

Luminance Prediction of Paper Model Surface Based on Non-Contact Measurement

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Abstract: The overall appearance perception is affected by luminance perception accuracy and efficiency mostly. The surface luminance prediction correlated with surface angle and surface tone value was performed by measuring and modeling the paper model surface luminance. First, we used a rotating bracket designed to facilitate to set the paper surface angle. Then, we set the surface angle from 5° to 85° at the interval of 5° using the designed rotating bracket. Additionally, the four primary color scales, cyan, magenta, yellow, and black, were printed and set at the designed angle. The angle-ware and tone-ware luminance was measured using spectroradiometer, CS-2000. Finally, we proposed and evaluated a mathematical model to reveal the relationship between luminance and surface angle and surface tone using the least squares method. The results indicated that the surface luminance of paper model could be predicted and obtained quickly and accurately for any surface angles and surface tone values by the proposed prediction model.

Keywords: luminance prediction model; non-contact measurement; paper model surface; surface angle; surface luminance prediction; surface tone

1 INTRODUCTION

Luminance prediction and analysis of object surfaces is becoming a hot research topic in the area related to colour reproduction, stereoscopic image processing and 3D printing. The luminance perception is made up of the total appearance perception for the physical objects. Luminance perception can also make more effects on the appearance perception and the details representation is also determined by the luminance perception, which contributes to object surface colour perception [1]. However, there are giant differences between the viewing conditions for 2D plain image and 3D stereoscopic image [2]. For 2D plain image perception, luminance perception, measurement, or reproduction is a mature technique used in the area of many research and industrial areas, such as printing colour reproduction [3]. Luminance perception is always restricted to deposit the measure point or focus at a given angle on the surface. Luminance can be measured easily with contact measurement or prediction models [4]. Similarly to luminance perception on 2D plain surface, the given point can be measured using contact measure method and instrument. In contrast, due to the irregular geometric shape of the 3D object surface, the luminance always gives different perception for the same viewing point. It is difficult to get total luminance for the 3D object surface with irregular geometric shape due to the limits of the measuring instruments, prediction models and complexity of viewing conditions [5]. Therefore, it is still necessary to do further research on the luminance perception and prediction of the 3D object surface with a simple method in colour research areas [6]. On one hand, it is easy to get the total appearance of 3D object with the help of 3D scanner. But the information obtained from the 3D object surface is almost about the distance information which is used to create the surface point cloud information to construct the object surface shape. It does not include the surface luminance and colour information which is obviously different from the information obtained using 2D scanner that mostly includes luminance information and colour information [7]. On the other hand, perception, prediction and representation of 3D object surface colour information must work with the help of luminance. It is not enough to perform the colour representation only with 3D

scanner [8]. How to predict the luminance of 3D object surface is becoming more and more important in such area. In this work, paper model was used to work as the primary object to represent luminance perception and prediction with the basic surface geometric and tone information. Surface angle and tone value are the main properties in such paper model surface geometric information. The function happening between light and paper on 3D paper model surface is similar to that on 2D plain paper surface from the perspective of micro-structure which is always described by the BRDF theory [9]. The paper surface angle and tone value relative to the observer were set to be non-contact measured luminance using spectroradiometer in our work. The relations between luminance and bi-factors, surface angle and tone value, were analysed to get the luminance perception and prediction of paper model surface. Paper surface luminance is affected by the interaction between paper and inks, paper surface roughness and other parameters [10]. Just like the human skin colour and luminance measurement, skin surface is processed specially to obtain the colour perception under different viewing angles [11], while the paper surface is processed to measure the luminance using four primary colour inks.

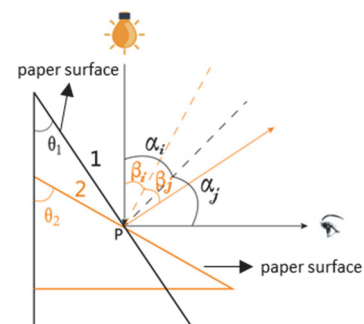


Figure 1 Perception varies with surface angle

Paper model surface is set in the exact viewing conditions, i.e., the lighting source position and observer viewing angles are fixed. Obviously, there are various surface angles against the observer for the irregular geometric surface of paper model. The perception caused by surface angle can be shown in Fig. 1. For paper model surfaces, its angles against vertical line or horizontal line

are various. For surface 1, the vertical angle is θ_1 , and the incident angle to the point P is α_i and the reflection angle is α_j . However, to the surface 2 whose angle is θ_2 , its incident angle and reflection angle will change to β_i and β_j , though the model position, light source position and perceiver position keep the same as before. It will cause the lightness, i.e., luminance, to change obviously.

