Microbial decomposition

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Mathematical Submodels in Water Quality Systems

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CHAPTER 12

MICROBIAL DECOMPOSITION

by
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12.1 INTRODUCTION

Role of microbial decomposition in biodegradation processes of organic pollutants.

Within aquatic ecosystems, microbial decomposition of organic matter plays a prominent role in the energy and mass transformation processes (Jørgensen, 1983a). Organic waste water discharge in a river results in dissolved oxygen uptake, either directly by chemical oxidation of the reducing pollutants (see Chap. 10), or by their metabolism by micro-organisms, i.e. their biodegradation. Raising the temperature of rivers reduces oxygen solubility and accelerates the kinetics of chemical and microbiological oxygen and polluting load reduction.

Several terms are used to describe globally these processes. **Self-purification** is a neutral expression, meaning elimination of dissolved or particulate matter with "polluting" properties, irrespective of the mechanism involved (Wuhrmann, 1972). **Biodegradation** is a more commonly accepted term which describes alterations of a compound sufficiently important to change its identity (Dart and Stretton, 1980). All biodegradable compounds are ultimately converted into one of the very few key intermediates such as acetyl-coenzyme A or one of the tricarboxylic acid cycle intermediates before total oxidation occurs. As such compounds are also used for the resynthesis of larger molecules, only a portion of biodegradable compounds are totally oxidized to inorganic constituents.

Water, soil, sewage and mud are extremely complex environments biologically, chemically and physically (Dart and Stretton, 1980). Large numbers of organisms from different species and genera may be present displaying a wide range of degradative abilities. The organisms may show a spectrum of interactions, ranging from predation through commensalism to synergism. The presence or absence of predators, parasites or hosts may cause microbial populations to fluctuate over a wide range. This chapter will not describe such microbial decomposition at a biological level, but will present mathematical and experimental submodels used to simulate this wide range of interacting processes.

A large part of waste water disposal regulations refers to the **ability of various organic wastes to be biodegraded** in the ecosystem. Various procedures have been developed for the measurement of biodegradability of chemical compounds, either in the innoculated die-away tests where water, salts and biomass is incubated during 5 to 40 days with the tested substance, or with activated sludge test methods where large amounts of biomass and additional organic substrates are continously fed with air or oxygen for better adaptation ot large amounts of substrates (Blok, 1975). Such tests were proposed for monitoring either carbon dioxide formation or oxygen consumption in oxygen regulated "Sapromat" respirometric cells (Remiche and Van der Wielen, 1975). In the former case, an alternative to barium carbonate measurement is the direct monitoring of $^{14}CO_2$ formation from traces of ^{14}C radiolabelled organic compounds, such as amines (Boethling and Alexander, 1979). The simultaneous monitoring of carbon dioxide and oxygen allows discrimination between microbial decomposition and chemical oxidation.

Determination of parameters related to biodegradation: dissolved oxygen (DO), organic matter (OM) and biomass (B).

Since organic pollution control has been the first concern in water quality studies and regulations parameters relating to biodegradation are relatively well defined.

Dissolved oxygen (DO) is easily determined either with absolute chemical methods such as the Winkler volumetric titration using manganous and iodide salts in basic media, or with relative electrochemical methods using Clark-type electrode, i.e. cathodic reduction of oxygen diffusing through an hydrophobic membrane.

If DO may easily and rapidly be monitored with a precision better then 1-2%, **organic matter** (OM) represents a large variety of compounds and may not be determined without ambiguity. Several methods have appeared, each of them corresponding to a given goal. The Biochemical Oxygen Demand test (BOD) intends to assess the pollutional potential of a waste water which contains an available organic carbon source for aerobic organotrophic microorganisms, by measuring the amount of oxygen utilized during growth of the organisms in a sample of waste water (Gaudy, 1972). Standard methods for measuring BOD have been described and compared. DO variations are usually measured in diluted samples after 5 or 21 days incubation at 20°C (Stack, 1972 and 1973); alternatively, automatic respirometers enable the direct recording of oxygen consumption of undiluted samples. In the Warburg method, gas volume variations are monitored, whether in Marais or

"Sapromat" methods, and oxygen is supplied to the sample so that its concentration remains constant throughout the incubation test (Mytelka and Brenner, 1969; Remiche and Van der Wielen, 1975; Hung and Eckenfeld, 1976; Illic, 1978). The term 'ultimate BOD' is usually referred to in 21-days incubation tests - this test duration being necessary for total biodegradation of nitrogen-containing compounds (Stack, 1972). Nevertheless, as nitrogeneous compounds are often specifically measured and their microbial decomposition kinetics taken into account (see § 2.2.1), carbonaceous OM is then estimated by 5 days BOD, called BOD_5. The amount of OM may alternatively be determined either by chemical oxidation in standard conditions, such as 2 hr ebullition with excess bichromate in sulphuric acid (Chemical Oxygen Demand, COD) (Green et al., 1981), or by total oxidation by oxygen at 900°C, or by persulphate in the presence of heavy UV radiation (Total Oxygen Demand, TOD) (Clark, 1974); finally the carbon dioxide released during such total oxidation procedures is monitored in various ways. Carbonaceous compounds present in organic pollutants may be determined by their Total Organic Carbon (TOC). Since the OM content in surface water and in waters generally is of great economic and ecological importance, BOD, COD, TOD and TOC have been thoroughly studied and "mixed" methods with the accuracy of chemical titration have been proposed (Stack, 1973).

Biomass concentration (B) is even more difficult to determine than OM. Numerous methods have been developed, but none of them is generally accepted by the scientific community. Adenosine Triphosphate (ATP) is frequently chosen for evaluation of biomass. Indeed it is a fundamental constituent of all living cells, and only living ones, since it is destroyed very rapidly after cell death. It has been shown that the amount of ATP is proportional to the amount of cell organic carbon, which is the usual indicator of biomass: 0.30 to 0.39 g ATP is contained in 100 g cell organic carbon of algae and bacteria of different sizes and species (Holm-Hansen, 1970). Furthermore, trace amounts of ATP can be easily determined by bioluminescence, after cell filtration and extraction. When mixed with luciferine and luciferase, ATP extracts yield light emission in which the intensity maximum is proportional to the ATP amount, with the lower detection limit being as low as 10^{-12} mol (Tobin et al., 1978; Apoteker, 1981). But an alternative to ATP determination has been proposed - Deoxyribonucleic acid (DNA) content, though this rarely used for biomass estimation since it is known to retain its concentration level even after cell death. Finally, when phytoplanktonic biomass is to be determined, chlorophyl s are measured after cell filtration and extraction.

12.2 MATHEMATICAL MODELS OF MICROBIAL DECOMPOSITION

Different types of kinetic models of microbial decomposition.

Numerous kinetic models of water quality have been proposed to describe DO and BOD variations along a stream (Gromiec et al., 1983; Gromiec, 1983) in lakes or reservoirs (Orlob, 1983, Jørgensen, 1983b) and in waste water treatment processes. The first, and most widely used model, was proposed by Streeter and Phelps (1925) for the Ohio river. It states that oxygen uptake is equal to BOD uptake, and that both kinetics are first-order. Since then several modifications have been proposed to take into account the effect of dispersion (O'Connor, 1961, 1962, 1967), sedimentation and adsorption (Dobbins, 1964), photosynthesis and respiration (O'Connor and Di Torro, 1970), thermal exchanges (Lin et al., 1973a, b, c), bental demand (Shelton et al., 1978) and nitrogeneous biodegradation (Shelton et al., 1978; Knowles and Wakeford, 1978). Nevertheless, it has been frequently observed that first-order curves do not fit well the experimental variations of BOD, so that *second-order* kinetics were proposed for DO and BOD uptakes (Woodward, 1953; Revelle et al., 1965; Young and Clark, 1965; Zanoni, 1967; Edeline and Lambert, 1979). Their success in describing actual river evolution was not generally accepted.

