# Super-capacitor energy storage system to recuperate regenerative braking energy in elevator operation of high buildings

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# ABSTRACT

In operating phases of elevators, accelerating, braking modes occur frequently, so braking energy recuperation of elevators has contributed considerably to decrease the total electric energy consumption for operating elevators in multi-floor buildings. In this paper, the supercapacitor energy storage system is used to recover regenerative braking energy of elevators when they operate down full-load and up no-load, reducing fluctuation of voltage on DC bus as well. Therefore, super-capacitor energy storage system (SCESS) will be parallel with line utility to recuperate regenerative braking energy in braking phase and support energy for acceleration phase. The surplus energy will be stored in the supercapacitors thanks to a DC-DC converter capable of exchanging energy bidirectionally in buck/boost modes, and designing control strategy including two control loops. Inner loopcurrent loop: controlling charge/discharge process of supercapacitors by current iL complying with operation characteristic of elevator; Outer loopvoltage loop: managing UDC-link at a fixed value. Simulation results with elevator system of the ten-floor building, Hanoi, Vietnam installed SCESS have been verified on MATLAB Simulink, SimPowerSystem with saving energy level about 30%.

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# 1. INTRODUCTION

In elevator operation, regenerative braking energy is mainly dissipated on braking resistors [1], [2]. Therefore, how to reduce energy consumption in these vertical transportation systems has long been one of hot research issues to pay much attention from scientists, engineers. With rapid growth of power electronics converters, traction motor making easier for many saving energy solutions in elevator operation to be performed [3]–[9].

Figure 1 showed three groups of solutions for saving energy in elevator operation: Recuperating regenerative braking energy, reducing the energy consumption of comfort functions, enhancing traction efficiency. Among them, percentage of recovering regenerative braking energy is the highest. This solution group can be divided into two categories: the direct use of regenerative energy by matching time of accelerating and braking elevators by timetable optimization using the optimal control theory so that regenerative braking energy of elevators operating in power generation state transfers to elevators operating

in motoring state [10], [11], and the indirect use of regenerative energy by applying energy storage devices recovering braking energy when elevators operate in no-load lifting, and full-load lowering [12]–[17], or active rectifiers, reversible rectifiers in order to back the braking energy to the grid source [18]–[20]. This paper proposes the method for recovering regenerative braking energy by the super-capacitor energy storage system (SCESS) with the saving energy percentage indicated in the simulation results on MATLAB of the building ten floor being up to 30%.



Figure 1. Block diagram of energy saving solutions in elevator operation

## 2. MODELING ELEVATOR SYSTEM

The structure for the full elevator system shown in Figure 2 includes the diode rectifier, elevator drive system, a bank of supercapacitors with bidirectional DC-DC converter paralleled to the DC bus. Modelling some main parts has been performed briefly.

#### 2.1. Modelling traction motor

The traction motor is a cage induction motor. The induction motor model in the d - q reference frame is obtained [21], [22]:

$$\begin{cases} \frac{di_{sd}}{dt} = -\left(\frac{1}{\sigma T_s} + \frac{1-\sigma}{\sigma T_r}\right)i_{sd} + \omega_s i_{sq} + \frac{1-\sigma}{\sigma T_r}\psi'_{rd} + \frac{1-\sigma}{\sigma}\omega\psi'_{rq} + \frac{1}{\sigma L_s}u_{sd} \\ \frac{di_{sq}}{dt} = -\left(\frac{1}{\sigma T_s} + \frac{1-\sigma}{\sigma T_r}\right)i_{sq} - \omega_s i_{sd} + \frac{1-\sigma}{\sigma T_r}\psi'_{rq} - \frac{1-\sigma}{\sigma}\omega\psi'_{rd} + \frac{1}{\sigma L_s}u_{sq} \\ \frac{d\psi_{rd}}{dt} = \frac{L_m}{T_r}i_{sd} - \frac{1}{T_r}\psi_{rd} + (\omega_s - \omega)\psi_{rq} \\ \frac{d\psi_{rq}}{dt} = \frac{L_m}{T_r}i_{sq} - (\omega_s - \omega)\psi_{rd} - \frac{1}{T_r}\psi_{rq} \\ m_M = \frac{3}{2}z_p\frac{L_m^2}{L_r}\psi'_{rd}i_{sq} = \frac{3}{2}z_p(1-\sigma)L_s\psi'_{rd}i_{sq} \\ m_M = m_L + \frac{J}{z_p}\frac{d\omega}{dt} \end{cases}$$
(1)