Microscopically speaking, the surface of paper model is similar to that of 2D plain paper, it has the same interaction between light and paper surface which is always described by BRDF and related theories [13]. To be noted that interaction occurring on the microfacet with light is shadowing and masking. Shadowing is the occlusion of the light source by the microgeometry while masking is the visibility occlusion of a microfacet by another microgeometry (see Fig. 2).

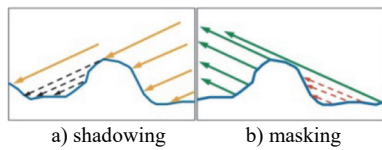


Figure 2 Shadowing and Masking on the microfacet

Actually, there is always interreflection between the microfacets or other optical interactions between the surface and the paper inside, such as scattering, absorption and refraction (see Fig. 3). Anyway, these optical matters are always ignored in measuring the surface lightness. We would not take that factor into account in our paper and it is consistent with the practical prediction and measurement.

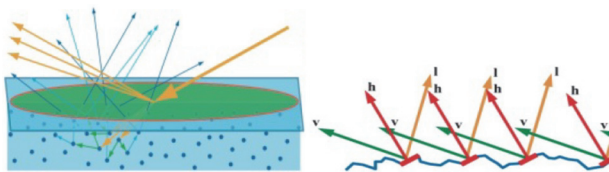


Figure 3 Interreflection between the microfacets on the surface

2 EXPERIMENT

2.1 Paper Model Surface Sample Design

We use electrophotography press, Konica Minolta (KM-C6000), to output colour patches with paper of 128 g/m². KM-C6000 is the colour equipment that uses electrophotography technique to output the colours on the paper surface. Its toner is controlled by electrostatic force and forms images on paper. The ink set we used is TN616 which includes Cyan, Magenta, Yellow and Black. TN616 is a group of Toner Cartridge for Konica Minolta.

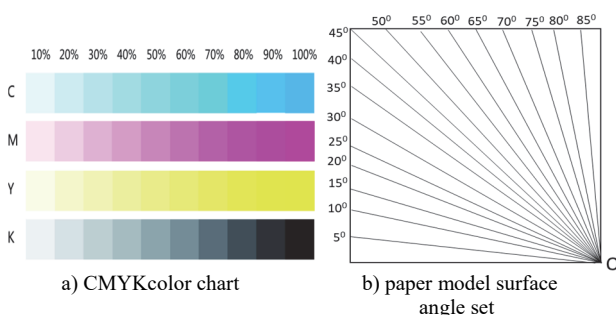


Figure 4 Tone scale and angle set of paper model surface

Tone chart, S , was designed from 10% to 100% with intervals of 10%. Here S is a group primary colour chart. The size of each colour patch is 3 cm × 3 cm, Fig. 4a. Model sample surface angles were designed from 5° to 85° with interval of 5°, Fig. 4b.

2.2 Measuring Conditions Set

We choose the non-contact method to measure the luminance for the paper model surface, and spectroradiometer, CS2000, was used to obtain the data from the paper sample surface. CS2000 is a high accuracy spectroradiometer designed to measure luminance and chromaticity up to super-low luminance regions. Paper samples were set in a standard light source box with D65.

The light box used in the experiment is suitable for the need to keep colour consistency and quality. It has multi-point source observation system, used in printing ink, paint, plastics, cosmetics, textiles, leather, food, paper, stain and other non-ferrous materials inspection and match colours. The colour box is made of solid material of medium density fiberboard, lighting box inside is TuMeng N5.5 self gray. And such light box is equipped with membrane switch, coming with a 45 degree tilt observatory and five standard light sources. They are F/A, TL84, D65, D50, UV.

All measurement data was obtained in darkroom which excludes the effect of environment light. The bracket used in this experiment was to help set the paper sample surface angle effectively and accurately [12]. The point measured should be kept the same for every surface and the measure distance should also be kept the same for every sample. Additionally, the vertical distance from the light to the sample surface should be kept the same for different samples. The experiment condition set is shown in Fig. 5. According to our experimental conditions, measuring distance is set as 172 cm. and the vertical distance was set as 49 cm.