Beside these field studies, Flegal and Schroeder (1976), Rauwel and Thévenot (1976) and Apoteker and Thévenot (1983) conducted laboratory experiments without renewal of DO: after organic discharges. All these authors observed lag-phases with no oxygen evolution, followed by exponential phases, similar to those encountered in experiments on cellular growth.

First-order kinetic models: Streeter-Phelps, O'Connor, Dobbins, Lin and Shelton models; examples and discussion.

Streeter and Phelps (1925) kinetic model of DO and BOD evolution in streams is based upon two main assumptions: firstly, both microbial decomposition of OM and reoxygenation of water by the atmosphere follow first-order kinetics; second, microbial DO and BOD uptakes are equal whatever the stage of OM decomposition and the type of OM. Taking these two assumptions as valid, two kinetic equations may be written:

$$dL / dt = -K_1 L \tag{12.1}$$

$$dC / dt = -K_1 L + K_2 (C_s - C) \tag{12.2}$$

where
L is the OM load, usually estimated as ultimate BOD, i.e. 21 days BOD ($M\ L^{-3}$),
C is the DO concentration ($M\ L^{-3}$) at time t (T),
C_s is the saturated DO concentration ($M\ L^{-3}$) at the water temperature T,
K_1 is the first-order biodegradation kinetic constant, also called deoxygenation rate constant (T^{-1}),
K_2 is the first-order oxygen transfer or reaeration kinetic constant (T^{-1}).

As presented later in this paragraph and in § 3.1, K_1 frequently does not take into account BOD excretion by nitrogeneous compounds and by sediments.

As DO concentration is frequently replaced by oxygen saturation deficit, $D = C_s - C$, equation (12.2) becomes:

$$dD\ /\ dt\ =\ K_1\ L\ -\ K_2\ D \tag{12.3}$$

The solutions to (12.1) and (12.3) are:

$$L\ =\ L_0\ \exp\ (\ -\ K_1\ t) \tag{12.4}$$

$$D_t\ =\ \frac{K_1\ L_0}{K_2\ -\ K_1}\ (\exp\ (-K_1\ t)\ -\ \exp\ (-K_2\ t))\ +\ D_0 \exp\ (-K_2\ t) \tag{12.5}$$

where
D_t is the dissolved oxygen saturation deficit after time t,
L_0 is the BOD at an initial reference time (t = 0),
D_0 is the dissolved oxygen deficit at t = 0.

Kinetic constants K_1 and K_2 are sometimes replaced by

$$\underline{k}_1\ =\ 0.434\ K_1\quad\text{and }\underline{k}_2\ =\ 0.434\ K_2$$

when exponential functions of (12.5) are replaced by power of 10 functions. Equation 12.5 is the Streeter-Phelps "oxygen sag formula" and a profile of DO along a stream is referred to as a "dissolved oxygen sag curve" (Figure 12.1). The critical point of this curve corresponds to the minimum of DO or the maximum of saturation deficit D_c, reached at critical time t_c. At this point $dD\ /\ dt\ =\ 0$, and the critical deficit is

$$D_c\ =\ \frac{K_1}{K_2}\ L\ =\ \frac{K_1}{K_2}\ L_0\ \exp\ (-K_1\ t_c) \tag{12.6}$$

and the critical time equals

$$t_c = \frac{1}{K_2 - K_1} \ \text{Ln} \ (\ \frac{K_2}{K_1} \ (\ 1 - \frac{D_0 \ (K_2 - K_1)}{L_0 \ K_1}) \ ) \tag{12.7}$$
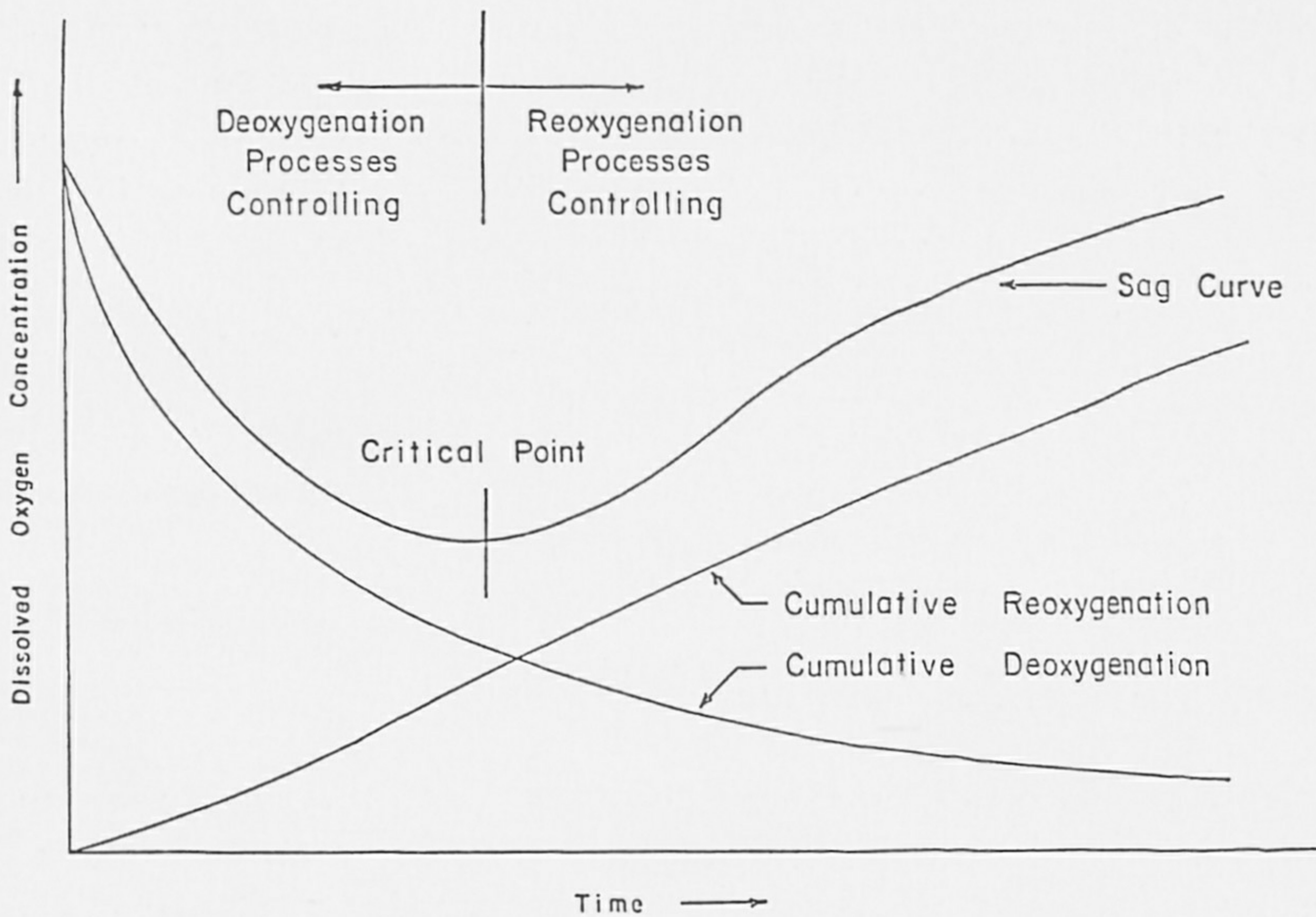
CLASSICAL OXYGEN SAG CURVE WITH DEOXYGENATION AND REOXYGENATION

Fig. 12.1: Dissolved oxygen sag curve using first-order kinetics. After Gates (1971).

