# Monte-Carlo simulation of photoproduction of Omega meson 

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# MONTE-CARLO SIMULATION OF PHOTOPRODUCTION OF OMEGA MESON 

By<br>Parikshit M. Junnarkar

A Thesis<br>Submitted to the Faculty of<br>Mississippi State University<br>in Partial Fulfillment of the Requirements<br>for the Degree of Master of Science<br>in Physics<br>in the Department of Physics and Astronomy

Mississippi State, Mississippi
December 2006

By<br>Parikshit M. Junnarkar

Approved:

Dr. James Dunne
Associate Professor of Physics and
Astronomy
(Major Professor)

Dr. Jeff Winger
Professor of Physics
and Astronomy
(Committee Member)

Dr. Wenchao Ma
Professor of Physics and
Astronomy
(Committee Member)

Dr. David Monts
Professor of Physics and
Astronomy
and Graduate Coordinator, Department of Physics and Astronomy

Phillip B. Oldham
Dean of
the College of
Arts and Sciences

Name: Parikshit M. Junnarkar

Date of Degree: December 9, 2006
Institution: Mississippi State University
Major Field: Physics
Major Professor: Dr. James Dunne
Title of Study: MONTE-CARLO SIMULATION OF PHOTOPRODUCTION OF OMEGA MESON

Pages in Study: 77
Candidate for Degree of Master of Science

The null result of December 2004 Sub-threshold photoproduction of $\mathbf{J} / \psi$ experiment has motivated this thesis. This monte-carlo predicts the cross-section for sub-threshold photoproduction process and provides an insight on the cross-section range of these processess.

Additionally calibration runs were performed for Omega and Eta mesons for the verification of correctness of experimental procedure. The results from this experiment are compared with the monte-carlo simulation for the number of omega meson events. This is primarily done as the models for photoproduction of omega meson are well tested. The monte-carlo provides satisfactory results for the photoproduction models and with a crude a spectrometer model predicts the number of events which are off by a factor less than two. A refined model from Jefferson lab will eliminate this discrepancy.

## DEDICATION

I dedicate this thesis to my parents. Without their support, I would not have seen this day.

## ACKNOWLEDGMENTS

First and foremost, I acknowledge Dr. Dunne for being a great advisor. This thesis would not have been successful without his invaluable guidance and encouragement. I am grateful to him for the financial support and all the unofficial help throughout my program. I appreciate his patience during the research which led to this thesis. I also thank him for allowing me to use his photoproduction code as a tool in this research.

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## CHAPTER I

## INTRODUCTION

### 1.1 From Quarks to Vector-mesons

Quarks and Leptons are the fundamental constituents of matter in the standard model of particle physics. The most striking property of quarks is the confinement. This property is expected to follow from the theory of strong interactions called Quantum Chromodynamics( QCD ) and is also well established experimentally as no free quarks have ever been observed. It is because of this property that quarks are bound inside subatomic particles. Quarks have spin-1/2, hence are fermions and are the building blocks of matter. Table 1.1 summarizes the properties of quarks. The quark model successfully predicts the constituents of all the observed hadrons [8].

Table 1.1
Properties of constituents quarks

| Quark | Charge(e) | Spin | I | $\mathrm{I}_{3}$ | S | C | B | Constituent Mass(MeV) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| u | $\frac{2}{3}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | 0 | 0 | 0 | 330 |
| d | $-\frac{1}{3}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $-\frac{1}{2}$ | 0 | 0 | 0 | 336 |
| s | $-\frac{1}{3}$ | $\frac{1}{2}$ | 0 | 0 | -1 | 0 | 0 | 540 |
| c | $\frac{2}{3}$ | $\frac{1}{2}$ | 0 | 0 | 0 | 1 | 0 | 1550 |
| b | $-\frac{1}{3}$ | $\frac{1}{2}$ | 0 | 0 | 0 | 0 | -1 | 4800 |
| t | $\frac{2}{3}$ | $\frac{1}{2}$ | 0 | 0 | 0 | 0 | 0 | 50000 |

Table 1.2
Lowest Lying multiplets of hadrons in terms of quark model

| Hadron <br> Rest energy (GeV) | Spin-Parity <br> $J^{\pi}$ | Type | Members <br> of Multiplets | Number <br> of Members |
| :---: | :---: | :---: | :---: | :---: |
| 0.5 | $0^{-}$ | Pseudoscalar mesons | $\pi K \bar{K} \eta \eta \prime$ | 9 |
| 0.8 | $1^{-}$ | Light Vector-mesons | $\rho K^{*} \omega \phi$ | 9 |
| 1.1 | $\frac{1}{2}^{+}$ | Baryons | $N \Lambda \Sigma \Xi$ | 8 |
| 1.4 | $\frac{3}{2}^{+}$ | Baryons | $\Delta \Sigma^{*} \Xi^{*} \Omega$ | 10 |

Table 1.2 presents a scheme of lowest-lying multiplets of hadrons based on the various flavor combinations of quarks. The rest hadron energy in Table 1.2 is roughly the central energy of the respective multiplet. Hadrons are classified according to their quark content namely baryons with three quarks $(q q q)$ and mesons with a quark and antiquark $(q \bar{q})$. We now focus more on the properties of mesons in terms of quarks due its relevance to this thesis.

The intrinsic parity of fermion-antifermion pair being negative and with two spin $\frac{1}{2}$ quarks can form two states with $l=0$ :

$$
\begin{array}{ccc}
{ }^{1} S_{0} & J^{\pi}=0^{-} & \text {pseudoscalar mesons } \\
{ }^{3} S_{1} & J^{\pi}=1^{-} & \text {vector mesons }
\end{array}
$$

To see how the observed mesons (as in Table 1.2) can be understood in terms of their constituent quarks, we consider the relevant masses of quarks from Table 1.1 which are below 1 GeV . Hence, if we consider the three lowest mass quarks $u, d$ and $s$ and their antiparticles in the following combination[8]:

$$
\begin{array}{lll}
u \bar{u} & d \bar{u} & s \bar{u} \\
u \bar{d} & d \bar{d} & s \bar{d} \\
u \bar{s} & d \bar{s} & s \bar{s}
\end{array}
$$

This implies the existence of nine different mesons in agreement with Table 1.2. However, the arrangement is not according to the quantum numbers and hence comparison with experimental observation is not obvious. In Table 1.3, the nine different combinations are arranged according to the strange( S ) and isospin $\left(\mathrm{I}_{3}\right)$ quantum numbers.

Table 1.3
Reordering of $q \bar{q}$ according to Strangeness S and isospin component $\mathrm{I}_{3}$

| S | $\mathrm{I}_{3}=-1$ | $-\frac{1}{2}$ | 0 | $\frac{1}{2}$ | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  | $d \bar{s}$ |  |  |  |
| 0 | $d \bar{u}$ |  | $u \bar{u}, d \bar{d}, s \bar{s}$ |  |  |
| -1 |  | $s \bar{u}$ |  | $s \bar{d}$ | $u \bar{d}$ |

These can now be compared with nine pseudoscalar and nine vector mesons. For the pseudoscalar mesons this scheme gives,

$$
\begin{array}{cccc}
K^{0} & & K^{+} & \\
\pi^{-} & \pi^{0}, \eta^{0}, \eta^{\prime} & & \pi^{+} \\
K^{-} & & \bar{K}^{0} &
\end{array}
$$

and for the vector mesons

$$
\begin{array}{llll}
K^{* 0} & K^{*+} \\
& \rho^{0}, \omega^{0}, \phi^{0} & & \rho^{+} \\
K^{*-} & & K^{* 0} &
\end{array}
$$

In both cases, the assignments for the six states of the outer ring are unambiguous. The three states in the center however have the same quantum numbers $S$ and $\mathrm{I}_{3}$. Since any linear combination of the states $u \bar{u}, d \bar{d}$ and $s \bar{s}$ have the same quantum numbers, it is not possible to identify one quark combination with one meson. Since any linear combination of states $u \bar{u}, d \bar{d}$ and $s \bar{s}$ will have the same quantum numbers, we cannot discern one quark combination with one meson uniquely. Since we are concerned only with vector mesons, we now extract the quark content of vector mesons.

In case of rho, since the charged members do not contain any strange quark content, the neutral rho also should not have any strangeness as it forms an isospin triplet with its charged relatives. Now adding up the spin of particle-antiparticle pairs of the states $u \bar{u}$ and $d \bar{d}$, we have

$$
\begin{equation*}
\rho^{0}=\frac{d \bar{d}-u \bar{u}}{\sqrt{2}} \tag{1.1}
\end{equation*}
$$

In case of $\phi^{0}$ meson, it experimentally observed that in the rest energy spectrum it lies above $K^{*}$ by 130 MeV and hence must be composed of,

$$
\begin{equation*}
\phi^{0}=s \bar{s} \tag{1.2}
\end{equation*}
$$

In case of $\omega$, th state function can now be found by setting,

$$
\begin{equation*}
\omega^{0}=c_{1} u \bar{u}+c_{2} d \bar{d}+c_{3} s \bar{s} \tag{1.3}
\end{equation*}
$$

Now, the state representing $\omega$ should be orthogonal to the states representing $\rho^{0}$ and $\phi^{0}$. From the above considerisations of $\rho^{0}$ and $\phi^{0}$, the $\omega^{0}$ is calculated to be,

$$
\begin{equation*}
\omega^{0}=\frac{u \bar{u}+d \bar{d}}{\sqrt{2}} \tag{1.4}
\end{equation*}
$$

One immediate observation that we can make here is, since the quark content of $\rho$ and $\omega$ are same their masses must be approximately close,

$$
\begin{equation*}
m_{\rho^{0}} \approx m_{\omega^{0}} \tag{1.5}
\end{equation*}
$$

This observation is indeed found true experimentally.

### 1.2 The Vector Meson Dominance Model

The Vector Meson Dominance(VMD) model is a non-perturbative, phenomenological model developed in the 1960's to explain photoproduction of light vector mesons. As a result of bulk experimental data[3] during these years, there was a growing awareness that the ability of the photon to transform into a vector mesons might play a broader role than in form factors and decay matrix elements. The VMD provides a physical picture of the photoproduction mechanism and is discussed here to provide the reader with a "physical intuition" of the photoproduction process [3].

The photon interactions with hadrons bear remarkable similarities to purely hadronic interactions. At a very crude level, this can understood if the physical photon $|\gamma\rangle$ were a superposition of two types of states: a bare photon $\left|\gamma_{B}\right\rangle$ and a small-of order $\sqrt{\alpha}$-hadronic component $\sqrt{\alpha}|h\rangle$ which undergoes conventional hadronic interactions. That is, we expect the important part of the physical photon state to be expressible as

$$
\begin{equation*}
|\gamma\rangle \cong \sqrt{Z_{3}}\left|\gamma_{B}\right\rangle+\sqrt{\alpha}|h\rangle \tag{1.6}
\end{equation*}
$$

where $Z_{3}$ introduced to assure the proper normalisation of $|\gamma\rangle$; all states in the above equation have the same 3-momentum k. Invariance considerations dictate that $|h\rangle$ should have
the same symmetry quantum numbers as the photon i.e., $J^{P C}=1^{--}, Q=B=S=0$. The copious photoproduction of vector mesons $\rho^{0}, \omega$ and $\phi$ suggests that they provide very important contributions to $|h\rangle$. The restrictive assertion that these three mesons are the sole hadronic components of the photon, and the bare component $|\gamma\rangle$ cannot interact with the hadrons, is the hypothesis of Vector Meson Dominance(VMD) in its most naive and clear cut form. The less restrictive assumption that all the interactions result from $|h\rangle$, which has more constituents than $\rho^{0}, \omega$ and $\phi$ is referred to Generalized Vector Dominance(GVD) [3].

### 1.3 Photoproduction of Vector mesons

This section is devoted to the generalised vector meson photoproduction and a brief overview of dominant mechanisms thereof. The high energy photons (in the order of GeV's) in photoproduction experiments are usually produced by colliding a high energy electron beam onto a radiator or they are generated inside the target as in this experiment.

Generalising the basic picture of the photoproduction process $\gamma p \rightarrow V p$, the photon fluctuates into a quark-antiquark $q \bar{q}$ pair, which then interacts with the proton $p$. This interaction depends on the mechanisms which will be discussed later. After the interaction, the vector meson $V$ with invariant mass $m_{V}$ is formed in the first approximation by the $q \bar{q}$ pair. In the kinematic region of centre-of-mass energy $W_{\gamma p}$ the time scales involved are the following: the typical lifetime $\tau_{\gamma \rightarrow q \bar{q}}$ of $\gamma \rightarrow q \bar{q}$ fluctuation and the time $\tau_{q \bar{q} \rightarrow V}$ for the
formation of vector meson $V$ are much longer than the duration $\tau_{i}$ of the interaction with the proton,

Figure 1.1
Diffractive cross-section of $\rho$ meson[2]

### 1.3.1 Rho Photoproduction

The rho meson is an unstable particle whose mass and width are roughly 770 MeV and 155 MeV respectively. Its quantum numbers $I^{G}\left(J^{P}\right) C$ are $1^{+}\left(1^{-}\right)^{-}$and its dominant decay mode is two charged pions [3]. It has been found experimentally that rho photoproduction has characteristics of a diffractive process- i.e., a sharply forward-peaked differential cross section varying slowly in magnitude with photon energy. This is clearly refected in
the Figure 1.1[2] above. Such behaviour is accounted for in the VMD model by a direct $\gamma \rightarrow \rho^{0}$ coupling.

### 1.3.2 Omega Photoproduction

The omega meson is an unstable particle with a mass of $(782.7 \pm 0.8) \mathrm{MeV}$ and width of (10.0 $\pm 0.4) \mathrm{MeV}$. Its quantum numbers $I^{G}\left(J^{P}\right) C$ are $0^{-}\left(1^{-}\right)^{-}$and its dominant decay modes are $\pi^{+} \pi^{-} \pi^{0}(90.0 \pm 0.6) \%, \pi^{0} \gamma(8.7 \pm 0.5) \%$ and $\pi^{+} \pi^{-}(1.3 \pm 0.3) \%$ [3]. Since omega has much a larger width for $\pi^{0} \gamma$ decay mode than $\rho$ meson, one-pion exchange plays a larger role in omega photoproduction, and at low energies dominates the photoproduction cross-section. In reality the cross-section is sum of diffractive and OPE effect as evidenced in the Figure 1.2 below[2].

