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# On the friction drag reduction mechanism of streamwise wall fluctuations

Tamás István Józsa<sup>a,\*</sup>, Elias Balaras<sup>b</sup>, Maria Kashtalyan<sup>c</sup>, Alistair George Liam Borthwick<sup>d</sup>, Ignazio Maria Viola<sup>e</sup>

<sup>a</sup>Department of Engineering Science, Institute of Biomedical Engineering, University of Oxford, Oxford OX1 3PJ, UK <sup>b</sup>Department of Mechanical and Aerospace Engineering, The George Washington University, Washington, DC 20052, USA <sup>c</sup>School of Engineering, Centre for Micro- and Nanomechanics (CEMINACS), University of Aberdeen, Aberdeen AB24 3UE, UK <sup>d</sup>School of Engineering, Institute for Infrastructure and Environment, University of Edinburgh, Edinburgh EH9 3FB, UK <sup>e</sup>School of Engineering, Institute for Energy Systems, University of Edinburgh, Edinburgh EH9 3FB, UK

#### Abstract

Understanding how to decrease the friction drag exerted by a fluid on a solid surface is becoming increasingly important to address key societal challenges, such as decreasing the carbon footprint of transport. Well-established techniques are not yet available for friction drag reduction. Direct numerical simulation results obtained by Józsa *et al.* (2019) previously indicated that a passive compliant wall can decrease friction drag by sustaining the drag reduction mechanism of an active control strategy. The proposed compliant wall is driven by wall shear stress fluctuations and responds with streamwise wall velocity fluctuations. The present study aims to clarify the underlying physical mechanism enabling the drag reduction of these active and passive control techniques. Analysis of turbulence statistics and flow fields reveals that both compliant wall and active control amplify streamwise velocity streaks in the viscous sublayer. By doing so, these control methods counteract dominant spanwise vorticity fluctuations in the near-wall region. The lowered vorticity fluctuations lead to an overall weakening of vortical structures which then mitigates momentum transfer and

<sup>\*</sup>Corresponding author

Email address: tamas.jozsa@eng.ox.ac.uk (Tamás István Józsa)

results in lower friction drag. These results might underpin the further development and practical implementation of these control strategies. *Keywords:* Turbulent channel flow, Active flow control, Passive flow control, Drag reduction, Compliant wall, Compliant surface 2010 MSC: 76D55

#### 1 1. Introduction

The question as to whether compliant walls can sustain drag reduction in turbulent flows has challenged fluid dynamicists in the decades [1] after Kramer's 3 somewhat controversial experiments [2-4]. The early research focus was on quantification of the impact of deformable surfaces on transitional flows. Studies based on linear stability analysis of flat plate boundary layers demonstrated that a pressure-driven surface can delay laminar-turbulent transition by damping Tollmien-Schlichting waves [5, 6]. It was reported that a wall made of 8 compliant panels could postpone natural transition indefinitely [7], and such transition delay was confirmed for in-plane channel flows [8]. Sixty years af-10 ter Kramer's experiments, this phenomenon is now widely accepted owing to 11 carefully conducted experiments [9–11] and numerical investigations [12, 13]. 12

Later research studies have aimed to characterise the interaction of compliant 13 surfaces and fully-developed turbulent flows. Theoretical [14] and experimental 14 [15–17] studies suggested that travelling wave-like surface deformations could 15 suppress turbulence production in turbulent boundary layers. Conversely, stud-16 ies based on Direct Numerical Simulations (DNS) [18-22] and resolvent analysis 17 [23, 24] reported minimal changes or increased friction drag in the presence of 18 compliant surfaces. The results implied that pressure-driven wall-normal de-19 formations cannot utilise the drag reduction mechanisms of opposition control 20 [25–28] and streamwise-travelling waves [29] at low Reynolds numbers. 21

To date, experimental work has mostly targeted single-layer isotropic viscoelastic materials that exhibit primarily wall-normal deformations [9–11, 15– 17, 30–32]. By comparison, the majority of computational studies solely ex<sup>25</sup> amined pressure-driven compliant walls represented by dynamic systems with <sup>26</sup> wall-normal displacement response [18, 20, 33]. Only a few studies have con-<sup>27</sup> sidered the effects of passive in-plane wall motions [19, 34–36]. Furthermore, <sup>28</sup> computational studies on flow control have been restricted to low Reynolds <sup>29</sup> numbers with few exceptions, such as [37].

Recently, it has been demonstrated by means of DNS that even small-scale spanwise deformations can act like a wall with spanwise slip [38] and result in substantial drag penalty [34]. The latter study also reported that a conceptual compliant wall can imitate streamwise active flow control originally proposed by [25]. Importantly, it was found that drag reduction is sustained by streamwise wall fluctuations driven by streamwise wall shear stress fluctuations.

The present study aims to examine the drag reduction mechanism of active 36 and passive flow control techniques with streamwise wall velocity responses at 37 low and moderate Reynolds numbers for the first time. To this end, a database 38 of controlled and uncontrolled canonical turbulent channel flows at low and 39 moderate friction Reynolds numbers ( $Re_{\tau} \approx 180$  and 1000) is analysed and 40 extended with flow visualisations, Reynolds stress transport statistics and La-41 grangian wall motion tracking [39]. The paper is structured as follows. Section 42 2 outlines the computational methodology. Section 3 presents the main results 43 for active and passive control methods in terms of integral variables, the fluc-44 tuating flow field, turbulence statistics, and Lagrangian wall motions. Section 45 4 lists the main findings. It should be noted that preliminary results were pre-46 sented at the Eleventh International Symposium on Turbulence and Shear Flow 47 Phenomena (TSFP11) [40]. 48

#### $_{49}$ 2. Methods

#### <sup>50</sup> 2.1. Simulation Settings

Herein, fully-developed turbulent flow in an idealised plane channel is modelled by the incompressible continuity and Navier-Stokes momentum equations (see e.g. [41]), which are discretised on a Cartesian staggered grid and solved

Table 1: Simulation settings.  $L_1$ ,  $L_2$ , and  $L_3$  are the streamwise, wall-normal and spanwise lengths of the computational domain, and  $n_1$ ,  $n_2$ , and  $n_3$  are the corresponding grid resolutions.  $\Delta t$  denotes the time step, whereas  $t_a$  is the averaging time.