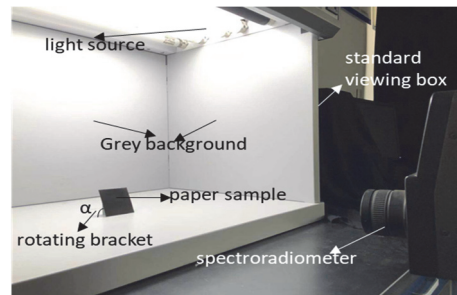


Figure 5 Experiment conditions

Table 1 Effect of measurement distances

| Horizontal/ cm | X(1931) | Y(1931) | Z(1931) | x(1931) | y(1931) |
|----------------|---------|---------|---------|---------|---------|
| 100 | 50.78 | 48.52 | 55.98 | 0.3270 | 0.3125 |
| 150 | 51.42 | 49.13 | 56.68 | 0.3270 | 0.3125 |
| 172 | 52.16 | 49.84 | 57.54 | 0.3269 | 0.3124 |
| 200 | 51.46 | 49.16 | 56.78 | 0.3269 | 0.3123 |

The chromatic coordinate difference is too small to perceive for different horizontal and vertical measuring differences (see Tab. 1 and Tab. 2). It showed that there is less effect from the horizontal and vertical measure distance in the experiment viewing conditions.

Table 2 Effect of vertical distances to light source

| Vertical / cm | X(1931) | Y(1931) | Z(1931) | x(1931) | y(1931) |
|---------------|---------|---------|---------|---------|---------|
| 49.5 | 52.72 | 50.37 | 58.07 | 0.3271 | 0.3125 |
| 49 | 54.25 | 51.84 | 59.80 | 0.3270 | 0.3125 |
| 48 | 53.87 | 51.27 | 60.08 | 0.3261 | 0.3103 |
| 47 | 57.15 | 55.16 | 61.98 | 0.3279 | 0.3165 |

3 RESULT AND DISCUSSION

3.1 Effects of Surface Angle on Luminance

The paper model surface luminance of angle-aware and tone-aware was measured. And the luminance values, surface angles and surface tone values were normalized to 0 to 1. The relations between the luminance and surface

angle with different tone values are shown in Fig. 6. Obviously, there is a mutation point at the angle of 30° for every tone of C, M, Y and K. Furthermore, Y has another mutation point at 60°, though it is less obvious compared with that of 30°. At 30°, luminance becomes higher for every sample, which is consistent with the objective perception while the effect of 30° for each tone value on luminance is smaller for Y primary tone compared with the other three primary colour tones. In Fig. 4, L_v is luminance and $angle$ is surface angle.

