

Robust Control Design of an Electro-Hydraulic Actuator

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Abstract—The paper proposes a hierarchical control design of an electro-hydraulic actuator. The high-level hydromotor is modeled with a linear form with parametric uncertainty, while the low-level spool valve is modeled with a polynomial system. The subsystems require different control strategies. At the high level a robust \mathcal{H}_∞/μ control is used in order to meet the performance specifications. At the low level a Control Lyapunov Function-based algorithm is proposed, which calculates discrete control input values for the valve. The interaction between the two control systems is guaranteed by the spool displacement, which is the control input at the high level and must be tracked at the low level. The operation of the actuator control system is illustrated through a simulation example.

I. INTRODUCTION AND MOTIVATION

Hydraulic actuators are used in several engineering applications, therefore, developing advanced control methods for these systems is relevant. One of these applications is active anti-roll bars, which enhance the roll stability of vehicles.

The literature of hydraulic control systems is very extensive. The robotic applications of the commonly-used electronically-controlled actuators, such as electromagnetic motors, hydraulic, pneumatic and piezoelectric actuators were detailed and compared, see e.g., [1]. A nonlinear PID controller for a hydraulic positioning system was proposed by [2]. A velocity tracking robust PID control of an hydraulic cylinder based on linear model with parameter uncertainties was published in [3]. A sliding control to deal with a highly nonlinear model was proposed by [4]. In [5] and [6] a robust low-order control design of an electro-hydraulic cylinder was presented and analyzed on a test bed. In [7] a feedback control scheme for motion control of nonlinear high-order systems was proposed. A Fuzzy control was also proposed for the design of a hydraulic cylinder, see [8].

The paper focuses on an electro-hydraulic actuator, i.e., an oscillating hydromotor and a spool valve. The oscillating hydromotor is a rotary actuator with two cells, which are separated by vanes. The pressure difference between the vanes generates a torque on the central shaft, which has a limited rotation angle. The hydromotor is connected to a symmetric 4/2 four-way valve and the spool is controlled by a solenoid valve. The spool has a limited distance to travel and the input current can only take discrete values. Since the presented system has a high energy density, it requires small space and it has low mass. Besides, the actuator has a simple construction, but it requires an external high-pressure pump [9].

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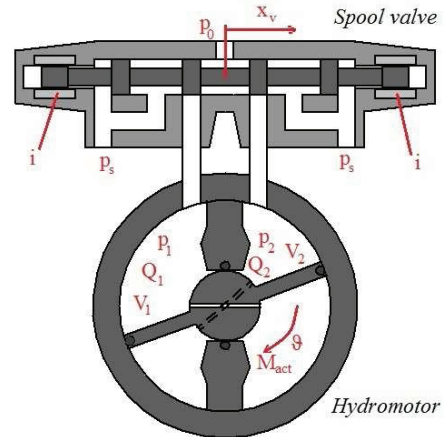


Fig. 1. Oscillating hydromotor actuator

The control-oriented model of the actuator is separated into two subsystems. The high-level hydromotor is modeled with a linear form with parametric uncertainty, while the low-level spool valve is modeled with a polynomial system. The subsystems require different control strategies. At the high level a robust \mathcal{H}_∞/μ control is used in order to meet the performance specifications. At the low level a Control Lyapunov Function-based algorithm is proposed, which calculates discrete control input values for the valve. The interaction between the two control systems is guaranteed by the spool displacement, which is the control input at the high level and must be tracked at the low level.

The paper is organized as follows. Section II presents the control-oriented hydromotor and valve models. Section III proposes the control design of the spool valve. Section IV presents the hierarchical control structure and proposes the design of the robust control of the hydromotor. Section V illustrates the operation of the multi-level control system through a simulation example. Finally, Section VI gives some concluding remarks.