Case	low Re	moderate Re		
Reynolds number, Re	2857	20000		
friction Reynolds number, $\operatorname{Re}_{\tau}$	$180.7 \ (\approx 180)$	990.2 ( $\approx 1000$ )		
domain size, $L_1 \times L_2 \times L_3$	$4\pi \times 2 \times 4\pi/3$	$2\pi \times 2 \times \pi$		
number of nodes, $n_1 \times n_2 \times n_3$	$290\times251\times290$	$770 \times 1001 \times 770$		
temporal resolution, $\Delta t u_{\tau}^2 / \nu$	$\approx 0.115$	$\approx 0.196$		
averaging time, $t_a u_\tau^2 / \nu$	$\approx 23000$	$\approx 19600$		

numerically by an in-house fractional step solver [42]. Spatial derivatives are 54 represented by second-order central-differences. The pressure-Poisson equation 55 is solved directly [43] using fast Fourier transforms in the periodic (stream-56 wise and spanwise) directions, and by a standard tridiagonal matrix algorithm 57 [44] in the wall-normal direction. For time integration, an explicit third-order 58 low-storage Runge-Kutta method is utilised for the streamwise and spanwise 59 momentum equations, whereas the implicit Crank-Nicolson scheme is used for 60 the wall-normal momentum equation. A detailed description of the in-house 61 incompressible Navier-Stokes solver is given by [45]. 62

We denote the streamwise, wall-normal, and spanwise Cartesian coordinates 63 in the channel as  $x_1, x_2, x_3$ , and the corresponding velocity and vorticity compo-64 nents as  $u_1, u_2, u_3$ , and  $\omega_1, \omega_2, \omega_3$ . Non-dimensional quantities are based on the 65 channel half-height  $\delta$  and bulk velocity  $u_b$ . The (bulk velocity) Reynolds num-66 ber is defined as  $Re = u_b \delta / \nu$ , where  $\nu$  denotes kinematic viscosity. Quantities 67 with + superscripts are non-dimensionalised with respect to the friction velocity 68  $u_{\tau} = \sqrt{\langle \tau_1 \rangle / \rho}$  and the viscous length scale  $\delta_{\nu} = \nu / u_{\tau}$  of the baseline (uncon-69 trolled) simulations. The friction Reynolds number is defined as  $\text{Re}_{\tau} = u_{\tau} \delta / \nu$ . 70 Here,  $\rho$  is the fluid density and  $\tau_1$  is the streamwise wall shear stress component. 71 The angled brackets  $\langle \rangle$  indicate an averaged variable and the prime symbol ' 72 denotes a fluctuating quantity. Table 1 lists the basic simulation settings. For 73 further details of the model and its verification and validation tests, the reader 74 is referred to [34, 39]. 75

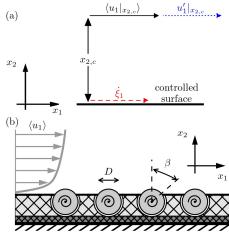


Figure 1: Schematic drawing of the implemented flow control techniques introducing streamwise wall fluctuations: (a) active control based on Eq. (1); (b) a compliant wall model including mounted rotating discs with spanwise aligned axes. The compliant wall is modelled using Eq. (2). These figures are modified with permission from Józsa *et al.* [34].

#### 76 2.2. Boundary Conditions

The streamwise  $(x_1)$  and spanwise  $(x_3)$  directions are by definition periodic. 77 In the uncontrolled (baseline) simulations, the channel walls (bounding  $x_1$ - $x_3$ 78 planes) are hydrodynamically smooth no-slip walls. The active flow control and 79 the compliant wall impose two different Dirichlet boundary conditions for the 80 streamwise wall velocity component at both channel walls. The other two veloc-81 ity components and the wall-normal pressure gradient at the channel walls are 82 set to zero. Figure 1(a) shows the active flow control introduced in [25], where 83 the fluctuating streamwise fluid velocity is measured at  $x_{2,c}$  distance from the 84 wall  $(u'_1|_{x_{2,c}}, \text{ sensing})$ , and the wall velocity directly below the measurement lo-85 cation is equal to the measured streamwise velocity fluctuation both in direction 86 and magnitude ( $\xi_1 = u_1|_{\text{wall}}$ , actuation). Based on figure 1(a), the active flow 87 control is implemented as 88

89 
$$\xi_1 = u_1'|_{x_{2,c}} = u_1|_{x_{2,c}} - \langle u_1|_{x_{2,c}} \rangle.$$
 (1)

The compliant wall case exploits a drag reduction mechanism similar to that of active flow control, with streamwise wall shear stress component  $(\tau_1)$  as input

and streamwise wall velocity components  $(u_{1,wall})$  as output [34, 39, 40]. Figure 92 1(b) shows a conceptual model of such a compliant surface utilising mounted 93 discs, inspired by a former active control study [46]. These discs have finite 94 spanwise extent that is comparable to the viscous length scale  $(\delta_{\nu})$ . Therefore, 95 the wall velocity response of the compliant surface exhibits streamwise and 96 spanwise variations which are required for a successful control, as demonstrated 97 in Sections 3.2 and 3.4. With sufficiently small disc diameter (D) and  $\beta$  angle 98 (e.g.  $D \sim \delta_{\nu}$  and  $\beta < \pi/6$ ), a simplified dimensionless governing equation of 99 the compliant wall can be written as 100

101

$$\underbrace{\frac{4C_m}{D^2 A_s}}_{\Lambda_m} \ddot{\xi}_1 + \underbrace{\frac{4C_d}{D^2 A_s}}_{\Lambda_d} \dot{\xi}_1 + \underbrace{\frac{4C_s}{D^2 A_s}}_{\Lambda_s} \xi_1 = \frac{1}{Re} \frac{\partial u_1}{\partial x_2} \Big|_{\text{wall}},\tag{2}$$

assuming that the motion of the discs is driven by the local wall shear stress. 102 Here,  $\Lambda_m$ ,  $\Lambda_d$  and  $\Lambda_s$  are the inertia, damping, and spring stiffness parameters of 103 the compliant surfaces, respectively. These parameters are proportional to the 104 moment of inertia  $(C_m)$ , viscous damping  $(C_d)$ , and torsion spring coefficient 105  $(C_s)$  of a single mounted disc, and inversely proportional to its wetted surface 106 area  $(A_s)$ . In Eq. (2),  $\xi_1$  is the tangential displacement of a disc. The resulting 107 tangential velocity is assumed to be equivalent to the introduced streamwise 108 wall velocity  $(\dot{\xi}_1 = u_{1,\text{wall}})$ . If the  $\beta$  angle shown in Fiure 1(b) is less than 109  $30^{\circ}$ , then this approximation leads to less than 5% error in the streamwise wall 110 velocity compared to the exact formulation which accounts for the Cartesian 111 velocity distribution over the disc surface [39]. Considering that the surface 112 integral of the wall-normal velocities over the wetted surface is zero, the disc 113 diameter is restricted so that the impact of the introduced wall-normal velocity 114 is negligible. 115