Irrespective of the prediction of the OPE effect due to dominant $\pi^{0} \gamma$ decay mode, the evidence of a large forward peak in differential cross-section in $t$ is a manisfestation of the single particle exchange mechanism at work at low $t$. The one-pion exchange model is specific case of single particle exchange mechanism which was formulated to distinguish between meson exchanges and baryon exchanges which led to forward and backward peaks respectively [12].

### 1.3.3 Phi Photoproduction

The $\phi$ meson is an unstable particle with a mass of $(1019.7 \pm 0.3) \mathrm{MeV}$ and a width of (4.1 $\pm 0.2) \mathrm{MeV}$. Its quantum numbers $I^{G}\left(J^{P}\right) C$ are $0^{-}\left(1^{-}\right)^{-}$and its dominant decay modes
are $K^{+} K^{-}(46.6 \pm 2.3) \%, K_{L} K_{S}(35.0 \pm 2.0) \%, \pi^{+} \pi^{-} \pi^{0}(16.4 \pm 1.5) \%, \eta \gamma(2.0 \pm 0.4) \%$ and $\pi^{0} \gamma(0.14 \pm 0.05) \%$ [3].


Figure 1.2
Diffractive and OPE nature of $\omega$ cross-section[2]

The $\phi$ meson is interesting from a number of standpoints. In addition to its being one of the three major vector mesons, the $\phi p$ scattering proceeds through Pomeron exchange. This is a consequence of the fact that $\phi$ is made up of strange-antistrange $s \bar{s}$ which are barred from resonance reactions with nonstrange mesons hadrons. Thus, on the diagonal VMD, one would expect $\phi$ photoproduction to be due dominantly to Pomeron exchange and hence provides an excellent information concerning Pomerons [3]. The Pomeron is a coherent color-singlet object, built from gluons. It is the object which is exchanged by any pair of hadrons that scatter at high energy and large impact parameter.

### 1.4 Models for $J / \psi$ Photoproduction

The $J / \psi$ is the first excited state of the bound charm-anticharm quark $(c \bar{c})$ with a mass of $(3096.87 \pm 0.04) \mathrm{MeV}$ and a width of $(87.0 \pm 5.0) \mathrm{keV}$. Its quantum numbers $I^{G}\left(J^{P}\right) C$ are $0^{-}\left(1^{-}\right)^{-}$and its dominant decay modes are to hadrons $(87.7 \pm 0.5) \%, e^{+} e^{-}(5.93 \pm$ $0.10) \%, \mu^{+} \mu^{-}(5.88 \pm 0.10) \%$ [5].

In case of photoproduction of $J / \psi$, the interaction mechanism of $J / \psi$ is not understood to date. The threshold energy in the the center of mass frame for the reaction $\gamma p \rightarrow J / \psi p$ is given by,

$$
\begin{equation*}
\sqrt{s}=\left(m_{p}+M_{J / \psi}\right)=4.034 \mathrm{GeV} \tag{1.8}
\end{equation*}
$$

The incident photon energy, corresponding to $\sqrt{s}=4.034 \mathrm{GeV}$ is,

$$
\begin{equation*}
E_{\gamma}=8.2 \mathrm{GeV} \tag{1.9}
\end{equation*}
$$

The maximum available photon energy at the Jefferson Lab is 5.7 GeV , hence to photoproduce the $J / \psi$ the target itself must provide the necessary $P_{p}>350 \mathrm{MeV}$ in the form of Fermi energy. This process is different in this sense as compared to all the photoproduction mechanisms above. Physically this means that the target nucleon momentum must point antiparallel to the incident beam(with the correct energy).

The exact reaction physics of the above process is absent, but there are some specific requirements that are needed to be satisfied for the above process to occur which will broaden our understanding of behaviour of nucleons at short range. Figure 1.3 shows characteristic scales for $J / \psi$ photoproduction near threshold. In this model [4], the photon
fluctuates into a $c \bar{c}$ over longitudinal length, $l_{c} \approx 2 E_{\gamma}^{l a b} / 4 m_{c}^{2}=0.36 \mathrm{fm}$ and interacts with the target proton through gluon exchanges. All the target partons have to transfer their energy to the charm quarks witin their proper creation time $1 / m_{c}$ and must be within the transverse distance from $c \bar{c}$. The success of this model is believed to provide a new window into multiquark


Figure 1.3
Characteristic scales for $J / \psi$ photoproduction near threshold

In case of photoproduction of charm near threshold, since the final nucleon is nearly at rest in the lab frame, the net momentum fraction carried by the spectator partons is $x \sim 0$. The production rate behaves near $x \rightarrow 1$ as $(1-x)^{2 n_{s}}$ where $n_{s}$ is the number of spectators. Perturbative QCD predicts three different gluonic components of the photoproduction cross-section[4]:

- The usual one gluon $(1-x)^{4}$ distribution for leading twist photon-gluon fusion $\gamma g \rightarrow c \bar{c}$, which leaves two quarks spectators;
- Two correlated gluons emitted from the proton with a net distribution $\frac{(1-x)^{2}}{R^{2} \mathcal{M}^{4}}$ for $\gamma g g \rightarrow c \bar{c}$, leave one quark spectator;
- Three correlated gluons emitted from the proton with a net distribution $\frac{(1-x)^{0}}{R^{4} \mathcal{M}^{4}}$ for $\gamma g g g \rightarrow c \bar{c}$, leaving no quark spectators.


Figure 1.4
$J / \psi$ cross-section measurement by Cornell and SLAC

Here $x \approx\left(2 m \mathcal{M}+\mathcal{M}^{2}\right) /\left(s-m^{2}\right)$ and $\mathcal{M}$ is the mass of $c \bar{c}$ pair. For elastic charm production (when the proton target remains bound), it is also necessary to take into the account the recombination of the three valence quarks into the proton via its form factor, as well as the coupling of the photon to the $c \bar{c}$ pair. For the two gluon exchange the crosssection of the $\gamma p \rightarrow J / \psi p$ takes the form[4]:

$$
\begin{equation*}
\frac{d \sigma}{d t}=\mathcal{N}_{2 g} \nu \frac{(1-x)^{2}}{R^{2} \mathcal{M}^{2}} F_{1}\left(\frac{t}{4}\right)\left(s-m^{2}\right)^{2} \tag{1.10}
\end{equation*}
$$

while for three gluon exchange it takes the form:

$$
\begin{equation*}
\frac{d \sigma}{d t}=\mathcal{N}_{3 g} \nu \frac{(1-x)^{0}}{R^{4} \mathcal{M}^{4}} F_{1}\left(\frac{t}{9}\right)\left(s-m^{2}\right)^{2} \tag{1.11}
\end{equation*}
$$

where $\mathcal{N}$ are the normalization coefficients. $F_{1}(t)$ is the isoscalar proton form factor and its argument takes into account that the momentum transfer is shared between two or three valence quarks in the proton. These models are used in the monte-carlo simulation in a simplified form[6]: $\frac{d \sigma}{d t}=a f(b t)$ :
$f(b t)=e^{b t}$ for the dipole form factor,
$f(b t)=\frac{1}{(1-b t)^{3}}$ for the 3-gluon exchange model, and
$f(b t)=\frac{(1-x)^{2}}{(1-b t)^{4}}$ for the 2-gluon exchange model.
The gluon exchange models are shown with the Cornell and SLAC data as in Figure 1.3. While both curves drop off rapidly with photon energies approaching threshold, both the Cornell and SLAC data seem to be flattening out below 12 GeV . It was believed earlier that this was a transition from 2-gluon process to the 3-gluon process near threshold. There are other popular models like the photon-gluon fusion model based on pQCD but these
models fail to match the cornell data by a factor of five and are expected to work at high energy. We present in this thesis analysis of 2-gluon and 3-gluon models.

## CHAPTER II

## EXPERIMENTAL SETUP

### 2.1 Introduction

The experiment of Sub-threshold $J / \psi$ photoproduction was conducted at the Hall-C of the Jefferson Lab in November-December 2004. In this experiment, electrons accelerated to the relativistic speeds are collided with a fixed target, which also acts as the radiator for the photon flux via bremsstrahlung. This photon flux further interacts with proton inside the target nucleus to produce an vector meson and proton. Of the several prominent decay modes of the Omega meson, we observed the electron-positron decay mode which has a branching ratio of $7 \times 10^{-5}$. These were further detected in coincidence using the two Hall-C spectrometers, the High Momentum Spectrometer (HMS) and the Short Orbit Spectrometer (SOS). The target used was Beryllium with the radiation length of $3 \%$. In this chapter the experimental set up is described.

### 2.2 Accelerator

The Thomas Jefferson National Accelerator Facility (TJNAF) utilizes two linear accelerators (LINAC), North LINAC and South LINAC, to accelerate the beam over a distance of approximately 2 km and 9 recirculation arcs, East arc and West arc, to bend the beam back in the LINACs. The beam can be recirculated up to a maximum of 5 times and is delivered
to three halls Hall-A, Hall-B and Hall-C with varying energies and currents which is done by splitting the beam at the Beam Switch Yard At present the accelerator is capable of delivering $200 \mu \mathrm{~A}$ and $\sim 6 \mathrm{GeV}$. The schematic diagram is shown in Figure 2.1


Figure 2.1
Schematic representation of Linear Accelerator [10]

The electron beam is generated in the injector by shining laser light on a $\mathrm{Ga}-\mathrm{Ar}$ cathode and is injected in the west side of North LINAC at $\sim 45 \mathrm{MeV}$. In the LINAC, the beam is accelerated in a resonant cavity driven at 1.497 GHz such that an accelerating field is produced which continuosly "kicks" electrons in the forward direction. Each LINAC adds upto $500-600 \mathrm{MeV}$ in one pass. The beams with different energies is split into different recirculation arcs (namely five) at the north end of east arc. At the re-entry to South LINAC, beams with different energies from the recirculation arcs are focused into single collimated beam and accelerated over the LINAC. According to the energy and current requirement
of the different halls, the beam is either recirculated in the west arc or separated in the Beam Switch yard and fed to the respective hall and collided with a stationary target.

### 2.3 Hall C Overview

The basic equipments in the Hall C comprise of two spectrometers: High Momentum Spectrometer (HMS) and the Short Orbit Spectrometer (SOS) focused on the target chamber as shown in the schematic Figure 2.2. This section will describe the Hall C equipment in detail.


Figure 2.2
Schematic representation of Hall-C [11]

### 2.4 The Target Vacuum Chamber

The target vacuum chamber is essentially an cylndrical aluminium tank. It was designed to accomodate both solid and cyrogenic target ladder. There are two large openings on the either side of beam entrance and exit. These openings are covered with aluminium windows to minimize the amount of material scattered particles must pass through before entering the spectrometers. Each window on the target chamber is designed to match the range and acceptance of respective spectrometer. Actually, the true opening on the SOS side of the chamber is larger vertically than the acceptance to accomodate the out of plane acceptance of the SOS. The target chamber is also housed with pumping and viewing ports. The lifting mechanism and solid target mechanism are housed on the top cover plate. A solid target of Beryllium with 3\% radiation length was used for omega calibration runs. A 4 cm liquid hydrogen target was use for eta calibration runs. The $J / \psi$ production runs use a $6 \%$ radiation length carbon target.

### 2.5 High Momentum Spectrometer

The High Momentum Spectrometer (HMS) is the largest of the two spectrometers in Hall-C. It is a super-conducting, magnetic spectrometer with a central momentum upto 7.5 GeV/c. In this experiment the HMS was used to detect positively charged leptons in coincidence with negatively charged leptons in the SOS. It comprises of three superconducting quadrupole magnets and one superconducting dipole magnet in QQQD configuration as shown in Figure 2.3. The quadrupole determine the focusing properties of
the spectrometer and hence to a large extent, its acceptance. The dipole magnet bends the focused electrons by an angle of $25^{\circ}$ into the detector hut. The HMS was set for the following parameters in this experiment,


Figure 2.3
Schematic representation of High Momentum Spectromter [7]

### 2.5.1 The HMS Detector Package

The detector package for High Momentum Spectrometer is shown in Figure 2.4. It consists of two multiwire proportional drift chambers for track reconstruction, a Čerenkov counter for e/ $\pi$ identification, two planes of XY scintillator hodoscopes for triggering and time-of-flight studies, and a lead glass calorimeter for energy measurement and additional e/ $\pi$ discrimination.

Table 2.1

HMS Parameters for Run 52148

| HMS Momentum(GeV/c) | 2.2 | 2.2 |
| :---: | :---: | :---: |
| Q1 Set Current (A) | -254.050 | -254.050 |
| Q2 Set Current (A) | 201.825 | 201.825 |
| Q3 Set Current (A) | -98.348 | -98.348 |
| Q1 B Field (G) | -3383.9000 | -3383.9000 |
| Q2 B Field (G) | 4091.9000 | 4091.9000 |
| Q3B Field (G) | -1976.6000 | -1976.6000 |
| D Current Readback | 596.310 | 596.310 |
| B_true | 0.5359740 | 0.5359740 |
| HMS Angle | 11.01 | 13.00 |



Figure 2.4
Detector package of High Momentum Spectrometer [11]

### 2.5.2 Scintillator Hodoscopes

A scintillation detector's operation is based on the fact that certain materials emit a small flash of light (scintillation) when struck by a nuclear particle or radiation. When coupled to a conversion and amplifying device such as a photomultiplier tube, these scintillations can be converted into electrical pulses (via the photoelectric effect).

The main purpose of the scintillator hodoscopes in the HMS was to provide a clean trigger. These detectors consisted of four planes. Two of these planes were segmented in X (S1X and S2X as in Fig) and two were segmented in Y (S1Y and S2Y). S1X and S1Y planes were about 2 m from S2X and S2Y. Each element was wrapped in aluminium foil for reflection, followed by two layers of Tedlar for external light rejection. The typical trigger was a three out of four coincidence of the scintillator planes.

