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Journal Pre-Pre-

1 Analysis of fault bend folding kinematic models and comparison with an analog experiment.

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24 Abstract:

Analog modeling of a flat-ramp-flat fault system was performed and its geometry and 25 displacement field were compared to those of different kinematic models such as classical fault 26 bend folding, fault parallel flow, incline-shear, curvilinear hinge, and backlimb trishear. To obtain 27 the displacement vectors of the analog experiment, a Particle Image Velocimetry was performed. 28 29 All analyzed kinematic models could explain the general configuration of the fault bend folding. However, only backlimb trishear could represent the geometry, directions of particle displacements, 30 and relations between the displacements' vectors. We propose in this paper that the combination of 31 32 different asymmetry angles and different apical angles of the backlimb trishear model for each bend 33 in a fault bend fold could be a very versatile and general kinematic model for simulating fault bend folds. Backlimb trishear apical angle can be used to control the shape of the hinges of a fold, while 34 the asymmetry can be used to convolve the velocity of the particles above the fault. Both apical 35 angle and asymmetries different from zero imply thickness changes. Fault bend folds with high 36 inclination forelimbs can be reproduced with high positive asymmetries in the anticline bends of the 37 fault. 38

39

40 1. Introduction

Fault bend folding forms as the result of the movement of a fault block along a non-planar 41 42 fault surface, which causes the bending of the block and therefore the formation of the fold. This deformation generally occurs in the hanging wall of the fault (Suppe, 1983; Poblet, 2004; Brandes 43 and Tanner, 2014). It is one of the main causes of the folding of the rocks in nature and the object of 44 different types of analog, numerical-mechanical, geometric, and kinematic modeling. Although, 45 mechanical models (either analog or numerical) allow a better understanding of the dynamics of 46 deformation, geometric and kinematic models have a practical utility when constructing complex 47 balanced cross-sections, and that is why they are the target focus of this work. Different geometric 48 and kinematic models (Figure 1) were proposed to simulate fault bend folding (Suppe, 1983; White 49

et al., 1986; Egan et al., 1997; Kane et al., 1997; Cristallini and Allmendinger, 2002), and some of
them were implemented in balance cross-section construction software (Contreras, 2002; Cristallini
et al., 2021). We use an analog model as a basis to analyze the different kinematic models and to
propose variations in the backlimb trishear method (Cristallini and Allmendinger, 2002) that may be
useful to simulate flat-ramp-flat fault systems.

55 "Insert Figure 1 here"

To produce a fault bend fold in our physical model, appropriate analog materials were used 56 to simulate the upper crust. We employed a flexible sugar paste, which allows us to generate the 57 58 folding. The analysis of a succession of images, using particle-image velocimetry (PIV), provides a digital visual record of the velocity/displacement vectors during the evolution of the structure. In 59 60 this work, the shape obtained and the displacement field measured in the analog model of fault bend 61 fold are compared with several geometric and kinematic models. Here we show that backlimb trishear is the model that most faithfully reproduces the geometry, directions of particle 62 displacements, and relations between the displacements' vectors in different parts of the fold. We 63 also prove that this method is well suited to replicate structures with high dipping forelimbs and that 64 by modifying the asymmetries of the backlimb trishear model, changes in the dipping of the layers 65 involved during folding can be achieved. 66

67 In the following section, we will first review existing geometric and kinematic models.68 Next, we will present the analog model performed, and finally, we discuss our overall results.

69 2. Fault bend folding models

The first quantitative model (here considered as classical fault bend folding model: CFBF) describing the geometry and kinematics of fault bend folds was proposed by Suppe (1983) based on conservation of area and thickness of beds during deformation (Figure 1a). Suppe (1983) formulated the equations that determine both the geometry and kinematics for a fold developed over a fault with a single step or break, as well as for more complex folds formed on ramps with different angles, sheared folds, and hybrid structures (Poblet, 2004; Brandes and Tanner, 2014). The initial

assumptions applied for the simplest case are that area is conserved and the thickness of the layers 76 is preserved throughout the evolution of the fold (Suppe, 1983). Therefore, the model ensures that 77 bed length in the slip direction remains constant during deformation. The layers are deformed by 78 79 flexural slip and axial surfaces are always bisectors of bed bendings (Figure 1a). According to this model, the characteristic shape of a fault bend fold consists of a frontal limb with a greater dip than 80 the backlimb, which remains parallel to the fault's ramp. The evolution of simple step fault bend 81 folds corresponds to two perfectly differentiated stages (Suppe, 1983; Poblet, 2004) known as the 82 lifting of the crest and widening of the crest. It is important to notice that, during the first stage, the 83 slip applied to the hanging wall is not all transmitted forward. In Figure 1a, applied slip is indicated 84 as S0 and transmitted slip as S1, so in this model S0 > S1. Suppe (1983) CFBF conserve area (in 85 cross-sections), thickness, and line length during deformation. 86