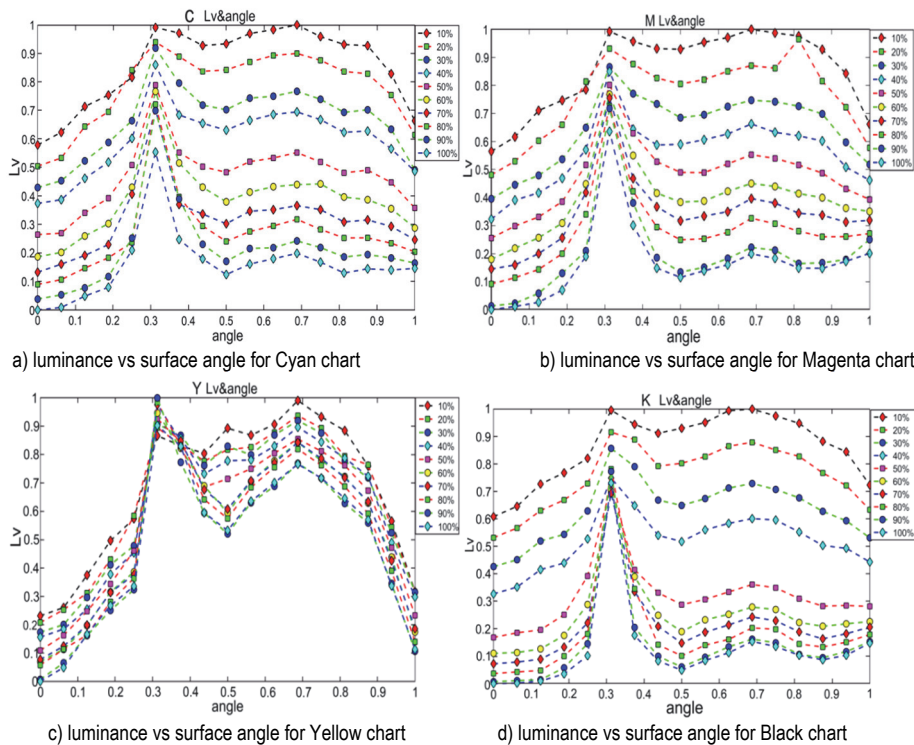


Figure 6 Effect of surface angle on luminance for four primary tones

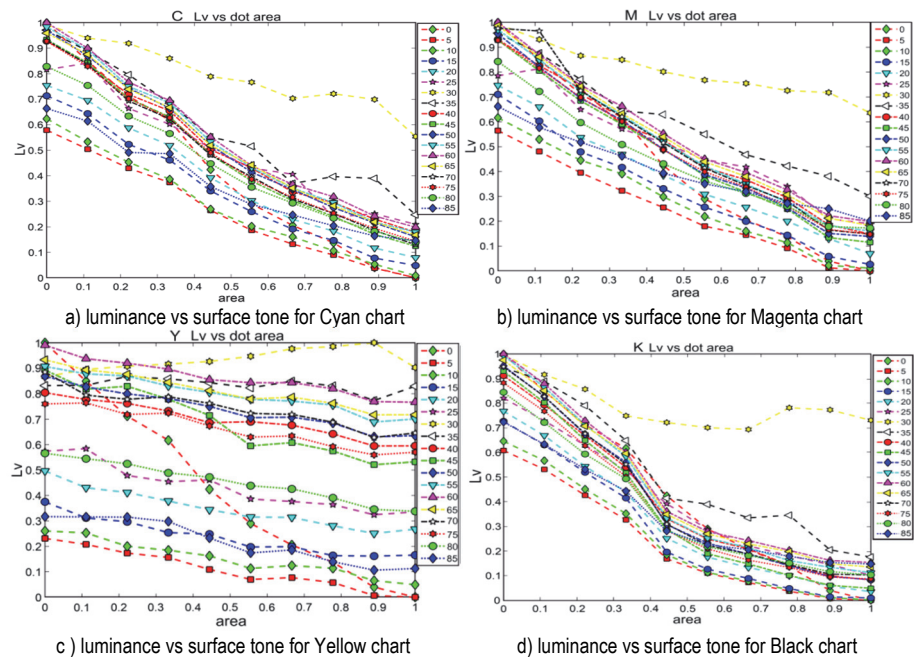


Figure 7 Effect of primary colour tones on luminance for various surface angles

3.2 Effects of Tone Value on Luminance

Luminance decreases with the increase of tone values in 2D printing process. For 3D paper model surface, luminance perception is affected by the tone value and surface angle simultaneously (see Fig. 5). The luminance of 30° surface has the brightest perception for all samples. It shows that the luminance perceived on 30° surface is less affected no matter the primary colour tone changes. For the same surface angle, luminance has similar trends to those that happened in 2D printing. Obviously, the Y primary tone has more dispersed luminance perceptions than other three primary tones. In Fig. 5, L_v is luminance and $dot\ area$ is surface tone value. And the luminance values, surface angles and surface tone values were normalized to 0 to 1.

4 LUMINANCE PREDICTION MODELLING AND ANALYSIS

4.1 Modelling

There are several sets of equations between the luminance and tone values, luminance and surface angles that have not been determined. The least squares method [14] is used to approximate the solution of the surface angle and tone value on the luminance perception for paper model surface. From Fig. 4 and Fig. 5, luminance is affected by tone value obviously and the relation can be shown as follows:

$$Lv_i = a_i \times S_i + b_i, \quad i = 1, 2, \dots, n \tag{1}$$

where, Lv_i is luminance, S_i is tone value, a_i and b_i are scale factor, i is the ordinal number of surface angle. For different surface angles, we rewrite the Eq. (1) as follows:

$$\begin{bmatrix} Lv_1 \\ Lv_2 \\ \dots \\ Lv_n \end{bmatrix} = \begin{bmatrix} S_{11} & \dots & S_{1n} \\ \dots & \dots & \dots \\ S_{n1} & \dots & S_{nn} \end{bmatrix} \begin{bmatrix} a_1 \\ a_2 \\ \dots \\ a_n \end{bmatrix} \tag{2}$$

