

A case study of energy absorption buildup factors in some human bones for gamma energies 30 keV to 1.5 MeV

Vishwanath P Singh¹, Seyed Pezhman Shirmardi*², Reza Bagheri³, Ruhollah Adeli⁴, Mansoureh Tatari⁵

¹Department of Physics, Karnataka University, Dharwad, India

²Radiation Application Research School, Nuclear Science and Technology Research Institute (NSTRI), Tehran, Iran

³Reactor School, Nuclear Science & Technology Research Institute (NSTRI), Tehran, Iran

⁴Nuclear Fuel Cycle Research School, Nuclear Science and Technology Research Institute (NSTRI), Tehran, Iran

⁵Physics Department, Yazd University, Iran

*Corresponding author: email address: pshirmardi@aeoi.org.ir (P.Shirmardi)

ABSTRACT

Human body consists of some tissues which bone is one of the important living and growing tissues. In this research, energy absorption buildup factor (EABF) values of 27 types of bone have been computed for photon energy 0.03 to 1.5 MeV up to 40 mean free path (40mfp) penetration depths. The Inner bone tissue, Spongiosa and Male sternum had the largest values of EABF in low photon energies, and great differences below 150 keV photon energy were noted relative to the other bones. This study would be of utmost importance for estimation of the effective dose to the human bones, radiation therapy and various medical applications.

Keywords: Energy absorption buildup factor; GP fitting; Bone; Photon

INTRODUCTION

The effect of radiation on human organs depends upon absorbed dose, energy, radiation types and organs irradiated. Gamma and x-rays have various interactions with the materials (Photo electric absorption, Compton scattering, Pair production and Coherent) [1-13]. These photons colliding the human organs not only loose energy and are absorbed, but also generate new photons by multiple scattering [2,3,12]. Buildup factor is an enhancing factor used to get the corrected response to un-collided photons by including the contribution of scattered photons. This factor depends upon the energy of the photons, atomic number of the target and the penetration depth, as well as the radiation source and the medium geometry. The buildup factor in which the quantity of interest is the absorbed energy in the medium is defined as the energy absorption buildup factor. In 1993, Harima prepared a review on calculations and applications of buildup factors [10]. In medical applications, photons (Gamma- and X-rays) are

mostly used for radiotherapy and diagnostic of a lot of diseases [12]. As a result, different body tissues are being exposed to photons. Therefore, having the data about how these radiations interact with the body is an essential piece of information. When gamma or x-rays enter the body, they reduce their energy inside the body, leading to secondary photon which can be estimated by buildup factor. Owing to the buildup of degraded gamma rays by scattering within the tissue, the maximum dose to the tissue is located at the inside when tissues are exposed to radiations. Considering the importance of buildup of scattered gamma rays, an attempt has been made to calculate the EABF for some bones. Lately, buildup factors for some polymers and tissue substitute materials were computed by Kurudirek and coworkers [12]. There is a need for gamma-ray buildup factors of low-Z complex materials, such as various bones, in radiotherapy and diagnostics for dose estimations. In general, the results of the study can help in estimating safe dose levels for radiotherapy and diagnostics. In

the present study, we have calculated energy absorption buildup factors (EABF) for various bones, such as inner bone tissue, Spongiosa and Male sternum, etc. The calculations have been performed for energies of 30keV–1.5 MeV up to penetration depths of 40 mean free paths. The produced buildup factor data is studied as a function of incident photon energy, etc. The data will be helpful for many applications especially in radiotherapy and diagnostic, for the preparation of phantoms using bone-equivalent materials.

MATERIALS AND METHODS

Elemental compositions of different bones in human body are seen in Table 1 [14]. The Z_{eq} of the bone tissues for interactions varies with the energy of photons. The buildup of photons in the materials is more due to Compton scattering, so Z_{eq} is derived from the Compton scattering process.

The buildup factors of bones are estimated by using GP fitting coefficients in the gamma energies up to 40 mfp using the equations [1-3, 9-11] given below,

$$B(E, x) = \begin{cases} 1 + \frac{(b-1)(K^x - 1)}{K - 1} & \text{for } K \neq 1 \\ 1 + (b-1)x & \text{for } K = 1 \end{cases} \quad (1)$$

$$K(E, x) = cX^a + d \frac{\tanh(x/X_k - 2) - \tanh(-2)}{1 - \tanh(-2)} \quad \text{for } x \leq 40 \text{ mfp} \quad (2)$$

where E is the energy of source, x is the penetration depth in units of mfp (mean free path), and a, b, c, d and X_k are GP fitting parameters. The value of the parameter b represents the buildup factor at 1 mfp. The variation of the parameter K with penetration depth corresponds to the photon dose multiplication.

Table 1. Elemental composition of some bones [14].

