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# 1 Investigation of Organic Rankine Cycle Integrated with Double 2 Latent Thermal Energy Storage for Engine Waste Heat Recovery

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## 6 **Highlights:**

- 7 • ORC integrated with double LTES for engine waste heat recovery is proposed
- 8 • Twelve inorganic-salt PCMs are screened and the optimal one has been identified
- 9 • System output performance under different LTES volume is studied
- 10 • Three different scenarios integrated with single or double LTES are compared

## 11 **Abstract**

12 In this work, organic Rankine cycle (ORC) integrated with Latent Thermal Energy Storage  
13 (LTES) system for engine waste heat recovery has been proposed and investigated to  
14 potentially overcome the intermittent and fluctuating operational conditions for vehicle  
15 applications. A melting-solidification model has been established to investigate and compare  
16 the performance of twelve Phase Change Materials (PCMs) under different heat source  
17 conditions. Among the twelve PCMs, LiNO<sub>3</sub>-KCl-NaNO<sub>3</sub> is identified as the optimal PCM for  
18 engine exhaust heat recovery. The performance of the ORC system integrating with different  
19 volume of LTES using LiNO<sub>3</sub>-KCl-NaNO<sub>3</sub> under dynamic heat source simulating vehicle  
20 conditions is studied. Results illustrate the fluctuation of engine exhaust heat can be potentially

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1 overcome by using the proposed solution. The condition of 100 L LTES provides 30.4% larger  
 2 total output work than that of 50 L LTES, while it is merely 1.5% larger than that of 90 L LTES.  
 3 The performance of three different LTES-ORC scenarios are compared and results show ORC  
 4 combining with double LTES delivers 17.2% larger total power output than that of single LTES  
 5 (100 L) under the same operational conditions.

6 **Keywords:** Latent Thermal Energy Storage, Phase Change Material, Organic Rankine Cycle,  
 7 Dynamic Heat Source, Engine Waste Heat Recovery

### Nomenclature

$A_{in}$	Area of exhaust side ( $m^2$ )
$A_{out}$	Area of working fluid side $m^2$
$c_i$	The specific heat capacity of exhaust at time interval $i$ (kJ/kg K)
$c_{melt}$	The specific heat capacity of exhaust at $T_{melt}$ . (kJ/kg K)
$C_p$	The specific heat capacity of PCM (kJ/kg K)
$C_{p_c}$	The specific heat capacity of coolant (kJ/kg K)
$C_{p_{exh}}$	The specific heat capacity of the exhaust (kJ/kg K)
$C_{p_l}$	The specific heat capacity of liquid PCM (kJ/kg K)
$C_{p_s}$	The specific heat capacity of solid PCM (kJ/kg K)
$d$	The diameter of the exhaust pipe (m)
$h_{exh}$	Heat transfer coefficient of the exhaust ( $W \cdot m^{-2} K^{-1}$ )
$h_{in}$	Enthalpy of working fluid at the inlet of LTES ( $kJ \cdot kg^{-1}$ )

$h_{out}$	Enthalpy of working fluid at the outlet of LTES ( $\text{kJ}\cdot\text{kg}^{-1}$ )
$h_{wf}$	Heat transfer coefficient of working fluid ( $\text{W}\cdot\text{m}^{-2}\text{K}^{-1}$ )
$h_{wf,l}$	Heat transfer coefficient of working fluid at liquid zones ( $\text{W}\cdot\text{m}^{-2}\text{K}^{-1}$ )
$h_{wf,tp}$	Heat transfer coefficient of working fluid at two-phase zones ( $\text{W}\cdot\text{m}^{-2}\text{K}^{-1}$ )
$i$	$n^{\text{th}}$ time interval
$\Delta L$	Latent heat of PCM ( $\text{kJ}\cdot\text{kg}^{-1}$ )
$mc$	The mass flow rate of coolant (kg/s)
$m_i$	The mass flow of exhaust at time interval $i$ ( $\text{kg}\cdot\text{s}^{-1}$ )
$m_{exh,i}$	The mass flow rate of exhaust at time interval $i$ ( $\text{kg}\cdot\text{s}^{-1}$ )
$m_{wf}$	The mass flow rate of working fluid ( $\text{kg}\cdot\text{s}^{-1}$ )
$m_{PCM}$	Total mass of PCM (kg)
$Nu_{exh}$	Nusselt number of exhaust gas
$Pr_{exh}$	Prandtl number of exhaust gas
$Q_{exh}$	Heat flux the exhaust released to PCM (kW)
$Q_{in}$	Heat flux received from the evaporator (kW)
$Q_{out}$	Heat dissipation at condenser (kW)
$Q_{store}$	Thermal energy stored by the PCM (kJ)
$Q_{store,max}$	Maximum thermal energy stored by the PCM (kJ)
$Q_{wf}$	Heat the working fluid absorbed from PCM (kW)
$Re_{exh}$	Reynolds number of exhaust gas
$T_0$	The initial temperature of PCM at solid state ( $^{\circ}\text{C}$ )

$T_{e,pp}$	Evaporator pinch point temperature difference
$T_{evap}$	Evaporating temperature (°C)
$T_{exh,in}$	The inlet temperature of the exhaust (°C)
$T_{exh,out}$	The outlet temperature of the exhaust (°C)
$T_i$	The temperature of exhaust at time interval $i$
$T_{melt}$	Melting temperature of PCM (°C)
$T_{PCM}$	The temperature of PCM (°C)
$\Delta T_{lm,char}$	Log mean temperature difference in the charging process (°C)
$\Delta T_{lm,disc}$	Log mean temperature difference in the discharging process (°C)
$T_{e,pp}$	Evaporator pinpoint temperature difference (°C)
$\Delta t_1$	Time step in the charging process (s)
$\Delta t_2$	Time step in the discharging process (s)
$V$	The volume of PCM (L)
$W_p$	Work consumed by the pump (kW)
$W_e$	Output work of expander (kW)
$W_{net}$	The net power output of ORC (kW)

***Greek letters***

$\Delta\beta_{char}$	The liquid mass fraction of the charging process
$\Delta\beta_{disc}$	The liquid mass fraction of the discharging process
$\lambda_{exh}$	The thermal conductivity of exhaust
$\rho_s$	The density of PCM at solid state

$\Delta\tau$	Length of discretized time
$\eta_{sE}$	Expander isentropic efficiency
$\eta_{sP}$	Pump isentropic efficiency
$\eta_{th}$	The thermal efficiency of the ORC system

***Acronym***

<i>ETC</i>	European Transient Cycle
<i>HTF</i>	Heat Transfer Fluid
<i>ICE</i>	Internal Combustion Engine
<i>LTES</i>	Latent Thermal Energy Storage
<i>ORC</i>	Organic Rankine Cycle
<i>TLC</i>	Trilateral Rankine cycle

1

2

## 1 **1. Introduction**

2 Increasing attention is focusing on the environmental problems caused by the emissions from  
3 burning fossil fuels [1, 2]. Integrating waste heat recovery system to the existing energy  
4 systems can be a potential solution to improve the overall system efficiency and reduce the  
5 consumption of conventional energy resources. For vehicle application, the Internal  
6 Combustion Engine (ICE) dissipates around 60-70% of the overall fuel energy through exhaust  
7 gas, engine coolant, exhaust gas recirculation and charge air cooler [3, 4]. Several Rankine  
8 based systems have been proposed by researchers to study the performance of different waste  
9 heat recovery technologies, which can be used to recover the engine waste heat [5-7]. Other  
10 solutions such as thermoelectric generator [8, 9] and chemical absorption [10, 11] to recover  
11 the engine waste heat have also been reported. Among all these proposed waste heat recovery  
12 technologies, Organic Rankine Cycle (ORC) has been considered as one of the most practical  
13 solutions because of its simplicity, reliability, flexibility and relatively high efficiency [12].

14 The mainstream methods to investigate ORC technologies include the investigation of  
15 different ORC working fluids [13, 14], optimisation of system parameters [15, 16], design and  
16 optimisation of components [17] such as heat exchanger and expander, and the design of  
17 system configurations. Wang et al. [13] proposed a method to select working fluids and  
18 conduct parametric optimisation using a multi-objective optimisation model based on the  
19 simulated annealing algorithm. Results indicated R123 is the best candidate under the  
20 temperature ranging from 100-180 °C [13]. When the heat source temperature is higher than  
21 180 °C, R141b is the optimal working fluid for the ORC system [13]. The investigation of the

1 ORC system using alkane working fluids due to their excellent thermo-physical and  
2 environmental characteristics for engine waste recovery was reported by Shu et al [14]. Six  
3 indicators including thermal efficiency, exergy destruction factor, turbine size parameter, total  
4 exergy destruction rate, turbine volume flow ratio and net power output per unit mass flow rate  
5 of exhaust were adopted to study the performance of the ORC system using Alkane-based  
6 working fluids [14]. Yang et al. [15] developed a thermo-economic model to study a dual-loop  
7 organic Rankine cycle and employed a multi-objective genetic algorithm to obtain the Pareto  
8 optimal solutions. The maximum net power output and the minimum total economic cost  
9 during the whole range of operating conditions for a CNG engine were investigated [15]. Liu et  
10 al. [16] established a heat transfer model for a fin-and-tube evaporator of the ORC system to  
11 recover the waste heat of a diesel engine. Particle swarm optimisation algorithm is adopted to  
12 study the key geometric parameters of the fin-and-tube evaporator including the inlet radius of  
13 tube side and a shell side, height and thickness of fins and fin spacing. Ayad M. et al. [17] used  
14 small-scale axial, radial-inflow and radial outflow turbines on a small scale ORC system and  
15 compared their performances under their single and two stage configurations based on  
16 three-dimensional CFD analysis. Results indicated the two-stage axial and radial-outflow  
17 configurations can achieve a considerably better performance [17].

18 Many researchers are approaching to design and study cascaded ORC technologies to fully  
19 recover the engine waste heat. For example, Song et al. [18, 19] investigated a cascade ORC  
20 system designed for a heavy-duty diesel engine. Results showed R236fa was the most suitable  
21 selection for LT loop while cyclohexane and water were the proper working fluids for the HT



1 loop. The system can potentially improve the engine power by 11.2-11.6%. Yari et al. [20]  
2 compared the performance of organic Rankine cycle, trilateral Rankine cycle and Kalina cycle  
3 for recovering low-grade waste heat considering based on the thermodynamic and  
4 thermo-economic analysis. The results revealed that the Trilateral Rankine cycle (TLC) can  
5 obtain a larger net output power than that of the ORC and Kalina systems. Yu et al. [21]  
6 proposed an innovative cascade cycle combining a Trilateral Cycle and an ORC for industry or  
7 transport application to recover the exhaust thermal energy. Compared to the performance of a  
8 conventional dual-loop ORC system, the proposed novel cycle can improve the overall thermal  
9 efficiency and exergy efficiency by 33.7% and 31.2%, respectively [21].