The kinematic field that is associated with the model of kink band migration (Suppe, 1983) 87 was presented by Johnson and Berger (1989). The model proposes that within a simple step 88 structure, 3 velocity domains can be defined based on the fault's geometry. Discontinuities separate 89 these domains and are equivalent to the active axial surfaces previously characterized by Suppe 90 (1983). Vectors are parallel to the lower fault plane in the first domain, then parallel to the ramp in 91 the second domain, and in the third domain, they are parallel to the top fault plane. Hardy (1995) 92 contributes to the development of the kinematic analysis of fault bend folds, describing the 93 94 horizontal and vertical components of the velocity vectors relying on trigonometric relationships that consider the ramp's dip. Just as in the kink band model the most important operating 95 mechanism is flexural slip (Suppe, 1983; Medwedeff and Suppe, 1997), other models rely on 96 97 different mechanisms for folding.

98 One of the most commonly used is the fault parallel flow (FPF in this work) proposed by 99 Egan et al. (1997) and Kane et al. (1997). This model (Figure 1b) is based on migration parallel to 100 the fault of the materials of the hanging wall, using axial surface bisectors of fault bends as limits 101 between different velocities. This method states that all particles within the hanging wall move

parallel to the fault surface, along virtual flow paths (Ziesch et al., 2014). Subsequent studies on
FPF allow calculating the associated deformation in different areas of the structure (Ziesch et al.,
2014). Figure 1b shows that slip applied to the hanging wall (S0) is completely transmitted forward:
S0 = S1. This model conserves only area (in cross-sections) during deformation; thickness and line
length are not preserved (see for example thinning of the forelimb in Figure 1b).

Another mechanism that can operate in kinematic reconstructions of fault bend folding is the 107 simple shear (Gibbs 1983; 1984) and its derivations (White et al., 1986; White, 1992; Yamada and 108 109 McClay, 2003). Initially, the method assumed that the hanging wall is deformed by simple shear in vertical planes (Gibbs 1983; 1984). As the angle of shear is vertical, the model is referred to as 110 vertical-shear (Figure 1c). Modifications were subsequently developed and the assumption about 111 the inclination of the shear planes to the vertical is removed (White et al., 1986); this is why the 112 model is commonly known as incline-shear (ISh in this work), where vertical-shear is a special 113 case. The direction of simple shear within the hanging wall block is constant and has a very strong 114 influence on the shape of the resulting fold (White et al., 1986; White, 1992). The slip applied to the 115 hanging wall could be amplified, conserved, or reduced depending on the shear angle. If the shear 116 117 angle is vertical, the slip is conserved along a complete simple step structure (Figure 1c). This model conserves only area (in cross-sections) during deformation; thickness and line length are not 118 preserved (see for example thinning of backlimb and forelimb in Figure 1c). 119

The theory initially formulated by Suppe (1983) covers exclusively folds formed from faults 120 composed of straight segments with angular breaks, so the modeled examples fail to mimic the 121 traits observed in natural cases. They fail to reconstruct the curved geometry seen in many of the 122 main faults from which the anticlines are generated (Medwedeff and Suppe, 1997). To achieve this 123 feature, Medwedeff and Suppe (1997) propose a model where the main fault has several segments. 124 The length of each segment is reduced, so the fault can be recreated with curved geometry. In this 125 way, the resulting hinge is no longer sharp; on the contrary, it is rounded, which is more consistent 126 with observations from field examples. In turn, each bend generates new axial surfaces that interfere 127

with each other, bringing greater complexity to the structure (Medwedeff and Suppe, 1997). This
same idea can also be applied, and simpler, to fault parallel flow and incline-shear models, and is
usually used in software cross-section construction. Another modification of the Suppe (1983)
CFBF includes the application of basal shear to be able to explain fault bend folds in which
backlimb inclination is less than fault dipping (Suppe et al., 2004).