During compliant wall simulations, Eq. (2) is imposed at every wall cell. To advance Eq. (2) in time, a fourth order Runge-Kutta scheme is employed, and a weak coupling scheme is implemented to treat the resulting fluid-structure interaction problem. The governing equation of the compliant surface ensures that the average streamwise wall velocity remains zero ( $\langle u_1 \rangle = 0$ ) because the average displacement of the discs balances the average streamwise wall shear stress.

#### 123 2.3. Measuring Control Effects

To keep the volumetric flow rate constant, the driving pressure gradient  $(\partial P/\partial x_1)$  is adjusted at every time step. With this in mind, the Drag Reduction (DR) in the case of controlled simulations is defined as

DR = 
$$1 - \frac{\langle \partial P / \partial x_1 \rangle_{\text{controlled}}}{\langle \partial P / \partial x_1 \rangle_{\text{baseline}}}.$$
 (3)

In addition, the following global (integral) variables are introduced to quantify
the effects of the control methods on the entire flow field [47]. Using the Einstein
summation convention, the global turbulent kinetic energy is defined as

$$k_g = \frac{1}{\delta} \int_0^\delta k \mathrm{d}x_2 = \frac{1}{\delta} \int_0^\delta \frac{\langle u_i' u_i' \rangle}{2} \mathrm{d}x_2. \tag{4}$$

Similarly, the global turbulent enstrophy is computed from the fluctuating vor-ticity components as

$$\mathcal{E}_g = \frac{1}{\delta} \int_0^\delta \mathcal{E} \mathrm{d}x_2 = \frac{1}{\delta} \int_0^\delta \langle \omega_i' \omega_i' \rangle \, \mathrm{d}x_2.$$
 (5)

Furthermore, the absolute change  $(\Delta)$  and the relative change  $(\Delta_r)$  of a general quantity (q) are defined as

$$\Delta q = q_{\text{controlled}} - q_{\text{baseline}},\tag{6}$$

138 and

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$$\Delta_r q = \frac{q_{\text{controlled}} - q_{\text{baseline}}}{q_{\text{baseline}}}.$$
(7)

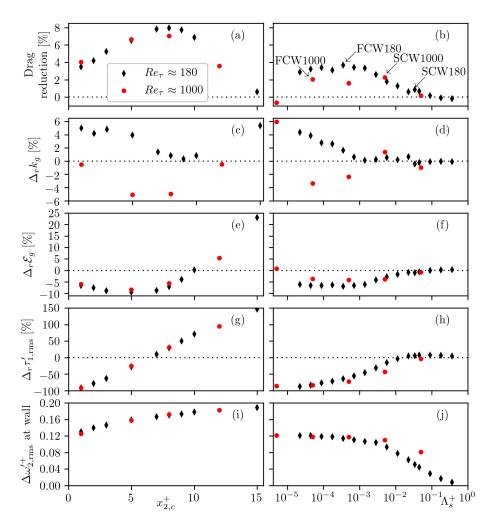


Figure 2: Effects of the active and passive control techniques on drag reduction (a)-(b), relative change in global turbulent kinetic energy (c)-(d), relative change in global turbulent enstrophy (e)-(f), relative change in rms streamwise wall shear stress fluctuations (g)-(h), and absolute change in rms wall-normal vorticity fluctuations at the wall (i)-(j), as functions of control distance (left column) and spring parameter (right column), respectively. The dotted lines indicate the zero level.

#### 140 3. Results and Discussion

#### 141 3.1. Integral variables

Figure 2 shows the effect of different control cases on certain integral vari-142 ables listed in Section 2.3. From Figures 2(a) and (g), it can be seen that the 143 Active Flow Control (AFC) with  $x_{2,c}^+ = 1$  leads to ca. 4% drag reduction accom-144 panied with a more than 90% drop in the root-mean-square (rms) streamwise 145 wall shear stress fluctuations  $\tau'_{1,\rm rms}$  at  $Re_{\tau} \approx 180$  and 1000. Maximum drag 146 reductions of 8% and 7% at  $Re_{ au} \approx$  180 and 1000 respectively are attained 147 for active control with  $x_{2,c}^+ = 8$ . Active control also performs well when the 148 global turbulent enstrophy is decreased, as indicated in Figure 2(e). However, 149 it is somewhat counter-intuitive that (i) maximum drag reduction occurs when 150 there is a 30% increase in  $\tau'_{1,\text{rms}}$ ; and (ii) drag reduction is accompanied by an 151 increase in global turbulent kinetic energy at  $Re_{\tau} \approx 180$ . This behaviour can 152 be observed in Figures 2(a), (c), and (g). From Figure 2(g), it can be concluded 153 that active control can have fluctuating shear-cancelling and shear-increasing 154 modes corresponding to decreased  $(\Delta_r \tau'_{1,\text{rms}} < 0)$  and increased  $(\Delta_r \tau'_{1,\text{rms}} > 0)$ 155 streamwise wall shear stress fluctuations, respectively. Both modes are tied to 156 an increase in wall-normal vorticity fluctuations as shown in Figure 2(i). Sec-157 tions 3.2 and 3.3 aim to explain these observations based on analyses of the flow 158 fields and turbulence statistics, respectively. 159