where the parameters are defined as:  $\psi'_{rd} = \psi_{rd}/L_m \operatorname{va} \psi'_{rq} = \psi_{rq}/L_m$ ,  $\sigma = 1 - \frac{L_m^2}{L_s L_r}$ : leakage factor,  $T_s = \frac{L_s}{R_s}$ : stator time constant,  $T_r = \frac{L_r}{R_r}$ : rotor time constant,  $T'_{\sigma} = \frac{\sigma L_{\sigma}}{r_{\sigma}}$ ,  $\omega_s = \omega + \frac{L_m}{T_r} \frac{i_{sd}}{\psi_{rd}}$ : slip estimation,  $\omega$ : mechanical rotor speed,  $z_p$ : number of pole pairs, J: Moment of inertia,  $m_L$ : Load torque,  $\psi_{rd}, \psi_{rq}$ : rotor flux, and  $L_m, L_r, L_s$ : mutual, rotor, and stator inductance.

#### 2.2. Determining static loads

Calculating static loads in order to determine power of traction motor. The tensile forces exerted on the active pulley along the cable branches are:

$$F_1 = [G_{cb} + G_t + G_c(H - H_{cb})] \cdot g(N)$$
<sup>(2)</sup>

$$F_2 = [G_{dt} + G_c(H - H_{dt})].g(N)$$
(3)

Total force exerted on active pulley when lifting and lowering full load:

$$F_n = F_1 - F_2 = (G_{cb} + 1000 - G_{dt})g + G_c(H_{dt} - H_{cb})g(N)$$
(4)

$$F_h = F_2 - F_1 = (G_{dt} - G_{cb} - 1000)g + G_c(H_{cb} - H_{dt})g(N)$$
(5)

where:  $F_n$ ,  $F_h$ : Lifting, lowering forces,  $G_{dt}$ : Counter-weight mass (Kg),  $G_c$ : Mass of a cable length unit (Kg/m),  $G_t$ : Load mass,  $H_{dt}$ : Counterweight height (m),  $H_{cb}$ : Cabin height(m), g: Acceleration of gravity (g=9.8 m/s<sup>2</sup>). The torque converted to the motor shaft calculated by the traction force:

$$M = \frac{F \cdot R}{i \cdot \eta} \text{ if } F > 0; M = \frac{F \cdot R}{i} \eta \text{ if } F < 0 \tag{6}$$

R: Cable pulley radius, i: Gear ratio,  $\eta$ : Transmitter efficiency. Full load lifting torque converted to motor shaft:

$$M_1 = \frac{G_{cb} + Gdt_{tmax}}{i.\eta} \tag{7}$$

No-load lifting torque converted to motor shaft:

$$M_2 = \frac{G_{cb} - G_{dt}}{i} g.R.\eta \tag{8}$$

Torque lowering full load converted to motor shaft:

$$M_3 = \frac{G_{cb} + Gdt_{tmax}}{i} \tag{9}$$

Torque lowering no-load double to the motor shaft:

$$M_4 = \frac{G_{cb} - G_{dt}}{i.\eta} g.R \tag{10}$$



Figure 2. Elevator drive system with induction motor and energy recovery braking

#### 2.3. Modeling bidirectional DC-DC converter

Power circuit diagram of the DC-DC converter shown in Figure 3 being capable of flowing energy bidirectionally from SCESS to traction motor and vice versa [23]–[25] operates in buck or boost modes because voltage on DC bus is high, voltage on supercapacitor is low.



Figure 3. Buck-boost converter schematics

Equivalent circuit of bidirectional DC-DC converter is demonstrated in Figure 4, an ideal transformer is replaced for switches with d(t) being transformer factor, and  $\begin{cases} u_1(t) = d(t)u_2(t) \\ i_2(t) = d(t)i_1(t), \end{cases}$ Mathematic model of the DC-DC is written [26]:

$$\begin{cases} L\frac{di_L}{dt} = -R_L i_L + du_{DC\_link} - u_{SC} \\ C\frac{du_{DC\_link}}{dt} = -di_L + i_{inv} \end{cases}$$
(11)

where control variable - duty ratio (d), the state variables -  $i_L$ ,  $u_{DC link}$ .