### 2.5.3 Drift Chamber

The drift chamber is used to provide position information of the incoming particle in the spectrometer. It consists of six planes arranged in order of $X, Y, U, V, X^{\prime}, Y^{\prime}$ each 1.4 cm apart as seen by an incoming particle. The fig shows the operation of the drift chamber.

The drift chamber is an ionization detector which consists of basic unit called drift cell. A drift cell is a region of space filled with a gas or gas mixture in which an anode and one or more cathode help establish a stationary electric field. As charged particles pass through the drift cell a certain number of electron-ion pairs are created due to dissociation of gas molecules which are further accelerated in the electric field. During this acceleration, these
charges also collide with other gas molecules and this creates a "drift"towards anode and cathode. The velocity of this collective drift is called drift velocity which depends on the ratio $E / p$ where $E$ is the electric field and $p$ is the gas pressure. The time interval between creation of electron-ion pairs in the cell and their subsequent collection is called "drift time". By measuring this drift time and knowing the drift velocity one can determine the drift distance, i.e. distance between the sense wire and the trajectory of the initial charged particle passing through cell.

### 2.5.4 Čerenkov Counter

A charged particle moving in a certain medium at a speed greater than the speed of light emits Čerenkov radiation along a conical wavefront. The angle of emission of $\theta$ of the radiation of a given wavelength $\lambda$ is related to the velocity of the particle relative to the speed of light $\beta=v / c$ and the refractive index $n$ of the medium:

$$
\begin{equation*}
\cos \theta=\frac{1}{\beta c} \tag{2.1}
\end{equation*}
$$

The number of Čerenkov photons $N_{\gamma}$ emitted per unit length $L$ is given by:

$$
\begin{equation*}
\frac{d N_{\gamma}}{d L}=2 \pi \alpha Z^{2} \int_{\lambda_{1}}^{\lambda_{2}}\left(1-\frac{1}{\beta^{2} n^{2}}\right) \frac{\mathrm{d} \lambda}{\lambda^{2}} \tag{2.2}
\end{equation*}
$$

where $\alpha$ is the fine structure constant, $Z e$ is the charge of the particle, and $\lambda_{1}, \lambda_{2}$ define the limits of the spectral range of detected radiation.

A threshold Čerenkov counter detects particles that have a velocity sufficient to produce Čerenkov light in the medium, i.e. above a certain velocity threshold. By choosing
the proper index of refraction $n$, one can set the threshold velocity in such way as to reject the unwanted particles, pions in this case. The appropriate index of refraction to achieve this is in the order of $\left(10^{-4} \leq(n-1) \leq 10^{-3}\right)$. Therefore a gas is used as a Čerenkov medium and typically the gas is chosen in such a way so as to maximize the signal for electrons.

The HMS Čerenkov counter used in Hall-C consists of a large cylindrical tank, 150 cm in diameter and 152 cm long. It consists two mirrors which focused light on the photomultiplier tubes. The gas used was $C_{4} F_{10}(n=1.00041)$. The threshold momentum in this case is $17.9 \mathrm{MeV} / \mathrm{c}$ for electrons and $4.9 \mathrm{GeV} / \mathrm{c}$ for pions. Hence, it is fully sensitive to electrons. The pressure was set so that it would trigger on muons also.

### 2.5.5 Lead Glass Calorimeter

The Lead Glass Calorimeter is also called Shower Counter as the measurement is proportional to radiation shower. It served two purposes namely particle identification and energy measurement. The high energy electrons entering the counter interact with the glass and radiate through Bremsstrahlung. These Bremsstrahlung photons further produce electronpositron pairs which inturn radiate more generating a cascade. The high energy electrons from above processes generate Čerenkov light as they are passing through glass which is collected by photomultiplier tubes. Hence, the collected Čerenkov light is proportional to energy of incident of electrons.

The HMS shower counter consists of 52 lead glass blocks. Lead glass is a transparent glass composed of lead dioxide and silicon dioxide. These blocks are stacked in a group of 13 and placed in 4 layers across the incident path. A photomultiplier tube is placed at one end of each block.

### 2.6 Short Orbit Spectrometer



Figure 2.5
Schematic representation of Short Orbit Spectrometer [7]

The Short Orbit Spectrometer (SOS) is magnetic spectrometer with water cooled conventional resistive magnets. The SOS combines a large acceptance, with solid angle and momentum, with a relatively short path length to the focal length. Hence called the Short Orbit Spectrometer. It is primarily designed to detect short lived particles. The maximum central momentum of the SOS is $1.5 \mathrm{GeV} / \mathrm{c}$. It consists of one quadrupole magnet and two dipole magnet in Q, D, -D configuration. The first dipole bends the single charged particles of the central momentum upwards by $33^{\circ}$ and the second dipole bends the beam
downwards by $15^{\circ}$, resulting in a $18^{\circ}$ through the detectors. The SOS was set with the following parameters in this experiment:

Table 2.2
SOS Parameters for Run 52148

| SOS Momentum(GeV/c) | -0.9 | -0.9 |
| :---: | :---: | :---: |
| SOS Angle | 25.18 | 27.83 |
| SOS Quad Momentum | -0.9 | -0.9 |
| SOS Dipole 1 Momentum | -0.9 | -0.9 |
| SOS Dipole 2 Momentum | -0.9 | -0.9 |

### 2.6.1 SOS Detector Package

The SOS detector package is similar to that of HMS. It consisted two drift chambers, a Čerenkov counter for particle identification, pair of XY scintillator hodoscopes and a shower counter for energy measurement and additional $e / \pi$ discrimination.

### 2.6.1.1 Scintillator Hodoscopes

The SOS hodoscope was similar to HMS hodoscope. It consisted of four layers (two X-planes, SX1 and SX2 and two Y-planes, SY1 and SY2). The SOS scintillators were mounted in aluminium frames, wrapped in one layer of aluminized mylar.

### 2.6.1.2 Drift Chambers

The SOS drift chamber module consisted of six planes $\left.X, X^{\prime}, U, U^{\prime}\right)$. The $U$ and $U^{\prime}$ were rotated $60^{\circ}$ clockwise from $X$ and the $v$ and $V^{\prime}$ planes are rotated $60^{\circ}$ counterclockwise
with X. A schematic view of the drift chamber is shown in the figure. It has three planes of gold-plated tungsten wires of two thickness: $30 \mu$ wires at ground potential, and $60 \mu$ wires held at negative potential. The gas used in SOS drift chambers was 50-50 mixture of argon and ethane.


Figure 2.6

> Schematic representation of SOS Detector package [7]

### 2.6.1.3 SOS Čerenkov Counter

A new Čerenkov detector was used in the SOS to be able to separate the muons from pions. The tank was pressurized above at 1.8 atm . The detector was modified from the 1.6 GeV SLAC end station Čerenkov detector. The gas used was $C_{4} F_{10}$.

### 2.6.1.4 Electromagnetic Calorimeter

The SOS electromagnetic calorimeter consisted of four stacks of TF1 lead glass. Each stack contained seven blocks. The blocks were identical to that HMS.

## CHAPTER III

## DATA ANALYSIS AND SIMULATION

This chapter provides a description of data analysis and monte-carlo simulation of photoproduction of vector mesons.

### 3.1 Analysis Software Overview

The experimental data for photoproduction runs of omega was analysed using the Hall-C analysis software(ENGINE). This section serves only an overview of the software functions as a detailed review is beyond the scope of this thesis[1].

The ENGINE is designed as a general purpose analysis software for Hall-C. The code for the software can be easily modified according to the needs of the various experiments that use the standard equipments(i.e. HMS and/or SOS). The raw data acquired from the experiment is recorded to the hard disk drive and backed up to the JLAB StorageTeK robotic library. The data is then retrievable and can be analysed by the replay software. The main tasks of this software will be very briefly reviewed here [11]:

- CODA event decoding - decode the hardware event information and translate into detector arrays .
- HMS and SOS reconstruction - reconstructs trajectories and records particle information for each event.
- Coincidence calculations - calculate the coincidence physics quantities, if both HMS and SOS have a trigger, and store all results.


### 3.2 Omega Analysis

In this section, the results from the omega runs are presented which will be further compared with the simulation from the monte-carlo. This experiment was set to detect the leptonic decays of vector meson but due to the cleaner sample of $e^{+} e^{-}$decays, this analysis focussed on electrons instead of both electrins and muons. A clear peak for omega was observed which was also evident from coincidence timing settings.

The invariant mass spectrum for omega for the interaction $\gamma p \rightarrow \omega p$ is calculated as follows,

$$
\begin{equation*}
M_{\omega}^{2}=\left(P_{e^{+}}+P_{e^{-}}\right)^{2} \tag{3.1}
\end{equation*}
$$

where, $P_{e^{+}}$and $P_{e^{-}}$are the 4-momenta of decay leptons as detected in the spectrometers. One can also observe that, as it was mentioned earlier that $m_{\rho^{0}} \approx m_{\omega^{0}}$, there two peaks on top of each other, the top one corresponding to $\omega$ meson and the bottom one corresponding to $\rho$ meson which is clearly seen in Figure 3.1 The coincidence timings plots as in Figure 3.2 indicate a clear peak for $e^{+} e^{-}$and $e^{-} h^{+}$coincidence.These observations confirm the particle ID to be omega meson. The calculation of number of $\omega$ events is done by background substraction of Figure 3.1 and is indicated in Figure 3.3

The background separated omega events are fitted with a guassian whose mean value is exactly the $\omega$ mass which is 0.782 GeV with the correct width of 8 MeV . The area under this peak is simply the number of $\omega$ events which is calculated using the Physics Analysis Workstation(PAW) software. The result gives 160 events.


Figure 3.1
Missing Mass Spectra( $\omega$ peak clearly visible near $m_{\omega}=0.782 \mathrm{GeV}$ )


Figure 3.2
Coincidence timings for $\omega$ meson


Figure 3.3
Background subtracted events for $\omega$

### 3.3 Monte-carlo Simulation

The Monte-carlo simulation attempts to reproduce the physical situation for photoproduction and gives satisfactory results(as we will see in the next chapter) and hence is reliable. The code is designed to simulate only real photons and with appropriate model can simulate any vector meson including, $\rho, \omega, \phi$ and $J / \psi$. This section will describe the structure of simulation and its features.

### 3.3.1 Main Event Loop

The main event loop simulates the interaction $\gamma p \rightarrow V p$, where $V$ is the particular vector meson, by generating the photon and nucleon events with appropriate models as described below. The code then accepts only those events whose center of momentum energy is greater than the photoproduction threshold of that particular vector meson. These events are then weighted by appropriate parameters as described in further sections and finally recorded so as to be analysed by the PAW software. This section now describes the detail structure of simulation and all the tasks in the same order as the code proceeds.

## - Initialisation

The simulation requires certain intial parameters to start with which are described below,

- Maximum Photon Energy This refers to the maximum energy of bremmstrahlung photons and is usually same as the beam energy in the experiment.
- Number of Events These are the desired number of events we wish to be recorded in the spectrometer. The code makes more attempts to match this as it is weighted by several other paramters.
- Particle ID This refers to the desired vector meson for which the code needs to be simulated. Actually, we specify the mass and width of the particular vector meson.
- Spectrometer Cuts This refers to turning on the spectrometer which also simulate the presence of spectromters. This increases the number of attempts as not all the events generated are recorded by the spectrometer.
- t-models $t$ is the 4 -momentum transfer to the target. This parameter provides an option to be run with different t -models. This will be described in detail in the later section.
- Cross-section weighting This parameter provides an option for weighting the number vector meson events by the photoproduction cross-section of that particular vector meson.


## - Bremsstrahlung photon flux

The high energy electron beam collides with the stationary target and produces high energy photons. The no of photons produced with a beam energy $E$ is given by [13],

$$
\begin{equation*}
d k(1 / k)\left[\frac{4}{3}(1-k / E)+(k / E)^{2}\right] \tag{3.2}
\end{equation*}
$$

where $k=E_{\gamma}$ is photon energy.
In the simulation, after initialisation, the code generates photon events based on above distribution. This is done by weighting a very accurate uniform random number generator from CERNLIB by the above ditribution.

- Nucleon model for bound proton The high energy photons collide with the bound proton to photoproduce a vector meson. In case of $J / \psi$, the proton must be off-shell for sub-threshold photoproduction. A model is therefore used to take into account the nucleon-nucleon correlations for momentum distribution.
- Event Selection

The event selection is done by calculating the center-of-mass energy squared and comparing with threshold energy in center-of-mass. The center-of-mass energy squared is calculated for the interaction $\gamma p \rightarrow V p$, with $p$ as the bound proton (with nucleon momentum $P_{p}$ ) and incident photon.

$$
\begin{equation*}
s=\left(E_{p}^{2}-P_{p}^{2}\right)+2 E_{\gamma} E_{p}-2 E_{\gamma} P_{p} \cos \theta \tag{3.3}
\end{equation*}
$$

where $\theta$ is angle between the incident photon vector and the nucleon momentum vector. This angle $\theta$ is also calculated flat in $\cos \theta$ with uniform random generator.

The threshold energy in a center-of mass is simply given by,

$$
\begin{equation*}
s_{t h}=\left(M_{V}+M_{p}\right)^{2} \tag{3.4}
\end{equation*}
$$

where $M_{V}$ is the mass of the particular vector meson and $M_{p}$ is mass of proton. A vector meson event can be considered to be generated when $s>s_{t h}$.

- Vector meson kinematics

The generation of vector meson event tells us nothing about kinematical quantities such as the energies, momenta, decay distribution etc. The energy of recoiling proton in the center-of-mass frame is given by,

$$
\begin{equation*}
E_{p c m}=\frac{s+M_{p}^{2}-M_{j}^{2}}{2 \sqrt{s}} \tag{3.5}
\end{equation*}
$$

The center-of-mass energy of the vector meson is simply,

$$
\begin{equation*}
E_{V}=\sqrt{s}-E_{p c m} \tag{3.6}
\end{equation*}
$$

A lorentz boost to above quantities tranform them to lab. These kinematical quantities are set in the code to be recorded as event properties and can be analysed using PAW. The results of these will be demonstrated in next chapter. At this stage, appropriate $t$-models are introduced to weight the differential cross-section with respect to $t$ as shown in Figure 1.1 and Figure 1.2. These will be discussed in later section.