The three-dimensional parameter space of the compliant wall is mapped 160 using a semi-analytical method, following [34, 35]. Using the resulting frame-161 work, we optimise parameters for maximal  $\tau'_{1,\rm rms}$ , noting that active control 162 provides maximum drag reduction when in a shear-increasing mode [39]. DNS 163 at  $Re_{\tau} \approx 180$  reveals that the resulting parameter set corresponds to a Stiff 164 Compliant Wall (SCW180), increases  $\tau'_{1,\text{rms}}$  by ca. 6%, and has a marginal 165 impact on friction drag (see Table 2). Taking SCW180 as the starting point, 166 a parameter sweep is performed by changing solely the spring parameter for 167 simplicity, as shown in Figure 2. The results presented in Figure 2(h) confirm 168 that compliant walls sustaining streamwise velocity fluctuations have shear-169

cancelling  $(\Delta_r \tau'_{1,\text{rms}} < 0)$  and shear-increasing  $(\Delta_r \tau'_{1,\text{rms}} > 0)$  modes, similar 170 to active control. Figure 2(b) shows a Flexible Compliant Wall (FCW180) cor-171 responding to peak drag reduction measured in the present study (see Table 172 2). FCW180 results in 3.68% drag reduction at  $Re_{\tau} \approx 180$  which is more than 173 twice the maximum value reported by other computational studies on compli-174 ant surfaces (1.7%) [20]. Considering other passive control techniques, the peak 175 drag reduction is lower than the value measured with riblets ( $\approx 8\%$ ) [48–50] 176 but higher than the value measured with wavy walls (0.6%) [51]. FCW180 has 177 been tested for modified domain sizes, spatial and temporal resolutions, and 178 sample sizes, and a thorough error quantification found a  $\pm 1\%$  uncertainty in 179 drag reduction [34]. The domain size has been identified as the primary error 180 source. Therefore  $\pm 1\%$  drag reduction uncertainty is representative of the low 181 Reynolds number cases but simulations at  $Re_{\tau} \approx 1000$  suffer from a somewhat 182 larger uncertainty. Detailed uncertainty quantification for the  $Re_{\tau} \approx 1000$  case 183 is an outstanding challenge because simulations at moderate Reynolds numbers, 184 especially with increased domain size, are extremely resource intensive 185

Table 2: Parameters of selected compliant walls (SCW180, FCW180, etc.) and corresponding drag reduction (DR).

ID	$Re_{\tau} \approx$	$\Lambda_m$	$\Lambda_d$	$\Lambda_s$	DR [%]
SCW180	180	$1.40 \cdot 10^{-3}$	0	$3.38 \cdot 10^{-2}$	0.86
FCW180	180	$1.40\cdot10^{-3}$	0	$3.50\cdot10^{-4}$	$3.68\pm1$
SCW1000	1000	$4.00\cdot 10^{-4}$	0	$5.00\cdot10^{-3}$	2.29
FCW1000	1000	$4.00 \cdot 10^{-4}$	0	$5.00 \cdot 10^{-5}$	2.04

Simulations are carried out at  $Re_{\tau} \approx 1000$  to gain insight into the effect 186 of increasing Reynolds number (Table 2 and Figure 2). The inertia parame-187 ter,  $\Lambda_m$  is decreased for these simulations to ensure that compliant surfaces 188 remain responsive. The investigated parameters lead to significant performance 189 degradation with increasing Reynolds number but both FCW180 and FCW1000 190 sustain a considerable decrease in  $\tau'_{1,\rm rms}$  accompanied with drag reduction. Ac-191 cording to Figure 2(b), the drag reduction curve breaks down with decreasing 192 spring parameter. Hence,  $\tau'_{1,\rm rms} = 0$  is not optimal for passive control. We 193

find that stiffer compliant walls can perform better at  $Re_{\tau} \approx 1000$  compared to 194  $Re_{\tau} \approx 180$  (see SCW180 and SCW1000 in Table 2 and Figure 2(b)). Although, 195 the impacts of the other parameters ( $\Lambda_m$  and  $\Lambda_d$ ) at  $Re_{\tau} \approx 180$  have been 196 reported in our previous studies [34, 39], the parameter space at  $Re_{\tau} \approx 1000$ 197 remains mostly unexplored because of the associated high computational cost. 198 Pairwise comparisons between Figures 2 (g)-(h) and (i)-(j) suggest that as 199  $\Lambda_s \to 0$ , the effect of passive control on wall quantities approaches that of active 200 control with  $x_{2,c}^+ = 1$ . The source of this similarity is determined through 201 manipulation of the control equations. Substituting a Taylor series expansion 202 of  $u'_1$  near the wall into Equation (1) leads to 203

$$\frac{\partial u_1'}{\partial x_2}\Big|_{\text{wall}} x_{2,c} + \frac{1}{2} \frac{\partial^2 u_1'}{\partial x_2^2}\Big|_{\text{wall}} x_{2,c}^2 + \mathcal{O}(x_{2,c}^3) = 0.$$
(8)

This equation suggests that if the control distance is small  $(x_{2,c}^+ = 1)$  then the active control cancels the spanwise vorticity fluctuations at the wall:

$$\omega_{3,\text{wall}}' = -\frac{\partial u_1'}{\partial x_2}\Big|_{\text{wall}} = -\frac{\tau_1'}{\rho\nu} = 0.$$
(9)

With respect to passive control, Equation (2) tends to Equation (9) as the control parameters tend to zero ( $\Lambda_m \rightarrow 0$ ,  $\Lambda_d \rightarrow 0$ , and  $\Lambda_s \rightarrow 0$ , leading to  $\tau'_1 \rightarrow 0$ ). This prediction regarding the asymptotic behaviour of the passive control overlaps with the result of parameter space mapping reported in [34, 39].

#### 212 3.2. Fluctuating Flow Field Analysis

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Both the active and passive control methods interact primarily with the so 213 called near-wall cycle that comprises quasi-streamwise vortices and streamwise 214 velocity streaks driven by the mean shear [52]. Figure 3 illustrates the three-215 dimensional arrangement of typical instantaneous vortical features, including a 216 hairpin vortex formation [53] and the connected counter-rotating vortices [52, 217 54]. The streamwise control techniques do not noticeably modify these vortical 218 features [39]. Visualisation of the vorticity field offers an alternative method by 219 which to detect qualitative changes in the flow field, and has been proven to be 220

an efficient means to understand flow control [55]. Here, the vorticity field is explored by seeding vorticity lines of the instantaneous fluctuating flow field as visualised in Figure 3. In Figure 3, the high and low momentum regions (streaks) corresponding to the vortical features are represented by the fluctuating vorticity lines. Within the streaks, where streamwise fluctuations and the corresponding shear dominate, fluctuating vorticity lines ( $\omega'$  lines) form a spiral shape with quasi-streamwise aligned axis.