10 For vehicle application due to the instantaneously operating conditions of the engines, the  
11 investigation of the dynamic performance of ORC systems attracted increasing attention.  
12 However, most of the studies focused on the performance of ORC under steady operating  
13 conditions of vehicle engines without considering the randomly and frequently operating  
14 conditions in the practical application. The violent fluctuation of engine exhaust mass flow rate  
15 and temperature lead to the unsteady ORC system operational state, which could damage the  
16 ORC system. When the inlet temperature at turbine inlet is out of the designed conditions, the  
17 ORC system works in a low efficient mode [22]. On the other hand, when the exhaust heat  
18 cannot provide sufficient heat to maintain the ORC systems operating within the designed  
19 conditions, the unsaturated working fluid will damage the expansion machine due to the  
20 existence of droplet [23]. The performance parameters of ORC systems such as thermal  
21 efficiency and net power output change greatly under different engine operating loads. Shu et

1 al. [24] studied the influence of engine operating conditions on a cascaded ORC system. When  
2 the temperature and mass flow rate of exhaust gas varies from 326 °C at 457.07 kg/h to 519 °C  
3 at 990.79 kg/h, the net power output and thermal efficiency change from about 12 kW at 6% to  
4 38 kW at 12% [24]. Katsanos et al. [25] investigated the potential improvement in the overall  
5 efficiency of a heavy-duty truck diesel engine equipped with an ORC system recovering engine  
6 exhaust heat. Results shown that the specific fuel consumption improvement ranging from  
7 10.2% (at 25% engine load) to 8.5% (at 100% engine load). In order to overcome the frequency  
8 variation of engine conditions, the ORC system with an oil storage was adopted and  
9 experimentally investigated by Shu et al. [23]. The results indicated that thermal oil loop  
10 brought a significant inertia to the response of a system which could be positive against the  
11 variation of engine condition. However, large space will be required to place the oil loop and  
12 related auxiliary devices, which is less possible to meet the requirement of compactness for the  
13 vehicle applications. Compared to the sensible heat storage method, latent thermal energy  
14 storage using Phase Change Material (PCM) possesses larger energy storage density with  
15 smaller volumes [26], and it can also provide a relatively homogeneous temperature field due  
16 to the phase change process of PCM. Therefore, LTES has the potential to be used for waste  
17 heat recovery and is suitable to bridge the mismatch between the energy supply and demand  
18 [27]. The energy storage device can act as a flywheel storing the waste heat of exhaust gas  
19 when the engine works under high load and releasing the stored heat to the ORC system when  
20 the engine works under low load.  
21 Integrating PCM latent thermal energy storage systems for recovering waste heat of engine

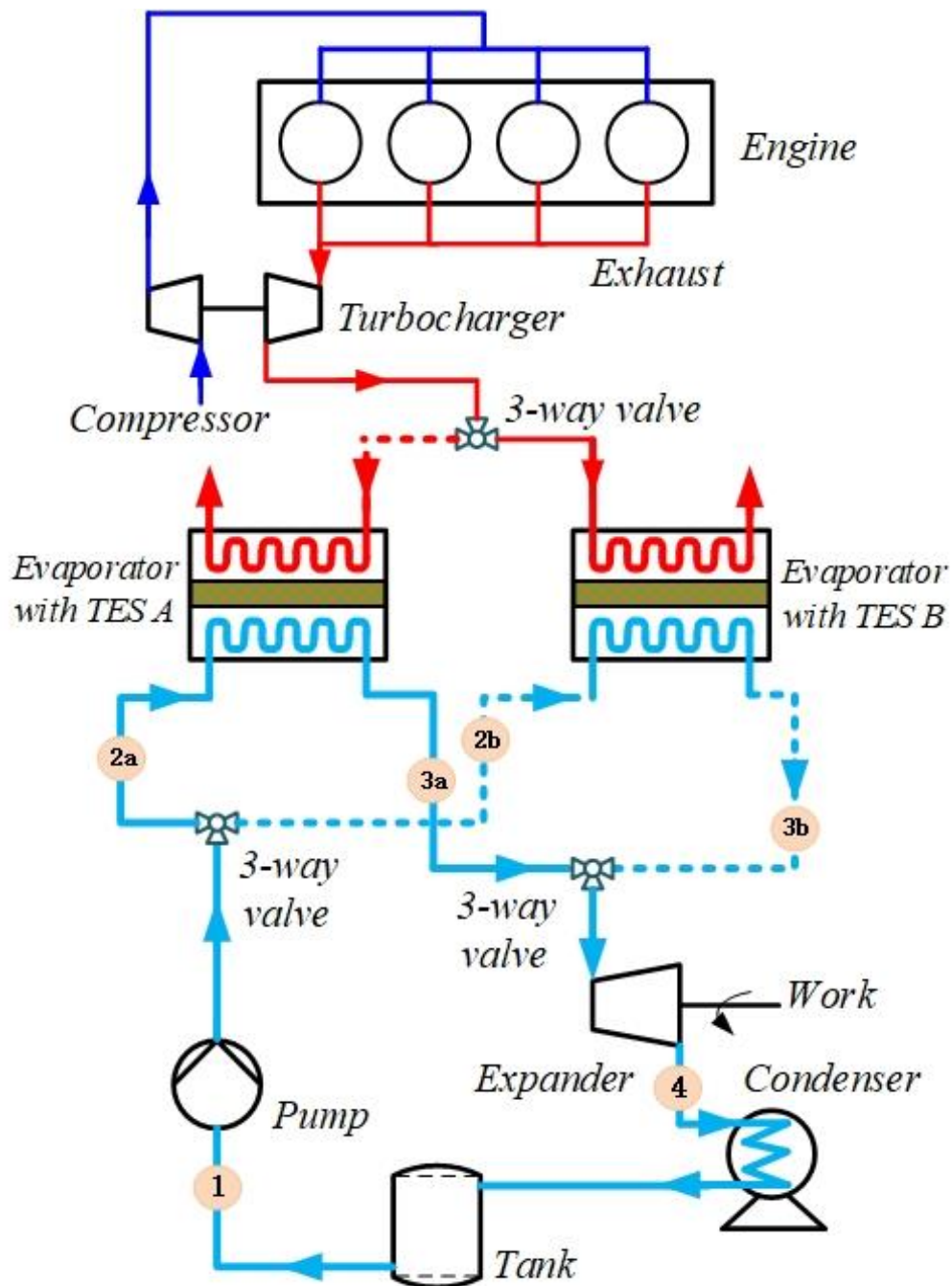
1 exhaust gas can be a potential solution. However, very limited researches have been found in  
2 the literature due to the concerns of system complicity and cost. Magro et al. [28] designed a  
3 PCM-based ORC recovering heat system for a billet reheating furnace. The conclusion is that  
4 the PCM-based technology can effectively reduce the adverse effects of fluctuating industrial  
5 waste heat and increase the average thermal efficiency from 15.5% to 16.4% and guarantee a  
6 payback period between 3 and 5 years [28]. Magro et al. [29] reported a study of a  
7 PCM-coupled steam generator for steel waste heat recovery. In the proposed system the  
8 thermal power fluctuation of exhaust gas was levelled in the PCM section before entering the  
9 steam generation section to generate constant superheated steam at the inlet of the turbine  
10 nearly at nominal load. The result showed that compared to traditional solutions the size of  
11 the steam generator and the turbine can be reduced to about 41% and the electric power can be  
12 improved by 22%. Freeman et al. [30] studied a small scale solar ORC system with various  
13 thermal energy storage media due to the fluctuation of solar irradiance intensity. A lumped  
14 model for the LTES was adopted to provide a simplified comparison of the various media.  
15 Results showed that the heat storage device with the volume of 400 L hydrated-salt PCM  
16 would increase the capital cost by 30%, but the overall cost is significantly lower than  
17 equivalent electricity storage solution [30]. The performance advantages achieved by PCM are  
18 mainly determined by the selection of suitable product with suitable melting temperature [30].  
19 Manfrida et al. [31] investigated the operation of a solar power plant associated with an LTES  
20 and an ORC unit is simulated under dynamic (time-varying) solar radiation conditions to  
21 design a system providing constant HTF power entering the evaporator of the ORC unit.

1 Results showed that the system is able to provide power in 78.5% of the time over the  
2 one-week period, with weekly averaged efficiencies of 13.4% for the ORC unit [31]. Although  
3 there are some references about ORC integrated with TES for solar energy utilisation and  
4 industrial applications considering the fluctuation of solar radiation intensity and industrial  
5 waste heat recovery, the majority of the ORC systems with LTES are indirect type. The ORC  
6 working fluid cannot extract heat from the PCM directly, which means a thermal fluid loop  
7 using heat transfer fluid should be added to the whole system. In this way, the system volume  
8 can increase to a large extent, which is less potential for vehicle application. Furthermore, the  
9 knowledge about phase change material options and scenario design of PCM-based ORC  
10 system for vehicle waste heat recovery require extensive research explorations. Because the  
11 temperature and mass flow rate change more frequently than that of solar radiation intensity  
12 and the requirement of compactness for vehicle using is much stricter than that of solar ORC  
13 system.

14 In this paper, an ORC system integrated with latent thermal energy storage has been proposed.  
15 The main aim of this paper is to evaluate the PCM options to reduce the adverse effect of the  
16 fluctuated exhaust on the ORC performance and maintain ORC working under the designed  
17 conditions. The concept of using double latent thermal energy storages have been proposed  
18 and studied in order to overcome the various operational conditions and randomly running time  
19 for vehicle application. The proposed ORC with double LTES can effectively reduce the  
20 adverse effect of unsteady and intermittent of vehicle operating loads maintaining ORC system  
21 work under relatively steady and efficient state.

1 **2. System description**

2 **2.1 Overall system description**



**Fig. 1.** Schematic diagram of the ORC integrated with double latent thermal energy storage

3 Fig. 1 presents the conceptual scheme of the ORC system integrated with double LTES. It

1 consists of two LTES evaporator, an expander, a condenser, a pump, a working fluid tank and  
2 several three-way valves. By switching three-way valves, it can be easily converted as a single  
3 LTES system.

4 The working process of this system can be described as follows. The high-temperature exhaust  
5 gas first flows into the LTES evaporator A, in which PCM starts the charging process and the  
6 waste heat is stored. When the PCM in the LTES evaporator A is fully melted, the exhaust gas  
7 flows into LTES evaporator B by switching the three-way valve and LTES evaporator B starts  
8 the same process as the LTES evaporator A. Meanwhile, the organic working fluid flows into  
9 LTES evaporator A and ORC starts working until the temperature of PCM decreases to the  
10 minimum driving temperature for ORC system. In this study, R245fa is adopted as the ORC  
11 working fluid, which has been previously studied for use in the low-temperature ORC waste  
12 heat recovery system and has a critical temperature of 154 °C [32]. The  $T$ - $s$  diagram of ORC  
13 with LTES is illustrated in Fig. 2.

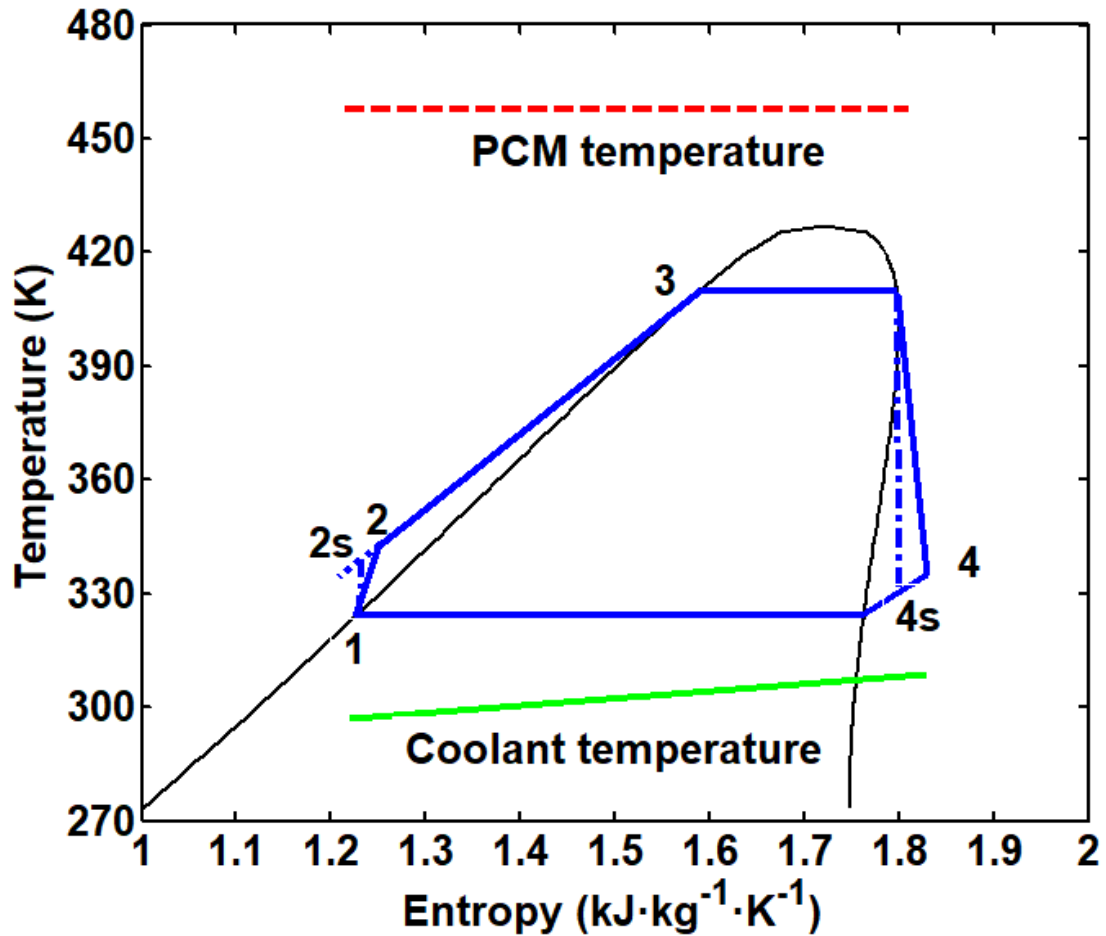
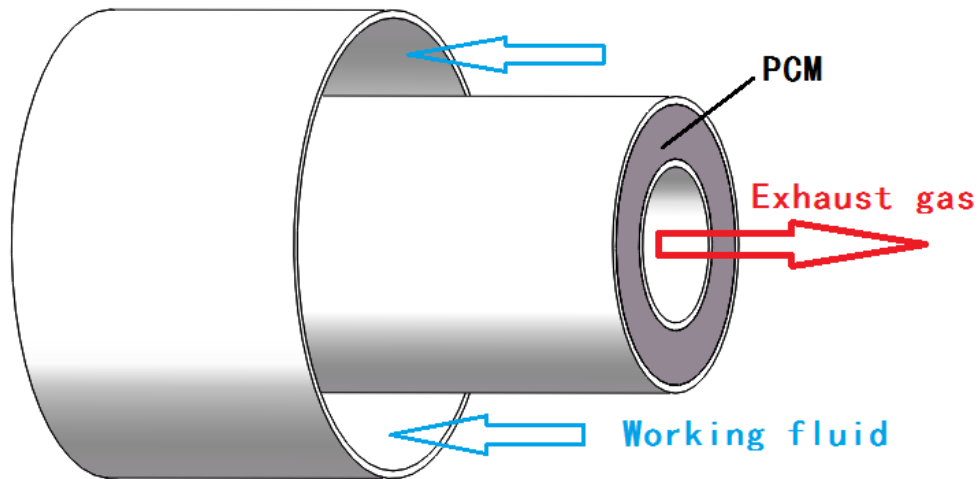


