

1 **Title**

2 Osmium and lithium isotope evidence for weathering feedbacks linked to orbitally paced  
3 organic carbon burial and Silurian glaciations

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30

### 31 **Abstract**

32 The Ordovician (~487 to 443 Ma) ended with the formation of extensive Southern  
33 Hemisphere ice sheets, known as the Hirnantian glaciation, and the second largest mass  
34 extinction in Earth History. It was followed by the Silurian (~443 to 419 Ma), one of the most  
35 climatically unstable periods of the Phanerozoic as evidenced by several large scale (> 5 ‰)  
36 carbon isotope ( $\delta^{13}\text{C}$ ) perturbations associated with further extinction events. Despite several  
37 decades of research, the cause of these environmental instabilities remains enigmatic. Here,  
38 we provide osmium ( $^{187}\text{Os}/^{188}\text{Os}$ ) and lithium ( $\delta^7\text{Li}$ ) isotope measurements of marine  
39 sedimentary rocks that cover four Silurian  $\delta^{13}\text{C}$  excursions. Osmium and Li isotope records  
40 resemble those previously recorded for the Hirnantian glaciation suggesting a similar causal  
41 mechanism. When combined with a new dynamic carbon-osmium-lithium biogeochemical  
42 model we suggest that astronomical forcing of the marine organic carbon cycle, as opposed to  
43 a decline in volcanic arc degassing or the rise of early land plants, resulted in drawdown of  
44 atmospheric  $\text{CO}_2$ , triggering continental scale glaciation, intense global cooling and eustatic  
45 sea-level lows recognised in the geological record. Lower atmospheric  $p\text{CO}_2$  and  
46 temperatures during the Hirnantian and Silurian glaciations suppressed  $\text{CO}_2$  removal by  
47 silicate weathering, driving  $^{187}\text{Os}/^{188}\text{Os}$  and  $\delta^7\text{Li}$  variability, supporting the existence of  
48 climate-regulating feedbacks.

49

50 **Keywords:** Osmium isotopes ( $^{187}\text{Os}/^{188}\text{Os}$ ), Lithium isotopes ( $\delta^7\text{Li}$ ), Silurian palaeoclimate,  
51 Hirnantian glaciation, Orbital obliquity, eccentricity and precession, Silicate weathering.

52

### 53 **1. Introduction**

54 The Earth's ecosystems underwent profound changes during the Ordovician and Silurian.  
55 Global cooling towards present-day equatorial sea surface temperatures (Trotter et al., 2008)  
56 coupled to a rise in atmospheric  $\text{O}_2$  led to an abrupt increase in marine diversity during the  
57 Great Ordovician Biodiversification Event (Rasmussen et al., 2019). Increased volcanism  
58 during the Katian led to a gradual decline in biodiversity toward the end of the Ordovician,  
59 terminating with the Late Ordovician mass extinction (Rasmussen et al., 2019). This first of  
60 the Phanerozoic 'Big Five' extinctions coincided with the initiation of icehouse conditions  
61 and the extensive expansion of Southern Hemisphere continental ice, the Hirnantian  
62 glaciation (Algeo et al., 2016). A return to rapid biodiversity accumulation rates did not occur  
63 in the Silurian (Rasmussen et al., 2019), which was characterised by environmental  
64 instabilities linked to both minor and significant extinctions such as the 'Ireviken', 'Mulde',  
65 'Lau' and 'Silurian-Devonian Boundary' bioevents (Fig. 1I; Calner, 2008).

66 The Hirnantian glaciation and Late Ordovician mass extinction are linked to a long-  
67 term decline in global temperatures brought about by some combination of: the enhanced  
68 weatherability of silicates, related to land-plant colonisation (Lenton et al., 2012) and/or the  
69 passage of fresh volcanic material through the tropics (Nardin et al., 2011); a reduction in  
70 volcanic arc degassing (McKenzie et al., 2016; Pogge von Strandmann et al., 2017); and/or  
71 an increase in organic carbon burial (Sproson, 2020). Although these processes continued to  
72 influence global climate well into the Silurian (Lenton et al., 2016; McKenzie et al., 2016;  
73 Nardin et al., 2011; Page et al., 2007), some explanations for Silurian bioevents have invoked  
74 a shift between two stable oceanic-climate states, driven by latitudinal changes in deep-water

75 formation (Jeppsson, 1990), or variations in global precipitation rates and continental runoff  
76 (Bickert et al., 1997). However, both the end-Ordovician and the Silurian extinction events  
77 are marked by similar variations in global  $\delta^{13}\text{C}$  (Fig. 1J), oxygen isotopes ( $\delta^{18}\text{O}$ ; Fig. 1L),  
78 eustatic sea-level (Fig. 1M) and lithological records (Calner, 2008; Munnecke et al., 2003),  
79 suggesting a similar causal link.

80 It has been postulated that Silurian climatic change and extinction events could have  
81 been driven by glacial expansion over Gondwana (Frýda et al., 2021; Munnecke et al., 2010;  
82 Trotter et al., 2016), much like the Late Ordovician that preceded it, astronomically paced by  
83 the  $\sim 4.5$  Myr amplitude modulation of the cyclic eccentricity (400 kyr and 100 kyr) or  
84 obliquity (41 kyr) parameters of the Earth's axial motion and orbit (Sproson, 2020).  
85 Astronomical forcing of Silurian climate is supported by graptoloid turnover rates from the  
86 Late Ordovician to latest Silurian which correlate to the  $\sim 2.6$  Myr eccentricity and  $\sim 1.3$  Myr  
87 obliquity cycles (Crampton et al., 2018). Moreover, high resolution stratigraphic records for  
88 the Hirnantian glaciation suggest multiple glacial maxima paced by the  $\sim 1.2$  Myr axial  
89 obliquity (Ghienne et al., 2014) or the  $\sim 100$  kyr eccentricity (Sutcliffe et al., 2000) cycles.  
90 However, the lack of glacial sedimentary rocks in the post-Sheinwoodian stratigraphic record  
91 (Fig. 1K) has prevented the extension of astronomically paced glaciations as an explanation  
92 for Silurian climate events (Caputo et al., 1998; Díaz-Martínez and Grahn, 2007; Grahn and  
93 Caputo, 1992), despite indirect evidence of glaciation from dramatic facies changes in the  
94 Ludfordian which indicate a rapid worldwide shallowing (Frýda et al., 2021; Loydell and  
95 Frýda, 2011). Here, we provide Os and Li isotope records of sedimentary rocks – proxies for  
96 weathering processes and provenance – and a new dynamic carbon-osmium-lithium-model to  
97 test hypotheses for the cause(s) and nature of the Silurian events.

98

## 99 **1.1 Tracing weathering using Os and Li isotopes**

100 The Re-Os system undergoes parent-daughter fractionation during mantle melting leading to  
101 more radiogenic  $^{187}\text{Os}/^{188}\text{Os}$  values in the upper continental crust relative to recent mantle  
102 derived minerals (Peucker-Ehrenbrink and Ravizza, 2000). The  $^{187}\text{Os}/^{188}\text{Os}$  values of rivers  
103 are therefore seen to reflect the provenance of continental weathering, from the silicate  
104 weathering of unradiogenic juvenile basaltic minerals ( $^{187}\text{Os}/^{188}\text{Os} = \sim 0.12$ ) through to the  
105 oxidative weathering of highly radiogenic organic-sulphide-rich rocks ( $^{187}\text{Os}/^{188}\text{Os} = \sim 1.37$ )  
106 (Georg et al., 2013). Stable Li isotopes, on the other hand, show limited fractionation during  
107 magmatic processes, and the primary components of the upper continental crust therefore  
108 display a narrow range of compositions (continental crust =  $\sim 0.6 \pm 0.6$  ‰, basalt = 0 to 5 ‰)  
109 (Sauzéat et al., 2015). However, Li isotopes fractionate significantly during chemical  
110 weathering, with the retention of  $^6\text{Li}$  in weathering residues causing the  $\delta^7\text{Li}$  values of rivers  
111 (2 to 44 ‰) to reflect ‘weathering congruency’, defined as the ratio of primary rock  
112 dissolution (congruent weathering drives rivers to low  $\delta^7\text{Li}$ ), to secondary mineral (e.g.,  
113 clays) formation (incongruent weathering drives rivers to high  $\delta^7\text{Li}$ ) (Huh et al., 1998; Pogge  
114 von Strandmann et al., 2017).

115 The respective  $^{187}\text{Os}/^{188}\text{Os}$  and  $\delta^7\text{Li}$  of organic-rich shales and carbonates record the  
116 isotopic composition of seawater at the time of deposition (Peucker-Ehrenbrink and Ravizza,  
117 2000; Pogge von Strandmann et al., 2017). In the modern oceans, the  $^{187}\text{Os}/^{188}\text{Os}$  and  $\delta^7\text{Li}$  of  
118 seawater ( $^{187}\text{Os}/^{188}\text{Os} = \sim 1.06$ ,  $\delta^7\text{Li} = \sim 31$  ‰) reflect the balance between riverine inputs  
119 ( $^{187}\text{Os}/^{188}\text{Os} = \sim 1.54$ ,  $\delta^7\text{Li} = \sim 23$  ‰), hydrothermal inputs ( $^{187}\text{Os}/^{188}\text{Os} = \sim 0.12$ ,  $\delta^7\text{Li} = \sim 7$   
120 ‰), cosmogenic inputs ( $^{187}\text{Os}/^{188}\text{Os} = \sim 0.13$ ), and outputs related to the incorporation of Li  
121 into low-temperature marine clays, which impose a fractionation of  $\sim 15$  ‰, and the  
122 scavenging of Os by organic or particulate matter (Misra and Froelich, 2012; Peucker-  
123 Ehrenbrink and Ravizza, 2000). The residence time of Os ( $\sim 10$ -60 kyr) and Li ( $\sim 1.2$  Myr) in  
124 the ocean has allowed variations in these inputs and outputs, inferred from changes in the

125 sedimentary records of seawater  $^{187}\text{Os}/^{188}\text{Os}$  and  $\delta^7\text{Li}$ , to provide unparalleled information  
126 concerning the response of weathering to climatic and geological events (Misra and Froelich,  
127 2012; Peucker-Ehrenbrink and Ravizza, 2000).