- Detection and Recording

In the experiment, the spectrometers are set in a particular geometry to detect the leptonic decays of the vector meson. The tasks of the code now are to generate the decay events and detect them.

The charactertics of the decay products are, they fly $180^{\circ}$ apart in the rest frame of the vector meson. The angular distribution of these leptons can be set in the simulation as flat(isotropic) or weighted by $\left(1+\cos ^{2} \theta\right)$. The kinematical properties of these decays are recorded after a lorentz boost to the lab.

The geometry of spectrometer is simulated by an option in the initialisation called 'spectrometer cuts'. The spectrometer cuts in the code are set by introducing the solid angle of the spectrometer openings to the target. Hence, the events generated over $4 \pi$ steradians are now weighted by these cuts. The events generated with spectrometer cuts are also used later for acceptance corrections.
Finally, the recording of the events is done by filling histograms of respective quantities. The code then checks over for set quantities such as number of events and loops over until it reaches those events.

### 3.3.2 Models for t-dependence

The vector mesons show a cross-section dependence in $t$ as can be clearly seen in Figure 1.1 and Figure 1.2 This factor is incorporated in the simulation, while calculating the
vector meson kinematics as was discussed earlier. In this section, these models are presented and the model for $\omega$ is presented in detail as it is to be compared with data.

### 3.3.2.1 Diffractive t distribution

Diffractive distribution is modeled in simulation with an exponential cross-section dependence given as $d \sigma / d t=N e^{b t}$ where, $N$ is normalised events and b is the slope of the exponential distribution. The total number of events to be recorded in the spectrometer are now weighted over this distribution. This model is more realistic and can simulate, for example, the photoproduction of $\rho$ meson as it exhibits diffractive distribution in Figure 1.1.

The diffractive events are generated by calculating,

$$
\begin{align*}
& t_{\min }=M_{V}^{2}-2 E_{\gamma} E_{V}+2 p_{\gamma} p_{V}  \tag{3.7}\\
& t_{\max }=M_{V}^{2}-2 E_{\gamma} E_{V}-2 p_{\gamma} p_{V} \tag{3.8}
\end{align*}
$$

corresponding to $\theta=0$ and $\theta=\pi$ respectively. The exponential range of the $t_{\min }$ and $t_{\max }$ is weighted by a random number generator to give a diffractive distribution. The acceptance results from diffractive cross-section will be presented in next chapter.

### 3.3.2.2 Diffractive and OPE Model for $\omega$

This model is simulated on the basis of the paper by [9]. This paper was written for electroproduction of $\omega$ based on the theory for photoproduction. Since this thesis deals with only photoproduction, the simplified calculation for $Q^{2}=0$ i.e. for real photons are
presented. According to this paper, the total differential cross-section dependence is the sum of OPE contribution and Diffractive contribution,

1. One Pion Exchange contribution The differential cross-section $d \sigma_{T}^{\pi} / d t$ for transverse photons, is given by

$$
\begin{equation*}
d \sigma_{T}^{\pi} / d t=\frac{1}{\left(P(0)^{2} W^{2}\right)} G^{2} \frac{\Lambda_{\omega \pi}^{2}}{16} \frac{-t}{\left(t-m_{\pi}^{2}\right)^{2}} \frac{(B+C)^{2}}{-C} F_{N} F_{\omega} \tag{3.9}
\end{equation*}
$$

where $G^{2}$ is square of the pion-nucleon coupling $=14.6$,

$$
\begin{equation*}
\Lambda_{\omega \pi}^{2}=96 \pi\left(\frac{m_{\omega}}{\left(m_{\omega}^{2}-m_{\pi}^{2}\right)}\right)^{3} \Gamma_{\omega \pi \gamma} \tag{3.10}
\end{equation*}
$$

with $\Gamma_{\omega \pi \gamma}=0.9 \mathrm{MeV} ; P(0)^{2}$ are the photon momenta in the hadron c.m.s for real and virtual photons, respectively; $m_{\pi}, m_{\rho}, m_{\omega}$ are the masses of $\pi, \rho$ and $\omega$ respectively; $F_{N}, F_{\omega}$ are the form-factors for the $\pi$-nucleon and $\gamma \pi \omega$ vertices respectively with:

$$
\begin{equation*}
F_{N}=\frac{\left(1+(2.9)^{2} Q_{N T}^{2}\right)}{\left(1+(2.9)^{2} Q_{N T}^{2}\right)} \tag{3.11}
\end{equation*}
$$

where

$$
\begin{gather*}
Q_{N}^{2}=\frac{m_{\pi}^{2}\left(m_{\pi}^{2}-4 m_{p}^{2}\right)}{4 m_{p}^{2}}  \tag{3.12}\\
Q_{N T}^{2}=\frac{t\left(t-4 m_{p}^{2}\right)}{4 m_{p}^{2}}  \tag{3.13}\\
F_{\omega}=\frac{U(2.3 Q F)}{U(2.3 Q T)}\left(\frac{Q T}{Q F}\right)^{2} \tag{3.14}
\end{gather*}
$$

where

$$
\begin{equation*}
U(x)=\frac{\left[\frac{2 x^{2}+1}{4 x^{2}} \log \left(4 x^{2}+1\right)-1\right]}{2 x^{2}} \tag{3.15}
\end{equation*}
$$

QT is the momentum of the on-shell pion (or $\gamma$ ) in the $\omega$ frame. The quantities $B, C, N_{3}$ are defined as follows,

$$
\begin{gather*}
B=0.25\left(m_{p}^{2}-W^{2}\right)\left(m_{p}^{2}+m_{\omega}^{2}-W^{2}-t\right),  \tag{3.16}\\
C=-0.25\left(W-m_{p}\right)^{2}\left(W+m_{p}\right)^{2}  \tag{3.17}\\
N_{3}=0.5\left[W^{2} t u-t m_{p}^{2}\left(m_{p}^{2}-m_{\omega}^{2}\right)-m_{p}^{2} m_{\omega}^{4}\right]^{1 / 2} \tag{3.18}
\end{gather*}
$$

with

$$
\begin{equation*}
W^{2}+t+u=2 m_{p}^{2}+m_{\omega}^{2} \tag{3.19}
\end{equation*}
$$



Figure 3.4
$t$-dependence for OPE and difraction from [9]


Figure 3.5
Presimulation of OPE and Diffractive model for real photons from [9]
2. Diffraction Contribution The diffractive contribution is given by

$$
\begin{equation*}
\sigma_{D}(\mu b)=9.3 e^{(6.7 t)}\left(1+\frac{1.4}{E_{\gamma}}\right) \tag{3.20}
\end{equation*}
$$

where

$$
\begin{equation*}
E_{\gamma}=\frac{\left(W^{2}-m_{p}^{2}\right)}{2 m_{p}} \tag{3.21}
\end{equation*}
$$

The results of their models is shown in the Fig 3.4. It must be noted that their model is based for electroproduction and hence $Q^{2} \neq 0$.

Now to simulate this model, it is too complicated and inefficient to directly use these relations in the main simulation. Hence, this model was 'pre-simulated' in MAPLE to reduce the number of variables to only two. Further, this pre-simulation was based on real photons and it was expected to represent the same fit as used by [9]. The result from MAPLE presimulation is shown in Fig 3.5. The presimulation is able to reproduce the the fit as by [9]. It can also be oberserved that, over the same range of ' $t$ ' this curve drops faster than by [9]. This is attributed by the fact this curve is for real photons i.e. $Q^{2}=0$.

### 3.4 Cross-section for $\omega$ Photoproduction

In the simulation, a vector meson event is generated by when $s>s_{t h}$. In reality, the crosssection has a photon energy dependence and this factor needs to be taken into account in the simulation. The energy dependence of the cross-section is presented in a paper by [2] and is shown is Fig 3.6.

To incorporate this model, the cross-section dependence was curve fitted in MAPLE by the points given in this paper. Further, the photon energy range for the above fit is
from 2.5 GeV to 3.5 GeV . The significance of this range is only photons produced in this range actually contribute to omega events in the spectromter. (This is shown in the results section. The appropriate curve fit was found to be Thiele Interpolation and the result is in fig 3.7.This cross-section fit was normalised to unity and normalisation cross-section is given by,

$$
\begin{equation*}
\sigma_{\text {normalised }}=6.277 \mu b \tag{3.22}
\end{equation*}
$$

Now, in the simulation, when a vector meson event is generated, the code weights a uniform random number generator to match the above which is normalised. Hence, now we have events which are weighted over Ballam data.


Figure 3.6
Cross-section dependence on Photon Energy [2]


Figure 3.7
Curve fitted Ballam data


Figure 3.8
Bremsstrahlung Spectrum [13]


Figure 3.9
Bremsstrahlung spectrum from MAPLE simulation

### 3.5 Bremsstrahlung Photons Calculation

The passage of high energy electrons through a stationary target produces a radiation shower called bremmsstrahlung radiation which produces high energy photons in the target. The bremsstrahlung spectrum of these photons is considered in a classic paper by [13] and the photon flux is given by,
$I_{\gamma}=e^{-(7 / 9) t} \int_{0}^{t} \frac{e^{(7 / 9) t}}{\Gamma\left(1+\frac{4}{3} t\right)}\left(\ln \frac{1}{u}\right)^{\left(\frac{4}{3} t^{\prime}\right)} \times\left[u+\sum_{n=0}^{\infty} \frac{1}{n!\left(n+\left(\frac{4}{3} t^{\prime}+1\right)\right.}\left[\frac{4}{3}(-1)^{n}-u^{2}\right] \times\left(\ln \frac{1}{u}\right)^{n+1}\right] d t^{\prime}$
where $u=k / E_{0}$ and This refers to equation (24) in [13]. The result of this relation as plotted by Tsai-Whitis is as in fig 3.8.

The calculation is used to find out the photon spectrum and thereof knowing the total number of photons produced. This is required to predict the number of omega events and to compare it with experimental results. The above relations were simulated in MAPLE to find out the probability of finding a photon in a particular photon energy range namely between 2.5 GeV and 3.5 GeV . It is shown later that only omega events corresponding to these energies make it into the spectrometer and hence need to be considered. The results from the MAPLE simulation is shown in fig 3.9.

The horizontal axis is photon energy and vertical axis the photon spectrum. The above plot is integrated over the photon energies from 2.5 GeV to 3.5 GeV , which tells us the probabilty of finding a photon between 2.5 GeV and 3.5 GeV with electron beam energy of 5.7 GeV .

$$
\begin{equation*}
I_{\gamma}=0.0215 \tag{3.24}
\end{equation*}
$$

We now proceed to calculate the total number of photons produced in the expreriment.From experimental data, the total no of electrons with energy 5.7 GeV collided with the target are,

$$
\begin{equation*}
N_{e}=8.467 \times 10^{17} \tag{3.25}
\end{equation*}
$$

The total no of photons produced are given by,

$$
\begin{equation*}
N_{\gamma}=I_{\gamma} \times N_{e} \tag{3.26}
\end{equation*}
$$

This gives $N_{\gamma}=9.127 \times 10^{15}$

## CHAPTER IV

## RESULTS AND DISCUSSION

This chapter will present the results from the simulations and calculations for number of $\omega$ events based on the various t-models. Further analysis of cross-section events and photon energy spectrum wil demonstrate the reliability of the simulation.

### 4.1 Acceptance Calculations and $\boldsymbol{t}$-model Results

Acceptance refers to the acceptance of the spectrometers which is defined here as,

$$
\text { Acceptance }\left(A_{\text {model }}\right)=\frac{\text { Number of events in spectromters }}{\text { Total Number of vector meson events generated }}
$$

In the laboratory, the spectromters are located at a particular angle from beam line and are able to detect only a fraction of the vector meson events. The code attempts to simulate this and these results will be used later for predicting number of events based on the acceptance given by the code. The code has been run for 100 events in the spectrometer for all cases, hence is numerator in above ratio is always 100 .

### 4.1.1 Diffractive Model

The diffractive model is characterised by an exponential tail as can be seen in the top of Figure 4.1. One might recall Figure 1.1which also posessess similar feature. For this
model and with Ballam cross-section fit, the total number of $\omega$ events the code had to generate were 193529 to have 100 events in the spectromters.. The acceptance is given by,

$$
\begin{equation*}
A_{\text {diffractive }}=\frac{100}{193529}=5.167 \times 10^{-4} \tag{4.1}
\end{equation*}
$$

### 4.1.2 OPE and Diffractive model

This $t$ distribution resulting from OPE and diffractive model is shown in bottom of Figure 4.2. One can immediately observe the forward peak chracteristic in OPE which was the characteritic of one particle exchange model as discussed in section 1.3.2. This due to presence of a pole at $t=m_{\pi}^{2}$ which is in general the particle exchanged in the single particle exchange model. Further the diffractive charactristics as in section 4.1.1 are expected to approximate the OPE effect as OPE is simply sharp peaked. This fact becomes clear on the basis of several factors which we will see as the acceptance, cross-section and photon spectrum of OPE and difractive models.