Cristallini and Allmendinger (2002) have pointed out that in several analog and mechanical 133 models of fault bend folding formed above faults composed of straight segments with angular 134 breaks, the resulting fold has rounded hinges. These results cannot be explained by classical fault 135 bend folding, neither by fault parallel flow nor incline-shear. To explain these cases, they propose 136 the backlimb trishear model (BLT in this work; Figure 1e, f, and g; Figure 2) where the fold hinge 137 describes soft curvatures in the upper strata while those layers near the fault zone show strong 138 angular breaks (Cristallini and Allmendinger, 2002). This model conserves only area (in cross-139 sections) during deformation; thickness and line length are not preserved. 140

To explain a similar situation, Tavani et al. (2005) replace axial surfaces represented with straight lines by circular zones that generate the curved geometry seen in fold's layers (Figure 1d). This curvilinear hinge model (CH in this paper) conserves area (in cross-sections), thickness, and line length during deformation, and transmits some shear forward. Tavani et al. (2005) model explains rounded anticline hinges, however, cannot explain rounded syncline hinges.

146 "Insert Figure 2 here"

The backlimb trishear model (Cristallini and Allmendinger, 2002) is conceptually analogous to forelimb trishear (Erslev, 1991, Allmendinger, 1998), and presupposes incompressible flow in triangular zones focused on the fault bends. It uses equations of area conservation, similar to those derived for forelimb trishear by Zehnder and Allmendinger (2000), but in these cases applied to the material above a fault bend. Cristallini and Allmendinger (2002) focused their paper on the backlimb of a fold and named their model as "backlimb trishear" (Figure 2). However, the idea (and of course the equations) can be applied to any bend in a fault and can be used to explain syncline

and anticline hinges (Figure 1 e, f, and g). The backlimb trishear, in addition to hanging wall slip 154 and fault bend angle, has basically two variables, the backlimb trishear apical angle, and the 155 asymmetry. The second is measured with respect to the fault bend bisector and is positive forward 156 157 and negative backward. Cristallini and Allmendinger (2002) showed that a symmetrical backlimb trishear zone does not produce the variation of the applied slip versus the transmitted slip. However, 158 asymmetrical zones produce slip variations. Changing the backlimb trishear asymmetry, the model 159 can satisfy the slip variations of classical fault bend folding (Figure 1e), fault parallel flow (Figure 160 1f), or incline-shear (Figure 1g). 161

162 3. Analog model methodology

Intending to analyze and test different kinematic models of fault bend folding, we perform an analog model to obtain the displacement field during the formation of simple step fault bend folds. In this way, it is possible to evaluate and compare the displacement field and the resulting geometries with those of the investigated kinematic models. The experiment focuses on evaluating the vectors for the first stage of fold growth, where lifting of the crest occurs.

The analog model technique is practical and simple for obtaining displacement fields during deformation. Vectors of displacement are obtained by particle image velocimetry (Sveen, 2004), a methodology widely used in geological process studies (Kincaid and Griffiths, 2003; Boutelier and Cruden, 2013; Strak and Schellart, 2014; Schellart and Strak, 2016) performed with PIVlab-MATLAB program (Thielicke and Stamhuis, 2014). The results obtained were compared with the previously analyzed kinematic models (Figure 1). The technique of analog modeling is useful since it allows the incorporation of a mechanical framework into the kinematic method.

175 *3.1. Analog model setup*

To simulate the stage of the lifting of the crest in a simple step fault bend fold, we used an experimental setup consisting of a footwall represented by a rigid, non-deformable wedge and a deformable hanging wall represented by a layered plastic material (Figure 3). To meet the objectives of this experiment, a material that would not fracture or fail was needed. Cohesionless

materials as sand, traditionally used in experiments of deformation of the upper crust (Cristallini et 180 al., 2009; Ritter et al., 2016; Marshak et al., 2019), do not meet these characteristics. The models 181 required a cohesive material being able to simulate the strata that constitute a sedimentary cover 182 183 involved in the folding, where no fractures are desired. For this reason, we used sheets of sugar paste to model the hanging wall. The preparation has a density of 1.27 g/cm^3 and a viscosity equal 184 to 2.2 x 10^7 Pa s, being this value similar to plasticines widely used as analog materials for 185 experimental setups (Schöpfer and Zulauf, 2002; Zulauf and Zulauf, 2004). The sheets are separated 186 from the bottom of the box, the metal wedge, and between them by low friction surfaces. To avoid 187 the formation of voids and to approach the challenging scaling conditions, all the experiment is run 188 189 inside a biaxial loading cell like that proposed by Bazalgette and Petit (2007). To fill the spaces above the layers of sugar paste, dough made with salt, flour, and water (density \Box 1.29 g/cm³ & 190 viscosity \Box 1.2 x 10⁵ Pa s) was used. This mass was placed at the top reaching 9 cm in height. 191 separated by a plastic film that acts as a moisture barrier. The dough is used to compress the entire 192 model, increasing vertical pressure over the sugar sheets (Bazalgette and Petit, 2007), and causing 193 the layers of sugar paste to accommodate by folding to the movement of the rigid wedge. As the 194 box is closed, this material allows an increase in the confining stress and thus inhibits the separation 195 of the sugar paste from the fault block. 196