Equations 12.6 and 12.7 are sometimes simplified, using the Fair coefficient $f = K_2 / K_1$, also called the self-purification factor:

$$t_c = \frac{1}{K_1 \ (f - 1)} \ \text{Ln} \ (\ f \ (\ 1 - (f - 1) \ \frac{D_0}{L_0}) \ ) \tag{12.8}$$

$$D_c = \frac{L_0}{f} \ (f \ (1 - (f - 1) \ \frac{D_0}{L_0}) \ )^{1/(1-f)} \tag{12.9}$$

Arababi et al. (1974, 1975) have given a linear approximation of D_c in relation to the initial oxygen deficit and pollution load

$$D_c = R \, L_0 + A \, D_0 \tag{12.10}$$

with

$$R = f^{f/(1-f)} \quad \text{and} \quad A = 1 - f^{1/(1-f)}$$

this approximation, better than 6.2%, being very usefull for water quality assessment studies.

Besides the two previously mentioned assumptions, the Streeter-Phelps model is based on a constant pollution load discharged at a single given point along a stream having a constant flow rate Q and uniform cross section. The lateral and vertical DO and BOD concentrations are assumed uniform throughout any cross section. Within lakes and reservoirs such assumptions are obviously erroneous. Water stratification, related to temperature gradients, play frequently a prominent role in lake water quality models. Thus equations 12.4 to 12.9 are mainly used for stream water quality models.

Since 1925 when the Streeter-Phelps kinetic model was presented, numerous modifications and improvements have been incorporated without changing the first-order kinetic basic assumptions.

Nitrogeneous compounds biodegradation.

When BOD tests are performed with waste water samples containing nitrogeneous compounds such as organic nitrogen (amines, amides, proteins) or ammonium salts, oxygen evolution curves, recorded on Sapromat or respiration equipments, frequently present two steps (Figure 12.2). The second step, significant after 7-10 days, is attributed to nitrogen containing compound from microbial decomposition, i.e. organic nitrogen mineralisation and ammonium nitrification.
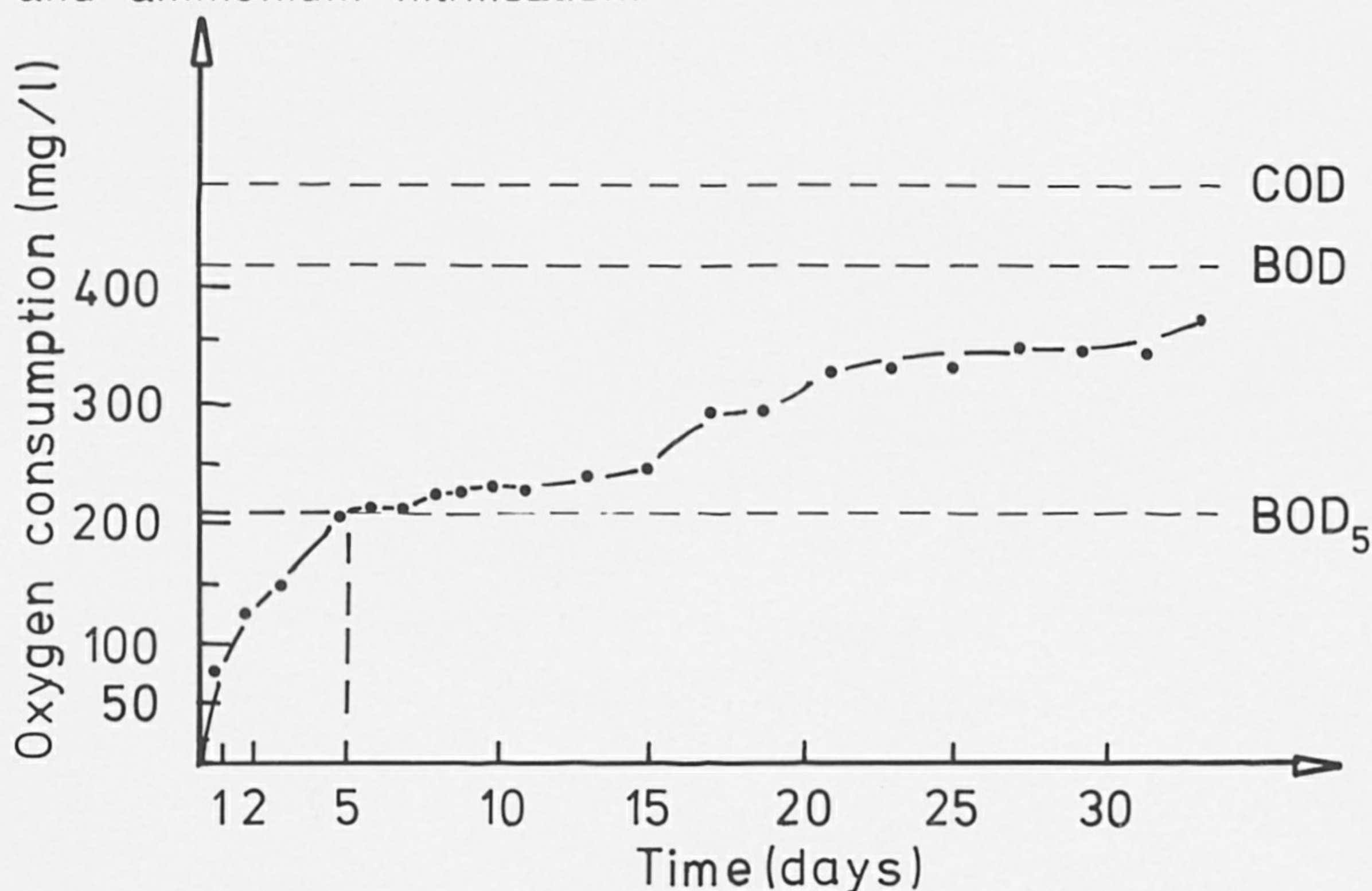

Fig. 12.2: Oxygen consumption of a waste water sample during a BOD test. After Wilderer et al. (1970).

As microbial decomposition of nitrogen-containing compounds is known to occur more slowly than carbonaceous biodegradation, the Streeter-Phelps kinetic models may incorporate in OM and DO uptake kinetic equations 12.1 and 12.2 specific terms for each form of nitrogen (O'Connor and Di Toro, 1970; Shelton et al., 1978):

$$d \, (\, NH_4\text{-}N \,) \, / \, dt \; = \; K_{1,NH_4} \, (\, NH_4\text{-}N \,) \qquad (12.11)$$

$$d \, (\, NO_2\text{-}N \,) \, / \, dt \; = \; K_{1,NO_2} \, (\, NO_2\text{-}N \,) \qquad (12.12)$$

$$dD/dt = K_1 \, L + 4.57 \, K_{1,NH_4} \, (NH_4\text{-}N) + 1.14 \, K_{1,NO_2} \, (NO_2\text{-}N) - K_2 \, D \qquad (12.13)$$

the numerical factors 4.57 and 1.14 being equal to the number of grams of oxygen necessary for the transformation of 1 g of NH_4-N or NO_2-N into nitrate. In equation 12.13 L relates to carbonaceous OM and is usually estimated by BOD_5.