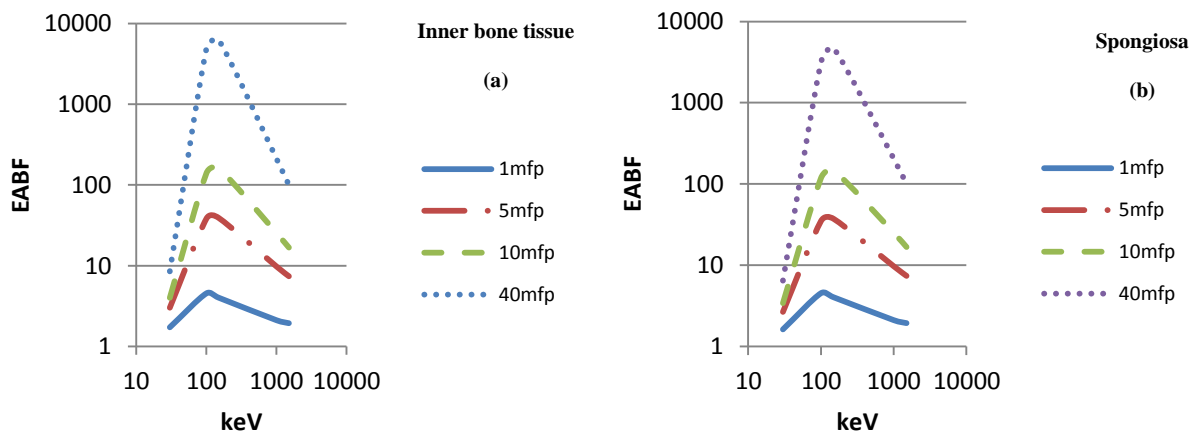
Sample Name	Density	H	C	N	O	Na	Mg	P	S	Cl	K	Ca	Fe
Inner bone tissue	1.12	8.6 80	13.01 4	3.60 4	66.47 3	0.08 0	0.06	2.433	0.46 1	0.00 0	0.23 0	4.965	0.00 0
Spongiosa	1.18	8.5 56	29.09 0	2.38 0	48.43 4	0.07 9	3.23 2	0.139	0.45 6	0.00 0	0.22 8	7.406	0.00 0
Male sternum	1.25	7.7 99	31.68 6	3.61 5	44.14 8	0.05 0	0.08 0	3.964	0.12 0	0.00 0	0.11 0	8.378	0.05 0
Sacrum Male	1.29	7.4 03	30.24 0	3.64 6	44.15 6	0.05 0	0.09 0	4.525	0.13 0	0.00 0	0.10 0	9.620	0.04 0
D6L3 male with cartilage	1.30	7.3 08	26.67 7	3.51 9	47.75 9	0.04 0	0.09 0	4.541	0.24 1	0.00 0	0.08 0	9.704	0.04 0
Famur whole column	1.32	7.0 89	25.96 0	3.54 0	47.66 9	0.04 0	0.10 0	4.853	0.24 1	0.00 0	0.08 0	10.39 8	0.03 0
Male vertebral column	1.33	7.0 98	25.79 2	3.59 9	47.18 6	0.10 0	0.10 0	5.098	0.30 0	0.10 0	0.10 0	10.49 7	0.03 0
D6L3 male no cartilage	1.33	6.9 87	28.70 6	3.67 3	44.10 6	0.05 0	0.10 0	5.100	0.15 0	0.10 0	0.09 0	10.89 9	0.04 0
Humerus spherical head	1.33	7.0 84	37.81 3	2.59 4	34.12 2	0.10 0	0.10 0	5.587	0.20 0	0.10 0	0.09 0	12.17 2	0.04 0
Famur spherical head	1.34	6.9 41	24.87 3	2.89 2	47.21 3	0.02 0	0.07 0	5.455	0.18 9	0.10 0	0.09 0	12.11 7	0.04 0
C4 male with cartilage	1.37	6.6 45	24.45 6	3.57 8	47.51 9	0.05 0	0.05 0	5.473	0.26 1	0.10 0	0.07 0	11.76 7	0.03 0
Famur conical traochanter	1.37	6.7 35	24.31 4	2.95 3	47.03 2	0.02 0	0.08 0	5.737	0.20 0	0.10 0	0.07 0	12.73 1	0.03 0
Secrum female	1.38	6.5 47	27.08 6	3.71 3	44.09 2	0.05 0	0.12 0	5.729	0.17 0	0.10 0	0.08 0	12.27 5	0.04 0
Humerus whole specimen	1.39	6.5 14	23.74 3	3.02 3	46.83 8	0.02 0	0.08 0	6.026	0.20 9	0.10 0	0.08 0	13.32 8	0.04 0
Male ribs 2 and 6	1.41	6.3	26.33	3.72	44.10	0.05	0.12	6.020	0.18	0.10	0.08	12.91	0.03

		39	5	4	5	0	0		0	0	0	8	0
Male pelvic bones	1.41	6.3 30	26.28 8	3.72 4	44.09 9	0.05 0	0.12 0	6.040	0.18 0	0.10 0	0.07 0	12.96 9	0.03 0
C4 male no cartilage	1.42	6.2 80	26.10 8	3.73 4	44.09 9	0.05 0	0.12 0	6.110	0.18 0	0.10 0	0.07 0	13.11 9	0.03 0
Famur whole specimen	1.43	6.1 76	22.84 0	3.12 3	46.53 8	0.03 0	0.10 0	6.476	0.22 0	0.10 0	0.07 0	14.29 9	0.03 0
Female pelvic bones	1.45	5.9 80	25.01 0	3.75 4	44.09 9	0.05 0	0.13 0	6.530	0.20 0	0.10 0	0.07 0	14.04 8	0.03 0
Humerus total bone	1.46	6.0 04	31.27 9	2.90 2	37.31 2	0.04 0	0.14 0	6.894	0.23 0	0.10 0	0.07 0	14.99 9	0.03 0
Male clavicle scapula	1.46	5.9 94	31.23 2	2.90 2	37.33 6	0.04 0	0.14 0	6.905	0.23 0	0.10 0	0.07 0	15.02 1	0.03 0
Humerus cylindrical shaft	1.49	5.7 19	21.62 7	3.26 3	46.12 8	0.03 0	0.12 0	7.086	0.23 0	0.10 0	0.07 0	15.59 9	0.03 0
Male ribs 10	1.51	5.5 69	23.49 3	3.78 2	44.07 2	0.05 0	0.15 0	7.126	0.21 0	0.10 0	0.08 0	15.32 9	0.04 0
Cranium	1.60	4.9 34	21.19 5	3.84 5	44.08 7	0.06 0	0.16 0	8.000	0.24 0	0.10 0	0.04 0	17.31 9	0.02 0
Mandible	1.66	4.5 86	19.89 2	3.86 7	44.09 0	0.06 0	0.17 0	8.502	0.26 0	0.10 0	0.03 0	18.43 3	0.01 0
Femur culindrical shaft	1.75	4.1 94	20.37 2	3.79 5	41.44 2	0.10 0	0.20 0	9.287	0.30 0	0.10 0	0.03 0	20.17 2	0.01 0
Cortical bone	1.90	3.3 87	15.48 8	3.96 7	44.06 5	0.06 0	0.21 0	10.19 2	0.31 0	0.10 0	0.03 0	22.18 2	0.01 0

RESULTS AND DISCUSSION

Figures (2-6) show the results of EABF for bones at selected energies (Figure 1(a -g)) as well as at different penetration depths. Also the variation of EABF with the some bones at different energies and penetration depth (Figure 7(a-e)) has been shown in graphical form. As shown in figure 1(a-g), it has been indicated that EABF values of bones start increasing with increase in gamma energy up to a maximum value at around 100-150keV. Due to the

photoelectric absorption, more increase in gamma energy decreases the value of EABF. With increase in gamma energy the Compton scattering process is dominant which results in more multiple scattering and leads to increase in EABF values. Maximum values of EABF for all bones have been observed at 150keV figure1 (a-g). In high energies (>1MeV), the variation of EABF with incident gamma energy seems to be independent of the chemical composition of given samples at this energy region.