197 "Insert Figure 3 here"

To ensure that the deformation occur on top of the wedge, it was decided not to move the 198 hanging wall, as in a classical fault bend fold, but move the footwall wedge instead. The sugar paste 199 layers were cut with different lengths to be in close contact with the ramp of the metal wedge to 200 simulate the fault. However, they cannot be extended to the right side of the experiment because a 201 classical fault bend fold transmits part of the applied slip forward by the upper plane. To simulate 202 this situation, the layers of sugar paste are constructed shorter than the box, and the space that is not 203 occupied by them is filled by a colorless silicone with non-Newtonian behavior with a density of 204 0.97 g/cm³ and a viscosity of 5 x 10^4 Pa s at 20° C (Weijermars, 1986). This idea is similar to that 205

used by Chester et al. (1991) in the apparatus to simulate a fault bend fold and is needed torepresent this type of structure.

Plane strain condition of the experiment was ensured with continuous observation. The 208 model was photographed on both sides of the deformation box, mounted with two opposite acrylic 209 walls for this purpose. The apparatus also has a motor-driven piston to compress the materials 210 arranged inside. The experiment carried out was 47 cm long by 15 cm wide and 19 cm high (Figure 211 3). Inside it and in contact with the piston, a rigid wedge of 30° was placed. The wedge is 22 cm 212 long at its base and 14 cm on the upper fault flat and its ramp is 9 cm long. This device simulates 213 the motion of the hanging wall past the fault bends (Zanon and Gomes, 2019). At the base of the 214 experiment, only 25 cm of sugar paste was placed while at the top were placed 37 cm and 10 cm of 215 transparent silicone in contact with the piston (Figure 3). Above the sugar paste and the silicon, the 216 dough was used to fill the box and increase vertical load over the experiment. 217

218 The model was compressed for 67 minutes, at 10 cm/hour, reaching a total of 11 cm of shortening and forming a fault bend fold. As the structure is generated, photographs were taken 219 perpendicular to the direction of motion of the piston on both sides of the model to follow the 220 evolution of the fold. Previous trials concluded that the deformation observed through the sidewalls 221 of the box is representative of the internal deformation within the models and plane strain can be 222 assumed. A total of 67 images were obtained, one per minute. These photographs were 223 subsequently processed using the Irfanview TM (Skiljan, 2012) software to crop the area of interest 224 225 and generate the serial images. These images were analyzed with the PIVlab-MATLAB program (Thielicke and Stamhuis, 2014) to obtain the kinematic vectors that illustrate the displacement field 226 of particles that generate the fold and the evolution during the lifting of the crest. 227

This experiment is a qualitative analog for a two bend fault bend fold system; it is not an accurately scaled physical model (Hubbert, 1937). It is intended to compare shapes and relative displacement and velocity relations with kinematics models. In this work, we focused on the

different domains of the displacement field during the evolution of a fault bend fold rather than theabsolute values of the displacement vectors.

3.2. Particle image velocimetry:

There are numerous programs to carry out a particle image velocimetry (Adam et al. 2002, Adam et al., 2005; Schellart and Strak, 2016), but we selected software PIVlab-MATLAB (Thielicke and Stamhuis, 2014) because it is easy to implement and enables complex graphics of both the displacement vectors and their corresponding PIV-derived parameters like the magnitude of displacement velocity (Krýza et al., 2019).

To calculate the vectors this tool divides each of the images into user-defined areas, of a 239 certain number of pixels to be analyzed. The image should be calibrated indicating both the actual 240 241 distance (in mm) between two points in the photo and the time interval (in ms) between 2 successive photos. In this experiment, each pixel in the photographs represents 0.02 mm of the 242 analog model and the time interval was equal to 60 s. In each defined area, the program compares 243 the pixels for two successive images, detecting differences that are attributable to the movement and 244 plotting the vectors. The presented displacement vectors are calculated on the basis of redistribution 245 246 of the pixels between the photographs taken 60 s apart, representing the total displacement over that interval. After processing, validation of the vectors is performed, crossing out outliers considering 247 that maximum velocity is the one of the motor-driven piston. 248

To concentrate the deformation just over the basal ramp, in this experiment the aluminum wedge that represents the footwall of the fault bend fold, worked as a piston, and the hanging wall was passively deformed. Therefore, to compare the results of these experiments with classical fault bend folds, the uniform displacement of the aluminum wedge was subtracted from the obtained vector field. The resultant field was analyzed and plotted in figures 6, 7, and 8.