Fig. 2.  $T-s$  diagram of the ORC system with thermal energy storage

Evaporator with latent thermal energy storage is crucial for the performance of the whole system, in which an interlayer between the exhaust tunnel and working fluid tunnel and PCM is proposed as shown in Fig. 3. The latent thermal energy storage evaporator has a cylindrical structure including an inner tunnel, PCM interlayer and outer tunnel. The exhaust gas passes through the central channel and it heats the PCM. Fig. 4 shows the detailed structure of evaporator with LTES from the view of the longitudinal section. The shape of the PCM unit for flowing fluid heating in pipes is cylindrical geometry, which maximises the contact area with the heating target, and the structure can take high-pressure fluid.



1

2

**Fig. 3.** Principle diagram of latent thermal energy storage evaporator



3

4

**Fig. 4.** Diagram of the longitudinal section of the evaporator with LTES

5

## 2.2 Phase change materials

6

The requirements of the ideal PCM for thermal energy storage have been listed as follows:

7

proper melting and solidification temperature, high latent heat, the high specific heat of liquid

8

state, high density, relatively high thermal conductivity, low vapour pressure. The average

9

temperature of the vehicle engine exhaust gases at the inlet of ORC is around 200 to 300 °C,

10

therefore, the selected PCMs should have a relatively high melting temperature. In this

11

research, inorganic eutectic-compound phase change materials are selected because they have



1 been widely studied for thermal storage applications. Due to their higher density and stability  
 2 in their liquid state, they have been used widely as ionic liquids in high temperature sensible  
 3 thermal storage systems (thermonuclear energy, concentrated solar thermal power) [33]. The  
 4 physical properties chosen for the PCMs are broadly representative of a range of inorganic  
 5 (hydrated-salt based) materials. Table 1 presents the detailed thermos-physical parameters of  
 6 the eutectic-compound phase change materials to be studied.

7 **Table 1.** Thermo-physical properties of selected eutectic-compound phase change materials [33]

No	Eutectic compounds	Mass ratio	$T_{melt}$	$\Delta L$	$C_{ps}$	$C_{pl}$	$\rho_s$
			$^{\circ}C$	$kJ/kg$	$J/kg K$	$J/kg K$	$kg/m^3$
1	KNO <sub>2</sub> -NaNO <sub>3</sub>	48-52	149	124	1050	1630	2080
2	LiNO <sub>3</sub> -NaNO <sub>2</sub>	62-38	156	233	1570	1910	2296
3	LiNO <sub>3</sub> -KCl	58-42	160	272	1260	1350	2196
4	LiNO <sub>3</sub> -KCl-NaNO <sub>3</sub>	45-5-50	160	266	1320	1690	2297
5	HCOONa-HCOOK	45-55	176	175	1150	930	1913
6	LiOH-LiNO <sub>3</sub>	19-81	183	352	1600	2000	2124
7	NaNO <sub>3</sub> -LiNO <sub>3</sub>	51-49	194	262	1350	1720	2317
8	NaNO <sub>3</sub> -KNO <sub>3</sub>	55-45	222	110	1010	1490	2028
9	LiOH-NaNO <sub>3</sub> -NaOH	6-67-27	230	184	1300	2000	2154
10	CaCl <sub>2</sub> -LiNO <sub>3</sub>	13-87	238	317	1500	1530	2362
11	LiCl-LiNO <sub>3</sub>	9-91	244	342	1580	1610	2351

1 **3. Mathematical model**

2 **3.1 Design of thermal energy storage evaporator**

3 The design criteria of LTES are determined by the latent heat of the selected PCM and waste  
 4 heat of the exhaust at temperatures higher than PCM melting point  $T_{melt}$ . The maximum thermal  
 5 energy stored by the PCM can be calculated as Eq. (1) [34].  $\Delta\tau$  is the length of discrete time  
 6 equal to the sampling interval of the temperature data at the inlet of LTES. For each time  
 7 interval  $i$ , the exhaust gas temperature  $T_i$  and the mass flow  $m_{exh,i}$  are derived from the  
 8 measured data shown in Fig. 5 [35], while the exhaust gas specific heat  $c_i$  is calculated as a  
 9 function of  $T_i$ , as well  $c_{melt}$  is specific heat capacity of exhaust at  $T_{melt}$ .

$$Q_{stored,max} = \sum_{i:T_i > T_{melt}} \Delta\tau \cdot m_{exh,i} [c_i T_i - c_{melt} T_{melt}] \quad (1)$$

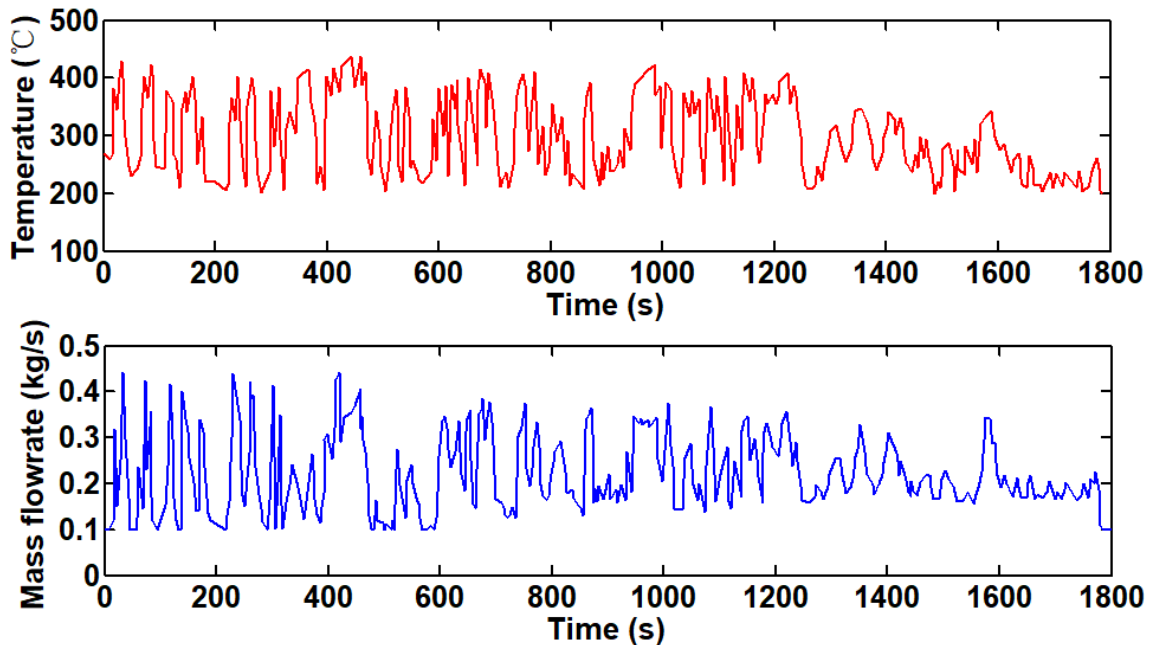


Fig. 5. Temperature and mass flow rate profiles of exhaust gas in ETC cycle [35]

10 Fig. 5 shows the temperature and mass flow rate profiles of vehicle diesel engine in the

1 European Transient Cycle (ETC). The temperature ranges from about 200 °C to 450 °C while  
 2 the mass flow rate is ranging from 0.1 to 0.4 kg/s. Based on this dynamic heat source, the  
 3 performance of ORC with LTES is simulated and analysed in the following sections.  
 4 PCM can store sensible heat and latent heat in the charging process. The relationship between  
 5 stored heat and mass of PCM is described by

$$Q_{stored} = Cp_s m_{PCM} (T_{melt} - T_0) + \rho_s \cdot V \cdot \Delta L + Cp_l m_{PCM} (T_{PCM} - T_{melt}) \quad (2)$$

### 6 3.2 Charging process for LTES

7 During the charging process, the temperature of PCM rises in solid phase until it reaches up to  
 8 the melting point of PCM. The temperature remains constant during the melting process. After  
 9 the phase change process is completed and all the PCM turns into the liquid phase, the  
 10 temperature of the liquid PCM continues to rise. The heat transfer coefficient between exhaust  
 11 and PCM is calculated by Dittus-Boelter correlation [28]

$$Nu_{exh} = 0.023 Re_{exh}^{0.8} Pr_{exh}^{0.4} \quad (3)$$

$$h_{exh} = \frac{Nu_{exh} \cdot \lambda_{exh}}{d} \quad (4)$$

12 The log mean temperature difference  $\Delta T_{lm, char}$  and the heat flow  $Q_{exh}$  are calculated as

$$\Delta T_{lm, char} = \frac{(T_{exh, in} - T_{PCM}) - (T_{exh, out} - T_{PCM})}{\ln \frac{T_{exh, in} - T_{PCM}}{T_{exh, out} - T_{PCM}}} \quad (5)$$

$$Q_{exh} = h_{exh} \cdot A_m \cdot \Delta T_{lm, char} \quad (6)$$

13 The heat balance reported in the following equation is used to calculate the outlet temperature

1  $T_{exh, out}$

$$Q_{exh} = m_{exh} \cdot Cp_{exh} \cdot (T_{exh, in} - T_{exh, out}) \quad (7)$$

2 When the calculation is converged, the relationship between the liquid mass fraction of PCM  
3 and the charging heat flow can be expressed as

$$Q_{exh} \cdot \Delta t_1 = \Delta L \cdot m_{PCM} \cdot \Delta \beta_{char} \quad (8)$$

4 When PCM is in the phase change process, the temperature of PCM is assumed to be  
5 constant. When PCM is in the sensible heat storage process, the updated temperature of PCM  
6 is calculated by Eq. (9), where  $Cp$  represents the specific heat capacity of PCM in the solid or  
7 liquid phase, which depends on its real-time state in the charging process.

$$T_{PCM}(t+1) = T_{PCM}(t) + \frac{Q_{exh}}{Cp \cdot m_{PCM}} \quad (9)$$

### 8 **3.3 Discharging process for LTES**

9 During the discharging process, thermal energy stored by liquid PCM is transferred to the heat  
10 transfer fluid (HTF). In the discharging process, the PCMs are considered as the heat source  
11 and it is assumed that one LTES is in the complete liquid state at the melting temperature while  
12 the other LTES is in the completely solid state at the melting temperature. Thermal losses in the  
13 charging and discharging process are neglected. Overall heat transfer coefficient of working  
14 fluid in liquid zones and two-phase zones are assumed to be constant [36].

15 The log mean temperature  $\Delta T_{lm, disc}$  is calculated as

$$\Delta T_{lm, disc} = \frac{(T_{wf, in} - T_{PCM}) - (T_{wf, out} - T_{PCM})}{\ln \frac{T_{wf, in} - T_{PCM}}{T_{wf, out} - T_{PCM}}} \quad (10)$$

1 The heat flux between PCM and the working fluid can be calculated by

$$Q_{wf} = h_{wf} \cdot A_{out} \cdot \Delta T_{lm, disc} \quad (11)$$

2 where  $h_{wf}$  represents the Overall heat transfer coefficient of working fluid at liquid zones and  
3 two-phase zone.