128

## 129 **2. Materials and methods**

### 130 **2.1 Palaeogeographic setting and sampling strategy**

131 To explore the response of weathering to climatic change during Silurian bioevents we  
132 determined the respective  $^{187}\text{Os}/^{188}\text{Os}$  and  $\delta^7\text{Li}$  composition of three shale sections and three  
133 carbonate sections that span much of the Silurian and include significant positive  $\delta^{13}\text{C}$   
134 excursions and extinctions: early Sheinwoodian (Aizpute-41 core, Latvia; Lusklint &  
135 Lickershamn, Sweden); mid-Homerian (Bartoszyce core, Poland; Hunninge-1 core, Sweden);  
136 and mid-Ludfordian (Kosov, Czech Republic), and the  $^{187}\text{Os}/^{188}\text{Os}$  composition of a further  
137 shale section (Klonk core, Czech Republic) that spans the Přídolí-Lochkovian boundary (see  
138 *Supplementary Material*). Carbonate sections from Gotland (Sweden) and shale sections from  
139 Latvia and Poland were respectively deposited in the shallow- and deep-waters of an  
140 epicontinental sea to the north of the Rheic Ocean, whereas sections from the Czech Republic  
141 represent deeper shelf sediments from the north coast of Gondwana, to the south of the Rheic  
142 ocean (Fig. 1A).

143

### 144 **2.2 Sample preparation**

145 Prior to crushing, 20-80 g of shale samples were polished to eliminate contamination from  
146 cutting and drilling marks and samples with any signs of veining or weathering were avoided.  
147 The shale samples were then dried at 60 °C for ~12 h before being broken into chips with no  
148 metal contact. Bulk carbonates and shales were crushed to a fine powder (~30  $\mu\text{m}$ ) in a  
149 Zirconia ceramic dish using a shatterbox. Bulk carbonates were leached using a sequential

150 extraction method (Pogge von Strandmann et al., 2013), whereby ~0.1 g of carbonate was  
151 leached for 5 h at room temperature using Na acetate buffered to pH 5 by acetic acid. The  
152 sample preparation and Re-Os isotope and trace metal analysis were carried out at the  
153 Durham Geochemistry Centre (Laboratory for Sulfide and Source Rock Geochronology and  
154 Geochemistry) at Durham University. The Li isotope analysis was carried out at the stable  
155 isotope laboratory at the University of Oxford and later at the London Geochemistry and  
156 Isotope Centre at UCL.

157

### 158 **2.3 Osmium isotope analysis of shales**

159 Rhenium and Os abundances and isotopic compositions were determined using isotope  
160 dilution negative thermal ionisation mass spectrometry using Cr<sup>VI</sup>-H<sub>2</sub>SO<sub>4</sub> digestion and  
161 solvent extraction (CHCl<sub>3</sub>), micro-distillation and anion chromatography methods (Creaser et  
162 al., 1991; Cumming et al., 2013; Selby and Creaser, 2003). The Cr<sup>VI</sup>-H<sub>2</sub>SO<sub>4</sub> digestion  
163 employed here principally dissolves the organic fraction of a shale, thus liberating the  
164 hydrogenous Re-Os load of the sediment and therefore avoiding detrital contamination (Selby  
165 and Creaser, 2003). The isolated Re and Os fractions were loaded onto Ni and Pt filaments  
166 respectively, and their isotopic composition was determined using a ThermoScientific  
167 TRITON mass spectrometer using Faraday collectors and the secondary electron multiplier,  
168 respectively.

169 Total procedural blanks for Re and Os are  $10.09 \pm 0.99$  and  $0.11 \pm 0.06$  pg  
170 respectively, with an average  $^{187}\text{Os}/^{188}\text{Os}$  of  $0.77 \pm 0.54$  (1SD; n=5). Raw Re and Os oxide  
171 values were corrected for oxygen contribution and mass fractionation. Calculated  
172 uncertainties include those associated with mass spectrometer measurements, blank  
173 abundance and isotopic composition, spike calibration, and sample and spike weights. In-  
174 house standard solutions of Re and Os (DROsS) yield an average  $^{185}\text{Re}/^{187}\text{Re}$  value of

175  $0.59872 \pm 0.00135$  (1SD,  $n = 24$ ), and  $^{187}\text{Os}/^{188}\text{Os}$  of  $0.16101 \pm 0.000401$  (1SD,  $n = 41$ ),  
176 respectively, which is identical to previously published values (Nowell et al., 2008).

177 Initial  $^{187}\text{Os}/^{188}\text{Os}$  ( $^{187}\text{Os}/^{188}\text{Os}_i$ ) values in this study were determined from Re-Os data  
178 and the  $^{187}\text{Re}$  decay constant ( $1.666e^{-11} \text{ a}^{-1}$ ) (Smoliar et al., 1996) and interpolated graptolite  
179 biozone ages (Fig. S8). Analytical uncertainty for individual calculated  $\text{Os}_i$  is  $< 0.05$ . The  
180 reproducibility of calculated  $^{187}\text{Os}/^{188}\text{Os}_i$  was based on 15 analyses of the USGS rock  
181 reference material SBC-1 (Bush Creek Shale) which has a value of  $\sim 0.65 \pm 0.07$  (2SD; Table  
182 S4). Calculated  $^{187}\text{Os}/^{188}\text{Os}_i$  ratios assume closed system behaviour after deposition and  
183 therefore reflects the isotope composition of the local seawater at the time of sediment  
184 deposition.

185

#### 186 **2.4 Lithium isotope analysis of bulk carbonates**

187 A split of each sample solution was retained for cation analysis using an Elan Quadrupole  
188 inductively coupled plasma mass spectrometer. Samples were matrix matched to  $10 \mu\text{g/g}$  Ca  
189 and calibrated against a set of synthetic standards made up from single element solutions. The  
190 Al/Ca and Mn/Ca ratios were monitored to detect the influence of Li leached from clays.  
191 Previous work suggests that carbonates must be  $>0.8 \text{ mmol/mol}$  before carbonate Li isotope  
192 ratios become measurably perturbed by Li leached from clays (Pogge von Strandmann et al.,  
193 2013). Accuracy and precision were assessed by repeated analyses of seawater, JLs-1, and  
194 repeated dissolutions of the Plenus Marl from Eastbourne. Sample reproducibility of Li/Ca  
195 and Al/Ca was  $\sim 7\%$  (2 SD,  $n=6$ ). The larger part of each sample (typically containing 5-10  
196 ng Li) was purified by passing it through a two-stage cation-exchange procedure (Pogge von  
197 Strandmann et al., 2017; Pogge von Strandmann et al., 2019). Given that Li isotopes  
198 fractionate during cation chromatography, it is critical to have column yields close to 100%.



199 To assess the efficacy of this process, splits of the solution were collected before and after the  
200 collected bracket for Li, which were shown to have <0.1% of Li.

201 The total procedural blank for Li isotope analysis is ~0.02 ng Li, which is  
202 insignificant compared to the mass of sample used. Analyses were performed on a Nu Plasma  
203 HR multi-collector ICP-MS at Oxford, and a Nu Plasma 3 MC-ICP-MS at UCL, using a  
204 sample-standard bracketing system relative to the LSVEC standard (Flesch et al., 1973). Each  
205 sample was measured three separate times during the same analytical session. Each  
206 individual measurement consisted of 10 ratios (10 s total integration time), giving a total  
207 integration time of 300 s/sample. At an uptake rate of 75  $\mu\text{l}/\text{min}$ , the sensitivity for a 20 ng/ml  
208 solution is ~180 pA of  $^7\text{Li}$  at Oxford (Pogge von Strandmann et al., 2019). Background  
209 instrumental Li intensity, typically ~0.01 pA, was subtracted from each measurement.  
210 Accuracy and external reproducibility, as assessed from seawater, is  $31.1 \pm 0.6 \text{‰}$  (2 SD, n =  
211 16). Precision was also assessed from repeated analyses of an in-house marl standard, which  
212 also gives a reproducibility of  $\pm 0.6 \text{‰}$  (n = 7). At UCL, a 5 ng/ml solution gives around 120  
213 pA of  $^7\text{Li}$ .

214

## 215 **2.5 Dynamic C-Os-Li geochemical model**

216 We developed a simple coupled carbon-cycle-climate model to explore potential drivers of  
217 new ( $^{187}\text{Os}/^{188}\text{Os}$ ,  $\delta^7\text{Li}$ ) and existing ( $\delta^{13}\text{C}$ ,  $\delta^{18}\text{O}$ ) isotope data over relatively short-term  
218 events in the Silurian. The carbon cycle component of the model is based on the  
219 GEOCARBSULF (Berner, 2006) and COPSE (Lenton et al., 2018) biogeochemical models,  
220 and the simple model used by Pogge von Strandmann *et al.* (2017) to study the Hirnantian,  
221 adding osmium cycling (Lechler et al., 2015; Pogge von Strandmann et al., 2013) to the  
222 existing lithium cycle. In essence, the model interactively captures the long-term inorganic  
223 carbon cycle with degassing input of  $\text{CO}_2$ , and any imbalance in the organic carbon cycle

224 such as carbon burial, assumed to be balanced by CO<sub>2</sub> drawdown from silicate weathering.  
225 Silicate weathering depends on CO<sub>2</sub>, temperature, and vegetation, providing negative  
226 feedback on climate variations. Silicate weathering, along with hydrothermal activity, drives  
227 input fluxes of Li and Os to the ocean and is balanced by sedimentary removal. A threshold  
228 response model is also considered to generate large (~5 ‰) δ<sup>13</sup>C variations via the growth  
229 and decay of the marine organic carbon reservoir (Laurin et al., 2015), driven by numerical  
230 solutions for orbital precession and obliquity (Laskar et al., 2004). The climate component of  
231 the model – capturing changes in global temperature and ice sheet extent – is based on a  
232 logarithmic relationship between CO<sub>2</sub> and radiative forcing from the GCM-ice sheet  
233 modelling results of Pohl *et al.* (2016). The model is solved numerically using Euler's  
234 method run from initial values (Table S3) at a timestep of 5000 years. A detailed description  
235 of the model can be found in the *Supplementary Material*.