4. Geometric and kinematic analog model results

255 4.1. Comparing fold shape

We use the final stage of the analog model to compare the resulting fold shape with those of 256 different kinematic models (Figure 4). The best fit (blue line in Figure 4) was visually made on the 257 yellow highlighted layer of the experiment. Figure 4a compares the analog model with classical 258 259 fault bend folding (CFBF; Suppe, 1983), Figure 4b with the fault parallel flow model (FPF; Egan et al., 1997; Kane et al., 1997), Figure 4c with a special case of vertically incline-shear, where the 260 261 inclination of the shear planes is vertical (ISh; White et al., 1986), Figure 4d with curvilinear hinge model (CH; Tavani et al., 2005) and Figure 4e with a special case of backlimb trishear (BLT; 262 Cristallini and Allmendinger, 2002). In a quick view, all the models explain the general geometry of 263 the fold of the analog experiment. However, there are differences, and some models explain better 264 265 some features than others. For example, CFBF, FPF, and ISh fail to explain the curvilinear shape of the fold, while CH and BLT represent very well this feature for the anticline, but CH does not copy 266 the curvilinear shape of the synclines. ISh model fits very well the area covered by the fold, 267 however, like CFBC, FPF, and CH, it does not fit the slip over the footwall ramp with that of the 268 analog model. 269

270 "Insert Figure 4 here"

To analyze backlimb trishear fitting, we tested different trishear apical angles and 271 asymmetries (Figure 5). In the initial code of Cristallini and Allmendinger (2002) both parameters 272 had to be the same for all the fault bendings. In Figure 5 we show the results of different 273 asymmetries, using 30° as trishear apical angle. If we compare the resulting curves with the vellow 274 highlighted bed, we can see that -10° asymmetry works better for the backlimb while $+8^{\circ}$ 275 asymmetry works better for the forelimb. For this work, we use the development version of Andino 276 3D software (Cristallini et al., 2020) to modify the original code of Cristallini and Allmendinger 277 (2002) to allow the use of different asymmetries and apical angles for each bend in the fault. In this 278 way, we can produce a better fitting of the yellow highlighted bed using asymmetries of -10° for the 279 backlimb bend and $+8^{\circ}$ for the forelimb bend (Figure 4e). 280

281 "Insert Figure 5 here"

Natural anticlines with flat-ramp-flat geometry, those in which the fault ramp did not broaden to the top but developed an upper flat in the middle of the stratigraphic column can be comparable with our analog model, in particular, if the sedimentary cover involved in the folding does not develop major secondary faults.

286 4.2. Comparing displacements and velocities

To trace the movement of the particles in the experiment, we use PIVlab-MATLAB 287 (Thielicke and Stamhuis, 2014). The results can be seen in Figure 6 for three steps with 1.25, 2.5 288 cm, and 4.8 cm of applied slip. The blue vectors in figures 6a, b and c show the incremental 289 displacement field calculated by the PIV. According to the kinematic field, two domains of rotation 290 291 defining triangular geometries can be recognized, and the movement of particles is concentrated inside them. Figures 6d, e, and f are color maps of the slip vectors direction for the corresponding 292 displacement field; a progressive rotation along the fault bending zone is outlined. The yellow 293 dashed lines of Figure 6 represent the backlimb trishear zones adjusted to the analog model. These 294 triangular zones fit very well the distortion zones seen in the displacement field (Figure 6). The 295 displacement vectors are initially composed of a single horizontal component, Vx. When particles 296 reach the backlimb rotation zone, the vertical component of the displacement vectors increases as 297 the experiment progresses (Figures 6d, e, and f). After that, the displacement vectors remain rather 298 parallel to the surface of the ramp (metal wedge), until particles enter the forelimb rotation zone 299 where they progressively lose the vertical component Vy. Finally, displacement vectors are 300 composed once again by horizontal vectors. The displacement vectors above the ramp are rather 301 parallel to it (Figures 6a and 6b). In advanced stages of the model, the displacement vectors are not 302 completely parallel to the fault, having an angle slightly bigger (Figure 6c). This happens perhaps, 303 because in the final stage of the experiment, the resulting structure, moves a little away from a 304 theoretical fault bend fold, and a smooth lift-off is beginning. Because of this, we considered that 305 the stages represented in figures 6a and b are the most appropriate to make a detailed comparison 306 with a kinematic model. 307