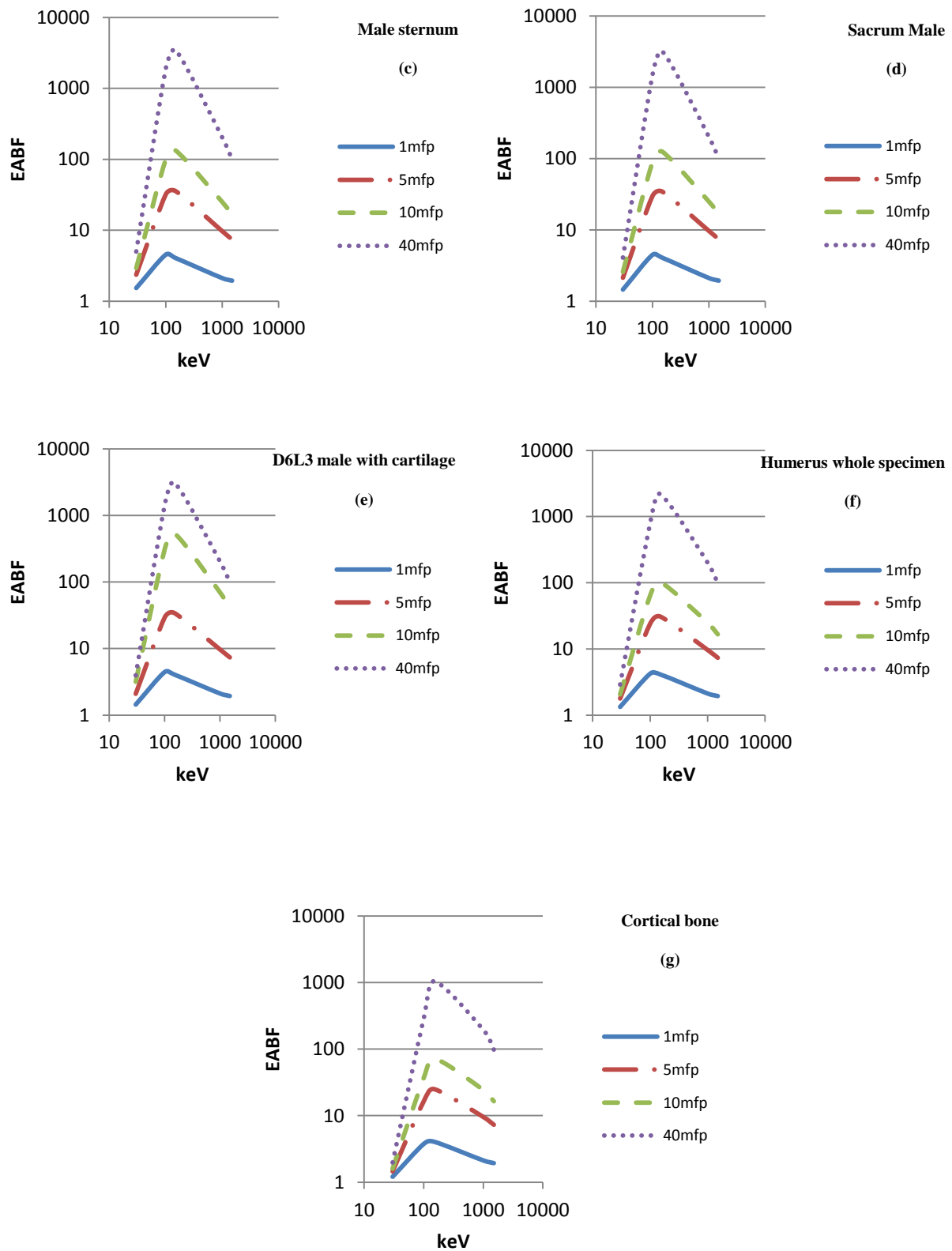
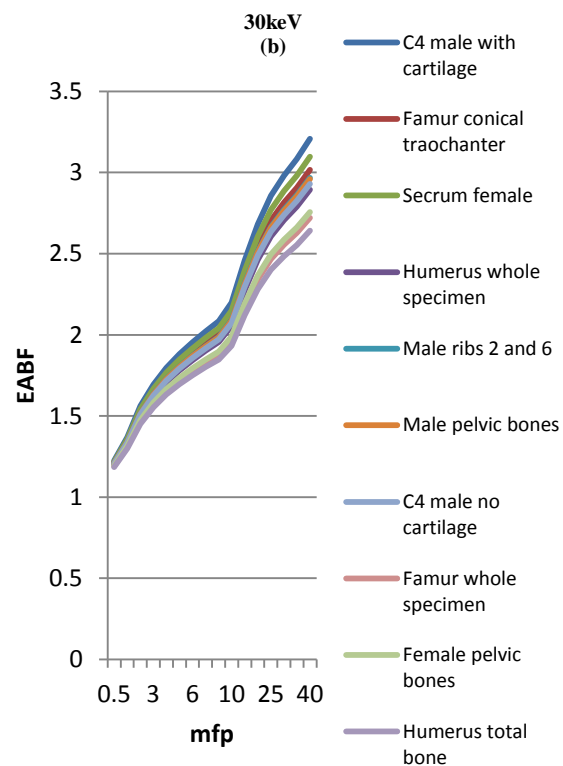
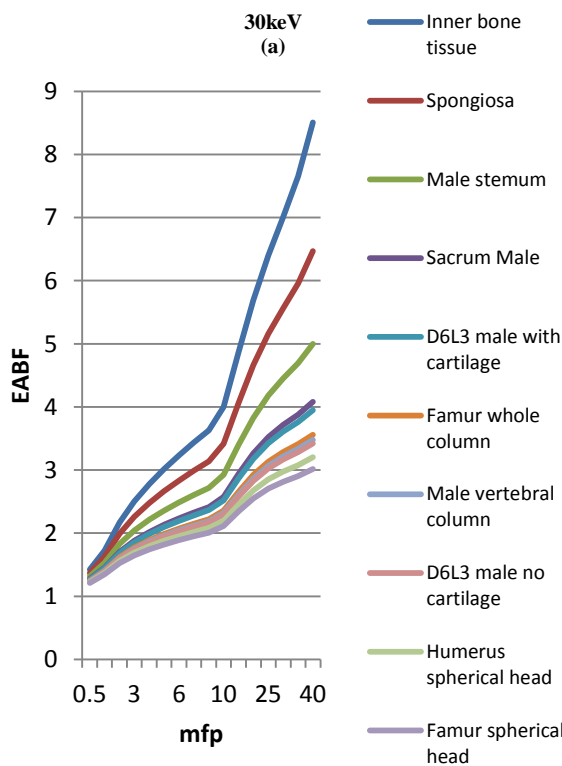