236 Key parameter settings for initialising the model are the rates of tectonic degassing  
237 and uplift, the areal coverage of land plants, and their effect on weathering. Normalised  
238 forcing factors for degassing (D), uplift (U), vegetation (V) and weathering (W) are derived  
239 from the COPSE and GEOCARBSULF biogeochemical model estimates for the Silurian (see  
240 Fig. 3 in Lenton et al. (2018)). Degassing was elevated relative to the present and we use an  
241 estimate for the start of the Silurian at ~443 Ma (D = 1.5). Uplift was comparable to today's  
242 conditions, and we use an average estimate for the Silurian (U = 0.94). The first non-vascular  
243 plants had colonised the land surface during the Late Ordovician, establishing an assumed  
244 modest fractional coverage (V = 0.15) but with a substantial effect on weathering (W = 0.75),  
245 consistent with previous work (Pogge von Strandmann et al., 2017). A key difference from  
246 GEOCARBSULF, which has been explored in COPSE (Lenton et al., 2018), is that we  
247 assume a larger plant amplification effect on weathering today ( $k_v^{-1}$ ) of a factor of 10 rather  
248 than a factor of 4. To test different hypotheses, the model is either perturbed after 0.5 Myr by

249 changing forcing factors D, U, V or W, or subjected to orbital forcing from numerical  
250 solutions for precession or obliquity.

251

### 252 **3. Results and discussion**

#### 253 **3.1 Os and Li isotope records for the Silurian**

254 New  $^{187}\text{Os}/^{188}\text{Os}$  and  $\delta^7\text{Li}$  profiles for these sections have been compiled with existing  $\delta^{13}\text{C}$   
255 and  $\delta^{18}\text{O}$  profiles and show similar trends for each time period studied, but with differing  
256 magnitudes of change (Fig. 1B-1H and S1-S7; Table S1-S2). Prior to a  $\delta^{13}\text{C}$  excursion there  
257 is a positive shift of magnitude 0.19 to 0.56 in the  $^{187}\text{Os}/^{188}\text{Os}$  composition, often associated  
258 with a positive shift in  $\delta^{18}\text{O}$  of magnitude 0.55 to 1.74 ‰. This is followed by a decline in the  
259  $^{187}\text{Os}/^{188}\text{Os}$  composition to pre-excursion values. During the  $\delta^{13}\text{C}$  excursions, of magnitude  
260 0.9 to 8.29 ‰, the  $^{187}\text{Os}/^{188}\text{Os}$  composition generally remains low. In contrast, the  $\delta^7\text{Li}$  of  
261 carbonates displays a positive shift of magnitude 4.7 to 9.6 ‰. During a plateau in  $\delta^{13}\text{C}$   
262 values, the  $\delta^{18}\text{O}$  and  $\delta^7\text{Li}$  values begin to return to pre-excursion values in some sections.  
263 During this decline, the  $^{187}\text{Os}/^{188}\text{Os}$  values observe a second positive shift of magnitude 0.26  
264 to 0.8 before returning to pre-excursion values either synchronously with the descending limb  
265 of the  $\delta^{13}\text{C}$  record or prior to it.

266 Processes that could cause these variations include contamination during sample  
267 processing, diagenesis, or a primary seawater signal driven by changes in Earth system  
268 processes. Contamination of Re and Os from the detrital fraction of shales was avoided by  
269 using the  $\text{CrO}_3\text{-H}_2\text{SO}_4$  digestion method, while cation exchange or leaching of clays, which  
270 could impart an isotopically light  $\delta^7\text{Li}$  signal, was monitored by analysing cation/Ca ratios of  
271 carbonates. Diagenesis can be discounted because the shale sections studied here show no  
272 signs of veining or metamorphism suggesting that the extracted organic-phase-Os remains  
273 unaltered (Selby and Creaser, 2003) and cation/Ca ratios display no discernible trend with

274  $\delta^7\text{Li}$  (Table S2). Furthermore,  $\delta^{13}\text{C}$  and  $\delta^{18}\text{O}$  values in studied profiles (Fig. S1-S7) show  
275 similar values to other correlated sections that span the same intervals (Fig. 1J and 1L). It is  
276 therefore suggested that the isotopic shifts in the shale and carbonate sections represent  
277 primary seawater signatures.

278         When compiled onto our new age-depth model (Fig. S8), variations in  $^{187}\text{Os}/^{188}\text{Os}$  and  
279  $\delta^7\text{Li}$  from this study (Fig. 2B-E) compare well, in terms of magnitude and timing of change,  
280 to records for the Hirnantian (Fig. 2A) suggesting similar causal processes. In general, we  
281 observe two peaks of radiogenic  $^{187}\text{Os}/^{188}\text{Os}$  (centred around the vertical grey dashed line)  
282 separated by  $\sim 270\text{-}700$  kyr (mean = 550 kyr;  $\sigma = 180$ ) and an ascending limb of  $\delta^7\text{Li}$  toward  
283 peak values (vertical black dashed line), which occurs  $\sim 210\text{-}630$  kyr (mean = 450 kyr;  $\sigma =$   
284 180) after the first peak in radiogenic  $^{187}\text{Os}/^{188}\text{Os}$  (Fig. 2). These broadly consistent patterns  
285 of change provide a target for numerical modelling. We use the model to test a series of  
286 hypotheses, attempting to reproduce: (1) the double-peaked  $^{187}\text{Os}/^{188}\text{Os}$  response of  
287 magnitude 0.2 to 0.8; (2) a single transient peak of  $\delta^7\text{Li}$  ( $>5$  ‰); (3)  $\delta^{13}\text{C}_{\text{carb}}$  variation of  $\sim 2\text{-}8$   
288 ‰ over  $\sim 1$  to 2.5 Myr (Fig. 1J); (4)  $\delta^{18}\text{O}_{\text{phos}}$  variation of  $\sim 1\text{-}2$  ‰ over  $\sim 1$  to 2 Myr (Fig. 1L);  
289 and, (5) sea-level drops of  $\sim 50\text{-}200$  m over  $\sim 1$  Myr (Fig. 1M).

290

### 291 **3.2 Initial state of the C-Os-Li geochemical model**

292 The relatively low plant cover of the Silurian, and corresponding suppression of the large  
293 assumed effect of plants on weathering, produces a high steady state  $\text{CO}_2$  at  $\sim 16$  PAL (and a  
294 global temperature relative to the present day,  $\Delta T$ , of  $\sim 9\text{K}$ ), which is consistent with the lack  
295 of a large, permanent ice sheet from the climate-ice sheet simulations of Pohl *et al.* (2016) for  
296 the Late Ordovician. A modest ice sheet extent of  $\sim 2$  Mkm<sup>2</sup> is predicted and fixed at this  
297 value in the model variant without interactive ice sheets. The initial model state is poised to  
298 grow an ice sheet if that option is included and  $\text{CO}_2$  declines, which is reasonable given that

299 the Hirnantian experienced a pronounced ice age. Initialising the model with higher D, lower  
300 U, V, or W, would all tend to increase the initial CO<sub>2</sub> making it harder to trigger glaciation.

301 In the initial state the ocean Li reservoir is  $\sim 4 \times 10^{16}$  mol,  $\delta^7\text{Li}_{\text{sw}} = 17.5$  ‰, and  
302  $\delta^7\text{Li}_{\text{carb}} = 13.5$  ‰, higher than the data, but close to the minimum allowable from isotopic  
303 mass balance (Fig. 1F to H). The Os reservoir is  $\sim 1 \times 10^8$  mol with a  $^{187}\text{Os}/^{188}\text{Os}$  of 0.64, in  
304 the range of the data (Fig. 1B to E). An initial  $\delta^{13}\text{C}$  of 1 ‰ is a reasonable baseline value for  
305 the Silurian (Fig. 1J). We begin by testing the hypotheses previously proposed as drivers of  
306 Hirnantian climate change, notably a decline in volcanic arc degassing and the colonisation  
307 of land plants, before considering orbital forcing of imbalances in organic carbon burial and  
308 the possibility of widespread Southern Hemisphere glaciations.

309

### 310 **3.3 Can tectonic or biological forcing explain observed Os and Li isotope records?**

311 Variations in the  $\delta^7\text{Li}$  of seawater during the Hirnantian (Fig. 2A) have been linked to a  
312 decrease in silicate weathering caused by a decline in global temperatures, ultimately linked  
313 to a decline in CO<sub>2</sub> degassing. Continental arc volcanism continued to decline into the  
314 Silurian (McKenzie et al., 2016) as the Iapetus Ocean closed during the formation of  
315 Laurussia suggesting a possible link between degassing and our Os and Li isotope records.  
316 An extreme halving of degassing over 1 Myr (Fig. 3A), which is unprecedented for the  
317 Phanerozoic, causes a halving of atmospheric CO<sub>2</sub> and a global cooling of  $\sim 4$  °C (Fig. 3B),  
318 driving an increase in  $\delta^{18}\text{O}_{\text{phos}}$  of 0.8 ‰ (Fig. 3C). A halving of the riverine and hydrothermal  
319 fluxes coupled to a reduction in the oceanic Li reservoir drives a  $\sim 3$  ‰ positive  $\delta^7\text{Li}$   
320 excursion over  $\sim 3$  Myr (Fig. 3C). Ocean Os content drops more rapidly, and because the  
321 unradiogenic hydrothermal and basalt weathering input halves, whilst relatively radiogenic  
322 sediment weathering remains constant, the  $^{187}\text{Os}/^{188}\text{Os}$  of seawater increases by  $\sim 0.19$  (Fig.  
323 3C). Although O, Li and Os variation is in the same direction as Silurian records, the

324 variation is too small and not transient (Fig. 2 and 1L), displaying a permanent shift to higher  
325 values (Fig. 3C). This suggests that even an abrupt and rapid decline in degassing cannot (on  
326 its own) explain the Li and Os isotope variations during the Silurian (or Hirnantian) events  
327 and transient changes in degassing are assumed not to be applicable for the timescales under  
328 consideration.