Figure 7 shows a comparison between the displacement vectors calculated by PIV in the experiment (blue arrows) and those calculated by the backlimb kinematic model using -10° and $+8^{\circ}$ asymmetries of backlimb and forelimb respectively and an apical angle of 30° (same model as Figure 6b and 6e). There is a very good agreement between both displacement fields, even in the rotation zones above the fault bendings (Figure 7).

313 "Insert Figure 6 here"

314 "Insert Figure 7 here"

To compare the mean velocity vectors, three windows of the experiment section were 315 selected to calculate the average velocity magnitudes outside of the triangular areas where vector 316 rotations take place (Figure 8): one over the basal plane (A), one over the ramp (B), and one over 317 318 the upper plane (C; Figure 8). The average velocities are 6.8 cm/h, 6.19 cm/h and 5.61 cm/h, respectively. In the same figure, a table shows the predicted velocities for the analyzed kinematic 319 models. The decrease in velocity of B with respect to A can only be explained by the backlimb 320 trishear model (BLT) using the same asymmetries as in figures 4e and 7 (backlimb asymmetry -10). 321 The decrease in velocity of C with respect to B can be explained by classical fault bend folding 322 (CFBF), curvilinear hinge model (CH), and backlimb trishear (BLT with +8° of forelimb 323 asymmetry). However, the BLT shows the best fit between the velocity magnitudes. 324

325 "Insert Figure 8 here"

To accurately compare the analog model to the different theoretical kinematic models, in Figure 9, we plotted the subtraction of kinematic models velocities to the analog model velocities. Backlimb trishear (BLT) model is the one with the least differences with respect to the analog model, for both the horizontal and vertical components of the velocity vectors (Vx and Vy).

330 "Insert Figure 9 here"

To facilitate the application of the equation proposed by Cristallini and Allmendinger (2002) to calculate velocity changes across fault bends, we develop the nomogram in Figure 10, where the resultant velocity after a bend can be calculated with respect to a normalized to 1 input velocity

334 asymmetry of the backlimb trishear zone (α). The blue curves are for syncline bending of the fault 335 (positives φ), while the orange curves are for anticlinal bendings (negatives φ). The curves for $\varphi =$ 336 $+30^{\circ}$ and $\varphi = -30^{\circ}$ shown in black are those used for the example of this paper. The blue point 337 corresponds to $\alpha = -10^{\circ}$ asymmetry of the backlimb adjusted to the experimental fold (Figures 4e 338 and 8) and the red point to the $\alpha = +8^{\circ}$ asymmetry adjusted to the forelimb (Figures 4e and 8). The 339 resultant velocity V1 is calculated as fractions of the input velocity normalized to 1 (V0 = 1). This 340 means that an output velocity of V1 = 1 implies that there is no change in velocities. Values of V1 < 1341 1 implies a reduction of velocity and V1 > 1 implies an increase. This graph allows sustaining that 342 the BLT model fits the experiment well. 343

344

"Insert Figure 10 here"

345 **5.** Discussion

The analog simulation described in this work does not represent the generality of the fault 346 bend folds, but it serves to analyze and compare the different kinematic models. We find that all the 347 analyzed kinematic models can broadly explain the fold geometry developed in the experiment 348 (Figure 4). However, backlimb trishear (BLT) is the only one that can mimic accurately the 349 350 geometry (Figure 4e), directions of particle displacements (Figure 7), and relations between the modulus of the velocity vectors (Figure 8). This is because BLT is the most flexible of the analyzed 351 kinematic models. With the trishear apical angle, the sharpness of the deformation zones above the 352 353 fault bends can be controlled, while the asymmetries variations can achieve different inclinations of the forelimb and changes in thickness. Moreover, when plotting the slip vectors directions in Figure 354 6, the change in their angle is gradual and occurs along a triangular shaped rotation zone. These 355 356 results fit well with the backlimb trishear model (BLT).