When such models have been applied to OM and DO variations in stream water, first-order kinetic constants were found to vary significantly from stream quality: K_1 ranges between 0.09 and 0.64 day^{-1} (the lowest values being obtained in non-polluted rivers) (Eckenfelder, 1970; Hung et al., 1978) and $K_{1,NH4}$ ranges between 0.07 and 0.14 day^{-1} (Lefort, 1971). In fact when values of DO, OM, NH_4-N and NO_2-N are measured along a stream section of homogeneous properties at initial and 't' time, K_1, K_2, $K_{1,NH4}$ and $K_{1,NO2}$ are determined from best fit of the data (Rinaldi and Soncini-Sessa, 1977).

Besides this specific introduction of nitrogenous compound biodegradation, the Streeter-Phelps kinetic model has received several sets of modifications and improvements which nevertheless do not change its first-order character.

Dispersion and transport.

O'Connor (1961, 1962, 1967) introduced Fick's diffusion law in BOD and DO profiles:

$$\frac{dL}{dt} + \frac{v \, dL}{dx} - \frac{E \, d^2 L}{dx^2} \; = \; - K_1 \, L \qquad (12.14)$$

$$\frac{dC}{dt} + \frac{v \, dC}{dx} - \frac{E \, d^2 C}{dx^2} \; = \; - K_1 \, L + K_2 \, (C_s - C) \qquad (12.15)$$

where
v   is the stream velocity $(L\ T^{-1})$
E   is the turbulent transport (longitudal mixing) coefficient $(L^2\ T^{-1})$

Sediments

Dobbins (1964) introduced the BOD removal by sedimentation and/or adsorption with a first-order kinetic constant $K_{1,s}$ and the removal of DO by benthic processes and by plant respiration/photosynthesis:

$$\frac{dL}{dt} + \frac{v\ dL}{dx} - \frac{E\ d^2 L}{dx^2} = -(K_1 + K_{1,s})\ L \qquad (12.16)$$

$$\frac{dC}{dt} + \frac{v\ dC}{dx} - \frac{E\ d^2 C}{dx^2} = -K_1 L + K_2 (C_s - C) - D_b \qquad (12.17)$$

where
$K_{1,s}$ is the kinetic constant of BOD evolution on sediments (T^{-1})
D_b is the rate of removal of DO caused by benthic demand and plants
     $(M\ L^{-3}\ T^{-1})$

The water exertion rate of BOD in streams, including all sinks such as sediments, is usually refered to as $K_{1,r}$. Thus one may replace in equation (12.16) $K_1 + K_{1,s}$ by $K_{1,r}$ if other terms such as resuspension or volatilisation of OM are neglected.

Photosynthesis and respiration

O'Connor and Di Toro (1970) adjusted the temporal form of the photosynthetic oxygen source in streams by a half-cycle sine wave. The daily rate of photosynthetic oxygen production P as a function of time was expressed as:

$$P = P_m \sin(pi/s)(t - t_s)) \qquad \text{when } t_s \leq t \leq t_s + s$$
$$P = 0 \qquad\qquad\qquad \text{when } t_s + s \leq t \leq t_s + 1 \qquad (12.18)$$

where
P_m is the maximum oxygen photosynthesis, in the stream $(M\ L^{-3}\ T^{-1})$
t_s is the time, expressed as a fraction of the day, at which the source

becomes active (T)

s   is the fraction of the day during which the source is active (period of sunlight) (T).

Taking into account the benthic and algal respiration rate and the algal photosynthesis, the DO equation becomes:

$$\frac{v\,dC}{dx} - \frac{E\,d^2C}{dx^2} = -K_1 L + K_2 (C_s - C) - S - R + P \qquad (12.19)$$

where
S = a function of distance x, is the benthic respiration rate (sink)(M L^{-3} T^{-1})
R = a function of distance x, is the algal respiration rate (sink) (M L^{-3} T^{-1})
P = a function of time t and distance x, is the algal photosynthetic oxygen production rate (source) (M L^{-3} T^{-1}).

Alfi et al. (1972) have determined in situ the above mentioned S, R and P parameters by implanting cylinder containers into a stream and recording in each of them the DO evolution. These closed cylinders were either transparent (with bottom open to sediments for benthic demand or bottom closed) or black (bottom closed) to prevent K_2, S and P influence. K_2 was determined using an unconfined oxygen probe situated in the vicinity.

Thermal exchanges

To the Dobbins model, Lin et al. (1973a, b, c) introduced a third equation representing water temperature T evolution:

$$\frac{dT}{dt} - \frac{E\,d^2T}{dx^2} + \frac{v\,dT}{dx} - Q_T = 0 \qquad (12.20)$$

where Q_T represents the air-water energy transfer rate, function of air and water temperature, specific mass and calorific capacity as well as wind velocity and radiation flux (Jacquet, 1983) (see Chap. 5).

Waste water discharge

Lin et al. (1973b) introduced also a continuous discharge of wastes along the stream and modified equation (12.14):

$$\frac{dL}{dt} + \frac{v\,dL}{dx} - \frac{E\,d^2L}{dx^2} = -K_1 L + L_a \qquad (12.21)$$

where L_a is the rate of BOD release along a river length unit ($M \ L^{-4}$).

Discussion

Whatever the improvements brought to the original Streeter-Phelps kinetic equations (12.1) and (12.2), all these models suffer from the two basic assumptions mentioned above. If one summarizes microbial decomposition processes by a biomass catalysed overall reaction

$$OM + O_2 \quad \text{------} \quad products \qquad\qquad (12.22)$$
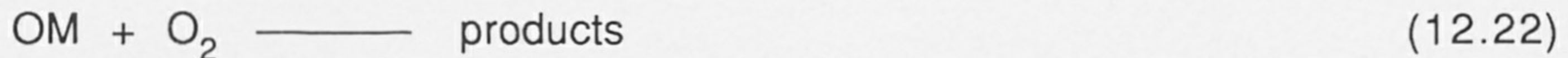
then, assuming a first-order kinetic of OM evolution means that reaction (12.22) is independent of DO and biomass concentration:. This is obviously erroneous, and in contradiction to any experimental microbial reaction kinetics. Both DO and B levels play a prominent role in aerobic biodegradation reactions (Gates, 1971; Wuhrmann, 1972; Edeline and Buet, 1978; Edeline and Lambert, 1979; Apoteker, 1981; Apoteker and Thévenot, 1983). Furthermore microbial metabolism as well as cell culture experiments demonstrate that the substrates and oxygen demands by microorganism are not proportional to but depend upon the cell development state.

As literature contains numerous reports of field studies in which the Streeter-Phelps kinetic models are used with reasonable success, there is an apparent contradiction between field and laboratory studies. Validity of experimental simulation methods for self-purification studies (Gates, 1971; Edeline and Lambert, 1974) and of cell culture kinetics does not seem to be questionable. Thus the apparent validity of first-order models may be related to the lack of precision of field determinations of concentration parameters such as C, L or T and even more dramatically to the very approximate evaluation of waste fluxes and quality, i.e. L_o and/or L_a.

Within lakes and reservoirs the main processes taken into account for water quality modelling are usually eutrophication reactions related to phosphorus and nitrogen cycles. In such systems the absence of any kinetic relation to biomass evolution is obviously erroneous. On the other hand, most stream kinetic models used in environmental assessment studies neglect eutrophication processes and biomass evolution:. Field data seem reasonably well fitted with previously mentioned Streeter-Phelps first-order kinetic models.