329         The evolution of non-vascular land plants had a potentially profound effect on silicate  
330 weathering fluxes during the Late Ordovician (Lenton et al., 2012). In the Silurian, their  
331 spread was augmented by the evolution of the first vascular land plants (Lenton et al., 2016).  
332 Conceivably, expansions in plant cover and associated increases in global weathering rates  
333 occurred during the Silurian (Lenton et al., 2016), albeit of uncertain magnitude. Modelling  
334 an extreme doubling of vegetation cover over 1 Myr (Fig. 3D) causes CO<sub>2</sub> to decline by ~2.5  
335 PAL, a < 2°C cooling (Fig. 3E) and a stepwise increase in δ<sup>18</sup>O (Fig. 3F). The increase in  
336 silicate weathering, by ~10 % until CO<sub>2</sub> and temperature have adjusted, brought on by land  
337 plant proliferation drives a transient negative ~0.6 ‰ excursion in δ<sup>7</sup>Li (Fig. 3F) because the  
338 unfractionated riverine source increases. The weathering of more radiogenic granitic and  
339 sedimentary rocks drives a similar transient decrease in the <sup>187</sup>Os/<sup>188</sup>Os of ~0.02 (Fig. 3F).  
340 Neither isotopic response is in the direction observed in Silurian records (Fig. 2).

341         If we include an intensification of pedogenesis and clay formation via incongruent  
342 weathering, the riverine δ<sup>7</sup>Li, and therefore oceanic δ<sup>7</sup>Li, can increase, but this shift is no  
343 longer transient and the <sup>187</sup>Os/<sup>188</sup>Os of seawater is unaffected. Increasing and then decreasing  
344 V, to represent phases of plant colonisation and associated weathering spikes (Lenton et al.,  
345 2016), can cause a small decrease then a small increase in <sup>187</sup>Os/<sup>188</sup>Os. However, even these  
346 large and rapid changes in plant cover cannot (alone) explain the Li and Os isotope variations  
347 during Late Ordovician and Silurian events (Fig. 2). Varying D (Fig. S9) or V (Fig. S10)  
348 alters the magnitude or duration of change, but it does not affect the overall modelled trends,

349 which do not compare favourably to observed records. It seems more likely that a modest,  
350 slower expansion of vegetation and/or decline in degassing could have helped ‘prime’ the  
351 Earth system to undergo the observed events.

352         Enhanced weatherability of silicate rocks during the Taconic (Finlay et al., 2010) and  
353 Scandian (Munnecke et al., 2010) orogenies or the passage of volcanic rocks through the  
354 tropics during the Late Ordovician and/or Silurian (Nardin et al., 2011) could have led to  
355 significant variation in the Li and Os isotope systems. To generate the Li isotope variation  
356 seen during the Hirnantian, previous isotope modelling would require a seemingly  
357 implausible increase in uplift of ~65 % above modern levels or going from zero to roughly  
358 double the present day area of basalt (Pogge von Strandmann et al., 2017). Moreover,  
359 seawater  $^{187}\text{Os}/^{188}\text{Os}$  and  $\delta^7\text{Li}$  has been shown to be driven lower during basaltic eruptions  
360 associated with oceanic anoxic events (Lechler et al., 2015; Pogge von Strandmann et al.,  
361 2013). Therefore, plausible changes in tectonic and biological forcing, including reductions  
362 in volcanic arc degassing, expansions of terrestrial plants, orogeny or enhanced basaltic  
363 weathering fail to reconcile Os and Li isotope records or generate the required magnitude of  
364 change observed, suggesting that other causal mechanisms are required to explain isotopic  
365 variations during the Silurian.

366

### 367 **3.4 Can orbital forcing of the organic carbon cycle explain Silurian isotope variations?**

368 Black shale deposition in palaeotropical restricted and semi-restricted settings during the late  
369 Katian and early Rhuddanian is associated with widespread anoxia and high rates of organic  
370 carbon burial comparable to Mesozoic oceanic anoxic events (Melchin et al., 2013; Stockey  
371 et al., 2020), possibly linked to increased primary productivity from nutrients supplied by  
372 upwelling or the weathering of newly exposed glaciogenic sediments (Pohl et al., 2017). A  
373 similar pattern of black shale deposition or anoxic seafloor conditions continued until the

374 Ludlow (Page et al., 2007). Organic carbon burial on continental margins can influence  
375 planetary climate and largely controls exogenic  $\delta^{13}\text{C}$  values, displaying a strong correlation to  
376 astronomical forcing (Kocken et al., 2019). Weaker forcing is associated with reduced  
377 seasonality which drives higher annual precipitation and sediment accumulation, leading to  
378 the burial of more isotopically light ( $^{12}\text{C}$ ) organic carbon, and therefore higher seawater  $\delta^{13}\text{C}$   
379 values, and  $\text{CO}_2$  sequestration, becoming reversed under stronger forcing (Kocken et al.,  
380 2019). Additionally, lower seasonality is associated with oceanic cooling (high  $\delta^{18}\text{O}$  values)  
381 leading to the greater storage of organic carbon as biogenic methane ( $\delta^{13}\text{C} = < -70$ ) in  
382 submarine methane hydrates (Kocken et al., 2019). The cyclical nature of Late Ordovician to  
383 Early Devonian  $\delta^{13}\text{C}$  (Fig. 1J) and  $\delta^{18}\text{O}$  (Fig. 1L) records has been linked to the long-term  
384  $\sim 4.5$  Myr amplitude modulation of the Earth's  $\sim 400$  kyr eccentricity and  $\sim 1.2$  Myr obliquity  
385 cycles, whereby prolonged intervals of exceptionally low forcing drove positive  $\delta^{13}\text{C}$  and  
386  $\delta^{18}\text{O}$  values via enhanced organic carbon burial, storage of biogenic methane and/or global  
387 cooling (Sproson, 2020).

388         In order to obtain the observed  $> 1$  ‰ variations in  $\delta^{13}\text{C}$  on Myr-timescales, carbon  
389 burial fluxes need to be tied to the development and decay of new carbon sinks, rather than  
390 changes in carbon production and burial in existing carbon reservoirs (Laurin et al., 2015).  
391 Here, we explore the potential of astronomically forced variations in marine organic carbon  
392 reservoir stability as a driver of observed isotope variations. Following Laurin *et al.* (2015),  
393 we assume that organic carbon moves via a series of quasi-stable reservoirs tied to the  
394 efficiency of carbon burial relative to the intensity of carbon production. Below an obliquity  
395 or precession threshold (th1), i.e., a period of low-amplitude insolation variation, the quasi-  
396 stable reservoir of bulk organic carbon grows, sequestering atmospheric  $\text{CO}_2$  and isotopically  
397 light carbon. Between th1 and another threshold (th2), this reservoir remains stable. Above  
398 th2, i.e., a period of high-amplitude insolation variation, the stored carbon is returned to the



399 exogenic reservoir as the bulk organic carbon reservoir decays, becoming a source of  
400 atmospheric CO<sub>2</sub> and isotopically light carbon (see *Supplementary Material*). Numerical  
401 astronomical models do not extend beyond 250 Ma and we therefore use sections of the  
402 La2004 numerical model (Laskar et al., 2004) over the last 30 Ma (Fig. 4) as a representative  
403 case for forcing Silurian palaeoclimate.

404 First, we consider obliquity forcing, using an illustrative exceptionally low obliquity  
405 variation between 9.4 and 11.6 Ma (inset in Fig. 4C; Fig. 5A) to drive variations in the  
406 stability of the marine sedimentary organic carbon reservoir (Fig. 5B). We assume that this  
407 forcing can generate a ~5 ‰ variation in δ<sup>13</sup>C (Fig. 5D), consistent with the larger Silurian  
408 events recorded in the geological record (Fig. 1J), corresponding to the transient  
409 accumulation of 8.5 x 10<sup>4</sup> Gt of carbon over 1.5 Myr (Fig. 5B). Such accumulation rates are  
410 an order of magnitude higher than those used previously to simulate δ<sup>13</sup>C variability during  
411 the Cretaceous (Laurin et al., 2015). We justify this accordingly: (1) the Silurian experienced  
412 a colder climate and a greater anoxic fraction of the ocean when compared to the Cretaceous  
413 (Lenton et al., 2018) leading to higher levels of organic matter preservation; (2) the numerical  
414 model of Laurin et al. (2015) did not account for any feedback mechanisms within the  
415 carbon-cycle that would otherwise reduce the impacts of reservoir stability on planetary  
416 climate; (3) we are attempting to simulate ~5 ‰ δ<sup>13</sup>C variations as opposed to ~1 ‰  
417 variations recorded in the Cretaceous; (4) we did not incorporate carbon storage in submarine  
418 methane hydrates in our model, which would otherwise reduce accumulation rates.

419 Two maxima of organic carbon accumulation (Fig. 5B) are separated by the ~1.2 Myr  
420 obliquity cycle (Fig. 5A), causing atmospheric CO<sub>2</sub> to decline from ~16 to ~10 PAL (Fig.  
421 5C), like previous estimates for the Ordovician and Silurian (Lenton et al., 2018), before  
422 obliquity forcing starts to generate net carbon release from the organic carbon reservoir (Fig.  
423 5B). This corresponds to a cooling of ~2°C (Fig. 5C) and increase of ~0.5 ‰ in δ<sup>18</sup>O<sub>phos</sub> (Fig.

424 5D), smaller than variations in the conodont apatite record (Fig. 1L). The drop in atmospheric  
425 CO<sub>2</sub> and temperature leads to a reduction in silicate weathering, driving a decline in the  
426 ocean Os and Li reservoirs. The reduced weathering of unradiogenic silicates, such as basalt,  
427 by ~50 % relative to more radiogenic Os-rich lithologies such as sediments, leads to a ~0.1  
428 increase in the <sup>187</sup>Os/<sup>188</sup>Os of seawater (Fig. 5E), with peak values during minimum  
429 atmospheric *p*CO<sub>2</sub> (Fig. 5C). Meanwhile a reduction in the riverine Li flux drives a gradual  
430 increase of ~1.5 ‰ in the δ<sup>7</sup>Li of seawater (Fig. 5E). The long ocean residence time of Li  
431 (~1.3 Myr in the model) relative to Os (~30 kyr in the model) leads to a more muted Li  
432 isotope response to climatic change when compared to Os isotopes. Although we capture the  
433 multiple peaks in Os isotopes relative to single peak in δ<sup>7</sup>Li records, the magnitude of change  
434 is smaller and more protracted, the peaks are separated by ~1.2 Myr in the model whereas  
435 Silurian records are separated by ~0.2-0.7 Myr (Fig. 2).