Figure 1. Variation of EABF as a function of incident photon energy (keV) for Inner bone tissue, spongiosa, mal sternum , sacrum male, D6L3 male with cartilage, Humerus whole specimen And cortical bone.

The curves at different energies in figures (2-6) show that there is increase in EABF with increase in penetration depth for all samples. It is due to the fact that the increase in penetration depth increases the interaction of gamma-radiation photons with matter resulting in generation of large number of low energy photons due to occurrence of Compton scattering process. It has been observed that at lower than 100keV energies the values of EABF for the bones is low and the variation is between 2-9 for 40 mfp. By increasing the energy to 100-150keV, EABF increases to higher than 6000 for 40 mfp. The variation in this range of energies will be more

severe. The variation of EABF in low penetration depth is not affected by the type of bone samples. In the energy range of 1-1.5MeV, EABF has the almost constant values for lower mfp (lower 10mfp), and increases to higher than 200 for 40 mfp. The EABF in high energies is not affected by the chemical composition; so, in the medium gamma energies, EABF has the maximum values for all bones, and in low energies has the minimum values. It is shown that for energies higher than 1MeV, there is a drop in the value of EABF which ultimately indicates the dominance of pair production process in this range of energy.



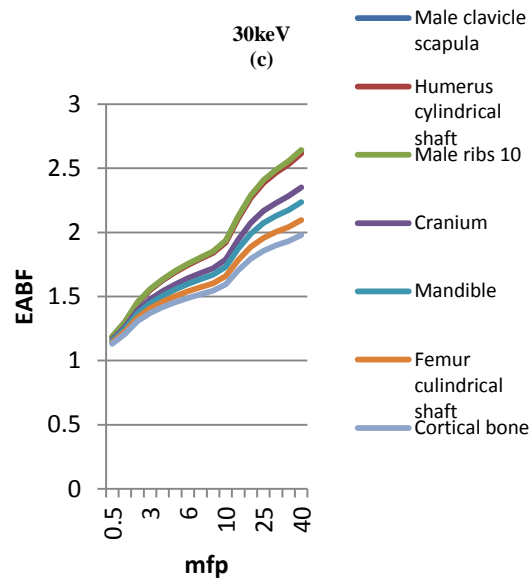
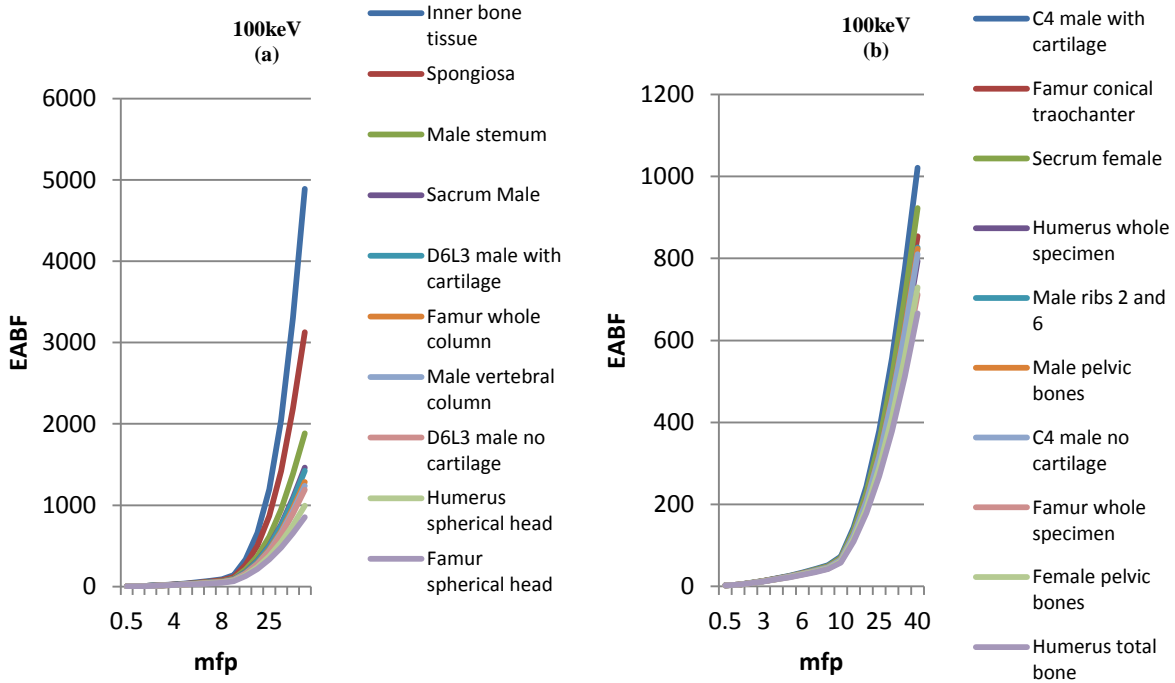