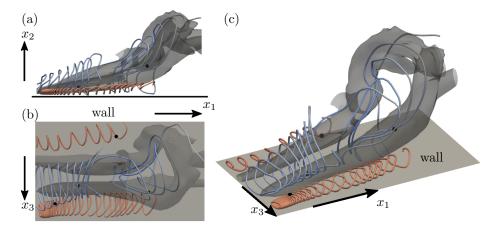


Figure 3: Instantaneous flow features near the wall at  $\text{Re}_{\tau} \approx 1000$ : (a) side view; (b) top view; (c) bird's eye view. The total wall-normal extent of the Q = 35 isosurface [56] is about  $100\delta_{\nu}$ . The streamwise and spanwise extent of the presented wall section is  $190\delta_{\nu}$ , and  $110\delta_{\nu}$ , respectively. The black spheres indicate fluctuating vorticity line seeding points. A hairpin vortex is formed around the blue fluctuating vorticity lines enclosed by a low momentum region. The remaining two red vorticity lines are enclosed by high momentum regions.

We now summarise the key kinematic properties of fluctuating vorticity lines 228 with increasing wall distance based on Figure 3 and baseline velocity and vor-229 ticity statistics given in Appendix A. First,  $\omega'_3 \gg \omega'_1 > \omega'_2$ , and hence  $\omega'$  lines 230 lie parallel to the  $x_1$ - $x_3$  plane. Near the wall,  $\omega'_3 \approx -\partial u'_1/\partial x_2 \propto \tau'_1$  represents 231 flow shear between the streaks and the wall. Fluctuating vorticity lines are di-232 rected towards the wall-normal direction between the low- and high-momentum 233 streaks, highlighting that  $\omega'_2 \approx -\partial u'_1/\partial x_3$ . In the buffer layer, streak instabil-234 ities emerge [52] as the viscous force weakens. The streamwise vorticity  $(\omega'_1)$ 235 exhibits a statistical local maximum at about  $x_2^+ = 20$ , corresponding to the 236 mean wall distance of the centre-line of quasi-streamwise vortices. If  $x_2^+ \ll 20$ , 237

then  $\omega_1' \approx \partial u_3' / \partial x_2 \propto \tau_3'$  gives a measure of shear between the wall and quasi-238 streamwise vortices. For  $x_2^+ > 50$ , vorticity fluctuations, unlike velocity fluctu-239 ations, are approximately isotropic [54], i.e.  $\langle \omega'_1 \omega'_1 \rangle \approx \langle \omega'_2 \omega'_2 \rangle \approx \langle \omega'_3 \omega'_3 \rangle$ . Above 240  $x_2^+\approx 100,$  hairpin vortices can be detected by the Q-criterion or vorticity line 241 bundles but vorticity lines are mostly disorganised [57, 58]. At the Reynolds 242 numbers investigated in this study, fluctuating vorticity lines remain rooted in 243 the viscous sublayer suggesting that the entire flow field is attached to the wall 244 and can be modified by wall motions. 245

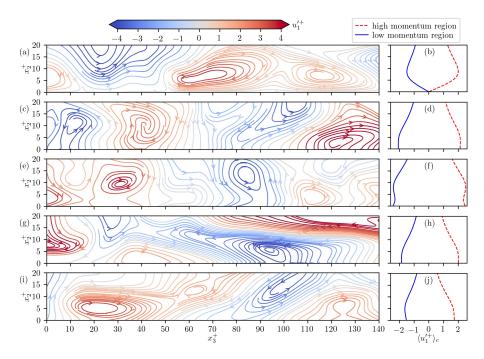


Figure 4: Effects of active and passive control techniques on instantaneous near-wall  $\omega'$  lines (left column) and  $\langle u'_1 \rangle_c$  profiles (right column) at  $\operatorname{Re}_{\tau} \approx 1000$ . The  $\omega'$  lines are visualised along a cross-section and are coloured by  $u'_1$ . Baseline case (a)-(b), active control with  $x^+_{2,c} = 1$  (c)-(d), active control with  $x^+_{2,c} = 8$  (e)-(f), FCW1000 (g)-(h), SCW1000 (i)-(j). Similar trends can be observed at  $\operatorname{Re}_{\tau} \approx 180$ .

Next, these vorticity features are investigated in the controlled channels, as depicted in the left column of Figure 4. In addition, conditionally averaged streamwise velocity profiles  $(\langle u'_1 \rangle_c)$  of the low and high momentum regions are presented in the right column of Figure 4. These regions are distinguished ac-

cording to the sign of the streamwise wall shear stress fluctuations and the sign 250 of the wall velocity fluctuations in the baseline and controlled cases, respectively. 251 The left column of Figure 4 suggests that the walls become part of the stream-252 wise velocity streaks as a result of the control. The  $\omega'$  lines highlight a twofold 253 impact on the near-wall vorticity fluctuations: (i) spanwise vorticity fluctua-254 tions are suppressed; and (ii) wall-normal vorticity fluctuations are introduced. 255 The flattened velocity profiles in the right column of Figure 4 confirm span-256 wise vorticity cancellation in the case of actively and passively controlled walls. 257 The streaky wall motions promoted by the control methods induce wall-normal 258 vorticity at the wall, as shown in Figures 2(i)-(j). The increased wall-normal 259 vorticity component  $\omega_2$  relates to enhanced shear-layers between low- and high-260 momentum streaks (see Figure 4(c), (e), (g), and (i)). 261

In shear-increasing mode, active control amplifies  $\omega'_3$  very close to the wall because of reversed shear, as depicted in Figure 4(f). This behaviour can be deduced from the second order approximation of the active control equation:

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$$\left. \frac{\partial u_1'}{\partial x_2} \right|_{\text{wall}} > 0 \text{ if } \left. \frac{\partial^2 u_1'}{\partial x_2^2} \right|_{\text{wall}} < 0, \tag{10}$$

and vice versa. Therefore, active control naturally creates a velocity profile with reversed shear as  $x_{2,c}$  increases. Active control attains peak performance by reversing fluctuating shear at the wall, and thus cancelling the dominant spanwise vorticity fluctuations. Sustaining such states requires energy input and hence it is not possible with a passive compliant surface [34].

