq 0.3$,

respectively. After the removal of ^{173}Yb atoms using the resonant light associated with the $^1S_0\text{-}^3P_1$ ($F' = 7/2$) transition, the atoms are loaded into the optical lattices, where the initial depths of the magic-wavelength optical lattice and the near-resonant optical lattice for the $|e\rangle$ atom are set to $30E_R$ and $6.8E_R$, respectively. Figure 1(c) shows the experimental procedure after loading atoms into an optical lattice. (i) Some fraction of the atoms are coherently transferred to the $|e \uparrow\rangle$ state in a magnetic field of 30 G by a stabilized clock laser [18] with a typical linewidth of a few Hz. To localize the $|e\rangle$ atom, the near-resonant optical lattice is then ramped up to $27E_R$ in 1 ms, which is longer than the inverse of the lattice-site trap frequency, regarded as an adiabatic ramp. To reduce the spatial inhomogeneity of the clock transition frequency due to the residual harmonic trap created by the near-resonant optical lattice, the $|g\rangle$ atoms are coherently transferred to the $|e\rangle$ state in the shallower optical lattice. A moderate lattice depth is required for the sideband-resolved excitation, on the other hand, which allows one to prepare $|e\rangle$ atoms in the lowest band. We thus perform the clock excitation with the lattice depth of $6.8E_R$. The hopping energies between the nearest-neighbor tubes J_\perp and between the adjacent sites of the near-resonant optical lattice J_y are estimated as $J_\perp = h \times 1.0$ Hz and $J_y = h \times 7.0$ Hz for the $|e\rangle$ atom, indicating that the hopping energy is negligible within the experimentally relevant timescales. (ii) After the clock excitation, the magnetic field is rapidly lowered to 0.5 G with about 3 ms settling time, and the spin-exchange dynamics is initiated. (iii) After the hold time, the spin polarization of the $|g\rangle$ atoms is detected with the optical Stern-Gerlach technique (OSG) [19], which enables one to separately observe the atoms in the $|g \uparrow\rangle$ and $|g \downarrow\rangle$ states using a spin-dependent optical potential gradient. The OSG light is blue-detuned by 875 MHz from the $^1S_0\text{-}^3P_1$ ($F' = 1/2$) transition.

III. RESULTS

Figure 2(a) shows the time evolution of the spin polarization of the $|g\rangle$ atoms, defined as $\Delta N_g/N_g$. Here ΔN_g denotes the atom number difference between the $|g \uparrow\rangle$ and $|g \downarrow\rangle$ states, and N_g is the total number of the $|g\rangle$ atoms. The result clearly shows the spin depolarization due to the spin-exchange interaction with $|e\rangle$ atoms. We note that we did not observe the depolarization in the case of no $|e\rangle$ atoms. Also, the relaxation rate of the spin polarization is controlled by the clock excitation rate r , which is associated with the number of $|e\rangle$ atoms. The spin polarization less than unity at the initial time could be ascribed to the imperfect optical pumping and the photon-scattering of the OSG light. It is noted that the remaining unwanted spin component is not removed after the optical pumping.

The observed relaxation dynamics is quantitatively analyzed with the following two-body rate equations [13]:

$$\begin{aligned} \dot{p}_{g\uparrow}(t) = & \Omega_{\text{ex}}[p_{g\downarrow}(t)p_{e\uparrow}(t) - p_{e\downarrow}(t)p_{g\uparrow}(t)] \\ & - \Gamma_{eg}p_{g\uparrow}(t)[p_{e\uparrow}(t) + p_{e\downarrow}(t)] \\ & + \frac{\gamma_{\text{sc}}}{2}[p_{e\uparrow}(t) + p_{e\downarrow}(t)], \end{aligned} \quad (3)$$