Figure 4. Equivalent circuit of DC-DC converter

## 3. CONTROL DESIGN FOR ELEVATOR SYSTEM

Designing control for elevator system comprises of designing field-oriented control (FOC) for elevator drive motor [21] and designing control for the bidirectional DC-DC converter [25]. However, in this section, focusing on controlling the DC-DC converter. Hence, using two - loop cascaded control structure is also called current mode control (CMC) [26] as shown in Figure 5. The outer loop is the voltage loop regulating error between  $u_{DC-linhk}$  and  $u_{DC-link}^*$ , which creating the current reference for the inner current

loop. The inner loop controls  $i_L$ - the inductor current in order to controlling charge or discharge process of super-capacitor system in an accordance with the elevator operation characteristic.



Figure 5. CMC structure for DC-DC converter

## 3.1. Design control of the current-loop

The inner loop controls charge and discharge process of supercapacitor. From the first equation of (11), building up the small-signal model.

$$\frac{d\tilde{\iota}_L(t)}{dt} = -\frac{R_L}{L}.\tilde{\iota}_L(t) + \frac{1}{L}.\tilde{d}(t).U_{DC\_link} + \frac{1}{L}.D.\tilde{u}_{DC\_link}(t) + \frac{1}{L}.\tilde{u}_{sc}(t)$$
(12)

In steady state,  $u_{sc}$  may be considered as constant in steady state so regarding as constant disturbance for the control loop. Therefore, the transfer function of the inductor current is computed:

$$G_{pi}(s) = \frac{\tilde{\iota}_L(s)}{\tilde{d}(s)} = \frac{U_{DC\_link}}{Ls + R_L}$$
(13)

The current controller PI with transfer function:

$$G_{Ci}(s) = k_p + \frac{k_i}{s} = \frac{T_i s + 1}{T_a s}$$
(14)

with  $T_i = \frac{k_p}{k_i}$ ;  $T_a = \frac{1}{k_i}$ ;  $T_{nl}$ : delay time caused by PWM. The closed-loop transfer function of Figure 6 is given:

$$G_{Si}(s) = \frac{U_{DC\_link}/R_L}{T_a.s(1+T_{nl}.s) + U_{DC\_link}/R_L}$$
(15)

Using module optimal method determines [27]:

$$T_{i} = \frac{L}{R_{L}}; K_{p} = \frac{L}{2.U_{DC\_link}.T_{nl}}; K_{i} = \frac{K_{p}}{T_{i}} = \frac{R_{L}}{2.U_{DC\_link}.T_{nl}}$$
(16)



Figure 6. Current-loop control structure

## **3.2.** Design control of the voltage-loop

From the second equation of (11), building up the small-signal model:

$$\frac{d\tilde{u}_{DC\_link}(t)}{dt} = \frac{1}{C} \cdot \tilde{\iota}_{inv}(t) - \frac{1}{C} \cdot \frac{U_{sce}}{U_{DC\_linke}} \cdot \tilde{\iota}_{L}(t) - \frac{1}{C} \cdot \tilde{d}(t) \cdot I_{Le}$$
(17)

Applying the Laplace transform for (17) leads to (18).

$$G_{vi}(s) = \frac{\tilde{u}_{DC_{link}}(s)}{\tilde{\iota}_{L}(s)} \bigg|_{\substack{\tilde{d}=0\\\tilde{\iota}_{inv}=0}} \cong \frac{\tilde{u}_{DC_{link}}(s)}{\tilde{\iota}_{L}^{*}(s)} \bigg| = \frac{U_{sce}}{CU_{DC_{linke}}s} = \frac{K_{u}}{s}$$
(18)

Assuming that synthesizing the current loop is extremely fast, accurate, so, ideally, its transfer function with a gain of unity as shown in Figure 7. Voltage controller -PI:

$$G_{vc}(s) = k_{pu}(1 + \frac{1}{T_{iu}s})$$
(19)

the closed- loop transfer function of voltage loop:

$$G_{ku}(s) = \frac{G_{hu}(s)}{1 + G_{hu}(s)} = \frac{k_1 \frac{1 + T_{iu} \cdot s}{s^2}}{1 + k_1 \frac{1 + T_{iu} \cdot s}{s^2}} = \frac{k_1 (1 + T_{iu} \cdot s)}{s^2 + k_1 (1 + T_{iu} \cdot s)} = \frac{k_1 \cdot T_{iu} \cdot s + k_1}{s^2 + k_1 \cdot T_{iu} \cdot s + k_1}$$
(20)