II. MODELING THE ELECTRO-HYDRAULIC ACTUATOR

A. Modeling the hydromotor

In the following the control-oriented modeling of the hydromotor is proposed. The output of the system is the actuator torque M_{act} , which improves the roll dynamics of the vehicle. The input of the system is the electromagnetic valve motion x_v . The illustration of the hydromotor construction is found in Figure 1.

The pressures in the chambers depend on the flows of the circuits Q_1 , Q_2 . p_L is the load pressure difference between

the two chambers. The average flow of the system, assuming the supply pressure p_s is constant, is as follows:

$$Q_L(x_v, p_L) = C_d A(x_v) \sqrt{\frac{1}{\rho} (p_s - \frac{x_v}{|x_v|} p_L)} \quad (1)$$

This equation can be linearized around $(x_{v,0}; p_{L,0})$ such as

$$Q_L = K_q x_v - K_c p_L \quad (2)$$

where K_q is the valve flow gain coefficient and K_c is the valve pressure coefficient, see [9]. In this modeling principle, the hydromotor model does not take into account the friction force and the external leakage flow. The compressibility of the fluid is function of the system pressure and the percentage of air trapped in the system. The volumetric flow in the chambers is formed as

$$\dot{p}_L = \frac{4\beta_E}{V_t} (Q_L - V_p \dot{\varphi} + c_{l1} \dot{\varphi} - c_{l2} p_L) \quad (3)$$

where β_E is the effective bulk modulus, V_t is the total volume under pressure and V_p is proportional to the areas of vane cross-sections. c_{l1} and c_{l2} are parameters of the leakage flow.

The motion equation of the shaft rotation $\dot{\varphi}$ due p_L and the external load M_{dist} can be written as follows:

$$J\ddot{\varphi} = -d_a \dot{\varphi} + V_p p_L + M_{dist} \quad (4)$$

where J is the mass of the hydromotor shaft and vanes, d_a is the damping constant of the system. The actuator torque M_{act} is written as:

$$M_{act} = 2A_v \frac{d_e}{2} p_L \quad (5)$$

with A_v being the area of the vanes and d_e is the effective diameter of the vanes.

Using (3) and (4) the state-space representation of the hydromotor is formed as:

$$\dot{x}_{HM} = A_{HM} x_{HM} + B_{1HM} w + B_{2HM} u \quad (6)$$

where the state vector is $x_{HM} = [p_L, \dot{\varphi}, \varphi]^T$.

B. Modeling the electromagnetic valve

The electronically controlled spool valve is modeled in a polynomial form, which creates dependence between current i and spool displacement x_v . The motion equation of the valve is written as follows:

$$\frac{1}{\omega_v^2} \ddot{x}_v + \frac{2D_v}{\omega_v} \dot{x}_v + x_v = k_v \omega_v^2 i \quad (7)$$

where k_v valve gain equals

$$k_v = \frac{Q_N}{\sqrt{\Delta p_N/2}} \frac{1}{u_{vmax}}. \quad (8)$$

Q_N is the rated flow at rated pressure and maximum input current, p_N is the pressure drop at rated flow and u_{vmax} is the maximum rated current. D_v is the valve damping coefficient, which can be calculated from the apparent damping ratio. ω_v stands for the natural frequency of the valve [8]. Let $K_f = \omega_v^2$, which is a spring-stiffness-like parameter. In the model the nonlinear friction of the valve is neglected.

The flow force stiffness of the system for control purposes is approximated as [9]

$$K_f(x_v) \approx 0.43(p_s - p_L) \cdot w(x_v) \quad (9)$$

where w is the area ratio depending on x_v . The stiffness K_f has a maximum value at $x_v = 0$, while at large valve displacement

$$\lim_{|x_v| \rightarrow \infty} K_f(x_v) = 0. \quad (10)$$

The illustration of K_f is shown in Figure 2 (nonlinear complex model). However, it is necessary to consider that the spool valve displacement is limited due to physical constraints ($x_{v,max} = \pm 0.01m$). Therefore, at $x_{v,max}$ the parameter $K_f(x_{v,max})$ is modified to a large value. It guarantees that the valve does not cause saturation. The modified piecewise function $K_f(x_v)$ is shown in Figure 2 (Broken line saturation approximation). Although the piecewise modeling results an appropriate formulation, for control-oriented modeling purposes a polynomial approximation is used. Thus, K_f is approximated by a tenth-order polynomial of x_v on the domain $[-x_{v,max}, +x_{v,max}]$.