$$\text{With } \begin{bmatrix} Lv_1 \\ Lv_2 \\ \dots \\ Lv_n \end{bmatrix} = Y, \quad \begin{bmatrix} S_{11} & \dots & S_{1n} \\ \dots & \dots & \dots \\ S_{n1} & \dots & S_{nn} \end{bmatrix} = C, \quad \begin{bmatrix} a_1 \\ a_2 \\ \dots \\ a_n \end{bmatrix} = X \quad Y \text{ and } C$$

are the samples, X is scale factor. The Eq. (2) can be rewritten as follows:

$$CX = Y \tag{3}$$

In Eq. (3), we can get:

$$C^T CX = C^T Y \tag{4}$$

where, C^T is transpose matrix of C , so we can rewrite Eq. (4) as follows:

$$X = (C^T C)^{-1} C^T Y \tag{5}$$

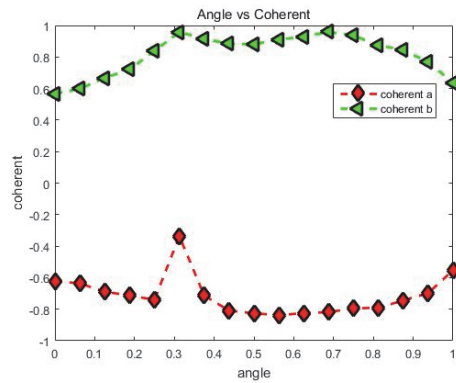


Figure 8 Scale factor a_i , b_i vs surface angle α

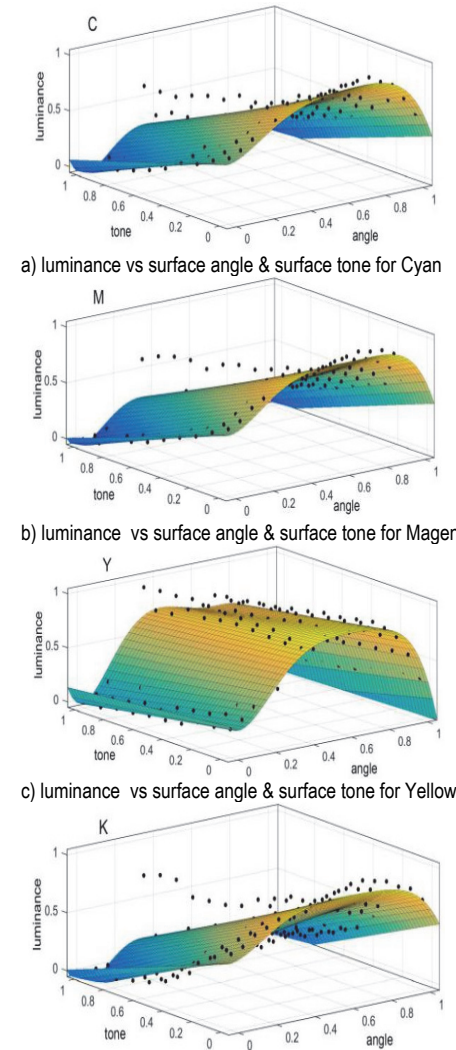


Figure 9 Luminance Predicted vs Luminance Measured: Colored continuous belts: Luminance predicted; Black points: Luminance measured

We need to solve this equation to calculate the scale factors of every surface angle α . For our 17 designed surface angles, one set of scale factors a_i and b_i were obtained as in Fig. 6. It showed that a and b can be calculated as functions of surface angle α as follows:

$$\begin{cases} a = g(\alpha) \\ b = t(\alpha) \end{cases} \tag{6}$$

where, we chose fifth-order nonlinear function to calculate the relation between scale factor and surface angle and finally converted the intrinsic relations between luminance and tone to intrinsic relations between luminance and tone & surface angle, as follows:

$$Lv = F(S, \alpha) = g(\alpha) \times S + t(\alpha) \tag{7}$$

We can compute the luminance prediction for four primary colour tone samples according to our proposed model, Eq. (5) and Eq. (7). The results are shown in Fig. 7. Black points are the sample luminance measured using our experimental sets. The colour surfaces are the predicted luminance using the model proposed in this paper. It showed that most of the points matched the model well except the 30°. We will further discuss the performance of our proposed prediction model when put in practice in the next section.