4 According to energy conservation, the mass flow rate of working fluid can be described as

$$m_{wf} = \frac{Q_{wf}}{(h_{out} - h_{in})} \quad (12)$$

5 The relationship between the liquid mass fraction of PCM and the discharging heat flow can  
6 be expressed as

$$Q_{wf} \cdot \Delta t_2 = \Delta L \cdot m_{PCM} \cdot \Delta \beta_{disc} \quad (13)$$

7 In the discharging process, the temperature of PCM is assumed to be constant when the PCM  
8 is during its phase change process. When PCM releases its sensible heat in the liquid or solid  
9 state, the temperature of PCM is calculated by

$$T_{PCM}(t+1) = T_{PCM}(t) - \frac{Q_{exh}}{Cp \cdot m_{PCM}} \quad (14)$$

### 10 **3.4 Thermodynamic model for ORC**

11 The temperature of PCM is assumed to be constant when it releases stored heat to the working  
12 fluid during the discharging process (solidification process). The key parameters for the sizing

1 of the ORC system in conjunction with the LTES are the working fluid mass flow rate and the  
 2 evaporation temperature. The evaporating temperature should meet the requirements of  
 3 liquid-liquid heat exchangers and gas-liquid heat exchangers [37]. Considering the potential  
 4 application on the vehicles, the pinch point temperature difference between the working fluid  
 5 and PCM has been set at 10 °C. The evaporation temperature is defined as follows

$$T_{evap} = \begin{cases} T_{melt} - T_{e,pp}, & T_{melt} \leq T_{PCM} \\ T_{PCM} - T_{e,pp}, & T_{melt} > T_{PCM} \end{cases} \quad (15)$$

6 The heat flux received from the evaporator and heat dissipation at the condenser

$$Q_{in} = m_{wf} (h_2 - h_3) \quad (16)$$

$$Q_{out} = C_p m_c (T_4 - T_1) \quad (17)$$

7 The work consumed by the pump can be calculated by the equations below

$$h_2 = h_1 + (h_{2s} - h_1) / \eta_{sp} \quad (18)$$

$$W_p = m_{wf} (h_2 - h_1) \quad (19)$$

8 For the expander

$$h_4 = \eta_{sE} (h_{4s} - h_3) + h_3 \quad (20)$$

$$W_e = m_{wf} (h_3 - h_4) \quad (21)$$

9 Then ORC net power and thermal efficiency

$$W_{net} = W_e - W_p \quad (22)$$

$$\eta_{th} = W_{net} / Q_{in} \quad (23)$$

1 The main parameters used in the calculation process are listed as Table 2. The isentropic  
 2 efficiency for expander and pump are conservatively selected as reported by reference [37].  
 3 Considering the practical vehicle application conditions, the condensing temperature is set  
 4 within the range of 35~60 °C [14, 24], in this paper it is set as 45 °C. The heat transfer  
 5 coefficients of working fluid in the liquid state, two-phase state and vapour state are given  
 6 reference value [36]. The organic fluid enthalpies and other parameters are functions of the  
 7 evaporating temperature chosen for the ORC and they are calculated with REFPROP. The  
 8 above model is solved by MATLAB.

9 **Table 2.** Parameters used in the ORC calculations

Parameters	Value
The inlet temperature of the cooling water	25 °C
Condensing temperature of working fluid $T_l$	45 °C
Evaporator pinch point temperature difference $T_{e,pp}$	10 °C
Expander isentropic efficiency $\eta_{sE}$	70%
Pump isentropic efficiency $\eta_{sP}$	80%
Heat transfer coefficient at liquid zone $h_{wf,l}$	260 W·m <sup>-2</sup> K <sup>-1</sup>
Heat transfer coefficient at two-phase zones $h_{wf,tp}$	900 W·m <sup>-2</sup> K <sup>-1</sup>

10 **4. Results and discussion**

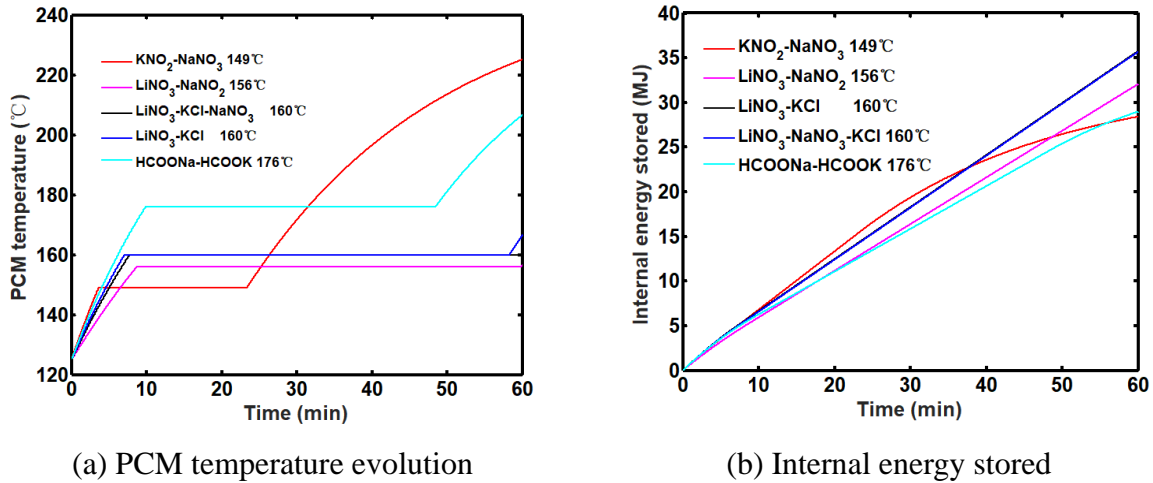
11 The investigation of PCM options within the fluctuation range of the vehicle engine exhaust  
 12 was studied on an ORC system integrated with single LTES for the purpose of selecting

1 potential PCM for the dynamic heat source. The performance of the ORC system with single  
2 LTES under different LTES volume has been evaluated based on the obtained proper PCM.  
3 Moreover, the performance of three different ORC-LTES systems including double LTES  
4 scheme and single LTES scheme were compared in a complete charging-discharging period  
5 under the dynamic heat source.

#### 6 **4.1 Analysis of PCM options under steady heat source conditions**

7 The effects of PCM options under different steady heat sources were analysed. The selection  
8 of potential PCM is important and necessary under steady heat source conditions because the  
9 exhaust temperature of the vehicle engines fluctuates from 200 °C to 450°C. Considering the  
10 requirement of compactness for vehicle application, the volume of LTES is set as 50 L. In  
11 this study, three different conditions of steady heat source are set at  $T=250$  °C, 325 °C and  
12 400 °C, and the mass flow rate is set at  $m=0.2$  kg/s. The duration of the charging process is  
13 set to be 60 minutes. Both the charging process and the discharging process were evaluated  
14 under several kinds of PCMs considering the relationship between the heat source  
15 temperature and the melting temperature in each case. Thermal losses are neglected and the  
16 initial condition of the store is set as the minimum temperature required to run the ORC  
17 system. The initial condition of the PCMs is assumed to be fully solidified and the internal  
18 energy increases isothermally as the melting of the PCM occurs. When the PCM is fully  
19 melted, the LTES stores heat sensibly and its temperature increases. Physical parameters of  
20 all the selected PCMs can be found in Table 1.



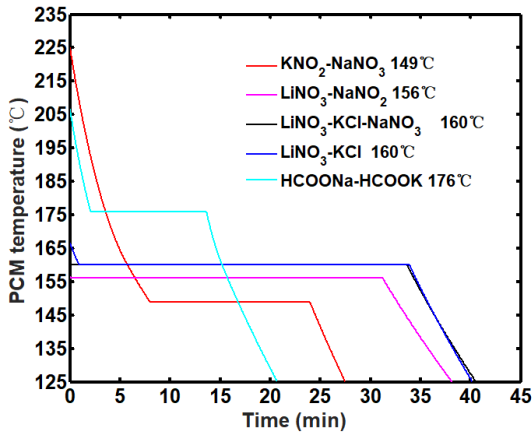


**Fig. 6.** Performance of the LTES with different PCMs during the charging process

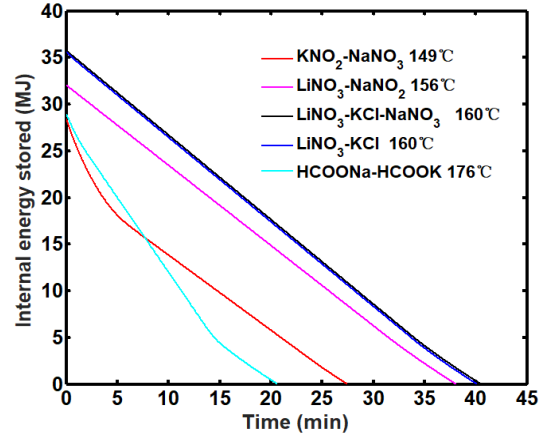
( $T=250\text{ }^\circ\text{C}$ )

- 1 Case 1:  $T=250\text{ }^\circ\text{C}$ ,  $m=0.2\text{ kg/s}$
- 2 The performance of the PCMs in the charging process has been illustrated in Fig. 6. Results
- 3 indicate within 60 minutes charging time,  $\text{KNO}_2\text{-NaNO}_3$  and  $\text{HCOONa-HCOOK}$  have the
- 4 same maximum storage temperature ( $225\text{ }^\circ\text{C}$ ) because of their small latent heat and specific
- 5 capacity while  $\text{LiNO}_3\text{-NaNO}_2$  has the minimum storage temperature ( $156\text{ }^\circ\text{C}$ ) due to its large
- 6 latent heat and specific capacity as shown in Fig. 6 (a).  $\text{LiNO}_3\text{-KCl}$  and  $\text{LiNO}_3\text{-KCl-NaNO}_3$
- 7 have similar physical parameters with large latent heat, so they can store heat isothermally for
- 8 a longer period as shown in Fig. 6 (a), and they can keep a lower average temperature in the
- 9 charging process, which is beneficial for the heat transfer process. As indicated in Fig. 6 (b),
- 10 PCMs with larger latent heat can store more heat in the charging process. Compared to
- 11  $\text{KNO}_2\text{-NaNO}_3$  and  $\text{HCOONa-HCOOK}$ ,  $\text{LiNO}_3\text{-NaNO}_2$ ,  $\text{LiNO}_3\text{-KCl}$  and  $\text{LiNO}_3\text{-KCl-NaNO}_3$
- 12 indicate lower maximum temperature and larger stored heat, which means these three PCMs

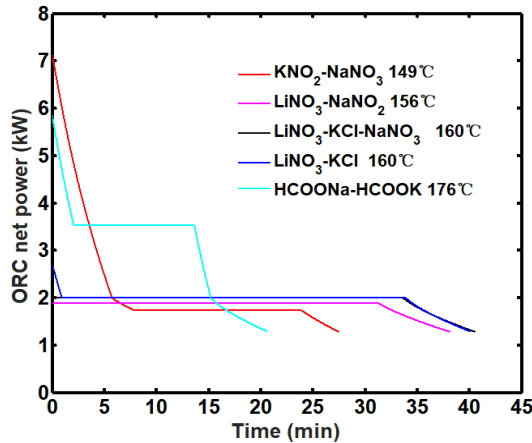
- 1 can maintain a steady LTES temperature for a longer time and have fewer heat losses in the
- 2 charging process and is suitable for ORC system to working under the designed point.



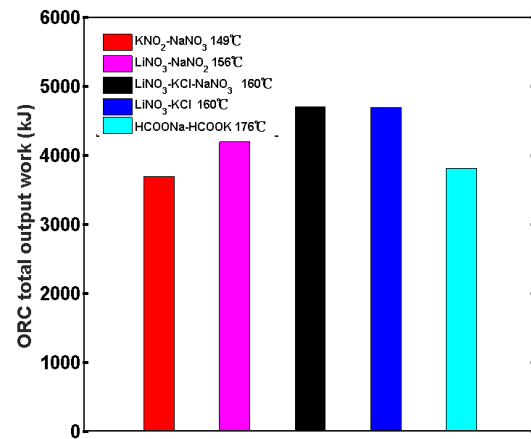
(a) PCM temperature evolution



(b) Internal energy released from PCM



(c) ORC power output

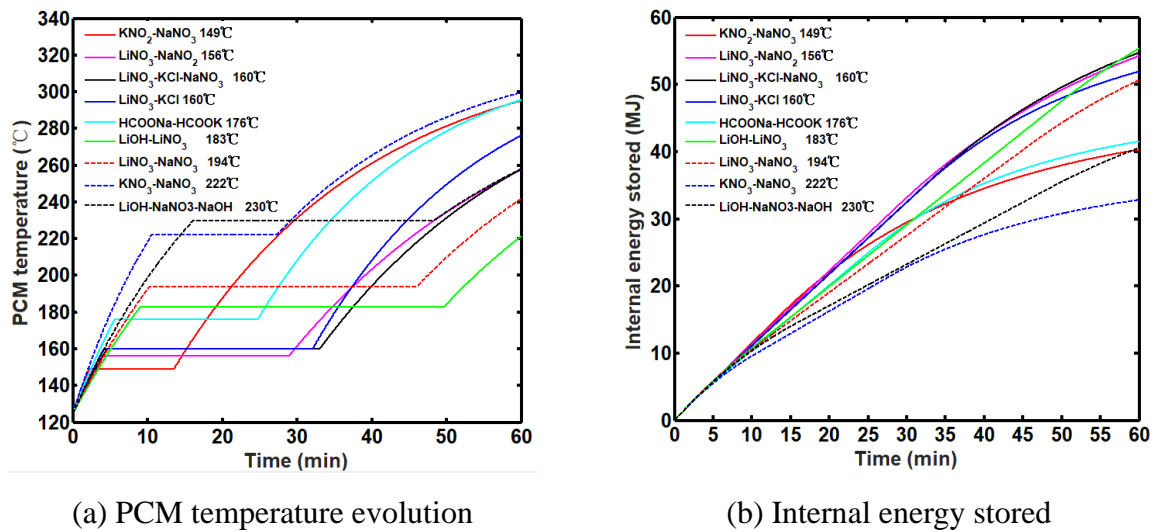


(d) ORC total power output

**Fig. 7.** Performance of the LTES with different PCMs in the discharging process ( $T=250\text{ }^{\circ}\text{C}$ )

- 3 Fig. 7 illustrates the performance of the PCMs in the discharging process. Results indicate the
- 4 duration of discharging time for  $\text{LiNO}_3\text{-KCl-NaNO}_3$  (41 min),  $\text{LiNO}_3\text{-KCl}$  (40.7 min) and
- 5  $\text{LiNO}_3\text{-NaNO}_2$  (36 min) and are longer than that of  $\text{KNO}_2\text{-NaNO}_3$  (27 min) and
- 6  $\text{HCOONa-HCOOK}$  (21 min). As shown in Fig. 7(c) it can be concluded that higher LTES
- 7 temperatures would result in higher initial power outputs at the start of the ORC operation

1 period due to the increased evaporating temperature of ORC working fluid. The total-work  
 2 output and the duration of the operating period are higher for the materials with the lower  
 3 storage temperatures as the results plotted in Fig. 7 (d). Therefore,  $\text{LiNO}_3\text{-KCl-NaNO}_3$  is the  
 4 most suitable PCM among the five PCMs due to its longest duration of the operating period and  
 5 largest total work output.

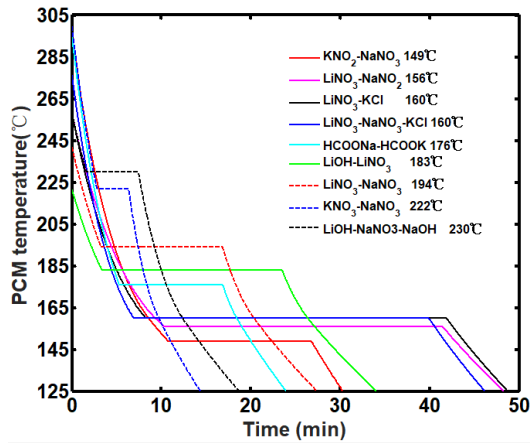


**Fig. 8.** Performance of LTES with different PCMs in the charging process ( $T=325\text{ °C}$ )

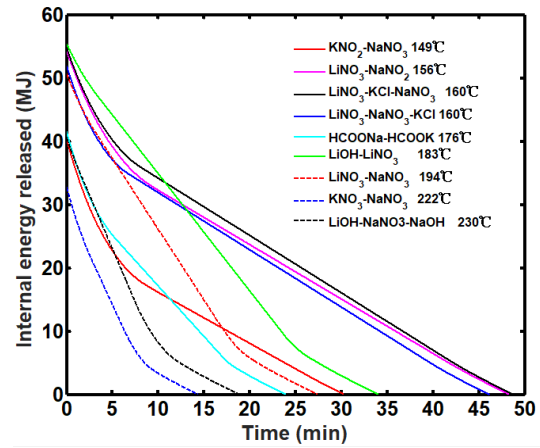
6 Case 2:  $T=325\text{ °C}$ ,  $m=0.2\text{ kg/s}$

7 In order to find out proper materials for this case, PCMs studied in case 1 were also  
 8 considered in this case and the PCMs with higher melting temperature were included. In Fig.  
 9 8, it can be found that the latent heat is the dominant factor that determines the duration of the  
 10 discharging process and the final storage temperature among the selected PCMs.  
 11  $\text{NaNO}_3\text{-KNO}_3$  shown the highest final storage temperature because of its smallest latent heat  
 12 and it stored the minimal heat during the charging process. The final storage temperature of  
 13  $\text{KNO}_2\text{-NaNO}_3$  and  $\text{HCOONa-HCOOK}$  were close to that of  $\text{NaNO}_3\text{-KNO}_3$ .

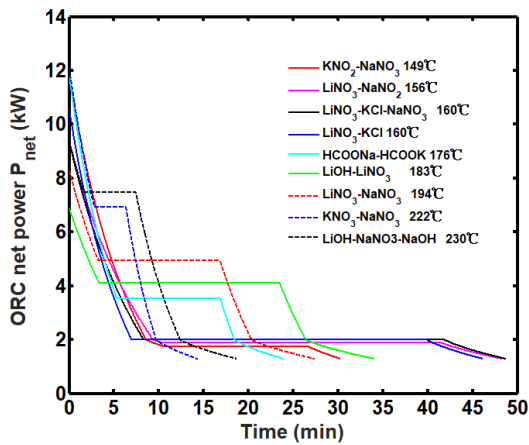
1 LiOH-NaNO<sub>3</sub>-NaOH stores the second smallest heat because it maintains the relatively high  
2 average temperature in the charging process although it has the medium latent heat resulting  
3 in medium final storage temperature, which is not beneficial for the heat transfer between the  
4 PCM and the exhaust. The temperature evolution of LiNO<sub>3</sub>-KCl is almost the same as that of  
5 LiNO<sub>3</sub>-KCl-NaNO<sub>3</sub> before they completely melt due to the similar latent heat and specific heat  
6 capacity at solid state as shown in Fig. 8 (a). However, LiNO<sub>3</sub>-KCl-NaNO<sub>3</sub> experiences a lower  
7 storage temperature and stores more heat than that of LiNO<sub>3</sub>-KCl, because LiNO<sub>3</sub>-KCl-NaNO<sub>3</sub>  
8 have a larger specific heat capacity at liquid state compared to LiNO<sub>3</sub>-KCl. Results also  
9 indicate LiNO<sub>3</sub>-NaNO<sub>2</sub> has a slightly smaller latent heat, but larger specific heat capacity  
10 compared with the above two PCMs. Therefore, it has approximately the same temperature  
11 evolution performance as LiNO<sub>3</sub>-KCl and LiNO<sub>3</sub>-KCl-NaNO<sub>3</sub>. NaNO<sub>3</sub>-LiNO<sub>3</sub> has almost  
12 equal latent heat but higher melting temperature to that of LiNO<sub>3</sub>-KCl and  
13 LiNO<sub>3</sub>-KCl-NaNO<sub>3</sub>. It experiences lower final storage temperature and it stores less heat in the  
14 charging process. The storage temperature of LiOH-LiNO<sub>3</sub> is lowest among all the PCMs, but  
15 it stores the most heat during the charging process since it possesses the much larger latent  
16 heat than among the selected materials.



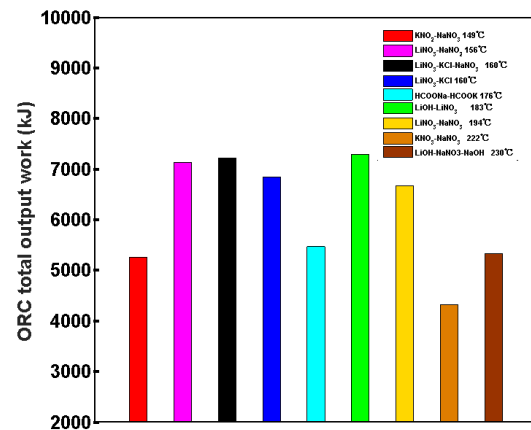
(a) PCM temperature evolution



(b) Internal energy released from PCM



(c) ORC power output

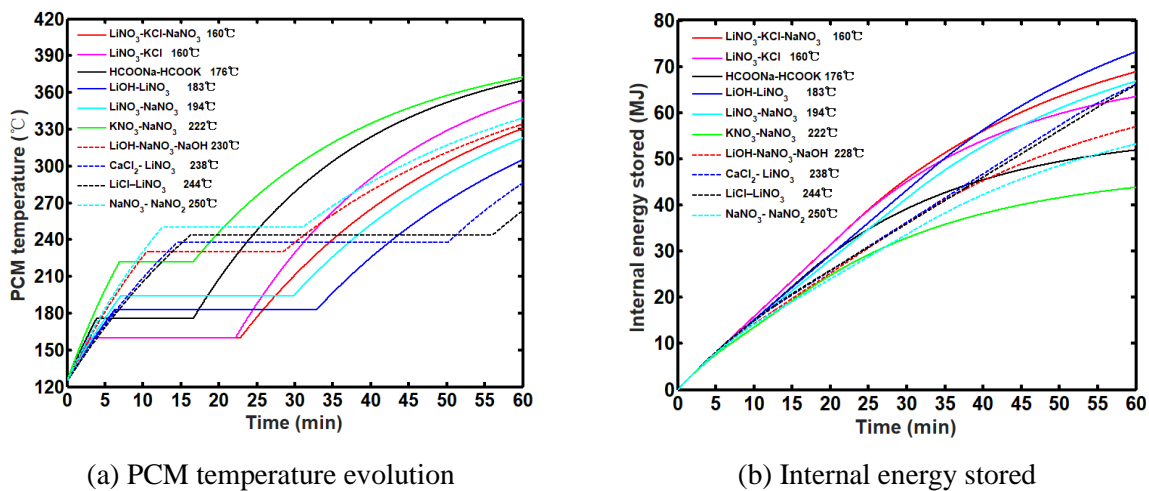


(d) ORC total power output

**Fig. 9.** Performance of the LTES with different PCM in the discharging process ( $T=325\text{ }^{\circ}\text{C}$ )

1 As shown in Fig. 9,  $\text{LiNO}_3\text{-KCl-NaNO}_3$  (48.8 min) has the longest duration of the  
 2 discharging process among all the candidates. PCMs such as  $\text{LiNO}_3\text{-NaNO}_2$  (48.3 min),  
 3  $\text{LiNO}_3\text{-KCl}$  (46.2 min) and  $\text{LiOH-LiNO}_3$  (34.1 min), who has large latent heat and low  
 4 melting temperature, shown better performance on the ORC operating duration than that of  
 5 other candidates. ORC evaporating temperature is determined by the PCM temperature and  
 6 pinch point temperature difference in the discharging process. Therefore, lower ORC  
 7 evaporating temperature can result in lower demand for PCM temperature and potentially

1 store more heat, which can maintain the ORC operation time to be longer. The performance  
 2 of ORC power output has been shown in Fig. 9 (c). LiOH-LiNO<sub>3</sub> generates the maximum total  
 3 power output among all the selected PCMs. LiNO<sub>3</sub>-KCl-NaNO<sub>3</sub>, LiNO<sub>3</sub>-NaNO<sub>2</sub> and  
 4 LiNO<sub>3</sub>-KCl rank second, third and fourth, all of which are slightly smaller (1.1%, 2.3% and  
 5 6.1%, respectively) than LiOH-LiNO<sub>3</sub>. The above three PCMs have longer ORC operating  
 6 duration than LiOH-LiNO<sub>3</sub>, which means they can stably deliver power for a long time for  
 7 utilisation. Considering the ORC operating duration and total power output,  
 8 LiNO<sub>3</sub>-KCl-NaNO<sub>3</sub> is identified as the optimal candidate in this case study.

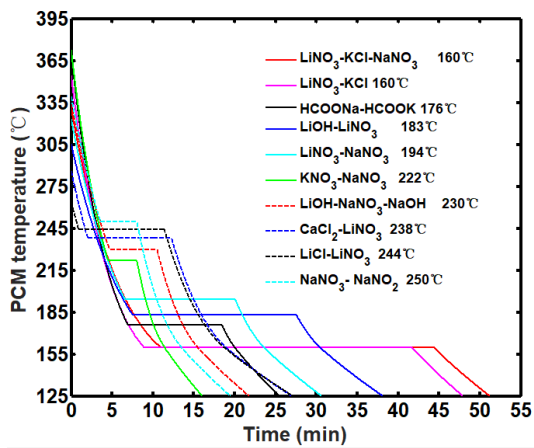


**Fig. 10.** Performance of LTES with different PCM in the charging process ( $T=400\text{ }^{\circ}\text{C}$ )

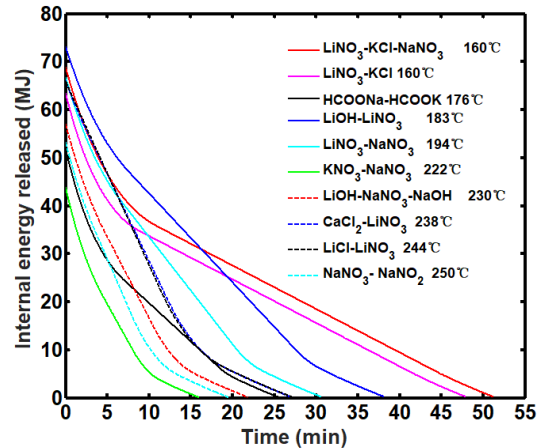
9 Case 3:  $T=400\text{ }^{\circ}\text{C}$ ,  $m=0.2\text{ kg/s}$

10 In this case, PCMs with higher melting temperature were studied while PCMs with low  
 11 melting temperature studied in case 2 were excluded because of the increase in exhaust  
 12 temperature. As previously discussed in case 1 and 2, PCM that has large latent heat and low  
 13 melting temperature experience lower final storage temperature and store more heat. PCMs

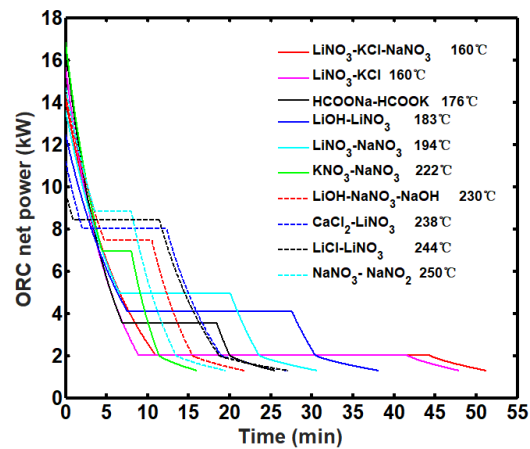
1 with large latent heat such as  $\text{LiCl-LiNO}_3$  (263 °C),  $\text{CaCl}_2\text{-LiNO}_3$  (286 °C),  $\text{LiOH-LiNO}_3$   
 2 (305 °C),  $\text{NaNO}_3\text{-LiNO}_3$  (322 °C) and  $\text{LiNO}_3\text{-KCl-NaNO}_3$  (330 °C) shown lower final  
 3 storage temperature and store more heat than other PCMs in the charging process as  
 4 illustrated in Fig. 10 (a) and (b). However,  $\text{LiOH-LiNO}_3$  and  $\text{LiNO}_3\text{-KCl-NaNO}_3$  shown  
 5 better heat storage ability than that of  $\text{LiCl-LiNO}_3$ ,  $\text{CaCl}_2\text{-LiNO}_3$  and  $\text{LiOH-LiNO}_3$ . Results  
 6 indicate other PCMs would lead to higher final storage temperature and store less heat since  
 7 they have improper latent heat and melting temperature in the operational conditions of the  
 8 case study.



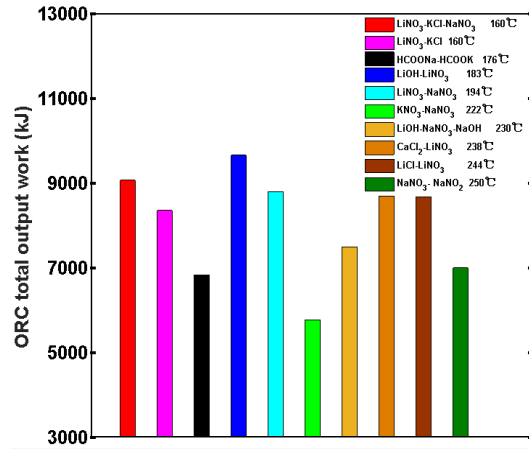
(a) PCM temperature evolution



(b) Internal energy released from PCM



(c) ORC power output



(d) ORC total power output

**Fig. 11.** Performance of the LTES with different PCM in the discharging process ( $T=400$  °C)

1 Fig. 11 illustrated the performance of different PCM during the discharging process. ORC  
2 operating duration of  $\text{LiNO}_3\text{-KCl-NaNO}_3$  (51.2 min),  $\text{LiNO}_3\text{-KCl}$  (47.9 min) and  
3  $\text{LiOH-LiNO}_3$  (38.1 min) are longer than other candidates. Although PCMs such as  
4  $\text{CaCl}_2\text{-LiNO}_3$  (26.9 min) and  $\text{LiCl-LiNO}_3$  (27.1 min) possesses large latent heat, their melting  
5 temperature is quite high, leading to higher evaporating temperature and larger mass flow rate  
6 of ORC working fluid. Therefore, the stored heat can be discharged faster and the ORC  
7 working duration is shorter. Other PCMs with small latent heat including  $\text{NaNO}_3\text{-KNO}_3$  (16.0  
8 min),  $\text{NaNO}_3\text{-NaOH}$  (19.5 min) and  $\text{LiOH-NaNO}_3\text{-NaOH}$  (21.8 min) shows the shortest ORC  
9 working duration. In terms of the total ORC power output,  $\text{LiOH-LiNO}_3$  delivers the largest  
10 total power output because of its largest latent heat and low melting temperature. The total  
11 power output of  $\text{LiNO}_3\text{-KCl-NaNO}_3$  is slightly smaller (about 5.5%) than that of  
12  $\text{LiOH-LiNO}_3$ . Compared to case 2, the difference in total power output between  
13  $\text{LiNO}_3\text{-KCl-NaNO}_3$  and  $\text{LiOH-LiNO}_3$  is increased from 1.1% to 5.5%. However, the  
14 difference of total power output between  $\text{NaNO}_3\text{-LiNO}_3$  and  $\text{LiNO}_3\text{-KCl-NaNO}_3$  is decreased  
15 from 7.5% to 3.0%, which indicates that the most proper melting temperature of PCM  
16 increases with the improvement of heat source temperature. PCMs with lower melting  
17 temperature melt faster with the increase of heat source due to higher final storage  
18 temperature is shown in Fig. 8 (a) and Fig. 10 (a). For  $\text{LiNO}_3\text{-KCl-NaNO}_3$  and  $\text{LiNO}_3\text{-KCl}$ ,  
19 the difference of total power output between them is also enlarged compared to that of case 2,  
20 because  $\text{LiNO}_3\text{-KCl-NaNO}_3$  has larger specific heat capacity in the liquid state. Considering



1 ORC operating duration and total power output as well as the temperature range of heat source  
2 conditions for engine exhaust heat recovery,  $\text{LiNO}_3\text{-KCl-NaNO}_3$  is expected to have better  
3 comprehensive performance.

4 It can be summarised that PCM with large latent heat and low melting temperature can store a  
5 large amount of heat in the charging process and have low final storage temperature.

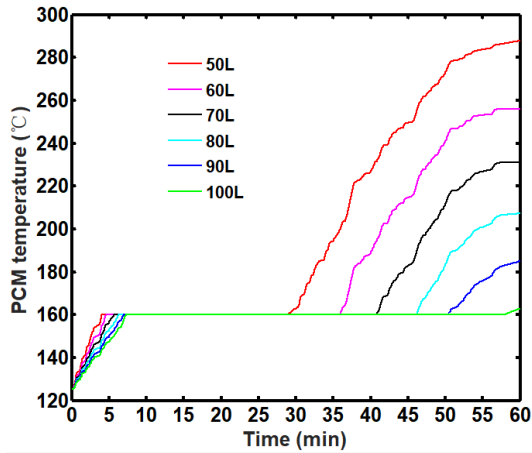
6 Moreover, the PCMs held the stated characteristics can produce long ORC operating duration  
7 and large total power output. Under the three case study conditions,  $\text{LiNO}_3\text{-KCl-NaNO}_3$  is  
8 proved to be the most suitable PCM among all the studied PCMs.  $\text{LiNO}_3\text{-KCl-NaNO}_3$   
9 delivers the highest total ORC output and has the longest ORC working duration in case 1.

10 Although  $\text{LiOH-LiNO}_3$  delivers the highest total power output both in case 2 and 3, its ORC  
11 working durations are only 34.1 min and 38.1 min. For  $\text{LiNO}_3\text{-KCl-NaNO}_3$ , the total ORC  
12 power output in case 2 and 3 is merely 1.1% and 5.5% smaller than that of  $\text{LiOH-LiNO}_3$ .

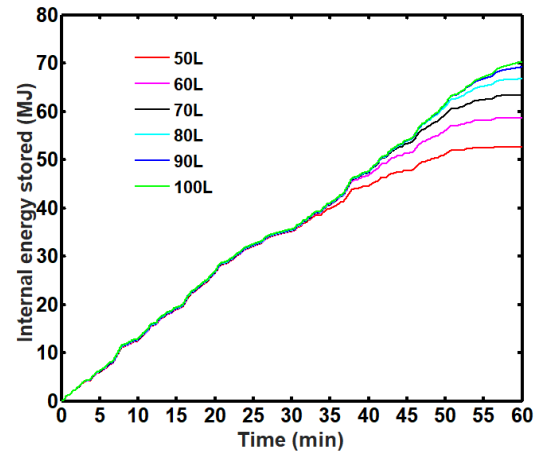
13  $\text{LiNO}_3\text{-KCl-NaNO}_3$  has the longest ORC working duration for 48.8 min and 51.2 min in case 2  
14 and 3, respectively. Therefore, the following section investigated the PCM-based ORC system  
15 under dynamic heat source conditions using  $\text{LiNO}_3\text{-KCl-NaNO}_3$  as the phase change material.

#### 16 **4.2 System performance under dynamic heat source conditions**

17 Based on this dynamic heat source shown in Fig. 5, the performance of ORC with LTES was  
18 simulated and analysed. The charging process and discharging process of LTES using  
19  $\text{LiNO}_3\text{-KCl-NaNO}_3$  under this dynamic heat source were investigated.