Finding values of  $k_{pu}$ ,  $k_{iu}$  by using symmetry optimal method,

$$G_{ku}(s) = \frac{k_1 \cdot T_{iu} \cdot s + k_1}{s^2 + k_1 \cdot T_{iu} \cdot s + k_1} \triangleq \frac{2 \cdot \xi \cdot \omega_n \cdot s + \omega_n^2}{s^2 + 2 \cdot \xi \cdot \omega_n \cdot s + \omega_n^2}$$
(21)

where  $\xi$  - Damping ratio ( $\xi = 0.71$ ),  $\omega_n$ - oscillation cycle,

$$\Rightarrow \begin{cases} k_1 = \omega_n^2 \\ k_1 \cdot T_{iu} = 2 \cdot \xi \cdot \omega_n \end{cases} \Leftrightarrow \begin{cases} k_1 = \frac{k_{pu} \cdot k_u}{T_{iu}} = \omega_n^2 \\ T_{iu} = \frac{2 \cdot \xi \cdot \omega_n}{\omega_n^2} = \frac{2 \cdot \xi}{\omega_n} \end{cases} \Leftrightarrow \begin{cases} k_{pu} = -\frac{\omega_n^2 \cdot T_{iu} \cdot C \cdot U_{DC\_linke}}{U_{sce}} \\ T_{iu} = \frac{2 \cdot \xi}{\omega_n} \end{cases}$$
(22)



Figure 7. Voltage-loop control structure

# 4. SIMULATION RESULTS

The simulation data in Table 1 are collected from the high building 10 floor, Hanoi, Vietnam; parameters used in simulation are shown in Tables 2 and 3. Simulation scenarios elevator system run up with full load running down with full load when the elevator operates ten floors with total time about 50.76 s. The speed of elevator running up full load is 1 m/s in Figure 8(a), and down full load is -1 m/s in Figure 8(b) accordance with the change of the power: 2600 and -1700 W shown in Figures 9(a) and 9(b).

Parameters	Values
Number of floors	10
Number of floors	10
Distance between floors (m)	2.8
Cabin's weight (kg)	1200
Counterweight (kg)	1600
Passengers weight (kg)	1000
Maximum speed, v <sub>max</sub> (m/s)	1
Acceleration and deceleration, a <sub>max</sub> (m/s2)	1.5
Pulley diameter, D (m)	0.4
Transmission ratio, i	1/20
Transmission performance, η	80%
Nominal power P (kW) of each motor	15
Number of elevators	01

Table 1. Parameters of elevator system for the building ten floor high

## Table 2. Parameters of DC-DC converter

Parameters	Values
Inductance, L(mH)	
Resistance, RL $(\Omega)$	0.05
Capacitance of DC-Link capacitor (µF)	1000
DC Link voltage (V)	650
Parameters of super-capacitor 2 F/325 V	

Table 3. Parameters of controllers

Parameters	$K_p$	$T_i$
Current loop	0.0154	0.04
Voltage loop	-0.284	0.0142



Figure 8. Speed responses (a) operating up with full load and (b) operating down with full load



Figure 9. Power on shaft of traction motor when elevator is in full load up/down operation (a) operating up with full load and (b) operating down with full load

Figures 10 and 11 compared  $U_{dc-link}$  with/without SCESS. Without SCESS, voltage fluctuation on bus DC when the elevator operates up with full load is from 620 to 650 V DC as shown in Figure 10(a). The elevator operates down with full load  $U_{dc-link}$  increases from 650 to 800 V DC as shown in Figure 10(b). Meanwhile, using SCESS helping to reduce fluctuation of the grid voltage only around 650 VDC. Comparing level of consumption energy when the elevator in the ten-floor building moving up with full load the heaviest load without/with using SCESS in Figures 12 and 13 is 23 Wh, 16 Wh respectively; calculating percent of saving energy is 30%. Additionally, unity consumption energy when the elevator runs down with full load without/with SCESS in Figures 14 and 15 is 1.23 and 0.6 W respectively.



Figure 10. Responses of  $U_{dclink}$  with diode rectifier (a) operating up with full load and (b) operating down with full load



Figure 11. Response of U<sub>dclink</sub> using SCESS





Figure 12. Response of unity consumption energy as operating up with full load



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Figure 14. Response of unity consumption energy as operating down with full load



Figure 15. Response of unity consumption energy as operating down with full load using SCESS

## 5. CONCLUSION

In this paper, focusing on recuperating regenerative braking energy in elevator operation by using SCESS paralleled with bus DC. The simulation results of the elevator drive system in the ten-floor building integrated with SCESS showed energy can save up to 30%.

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