Figure 2. Variation of EABF with penetration depth of all bones at energy 30keV



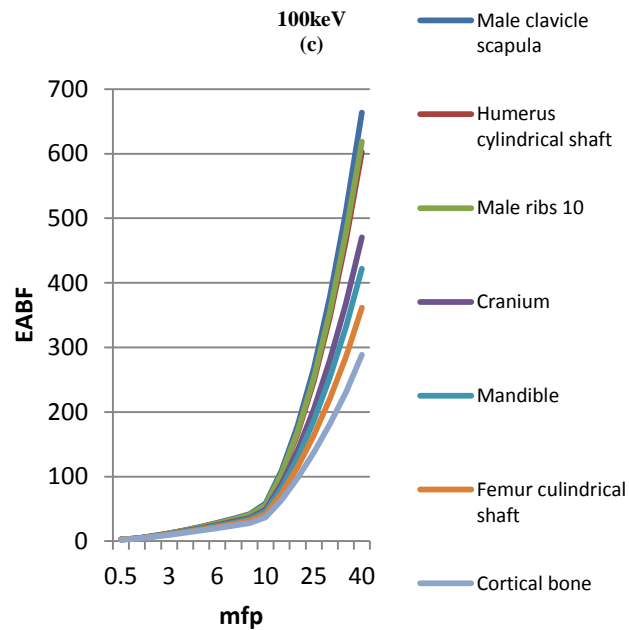
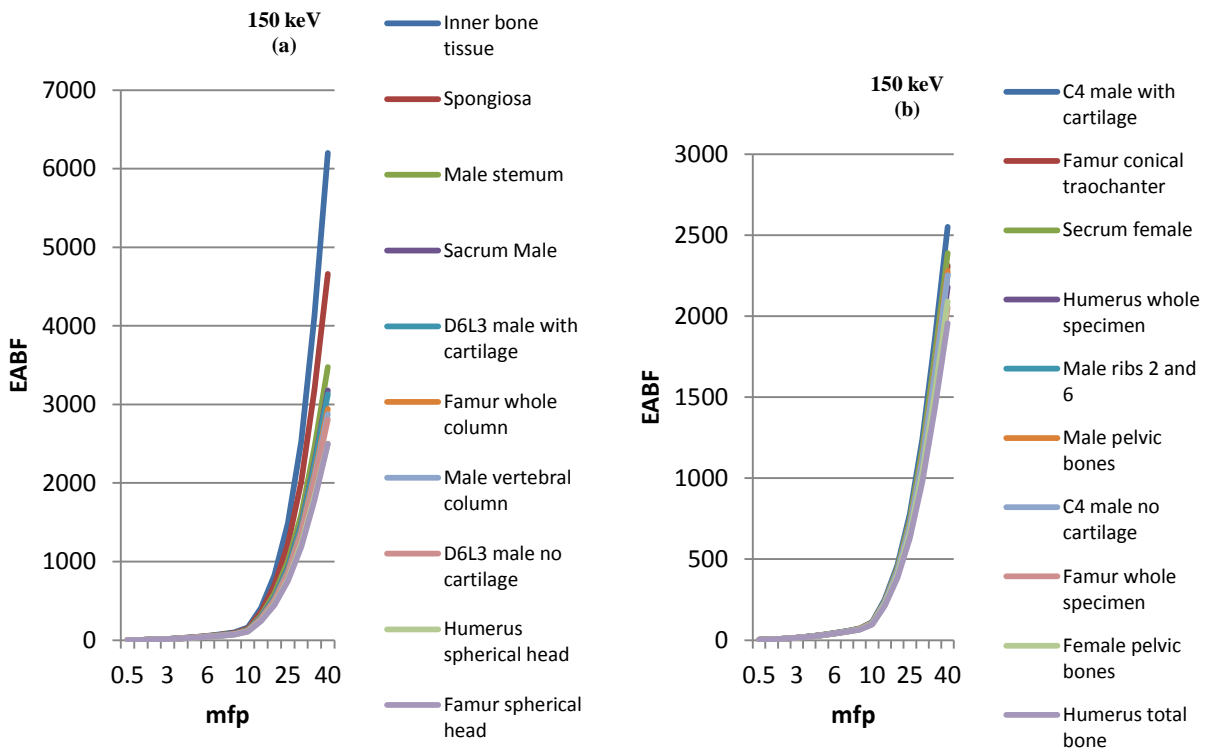