The plot obtained below represents the differential cross-section in $t$ as given by [9] which was simplified to two variables using MAPLE and then"fed"to the main simulation. The total number of wevents the code generated for this model were 206931. The acceptance is given by,

$$
\begin{equation*}
A_{O P E+\text { diffractive }}=\frac{100}{206931}=4.835 \times 10^{-4} \tag{4.2}
\end{equation*}
$$



Figure 4.1
Diffractive $t$ distribution


Figure 4.2
OPE+Diffractive $t$ distribution


Figure 4.3
Photon Spectrum without Spectrometer cuts for Diffractive model


Figure 4.4
Photon Spectrum including Spectrometer cuts for Diffractive model


Figure 4.5
Photon Spectrum without Spectrometer cuts for OPE+Diffractive model


Figure 4.6
Photon Spectrum including Spectrometer cuts for OPE+Diffractive model

### 4.2 Photon Spectrum

This section shows results of the photon spectrum from the simulation which refers to the bremsstrahlung photon spectrum in the laboratory. The plots in Figure 4.2 show the effect of the spectrometer cuts on the spectrum. The photon spectrum after applying the spectrometer cuts tells us about the energy range of photons that make it into spectrometer. This range can be clearly seen to be from 2.5 GeV to 3.5 GeV . This serves an important simplication in such a way that, since we now know that only photons from 2.5 GeV to 3.5 GeV make it into the spectromter, the photon spectrum in Tsai and Whitis needs to be integrted only for this range. For the same reason, the ballam cross-section is considered only from 2.5 GeV and 3.5 GeV , as considering the entire spectrum will result in inefficiency and inaccuracy.

The effect of diffractive and OPE+diffractive model seem not to affect the photon spectrum, since the 'peaked characteristics' of these models is expected to have similar behaviour qualitatively.

As a check, one can also observe the effect of Ballam cross-section on the photon spectrum, the number of photon events tend to decrease with the photon energy meaning there are lesser omega events with higher photon energy.


Figure 4.7
Cross-section results for Diffractive model


Figure 4.8
Cross-section results for OPE + Diffractive model

### 4.3 Cross-section Calculations

The simulation results for Ballam cross-section are presented here and further this is used to obtain the mean value of cross-section which will be later used to calculate the number of omega events.

Figure 4.4 shows cross-section events for Diffractive and OPE+diffractive models. One might expect larger number of events for higher cross-section which is contrary to the plots. The drop in the cross-section is due to the spectrometer cuts which is seen from the plots wihtout spectrometer cuts.

The cross-section in the simulation is normalised to unity, where the normalisation factor was calculated in section 3.4. The cross-section calculations for the two models is as below,

1. Cross-section for Diffractive model The mean value of the cross-section is obtained from the top plot of Figure 4.4.

$$
\begin{equation*}
\sigma_{d i f f}=0.822 \mu b \tag{4.3}
\end{equation*}
$$

The normalised cross-section from section 3.4 is $\sigma_{\text {norm }}=6.277 \mu b$. Hence, the total cross-section is given by,

$$
\begin{equation*}
\sigma_{t o t}=\sigma_{\text {diff }} \sigma_{\text {norm }}=5.15 \mu b \tag{4.4}
\end{equation*}
$$

2. Cross-section for OPE+Diffractive model The mean value of the cross-section is obtained from the bottom plot of Figure 4.4.

$$
\begin{equation*}
\sigma_{d i f f}=0.8428 \mu b \tag{4.5}
\end{equation*}
$$

The total cross-section is given by,

$$
\begin{equation*}
\sigma_{t o t}=\sigma_{\text {diff }} \sigma_{\text {norm }}=5.29 \mu b \tag{4.6}
\end{equation*}
$$

### 4.4 Number of $\omega$ Events

In the laboratory, the experiment was conducted for five runs with known parameters such as the beam current, total beam charge, target configuration. The number of $\omega$ events are calculated from a simple relation from first principles in scattering as,

$$
\begin{equation*}
N_{\omega}=\frac{\sigma_{\omega} N_{0} \rho t N_{\gamma}}{A} \tag{4.7}
\end{equation*}
$$

where,(The target in this experiment was $3 \% \mathrm{Be}_{9}$ )

- $\sigma_{\omega}$ is the photoproduction crossection for $\omega$ from previous section,
- $N_{0}$ is Avogadro's number,
- $\rho$ is density of target $=1.848 \mathrm{gm} / \mathrm{cm}^{3}$,
- $t$ is thickness in radiation length $=1.06 \mathrm{~cm}$ for $3 \%$ r.l.
- $N_{\gamma}$ Number of incident photons as calculated in section 3.5
- $A$ is number of nucleons $=9$ for Be

Now for Diffractive model the number of events are given by

$$
\begin{equation*}
N_{\omega}=5.532 \times 10^{10} \tag{4.8}
\end{equation*}
$$

These are now corrected for the acceptance of the spectrometer $A_{d i f f}$ and the branching ratio of omega which is $=7.5 \times 10^{5}$

Hence the total Number of $\omega$ events predicted by from the simulation are,

$$
\begin{equation*}
N_{\omega d i f f}=1863 \text { events } \tag{4.9}
\end{equation*}
$$

The number of events for OPE and Diffractive are given by,

$$
\begin{equation*}
N_{\omega}=5.6831 \times 10^{10} \tag{4.10}
\end{equation*}
$$

The total events after acceptance correction and branching ratio is,

$$
\begin{equation*}
N_{\omega+O P E}=1923 \text { events } \tag{4.11}
\end{equation*}
$$

### 4.5 Conclusions and Future Work

Based on the resonable agreement between the monte-carlo prediction of the number of omega events with actual data, the monte-carlo is verified. In future, it will be used to determine the upper limit to the $J / \psi$ photoproduction cross-section from the null result of sub-threshold experiment. In addition, it will be used in the planning of future studies for the Jefferson lab high energy upgrade.

## REFERENCES

[1] J. R. Arrington, Inclusive electron scattering from nuclei at $x>1$ and high $Q^{2}$, doctoral dissertation, CALTECH, 1998.
[2] J. Ballam et al., "Vector-Meson Production by Polarized Photons at 2.8, 4.7, 9.3 GeV," Physical Review D, vol. 7, no. 11, June 1973.
[3] T. H. Bauer, R. D. Spital, D. R. Yennie, and F. M. Pipkin, "The hadronic properties of the photon in high-energy interactions," Review of Modern Physics, vol. 50, no. 2, April 1978.
[4] S. J. Brodsky, E. Chudakov, P. Hoyer, and J. M. Laget, "Photoproduction of charm near threshold," Phys. Lett. B498, Nov 2000.
[5] C. Caso, "Particle Data Group,".
[6] J. Dunne, "Hadron-05," Hadron-05, 2005.
[7] D. Dutta, The $\left(e, e^{\prime}, p\right)$ Reaction Mechanism in the Quasi-Elastic Region, doctoral dissertation, Northwestern University, Evanston, Illinois, June 1999.
[8] H. Frauenfelder and E. M. Henley, Subatomic Physics, 2 edition, Prentice Hall, New Jersey, 1991.
[9] P. Joos et al., " $\omega$ meson production by virtual photons," Nuclear Physics B122, , no. 365-382, 1977.
[10] D. Meekins, Coherent $\pi^{0}$ photoproduction on the deuteron, doctoral dissertation, College of William and Mary, Williamsburg, VA, 1996.
[11] M. I. Niculescu, Inclusive Resonance Electroproduction data from hydrogen and deuterium and studies of quark-hadron duality, doctoral dissertation, Hampton University, Hampton, VA, May 1999.
[12] M. L. Perl, "High Energy Hadron Physics," 1974.
[13] Y. S. Tsai and V. Whitis, "Thick-Target Bremsstrahlung and Target Considerations for Secondary-Particle Production vy Electrons," Physical Review, vol. 149, no. 4, September 1966.

## APPENDIX

THE MONTE-CARLO CODE

```
    Program photon
c
C
integer nwpawc,i,ink,lim,j,icycle,istat,count,irlu
integer N ! step size for event # print statement
parameter (nwpawc=200000)
real*4 h(nwpawc)
common/pawc/h
integer*4 nb_events,iocode,decay_ang_dep,nb_attempts,t_dep
logical mono_E,finished
character*4 extension
character*22 filename
character*4 targ
real*4 Nk_dev_range,Nk_dev,Nk_min,Nk_max,Nk
real*4 brem_dev_range,brem_dev,brem_min,brem_max,nu
real*4 Pp(4),Ppcm(4),Pg(4),Pgcm(4),beta(4),betasq, dir(3)
real*4 Pprf(3),Pgrf(4)
real*4 Ep,Eppcm,Ejcm,s,sth,theta,phi
real*4 pcm(4,2),pmu1,thmu1,phmu1,pmu2,thmu2,phmu2
real*4 thmu1_s,thmu2_s,phmu1_s,phmu2_s
real*4 Mp,Mj,pi,mj_width,mj0
real*4 b,z,p,m,q
real*4 alpha,random,ran_k,t_min,t_max,t_dev_range,t_dev,t,t_new
real*4 pppcm,pjcm,pjcm_v(4),pgcm_mag
real*4 thjcm,phjcm
real*4 Ejlab,Pjlab,Pjlab_v(4),thjlab,phjlab
real*4 k_cutoff ! splits the nk dist of nuclear matter into 2 regions
real*4 x_cutoff ! prob. of k being in region 1 (depends on max Egamma)
real*4 flat_int
real*4 exp_int
real*4 norm_flat
real*4 norm_exp
real*4 mjlow, mjhi
real*4 x(1001),y(1001),slope
real*4 raddeg/57.29578/
real*4 r,XX(200),XRAN
real*4 YY(200),YRAN
real*4 ZZ(200), ZRAN, crosssection, rand
real*4 sig,sig_min,sig_max,sig_dev
external breit_wigner
real*4 breit_wigner
external diff
real*4 diff
external ballamfit
real*4 ballamfit
COMMON s
real*4 tftot, rteps, x2low, x2high, xlow, xhigh
integer*4 ifunc,ierr
real*4 uncert, x2, x3, tftot1, tftot2, xrange
parameter (rteps = 0.0002)
C
```


## COMMON/FUNINT/TFTOT

```
logical spect_cuts,record_ntuple,weight,keep
```

logical spect_cuts,record_ntuple,weight,keep
real*4 sos_p0,sos_p_range,sos_th0,sos_th_range,sos_ph0,
real*4 sos_p0,sos_p_range,sos_th0,sos_th_range,sos_ph0,
> sos_ph_range, hms_p0,hms_p_range,hms_th0,hms_th_range,
> sos_ph_range, hms_p0,hms_p_range,hms_th0,hms_th_range,
> hms_ph0,hms_ph_range
> hms_ph0,hms_ph_range
common/spect_cuts/sos_p0,sos_p_range,sos_th0,sos_th_range,
common/spect_cuts/sos_p0,sos_p_range,sos_th0,sos_th_range,
> sos_ph0,sos_ph_range,hms_p0,hms_p_range,

```
> sos_ph0,sos_ph_range,hms_p0,hms_p_range,
```

```
>
hms_th0,hms_th_range,hms_ph0,hms_ph_range
C
```

```
        integer nb_var
```

        integer nb_var
        parameter (nb_var=32)
        parameter (nb_var=32)
        real*4 angs(nb_var)
        real*4 angs(nb_var)
        common/ntup/angs
        common/ntup/angs
    character*8 tags(nb_var)
    character*8 tags(nb_var)
    data angs/nb_var*0.0/
    data angs/nb_var*0.0/
    data tags/'Nu','Nk','Thp','Php','s','Pjcm','Ejcm','THjcm','PHjcm',
    data tags/'Nu','Nk','Thp','Php','s','Pjcm','Ejcm','THjcm','PHjcm',
    > 'PjLab','EjLab','ThjLab','PhjLab','z','t','tprime',
> 'PjLab','EjLab','ThjLab','PhjLab','z','t','tprime',
> 'Pmu_cm','Thmu_cm','Phmu_cm','Pmu1_l','Thmu1_l',
> 'Pmu_cm','Thmu_cm','Phmu_cm','Pmu1_l','Thmu1_l',
> 'Phmu1_l','Pmu2_l','Thmu2_l','Phmu2_l','Egam_rf','Mj',
> 'Phmu1_l','Pmu2_l','Thmu2_l','Phmu2_l','Egam_rf','Mj',
> 'Phsmu1','Thsmu1','Phsmu2','Thsmu2','crosssection'/
> 'Phsmu1','Thsmu1','Phsmu2','Thsmu2','crosssection'/
C
common/const/pi,raddeg,mj,mj0,mj_width
data pi/3.1415927/
data Mp/0.93827/
data Nk_min/0.0/
data Nk_max/1.0/
data brem_min/4.0/
data brem_max/8.0/
data k_cutoff/0.295/
data alpha/7.6753/
data norm_exp/47.3631/
data norm_flat/117.0/
external rndm
real*4 rndm
real rlu
Read input parameters
open(20,file='input.dat',iostat=iocode,status='old')
read (20,*) brem_max
read(20,*) nb_events
read(20,*) mono_E
read(20,*) extension
read(20,*) targ
read (20,*) b
read(20,*) mj
read(20,*) mj_width
read(20,*) N
read(20,*) decay_ang_dep
read (20,*) t_dep
read(20,*) spect_cuts
read(20,*) weight
close(20)
if(spect_cuts) then
if(mj.eq.3.098) then
open(20,file=' spect_cuts_jpsi.dat',
iostat=iocode,status='old')
>
elseif(mj.eq.1.02) then
open(20,file='spect_cuts_phi.dat',
>
elseif(mj.eq.0.782) then
open(20,file='spect_cuts_omega.dat',
>
iostat=iocode,status=' old')
endif
read(20,*) sos_p0
read(20,*) sos_p_range

```
```

        read(20,*) sos_th0
        read(20,*) sos_th_range
        read(20,*) sos_ph0
        read(20,*) sos_ph_range
        read (20,*) hms_p0
        read(20,*) hms_p_range
        read(20,*) hms_th0
        read(20,*) hms_th_range
        read(20,*) hms_ph0
        read(20,*) hms_ph_range
        close(20)
        sos_th0 = sos_th0/raddeg
        sos_th_range = sos_th_range/raddeg
        sos_ph0 = sos_ph0/raddeg
        sos_ph_range = sos_ph_range/raddeg
        hms_th0 = hms_th0/raddeg
        hms_th_range = hms_th_range/raddeg
        hms_ph0 = hms_ph0/raddeg
        hms_ph_range = hms_ph_range/raddeg
        record_ntuple=.false.
        else
            record_ntuple=.true.
    endif
open(20,file='int_'//targ//'_500.dat',iostat=iocode,status='old')
do i=1,501
read(20,*)y(i),x(i)
CX
write(6,*)x(i),y(i)
enddo
close(20)
filename = 'photon_'//targ//' _'//extension//'.hbook'
CX
if(mj.eq.3.098) then
brem_min = brem_max-0.3 ! I'm using a small E bin to compare w/ est.
elseif(mj.eq.1.02) then
brem_min = brem_max-0.1
elseif(mj.eq.0.782) then
brem_min = 2.5
endif
CX
C
call hlimit(nwpawc)
if(mj.eq.3.098) then
call hropen(2,'jpsi','jpsi_'//targ//' _'//extension//'.rz',
>
'N',1024,istat)
> elseif(mj.eq.1.02) then
call hropen(2,'jpsi','phi_'//targ//'_'//extension//'.rz',
>
'N',1024,istat)
elseif(mj.eq.0.782) then
if(t_dep.eq.0)then
call hropen(2,'jpsi','omeg0_'//targ//'_'//extension//'.rz',
>
'N',1024,istat)
elseif(t_dep.eq.1)then
call hropen(2,'jpsi','omeg1_'//targ//'_'//extension//'.rz',
>
'N',1024,istat)
elseif(t_dep.eq.2)then
call hropen(2,'jpsi','omeg2_'//targ//'_'//extension//'.rz',
>
'N',1024,istat)
endif
else
call hropen(2,'jpsi','unkn_'//targ//'_'//extension//'.rz',

```
```