$$K_f(x_v) = p_{10}x_v^{10} + p_9x_v^9 + \dots + p_1x_v + p_0 \quad (11)$$

where p_i are the coefficients of the polynomial. Figure 2 also shows the polynomial approximation $K_f(x_v)$.

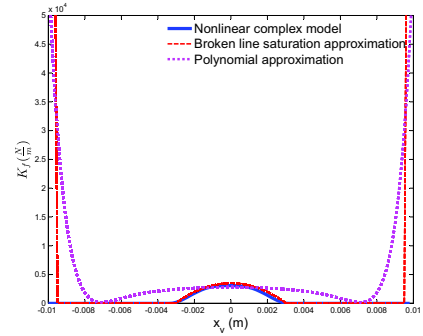


Fig. 2. Approximation of parameter K_f

Finally, the original dynamical equation (7) is transformed to the next form using (11)

$$\ddot{x}_v = -2D_v \omega_v \dot{x}_v - K_f(x_v)x_v + k_v \omega_v^2 i \quad (12)$$

III. CONTROL STRATEGY OF THE VALVE

The valve control aims to track the reference spool displacement, defined by the controller of the hydromotor. This performance must be satisfied with the shortest settling time possible. Also the control input i can only take three discrete values:

$$i = \{-i_{max}, i_0, i_{max}\}, \quad (13)$$

where $i_0 = 0$. The control strategy is based on the Control Lyapunov Function. It is used to test whether a control input is able to stabilize the system.

Definition: Let a dynamical system be given the form

$$\dot{x}(t) = f(x(t)) + g(x(t))u \quad (14)$$

where $x(t) \in \mathbb{R}^n$, $u(t) \in \mathbb{R}$ and f and g are smooth vector fields and $f(0) = 0$. A function V is a Control Lyapunov Function if $V : \mathbb{R}^n \rightarrow \mathbb{R}$ is a smooth, radially unbounded and positive definite function.

The existence of such function implies that the system is asymptotically stabilizable at the origin, see [10].

The dynamical system has a differentiable Control-Lyapunov Function if and only if there exists a regular stabilizing feedback $u(x)$. It is called Artstein's theorem.

The tracking error of the control is given as follows:

$$e = x_{v,ref} - x_v. \quad (15)$$

The derivative of this expression, assuming that the reference signal is constant for a given interval:

$$\dot{e} = -\dot{x}_v. \quad (16)$$

Define the function r and its derivative:

$$r = \dot{e} + \alpha e = -\dot{x}_v + \alpha(x_{v,ref} - x_v), \quad (17a)$$

$$\dot{r} = \ddot{e} + \alpha \dot{e} = -\ddot{x}_v - \alpha \dot{x}_v, \quad (17b)$$

where α is a positive tuning parameter. Let the Lyapunov Function be given in the form

$$V = \frac{1}{2}r^2 \quad (18)$$

This function is positive definite for every r . By deriving this function and substituting (17) the following equation is obtained:

$$\dot{V} = r\dot{r} = (-\ddot{x}_v - \alpha\dot{x}_v)(-\dot{x}_v + \alpha(x_{v,ref} - x_v)) \quad (19)$$

Substituting the first row of (12) into (19):

$$(2D_v\dot{x}_v + K_f x_v - k_v i - \alpha\dot{x}_v)(-\dot{x}_v + \alpha(x_{v,ref} - x_v)) = 0 \quad (20)$$