4.2 Analysis

We use R^2 (coefficient of determination) to analyze the proposed model. R^2 is the proportion of variance in the dependent variable from the independent variables [15]. It is a static that gives information about the goodness of fit of our model. R^2 can be defined as follows [13]:

$$R^2 = 1 - \frac{\sum (y_i - \hat{y}_i)^2}{\sum (y_i - \bar{y}_i)^2} \tag{8}$$

where, y_i is sample value, \hat{y}_i is predicted value, \bar{y}_i is average value of samples, n is the total number of samples. Values of R^2 are from 0 to 1. An R^2 of 0 indicates that the fitting prediction values does not match the measurement values at all while a R^2 of 1 indicates that the prediction values perfectly fit the data. In this experiment, R^2 of four primary color samples were computed as in Tab. 3. Both values of R^2 of Cyan and Magenta are over 0.9 which shows the fitting process matches well with the measurement, i.e., over 90% of fitting prediction luminance data matched the measured data. And values of R^2 of Yellow and Black are over 0.8 which shows the fitting process is still accepted and over 80% of fitting prediction luminance data matched the measured data.

Table 3 Values of R^2 of four primary color samples

| | C | M | Y | K |
|-------|--------|--------|--------|--------|
| R^2 | 0.9115 | 0.9013 | 0.8747 | 0.8268 |

Additionally, according to the model proposed in Eq. (5) and Eq. (7), all samples of designed surface angles with primary color tones were computed and measured. The results are shown in Tab. 4. It shows that the difference Δ between prediction value and measured value is from 0.01 to 8.06. The average difference of yellow is the smallest while the black is the biggest. The average value of the total differences is 3.03. And the minimum differences of all primary color samples almost happened at 30° surface angle or its neighbor point.

Table 4 Prediction values vs Measured values for designed surface angles

| Surface-Angle | Unprinted Paper Surface | C-tone | | | M-tone | | | Y-tone | | | K-tone | | |
|---------------|-------------------------|--------|-------|----------|--------|-------|----------|--------|-------|----------|--------|-------|----------|
| | | Mea. | Pre. | Δ | Mea. | Pre. | Δ | Mea. | Pre. | Δ | Mea. | Pre. | Δ |
| 5 | 43.018 | 50.56 | 48.69 | 1.87 | 53.40 | 51.18 | 2.22 | 61.04 | 61.13 | -0.09 | 51.21 | 46.81 | 4.40 |
| 10 | 44.473 | 53.40 | 51.51 | 1.89 | 56.30 | 54.08 | 2.22 | 64.21 | 64.20 | 0.01 | 54.90 | 50.11 | 4.79 |
| 15 | 44.154 | 59.18 | 57.33 | 1.85 | 61.39 | 59.20 | 2.19 | 68.96 | 68.74 | 0.22 | 61.86 | 56.92 | 4.95 |
| 20 | 48.55 | 61.77 | 60.05 | 1.71 | 65.33 | 63.33 | 2.00 | 73.68 | 73.50 | 0.19 | 64.72 | 60.29 | 4.43 |
| 25 | 48.484 | 65.73 | 65.81 | -0.08 | 72.05 | 70.25 | 1.80 | 74.94 | 76.28 | -1.34 | 70.92 | 66.72 | 4.21 |
| 30 | 50.977 | 76.92 | 75.80 | 1.21 | 87.04 | 85.92 | 1.21 | 96.39 | 99.40 | -3.02 | 84.69 | 83.08 | 1.62 |
| 35 | 56.265 | 75.65 | 73.59 | 2.06 | 82.99 | 80.79 | 2.19 | 90.33 | 91.97 | -1.64 | 81.57 | 77.06 | 4.51 |
| 40 | 59.63 | 72.86 | 70.44 | 2.42 | 81.58 | 78.52 | 3.07 | 89.68 | 89.67 | 0.01 | 79.11 | 73.59 | 5.55 |
| 45 | 62.73 | 73.26 | 70.30 | 2.97 | 81.85 | 78.13 | 3.72 | 93.99 | 93.85 | 0.14 | 81.60 | 74.82 | 6.78 |
| 50 | 64.665 | 75.56 | 72.30 | 3.26 | 83.70 | 79.70 | 4.00 | 92.51 | 92.29 | 0.22 | 82.98 | 75.63 | 7.36 |
| 55 | 67.827 | 76.44 | 72.99 | 3.44 | 84.58 | 80.42 | 4.15 | 94.19 | 93.83 | 0.36 | 84.69 | 76.80 | 7.88 |
| 60 | 71.594 | 77.50 | 73.80 | 3.50 | 86.83 | 82.59 | 4.24 | 97.36 | 96.89 | 0.47 | 85.78 | 77.72 | 8.06 |
| 65 | 74.386 | 74.87 | 71.45 | 3.42 | 83.71 | 79.46 | 4.25 | 96.75 | 96.14 | 0.61 | 83.68 | 75.70 | 7.98 |
| 70 | 76.609 | 73.10 | 69.72 | 3.38 | 86.52 | 82.29 | 4.23 | 92.78 | 92.18 | 0.60 | 80.73 | 72.95 | 7.78 |
| 75 | 82.324 | 72.83 | 69.52 | 3.31 | 83.36 | 79.18 | 4.18 | 87.58 | 87.25 | 0.33 | 75.91 | 68.68 | 7.22 |
| 80 | 85.318 | 66.52 | 63.34 | 3.18 | 72.51 | 68.71 | 3.79 | 78.64 | 78.82 | -0.18 | 71.12 | 64.45 | 6.67 |
| 85 | 87.793 | 55.99 | 52.99 | 3.00 | 61.85 | 58.60 | 3.25 | 67.04 | 68.25 | -1.21 | 60.48 | 54.70 | 5.78 |
| Ave. Δ | -- | 2.50 | | | 3.10 | | | 0.63 | | | 5.88 | | |