Zero-order kinetic models;　examples and discussion

When Seine River water DO and BOD was modelled by Lesouef (1981), it was found that, although first-order kinetic models provided a good fit above the Paris general sewage plant at Achères, below that point zero-order BOD kinetics seem to fit much better. Equation (12.13) becomes:

$$\frac{dD}{dt} = K_1 + 4.57 \, K_{1,NH4} \, (NH_4\text{-}N) - K_2 \, D \tag{12.23}$$

One should point out that for very slow biodegradation processes there is no large difference between first- and zero-order kinetics and this seems to be the case in the Seine River below Achères general sewage plant of Paris.

Furthermore, Lesouef (1979) demonstrated that the ammonium uptake first-order kinetic constant $K_{NR,NH4}$ was frequently two times larger than the ammonium oxidation (nitrification) kinetic constant $K_{1,NH4}$. Indeed ammonium uptake correspond to nitrification but also to assimilation or even ammoniac evaporation reactions. For this equations (12.11) (12.23) and (12.5) become:

$$\frac{d \, (NH_4\text{-}N)}{dt} = - K_{NR,NH4} \, (NH_4\text{-}N) \tag{12.24}$$

$$\frac{dD}{dt} = K_1 + 4.57 \, K_{1,NH4} \, (NH_4\text{-}N)_o \, \exp(-K_{NR,NH4} \, t) - K_2 \, D \tag{12.25}$$

$$D_t = \frac{4.51 \, K_{1,NH4\text{-}N} \, (NH_4\text{-}N)_o}{K_2 - K_{NR,NH4\text{-}N}} \, (\exp(-K_{NR,NH4\text{-}N} \, t) - \exp(-K_2 \, t))$$

$$+ \, \frac{K_1}{K_2} \, (1 - \exp(-K_2 \, t)) + D_o \, \exp(-K_2 \, t) \tag{12.26}$$

with K_1 at 20°C equal to 1.4 mg l^{-1}day^{-1} and $K_{NR,NH4}$ equal to 0.11 and 0.06 day^{-1} in spring-summer and in autumn respectively.

When first-order kinetics are used for DO, BOD and NH_4 evolution, as well as for ammonium nitrification, equations (12.23), (12.25) and (12.26) become:

$$\frac{dD}{dt} = K_1 L + 4.57 K_{1,NH4} (NH_4\text{-}N) - K_2 D \tag{12.27}$$

$$\frac{dD}{dt} = K_1 L_o \exp(-K_1 t) + 4.57 K_{1,NH4} (NH_4\text{-}N)_o \exp(-K_{NR,NH4} t) - K_2 D \tag{12.28}$$

$$D_t = \frac{4.51 K_{1,NH4\text{-}N} (NH_4\text{-}N)_o}{K_2 - K_{NR,NH4\text{-}N}} (\exp(-K_{NR,NH4\text{-}N} t) - \exp(-K_2 t))$$

$$+ \frac{K_1 L_o}{K_2 - K_1} (\exp(-K_1 t) - \exp(-K_2 t)) + D_o \exp(-K_2 t) \tag{12.29}$$

with K_1 ranging between 0.4 and 0.6 day^{-1}.

Such zero-order kinetic models for DO evolution in highly polluted streams seem to be only related to attempts to fit correctly sets of field data. They are not based on chemical or microbiological kinetic assumptions.

12.3   PARAMETERS ESTIMATION

Determination of the reaeration kinetic constant K_2

Although this point has been already considered in the Chapter 3, the most recent methods of calculation of the reaeration kinetic constant K_2 will be presented here. It will also be assumed that the reoxygenation will occur at the interface air-water and follow a first order kinetic law:

$$\frac{dR_o}{dt} = K_2 (C_s - C) \tag{12.30}$$

where
dR$_o$/dt   is the rate of reoxygenation (M L^{-3} T^{-1})
C_s is the concentration of oxygen at saturation (M L^{-3})
C   is the concentration of oxygen in the river (M L^{-3})
K_2 is the reaeration kinetic constant (T^{-1}).

The reaeration kinetic constant is influenced by many factors. The most important to be considered are: (see Chapter 3 for further details)

a. the water temperature T
b. the river flow characteristics (flow velocity v, depth of the river H)
c. the meteorological characteristics (air temperature and wind velocity)

a. The water-temperature T dependence of the reaeration coeffient K_2 is usually assumed to follow an Arrhenius-type law:

$$K_2 = (K_2)_{20} \; theta^{(T-20)} \tag{12.31}$$

where

T is the temperature of the water (°C),

$(K_2)_{20}$ is the value of K_2 at 20°C (T^{-1}), and

theta is a dimensionless parameter varying from 1.008 (Truesdale et al., 1958) to 1.046 (Streeter et al., 1936).

b. The influence of two parameters characteristic of the river flow (stream velocity and depth) on K_2 was investigated by Covar, 1976.

A graph has been plotted of the data collected by O'Connors et al. (1958; Churchill et al. (1968) and Owens et al. (1964), as presented in Chapter 3.

Table 12.1 presents some reaeration coefficient values for rivers and streams of different depth and velocities.

Determination of the biodegradation kinetic constant K_1

Numerous methods have been developed and used to determine the biodegradation kinetic constant rate, K_1, of the first-order Streeter-Phelps kinetic model. Three different rates can be found in the literature (Bowie et al., 1985):

K_1 water deoxygenation rate due to BOD exertion (T^{-1})

$K_{1,l}$ laboratory deoxygenation rate due to BOD exertion (T^{-1})

$K_{1,r}$ water BOD exertion rate, including all sinks (T^{-1})

The significance of these three parameters is very different and has to be taken into account when a model is built up.

Table 12.1
Reaeration coefficient K_2 for different rivers and streams. After Hydroscience (1971)

River name	Category	Depth (m)	Area (m^2)	Flow (m^3/s)	Velocity (m/s)	K_2 20°C (l/day)	Reference
Grand River (Michigan)	Shallow	0.579	29.729	8.336	0.280	4.500	O'Connor et al. (1970)
Clinton River (Michigan)	Shallow	0.482	4.143	0.909	0.219	5.900	O'Connor et al. (1970)
Truckee River (Nevada)	Shallow	0.509	13.935	7.688	0.552	6.600	O'Connor et al. (1970)
Jackson River (Virginia)	Shallow	0.914	33.910	2.791	0.082	4.100	Hydroscience (1967)
Ivel River (GB)	Shallow	0.369	3.200	0.138	0.043	2.350	Owens et al. (1962)
Mohawk River (New York)	Inter-mediate	4.572	353.032	22.597	0.064	0.07-4.0	O'Connor et al. (1968)
New River (Virginia)	Inter-mediate	1.524	159.793	34.093	0.213	1.040	Hydroscience (1966)
Clinch River (T.V.)	Inter-mediate	2.185	208.594	167.918	0.805	1.130	Churchill et al. (1962)
Holston (T.V.)	Inter-mediate	3.478	330.416	294.070	0.890	0.280	Churchill et al. (1962)
Wautasa (T.V.)	Inter-mediate	1.042	57.82	88.122	1.524	5.600	Churchill et al. (1962)
Ohio River	Deep	9.754	3994.831	170.467	0.043	0.060	Streeter et al. (1925)
Upper Hudson	Deep	6.401	627.096	286.708	0.457	0.165	Hydroscience (1965)
Upper James	Deep	4.724	1393.546	55.218	0.040	0.220	Hydroscience (1964)

The $K_{1,r}$ coefficient includes all sinks of BOD and especially the physical processes like sedimentation, floculation, resuspension and mixing, and special chemical processes like volatilization. Thus the use of $K_{1,r}$, or of K_1, in the model depends only on the system analysis of the system which is modelled. If just BOD and DO are taken into account, then $K_{1,r}$ has to be used; if the model deals specifically with nitrogen-containing species, then K_1 is prefered.