By performing the multiplications, formally an equation of an ellipsoid for \dot{x}_v and x_v is obtained. The solution to the equation gives the limit of the controllable regions, wherein the states of the system can exist. The equation is written as follows:

$$A_e \dot{x}_v^2 + B_e x_v^2 + C_e \dot{x}_v x_v + D_e \dot{x}_v + E_e x_v + F_e = 0 \quad (21)$$

where A_e, B_e, \dots, F_e are the coefficients of the ellipsoid which are achieved by rearranging: $A_e = \alpha - 2D_v$, $B_e = -K_f(x_2) - 2D_v\alpha + \alpha^2$, $C_e = -K_f(x_2)\alpha$, $D_e = k_v\omega_v^2 i + 2D_v\alpha x_{ref} - \alpha^2 x_{ref}$, $E_e = K_f(x_2)\alpha x_{ref} + k_v\omega_v^2 i\alpha$, $F_e = -k_v\omega_v^2 i\alpha x_{ref}$.

The parameter α must be tuned so that the system can reach the feasible states with the given control input. Note that $A_e, B_e, C_e, D_e, E_e, F_e$ are all functions of α so it has a significant effect on the shape of the set of the controllable regions. To achieve an acceptable performance, the aforementioned parameter must be selected carefully.

The states which can be stabilized by the control input are shown in Figure 3. Since the coefficients in (21) depend on the states, the ellipsoid is degenerated and opened on the \dot{x}_v , x_v plane. The reference signal $x_{v,ref}$ can only take values

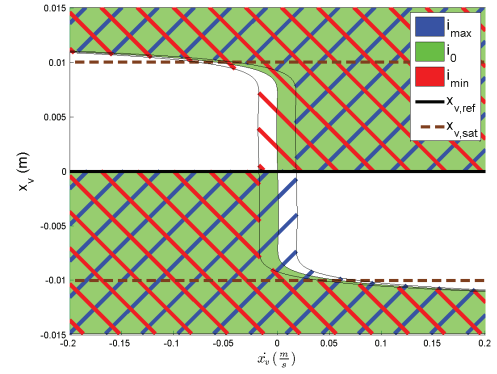


Fig. 3. Controllability regions of the discrete control inputs ($x_{v,ref} = 0m$)

between $\pm x_{v,sat}$, which represent the saturation where the spool of the valve can not open more. The subsets where each control input can stabilize the plant are indicated with different colors. There are two domains where none of the control inputs can stabilize the system. However, this does not pose a problem since the system is stable, see (12). There are also domains where multiple inputs can take the system to the reference value. The control strategy exploits this feature to switch between control inputs.

The control algorithm for the spool valve is based on solving the Control Lyapunov Function. For every time step the control strategy calculates the values of the ellipsoids (21) by substituting the momentary values of the states and the reference signal for each discrete control input. The controller switches between input signals by choosing the appropriate solution. In the strategy the lowest value of the possible solutions is selected in order to guarantee reference tracking, i.e., x_v tends toward $x_{v,ref}$.

Assuming E_{max} , E_0 , E_{min} are the solutions of the ellipsoid equations (21) for i_{max} , i_0 , i_{min} respectively, the control algorithm can be formulated mathematically as follows:

$$i = \begin{cases} 0 & \text{when } \{E_{max}, E_0, E_{min}\} \geq 0 \\ i_{max} & \text{when } \min\{E_{max}, E_0, E_{min}\} = E_{max} \\ i_0 & \text{when } \min\{E_{max}, E_0, E_{min}\} = E_0 \\ i_{min} & \text{when } \min\{E_{max}, E_0, E_{min}\} = E_{min} \end{cases} \quad (22)$$

For energy saving considerations, the control strategy presented above shall be augmented with an additional criterion. If the reference torque on the high level M_{ref} is a predefined small value, the control input is always set at zero. This criterion is necessary because otherwise the output x_v would fluctuate around the reference $x_{v,ref}$, which is zero at this point and the controlled system would never reach equilibrium.