Figure 3. Variation of EABF with penetration depth of all bones at energy 100keV



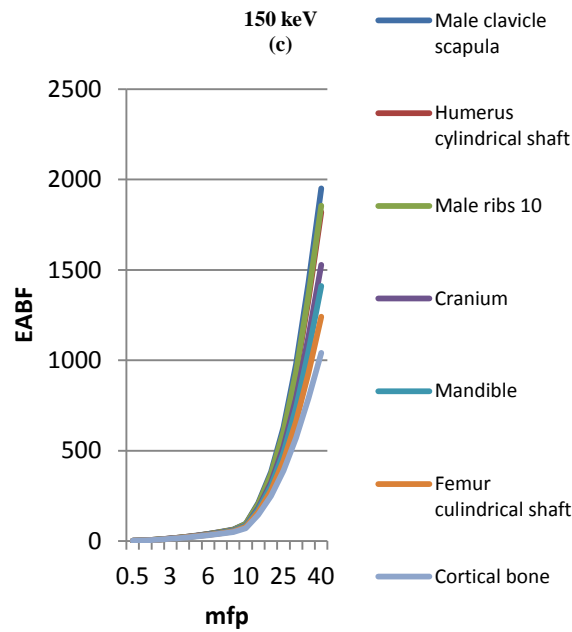
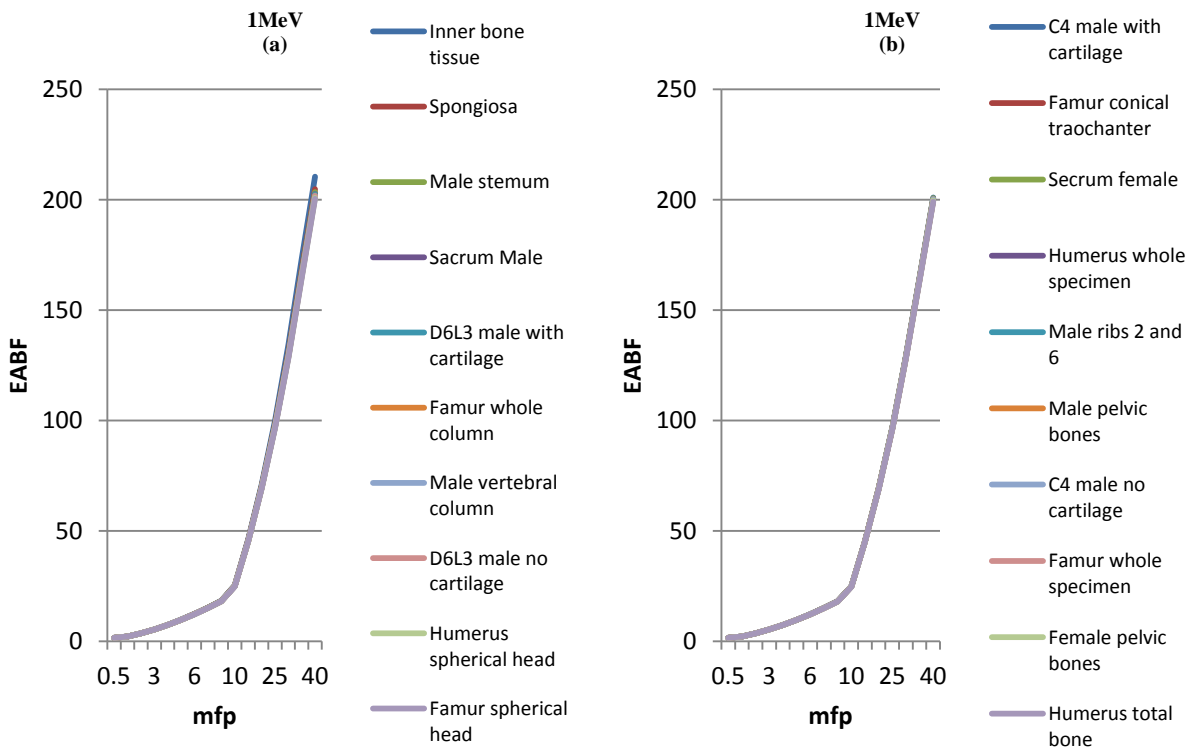


Figure 4. Variation of EABF with penetration depth of all bones at energy 150keV



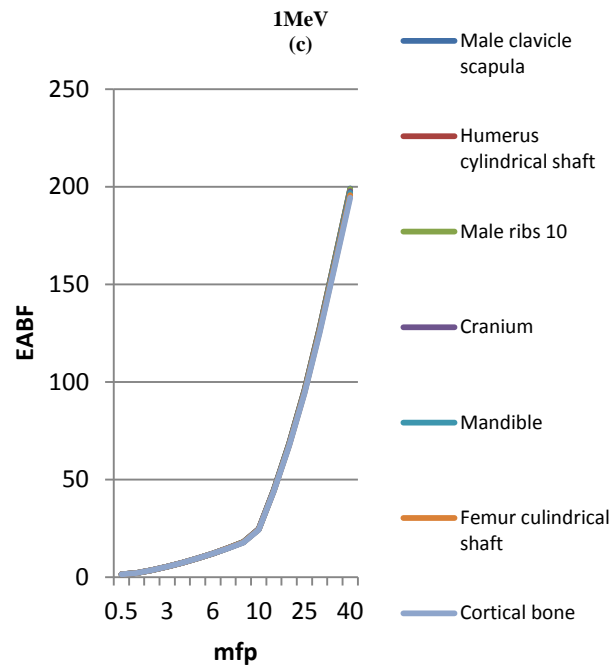
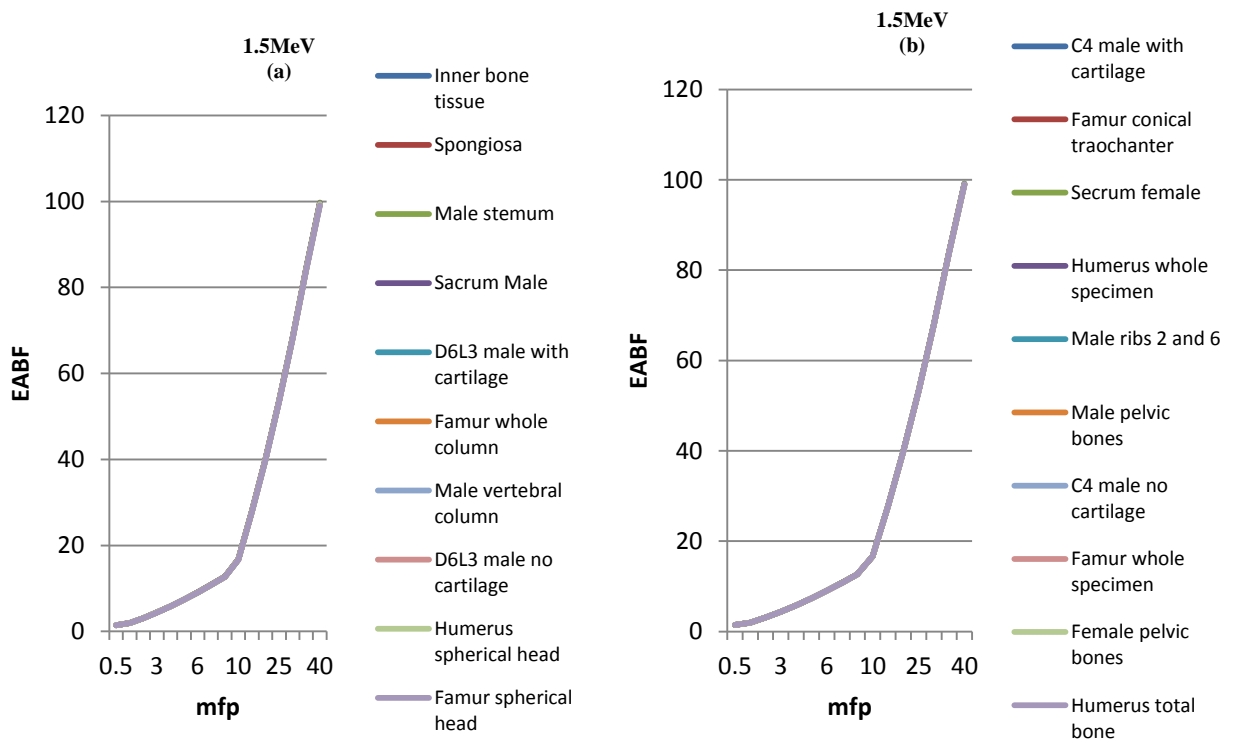