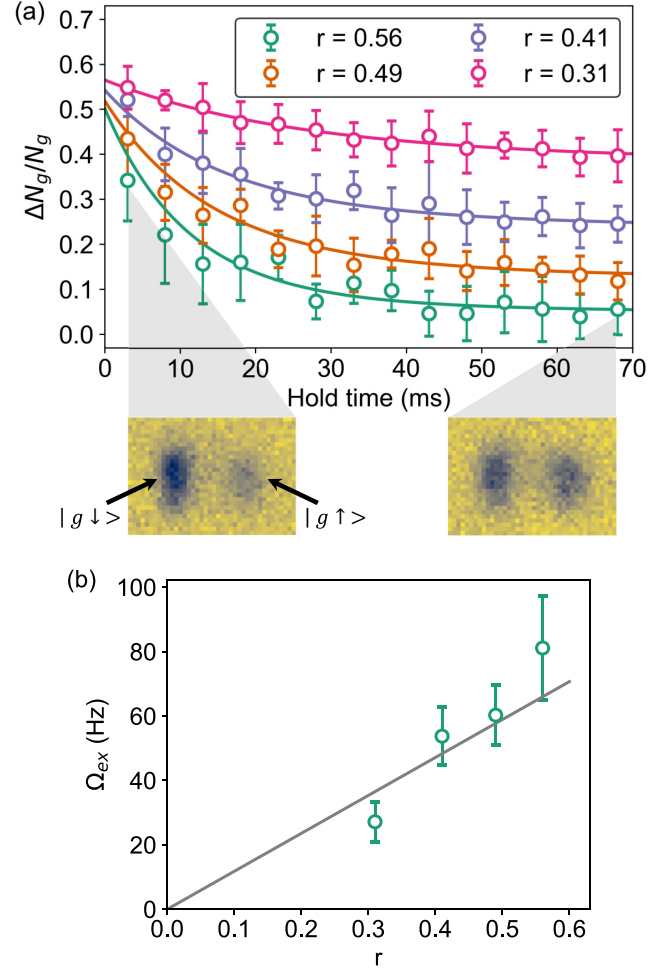


FIG. 2. Observation of spin-exchange dynamics. (a) Time evolution of the spin polarization of the $|g\rangle$ atoms $\Delta N_g/N_g$ with the different excitation rates to the $|e\rangle$ state: $r = 0.56, 0.49, 0.41$, and 0.31 . Error bars show the standard deviations of the mean values obtained by averaging 10 measurements. Solid lines represent fits to the data with Eqs (3)–(6). False color time-of-flight images of the $|g\rangle$ atoms after the spin-exchange dynamics with $r = 0.56$ are shown. The left and right figures correspond to the hold time of 3 and 68 ms, respectively. (b) Spin-exchange rate Ω_{ex} as a function of the excitation rate. Error bars are 1σ confidence intervals of the data fits. The solid line represents linear fits to the data.

$$\begin{aligned} \dot{p}_{g\downarrow}(t) = & \Omega_{\text{ex}}[p_{e\downarrow}(t)p_{g\uparrow}(t) - p_{g\downarrow}(t)p_{e\uparrow}(t)] \\ & - \Gamma_{eg}p_{g\downarrow}(t)[p_{e\uparrow}(t) + p_{e\downarrow}(t)] \\ & + \frac{\gamma_{\text{sc}}}{2}[p_{e\uparrow}(t) + p_{e\downarrow}(t)], \end{aligned} \quad (4)$$

$$\begin{aligned} \dot{p}_{e\uparrow}(t) = & \Omega_{\text{ex}}[p_{e\downarrow}(t)p_{g\uparrow}(t) - p_{g\downarrow}(t)p_{e\uparrow}(t)] \\ & - \Gamma_{eg}p_{e\uparrow}(t)[p_{g\uparrow}(t) + p_{g\downarrow}(t)] \\ & - \gamma_{\text{sc}}p_{e\uparrow}(t), \end{aligned} \quad (5)$$

$$\begin{aligned} \dot{p}_{e\downarrow}(t) = & \Omega_{\text{ex}}[p_{g\downarrow}(t)p_{e\uparrow}(t) - p_{e\downarrow}(t)p_{g\uparrow}(t)] \\ & - \Gamma_{eg}p_{e\downarrow}(t)[p_{g\uparrow}(t) + p_{g\downarrow}(t)] \\ & - \gamma_{\text{sc}}p_{e\downarrow}(t). \end{aligned} \quad (6)$$

Here $p_{\alpha\sigma}(t) = \bar{n}_{\alpha\sigma}(t)/\bar{n}_0$ denotes the relative population of the atom in the $|\alpha\sigma\rangle$ state ($\alpha = g, e, \sigma = \uparrow, \downarrow$), where $\bar{n}_{\alpha\sigma}$ and \bar{n}_0 denote the mean density of the atom in the $|\alpha\sigma\rangle$ state and the mean density of the total atoms in the initial state, respectively. Also, Ω_{ex} and Γ_{eg} correspond to the spin-exchange rate and the two-body loss rate between the $|g\rangle$ atom and the $|e\rangle$ atom, respectively, and they are proportional to \bar{n}_0 . In addition, γ_{sc} is the one-body loss rate of the $|e\rangle$ atom. We assume that the inelastic collision between the $|e\rangle$ atoms is ignored since the hopping rates J_{\perp} and J_y are much smaller than the spin depolarization rate. In addition, Γ_{eg} is assumed to be independent of the spin state and is estimated from the measurement of the lifetime of the $|e\rangle$ atom during the spin-exchange dynamics, resulting in $\Gamma_{eg} = 10$ Hz. On the other hand, using the inelastic loss-rate coefficient $\beta_{eg\pm} \leq 2.6(3) \times 10^{-16} \text{ cm}^3/\text{s}$ obtained by the measurement of the lifetimes of the $|eg^+\rangle$ and $|eg^-\rangle$ states in the 3D magic-wavelength optical lattice [20], the two-body loss rate is calculated as 2.3×10^{-2} Hz, where $|eg^+\rangle$ and $|eg^-\rangle$ correspond to the spin-singlet state and the spin-triplet state, respectively. Although the origin of the discrepancy is not known, here we note that the analysis using Eqs. (3)–(6) does not depend sensitively on the value of Γ_{eg} , due to the existence of photon scattering loss $\gamma_{\text{sc}} = 5$ Hz, and in fact $\Gamma_{eg} = 10$ Hz and $\Gamma_{eg} = 0$ give almost the same results. In the following analysis, we adopt $\Gamma_{eg} = 10$ Hz. It should be noted that the two-body loss between the $|e\rangle$ atoms via a tunneling process is suppressed due to the on-site repulsive interaction and the two-body dissipation via a quantum Zeno effect [21,22]. In our experiment, this effective loss rate is estimated as 0.28 Hz, suggesting that the inelastic loss between the $|e\rangle$ atoms would not occur during the spin-exchange dynamics. Solid lines in Fig. 2(a) represent the fits to the data using the two-body rate equations (3)–(6) by treating Ω_{ex} as a free parameter. Figure 2(b) shows the spin-exchange rate obtained from the data fits in Fig. 2(a) as a function of the excitation rate to the $|e\rangle$ state, exhibiting an enhancement of the spin-exchange rate with the increase of the number of atoms in the $|e\rangle$ state. The linear dependence of the spin-exchange rate Ω_{ex} on the excitation rate r is expected when no correlation between the $|e\rangle$ atoms is considered. The validity of this assumption is related to the characteristic energy of the RKKY interaction $V_{\text{ex}}^2/\epsilon_{\text{F}}$ [23], where V_{ex} and ϵ_{F} are the spin-exchange energy and the Fermi energy, respectively. In our experiment, this is estimated as $k_{\text{B}} \times 1.4$ nK, which is much smaller than the atomic temperature. Thus, the RKKY correlation is negligible. In addition, this linearity is expected for a small excitation rate, and the investigation of the spin-exchange dynamics with a higher excitation rate will be an interesting future study.

Also, we investigate the magnetic-field dependence of the spin-exchange dynamics. The interorbital spin-exchange interaction energy V_{ex} can be estimated as

$$V_{\text{ex}} = \frac{4\pi\hbar^2}{m} \frac{a_{eg}^+ - a_{eg}^-}{2} \int d^3\mathbf{r} n_g(\mathbf{r}) |\psi_e(\mathbf{r})|^2, \quad (7)$$

where m denotes the mass of the atom and $\psi_e(\mathbf{r})$ is the single-particle wave function of the $|e\rangle$ atom. The spin-exchange is characterized by the difference between the spin-singlet scattering length $a_{eg}^+ = 240(4)a_0$ and the spin-triplet scattering

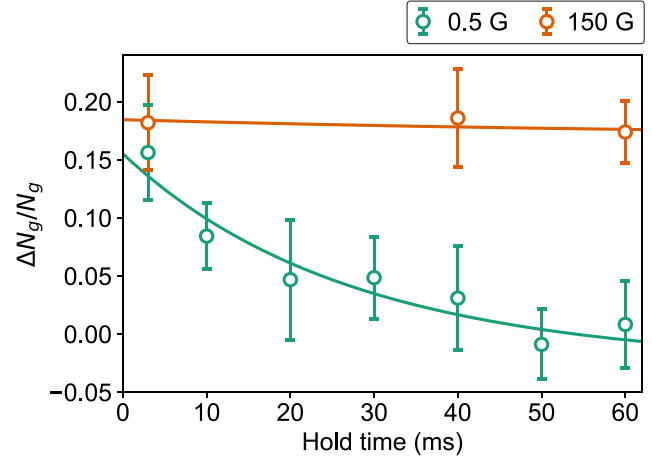


FIG. 3. Magnetic-field dependence of spin-exchange dynamics with the 3P_0 excitation rate $r = 0.56$. Error bars show the standard deviations of the mean values obtained by averaging 10 measurements. In this experiment, the initial state of the exchange dynamics is prepared by the excitation $|g \uparrow\rangle \rightarrow |e \uparrow\rangle$ of the spin-balanced ^{171}Yb atoms using π -polarized light since this scheme results in reduced uncertainty.

length $a_{eg}^- = 389(4)a_0$ [20], resulting in an antiferromagnetic coupling $V_{\text{ex}} < 0$. Here a_0 denotes the Bohr radius. In the central tube, V_{ex} is estimated to be $V_{\text{ex}}/h = -0.25$ kHz. On the other hand, the differential Zeeman shift between the $|g \uparrow\rangle$ state and the $|e \uparrow\rangle$ state amounts to $-200.0(6)$ Hz/G [15]. Figure 3 shows a comparison between the spin relaxation dynamics in a magnetic field of 0.5 G and that in a magnetic field of 150 G, where the Zeeman energy is two orders of magnitude larger than V_{ex} . The result shows that the spin depolarization dynamics is frozen in a higher magnetic field, which is consistent with the fact that the spin-exchange process is energetically costly.

IV. CONCLUSIONS

In conclusion, we successfully realized the quasi-1D fermion system in the presence of immobile spin using the 2D magic-wavelength optical lattice and the 1D near-resonant optical lattice. Using this system, the spin-exchange dynamics between the itinerant $|g\rangle$ atom and the localized $|e\rangle$ atom is observed. Our work can pave the way to the quantum simulation of the Kondo effect. Although the near-resonant lattice causes the one-body loss of the $|e\rangle$ atom, which is detrimental to the exploration of many-body physics, the scattering rate γ_{sc} will be reduced by using a far-detuned laser source with, for example, a wavelength of 652 nm. It will be interesting in future work to compare the observed spin-exchange rates with theoretical calculations [24–26]. The Kondo effect manifests itself as a many-body singlet state, resulting in the screening of a localized spin by an itinerant fermion, which is called Kondo screening. The screening cloud of itinerant fermions could be observed in the two-orbital system using a Yb quantum gas microscope [27,28], as in a quantum dot system [29]. In addition, it is interesting to detect the spin correlation between the excited-state atoms as a signature of the RKKY interaction [4].

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