IV. ROBUST CONTROL DESIGN OF THE HYDROMOTOR

The actuator can be separated into two subsystems: the hydromotor (high level) and the valve (low level), which are interconnected. The goal of the hydromotor control is to track a reference torque M_{ref} . The output signal of the high-level controller $K_{act,up}$ is a reference spool displacement

$x_{v,ref}$, which must be realized by the valve. The tracking of this reference signal is ensured by the low-level controller $K_{act,low}$, which computes discrete values of current i on the solenoids, which cause the displacement of the spool.

In case of the independent control design the global stability of the controlled interconnected system must be ensured. A possible solution to guarantee the global stability of the individually stable systems is to prove the existence of a Common Lyapunov Function. In this paper the global stability of the system is guaranteed by the robust control design of the high-level control. In the design method the inaccuracy of the low-level tracking control is incorporated, which guarantees the interaction in the hierarchy. Moreover, other uncertainties of the actuator are considered in the robust control method.

In the following the robust control design of the upper-level hydromotor is presented. The purpose of the control design is to guarantee the tracking of the reference torque M_{ref} by an appropriate valve motion x_v , which is physically realized by the low-level controlled valve system. Another important goal of the robust control design is to guarantee the global stability of the entire controlled actuator. First uncertainties of the actuator is detailed and second the robust \mathcal{H}_∞/μ design is proposed.

A. Uncertainties of the actuator

1) *Inaccuracy of low-level control*: The aim of the analysis is to formulate the maximum tracking error of the low-level control. The result is incorporated in the design of the high-level robust control. Thus, the effect of the valve positioning inaccuracy is minimized.

The process of the analysis is the following. Several simulations are performed using different initial values $x_v(0)$, $\dot{x}_v(0)$ and reference position $x_{v,ref}$. The intervals of the initial values are $x_v(0) = -0.01 \text{ m} \dots 0.01 \text{ m}$, $\dot{x}_v(0) = -0.1 \text{ m/s} \dots 0.1 \text{ m/s}$ and $x_{v,ref} = -0.01 \text{ m} \dots 0.01 \text{ m}$. In each case the maximum tracking error is calculated. The

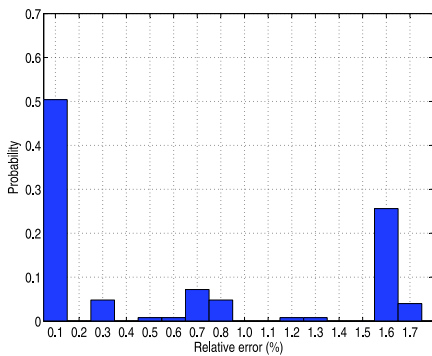


Fig. 4. Relative frequency of valve positioning

statistical results of the analysis are illustrated in Figure 4. It can be stated that the relative error of the valve positioning is reasonable. The error is below 0.1% and the maximum value is 1.7%.

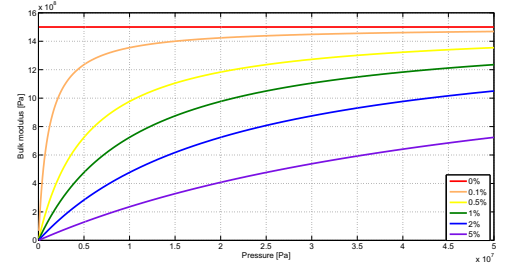


Fig. 5. Bulk modulus with different air contents

The results of the simulation-based statistical analysis are used for the modeling of an uncertainty in a multiplicative form. In the robust control design the worst case scenario is considered.

2) *Uncertainty of the Bulk modulus*: The Bulk modulus β_E of the system (6) is an important physical parameter in the behavior of the hydromotor. It depends on several parameters, such as pressure and entrapped air. Generally, the pressure dependence at constant temperature can be formulated as $\beta_E = -V_0 \frac{\partial p}{\partial V}$, where V_0 is the initial volume and p is the pressure of the chamber.