Figure 5. Variation of EABF with penetration depth of all bones at energy 1MeV



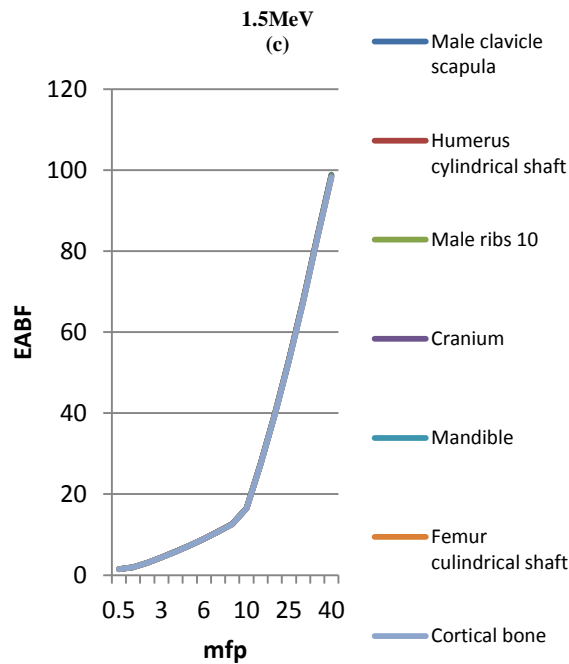
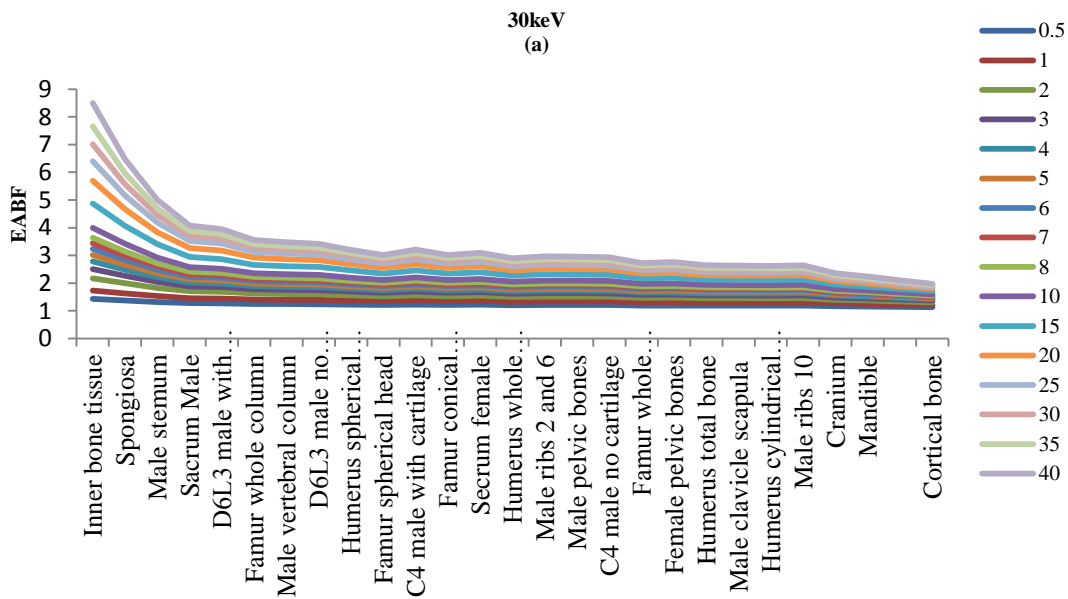
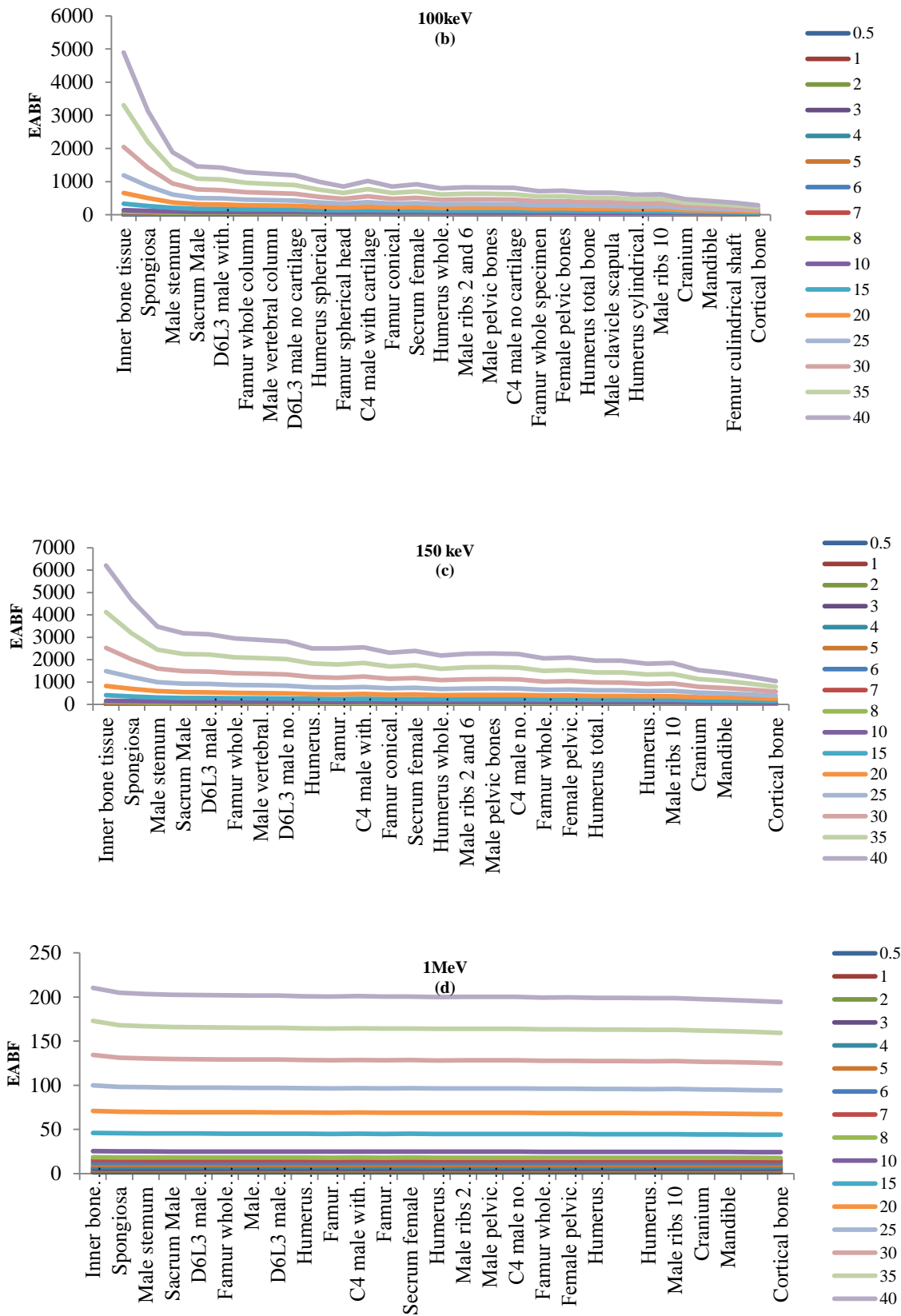