Relation between K_1 and $K_{1,l}$

The difference between $K_{1,l}$ and K_1 is related to the difference of flow characteristics in the river and in a BOD bottle. Many relations have been developed between these parameters. We will present two of these methods.

The first one (Nejedly, 1973) relates $K_{1,l}$ and K_1 to the longitudinal dispersion coefficient, E, of the river. Indeed, the dispersion increases significantly the rate of BOD exertion. Thus for a given temperature, the following relation is used:

$$K_1 = K_{1,l}\, a^{E*b} \tag{12.32}$$

where
a and b are adjustable dimensionless parameters
E is the longitudinal dispersion ($L^2\,T^{-1}$)
E can be calculated with empirical relations or determined experimentally on
   the river (using dyes such as rhodamine, for example).

The second formulation (Bosko, 1966; Novtony, 1969) replaces in equation (12.32) the multiplicative correction by an additive one. Thus the BOD exertion is more activated by the river, but caused partially by the river itself.

$$K_1 = K_{1,l} + A \tag{12.33}$$

where A is a kinetic coefficient describing absorption by biological slimes attached to a solid bottom or by dispersed biological flocs (Velz et al., 1962). Bosko proposed for coefficient A:

$$A = n\,(v/H) \tag{12.34}$$

where
v is the river velocity ($L\,T^{-1}$),
H is the river depth (L), and
n is a dimensionless coefficient of bed activity.
The last mentioned coefficient takes into account hydraulic parameters and chemical properties of the bed of the river. It is taken as a step function of the slope of the bed of the river (Table 12.2).

An alternative relation between coefficient A and stream flow characteristics was proposed by Novtony (1969):

$$A = w * \frac{S_e^{1/6}}{H^{0.75}} \qquad (12.35)$$

where

w   is a coefficient varying from 0.1 (streams with moving bottoms)   to 3.0
    (rocky streams)
S_e is the slope of the river (m/km).

Table 12.2
Stream slope dependance of coefficient of bed activity n.   After
Bowie et al. (1985) K_1 = $K_{1,l}$ + n (v/H)

Slope of the river (km/m)	1.22	2.45	4.90	12.26
n	0.10	0.15	0.25	0.40

Novotny et al. (1975)   compared equations (12.34) and (12.35) for different types of rivers, assuming that K_1 took into account a benthal oxygen demand (Table 12.3).

Two possibilities are available for determining a biodegradation kinetic constant: either calculate $K_{1,l}$ through laboratory experiment and evaluate K_1 with one of the previously mentioned equations (12.34) or (12.35), or calculate directly K_1 with a numerical optimisation technique or an statistical-experimental law.

Table 12.3
Comparison of experimental and calculated values of the A coeff-icient, according to Bosco and Novotny, for Holston River, Tenessee.   After Novotny et al. (1974)

Character of bottom	Velocity (m/s)	Depth (m)	Slope (m/km)	A Bosko	A Novotny	Measured K_1-$K_{1,l}$
Gravel	0.19	0.76	0.62	0.30	1.08	1.0
Sand	0.13	0.76	0.62	0.10	0.43	0.25
Grav. rock	0.52	0.58	0.50	1.34	1.90	2.12
Grav. rock	0.32	0.73	0.80	0.65	1.79	1.60
Grav. rock	0.29	0.73	0.234	0.59	1.34	1.14
Grav. low poll.	0.42	0.70	0.234	0.41	0.55	0.55
Grav. low poll.	0.27	1.86	0.234	0.12	0.22	0.15

Calculation of $K_{1,l}$

a. Experimental study of BOD exertion.

The results of a BOD test in standard conditions (see paragraph 12.2) provides a DO versus time curve similar to that presented in Figure 12.2 (Wilderer et al., 1970). This curve frequently presents two plateaus, the first between 5 and 15 days, and the second one after 25 days. The first step with a quite marked slope corresponds to the carbonaceous degradation while the second corresponds to the nitrification stage of the biochemical degradation. Thus we see that the hypothesis of a first order reaction with a constant parameter $K_{1,l}$ is really an approximation. However, a first-order kinetic may be reasonably fitted during the first step of the experiment (before the curve reaches the first plateau): $K_{1,l}$ can be determined following DO uptake during 5 or 7 days, this last value being frequently preferred for practical considerations.

b. Graphical and mathematical procedures for determining $K_{1,l}$.

Before the general use of computers - before c.1965 - many authors developed graphical methods to determine the constant K_1. These all suppose that the biodegradation follows the first-order Streeter-Phelps kinetic law:

$$C_o - C_t = L_o (1 - exp(K_{1,l} * t))$$ (12.36)

where
$C_o - C_t$ is the oxygen consumption at time t (M L^{-3})
L_o is the ultimate BOD at time zero (M L^{-3})

Hewitt et al. (1975) compared seven of these methods with 20 sets of data (Table 12.4). It is beyond the scope of this book to detail all of these methods, which have now been overtaken by other methods. The different approaches used by each author depend on the limitations inherent in the local conditions of the study (Bansal, 1975). The variation of the results lies between 0 and 50% depending to the method. However, according to Marske et al. (1972) who compared four of the previous methods, the Reed-Theriault method seems to give the best results.

Table 12.14

Graphical and mathematical K₁ procedures compared by Hewitt et al. (1975)

Name of the author	Name of the method	Date	Formulation
Reed & Theriault	Theriault	1927-31	integral
Fair	Log-differences	1936	integral
Thomas	Slope	1937	differential
Rhame	Two point	1957	integral
Sheehy	Slide Rule	1960	integral
Moore	Moments	1960	integral
Navone	Simplified slope	1960	differential

c. Numerical methods for determining $K_{1,l}$.

The advent of the computer now allows the use of numerical optimization techniques for determining $K_{1,l}$. More efficient than the graphical techniques, these methods allow checking of the validity of the results through confidence contour determination, for example. The most used method is a modified least-square method for non-linear problems (Marske et al., 1972; Berthouex, 1971; Balland, 1982). In the following, we note:

$(C_o - C_t)_{obs}$ the observed value of DO consumed at time t,

$\underline{L}$ the calculated value of BOD exerted at time t, with the relation $\underline{L} = L_o (1 - \exp(K_{1,l} * t))$,

$S = sigma ((C_o - C_t)_{obs} - \underline{L})$, over 1 the number of observations.

Because of the non-linearity of the problem a search is conducted with an iterative algorithm for L_o and $K_{1,l}$ which minimize S. If S remains high even when these L_o and $K_{1,l}$ values represnet the best fit for the observed data - calculated data, the first-order law does not represent the observed phenomena well. The confidence contour around the best estimate are those for which $S(L_o, K_{1,l})$ = constant. Although this problem is non-linear, a confidence level: 100 (1 - q) % associated to a confidence contour can be defined:

$$S_q = S(L_o, K_{1,l})(1 + (p/l-p) F(p,l-p,1-q)) \qquad (12.37)$$

with p the number of parameters for the model,

1 the number of observations
q the confidence level

For p = 2; $F(2, 1-2, 1-q) = I-2/2 (q^{-2/I-2} - 1)$ (12.38)
$S_q = S(L_o \text{ and } K_{1,I}) * q^{-2/I-2}$ (12.39)

Since this method gives the best parameters $K_{1,I}$ and L_o or $K_{1,I}$ and BOD_5 for each sample, it is possible to improve it and then to simplify the $K_{1,I}$ calculation, searching a regression relation between the two parameters (linear or log-log). Thus with this relation, valid at a certain location, it becomes possible to calculate $K_{1,I}$ with a simple measure of BOD_5 (Balland, 1982).