Furthermore, by subtracting the vertical and horizontal components of the velocity vector 357 from the fields proposed in theoretical kinematic models from the field obtained for the analog 358 model, the backlimb trishear model (BLT) is the one that presents the smallest differences. 359

Therefore, it is possible to state that this model is the one that most accurately represents the fold 360 generated in the laboratory and its kinematic evolution. It is postulated that this may be due to the 361 flexibility of the backlimb trishear model (BLT), where a wide range of geometries can be 362 363 represented from modifications in the aforementioned parameters. The nature of the materials used for the analog model support this conclusion: the sugar paste does not break during deformation, but 364 distributes along the rotation zone presented in BLT model. The same could happen with other 365 cohesive materials such as clay, while coarser granular materials such as dry sand do not develop 366 progressive rotation zones, being probably best represented with other theoretical models. 367

Cristallini and Allmendinger (2002) focused their work on explaining the geometry of the 368 backlimb in a fault bend fold. However, as we pointed before, their equations are more flexible and 369 can be applied to any bend in the fault surface. We modify their original code to enable the use of 370 independent backlimb trishear apical angles and asymmetries for each bend in the fault. In 371 Cristallini and Allmendinger (2002), the authors compare the BLT model with one of the 372 experiments of Chester et al. (1991). However, they only could compare the backlimb of the fold, 373 because of the limitations of the code. Now, we can show a complete comparison of the same fold 374 (Figure 11). There is a very good fit using a backlimb trishear apical angle of 30° and asymmetries 375 of -10° and $+35^{\circ}$ for backlimb and forelimb respectively (Figure 11). 376

377 "Insert Figure 11 here"

One of the restrictions of geometric and kinematic models of fault bend folding is their ability to represent highly dipping forelimbs. However, this can be solved by adjusting the asymmetry parameter of the BLT model. Figure 12 represents the comparison of one of the models of Chester et al. (1991) with a BLT simulation. In this case, with a forelimb asymmetry of +50, forelimb dipping of 80° can be achieved.

383 "Insert Figure 12 here"

Finally, based on the analyzes carried out in this work and on cited references, it is clearly observed that most of the described fault bend models (CFBF, FPF, and ISh) imply velocity vectors

parallel to the fault, where the only differences are the boundary between domains and the 386 magnitude of the velocity vectors. If we consider the simple step structure as a system of a backlimb 387 fold and a forelimb fold, all these models can be visualized as incline-shear cases, where the field 388 389 boundaries are in the direction of shear. When the boundary is established symmetrically concerning the fault bend (as a bisector) the velocity magnitudes are conserved. If the boundary is 390 not the bisector of fault bend, the velocity is not preserved on either side of the axial surface. With 391 positive asymmetries, the velocity is incremented after the boundary in a syncline bend and 392 decremented in an anticline bend, while with negative asymmetry the opposite occurs. Fault parallel 393 flow models (FPF) give rise to a symmetrical position of field boundaries with respect to the fault 394 bends and therefore velocities magnitudes are conserved above each fault bend (Figure 1b). In 395 contrast, in the first stage of a classical fault bend folding (CFBF), the axial surfaces are oriented to 396 preserve bedding thickness, and therefore the forward active axial surface does not bisect the fault 397 bend, causing velocity not to be preserved (Figure 1a). For the incline-shear model (ISh), the 398 velocity magnitudes are generally not conserved for each fault bend, and they are incremented or 399 400 decreased depending on the asymmetry. In the special case of vertical-shear, although the slip is not conserved for each fault bend, it is conserved for the complete system of a simple step structure 401 (Figure 1c). Backlimb trishear (BLT) can be applied to all the previous models (FPF, CFBF, or ISh) 402 403 just to add progressive rotation to the limbs and to increase the curvilinear geometry of the folds, distributing deformation within a triangular shape shear zone. 404

Although in this article we were able to simulate a fault bend fold using the BLT model, more work still needs to be done to determine which are the mechanical conditions that control asymmetry and apical angle. Although the discrete-elements model of Hardy and Finch (2007) and the analog models of Bazalgette and Petit (2007) were not made to analyze the BLT, they may suggest that the apical angle depends on the mechanical stratigraphy and friction between beds. With a strongly layered mechanical stratigraphy or very low friction between beds, a parallel layer mechanism is favored and consequently low apical angles in the BLT model. Contrary, the high

412 coupling between beds or a weakly layered mechanical stratigraphy could favor high BLT apical 413 angles. However, these relations need to be demonstrated, and others have to be found concerning 414 the asymmetry. For example, in our experience, the folding above most syncline bends of faults can 415 be described with negative asymmetries in the BLT model, but we have no conclusion about the 416 mechanical causes of this.