(a) PCM temperature evolution

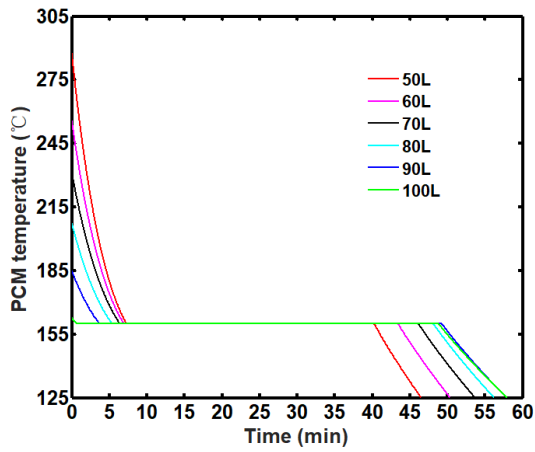


(b) Internal energy stored by PCM

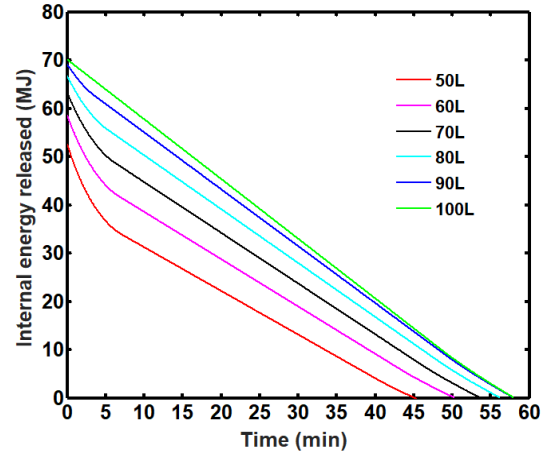
**Fig. 12.** Temperature evolutions and internal energy stored by  $\text{LiNO}_3\text{-KCl-NaNO}_3$  under different LTES volume

1 Fig. 12 shows the temperature evolution and internal energy stored by  $\text{LiNO}_3\text{-KCl-NaNO}_3$   
 2 under different LTES volume. The larger LTES volume means the heavier weight of PCM  
 3 and larger heat transfer area between the exhaust and PCM. As shown in Fig. 12(a), it can be  
 4 found that the final heat storage temperature decreases with the increase of the LTES volume.  
 5 The final storage temperature of LTES with a volume of 100L is 162.8 °C while it is 287.8 °C  
 6 for LTES with a volume of 50 L. Due to the phase change process of PCM, the large  
 7 fluctuation of engine exhaust can be significantly reduced, which is beneficial to the waste  
 8 heat recovery using ORC. Meanwhile, the duration of constant temperature has a positive  
 9 correlation to the LTES volume. When the duration of the melting process is longer, the  
 10 duration of sensible heat storage process can be shorter. Furthermore, during sensible heat  
 11 storage processes, the great fluctuation of the heat source is also reduced despite some little  
 12 irregularity of temperature evolution. Results in Fig. 12 (b) indicate the total internal energy  
 13 stored by LTES increases with the rise of the LTES volume but the increase rate is reduced. It

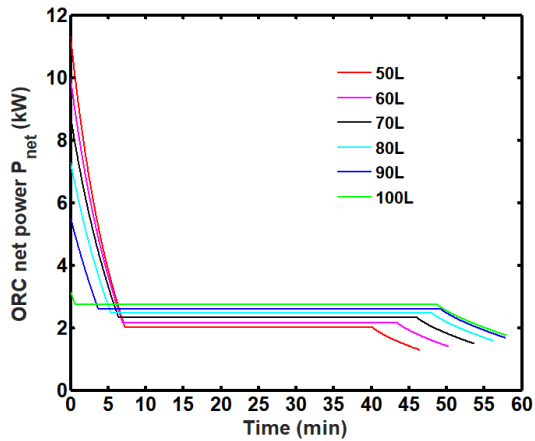
1 can, therefore, be concluded that the volume of LTES should be properly designed in order to  
 2 obtain low final storage temperature and store a high amount of heat considering the  
 3 requirement of the low cost of LTES devices and compactness.



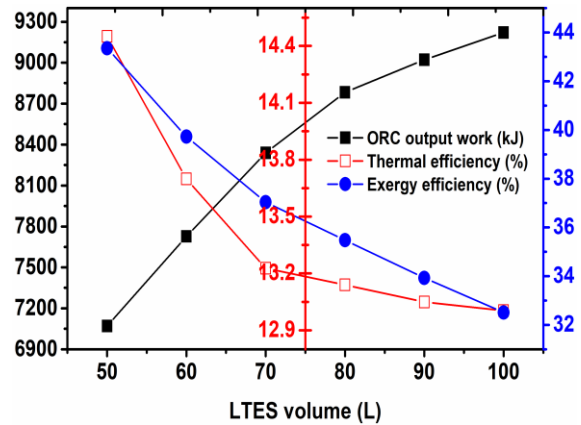
(a) PCM temperature evolution



(b) Internal energy released by PCM



(c) ORC power output  $P_{net}$ .



(d) Output work, thermal and exergy efficiency

**Fig. 13.** Performance of the LTES with  $\text{LiNO}_3\text{-KCl-NaNO}_3$  under different LTES volume in the discharging process

4 Fig. 13 illustrates the performance of ORC under different LTES volumes during the  
 5 discharging process. The temperature evolution in the discharging process shown in Fig. 13  
 6 (a) indicates that LTES maintains a constant temperature in most of the time because of the

1 solidification process under. Furthermore, the duration of constant temperature increases with  
2 the LTES volume without exceeding 90 L, but the increase rate of duration decreases as the  
3 LTES volume increase. The ORC system could work under steady state as a result of the  
4 relatively constant temperature of PCM, which is depicted in Fig. 13 (b) and (c). The net  
5 power of the ORC system under each condition first decreases in the sensible heat  
6 discharging process of liquid PCM, then it maintains constant during the solidification  
7 process of PCM. Once the solidification process is completed, it continues to decrease until  
8 the PCM temperature is close to the driving temperature of ORC in the sensible heat  
9 discharging process of solid PCM. ORC system can deliver the largest net power of 2.74 kW  
10 for about longest time of 48.2 min in the condition of 100 L while the value is 2.00 kW for  
11 about shortest time of 33.6 min in the condition of 50 L. The total output work of ORC,  
12 thermal efficiency and exergy efficiency in the whole discharging process are shown in Fig.  
13 13 (d). It can be found that the total output work improves with the increase of LTES volume,  
14 which is because the total internal energy stored by LTES increases with the rise of the LTES  
15 volume, but the increase rate is reduced. The condition of 100 L LTES provides 30.4% larger  
16 total output work than that of 50 L LTES, while it is merely 1.5% larger than that of 90 L  
17 LTES. 50-L LTES corresponds the maximum thermal and exergy efficiency while the 100-L  
18 LTES leads to the minimum ones. The reason is due to the final storage temperature of LTES  
19 shown in Fig. 12(a). The higher LTES temperature during the ORC working process  
20 (discharging process) can lead to larger thermal efficiency and exergy efficiency because of  
21 higher evaporating temperature. In addition, the thermal efficiency and exergy efficiency both  
22 decrease with the increase of LTES volume.

### 23 **4.3 Performance comparison of double and single LTES**

24 The previous investigations and analysis are based on single LTES. However, single LTES  
25 could not absorb heat from the exhaust gas and release heat to ORC working fluid at the same  
26 time because heat fluxes between both sides are not balanced and the temperature of LTES

1 cannot be easily monitored and controlled. The proposed solution is to adopt double LTES,  
 2 which can store excess thermal energy and releases it on demand. Three operating modes  
 3 listed in Table 3 for single LTES and double LTES are designed to evaluate and compare the  
 4 performances of different ORC systems. LTES in all the operating modes is assumed to be  
 5 the solid state with an initial temperature of 125 °C. The dynamic heat source is shown in Fig.  
 6 11 is assumed to be a periodic heat source with the period of 30 min in this section.

7 **Table 3.** Design and description of different modes for LTES

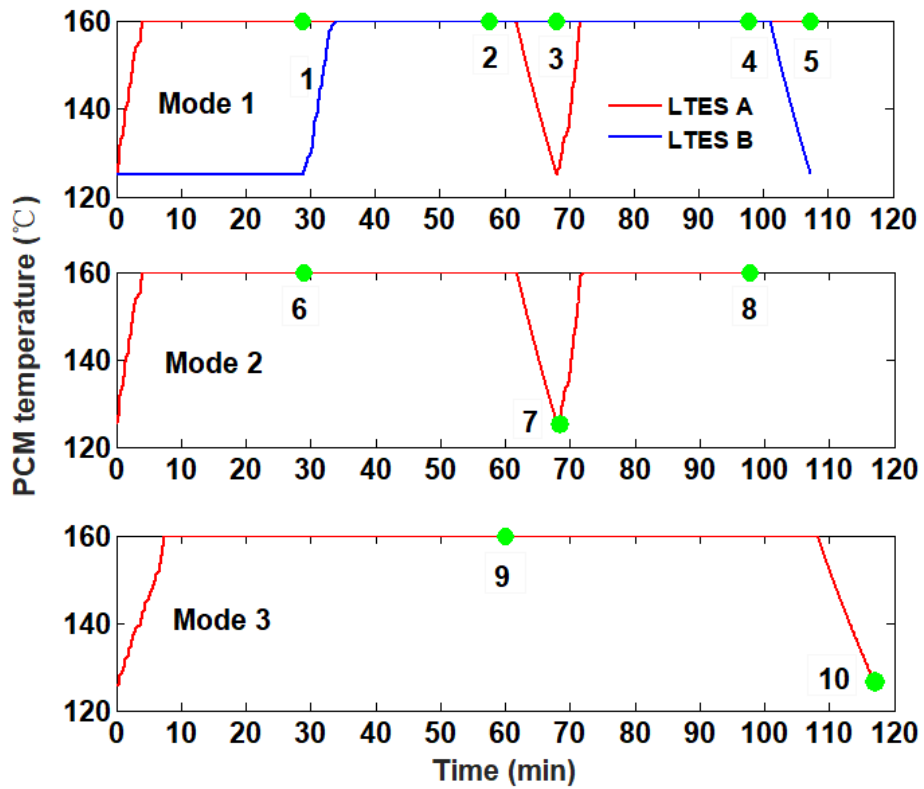
Modes	LTES Volume	LTES Number	Descriptions
Mode 1	50L (A)+50L (B)	Double	Discharging process of LTES A (B) starts when the PCM fully melts and charging process of LTES B (A) starts at the same time. The charging process for both A and B starts when the temperature of PCM decreases to 125 °C. That is, the charging process and discharging process for LTES A and B operate alternatively.
Mode 2	50L	Single	Discharging process starts when the PCM fully melts and the charging process starts when the temperature of PCM decreases to 125 °C.
Mode 3	100L	Single	Discharging process starts when the PCM fully melts and the charging process starts when the temperature of PCM decreases to 125 °C.

8 Fig. 14 shows the performance of LTES and ORC system for three different modes in an  
 9 integrated charging-discharging period. As for PCM temperature as shown in Fig. 14 (a), in  
 10 mode 1, LTES A first enters the charging process and LTES B waits for the start of charging

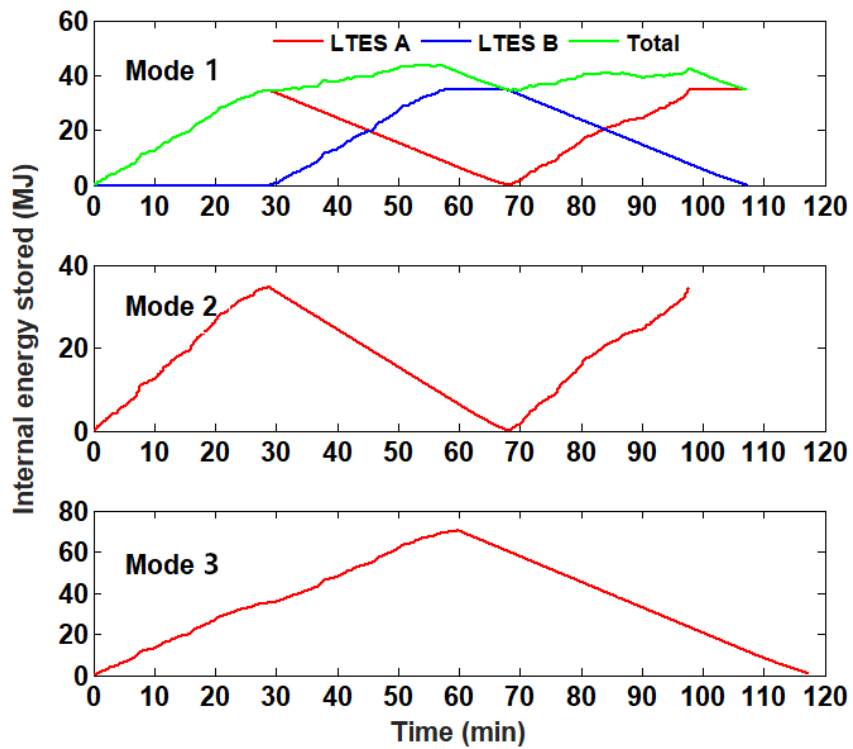
1 process till the charging process of LTES A completes (Time elapsed from  $t_0$  to  $t_1$ ). Then  
2 LTES A starts its discharging process and ORC system starts recovering stored heat (from  $t_1$   
3 to  $t_3$ ). LTES B starts its charging process at  $t_1$  and ends at  $t_2$  and from  $t_2$  to  $t_3$  it does not store  
4 heat. From  $t_3$  to  $t_4$  LTES A is during charging process while LTES B is during the discharging  
5 process. The whole process lasts for 107.3 min and ORC system works from  $t_1$  to  $t_5$  for 78.6  
6 min. In mode 2, the charging process of LTES ends at  $t_6$  and the discharging process finishes  
7 at  $t_7$  (68.1 min). Considering the period of mode 2 is shorter than that of mode 1, LTES in  
8 mode 2 is assumed to continue experiencing an integrated charging process from  $t_7$  to  $t_8$  (97.7  
9 min). The working duration of the ORC system is about 39.3 min. In mode 3, the charging  
10 process and discharging process last from  $t_0$  to  $t_{10}$  (117.4 min), while the ORC system  
11 recovers waste heat for 59.9 min. The ORC working duration of mode 1 is significantly  
12 higher than that of mode 2 and 3, which means ORC system in mode 1 can deliver effective  
13 work for a longer period and can be easier to meet the demand of users.