Marske et al. (1972) compared this technique with three of the previously mentioned graphical methods, and plotted their results as the percentage of the distance from the best fit of $K_{1,I}$ vs ultimate BOD (Figure 12.3). It will be noticed that the graphical Reed-Theriault method gives as good results as the numerical least-squares method.
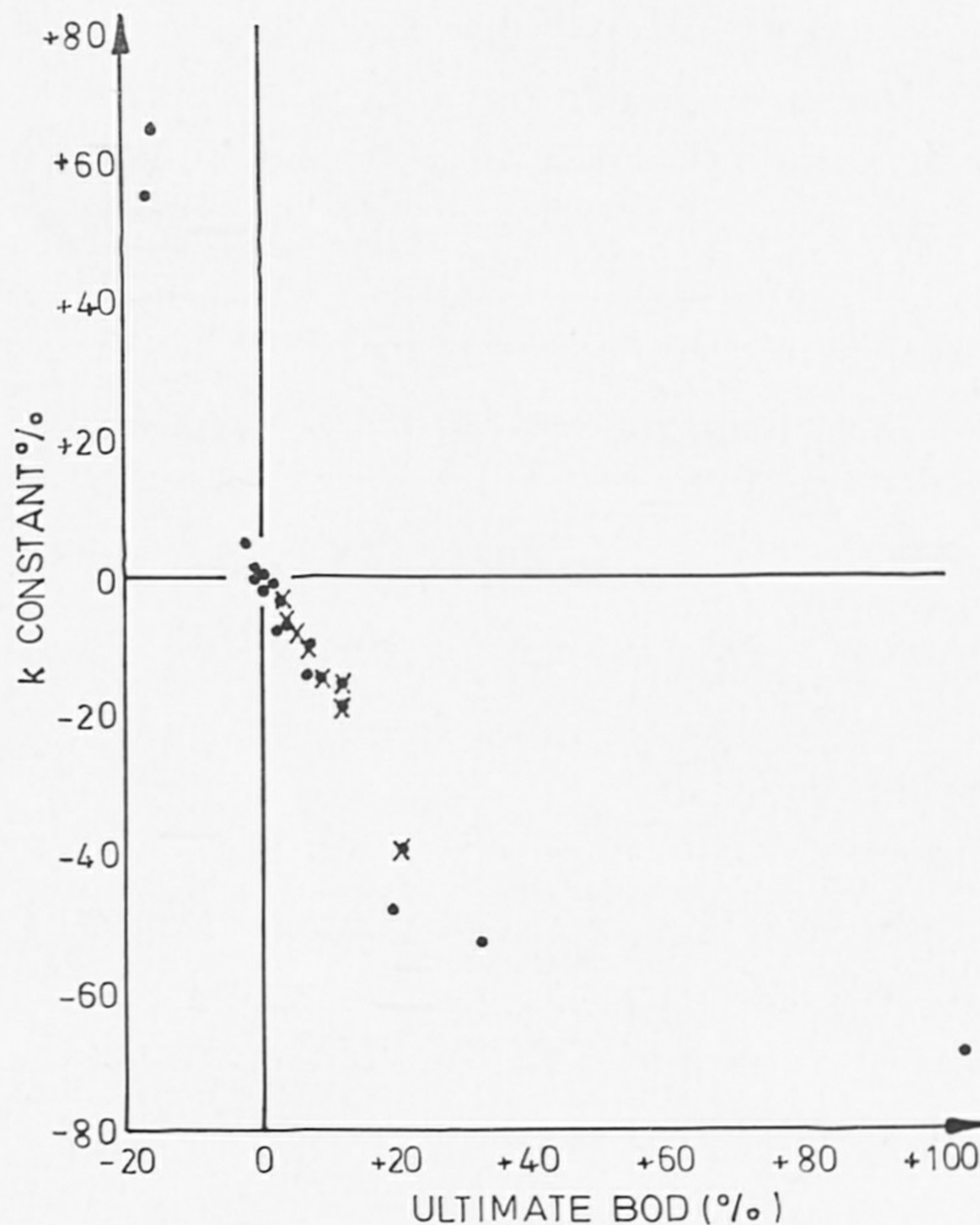

Fig. 12.3: Biodegradation kinetic constant determination: deviation from the best estimate. After Marske et al., 1972.
o: Method of Moments, x: Thomas Slope Method, •: Log-difference Method.

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d. Order of magnitude of K_1

Table 12.5 presents some deoxygenation rate constants K_1 observed for different locations and temperatures, in the United States. From these values it is clear that K_1 may vary over more than one order of magnitude.

Table 12.5
Deoxygenation rate constants K_1. After Bansal (1975)

	Discharge (m^3/s)	Section (m^2)	Top width (m)	Temperature (°C)	K_1 (base e) (l/day)
Kansas River at Bonner Springs					
	430.416	399.483	234.696	25.000	0.020
	61.164	111.464	153.924	28.000	0.120
Kansas River at Topeke	86.083	134.709	142.646	22.000	0.080
	76.172	119.380	142.037	18.000	0.370
Big Blue River at Tuttle Creek	30.016	97.548	59.131	22.000	0.210
	27.212	92.903	59.131	8.000	0.600
Republican River below Milford	7.306	17.094	59.741	24.000	0.180
	17.243	36.418	75.795	24.000	0.070
Smoky Hill River at Enterprise	10.562	19.603	39.929	24.000	0.160
	4.446	8.175	29.566	14.000	0.240
Flint River. Michigan	3.794	19.510	30.480	20.000	0.560
	4.927	37.161	46.878	20.000	0.690
	4.927	18.581	23.439	2.000	0.630
Upper Hudson, Troy, New York	84.951	557.416	104.546	20.000	0.125
	127.426	627.096	97.841	20.000	0.165

Determination of K_1 or $K_{1,r}$ by direct methods

a. Statistical experimental method

The aim of this method is to determine K_1 without use of any relation between $K_{1,l}$ and K_1 . As the river flow may be characterized by Froude (Fr) and Reynolds (Re) numbers, Bansal (1975), tried to relate, on the basis of data gathered by the E.P.A., K_1 , Re and Fr. The following relation was found with a correlation coefficient of 0.93 and a standard deviation of 0.41.

$$\text{Log} (K_1 * H^2 / \text{nu}) = 3.606 + \text{Log} (Re/Fr) \tag{12.40}$$

with

$$Re = v * H / nu \qquad (12.41)$$

$$Fr = v / (g * H)^{1/2} \qquad (12.42)$$

where
nu is the kinematic viscosity coeffcient $(L^2 \, T^{-1})$
H is the depth of the river (L)
g is the acceleration of gravity $(L \, T^{-2})$

The temperature influence is included into the variation of nu with temperature. It is also possible to use this relation at 20°C and then use Arrhenius law. The major advantage of this method is its simplicity. It may be possible to use a Streeter-Phelps model with good accuracy, without any knowledge of the location of the river or the pollution. This is very useful for fast diagnosis of the biodegradation in a river.