> 'N',1024,istat)
endif
call hropen(3,'hbook',filename,'N',1024,istat)
call hbookn(9,'jpsi',nb_var,' jpsi',2000,tags)
call hbook1(100,'Photon spectrum',100,brem_min,brem_max,0.)
call hbook1(101,'Nk spectrum',100,nk_min,nk_max,0.)
if(brem_max.gt.8.5) then
call hbook1(102,'theta',200,0.0,180.,0.)
call hbook1(108,'theta thres',200,0.0,180.0,0.)
else
call hbook1(102,'theta',100,90.0,180.,0.)
call hbook1(108,'theta thres',100,90.0,180.0,0.)
endif
call hbook1(103,'phi',100,-180.,180.,0.)
if(mj.eq.3.098) then
call hbook1(104,'s',100,10.,20.,0.)
call hbook1(105,'s thres',100,10.,20.,0.)
call hbook1(110,'Eff. Photon E ',100,8.0,24.0,0.)
call hbook1(111,'Jpsi CM Energy ',100,3.0,4.0,0.)
call hbook1(112,'Jpsi CM momentum ',100,0.,2.0,0.)
call hbook1(115,'Jpsi Lab Energy ',100,3.0,8.0,0.)
call hbook1(116,'Jpsi Lab momentum ',100,0.,8.0,0.)
call hbook1 (120,'Muon1 Lab momentum ',100,0.,8.0,0.)
call hbook1(123,'Muon2 Lab momentum ',100,0.,8.0,0.)
call hbook2(300,'Lab P vs Lab theta',100,0.,180.,100,0.,9.0,30)
elseif(mj.eq.1.02) then
call hbook1(104,'s',100,2.,8.,0.)
call hbook1(105,'s thres',100,2.,8.,0.)
call hbook1(110,'Eff. Photon E ',100,1.5,4.0,0.)
call hbook1(111,'Jpsi CM Energy ',100,1.0,3.0,0.)
call hbook1(112,'Jpsi CM momentum ',100,0.,0.5,0.)
call hbook1(115,'Jpsi Lab Energy ',100,1.0,3.0,0.)
call hbook1(116,'Jpsi Lab momentum ',100,0.,3.0,0.)
call hbook1(120,'Muon1 Lab momentum ',100,0.,1.6,0.)
call hbook1(123,'Muon2 Lab momentum ',100,0.,1.6,0.)
call hbook2(300,'Lab P vs Lab theta',100,0.,180.,100,0.,1.6,30)
elseif(mj.eq.0.782) then
call hbook1(104,'s',100,2.,8.,0.)
call hbook1(105,'s thres',100,2.,8.,0.)
call hbook1(110,'Eff. Photon E ',100,1.5,4.0,0.)
call hbook1(111,'Jpsi CM Energy ',100,1.0,3.0,0.)
call hbook1(112,'Jpsi CM momentum ',100,0.,0.5,0.)
call hbook1(115,'Jpsi Lab Energy ',100,1.0,3.0,0.)
call hbook1(116,'Jpsi Lab momentum ',100,0.,3.0,0.)
call hbook1(120,'Muon1 Lab momentum ',100,0.,1.6,0.)
call hbook1(123,'Muon2 Lab momentum ',100,0.,1.6,0.)
call hbook2(300,'Lab P vs Lab theta',100,0.,180.,100,0.,1.6,30)
endif
call hbook1(106,'Nk thres',100,nk_min,nk_max,0.)
call hbook1(107,'Photon thres',100,brem_min,brem_max,0.)
call hbook1(113,'Jpsi CM theta ',100,0.,180.,0.)
call hbook1(114,'Jpsi CM phi ',100,-180.,180.,0.)
call hbook1(117,'Jpsi Lab theta ',100,0.,20.,0.)
call hbook1(118,'Jpsi Lab phi ',100,-180.,180.,0.)
call hbook1(121,'Muon1 Lab theta ',100,0.,180.,0.)
call hbook1(122,'Muon1 Lab phi ',100,-180.,180.,0.)
call hbook1(124,'Muon2 Lab theta ',100,0.,180.,0.)
call hbook1(125,'Muon2 Lab phi ',100,-180.,180.,0.)
call hbook2(301,'Lab P vs Lab theta',100,0.,180.,100,0.,180.0,30)
call hbook1(200,'Random',100,0.,1.,0.)

```
        exp_int = -norm_exp/alpha*
    > (exp(-alpha*nk_max) - exp(-alpha*k_cutoff))
    flat_int = norm_flat*(k_cutoff-nk_min)
    x_cutoff = flat_int/(flat_int + exp_int)
    finished = .false.
    count = 0
    nb_attempts=0
    mj0 = mj
    mjlow=mj0-mj_width*15
    mjhi =mj0+mj_width*15
    p=0
    q=0
    m=0
    do while(.not.finished)
        nb_attempts=nb_attempts+1
C do i =1,nb_events
C if(mod(i,N).eq.N-1) write (6,*)'Processing event number: ',i+1
            if(mono_E) then
                    nu = brem_max
                    nk}=0
                theta = 0.
                phi = 0.
        else
            brem_dev_range = log(brem_max/brem_min)
            random = rlu(irlu)
            brem_dev = brem_dev_range*random+ log(brem_min)
            nu = exp(brem_dev)
            ran_k = rlu(irlu)
            do ink=1,501
                    if(x(ink).gt.ran_k) then
                        lim=ink-1
                        goto 10
                    endif
            enddo
            continue
            slope=(y(lim+1)-y(lim))/(x(lim+1)-x(lim))
            nk=y(lim)+slope*(ran_k-x(lim))
            theta = acos(2.0*rlu(irlu)-1.0)
            phi= 2*pi*rndm(4)-pi
        endif
            if(ran_k.le.x_cutoff) then
                Nk = (exp_int+flat_int)/norm_flat*ran_k
            else
                Nk_dev_range= exp(-alpha*k_cutoff) - exp(-alpha*Nk_max)
                Nk_dev = Nk_dev_range*rlu(irlu) + exp(-alpha*Nk_max)
                Nk = -log(Nk_dev)/alpha
            endif
C Create j/psi's
        Pg(1)=0.0
        Pg(2)=0.0
        Pg(3) =nu
        Pg(4)=nu
        Ep = sqrt(Nk**2 + Mp**2) - (Nk**2)/(2*Mp) ! off-shell proton
        s = Ep*Ep-Nk*Nk +2.0*nu*Ep - 2.0*nu*Nk*cos(theta)
C Lorentz distribution for the mass
    CALL FUNLXP (breit_wigner,XX,mjlow,mjhi)
    CALL FUNLUX(XX,XRAN,1)
    mj=XRAN
    sth = (Mj+Mp)**2
```

```
        if(s.gt.sth) then
    keep =.true.
        if(weight) then
                crosssection = ballamfit(nu)
            rand = rlu(irlu)
            if(rand.ge.crosssection)then
                keep = .false.
            endif
            endif
    if(keep)then
        m=m+1
        if(t_dep.eq.0)then
        open(22,file=' omegaevents0.dat',iostat=iocode, status=' old')
        write(22,*)'Number of Omega Events: Uniform distribution:',m
        close(22)
        elseif(t_dep.eq.1)then
        open(22,file=' omegaevents1.dat',iostat=iocode, status='old')
        write(22,*)'Number of Omega Events: Exp distribution:',m
        close(22)
        elseif(t_dep.eq.2)then
        open(22,file=' omegaevents2.dat',iostat=iocode,status=' old')
        write(22,*)'Number of Omega Events: OPE distribution:',m
        close(22)
        endif
C Nucleon momentum in lab coordinate system
    Pp(1) = Nk*sin(theta)*cos(phi)
    Pp(2) = Nk*sin(theta)*sin(phi)
    Pp(3) = Nk*cos(theta)
    Pp(4) = Ep
C Calculate photon energy in off-shell proton's rest frame
    beta(1) = (Pp(1))/(Ep) !Beta is the vel of proton in LAB
    beta(2) = (Pp (2))/(Ep)
    beta(3) = (Pp(3))/(Ep)
    betasq = beta(1)**2+beta(2)**2+beta(3)**2
    beta(4) = (Ep)/sqrt(Ep**2-(Pp(1)**2+Pp(2)**2+Pp(3)**2))
    dir(1) = beta(1)/sqrt(betasq) ! Dir is dir of beta in LAB
    dir(2) = beta(2)/sqrt(betasq)
    dir(3) = beta(3)/sqrt(betasq)
    call gloren(beta,Pp,Pprf)
    call gloren(beta,Pg,Pgrf)
* Calculate CM quantities
    beta(1) = (Pp(1) +pg(1))/(Ep+pg(4)) !Beta is the vel of CM in LAB
    beta(2) = (Pp(2)+pg(2))/(Ep+pg(4))
    beta(3)=(Pp(3)+pg(3))/(Ep+pg(4))
    betasq = beta(1)**2+beta(2)**2+beta(3)**2
    beta(4) = (Ep+Pg(4))/sqrt(s)
    dir(1) = beta(1)/sqrt(betasq) ! Dir is dir of beta in LAB
    dir(2) = beta(2)/sqrt(betasq)
    dir(3) = beta(3)/sqrt(betasq)
    call gloren(beta,Pp,Ppcm)
    call gloren(beta,Pg,Pgcm)
* Calculate CM energies, momenta of j/psi and recoiling proton
    Eppcm = (s+Mp**2-Mj**2)/(2*sqrt(s)) ! recoiling proton cm energy
    Ejcm = sqrt(s)-Eppcm ! j/psi's cm energy
    Pppcm = sqrt(Eppcm**2-Mp**2)
    Pjcm = Pppcm
    if(t_dep.eq.1) then ! theta weighted by dsig/dt=exp(bt)
            pgcm_mag = sqrt(pgcm(1)**2+pgcm(2)**2+pgcm(3)**2)
            t_min = Mj**2 - 2.0*Pgcm(4)*Ejcm + 2.0*Pgcm_mag*Pjcm
            t_max = Mj**2 - 2.0*Pgcm(4)*Ejcm - 2.0*Pgcm_mag*Pjcm
            t_dev_range = exp (b*t_min) - exp (b*t_max)
            t_dev = t_dev_range*rlu(9) + exp (b*t_max)
            t = 1/b*log(t_dev)
```

```
    thjcm = acos((t-Mj**2+2*Pgcm(4)*Ejcm)/(2*Pgcm_mag*Pjcm))
    elseif(t_dep.eq.2) then ! diffractive cross-section terms
        pgcm_mag = sqrt (pgcm(1)**2+pgcm(2)**2+pgcm(3)**2)
        t_min = abs(Mj**2 - 2.0*Pgcm(4)*Ejcm + 2.0*Pgcm_mag*Pjcm)
        t_max = abs(Mj**2 - 2.0*Pgcm(4)*Ejcm - 2.0*Pgcm_mag*Pjcm)
            if(t_max.gt.4.5)then
                q=q+1
                    open(23,file='t_max.dat',iostat=iocode,status=' old')
                    write(23,*)'Value of s, t_min, t_max : ', s,t_min,t_max
                    close(23)
                t_max = 4.5
                CALL FUNLXP(diff,YY,t_min,t_max)
                    CALL FUNLUX(YY,YRAN,1)
                t=YRAN
        else
            CALL FUNLXP(diff,YY,t_min,t_max)
            CALL FUNLUX(YY,YRAN,1)
            t=YRAN
        endif
    elseif(t_dep.eq.0)then
        thjcm = acos(2.0*rlu(irlu)-1) ! theta uniform in cos
        t = Mj**2-2.0*Pgcm(4)*Ejcm+2.0*Pgcm_mag*Pjcm*Cos(thjcm)
        endif
        phjcm = 2*pi*rlu(irlu)-pi ! phi uniform from -pi to pi
    J/psi momentum in lab coordinate system
        Pjcm_v(1) = Pjcm*sin(thjcm)*cos(phjcm)
        Pjcm_v(2) = Pjcm*sin(thjcm)*sin(phjcm)
        Pjcm_v(3) = Pjcm*cos(thjcm)
        Pjcm_v(4) = Ejcm
        do j = 1,3 ! beta to go from CM to lab
            beta(j)=-beta(j)
        enddo
        call gloren(beta,Pjcm_v,Pjlab_v)
        Pjlab = sqrt(Pjlab_v(1)**2+Pjlab_v(2)**2+Pjlab_v(3)**2)
        Ejlab = Pjlab_v(4)
        thjlab = acos(Pjlab_v(3)/Pjlab)
        if(Pjlab_v(1).lt.0.0) then
        if(Pjlab_v(2).gt.0.0) then
            phjlab = atan(Pjlab_v(2)/Pjlab_v(1))+pi
        else
            phjlab = atan(Pjlab_v(2)/Pjlab_v(1))-pi
        endif
    else
        phjlab = atan(Pjlab_v(2)/Pjlab_v(1))
    endif
C Decay j/psi into 2 muons
    call decay(pjlab_v,pcm,decay_ang_dep)
C
    pmu1 = sqrt (pcm (1,1) **2+pcm (2,1) **2+\operatorname{pcm}(3,1) **2)
    thmu1= acos(pcm(3,1)/pmu1)
    if(pcm(2,1).lt.0.0) then
        if(pcm(1,1).gt.0.0) then
            phmu1 = atan (pcm(1,1)/pcm (2,1))+pi
        else
            phmu1 = atan(pcm(1,1)/pcm(2,1))-pi
        endif
        else
            phmu1 = atan(pcm(1,1)/pcm(2,1))
        endif
C Spectrometer angles
    phmu1_s = asin(sin(thmu1)*sin(phmu1))
    thmu1_s = acos(cos(thmu1)/cos(phmu1_s))
```

```
        pmu2 = sqrt (pcm (1,2) **2+pcm (2,2) **2+pcm (3,2) **2)
        thmu2= acos(pcm(3,2)/pmu2)
        if(pcm(2,2).lt.0.0) then
            if(pcm(1,2).gt.0.0) then
            phmu2 = atan (pcm (1,2)/pcm (2,2))+pi
        else
            phmu2 = atan (pcm (1,2)/pcm (2,2))-pi
        endif
        else
            phmu2 = atan(pcm(1,2)/pcm(2,2))
        endif
        if(spect_cuts) call spectrom(pmul,thmu1_s,phmu1_s,
                pmu2,thmu2_s,phmu2_s,record_ntuple)
            if(record_ntuple) then
            angs(1) = nu
            angs(2) = Nk
            angs(3) = theta
            angs(4) = phi
            angs(5) = s
            angs(6) = Pjcm
            angs(7) = Ejcm
            angs(8) = thjcm*raddeg
            angs(9) = Phjcm*raddeg
            angs(10) = Pjlab
            angs(11) = Ejlab
            angs(12) = thjlab*raddeg
            angs(13) = Phjlab*raddeg
            angs(14) = z
            angs(15) = t
            angs(16) = t-t_min
            angs(20) = pmul
            angs(21) = thmu1*raddeg
            angs(22) = phmul*raddeg
            angs(23) = pmu2
            angs(24) = thmu 2*raddeg
            angs(25) = phmu 2*raddeg
            angs(26) = Pgrf(4)
            angs(27) = mj
            angs(28) = phmul_s*raddeg
            angs(29) = thmul_s*raddeg
            angs(30) = phmu2_s*raddeg
            angs(31) = thmu2_s*raddeg
            angs(32) = crosssection
C
    call hfn(9,angs)
    do j = 1,nb_var
            angs(j) = 0.0
    enddo
    count = count + 1
    if(count.ge.nb_events) finished = .true.
    if(mod(count,N).eq.N-1) then
            write(6,*)'Processing event number: ',count+1
        endif
        endif
C
C
                                    Fill histograms
```

```
C
        if(nb_attempts.le.1000000) then
            call hfill(105,s,0.,1.)
            call hfill(106,nk,0.,1.)
            call hfill(107,nu,0.,1.)
            call hfill(108,theta*raddeg,0.,1.)
            call hfill(110,pgrf(4),0.,1.)
            call hfill(111,Ejcm,0.,1.)
            call hfill(112,Pjcm,0.,1.)
            call hfill(113,thjcm*raddeg,0.,1.)
            call hfill(114,phjcm*raddeg,0.,1.)
            call hfill(115,Ejlab,0.,1.)
            call hfill(116,Pjlab,0.,1.)
            call hfill(117,thjlab*raddeg,0.,1.)
            call hfill(118,phjlab*raddeg,0.,1.)
            call hfill(120,pmu1,0.,1.)
            call hfill(121,thmul*raddeg,0.,1.)
            call hfill(122,phmul*raddeg,0.,1.)
            call hfill(123,pmu2,0.,1.)
            call hfill(124,thmu2*raddeg,0.,1.)
            call hfill(125,phmu 2*raddeg,0.,1.)
            call hfill(300,thmu1*raddeg,pmu1,1.)
            call hfill(301,thmu1*raddeg,thmu2*raddeg,1.)
        endif
        endif
        endif
        if(nb_attempts.le.1000000) then
            call hfill(100,nu,0.,1.)
            call hfill(101,Nk,0.,1.)
            call hfill(102,theta*raddeg,0.,1.)
            call hfill(103,phi*raddeg,0.,1.)
            call hfill(104,s,0.,1.)
            call hfill(200,random,0.,1.)
        endif
    enddo
    write(6,*)'Number of times t > 4.0: ',p
    write( }6,*\mp@subsup{)}{}{\prime}\mathrm{ Number of times t_max > 4.0: ',q
    write(6,*) 'The number of attempts is: ',nb_attempts
    close(21)
    call hrout(0,icycle,' ')
    call hrend('jpsi')
    do i=100,125
        if(i.ne.109.and.i.ne.119) then
            call hrput(i,filename,'n')
        endif
        enddo
        call hrput(200,filename,'n')
        call hrput(300,filename,'n')
        call hrput(301,filename,'n')
        end
C
C********************************************************************************
    subroutine decay(jlab,gkin,ang_dep)
    Hardwired for j/psi as parent particle
            I should generate the mass from a Lorentz distribution
            if the lifetime is less than 10^-15 sec
        integer irlu
        real*4 jlab(4) ! Lab 4 momentum of parent particle
    real*4 jlab_mag ! Lab 3 momentum squared
```

```
    real*4 gkin(4,2) ! Lab 4 momentum of decay particles
    real*4 pcm(4,2)
    real*4 beta(4)
    real*4 dir(3) ! direction of parent in Lab coordinate
    real*4 costh,sinth,cosph,sinph
    real*4 xm(2)
    real*4 mj,pi,raddeg,mj_width,mj0
    real*4 mmu/0.105659/
    real rlu
    integer ang_dep ! 0: isotropic in decay angle
            ! 1: weighted by 1+cos(th_cm)**2
    logical rotate
C
    common/const/pi,raddeg,mj,mj0,mj_width
C
C 2 body decay
C
    xm(1) =mmu
    xm(2) =mmu
c
    call deca2(mj,xm(1),xm(2),pcm,ang_dep)
    boost into LAB along parent vector followed by rotation back into
    correct coordinate system
    jlab_mag = sqrt(jlab(1)**2+jlab(2)**2+jlab(3)**2)
    do i = 1,3
    dir(i) = jlab(i)/jlab_mag
    enddo
    beta(1) = 0.0
    beta(2) = 0.0
    beta(3) = -jlab_mag/jlab(4)
    beta(4) = jlab(4)/mj
    call gfang(dir,costh,sinth,cosph,sinph,rotate)
C
    do i = 1,2
        if(jlab_mag.le.0.0) then
            do j = 1,3
                gkin(j,i)=pcm(j,i)
            enddo
        else
        call gloren(beta,pcm(1,i),gkin(1,i))
            endif
CX remove
            rotate=.false.
CX
            if(rotate) call gdrot(gkin(1,i),costh,sinth,cosph,sinph)
            gkin(4,i)=\operatorname{sqrt}(\operatorname{gkin}(1,i)**2+gkin}(2,i)**2+gkin(3,i)**2+xm(i)**2
        enddo
C
        return
        end
C
C****************************************************************************
    subroutine deca2(xm0,xm1,xm2,pcm,ang_dist)
    C
C
    implicit none
    integer irlu
    integer ang_dist ! 0: isotropic in decay angle; 1: 1+cos^2(theta)
    real*4 xm0 ! mass of parent particle
    real*4 xm1,xm2 ! masses of two body decay products
    real*4 pcm(4,2) ! momenta of decay products
```

```
    real*4 costh,sinth
    real*4 phi
    real*4 E1,P1
    real*4 twopi/6.283185307/
    real*4 raddeg/57.29578/
C
C
C
C
C
C
C
C
C
    pcm(1,1)=P1*sinth*cos(phi)
    pcm(2,1)=P1*sinth*sin(phi)
    pcm (3,1) =P1*costh
    pcm(4,1)=E1
C
C
C
        pcm(1,2)=-pcm (1,1)
    pcm (2,2) =-pcm (2,1)
    pcm (3,2) =-pcm (3,1)
        pcm}(4,2)=\operatorname{sqrt}(\operatorname{pcm}(1,2)**2+\operatorname{pcm}(2,2)**2+\operatorname{pcm}(3,2)**2+xm2*xm2
C
        return
        end
C*******************************************************************************
        subroutine spectrom(p1,th1,ph1,p2,th2,ph2,record)
            See if muons make it into the spectrometers
    integer nb_var
    parameter (nb_var=32)
    real*4 angs(nb_var)
    common/ntup/angs
    external rndm
    real*4 rndm
    real rlu
    Generate first decay product in CMS
    E1=(xm0*xm0+xm1*xm1-xm2*xm2) / (2*xm0)
    P1=sqrt (abs((E1-xm1) *(E1+xm1)))
        Generate angular distribution
        if(ang_dist.eq.0) then
        costh=2.*rlu(irlu)-1.
    else
        costh=2.*rlu(irlu)-1.
        if(2*rlu(irlu).ge.(1+(costh)**2)) goto 30
        endif
        if(abs(costh).ge.1.0) then
        costh=sign(1.0, costh)
        sinth=0.
    else
        sinth=sqrt((1.-costh)*(1.+costh))
    endif
    phi=twopi*rlu(irlu)
    angs(17) = p1
    angs(18) = acos(costh)*raddeg
    angs(19) = phi*raddeg
    Polar co-ordinates to momentum components
    Generate second decay product
```