14 In terms of the internal energy stored by LTES as shown in Fig. 14 (b), the energy stored by  
15 LTES A and B in mode 1 first increases and then it decreases due to the switch between LTES  
16 A and B for charging and discharging process. The total internal energy stored by LTES A  
17 and B is relatively uniform and keeps above 35 MJ after the first charging process, which  
18 means the ORC system can be steadily operated within the designed conditions. In mode 2  
19 the evolution of energy stored by LTES is the same as that of LTES A in mode 1, which  
20 changes with elapsed time periodically leading to the intermittent operation of the ORC  
21 system. The evolution of energy stored by LTES in mode 3 is similar to that of mode 2.

1 The results of ORC net power output are shown in Fig. 14 (c). In mode 1, the ORC system  
2 delivers an average net power of 2.0 kW for 78.6 min. In mode 3, ORC system delivers an  
3 average net power of 2.7 kW for 59.9 min due to the LTES volume of mode 3 is larger than  
4 that of mode 1, which leads to larger heat transfer area and more energy stored. In mode 2,  
5 ORC net power output is the same as that of LTES A in mode 1. As the period of mode 2 is  
6 shorter than that of mode 1, ORC net power output can last for a longer duration after  $t_8$ , but  
7 ORC working duration is still shorter than that of mode 1. Fig. 14 (d) shows the ORC total  
8 output work in an integrated period for three different modes. In mode 1, the power output  
9 increase after the first discharging process and reaches 9.125 MJ during a period of 107.3 min.  
10 The ORC output work in mode 2 is about 4.557 MJ. In mode 3, the total ORC output work  
11 can attain 9.123 MJ at 117.4 min, which is slightly lower than that of mode 1 at 9.125 MJ.  
12 However, within the designed period  $t_{11}$ , the ORC total power output of mode 1 is 17.2%  
13 higher than that of mode 3.

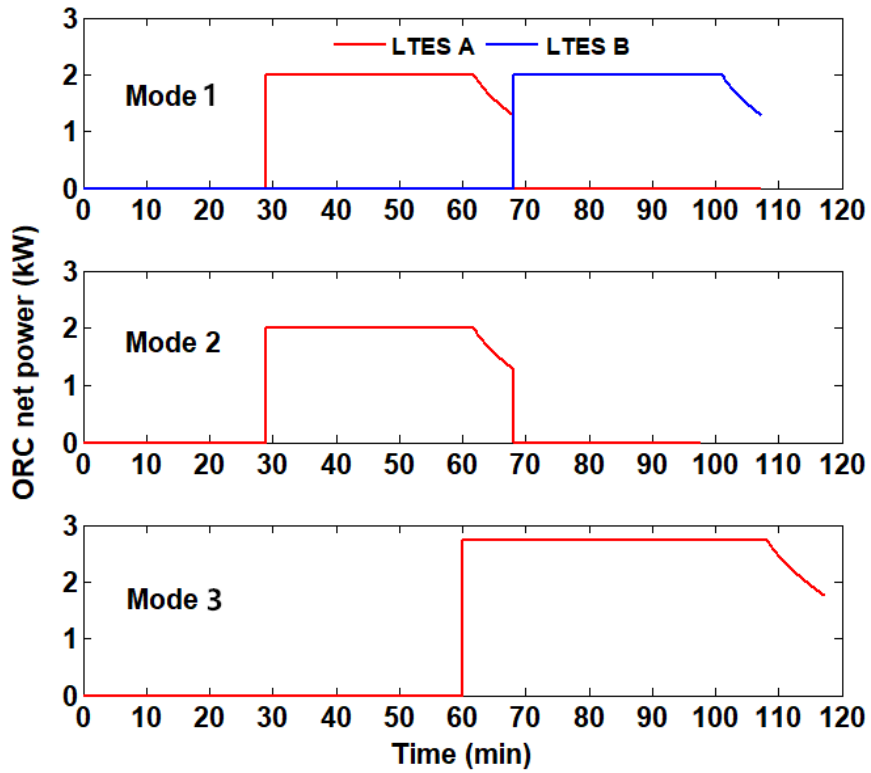


(a) Temperature evolution of LTES for three different modes

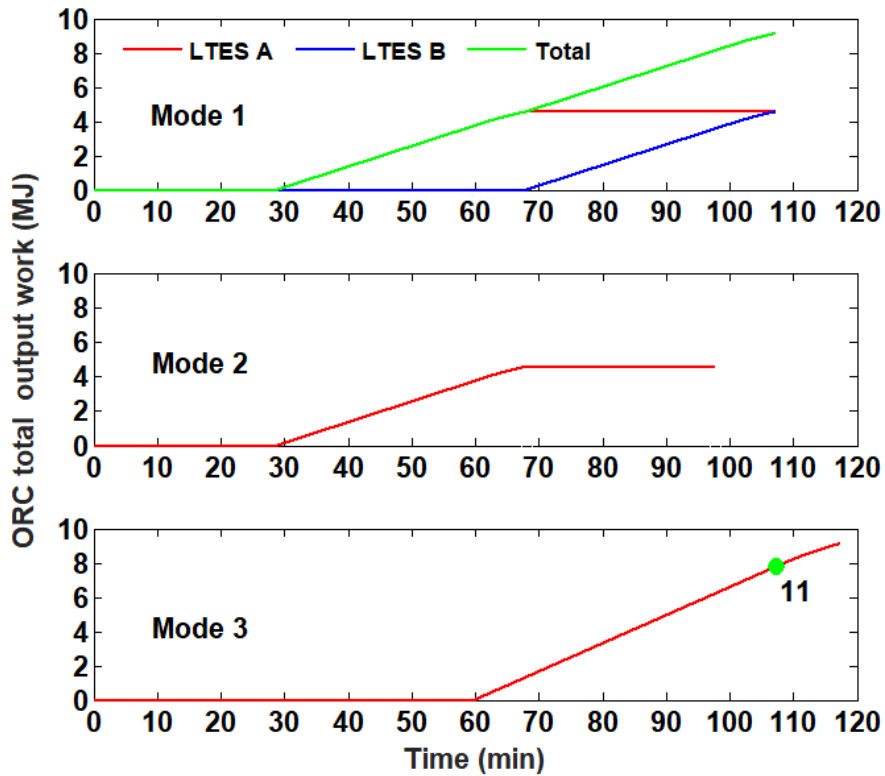


(b) Internal energy evolution of LTES for three different modes





(c) ORC net power output with time for three different modes



(d) Total ORC output work with time for three different modes

**Fig. 14.** Performances of LTES and ORC system for three different modes

#### 1 **4.4 Discussion on practical differences and costs**

2 This section provides a short discussion about the practical differences and costs among the  
3 three different operating modes studied in section 4.3. For each mode, the size and  
4 investment for ORC are almost the same. For mode 1 and 2, the main difference between  
5 them is the amount of LTES tanks. The initial research and development of a 50-L LTES tank  
6 for mode 1 and mode 2 is the same, but the total initial investment for the whole system of  
7 mode 1 is larger than that of mode 2 since an additional LTES tank and auxiliary pipes are  
8 needed. Considering the much larger ORC total output work and working duration over a  
9 charging-discharging period, mode 1 is recommended because of its shorter payback time. As  
10 for mode 1 and mode 3, the LTES tank volume of mode 1 (50 L) is smaller than that of mode  
11 3 (100 L), leading to a lower initial expenditure during the research and development process.  
12 Although the total LTES volume is equal to the that of mode 3, the whole initial investment  
13 for mode 1 is also lower than that of mode 3, because the scientific research and development  
14 expenditure for a new product is much higher than its commercialized price. In addition, the  
15 total output work of ORC for mode 1 is 9.125 MJ during a period of 107.3 min while it is  
16 9.123 MJ for mode 3 during a period of 117.4 min, the corresponding ORC working  
17 durations for mode 1 and mode 3 are 78.6 min and 59.3 min, respectively. Therefore, mode 1  
18 is more potential for engine waste heat recovery than mode 3. In conclusion, mode 1  
19 possesses comprehensively larger total ORC output work and longer working duration than  
20 those of mode 2 and 3. Therefore, mode 1 is recommended among the three operating modes.

## 1 **5. Conclusions**

2 This paper investigated the potential application of PCM-based ORC system in order to  
3 overcome the fluctuation of the vehicle engine heat source. Performance of ORC system  
4 integrated LTES were evaluated under steady and dynamic heat source conditions. The  
5 investigation of the ORC system under different LTES volume and ORC-LTES modes were  
6 studied. This research has effectively supplemented the knowledge about the potential  
7 application of ORC system integrated with double LTES for engine waste heat recovery. Key  
8 findings could be drawn as follows,

9 (1) PCMs with large latent heat and low melting temperature indicated a lower final  
10 storage temperature and store more heat in the charging process. During the  
11 discharging process, the PCMs held the stated characteristic could have longer ORC  
12 operating duration and larger total output work. Results indicated among the selected  
13 PCM candidates,  $\text{LiNO}_3\text{-KCl-NaNO}_3$  is the optimal thermal energy storage material  
14 considering its longest ORC operating duration and almost the largest ORC total  
15 output work.

16 (2) Results under dynamic heat source showed that the large fluctuation of engine heat  
17 source can be significantly reduced due to the phase change process of PCM. ORC  
18 net power and duration of delivering constant net power increase with the increase of  
19 LTES volume. 100 L LTES can improve the ORC total output work by 30.4% than  
20 that of 50 L. However, ORC output from 100 L LTES is only 1.5% higher than that of

1 90 L, which means optimal design methods should be adopted under targeted  
2 dynamic heat source conditions.

3 (3) Mode 1 (double LTES, 50 L+50 L) has the best comprehensive performance while  
4 Mode 2 (single LTES, 50 L) is the worst. The proposed double LTES (Mode 1)  
5 solution can steadily generate power from the ORC system and the Mode 1 can store  
6 the internal energy more uniform than that of Mode 2 and 3. The solution can  
7 effectively overcome the intermittent problem of single LTES system. The power  
8 output from ORC in Mode 1 delivers an average net power of 2.0 kW for 78.6 min in  
9 a period of 107.3 min while in Mode 3 it is 2.7 kW for 59.9 min in a period of 117.4  
10 min. At the end of 2 hours operational time, the ORC total output work from Mode 3  
11 can achieve 9.125 MJ, which is slightly higher than that of Mode 1 at 9.123 MJ.  
12 However, when the time is set at the designed condition for Mode 1, the ORC total  
13 output work of Mode 1 is 17.2% larger than that of Mode 3.

## 14 **6. Suggestion for the future work**

15 The proposed organic Rankine cycle integrating with double latent thermal energy storage  
16 (LTES) is a potential solution to overcome the fluctuation and intermittence of engine exhaust  
17 energy. In this work, the effects of different PCMs and LTES volume are preliminarily  
18 investigated to demonstrate the feasibility of the proposed system. In addition to the stated  
19 parameters, other important technical parameters include: (1) the design and optimisation of  
20 highly efficient thermal energy storage heat exchanger to meet the requirements of

1 compactness for transport application. This involves designing a compact latent thermal energy  
2 storage, achieving a perfect combination with heat exchanger and phase change materials.  
3 Relatively high energy storage density and heat transfer rate (charging-discharging rate) are the  
4 main technical barriers. (2) Operating and control strategy of the system is also a crucial factor  
5 to adapt to the variation of heat source and energy demand under different driving conditions,  
6 realising the high energy utilisation efficiency of the whole system. The characteristics of the  
7 engine exhaust gas are much distinguishing under different driving conditions (urban and  
8 suburban conditions). Therefore, PCM selection, ORC working fluid selection and switch  
9 strategy of double LTES should be further optimised according to the objective driving  
10 conditions.

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