Additionally, we chose 7 arbitrary surface angles and used the proposed model to get the prediction luminance value of paper model surface. The surface color tones are still from 10% to 100%. It is shown in Tab. 5. The highest value of luminance differences is 7.96 and the lowest value of luminance differences is 0.11. The average value of

luminance differences is 2.62. Most of the luminance differences can almost not be perceived by human eyes. The results indicate that luminance of arbitrary surface angle and tone values can be predicted using our proposed model.

Tab. 5 Prediction values vs Measured values for arbitrary surface angles

| Surface-Angle | C-Tone | | | M-Tone | | | Y-Tone | | | K-Tone | | |
|---------------|--------|-------|----------|--------|-------|----------|--------|-------|----------|--------|-------|----------|
| | Mea. | Pre. | Δ | Mea. | Pre. | Δ | Mea. | Pre. | Δ | Mea. | Pre. | Δ |
| 17 | 62.31 | 59.48 | 2.83 | 59.27 | 57.47 | 1.80 | 66.15 | 66.26 | -0.11 | 58.36 | 53.43 | 4.93 |
| 28 | 78.45 | 75.19 | 3.26 | 74.59 | 72.57 | 2.03 | 82.57 | 90.47 | -7.9 | 74.48 | 70.01 | 4.47 |
| 33 | 83.27 | 80.27 | 3.00 | 82.20 | 81.48 | 0.72 | 91.47 | 98.29 | -6.82 | 82.28 | 80.81 | 1.47 |
| 42 | 81.16 | 77.16 | 4.00 | 76.81 | 75.38 | 1.43 | 84.92 | 83.02 | 1.9 | 75.10 | 70.75 | 4.45 |
| 48 | 80.53 | 77.74 | 2.79 | 79.16 | 76.85 | 2.31 | 85.63 | 85.11 | 0.52 | 76.38 | 71.47 | 4.91 |
| 57 | 86.79 | 82.73 | 4.06 | 83.10 | 80.18 | 2.92 | 95.61 | 95.30 | 0.31 | 81.39 | 74.41 | 6.98 |
| 62 | 87.62 | 82.62 | 5.00 | 83.14 | 80.56 | 2.58 | 93.63 | 93.41 | 0.22 | 81.26 | 73.30 | 7.96 |
| Ave. Δ | 3.56 | | | 1.97 | | | 2.54 | | | 5.02 | | |

5 CONCLUSION

The surface luminance prediction based on different surface angles and surface tone values was performed by measuring and modeling the paper model surface luminance. We set the angle from 5° to 85° at the interval of 5° . In addition, four primary color scales, cyan, magenta, yellow, and black, were printed and set at paper model surface. The angle-ware and tone-ware luminance was measured using non-contact measuring method. Finally, we proposed and evaluated a mathematical model to reveal the relationship between luminance and surface angles and surface tones. It indicated that the surface luminance of paper model could be predicted and obtained quickly and accurately by the proposed prediction model.

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