It appears that a decrease in net vorticity fluctuations at the wall damps 271 vorticity fluctuations throughout the boundary layer, and mitigates momentum 272 transfer which in turn contributes to turbulent friction drag. Wall motions 273 induced by the control techniques lower spanwise vorticity fluctuations by de-274 creasing the shear between wall and streaks; this process inevitably increases 275 shear between the streaks. Amplified shear between the streaks manifests itself 276 as increased wall-normal vorticity in the near-wall region (shown in Figures 2(i) 277 and (j)), which is undesirable according to the above hypothesis. Consequently, 278

streamwise control has simultaneously positive and negative effects which limit
the control performance and cause the corresponding drag reduction curve to
break down.

In summary, streamwise wall motions dictated by the control methods can re-282 duce spanwise vorticity fluctuations (i.e. shear between the streaks and wall) but 283 increasingly build up undesirable wall-normal vorticity fluctuations (i.e shear be-284 tween the streaks) by doing so. For this reason, streamwise wall fluctuations can 285 weaken turbulence when  $\omega'_3$  cancellation dominates over  $\omega'_2$  amplification but 286 such wall motions cannot relaminarise the flow. In this sense, this drag reduction 287 mechanism is unique. By comparison, wall-normal and spanwise opposition con-288 trol [25–28] and spanwise wall oscillations [37, 59, 60] increase near-wall vorticity 289 fluctuations to counteract quasi-streamwise vortices and weaken the near-wall 290 cycle (which is known to be a major contributor to turbulence production). 291

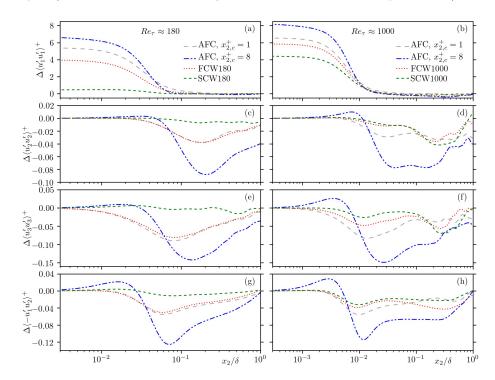


Figure 5: Change in Reynolds stresses with wall distance for different control techniques at  $\text{Re}_{\tau} \approx 180$  (left column) and at  $\text{Re}_{\tau} \approx 1000$  (right column). Streamwise (a)-(b), wall-normal (c)-(d), spanwise (e)-(f) components, and Reynolds shear stress (g)-(h).

#### 292 3.3. Turbulence Statistics

To investigate the drag reduction mechanism, we examine how the control 293 methods modify turbulence statistics in comparison to baseline values available 294 in Appendix A. The control techniques cause qualitative changes only in the 295 most energetic streamwise velocity fluctuations characterised by  $\langle u'_1 u'_1 \rangle$ . Fig-296 ures 5(a) and (b) indicate that the control methods amplify streamwise velocity 297 streaks by inducing significant streamwise fluctuations in the near-wall region. 298 In exchange, a slight drop in the remaining Reynolds stress components is ev-299 ident from Figures 5(c)-(h). According to Figure 5(a), the global turbulent 300 kinetic energy at  $Re_{\tau} \approx 180$  is increased (Figure 2(c)-(d)) when the control 301 methods are applied because the amplified streaks fill about 10% of the chan-302 nel. At  $Re_{\tau} \approx 1000$ , the control techniques energise the streaks similarly, but 303 with increasing Reynolds number the wall-normal extent of the streaks reduces. 304 Based on Figure 5(b), near-wall streaks occupy only ca. 2% of the channel 305 at  $Re_{\tau} \approx 1000$ . In addition, at  $Re_{\tau} \approx 1000$ , the control methods weaken the 306 large-scale motions of the log-layer, which contain most of the turbulent kinetic 307 energy at high Reynolds numbers [61, 62]. This phenomenon can be observed 308 in Figure 5(b), where  $\Delta \langle u'_1 u'_1 \rangle$  is negative above  $x/\delta = 0.05$ . The increase in 309  $\langle u'_1 u'_1 \rangle$  in Figure 5(a)-(b), and decreases in  $\langle u'_2 u'_2 \rangle$ ,  $\langle u'_3 u'_3 \rangle$ , and  $\langle -u'_1 u'_2 \rangle$  visi-310 ble in Figure 5(c)-(h) suggest that momentum transfer decreases between the 311 streamwise and other velocity components compared to the baseline case. 312

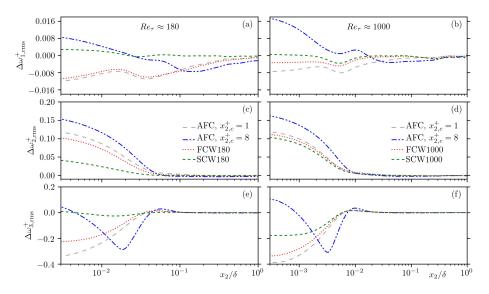


Figure 6: Change in root-mean-square fluctuating vorticity components with wall distance for different control techniques at  $\text{Re}_{\tau} \approx 180$  (left column) and at  $\text{Re}_{\tau} \approx 1000$  (right column). Streamwise (a)-(b), wall-normal (c)-(d), and spanwise (e)-(f) components.