436       Next, we consider precession forcing, using an illustrative period of exceptionally low  
437 precession variation between 9.6 to 10.6 Ma (inset in Fig. 4A; Fig. 5F) to drive variations in  
438 the stability of the marine organic carbon reservoir (Fig. 5G). This forcing can generate a  
439 similar magnitude of change to obliquity forcing (Fig. 5G-5J), but unlike obliquity forcing,  
440 the two maxima of organic carbon accumulation are separated by the ~400 kyr eccentricity  
441 cycle (Fig. 5F), leading to a transient accumulation of ~5 x 10<sup>4</sup> Gt of carbon over ~0.7 Myr  
442 (Fig. 5G). This places peaks in Os and Li isotopes (Fig. 5J) within the ~0.2 to 0.7 Myr range  
443 recorded in the data (Fig. 2). However, the large uncertainty associated with the age-depth  
444 model used here (Fig. 2) precludes us from discounting the influence of obliquity. Although  
445 the precession forced model improves on the obliquity model by giving a timing more  
446 consistent with the Os and Li isotope variation, the magnitude of change remains insufficient  
447 (Fig. 2). Hence, we consider an additional factor – the hypothesis that astronomical forcing of

448 the organic carbon cycle triggered intermittent glaciations during the Hirnantian and Silurian  
449 (Sproson, 2020).

450

### 451 **3.5 Orbitally paced Silurian glaciations**

452 A decline in atmospheric CO<sub>2</sub> during the Late Ordovician led to extensive Southern  
453 Hemisphere glaciation over Gondwana, associated with a glacio-eustatic sea-level change of  
454 ~70-100 m, during the Hirnantian (Algeo et al., 2016). According to an Earth system model  
455 for the Late Ordovician, there is a nonlinear response of southern hemisphere continental ice  
456 sheet build-up to a decrease in radiative forcing (Pohl et al., 2016). At a *p*CO<sub>2</sub> of 16 PAL,  
457 small ice caps begin to nucleate at the pole and high latitudes ( $\geq 60^\circ\text{S}$ ), but by 12 PAL ice  
458 sheet feedback processes cause these sporadic glaciers to coalesce rapidly into a single  
459 continental-scale ice sheet that extends to mid latitudes ( $45^\circ\text{S}$ ) where it remains relatively  
460 stable. This transition corresponds to a global cooling of  $\sim 4^\circ\text{C}$  and high climate sensitivity of  
461  $>9^\circ\text{C}$  for a doubling/halving of atmospheric CO<sub>2</sub>.

462 Running the previous obliquity (Fig. 6A) and precession forcing (Fig. 6G) of the  
463 marine sedimentary organic carbon reservoir with an ice sheet and climate sensitivity derived  
464 from Pohl *et al.* (2016) again leads to a transient accumulation of  $\sim 5\text{-}9 \times 10^4$  Gt of carbon  
465 (Fig. 6B and 6H), generating a  $\delta^{13}\text{C}$  variation of  $\sim 4.5\text{-}5$  ‰ (Fig. 6E and 6K). With the  
466 increased climate sensitivity, this drives a rapid cooling of  $\sim 4\text{-}5$  °C (Fig. 6C and 6I) and an  
467 increase in the Gondwanan ice sheet area of  $\sim 36$  Mkm<sup>2</sup>, expanding from  $\sim 90^\circ\text{S}$  to  $\sim 45^\circ\text{S}$ ,  
468 equating to a glacioeustatic drop of  $\sim 65$  m (Fig. 6D and 6J). Subsequent net carbon loss can  
469 generate a recovery of CO<sub>2</sub> to  $\sim 15$  PAL, warming of  $\sim 4$  °C, and shrinkage of ice sheets to  $\sim 5\text{-}$   
470  $10$  Mkm<sup>3</sup>. Then, a further phase of net carbon accumulation causes CO<sub>2</sub> to decline to  $\sim 11$   
471 PAL, corresponding cooling of  $\sim 4$  °C (Fig. 6C and 6I), and ice sheets again expanding to 36

472 Mkm<sup>3</sup> (Fig. 6D and 6J). Then, as eccentricity or obliquity variation increases again, net  
473 carbon loss causes CO<sub>2</sub> to rise to ~18 PAL, eliminating ice sheets.

474 Projected cooling is comparable to estimated temperature anomalies of >5°C for the  
475 Ludlow and Přídolí (Trotter et al., 2016) whilst modelled sea-level change is comparable to  
476 reconstructed sea-level variations of 50-80 m during Silurian climate events (Fig. 1M).  
477 Cooling coupled to an increase in ice volume, which directly influences the δ<sup>18</sup>O of seawater,  
478 leads to a δ<sup>18</sup>O<sub>phos</sub> increase of ~2 ‰ (Fig. 6E and 6K), similar to δ<sup>18</sup>O perturbations recorded  
479 in the Silurian conodont apatite record (Fig. 1L). Following a series of sensitivity tests, a  
480 doubling of the average thickness of the ice sheet from 1 km to 2 km (Fig. 7A) increases the  
481 magnitude of δ<sup>18</sup>O<sub>phos</sub> variability from ~2 ‰ to ~2.5 ‰ (Fig. 7C). Tripling the thickness of  
482 the ice sheet to 3 km (Fig. 7D), consistent with Pohl et al.'s (2016) simulations, increases the  
483 magnitude of δ<sup>18</sup>O<sub>phos</sub> variability to ~3.5 ‰ (Fig. 7F), consistent with conodont apatite  
484 records for the Hirnantian (Trotter et al., 2008) and Mid-Ludfordian (Frýda et al., 2021), but  
485 generally higher than other Silurian records (Trotter et al., 2016). An increase in ice thickness  
486 to 2 and 3 km drives a larger sea-level drop of 120 m and 190 m, respectively (Fig. 7B and  
487 7E). The former is comparable to sea-level estimates for the Hirnantian whilst the latter is far  
488 higher than anything interpreted for the Ordovician and Silurian (Haq and Schutter, 2008).  
489 This suggests that although the Hirnantian glaciation likely had an ice sheet thickness of up to  
490 ~3 km, Silurian ice sheets were much smaller, reaching an average ice sheet thickness closer  
491 to ~1 km, explaining the lack of marine terminating glaciers and the therefore glacial tillites  
492 in the post-Sheinwoodian geological record (Fig. 1K) and low amplitude sea level variation  
493 (Calner, 2008).

494 A reduced riverine flux of Os and Li, coupled to a shift to more incongruent  
495 weathering due to increased clay formation caused by a longer continental residence time of  
496 water, proposed for the Hirnantian glaciation (Pogge von Strandmann et al., 2017), causes an

497 increase in the  $^{187}\text{Os}/^{188}\text{Os}$  of seawater and the  $\delta^7\text{Li}$  of carbonate by  $\sim 0.13$ - $0.2$  and  $\sim 2.5$ - $4.5$   
498 ‰, respectively (Fig. 6F and 6L), still substantially lower than recorded values (Fig. 2).  
499 Although it is not possible to estimate the exact parameters governing the isotope systems  
500 during the Palaeozoic, we speculate as to the possible causes of discrepancies between  
501 modelled and observed data based on known processes. Physical erosion of Os-rich  
502 sediments, such as shales and pyrite, in response to the expansion of large scale rock-grinding  
503 glaciers has been shown to influence the Late Pleistocene Os record through the injection of  
504 radiogenic Os to the ocean (Georg et al., 2013). Doubling sediment weathering (Fig. 7H)  
505 with maximum ice sheet extent (Fig. 7G), to mimic the erosion of Os-rich lithologies,  
506 increases the magnitude of the  $^{187}\text{Os}/^{188}\text{Os}$  response to  $\sim 0.4$  (Fig. 7I) on a similar order to  
507 Silurian records (Fig. 2). The residence time of Li in the ocean is estimated to be  $\sim 1$  to  $1.5$   
508 Myr for the present day (Huh et al., 1998), but if we assume that the oceanic Li residence  
509 time was half that of the present, due to a higher Li removal rate on continental margins with  
510 a higher sediment accumulation rate than present (Fig. 7K), the  $\delta^7\text{Li}$  of seawater increases by  
511  $\sim 4$ - $5$  ‰ (Fig. 7L). Additionally, if we assume that the  $\delta^7\text{Li}$  of riverine inputs underwent a  
512 larger fractionation of  $20$  ‰, due to even higher clay formation associated with the expansion  
513 of ice sheets (Fig. 7M-N), the magnitude of the seawater  $\delta^7\text{Li}$  response increases to  $\sim 7$ - $10$  ‰  
514 (Fig. 7O).

515 Finally, numerical models used here generate multiple peaks in  $\delta^{13}\text{C}$  tied to  
516 eccentricity or obliquity minima (Fig. 6E, K) which are not clearly observed in  $\delta^{13}\text{C}$  records  
517 (Fig. 1J). This discrepancy could be an artefact of undersampling incomplete geological  
518 sections, indicating the need for more complete Silurian  $\delta^{13}\text{C}$  records. For example,  
519 exceptionally complete sedimentary records for the Hirnantian reveal several  $\delta^{13}\text{C}$  cycles  
520 associated with glacial apices, similar to our model, that would otherwise be missing due to  
521 hiatuses during sea level lowstands (Ghienne et al., 2014). Alternatively, simply forcing

522 organic carbon burial alone may be too simplistic to recreate the full complexity of records,  
523 and an interactive organic carbon cycle and/or additional forcing mechanisms, such as  
524 volcanic arc degassing or land-plant development, may be needed to reconcile numerical  
525 models with the geological record.