417 6. Conclusions

An analog model made in the laboratory is described and processed to derive a particle 418 image velocimetry. The generated displacement vectors illustrate the migration of materials as a 419 fault bend fold evolves. We use this example as a trigger to analyze different geometric and 420 kinematic models: CFBF (classical fault bed folding), FPF (fault parallel flow), ISh (incline-shear), 421 CH (curvilinear hinge model), and BLT (backlimb trishear). All models can explain the bulk 422 displacements of fault bend folding. However, only BLT can represent the geometry (Figure 4e), 423 directions of particle displacements (Figure 7), and relations between the velocity vector fields 424 (Figure 8). 425

We propose that the combination of different asymmetry angles and different apical angles 426 of BLT model for each bend in a fault bend fold could be a very versatile and general kinematic 427 428 model for describing these types of structures. BLT apical angle can be used to control the shape of the hinges of a fold, while the asymmetry can be used to convolve the velocity of the particles 429 above the fault. Both apical angle and asymmetries different from zero imply thickness changes. 430 431 BLT mode ensures the conservation of area (in a section) during deformation, even when the asymmetry and apical angle are variable for the different bends of the fault. Fault bend folds with 432 high inclination forelimbs can be reproduced with high positive asymmetries in the anticline bends 433 434 of the fault.

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558 Figure Captions:

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Figure 6: Total component of the displacement field represented with blue vectors. a. 584 Photograph of the experiment with 1.25 cm of applied slip. **b.** Photograph of the experiment with 585 2.5 cm of applied slip. c. Photograph of the experiment with 4.8 cm of applied slip. d., e., and f. 586 Color map graphics of slip vectors direction measured anticlockwise from the x-axis. Yellow 587 dashed lines represent the backlimb trishear zones adjusted to the analog model. 588

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609 Figure 10: a. Scheme showing resultant velocity (V_1) after a fault bend, calculated with respect to a normalized to 1 input velocity (V_0), the angle between both sections of the fault (φ) and 610 the asymmetry of the backlimb trishear zone (α). V₀ and V₁ are the velocities on either side of the 611 triangular zone. φ is the angle between both sections of the fault. α is the angle of asymmetry of the 612 backlimb trishear zone - the angle between the bisector of the fault bend angle (in a fine black 613 straight line) and the bisector of the apical angle of backlimb trishear (BLT axial line, dashed). 1. 614 Syncline bending of the fault (positives φ). 2. Anticlinal bending (negatives φ) (Modified from 615 Cristallini and Allmendinger 2002). b. Curves showing resolution for Cristallini and Allmendinger 616 (2002) velocity variation equation. Blue curves are for syncline bending of the fault (positives φ). 617 while the orange curves are for anticlinal bendings (negatives φ). In the analog model, the angle of 618 the fault was 30° (black curves). Blue point corresponds to $\alpha = -10^{\circ}$ asymmetry of the backlimb 619 adjusted to the experiment fold (Figures 4e and 7). Red point corresponds to the $\alpha = +8^{\circ}$ asymmetry 620 of the forelimb adjusted to the experiment fold (Figures 4e and 7). 621

Figure 11: Comparison between analog model from Chester et al. 1991 and a backlimb trishear with 30° of apical angle, $\alpha = -10^{\circ}$ asymmetry for the backlimb and $\alpha = +35^{\circ}$ asymmetry for the forelimb.

Figure 12: Backlimb trishear model reconstruction using ANDINO 3D software. The geometry obtained in the analog model with a high dipping forelimb can be reproduced. **a.** Backlimb trishear model with 40° of apical angle, $\alpha = -20^{\circ}$ asymmetry for the backlimb and $\alpha =$ +50° asymmetry for the forelimb. **b.** Analog model from Chester et al. 1991.



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G <i>i</i>			
Kinematic model	A (cm/h)	B (cm/h)	C (cm/h)
CFBF	6.8	6.8	3.9
FPF	6.8	6.8	6.8
ISh (vert.)	6.8	7.85	6.8
СН	6.8	6.8	3.9
BLT (-10;+8)	6.8	6.19	5.7



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Black and white versions:



Figure 1







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Figure 5











а.			
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BLT (-10;+8)	6.8	6.19	5.7



Figure 9





Figure 11





Highlights:

Analogue model was performed to obtain the velocity field during deformation.

Documentation of velocity vectors comes from particle image velocimetry.

Backlimb trishear can represent the geometry and directions of particles velocities.

Steeper-dipping forelimbs can be reproduced using high positive asymmetries.

Backlimb trishear apical angle can be used to control the shape of the hinges.

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Declaration of interests

 \boxtimes The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: