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**Citation for published version:**

Keen, HDJ, Julian, SR & Hermann, A 2021, 'Ab initio study of pressure-induced structural and electronic phase transitions in Ca<sub>2</sub>RuO<sub>4</sub>', *Physical Review B*, vol. 104, no. 8, 085143, pp. 1-8.  
<https://doi.org/10.1103/PhysRevB.104.085143>

**Digital Object Identifier (DOI):**

[10.1103/PhysRevB.104.085143](https://doi.org/10.1103/PhysRevB.104.085143)

**Link:**

[Link to publication record in Edinburgh Research Explorer](#)

**Document Version:**

Peer reviewed version

**Published In:**

Physical Review B

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# *Ab initio* study of pressure-induced structural and electronic phase transitions in $\text{Ca}_2\text{RuO}_4$

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(Dated: August 24, 2021)

$\text{Ca}_2\text{RuO}_4$  is a compound with a Mott insulating ground state, which responds to external pressure in a variety of ways, some of which are expected (an insulator-metal transition) while others are more surprising (an expansion of the  $c$  lattice constant). We provide here a comprehensive study of these pressure-induced structural and electronic changes using DFT+U calculations, and demonstrate generally good agreement with experiment. The insulator-metal transition is reproduced and coincides with an isostructural transition, the  $c$  lattice expansion,  $\text{RuO}_6$  octahedral distortions and associated changes to the Ru  $4d$  orbital order. The metallic part of the phase diagram features several competing phases. The high-pressure  $Bbcm$  phase is found to be unstable in the ground state over a broad pressure range and suggested to be thermally stabilised instead.

$\text{Ca}_2\text{RuO}_4$  is a layered perovskite compound with a rich phase diagram, featuring a metal-insulator transition with a structural distortion upon cooling, antiferromagnetic ordering upon further cooling, and metallisation and ferromagnetic order, followed by a further structural transition, under pressure [1–3]. It is one end member of the  $\text{Ca}_{2-x}\text{Sr}_x\text{RuO}_4$  series that includes the unconventional superconductor  $\text{Sr}_2\text{RuO}_4$  at the other end [4, 5].  $\text{Ca}_2\text{RuO}_4$  shows intriguing collective phenomena in its own right, such as pressure-driven superconductivity, electric-field-induced metallisation, negative thermal expansion, and a Higgs mode [6–9]. Several of these properties are intricately linked to structural distortions of the  $\text{RuO}_6$  octahedra, which in turn can be controlled by applying hydrostatic [2, 3] or uniaxial [10, 11] pressure or strain.

High-pressure resistivity and x-ray and neutron diffraction measurements of  $\text{Ca}_2\text{RuO}_4$  have been reported [2, 3]. At 0.5 GPa at room temperature  $\text{Ca}_2\text{RuO}_4$  undergoes a Mott insulator-metal transition [2], which is accompanied by a simultaneous first-order structural transition [3] that retains the same orthorhombic symmetry. The transition pressure is insensitive to cooling [2]. The low pressure insulating phase is referred to as  $S\text{-}Pbca$  (with a ‘short’  $c$ -axis) and the high pressure metallic phase as  $L\text{-}Pbca$  (with a ‘long’  $c$ -axis, this is also the high-temperature ambient pressure phase). The metallic  $L\text{-}Pbca$  phase is a two-dimensional, itinerant ferromagnet [2]. Upon pressure increase both  $S\text{-}Pbca$  and  $L\text{-}Pbca$  show rather peculiar structural behaviour: an expansion of the  $c$  lattice constant as a function of pressure, i.e.  $\partial c/\partial P > 0$  [3]. This behaviour persists until a second-order structural phase transition from  $L\text{-}Pbca$  to a higher symmetry  $Bbcm$  phase at 5.5 GPa, which marks a maximum in  $c$ . Within the  $Bbcm$  phase the  $c$  axis returns to conventional behaviour;  $\partial c/\partial P < 0$ . In the transition from the  $L\text{-}Pbca$  to  $Bbcm$  the octahedral tilt against the  $c$  axis vanishes, while the system remains metallic. This sequence of structural and electronic changes remains unexplored from an *ab initio* perspective.

At ambient conditions, the electronic structure of  $\text{Ca}_2\text{RuO}_4$  has been explored in several computational studies, which typically combine density functional (DFT) and dynamical mean field theory to capture the dominant Mott insulator physics, and tend to focus largely on magnetic degrees of freedom [12–21]. However, these studies have all used experimental lattice parameters (in some cases interpolations between  $S\text{-}$  and  $L\text{-}Pbca$  or along the  $\text{Ca}\text{-}\text{Sr}$  composition axis) and almost all bypass the relative energies of the different structures. While there is recognition that the Mott transition in  $\text{Ca}_2\text{RuO}_4$  correlates with structural changes [18–20], pressure effects have only very recently been modeled, in a Landau-Ginzburg free energy expansion of the ambient pressure structures [20] and dynamical mean field theory applied to experimental high-pressure structures [21].

In this paper, we study the high-pressure phase evolution of  $\text{Ca}_2\text{RuO}_4$  using DFT and DFT+ $U$  calculations. We consider a range of on-site repulsion terms  $U$  in order to reflect the expected sensitivity of  $U$  to pressure. All presented structures are fully self-consistent, with simultaneously optimised electron density and crystal structure. This work presents the first reported attempt at calculations of this type for  $\text{Ca}_2\text{RuO}_4$ . We reproduce the first-order structural phase transition and show that it coincides with the insulator-metal transition. We also find that the  $c$  lattice expansion under pressure in the  $S\text{-}Pbca$  and (to some extent)  $L\text{-}Pbca$  phases correlates with octahedral distortions and changes in the Ru  $4d$  occupancies, reaffirming the intimate connection between electronic and structural degrees of freedom in  $\text{Ca}_2\text{RuO}_4$ . While the insulating  $S\text{-}Pbca$  phase is robust in our calculations, we find several different metallic  $Pbca$  ground state phases, indicating a complex energetic landscape in the metallic region of the phase diagram.

## I. COMPUTATIONAL METHOD

DFT calculations are carried out using the Vienna *Ab initio* Simulation Package (VASP) [22] using the Perdew, Burke and Ernzerhof (PBE) exchange-correlation functional [23] in conjunction with a plane wave basis (cutoff energy  $E_c = 500$  eV) and the projector augmented wave method [24]. Tests with the LDA and SCAN functionals [25, 26] revealed qualitatively similar results (see the Supplemental Material, SM, for details [27]). Brillouin zones are sampled using regular  $8 \times 8 \times 4$  k-point grids. All lattice vectors and atomic positions are fully optimised at all pressures, and considered converged once all force components are smaller than 1 meV/Å. The inclusion of spin-orbit coupling (SOC) is prohibitively expensive for the number of calculations we present here. In addition, our tests at zero pressure show that SOC does not significantly influence the results (see the SM), so it is omitted here.

Magnetism is an important ingredient for enforcing a realistic orbital structure on the Ru sites, which is in turn intimately connected to the octahedral distortions. In fact, the failure to include magnetism can induce spurious structural and electronic properties (see SM). However, correlation between Ru moments should have little influence on the crystal structure, so for all calculations presented here we use a uniform ferromagnetic state with moments along  $c$ . The effect of single-ion anisotropy (which forces moments to lie roughly in the  $ab$ -plane in experiment) relies on the inclusion of SOC [3], so it is a small effect which we neglect here.

The treatment of Coulomb interactions between localised states in DFT is insufficient to capture the Mott localisation of the Ru  $4d$  electrons that controls the physics of  $\text{Ca}_2\text{RuO}_4$ . The only available approach for correcting the over-delocalisation of these states that also allows for structural relaxation under pressure is the DFT+ $U$  method [32]. For our calculations, we use the simplified formalism by Dudarev [33] with a single effective parameter  $U$  (sometimes referred to as  $U_{\text{eff}} = U - J$  in the literature).

The pressure dependence of  $U$  is not straightforward. As the application of pressure is expected to delocalise electrons, the failures of DFT should become less severe under compression. From a DFT+ $U$  perspective, increasing pressure should thus be accompanied by a corresponding decrease in the correction  $U$ . In this work the precise pressure dependence of  $U$  is not pursued. Instead, all calculations are performed for a range of  $U$  values in the vicinity of the Mott transition. Qualitatively, the complete picture will be an interpolation from results at large  $U$  at low pressures to the results at small  $U$  for high pressures.

## II. RESULTS

The results of our calculations are presented as fol-

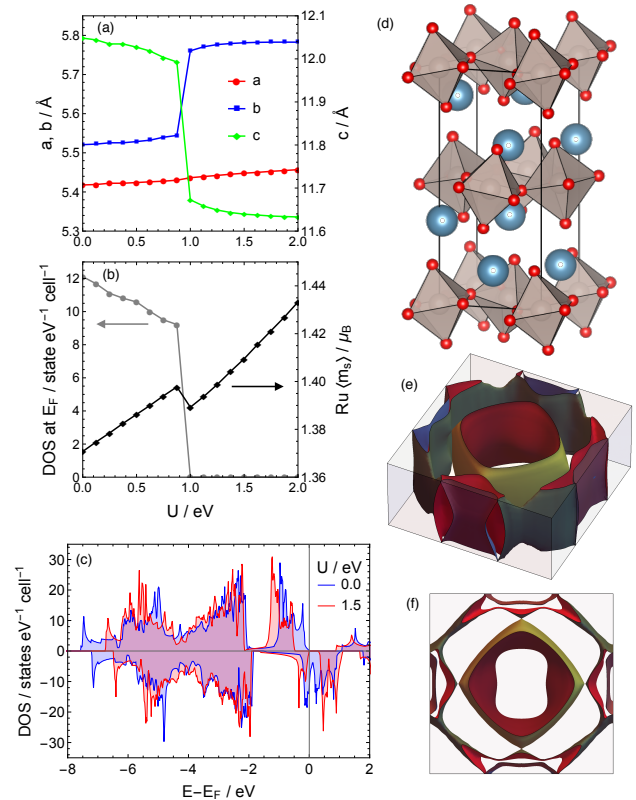


FIG. 1. (a) Optimised lattice parameters of  $\text{Ca}_2\text{RuO}_4$  at atmospheric pressure as function of  $U$ . Left axis is for  $a$  and  $b$ , right axis for  $c$ . (b) DOS at the Fermi energy (left axis) and average Ru spin moment (right axis) as a function of  $U$  at atmospheric pressure. (c) Spin-resolved DOS near the Fermi energy for  $U = 0.0$  eV (a half-metallic phase) and  $U = 1.5$  eV (an insulating phase). (d) The experimental  $S-Pbca$  crystal structure. Blue spheres are Ca, brown polyhedra are the  $\text{RuO}_6$  octahedra. (e) The Fermi surface for  $U = 0.0$  eV. (f) The Fermi surface viewed along  $k_z$ .

lows: In section II A the  $U$  dependence of  $\text{Ca}_2\text{RuO}_4$  is probed at zero pressure. The phase diagram in  $(P, U)$  space is presented in section II B where pressure driven phase transitions are identified with reference to crystal structures and the electronic density of states (DOS). In section II C and II D respectively the octahedral distortions and Ru  $4d$  orbital structure are examined more closely to identify signatures of the pressure driven phase transitions. Finally, in section II E, the stability of the high symmetry  $Bbcm$  phase is considered with reference to the relaxed  $Pbca$  structures at high pressure.

### A. Atmospheric pressure

DFT, without any corrections for strong Coulomb interactions, incorrectly predicts that  $\text{Ca}_2\text{RuO}_4$  is a metal at atmospheric pressure. The addition of the on-site  $U$  term is sufficient to correct this. Figure 1 shows the  $U$  dependence of the crystal and electronic structure. For

$U < 1$  eV the system relaxes into a half-metallic state with  $c \sim 12.05$  Å. This is somewhat shorter than the experimental measurements of the metallic L-*Pbca* phase, which are  $c = 12.26$  Å at 400 K and atmospheric pressure [34], and  $c = 12.29$  Å at 295 K and 1 GPa [3]. While the Fermi surface is largely two-dimensional (Figure 1e–f), this half-metallic phase also has a large spin moment of  $1.4 \mu_B$ , which is inconsistent with the small itinerant moment of  $\sim 0.4 \mu_B$  seen in the L-*Pbca* phase [2, 3]. For  $U \geq 1.0$  eV the system relaxes into an insulating phase where the  $c$  axis drastically shortens and the difference between the  $a$  and  $b$  axes increases. This is accompanied by a reduced bandwidth and a gap opening in the spin-minority DOS. The lattice parameters of this phase are broadly consistent with the insulating S-*Pbca* phase at low temperature measured by Porter *et al.* [34], albeit with a slightly exaggerated difference between  $a$  and  $b$ . The large moment size of  $1.4 \mu_B$  persists in this insulating phase, consistent with experiment [3].

### B. Pressure-induced *Pbca* transitions

The optimised structures at atmospheric pressure serve as a starting point for our calculations under pressure. For a selection of  $U$ , these structures are compressed up to an external pressure of 20 GPa; firstly in steps of 0.2 GPa up to 2 GPa, then in steps of 0.5 GPa. Each calculation starts from the optimised structure at the preceding pressure. In this section we present the lattice vectors and classify structures based on the DOS; the more subtle structural features of the octahedra are discussed in section II C.

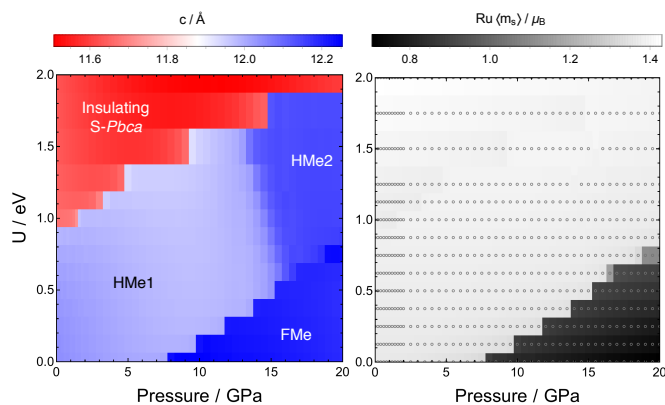


FIG. 2. *Left*: Phase diagram of the  $\text{Ca}_2\text{RuO}_4$  ground state in  $(P, U)$  space, based on analysis of *Pbca* structures. Four phases are identified: insulating S-*Pbca*, half-metallic *Pbca*-1 (HMe1), half metallic *Pbca*-2 (HMe2), and a fully metallic *Pbca* (FMe). Colour scale indicates the length of the  $c$  axis. *Right*: The magnitude of the Ru spin moment in  $(P, U)$  space. Overlaid points show the grid of calculations used to build both diagrams.

Figure 2 shows the main result as a phase diagram in

$(P, U)$  space. The insulating S-*Pbca* phase becomes less stable under compression, and a pressure-driven phase transition to the half-metallic phase (HMe1) appears. With increased pressure the landscape becomes more complex as new metallic phases appear. For small  $U$ , a fully metallic phase (FMe) appears with a longer  $c$  axis and much smaller moment of  $\sim 0.8 \mu_B$ , much closer to experiment and indicative of itinerant electron magnetism. For larger  $U$ , this is replaced by a second half-metallic phase (HMe2) with an intermediate  $c$  axis length. The Fermi surfaces and DOS's of these two new metallic phases are shown in figure 3. Compared to the first HMe1 (as shown in figure 1 and discussed in the previous section), both of these structures have much larger bandwidths. For smaller  $U$ , where on-site Coulomb interactions are energetically less penalising, both spin channels cross the Fermi energy and a smaller total moment is stabilised. For larger  $U$ , the cost of double occupancy in the Ru  $4d$  states is too severe, and thus the large moment and half-metallicity is preserved. The Fermi surfaces show that both high-pressure metals, HMe2 and FMe, are more two-dimensional than HMe1, and have promising support for nesting vectors.

The consequences of these transitions on the lattice parameters are shown in figure 4, compared with experimental data. Despite the S→L transition being sharply first order, the S-*Pbca* phase shows a smooth upturn in the  $c$  lattice constant prior to the transition pressure, reproducing the  $c$  axis increase seen in experiment. Of the metallic phases on offer, the FMe phase offers the best agreement with experiment in both the length of the  $c$  axis, and in predicting that  $a \approx b$ . However, it does not show an increase of the  $c$  axis,  $\partial c/\partial P > 0$ , whereas the boundary between the two half-metallic phases does. Nevertheless, the experimental data for the  $c$  axis in the L-*Pbca* phase is rather noisy. This may be indicative of the complex energetic landscape that the metallic phase navigates, and the positive slope a result of the imminent *Bbcm* phase.

The insulator-metal transition pressure is extremely sensitive to changes in  $U$ . The experimental transition pressure is 0.5 GPa at room temperature [3], and remains unchanged at much lower temperatures [2]. This suggests that  $U \lesssim 1.0$  eV is appropriate for modelling the S-*Pbca* phase. Furthermore, for any comparisons it is important to appreciate the significant temperature dependence of the  $\text{Ca}_2\text{RuO}_4$  crystal structure. Low-temperature structural data exists only at ambient pressure [34] and is included in Figure 4. Within the S-*Pbca* phase, the  $c$  lattice constant expands with increased temperature, while  $b$  contracts (both with coefficients  $\alpha \approx \pm 10^{-4} \text{K}^{-1}$ ) and  $a$  remains constant. Our ground state results for  $U \leq 1.0$  eV are therefore in good agreement with experimental data on the S-*Pbca* phase. For L-*Pbca*, comparisons are further complicated by lack of thermal expansivity data at high pressure. Figure 4 implies that the FMe phase stabilised with  $U = 0.0$  eV at high pressure, gives the best agreement with experiment. This is not

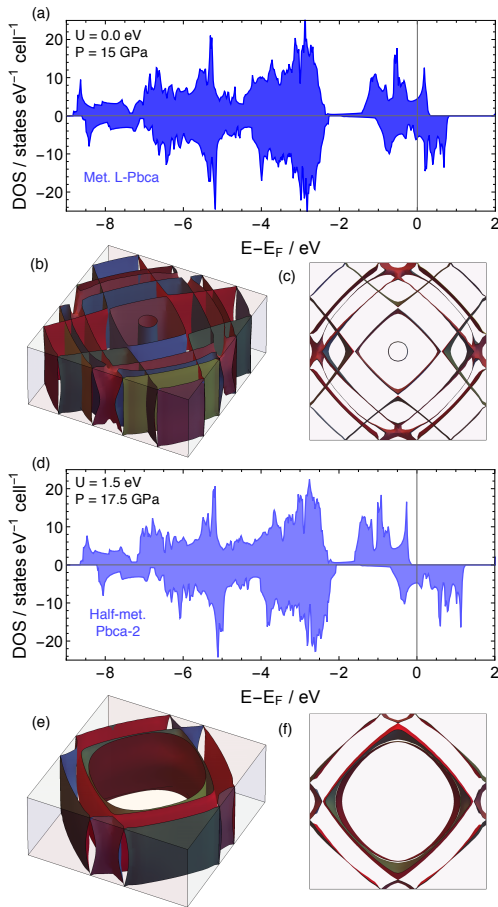


FIG. 3. (a) DOS of the FMe phase at  $P = 15$  GPa for  $U = 0.0$  eV. (b) The corresponding Fermi surface and (c) the Fermi surface viewed along  $k_z$ . (d)–(f) show the same for the HMe2 phase at  $P = 17.5$  GPa for  $U = 1.5$  eV.

necessarily in contradiction with the  $S$ - $Pbca$  results: one should not expect that a constant value of  $U$  is sufficient for all phases. The discontinuous change in crystal and electronic structure will result in a discontinuous change in the effective  $U$  required to model the metallic phase. Specifically,  $U$  should decrease after the phase transition, which puts the system much closer to the more physical FMe phase.

### C. Octahedral distortion under pressure

The pressure dependence of perovskite-like materials is usually adequately captured by rotations and tilts of rigid octahedra [35–37]. For instance, in Steffens *et al.*'s analysis of  $\text{Ca}_2\text{RuO}_4$  it was assumed that the octahedral basal plane Ru-O bonds remained equal and perpendicular [3]. However, polyhedral plasticity has been identified as a catalyst for unexpected structural behaviour in  $\text{SrRuO}_3$  and coupling to electronic transitions in rare earth nickelates  $\text{RENiO}_3$  [38–42]. We therefore investigate the geometry of the  $\text{RuO}_6$  octahedra in  $\text{Ca}_2\text{RuO}_4$

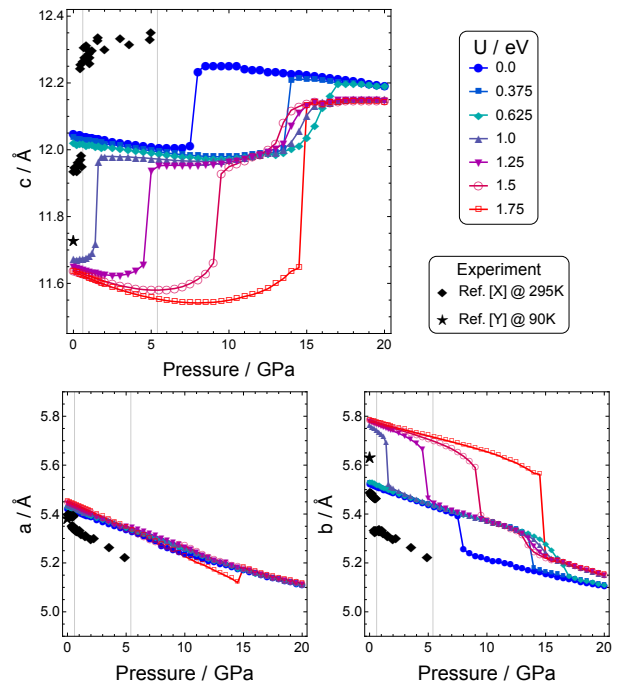


FIG. 4. Pressure dependence of the lattice parameters for a range of representative  $U$  values. Experimental data at two different temperatures is marked by filled black symbols, and vertical lines indicate the pressure-driven structural phase transitions identified in experiment at 295 K by Steffens *et al.* [3]. For clarity, only the experimental data in the  $Pbca$  phases are shown [3, 34].

in more detail here.

To capture the different high-pressure scenarios identified in the previous section, we select three exemplar values of  $U$ . These are  $U = 0.0$  eV ( $\text{HMe1} \rightarrow \text{FMe}$ ),  $U = 1.25$  eV (ins.  $S$ - $Pbca \rightarrow \text{HMe1} \rightarrow \text{HMe2}$ ) and  $U = 1.75$  eV (ins.  $S$ - $Pbca \rightarrow \text{HMe2}$ ), which covers all pressure-induced phase transitions seen in DFT+ $U$ . Figures 5b–g show the pressure dependencies of the octahedral Ru–O bond lengths and distortion angles. The labelling conventions for these parameters are given in figure 5a. The Ru–O(3) bond is the apical bond which points predominantly along  $c$ , while Ru–O(1) and Ru–O(2) are the basal bonds predominantly in the  $ab$  plane. The distortion angles are the tilt  $\Theta$ , the angle between the Ru–O(3) bond and the  $c$  axis, and rotation  $\Phi$ , which measures the angle between the Ru–O(2) basal bond and the  $[110]$  direction.

The octahedral structures are, again, very sensitive to temperature. The ambient pressure measurements by Porter [34] and Steffens [3] at 90 K and 295 K respectively are both included in figure 5b–g (open *vs* closed symbols). Both measure the  $S$ - $Pbca$  phase. At room temperature the apical bond is *longer* than the basal bonds (elongated octahedra), but at low temperatures it is *shorter* (compressed octahedra). The latter agrees well with our ground state calculations, where the insu-

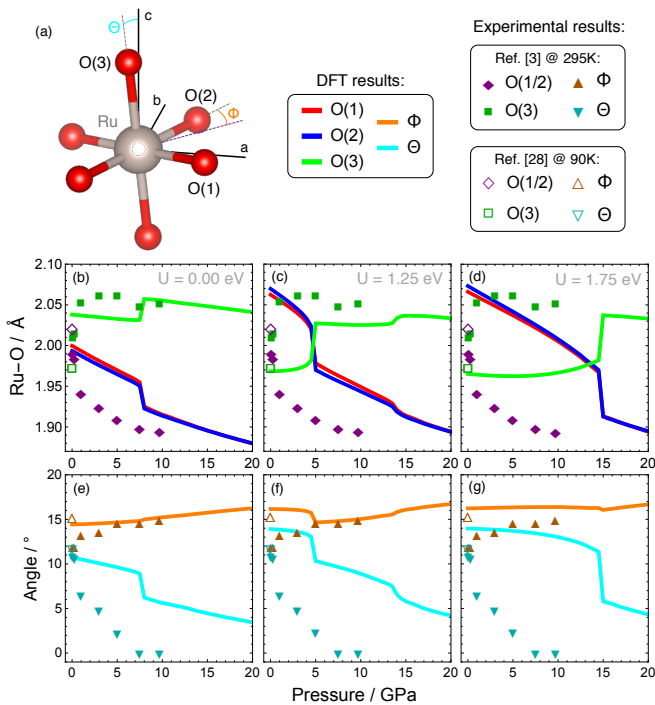


FIG. 5. (a) Labeling convention for O sites and distortion angles in  $\text{RuO}_6$ . Purple dashed line is the  $[110]$  direction.  $\Theta$  and  $\Phi$  are the tilt and rotation angles respectively. (b)–(g) Octahedral bond lengths and distortion angles as a function of pressure for  $U = 0.0, 1.25$  and  $1.75$  eV.

lating phase is associated with axially compressed octahedra and all metallic phases are axially elongated – in concert with the  $c$  axis behaviour (figure 4). HMe1 and HMe2 (seen for  $U = 1.25$  eV,  $P > 5$  GPa) have very similar octahedral structures, but the fully metallic phase ( $U = 0.0$  eV,  $P > 8$  GPa) shows the best agreement with experiment (albeit at a higher pressure).

The distortion angle  $\Theta$  decreases significantly with temperature, while  $\Phi$  is found to be quite insensitive to temperature [34]; note that the magnitude of  $\Phi$  reported in [34] at room temperature disagrees somewhat with previous measurements [3]. Our results for  $\Phi$  agree with the low temperature data at ambient pressure and with reported small increases under pressure in the metallic phases. Steffens’ room temperature measurements of  $\Theta$  show a sudden drop at the insulator-metal transition, followed by a steep decline towards  $0^\circ$ . Our results reproduce the drop at the transition, but show a much slower reduction of  $\Theta$  with pressure. This is likely to be a signal of the higher-symmetry  $Bbcm$  phase emerging in the room temperature experiment. We will discuss the emergence of this phase in more detail in section II E.

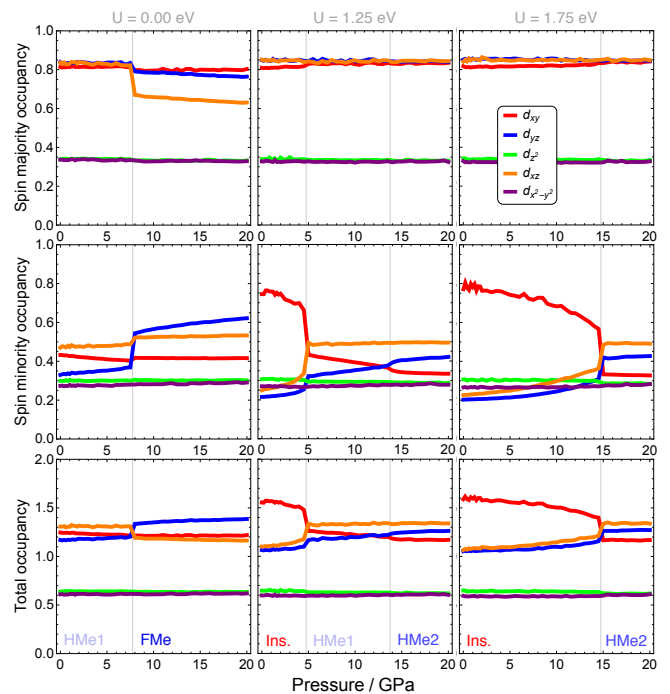


FIG. 6. Ru  $4d$  orbital occupancies for  $U = 0.0, 1.25$  and  $1.75$  eV as a function of pressure. *Top*: Majority spin channel (up spins). *Middle*: Minority spin channel (down spins). *Bottom*: Total orbital occupancies (up + down). Vertical lines mark phase transitions.

#### D. Orbital structure under pressure

We now probe the occupancies of the Ru  $4d$  orbitals to characterize the electronic behavior alongside the pressure induced structural changes. The Ru atom at the origin is chosen for our analysis (figure 5a), to which all other Ru sites are equivalent via appropriate symmetry operations [19]. For the basis set to be appropriate, the  $z$  axis for the orbital projection is chosen along the apical bond. The  $x$  axis is then chosen such that the Ru-O(1) bond is in the  $xz$ -plane, which then fully determines the  $y$  axis. In practice, the Ru-O bonds are always within  $5^\circ$  of these cartesian axes. Occupancies are computed by integrating over the valence space of the  $\ell m$  resolved DOS, from  $-10$  eV to the Fermi energy. The partial DOS in turn is obtained by projecting all electronic states onto spherical harmonics within a fixed radius around the Ru site. Absolute occupancies should therefore be treated with caution but relative changes and trends across pressure and phase transitions will be identifiable. Figure 6 shows the total orbital occupancies for the three exemplary  $U$  discussed above, in addition to the spin majority (up) and minority (down) channels.

The majority spin channel is remarkably robust across the insulating  $S-Pbca$  and both HMe phases, with archetypal splitting between  $e_g$  and  $t_{2g}$  orbitals. The residual occupancies of the  $e_g$  states (about 0.3 in both  $d_{z^2}$  and  $d_{x^2-y^2}$ ) reflect the numerical limitations of the

DOS projection scheme of a DFT band structure. The insulator–metal transition has no impact on the up-spin occupancies (see  $U = 1.25$  and  $1.75$  eV) but is clearly noticeable in the minority spin state occupancies. For all metallic phases the total occupancy of the  $t_{2g}$  states is approximately 1.25, consistent with DMFT results of  $4/3$  [16, 18]. In the insulating phase the only the  $d_{xy}$  orbital is doubly occupied while  $d_{xz}$  and  $d_{yz}$  are half occupied, also consistent with DMFT results. Electronic charge is localised in the basal plane of the octahedra, which correlates with the compressed octahedral shape. However, close to the insulator–metal transition, but still within the S-*Pbca* phase, charge density is redistributed into the  $d_{yz}$  and  $d_{xz}$  orbitals that are extended along the apical bond, correlating with reduction of the octahedral compression, and the anomalous  $c$  lattice expansion under pressure.

The occupancies change somewhat differently in the different half metallic phases. HMe1 retains some charge density in the  $d_{xy}$  orbital, which is steadily shifted into the  $d_{yz}$  orbital as pressure increases. HMe2 is qualitatively the same, but the  $d_{xy}$  occupancy is lower and eclipsed by the  $d_{yz}$  orbital occupancy from the onset of metallicity. The crossover from  $d_{xy}$  to  $d_{yz}$ , and resulting charge transfer from the basal plane to the apical direction, correlates with the weak  $c$  lattice expansion seen in the half metallic phases (see Figure 4).

Finally, in the FMe phase, the majority spin channel loses charge density, primarily from the  $d_{xz}$  orbital, to the  $d_{yz}$  orbital in the minority spin channel. The charge density remains distributed largely along the apical bond, but with more substantial double occupancy of the  $d_{yz}$  orbital, hence the reduction in overall magnetic moment  $\mu_B$ . This has little consequence for the total occupancy; the orbital polarisation remains small.

### E. L-*Pbca* $\rightarrow$ *Bbcm* transition

At atmospheric pressure  $\text{Ca}_2\text{RuO}_4$  undergoes a phase transition to a higher symmetry *Bbcm* structure at 650 K, which is characterised by a vanishing tilt angle (octahedra aligning along the  $c$  axis). This type of phase transition is typical of compounds with polyhedral structures, where the high symmetry phase is dynamically stabilised by thermal fluctuations in the tilt angle [43]. Steffens *et al.* showed that, at 295 K, this transition appears at 5.5 GPa [3], indicating that pressure also acts to stabilise this phase. Here, we probe the pressure dependence of the *Bbcm* phase up to much higher pressures to determine its static stability relative to the L-*Pbca* phase. We use  $U = 0.0$  eV since the pressures here are more extreme.

The L-*Pbca* and *Bbcm* structures are independently pressurised up to 45 GPa. One expects that the L-*Pbca* phase converges to the *Bbcm* structure as the octahedral tilt is suppressed by pressure. However, both structures remain distinct and L-*Pbca* remains the lower-enthalpy phase over the full pressure range tested, see

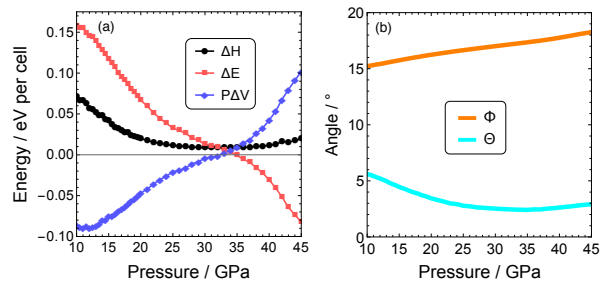


FIG. 7. (a) Enthalpy, energy, and pressure-volume differences between the *Bbcm* and FMe L-*Pbca* phases as a function of pressure.  $\Delta X = X_{Bbcm} - X_{Pbca}$ . (b) Octahedral distortion angles of the FMe L-*Pbca* phase under high pressure. See figure 5a for definitions of  $\Theta$  (tilt) and  $\Phi$  (rotation).

figure 7a. The enthalpy difference decreases to a minimum of  $\Delta H = 2.1$  meV/Ru at 33 GPa, before increasing again with further compression. The tilt angle follows the same trend, so that *Bbcm* symmetry (where  $\Phi = 0$ ) is never reached, see figure 7b. This behaviour is driven by deformation of the octahedra in the L-*Pbca* phase (see SM for details) and suggests that this second-order phase transition line never meets the  $T = 0$  axis. However, perovskite-type compounds are known to undergo a variety of structural phase transitions under extreme compression [44, 45], which might be the case for  $\text{Ca}_2\text{RuO}_4$  as well but was not considered in this work.

## III. CONCLUSIONS

In summary, we have studied the high pressure evolution of the structural and electronic properties of  $\text{Ca}_2\text{RuO}_4$  using DFT and DFT+ $U$  calculations. Despite being conceptually very simple, the full structural optimisations (and therefore truly self-consistent electronic structures) are able to describe many of the interesting features seen in experiments, provided the on-site correction  $U$  is chosen appropriately. Namely, this includes the association of a ‘short’ (S) crystal structure with an insulating band structure, and a ‘long’ (L) crystal structure with a metallic band structure. Pressure-driven insulator-metal transitions also appear naturally, which coincides with a transition from S to L crystal structures. Generally, lattice parameters agree well with low temperature experimental measurements, but a full theoretical picture is complicated by the appearance of three metallic phases as a function of pressure: two half-metallic (HMe), local-moment phases and a fully metallic (FMe) itinerant magnet which best matches the experimental L-*Pbca* phase. The Fermi surface of the FMe phase is also, geometrically, very well nested, suggesting that density-wave order may play a role in the phase diagram of  $\text{Ca}_2\text{RuO}_4$ .

The Mott transition is a simultaneous restructuring of both crystal and orbital structure. Pressure squeezes

electrons out of the basal  $d_{xy}$  orbital and into the  $d_{yz}$  and  $d_{xz}$  orbitals. The crystal structure responds by extending the apical bond of the octahedra and in turn, the  $c$  axis. This is generally in agreement with the previous DMFT study of the temperature driven transition [18]. The  $Pbca \rightarrow Bbcm$  transition is also probed to much higher pressures, which reveals that  $Bbcm$  never becomes the enthalpically stable phase at sufficiently low temperature. A high pressure, post-perovskite-type phase is likely to take its place. Hence, the low-temperature, high-pressure region of the  $\text{Ca}_2\text{RuO}_4$  phase diagram remains a promising refuge for exotic structural, electronic, and magnetic phases.

## ACKNOWLEDGEMENTS

HDJK acknowledges studentship funding from EPSRC under grant No. EP/L015110/1. Computing re-

sources provided in parts by the UK national high performance computing service, ARCHER, and the UK Materials and Molecular Modelling Hub, which is partially funded by EPSRC (EP/P020194), and for which access was obtained via the UKCP consortium funded by EPSRC grant No. EP/P022561/1, are gratefully acknowledged. SRJ is grateful to NSERC for funding (RGPIN-2019-06446), and to Andrew Huxley and the University of Edinburgh for hosting a sabbatical visit.

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