C

```
        real*4 p1,th1,ph1,p2,th2,ph2
        logical record
        real*4 ph1_s,ph2_s
    real*4 sos_p0,sos_p_range,sos_th0,sos_th_range,sos_ph0,
    > sos_ph_range, hms_p0,hms_p_range,hms_th0,hms_th_range,
> hms_ph0,hms_ph_range
    common/spect_cuts/sos_p0,sos_p_range,sos_th0,sos_th_range,
    > sos_ph0,sos_ph_range,hms_p0,hms_p_range,
> hms_th0,hms_th_range,hms_ph0,hms_ph_range
    >
```

    record=.false.
    ph1_s=atan (tan (ph1) *sin(th1))
    ph2_s=atan(tan(ph2)*sin(th2))
    if(ph1.ge.sos_ph0-sos_ph_range.and.
    $>$ ph1.le.sos_ph0+sos_ph_range) then
if (ph2.ge.hms_ph0-hms_ph_range.and.
> ph2.le.hms_ph0+hms_ph_range) then
if (th1.ge.sos_th0-sos_th_range.and.
$>\quad$ th1.le.sos_th0+sos_th_range) then
if (th2.ge.hms_th0-hms_th_range.and.
if (th2 $\cdot$ ge.hms_th0-hms_th_range.and.
th2.le.hms_th0+hms_th_range) then
if(p1.ge.sos_p0*(1.0-sos_p_range).and.
$>\quad$ if(p1.ge.sos_p0*(1.0-sos_p_range) .and.
$\left.>\quad \begin{array}{rl}\mathrm{p} 1 . l e . \operatorname{sos} \_p 0 *(1.0+\text { sos_p_range })\end{array}\right)$ then
$\left.>\quad \begin{array}{c}\mathrm{p} 1 . \mathrm{le} . \mathrm{sos} \_\mathrm{p} 0 *\left(1.0+\mathrm{sos} \_\mathrm{p} \_ \text {range }\right)\end{array}\right)$
$>\quad \mathrm{p} 2 . \mathrm{le} . \mathrm{hms} \_\mathrm{p} 0 *\left(1.0+\mathrm{hms} \_\right.$p_range $)$) then
record=.true.
endif
endif
endif
endif
endif
endif
return
end
BREIT-WIGNER MASS DISTRIBUTION FUNCTION
real*4 function Breit_Wigner(x)
real*4 pi,raddeg, mj, mj_width,mj0
common/const/pi,raddeg,mj,mj0,mj_width
Breit_Wigner=
$>1 . /(\mathrm{mj} 0 * \mathrm{pi} * \mathrm{mj}$ _width*( $1+(((\mathrm{x} * * 2-\mathrm{mj} 0 * * 2) /(\mathrm{mj} 0 * \mathrm{mj}$ _width $)) * * 2)))$
return
end
FUNCTION FOR ONE PION EXCHANGE AND DIFFRACTIVE CROSS-SECTION
C
C

FUNCTION FOR ONE PION EXCHANGE AND DIFFRACTIVE CROSS-SECTION

```
    real*4 function diff(t)
    real*4 pi,raddeg,mj,mj_width,mj0,s
    common/const/pi,raddeg,mj,mj0,mj_width
    common s
    diff = (0.215e4*t*(.25*(.880-s)*(1.49-s+t)-.25*(s**(1/2)-.938)**2*
>(s** (1/2)+.938)**2)**2* (0.472e-1* (4.34*t**2+5.28*t+2.63)*log (8.68
>*t**2+10.6*t+4.26)/(.410*t**2+.500*t+.154)-1)/((s-.880)**2*s*(t+0
>.196e-1)**2*(s**(1/2)-.938)**2*(s**(1/2)+.938)**2*(1+2.40*t* (t+3.5
>2))*(.410*t**2+.500*t+.154)**2))+(62.61*exp (-6.7*t)* (1+(2.626/
>(s-0.879))))!differential cross-section OPE and diffractive terms
C (THIS DIFFERENTIAL CROSS-SECTION IS OBTAINED BY PLUGGING t=(-t) IN ORIGINAL CODE)
    continue
    return
```

end
FUNCTION FOR CROSS-SECTION FIT FOR BALLAM DATA

```
        real*4 function ballamfit(z)
        ballamfit =
        >.8442613249+(.1592945896*((z-2.8)/(.2831924835-.2360169021*z)))
C THIS FUNCTION IS TO BE USED ONLY WHEN spect_cuts IS ON
C BCOZ IT IS OVER THE RANGE brem_min to brem_max
    continue
    return
    end
```