Furthermore, β_E depends significantly on the percentage of entrapped air in the system [9]. It seriously affects system performance in terms of loss of hydraulic power, slower response time, degradation in accuracy and the change in natural frequencies, which may cause stability issues [11]. When air is present in the system, the bulk modulus can be considered as two springs, connected in series:

$$\frac{1}{\beta_E} = \frac{1}{\beta_{fluid}} + \frac{V_{air}}{V_{total}} \frac{1}{\beta_{air}} \quad (23)$$

The adiabatic bulk modulus of air can be written as follows:

$$\beta_{air} = \frac{c_p}{c_v} p = 1.4p \quad (24)$$

where c_p and c_v are heat capacities at constant pressure and constant volume, respectively. Let $s = V_{air}/V_{total}$ be the percentage of air in the system. Using the expressions above, (23) can be written into the following form:

$$\frac{1}{\beta_E} = \frac{1}{\beta_{fluid}} + \frac{s}{1.4p} \quad (25)$$

The connection between pressure and air content is illustrated in Figure 5.

It can be stated that β_E is an important uncertain parameter of the system, which must be handled, see [12]. To formulate β_E as a real parametric uncertainty, it is written in a lower linear fractional transformation (LFT) form:

$$\beta_E = \bar{\beta}_e(1 + d_e \delta_e) = \mathcal{F}_l \left(\begin{bmatrix} \bar{\beta}_e & 1 \\ d_e \bar{\beta}_e & 0 \end{bmatrix}, \delta_e \right) = \mathcal{F}_l(M_e, \delta_e) \quad (26)$$

In the LFT structure the relationship between the output and the input of the block M_e is $\tilde{y}_e = \beta_e \tilde{u}_e + u_e$, while the uncertainty block δ_e is pulled out of the equation. $\bar{\beta}_e$ denotes the nominal value of the parameter and d_e is a scalar,

which represents the percentage of variation that is allowed for a given parameter around its nominal value. Moreover, $-1 \leq \delta_e \leq 1$ determines the actual parameter deviation. In the formulation of parametric uncertainties, δ_e , $i \in (e)$ block must be pulled out of the motion equations.

The formulated \tilde{y}_e output is used in (3) to express the parametric uncertainty of the system as follows:

$$\begin{aligned} \dot{p}_L = & \frac{4\bar{\beta}_e}{V_t} (\bar{K}_q x_v - \bar{K}_c p_L - V_p \varphi + c_{l1} \dot{\varphi} - c_{l2} p_L) + \\ & + \frac{4}{V_t} (\bar{\beta}_e u_q - \bar{\beta}_e u_c + u_e) \end{aligned} \quad (27)$$

B. Robust \mathcal{H}_∞/μ control design

After the formulation of uncertainties, the robust control design of the hydromotor is presented. The purpose of the control is to guarantee the tracking performance of the system, formulated as follows:

$$z = M_{ref} - M_{act}; \quad |z| \rightarrow \min \quad (28)$$

where M_{ref} is a reference torque signal, which is defined by the vehicle dynamic control. The goal of the controller is to guarantee criterion (28) against parameter uncertainties and disturbances (sensor noise and external load).

In the state-space representation, on which the control design is based, the parametric uncertainty and the inaccuracy of the low-level control are involved. Modifying the original system description (6) and considering the formulated performance (28), the hydromotor state-space representation is formed as:

$$\dot{x}_{HM} = A_{HM,u}x_{HM} + B_{1HM,u}w + B_{2HM,u}u \quad (29a)$$

$$z_{HM} = C_1 x_{HM} + D_{1,1} w \quad (29b)$$

$$y_{HM} = C_{HM}x_{HM} \quad (29c)$$

where the state vector, the disturbance and the control input are $x_{HM} = [p_L \ \dot{\varphi} \ \varphi]^T$, $w_u = [M_{dist} \ M_{ref} \ u_e \ w_n]^T$ and $u_u = x_v$, respectively.