526

#### 527 **4. Conclusion**

528 The  $^{187}\text{Os}/^{188}\text{Os}$ ,  $\delta^7\text{Li}$ ,  $\delta^{13}\text{C}$ ,  $\delta^{18}\text{O}$ , and sea level response from our dynamic carbon-osmium-  
529 lithium-model can recreate the variability within Os and Li isotope records from this study  
530 and the magnitude of  $\delta^{13}\text{C}$ ,  $\delta^{18}\text{O}$  and sea-level records from the literature, combining all lines  
531 of evidence under one causal mechanism for the first time. We propose that the long-term  
532  $\sim 4.5$  Myr amplitude modulation of the Earth's orbital eccentricity and/or obliquity led to  
533 prolonged periods of high organic carbon burial, atmospheric  $\text{CO}_2$  drawdown, cooling and  
534 continental glaciation during the Hirnantian, the early Sheinwoodian, the Homeric, the mid  
535 Ludfordian and the late Přídolí-early Lochkovian, extending the notion of 'Cenozoic-style'  
536 glacial cycles and high-order phenomena during the Late Ordovician (Ghienne et al., 2014) to  
537 the Silurian. Dramatic cooling or eustatic regression associated with glaciations and/or  
538 preceding marine anoxic/euxinic conditions would have removed the habitat space of marine  
539 taxa leading to extinctions including the Late Ordovician, 'Ireviken', 'Mulde', 'Lau' and  
540 'Silurian-Devonian Boundary' events.

541         Due to the large uncertainty associated with the age model used in this study, and  
542 potential temporal aliasing arising from the under-sampling of incomplete geological  
543 sections, we are unable to determine whether eccentricity or obliquity was the dominant pace  
544 setter for Silurian glaciations. Future work should look to develop high resolution records  
545 with improved age control, akin to Ghienne et al. (2014), for the Silurian. Finally, the  
546 dynamic model developed in this study is too simplistic (see section 4.8 in the *Supplementary*

547 *Material*) to recreate the nuances of observed Hirnantian and Silurian records. More complex  
548 modelling that includes a full description of the Earth's C-O-N-P-S cycles (e.g., Lenton et al.,  
549 2018) and ice-sheet feedbacks (e.g., Pohl et al., 2016) is needed to fully reconcile the forcing  
550 parameters explored here with Silurian records.

551

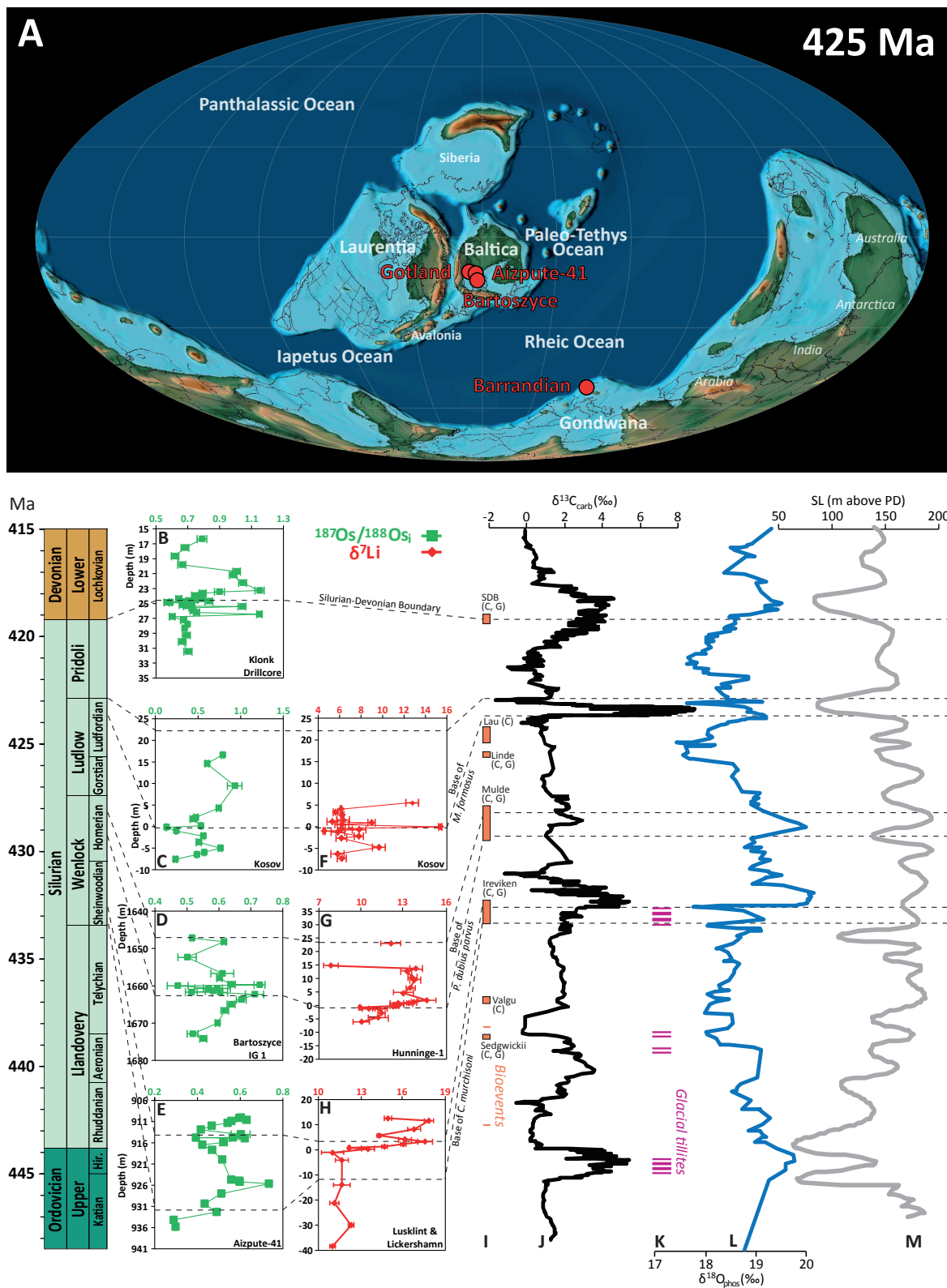
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564

## 565 **Appendix A. Supplementary material**

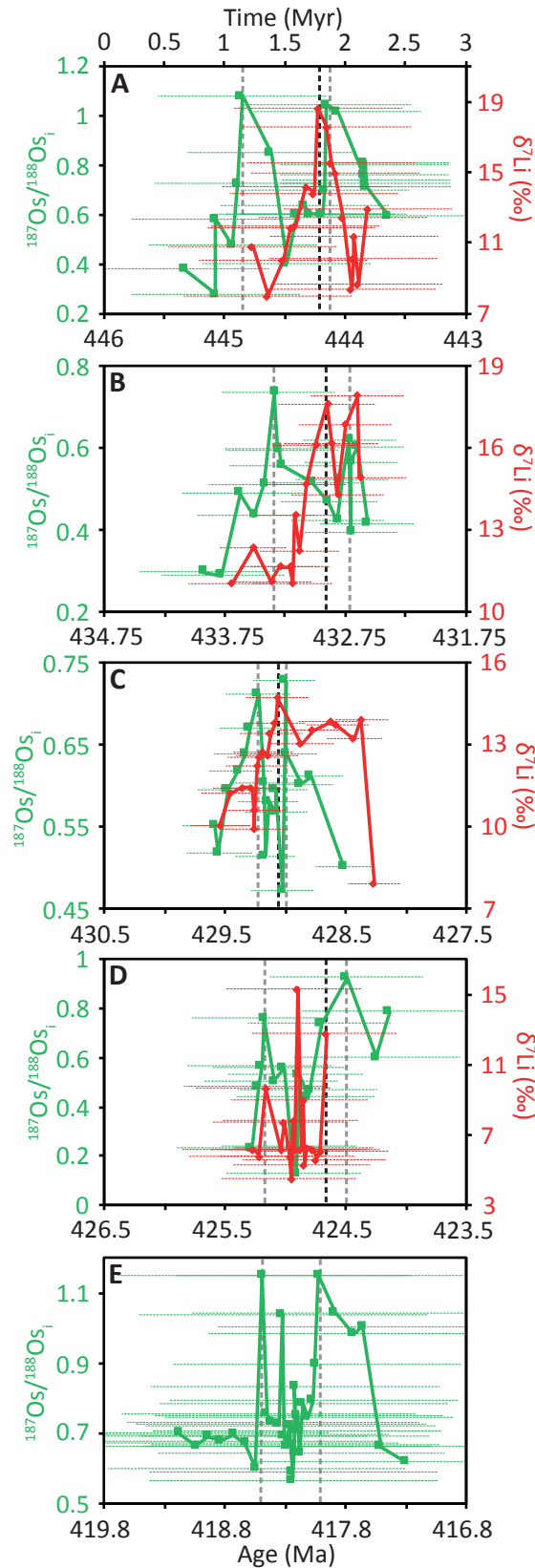
566 The supplementary material contains a description of the geological setting, supplementary  
567 results, age-depth model, and the dynamic C-Os-Li geochemical model along with Table S1-  
568 S3 and Fig. S1-S10. An excel version of the supplementary tables, including Re-Os data for  
569 the USGS rock reference material SBC-1 (Table S4), and dynamic C-Os-Li geochemical  
570 models used in this study are also provided.