The streamwise wall motions of the control methods directly modify the 313 spanwise vorticity fluctuations depicted in Figure 4. Figure 6(e)-(f) shows un-314 equivocally the strong influence of the control techniques on the spanwise vor-315 ticity fluctuations (and therefore on streamwise wall shear stress fluctuations), 316 especially in the near-wall region. The rms spanwise vorticity profiles underline 317 that the active control in shear-cancelling mode  $(x_{2,c}^+ = 1)$  and efficient compli-318 ant walls, such as FCW180, FCW1000, and SCW1000, damp spanwise vorticity 319 fluctuations at the wall. In shear-increasing mode, the active control amplifies 320  $\omega_3'$  very close to the wall. However, as depicted by the lines corresponding to 321  $x_{2,c}^+ = 8$  in Figures 6(e) and (f), the increase in  $\omega'_3$  at the wall turns into a net 322 cancellation of  $\omega'_3$  in the near-wall region. This behavour is a direct consequence 323 of the fluctuating velocity profiles with reversed shear, as visualised in Figure 324 **4**(f). 325

The rms wall-normal vorticity profiles  $(\omega'_2)$  in Figures 6(c)-(d) confirm that the control methods introduce statistically significant wall-normal vorticity fluctuations representing increased shear between the streaks. Whereas FCW180,

FCW1000 and the active control with  $x_{2,c}^+ = 1$  lower  $\omega'_1$  throughout the do-329 main, streamwise vorticity fluctuations are amplified in the vicinity of the wall 330 in the case of active control with  $x_{2,c}^+ = 8$  and SCW180 and SCW1000 according 331 to Figures 6(a)-(b). In every case where statistically significant drag reduction 332 (more than 1%) occurs, vorticity fluctuations are increased only in the near-wall 333 regions, which account for 10% and 2% of the channels, at  $\text{Re}_{\tau} \approx 180$  and 1000, 334 respectively. Figures 6(a)-(d) and Figures 6(e)-(f) reveal that successful control 335 methods weaken vorticity fluctuations throughout the majority of the channel 336 compared to the baseline case, owing to spanwise vorticity cancellation near the 337 wall. 338

The near-wall cycle contributes significantly to turbulence production in 339 boundary layers [52]. Nonlinear interactions between the mean flow, quasi-340 streamwise vortices, and velocity streaks redistribute near-wall streamwise mo-341 mentum fluctuations first to spanwise and then to wall-normal momentum 342 fluctuations as the wall distance increases [54]. The negative regime of the 343  $\Delta_r \omega'_{1,\text{rms}}$  curves in Figures 6(a)-(b) implies that quasi-streamwise vortices are 344 weakened by the control. For this reason, a lower turbulence production and 345 inter-component momentum transfer compared to the baseline case should be 346 measurable based on the Reynolds stress budgets. 347

The Reynolds stress transport equation [41, 63] for statistically steady state turbulent flows reads as

350

$$\langle u_k \rangle \frac{\partial \langle u'_i u'_j \rangle}{\partial x_k} = P_{ij} + T_{ij} + \Pi_{ij} + D_{ij} + \epsilon_{ij}.$$
 (11)

where  $P_{ij}$  is the production rate,  $T_{ij}$  is the turbulent transport rate,  $\Pi_{ij}$  denotes the velocity-pressure gradient term,  $D_{ij}$  is the viscous diffusion rate, and  $\epsilon_{ij}$  is the dissipation rate of the corresponding Reynolds stress components. Expand-

ing these terms from the right hand side of Eq. (11) leads to 354

$$P_{ij} = -\langle u'_i u'_k \rangle \frac{\partial \langle u_j \rangle}{\partial x_k} - \langle u'_j u'_k \rangle \frac{\partial \langle u_i \rangle}{\partial x_k};$$

$$T = \frac{\partial \langle u'_i u'_j u'_k \rangle}{\partial x_k}.$$

56 
$$T_{ij}$$

3

357

359 360

$$\Pi_{ij} = -\frac{\partial x_k}{\partial x_k},$$
$$\Pi_{ij} = -\left\langle u'_i \frac{\partial p'}{\partial x_j} \right\rangle - \left\langle u'_j \frac{\partial p'}{\partial x_i} \right\rangle;$$

$$D_{ij} = \frac{1}{\text{Re}} \frac{\partial^2 \langle u'_i u'_j \rangle}{\partial x_k \partial x_k} \text{ and}$$

$$\epsilon_{ij} = -\frac{2}{\text{Re}} \left\langle \frac{\partial u'_i}{\partial x_k} \frac{\partial u'_j}{\partial x_k} \right\rangle.$$
(12)

Thereafter, turbulent kinetic energy transport terms can be computed based on 361 Equations (4) and (11) so that, for instance,  $P_k = P_{ii}/2$ . 362

Baseline turbulent kinetic energy and Reynolds shear stress budgets are 363 listed in Appendix B. Regarding near-wall turbulent kinetic energy transport, 364 the control techniques cause the most distinct increase in dissipation (less loss) 365 balanced by diffusion (D) as shown in Figures 7(a) and (b). Global turbulent 366 kinetic energy dissipation is linked to global enstrophy [47], and hence the con-367 trol techniques weaken dissipation (the leading loss term of turbulent kinetic 368 energy) by reducing vorticity fluctuations. Weakened turbulent dissipation is 369 naturally accompanied by amplified near-wall (mainly streamwise) fluctuations. 370

The sum of the velocity-pressure gradient term and the turbulent transport 371 rate  $(\Pi_{ij} + T_{ij})$  dictates momentum distribution between the diagonal Reynolds 372 stress components [63]. From Figures 7(a) and (b), decreased  $\Pi + T$  is evident 373 highlighting that the control techniques indeed mitigate inter-component mo-374 mentum transport. Therefore, in the successful controlled cases, fluctuations 375 remain somewhat restricted to the streamwise velocity component. The corre-376 sponding suppressed momentum transfer between the mean flow and the fluc-377 tuations is symbolised by turbulent kinetic energy and Reynolds shear stress 378 production decay as shown in Figures 7(a)-(d). According to the Fukagata-379 Iwamoto-Kasagi identity [64], suppressing the integrated Reynolds shear stress 380 is equivalent to drag reduction. The statistical analysis of the control techniques 381

emphasises a connection between vorticity fluctuations and drag reduction which overlaps with the findings of previous studies uncovering links between friction drag, enstrophy [47] and velocity-vorticity correlations [65].

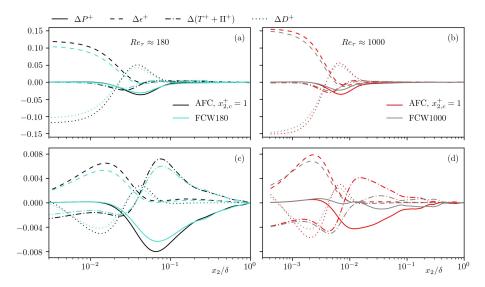


Figure 7: Change in turbulent kinetic energy and Reynolds shear stress transport terms with wall distance for different control techniques at  $\text{Re}_{\tau} \approx 180$  (left column) and  $\text{Re}_{\tau} \approx 1000$  (right column). Turbulent kinetic energy (a)-(b), and Reynolds shear stresses  $-\langle u'_1 u'_2 \rangle$  (c)-(d).