In \mathcal{H}_∞/μ control design several weighting functions are formulated which guarantee a balance between the performances and scale the different signals of the system. Figure 6 illustrates the closed-loop interconnection structure of control design.

The performance z is considered with a weighting functions in the following form: $W_z = (\alpha_1 s + \alpha_0)/(T_1 s + T_0)$, where α_1 , α_0 and T_1 , T_0 are design parameters. The role of W_{dist} and W_{ref} is to scale torque disturbance signal M_{dist} and reference torque M_{ref} . The control system requires the measurement of tracking error $M_{ref} - M_{act}$, as shown in Figure 6. The sensor noise w_n of the measured signal is considered with weighting function W_n , which gives information about the bound of noise amplitude. Two uncertainty blocks are involved in the closed-loop interconnection structure. Δ_r incorporates the parametric uncertainty of the system, while Δ_m represents the uncertainty on the control input signal, which is derived from the imprecise realization of x_v during low-level control. $W_u = (\alpha_{u,2}s^2 + \alpha_{u,1}s + \alpha_{u,0})/(T_{u,1}s^2 + T_{u,1}s + T_{u,0})$ scales the bound of input

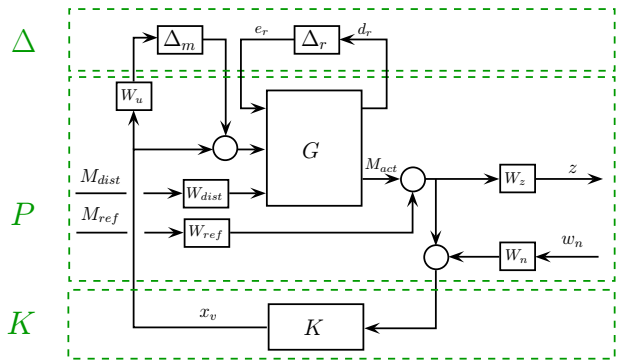


Fig. 6. Closed-loop interconnection structure

multiplicative uncertainty, where $\alpha_{u,2}$, $\alpha_{u,1}$, $\alpha_{u,0}$ and $T_{u,2}$, $T_{u,1}$, $T_{u,0}$ are design parameters.

In the robust \mathcal{H}_∞/μ control design the controller synthesis problem is the following. Find a controller K such that

$$\mu_{\tilde{\Delta}}(M(i\omega)) \leq 1, \forall \omega \Leftrightarrow \min_{K \in \mathcal{K}_{stab}} \left[\max_{\omega} \mu(M(i\omega)) \right] \quad (30)$$

where μ is the function of the structured singular value of the system $M(i\omega)$ with a given uncertainty set $\tilde{\Delta} = \text{diag}[\Delta_r, \Delta_m, \Delta_p]$. Δ_r represents the parametric uncertainties, Δ_m describes the unmodelled dynamics and Δ_p is a fictitious uncertainty block, which incorporates the performance objectives into the μ framework.

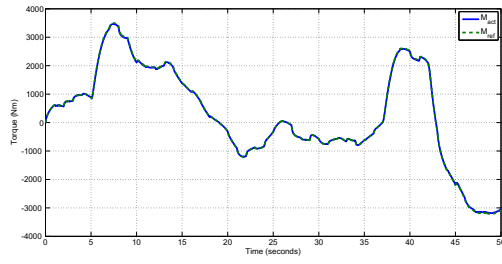
The optimization problem can be solved in an iterative way by using scaling components. For fixed K the problem of finding scaling components D and G is based on optimization problems. For calculated scaling components the problem of finding controller $K(s)$ leads to another optimization step. The procedure is called a standard $D, G - K$ iteration. The optimization problem is intractable in most cases, but an ad hoc algorithm has been developed, see [13].