572 **Fig. 1.** Palaeoclimate records for the Upper Ordovician to the Lower Devonian. (A)  
 573 Palaeogeographic reconstruction of the Wenlock (425 Ma) with sample locations highlighted  
 574 by red circles (Scotese, 2016). Osmium (green squares) and  $\delta^7\text{Li}$  (red diamonds) isotope data



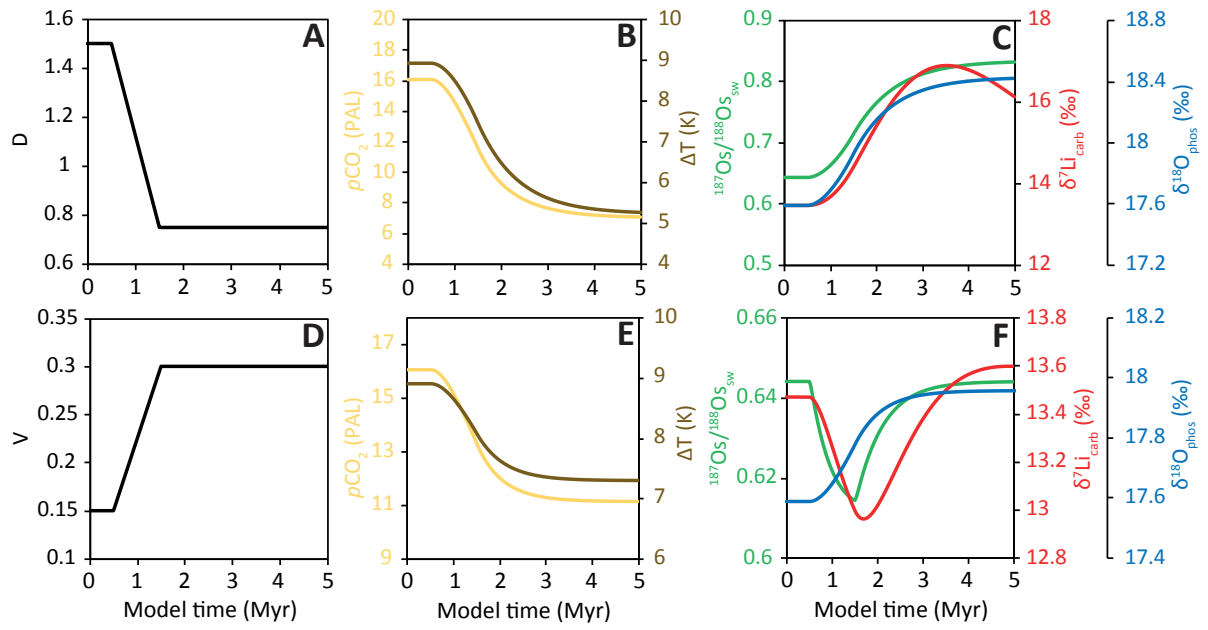
575 are shown for the Klonk (**B**), Kosov (**C** and **F**), Bartoszyce IG-1 (**D**), Aizpute-41 (**E**),  
576 Hunninge-1 (**G**), Lusklint (**H**) and Lickershamn (**H**) sections (see Fig. S1-S7 for more  
577 details). Regional data sets from this study are compared to global conodont (**C**) and  
578 graptolite (**G**) bioevents (**I**), carbonate  $\delta^{13}\text{C}$  (**J**), glacial tillites (**K**) conodont apatite  $\delta^{18}\text{O}$  (**L**)  
579 and eustatic SL (**M**) records (Caputo et al., 1998; Díaz-Martínez and Grahn, 2007; Grahn and  
580 Caputo, 1992; Haq and Schutter, 2008; Sproson, 2020; Trotter et al., 2008; Trotter et al.,  
581 2016).  
582



583 **Fig. 2.** Osmium and lithium isotope data for the Hirnantian (Finlay et al., 2010; Pogge von  
 584 Strandmann et al., 2017) (A), Telychian-Sheinwoodian boundary (B), mid-Homerian (C),  
 585 mid-Ludfordian (D) and Přídolí-Lochkovian boundary (E) compiled onto our new age-depth

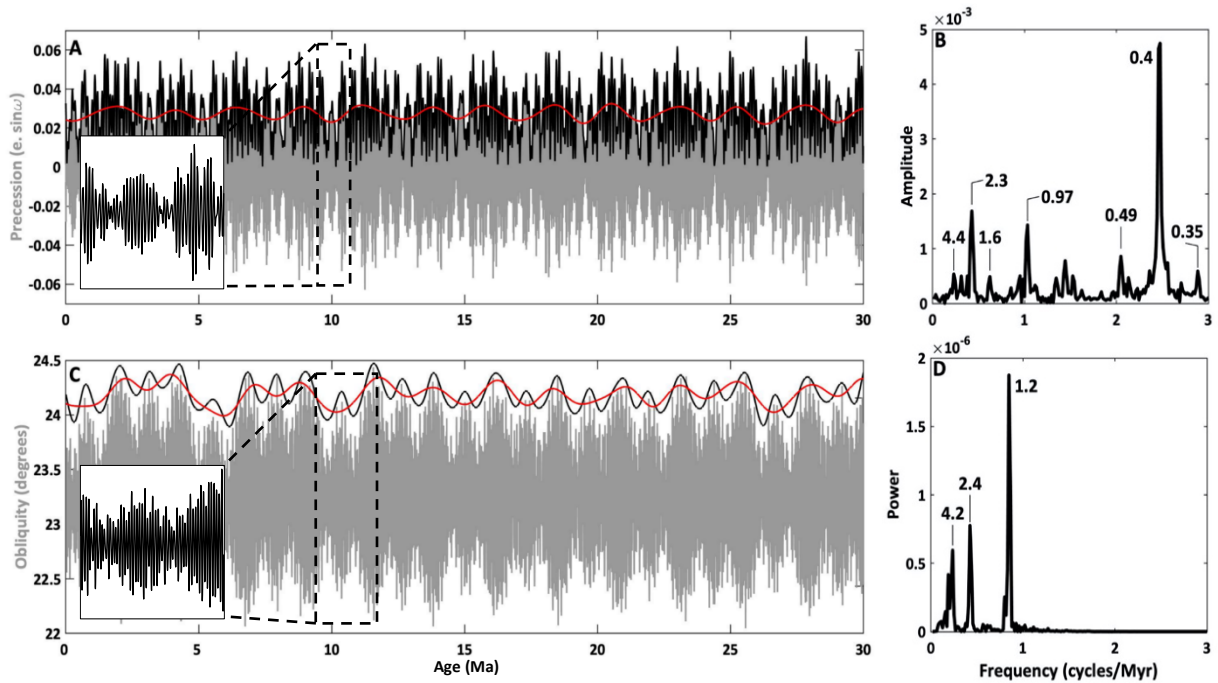
586 model (Fig. S8). The vertical dashed grey and black lines highlight the key respective  
587 features of Os and Li isotope variation the dynamic carbon-osmium-lithium-model will  
588 attempt to recreate. The horizontal dashed lines represent  $1\sigma$  age uncertainty for Os (green)  
589 and Li (red) isotope records.

590

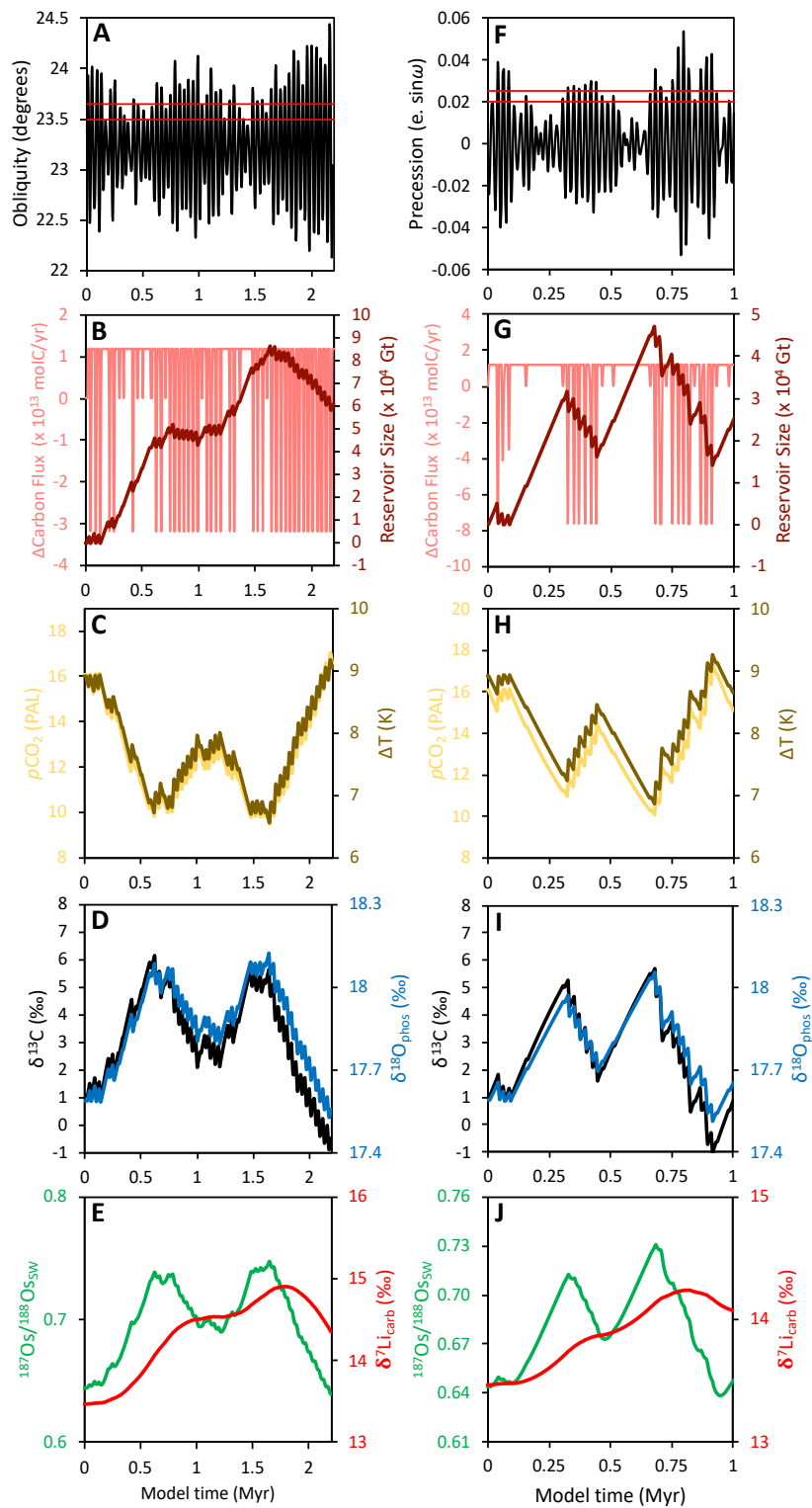


591 **Fig. 3.** The effect of degassing (A-C) and vegetation (D-F) on the O, Os and Li isotope systems  
 592 using a dynamic carbon-osmium-lithium-model.