SUBROUTINE FUNLXP (FUNC, XFCUM, X2LOW, X2HIGH)
F. JAMES, Sept, 1994
Prepares the user function FUNC for FUNLUX
Inspired by and mostly copied from FUNPRE and FUNRAN
except that
1. FUNLUX uses RANLUX underneath,
2. FUNLXP expands the first and last bins to cater for
functions with long tails on left and/or right,
3. FUNLXP calls FUNPCT to do the actual finding of percentiles.
4. both FUNLXP and FUNPCT use RADAPT for Gaussian integration.
real*4 tftot, rteps, x2low, x2high, xlow, xhigh
integer*4 ifunc,ierr
real*4 uncert, $x 2$, $x 3$, tftot1, tftot 2 , xrange
EXTERNAL FUNC
DIMENSION XFCUM (200)
COMMON/FUNINT/TFTOT
PARAMETER (RTEPS=0.0002)
SAVE IFUNC
DATA IFUNC/0/
IFUNC $=$ IFUNC +1
FIND RANGE WHERE FUNCTION IS NON-ZERO.
CALL FUNLZ (FUNC, X2LOW, X2HIGH, XLOW, XHIGH)
XRANGE $=$ XHIGH-XLOW
IF (XRANGE .LE. O.) THEN
WRITE (6,'(A,2G15.5)') ' FUNLXP finds function range .LE.0',
+ XLOW,XHIGH
GO TO 900
ENDIF
CALL RADAPT (FUNC, XLOW, XHIGH,1,RTEPS, 0., TFTOT ,UNCERT)
C WRITE $(6,1003)$ IFUNC, XLOW, XHIGH, TFTOT
C 1003 FORMAT(' FUNLXP: integral of USER FUNCTION',
C + I3,' from ',E12.5,' to ',E12.5,' is ',E14.6)
C
C WRITE (6,' (A,A)') ' FUNLXP preparing ',
C + 'first the whole range, then left tail, then right tail.'
CALL FUNPCT (FUNC, IFUNC, XLOW, XHIGH, XFCUM, 1, 99, TFTOT,IERR)
IF (IERR .GT. 0) GO TO 900
$\mathrm{X} 2=\mathrm{XFCUM}(3)$
CALL RADAPT (FUNC, XLOW, X2, 1,RTEPS, 0.,TFTOT1 , UNCERT)
CALL FUNPCT (FUNC, IFUNC, XLOW, X2 ,XFCUM,101,49,TFTOT1,IERR)
IF (IERR.GT. 0) GO TO 900
$\mathrm{X} 3=\mathrm{XFCUM}(98)$
CALL RADAPT (FUNC, X3, XHIGH, 1, RTEPS, 0., TFTOT2 , UNCERT)

```
        CALL FUNPCT (FUNC, IFUNC, X3,XHIGH,XFCUM,151,49,TFTOT2,IERR)
        IF (IERR .GT. 0) GO TO 900
C WRITE (6,1001) IFUNC,XLOW,XHIGH
C 1001 FORMAT(' FUNLXP has prepared USER FUNCTION',I3,
C + ' between',G12.3,' and',G12.3,' for FUNLUX')
    RETURN
    900 CONTINUE
        WRITE (6,'(A)') ' Fatal error in FUNLXP. FUNLUX will not work.'
        END
C
    SUBROUTINE FUNPCT (FUNC,IFUNC,XLOW,XHIGH,XFCUM,NLO,NBINS,TFTOT,
    + IERR)
        Array XFCUM is filled from NLO to NLO+NBINS, which makes
        the number of values NBINS+1, or the number of bins NBINS
    EXTERNAL FUNC
    DIMENSION XFCUM(*)
    PARAMETER (RTEPS=0.005, NZ=10, MAXZ=20, NITMAX=6,PRECIS=1.E-6)
        DOUBLE PRECISION TPCTIL, TZ, TCUM, XINCR, DTABS,
CC DOUBLE PRECISION TPCTIL, TZ, TCUM, XIN
C
    IERR = 0
    IF (TFTOT .LE. O.) GO TO 900
    TPCTIL = TFTOT/NBINS
    TZ = TPCTIL/NZ
    TZMAX = TZ * 2.
    XFCUM (NLO) = XLOW
    XFCUM(NLO+NBINS) = XHIGH
    X = XLOW
    F = FUNC (X)
    IF (F .LT. O.) GO TO 900
C
    TCUM = 0.
    X1 = X
    F1 = F
    DXMAX = (XHIGH -X) / NZ
    FMIN = TZ/DXMAX
        FMINZ = FMIN
C
    XINCR = TZ/MAX(F1,FMIN,FMINZ)
    350 X = X1 + XINCR
    F = FUNC (X)
        IF (F .LT. O.) GO TO 900
        TINCR = (X-X1) * 0.5 * (F+F1)
        IF (TINCR .LT. TZMAX) GO TO 370
        XINCR = XINCR * 0.5
        GO TO 350
    370 CONTINUE
        TCUM = TCUM + TINCR
        IF (TCUM .GE. TPCTIL*0.99) GO TO 520
        FMINZ = TZ*F/ (TPCTIL-TCUM)
        F1 = F
        X1 = X
    500 CONTINUE
        WRITE(6,'(A)') ' FUNLUX: WARNING. FUNPCT fails trapezoid.'
            END OF TRAPEZOID LOOP
            Adjust interval using Gaussian integration with
            Newton corrections since F is the derivative
    5 2 0 ~ C O N T I N U E
        X1 = XFCUM(IBIN)
        XBEST = X
        DTBEST = TPCTIL
```

```
    TPART = TPCTIL
C
    DO 550 IHOME= 1, NITMAX
    535 XINCR = (TPCTIL-TPART) / MAX(F,FMIN)
        X = XBEST + XINCR
        X2 = X
            IF (IHOME .GT. 1 .AND. X2 .EQ. XBEST) THEN
            WRITE (6,'(A,G12.3)')
        + ' FUNLUX: WARNING from FUNPCT: insufficient precision at X=',X
            GO TO 580
            ENDIF
        REFX = ABS (X) +PRECIS
        CALL RADAPT (FUNC, X1,X2,1,RTEPS,0.,TPART2,UNCERT)
        DTPAR2 = TPART2-TPCTIL
        DTABS = ABS (DTPAR2)
        IF (ABS (XINCR)/REFX .LT. PRECIS) GOTO 545
        IF (DTABS .LT. DTBEST) GOTO 545
        XINCR = XINCR * 0.5
        GOTO 535
    545 DTBEST = DTABS
        XBEST = X
        TPART = TPART2
        F = FUNC(X)
        IF(F .LT. O.) GOTO 900
        IF(DTABS .LT. RTEPS*TPCTIL) GOTO 580
    5 5 0 ~ C O N T I N U E ~
        WRITE (6,' (A,I4)')
        + ' FUNLUX: WARNING from FUNPCT: cannot converge, bin',IBIN
C
    5 8 0 ~ C O N T I N U E
        XINCR = (TPCTIL-TPART) / MAX(F,FMIN)
        X = XBEST + XINCR
        XFCUM(IBIN+1) = X
        F = FUNC (X)
        IF(F .LT. O.) GOTO 900
    600 CONTINUE
C END OF LOOP OVER BINS
        X1 = XFCUM(NLO+NBINS-1)
        X2 = XHIGH
        CALL RADAPT(FUNC,X1,X2,1,RTEPS,0.,TPART ,UNCERT)
        ABERR = ABS(TPART-TPCTIL)/TFTOT
C WRITE (6,1001) IFUNC,XLOW,XHIGH
C IF(ABERR .GT. RTEPS) WRITE (6,1002) ABERR
    RETURN
    900 WRITE (6,1000) X,F
        IERR = 1
        RETURN
    1000 FORMAT(/' FUNLUX fatal error in FUNPCT: function negative:'/
    + ,' at X=',E15.6,', F=',E15.6/)
C 1001 FORMAT(' FUNPCT has prepared USER FUNCTION',I3,
C +' between',G12.3,' and',G12.3,' for FUNLUX.')
C 1002 FORMAT(' WARNING: Relative error in cumulative distribution',
C + ' may be as big as',F10.7)
        END
        SUBROUTINE FUNLUX(ARRAY,XRAN,LEN)
C Generation of LEN random numbers in any given distribution,
C by 4-point interpolation in the inverse cumulative distr.
            by 4-point interpolation in the inverse 
        COMMON/FUNINT/XUNI
        DIMENSION ARRAY(200)
        DIMENSION XRAN(LEN)
C Bin width for main sequence, and its inverse
    PARAMETER (GAP= 1./99., GAPINV=99.)
```

```
C Top of left tail, bottom of right tail (each tail replaces 2 bins)
    PARAMETER (TLEFT= 2./99.,BRIGHT=97./99.)
    Bin width for minor sequences (tails), and its inverse
        PARAMETER (GAPS=TLEFT/49., GAPINS=1./GAPS)
C
C
C
C
C
C
C
C
C
    CALL RANLUX(XRAN,LEN)
    DO 500 IBUF= 1, LEN
    X = XRAN(IBUF)
    J = INT( X *GAPINV) + 1
    IF (J .LT. 3) THEN
        J1 = INT( X *GAPINS)
            J = J1 + 101
            J = MAX(J,102)
            J = MIN(J,148)
        P = ( X -GAPS* (J1-1)) * GAPINS
        A = (P+1.0) * ARRAY (J+2) - (P-2.0)*ARRAY (J-1)
        B = (P-1.0) * ARRAY(J) - P * ARRAY (J+1)
        XRAN(IBUF) = A*P* (P-1.0)*0.16666667+B*(P+1.0)*(P-2.0)*0.5
    ELSE IF (J .GT. 97) THEN
        J1 = INT((X-BRIGHT)*GAPINS)
            J = J1 + 151
            J = MAX (J,152)
            J = MIN(J,198)
        P = (X -BRIGHT -GAPS*(J1-1)) * GAPINS
        A = (P+1.0) * ARRAY (J+2) - (P-2.0)*ARRAY (J-1)
        B = (P-1.0) * ARRAY(J) - P * ARRAY (J+1)
        XRAN(IBUF) = A*P* (P-1.0)*0.16666667 + B* (P+1.0)* (P-2.0)*0.5
    ELSE
        J = MAX (J,2)
        J = MIN(J,98)
        P = ( X -GAP* (J-1)) * GAPINV
        A = (P+1.0) * ARRAY (J+2) - (P-2.0)*ARRAY (J-1)
        B = (P-1.0) * ARRAY(J) - P * ARRAY (J+1)
        XRAN(IBUF) = A*P* (P-1.0)*0.16666667 + B* (P+1.0)* (P-2.0)*0.5
    ENDIF
5 0 0 ~ C O N T I N U E ~
    XUNI = X
    RETURN
    END
    SUBROUTINE FUNLZ (FUNC,X2LOW,X2HIGH,XLOW,XHIGH)
            FIND RANGE WHERE FUNC IS NON-ZERO.
            WRITTEN 1980, F. JAMES
            MODIFIED, NOV. 1985, TO FIX BUG AND GENERALIZE
            TO FIND SIMPLY-CONNECTED NON-ZERO REGION (XLOW,XHIGH)
            ANYWHERE WITHIN THE GIVEN REGION (X2LOW,H2HIGH).
            WHERE 'ANYWHERE' MEANS EITHER AT THE LOWER OR UPPER
                    EDGE OF THE GIVEN REGION, OR, IF IN THE MIDDLE,
            COVERING AT LEAST 1% OF THE GIVEN REGION.
            OTHERWISE IT IS NOT GUARANTEED TO FIND THE NON-ZERO REGION.
            IF FUNCTION EVERYWHERE ZERO, FUNLZ SETS XLOW=XHIGH=0.
    EXTERNAL FUNC
    XLOW = X2LOW
    XHIGH = X2HIGH
            FIND OUT IF FUNCTION IS ZERO AT ONE END OR BOTH
```

```
        XMID = XLOW
        IF (FUNC(XLOW) .GT. O.) GO TO 120
        XMID = XHIGH
        IF (FUNC(XHIGH) .GT. O.) GO TO 50
            FUNCTION IS ZERO AT BOTH ENDS,
C
    LOOK FOR PLACE WHERE IT IS NON-ZERO.
        DO 30 LOGN= 1, 7
        NSLICE = 2**LOGN
        DO 20 I= 1, NSLICE, 2
        XMID = XLOW + I * (XHIGH-XLOW) / NSLICE
        IF (FUNC (XMID) .GT. 0.) GO TO 50
    20 CONTINUE
    3 0 ~ C O N T I N U E
            FALLING THROUGH LOOP MEANS CANNOT FIND NON-ZERO VALUE
        WRITE (6,554)
        WRITE (6,555) XLOW, XHIGH
        XLOW = 0.
        XHIGH = 0.
        GO TO 220
C
C
        = XMID
        XL = XLOW
        DO 70 K= 1, 20
        XNEW = 0.5*(XH+XL)
        IF (FUNC(XNEW) .EQ. O.) GO TO 68
        XH = XNEW
        GO TO 70
    6 8 ~ X L ~ = ~ X N E W ~
    70 CONTINUE
        XLOW = XL
        WRITE (6,555) X2LOW,XLOW
    120 CONTINUE
        IF (FUNC(XHIGH) .GT. O.) GO TO 220
            DELETE 'TRAILING' RANGE OF ZEROES
        XL = XMID
        XH = XHIGH
        DO 170 K= 1, 20
        XNEW = 0.5* (XH+XL)
        IF (FUNC(XNEW) .EQ. O.) GO TO 168
        XL = XNEW
        GO TO 170
    168 XH = XNEW
    170 CONTINUE
        XHIGH = XH
        WRITE (6,555) XHIGH, X2HIGH
C
    2 2 0 ~ C O N T I N U E
        RETURN
    5 5 4 ~ F O R M A T ( ' O C A N N O T ~ F I N D ~ N O N - Z E R O ~ F U N C T I O N ~ V A L U E ' ) ,
    555 FORMAT(' FUNCTION IS ZERO FROM X=',E12.5,' TO ',E12.5)
        END
```