V. DEMONSTRATION EXAMPLE

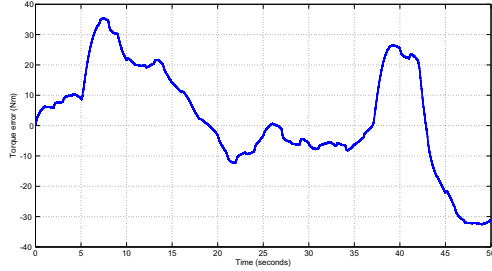
In this section the operation of the electro-hydraulic actuator is presented through a simulation example. The maximum spool valve displacement is $|x_{v, sat}| = 0.01m$, the discrete current inputs are $i = \{-0.35; 0; 0.35\}A$.

The reference torque signal M_{ref} is generated by the vehicle dynamic control. The torque tracking performance of the actuator is shown in Figure 7(a). In most of the simulation the difference between M_{act} and M_{ref} is sufficiently low as illustrated in Figure 7(b). The relative tracking error is approximately 1%. The tracking error only increases at high reference torque values and it is proportional to the magnitude of the reference signal. Noise on the torque measurement shown in Figure 7(c) does not have a significant effect on the tracking performances. Thus, the undesirable sensor noise can be rejected by the designed robust \mathcal{H}_∞/μ control.

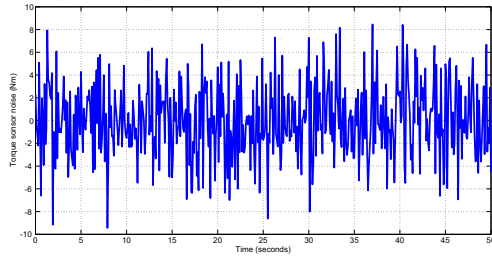
The valve positioning is shown in Figure 7(d). The lower-level operates with high precision, and does not exceed the saturation limit of the actuator. The control current of the valve system i is found in Figure 7(e). The Figure 7 shows



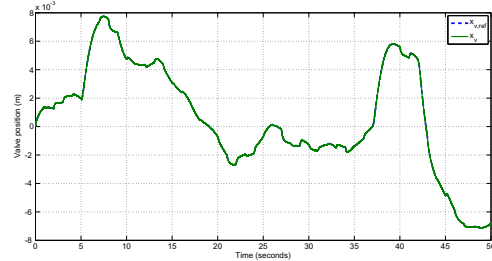
(a) Active torque of hydromotor



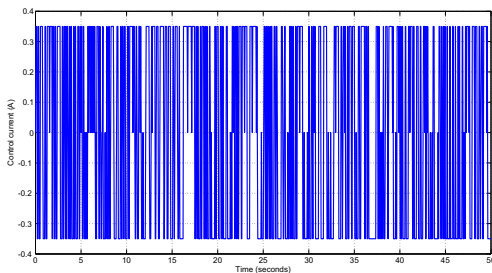
(b) Tracking error of hydromotor torque



(c) Sensor noise on torque



(d) Motion of electrohydraulic valve



(e) Control input i

Fig. 7. Time responses of the closed-loop actuator

that the low-level control is able to work adequately with fixed input values.

VI. CONCLUSION

The paper has proposed the control design of an electro-hydraulic actuator. The design is in line with the concept of hierarchical control systems. The control-oriented model of the hydromotor is formed as a linear system while the valve is a polynomial system. The valve model has a state constraint for the spool displacement due to physical considerations and it uses the Control Lyapunov Function to calculate discrete input current values. The hydromotor control is based on the \mathcal{H}_∞/μ method, in which the inaccuracy of the lower-level control, parametric uncertainty and disturbances are incorporated. Thus, it guarantees the stability of the entire system. The advantage of this modular design is that the different requirements can be guaranteed for smaller-complexity subsystems. Simulation results prove that the control system can effectively track the reference torque in reasonable bounds, while the constraint of the system is not violated.

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