#### 385 3.4. Lagrangian Wall Motions

Finally, wall motions of the compliant surfaces are analysed to evaluate their realisation potential. To this end, the solely streamwise Lagrangian displacement field of the wall is determined by integrating the velocity field. Considering the mounted rotating disc model in Figure 1(b), the analysed Lagrangian displacement field describes points travelling from one disc to another. For video sequences visualising the wall velocity and the displacement fields, see the Supplementary Data available online.

The material lines corresponding to SCW180 preserve their consistency and exhibit standing wave-like movements but such wall motions are not sufficient to sustain statistically significant friction drag reduction (see Table 2). By comparison, in the case of FCW180, the wall needs to support large deformations in positive and negative directions within a short distance in order to cancel wall shear stress fluctuations originating from streaks. After the material points are clustered in the neighbourhood of low wall velocity regions between streaks, they travel together. Both FCW1000 and SCW1000 behave similarly to FCW180 resulting in dense and sparse wall sections which are difficult to realise beyond the conceptual rotating disc model. Representative rms displacement values for the selected compliant walls are summarised in Table 3. Table 2. Root mean acuum displacement values corresponding to colorted compliant walls

Table 3: Root-mean-square displacement values corresponding to selected compliant walls after  $t_{\rm int}$  time.

ID	$t_{ m int}$	rms displacement
SCW180	$2.74\delta/u_{\tau} = 495\nu/u_{\tau}^2$	$30\delta_{\nu}$
FCW180	$2.74\delta/u_{\tau} = 495\nu/u_{\tau}^2$	$501\delta_{\nu}$
SCW1000	$0.50\delta/u_{\tau} = 495\nu/u_{\tau}^2$	$393\delta_{\nu}$
FCW1000	$0.50\delta/u_{\tau} = 495\nu/u_{\tau}^2$	$764\delta_{\nu}$

#### 404 4. Conclusions

Active and passive flow control strategies for drag reduction have been in-405 vestigated by means of direct numerical simulations of canonical channel flows 406 at friction Reynolds numbers of 180 and 1000. The active control technique 407 used herein was proposed by Choi et al. [25], and promoted solely stream-408 wise wall fluctuations driven by the streamwise wall shear stress. The passive 409 control technique comprised a compliant surface based on an array of damped 410 harmonic oscillators that ensured solely streamwise wall fluctuations similar to 411 those of the foregoing active control approach. Our previous studies demon-412 strated [34, 39, 40] that the foregoing conceptual compliant surface can sustain 413 drag reduction by exploiting behaviour similar to that of active control. Using 414 direct numerical simulation, we have uncovered the corresponding drag reduc-415 tion mechanism. 416

For detailed analysis, active control techniques were selected, in addition to relatively flexible and stiff compliant surfaces. It has been demonstrated that, when successful, both active and passive control methods reduce spanwise vorticity fluctuations at the wall (and hence the shear between velocity

streaks and the wall). By doing so, the control techniques inevitably strengthen 421 shear between the streaks, leading to increased wall-normal vorticity fluctua-422 tions. The former effect seems to be beneficial from the drag reduction point of 423 view, whereas the second appears to limit control performance. The Reynolds 424 stress, vorticity, and Reynolds stress transport statistics suggest that reducing 425 spanwise vorticity fluctuations at the wall effectively lower vorticity fluctuations 426 and momentum transfer over the majority of the turbulent boundary layer. The 427 drag reduction mechanisms of the investigated active and passive control meth-428 ods differ from established flow control strategies, such as opposition control 429 [25–28] and spanwise wall oscillations [37, 59]. According to the Lagrangian 430 displacement field analysis, large-scale wall motions are required to achieve a 431 modest friction drag reduction. 432

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#### 441 Appendix A. Baseline velocity and vorticity statistics

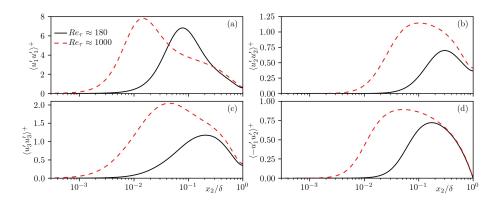


Figure A.8: Reynolds stresses as functions of the wall distance and Reynolds number: streamwise (a), wall-normal (b), spanwise (c) components, and Reynolds shear stress (d).

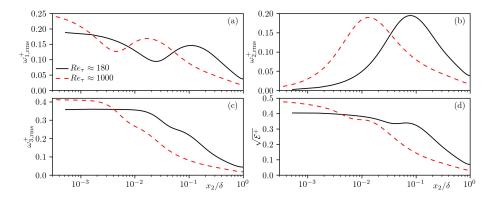


Figure A.9: Vorticity statistics as functions of the wall distance and Reynolds number: streamwise (a), wall-normal (b), spanwise (c) components, and square root of turbulent enstrophy representing the magnitude of the fluctuating vorticity vector (d).

#### 442 Appendix B. Baseline Reynolds stress transport budgets

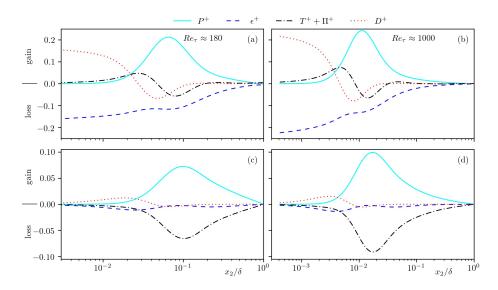


Figure B.10: Turbulent kinetic energy and Reynolds shear stress transport terms as functions of the wall distance at  $\text{Re}_{\tau} \approx 180$  (left column) and at  $\text{Re}_{\tau} \approx 1000$  (right column): turbulent kinetic energy (a)-(b) and Reynolds shear stress  $-\langle u'_1 u'_2 \rangle$  (c)-(d).

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