b.   Determination of K_1 or $K_{1,r}$ with manual or automatic calibration

These methods are no longer based on laboratory BOD test. Now the computer is considered as a numerical laboratory and after seting the model description   (simple with Streeter-Phelps first-order kinetics), parameter values are determined for achieving the best fit between the observed and calculated data along the river.   The fact that either K_1 or $K_{1,r}$ are determined depends on the previous analysis of the system which is being modelled.   If just the BOD exertion is taken into account, then K_1 will be found.   If BOD exertion and $N-NH_4^+$ nitrification in water and on the sediments, and the respiration and photosynthesis are taken into account, then $K_{1,r}$ will be found.

b.1   Manual methods

The simplest way, for a simple Streeter-Phelps model, with just two parameters, is to simulate the behaviour of the river for different sets of parameters until a good adjustment between experimental and simulated values is observed   (Lesouef, 1980).   Although this method is especially rough, it can be very helpfull and it provides good results if the model remains simple.

b.2   Numerical methods

If the model is a more complicated one, the difficulty of manual parameter estimation increases. The only way which can be used is an auto-matic calibration procedure.   Two strategies are available for a numerical calculation of the estimate   (Rinaldi et al., 1980):   the recursive and the

accumulative estimation. Accumulative procedures are designed for calculating estimates from a fixed set of data, while recursive schemes are suited for estimates which are to be updated as new information becomes available. While the first method is used when the parameters are not supposed to vary in time, the second one is very usefull for real time state estimation. Since BOD measurements need a minimum of 5 days, the utilization of such a method in biodegradation remains rare.

b.2.1   Accumulative procedures

These procedures are based on an error estimator function to minimize , for example, a least squares estimator. Various numerical methods are available to solve a minimization problem, such as the *quasi-linearization* technique (Stehfest, 1973), which has the advantage of a fast convergence rate. These accumulative techniques are now much used (Shastry et al., 1973; Rinaldi, 1979; Radhakrishnan et al., 1974), and allow the building of sophisticated models with many parameters. After a successful calibration the set of parameters found has to be validated on another set of data.

b.2.2   Recursive procedures

The recursive procedures are based on stochastic mechanistic models. The problem is to determine the state estimation for the time interval, t_s, from the input - output measurement for the previous intervals $(0 < t < t_s)$.

Parameter estimation can be done with the well known numerical technique of Kalman filtering, or another method which appears to provide an improvement in statistical efficiency - the multivariate extension of the Instrumental Variable Approximate Maximum Likehood (IVAML) method of time series analysis (Whitehead et al., 1979). This procedure has been successfully applied to the real-time monitoring scheme of the River Ouse at Bedford on a modified Streeter-Phelps model (DO, $N-NH_4^+$) (Whitehead, 1983).

12.4   FUTURE RESEARCH NEEDS

Difficulties encountered in modelling microbial decomposition of organic matter are possibilities of descriptive or interpretative mathematical models and relation between the model structure and its applications.

Experimental and field research needs for microbial decomposition models: differences between intrinsic parameters and parameters fitted from field data, difficulties arising from non-linear kinetics.

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NOTATIONS

A   is an additional coefficient describing the augmentation of $K_{1,l}$ in natural sites (T^{-1})

ATP   adenosine triphosphate

B   biomass concentration $(M\ L^{-3})$

BOD   biochemical oxygen demand $(M\ L^{-3})$

C   dissolved oxygen concentration $(M\ L^{-3})$

C_s saturated dissolved oxygen concentration $(M\ L^{-3})$

COD   chemical oxygen demand $(M\ L^{-3})$

D   dissolved oxygen deficit, i.e. $C_s - C$ $(M\ L^{-3})$

D_b rate of removal of DO caused by benthic demand and plants $(M\ L^{-3})$

D_c critical dissolved oxygen deficit, i.e. maximum of D $(M\ L^{-3})$

DNA   deoxyribonucleic acid

DO   dissolved oxygen

dR_o/dt rate of reoxygenation $(M\ L^{-3}\ T^{-1})$

E   turbulent transport (longitudinal mixing) coefficient $(L^2\ T^{-1})$

F   source or drain of organic pollutant $(M\ L^{-3})$

Fr   Froude number (dimensionless)

f   Fair coefficient, also called self-purification factor, i.e. K_2 / K_1 (dimensionless)

g   acceleration of gravity $(L\ T^{-2})$

H   depth (L)

K_1 biodegradation kinetic constant in first-order kinetic models, i.e. water deoxygenation rate due to BOD exertion (T^{-1})

$K_{1,l}$ laboratory deoxygenation rate due to BOD exertion (T^{-1})

$K_{1,r}$ water exertion rate of BOD, includes all sinks of BOD (T^{-1})

$K_{1,s}$ kinetic constant of BOD evolution on sediments (T^{-1})

$K_{1,NH4}$ ammonia biodegradation (oxidation) kinetic constant in first-order nitrification kinetic models (T^{-1})

$K_{NR,NH4}$ ammonium uptake kinetic constant in first-order kinetic models (T^{-1})

$K_{1,NO2}$ nitrite biodegradation (oxidation) kinetic constant in first-order

	kinetic models (T^{-1})
K_2	oxygen transfer kinetic constant, also called reaeration kinetic constant (T^{-1})
$(K_2)_{20}$	value of K_2 at 20°C (T^{-1})
L	concentration of organic matter, generally expressed in ultimate BOD and frequently related to carbonaceous compounds $(M\ L^{-3})$
L_o	initial value of ultimate BOD $(M\ L^{-3})$
L_a	rate of BOD release along a river length unit $(M\ L^{-4})$
I	number of observations (dimensionless)
NH_4-N	ammonium nitrogen concentration $(M\ L^{-3})$
NO_2-N	nitrite nitrogen concentration $(M\ L^{-3})$
n	coefficient of bed activity (Bosko, 1966) (dimensionless)
OM	organic matter
P	algal photosynthetic oxygen production rate (source) $(M\ L^{-3}\ T^{-1})$
P_m	maximum algal photosynthetic oxygen production rate (source) $(M\ L^{-3}\ T^{-1})$
P	number of parameters of the model
Q	flow rate (downstream) $(L^3\ T^{-1})$
Q_T	thermal air-water energy transfer rate
q	confidence level
R	algal respiration rate (oxygen sink) $(M\ L^{-3}\ T^{-1})$
Re	Reynolds number (dimensionless)
S	benthic respiration rate (oxygen sink) $(M\ L^{-3}\ T^{-1})$
S_e	slope of the river (dimensionless or m/km)
s	period of sunlight, i.e. fraction of the day at which photosynthesis is active (T)
T	temperature of the water (°C)
t	time (T)
t_s	time, expressed as a fraction of the day, at which oxygen photosynthesis becomes active (T)
TOC	total organic carbon $(M\ L^{-3})$
TOD	total oxygen demand $(M\ L^{-3})$
V	volume (L^3)
v	velocity (downstream) $(L\ T^{-1})$
w	coefficient of bed activity (Novotny, 1969)
x	distance (downstream) (L)
Y	biomass yield from organic matter (dimensionless)
mu	bacterial growth rate (T^{-1})
mu_M	maximal growth rate (T^{-1})
nu	kinematic viscosity coefficient $(L^2\ T^{-1})$
ro	water specific mass $(M\ L^{-3})$

pi   3.1416

theta   temperature coefficient of K_1 (dimensionless)

phi   temperature coefficient of K_2 (dimensionless)

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