Figure 6. Variation of EABF with penetration depth of all bones at energy 1.5MeV

The results show that with the increase in energy, EABF for all bones got constant values. Therefore,, the curves are straight lines in 1.5 MeV.

EABF values for bones with lower density such as inner bone tissue, spongiosa and male sternum are the maximum in low energies (30keV) relative to the other bones.





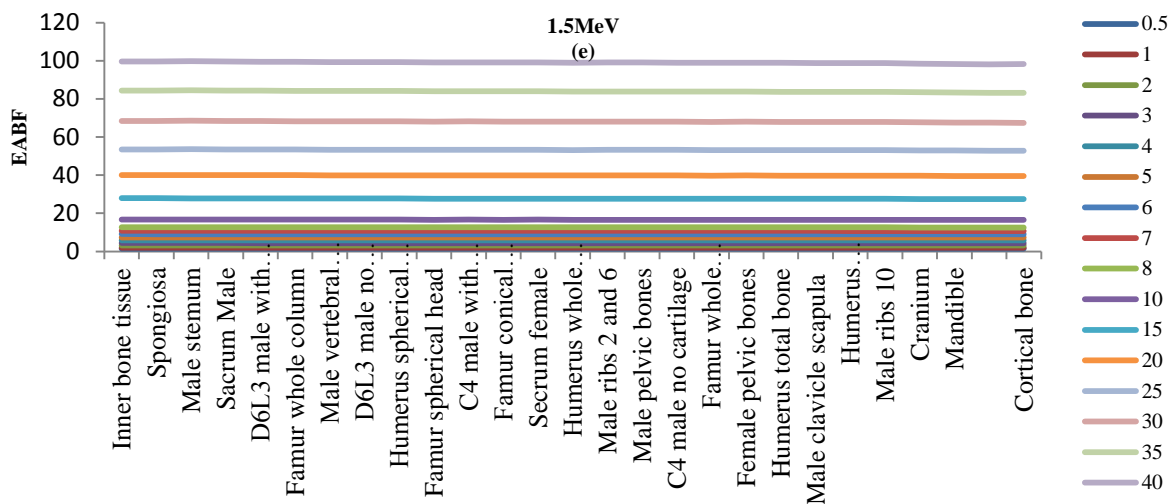


Figure 7. (a-e). Variation of EABF with the kinds of bones at different energies and mfps.

Generally, the EABF is small for all depths of penetration (mfp) at low energies. Photoelectric is the conquering gamma interaction process at low energies, leading to an exclusion of the incident of low-energy gamma rays and thus not allowing any tangible buildup of gamma rays. The EABF got large values at range of energies 100-150keV; at this range of energy the interaction cross sections for Compton scattering is high and the EABF reaches large values for a given penetration depth. This is owed to the multiple scattering of gamma rays in Compton scattering. The multiple scattered gamma rays exist for a longer time in the material, which results in a higher value of buildup factor.

CONCLUSION

In this research, the energy absorption buildup factor (EABF) values of different bones in energy range 30keV to 1.5 MeV up to 40 mfp penetration depths were calculated. The variation of EABF values of the bones proved to be dependent upon the photon energy, the penetration depth and the chemical compositions. According to the results, increase in gamma energy decreases the value of EABF; moreover, in high mfp's, EABF has an enhancing state for all bone tissues increase (EABF variations are severe in above 8mfp). EABF variations for bone tissues are almost constant in high gamma

energies. The bone equivalent and dosimetric properties of the present selected bone tissues are useful in clinical applications such as radiological examinations and therapeutic under radiation conditions where the effective energy of the photon attenuation field is difficult to assess.

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"The authors declare no conflict of interest"

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