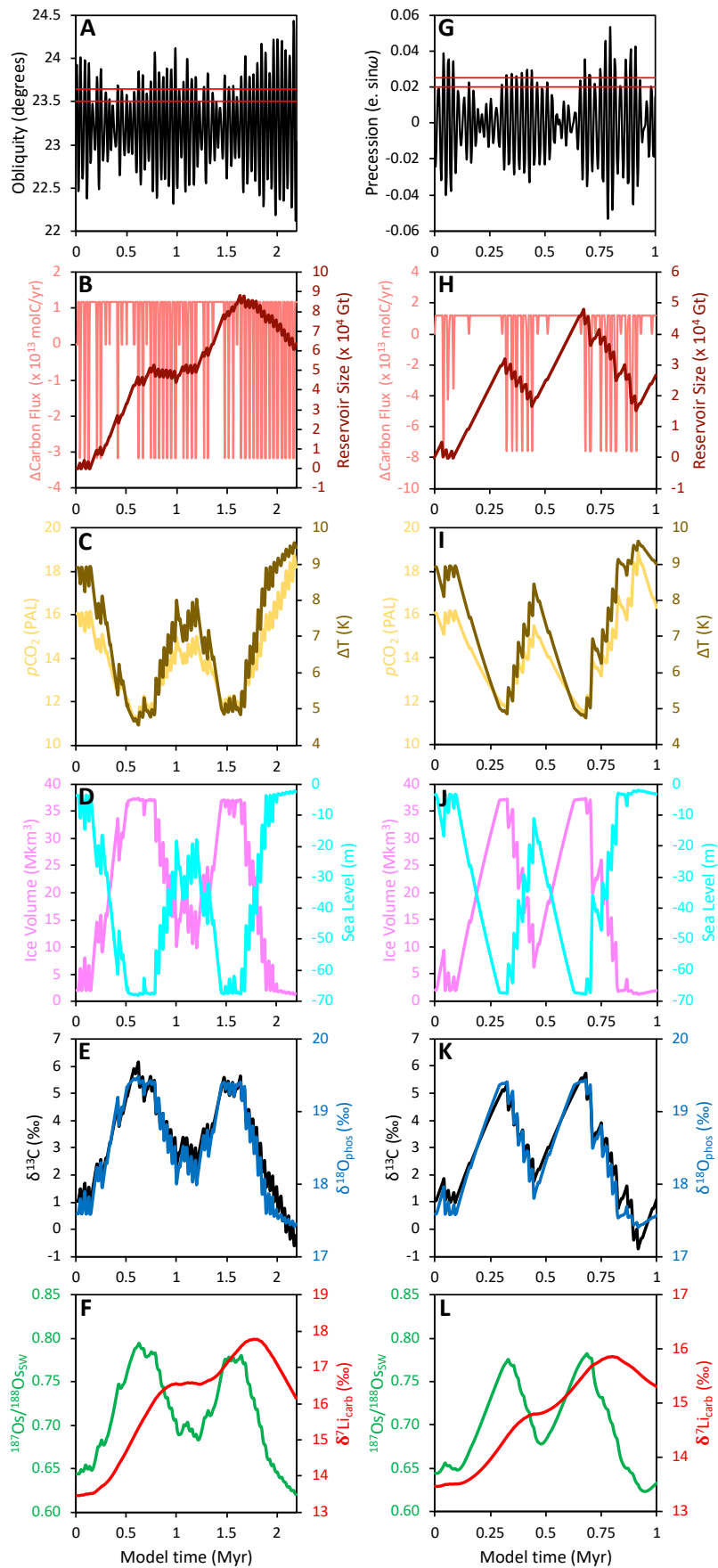
593



594 **Fig. 4.** Orbital records for the last 30 Myr. Precession (A) and obliquity (C) from the La2004  
 595 numerical model (grey) (Laskar et al., 2004) used to drive carbon-cycle models (inset of A  
 596 and B). The eccentricity (A) and the amplitude modulation of obliquity (C) along with their  
 597  $\sim 2.4$  Myr (0 to 0.7 cycles/myr) low pass filtering are show by black and red lines,  
 598 respectively. A periodogram of the eccentricity (B) and the obliquity amplitude modulation  
 599 (D) are shown along with dominant periods (Myr) (Sproson, 2020).  
 600



602 **Fig. 5.** The effect of an astronomically controlled quasi-stable reservoir on the C, O, Os and  
 603 Li isotope systems. Modelled for a period of exceptionally low obliquity (A-E) and  
 604 precession (F-J) variability using a dynamic carbon-osmium-lithium-model.

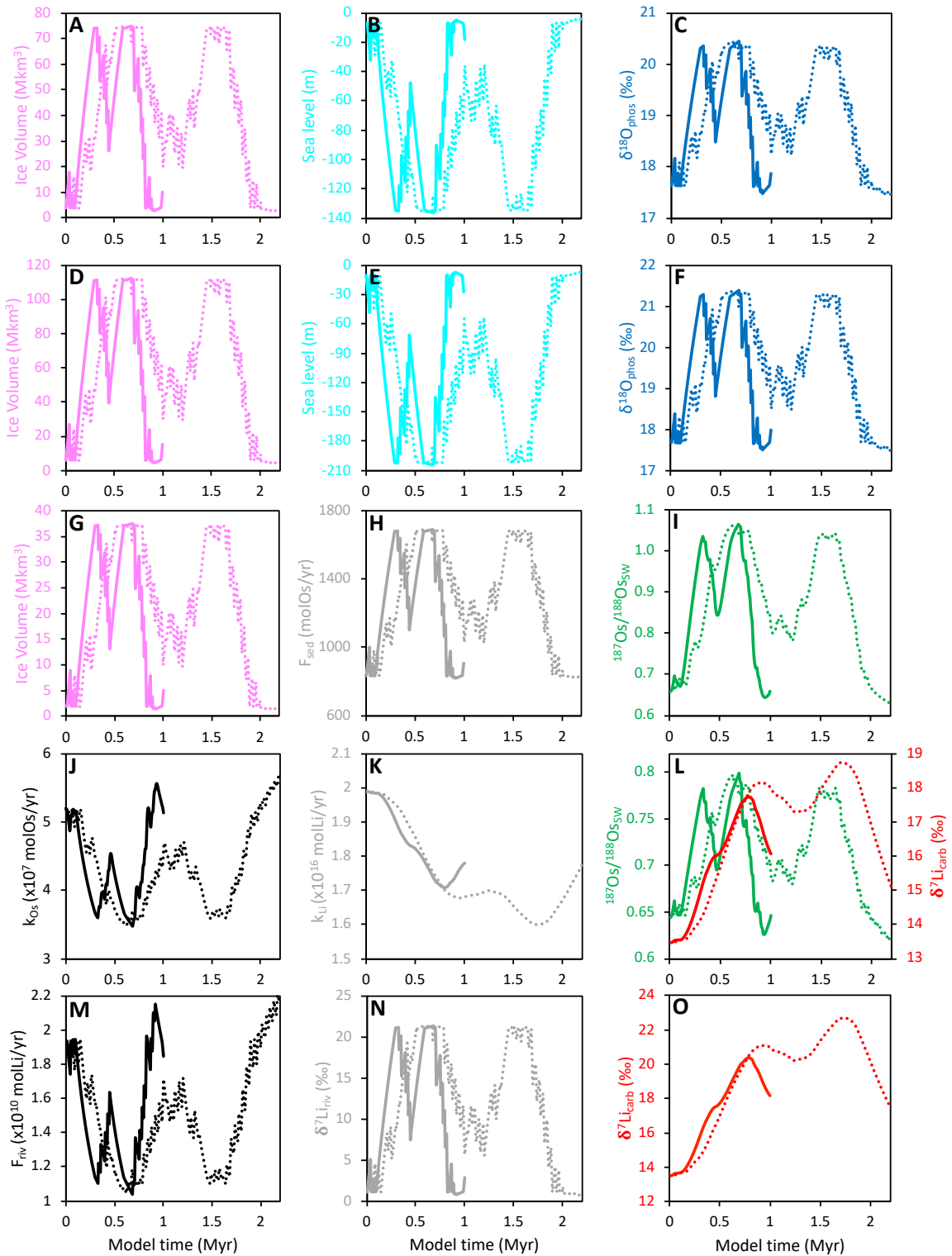


606 **Figure 6.** The effect of an astronomically controlled quasi-stable reservoir on the C, O, Os

607 and Li isotope systems for a period of exceptionally low obliquity (A-F) and precession (G-  
608 L) variability. As opposed to scenarios presented in Fig. 3 and Fig. 5, the ice sheet and  
609 climate sensitivity of Pohl *et al.* (2016) has been added.

610





611 **Fig. 7.** Sensitivity studies for the effect of an astronomically controlled quasi-stable reservoir  
612 on the C, O, Os and Li isotope systems for a period of exceptionally low obliquity (dashed  
613 lines) and precession (solid lines) variability with the ice sheet and climate sensitivity of Pohl  
614 *et al.* (Pohl *et al.*, 2016). Sensitivity studies are as follows: ice volume, sea level and  $\delta^{18}\text{O}_{\text{phos}}$

615 for an ice sheet thickness of 2 km (A-C) and 3 km (D-F); the effect of tying ice volume (G)  
616 to sedimentary Os flux (H) on the  $^{187}\text{Os}/^{188}\text{Os}$  of seawater (I) after replacing Eq. 29 with Eq.  
617 31; the influence of doubling the partition coefficient (k) of Os (J) and Li (K) on the  
618  $^{187}\text{Os}/^{188}\text{Os}_{\text{sw}}$  and  $\delta^7\text{Li}_{\text{carb}}$  values (L); the effect of increasing the fractionation factor of the Li  
619 riverine endmember to 20 ‰ (M and N) on  $\delta^7\text{Li}_{\text{carb}}$  (O).

620

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