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# 3D deformable registration of longitudinal abdominopelvic CT images using unsupervised deep learning



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#### ABSTRACT

Background and Objectives: Deep learning is being increasingly used for deformable image registration and unsupervised approaches, in particular, have shown great potential. However, the registration of abdominopelvic Computed Tomography (CT) images remains challenging due to the larger displacements compared to those in brain or prostate Magnetic Resonance Imaging datasets that are typically considered as benchmarks. In this study, we investigate the use of the commonly used unsupervised deep learning framework VoxelMorph for the registration of a longitudinal abdominopelvic CT dataset acquired in patients with bone metastases from breast cancer.

Methods: As a pre-processing step, the abdominopelvic CT images were refined by automatically removing the CT table and all other extra-corporeal components. To improve the learning capabilities of the VoxelMorph framework when only a limited amount of training data is available, a novel incremental training strategy is proposed based on simulated deformations of consecutive CT images in the longitudinal dataset. This devised training strategy was compared against training on simulated deformations of a single CT volume. A widely used software toolbox for deformable image registration called NiftyReg was used as a benchmark. The evaluations were performed by calculating the Dice Similarity Coefficient (DSC) between manual vertebrae segmentations and the Structural Similarity Index (SSIM).

Results: The CT table removal procedure allowed both VoxelMorph and NiftyReg to achieve significantly better registration performance. In a 4-fold cross-validation scheme, the incremental training strategy resulted in better registration performance compared to training on a single volume, with a mean DSC of  $0.929 \pm 0.037$  and  $0.883 \pm 0.033$ , and a mean SSIM of  $0.984 \pm 0.009$  and  $0.969 \pm 0.007$ , respectively. Although our deformable image registration method did not outperform NiftyReg in terms of DSC  $(0.988 \pm 0.003)$  or SSIM  $(0.995 \pm 0.002)$ , the registrations were approximately 300 times faster.

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Conclusions: This study showed the feasibility of deep learning based deformable registration of longitudinal abdominopelvic CT images via a novel incremental training strategy based on simulated deformations

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#### 1. Introduction

Deformable medical image registration problems can be solved by optimizing an objective function defined on the space of transformation parameters [1]. Traditional optimization-based methods typically achieve accurate registration results but suffer from being computationally expensive, especially in the case of deformable transformations of high-resolution, three-dimensional (3D) images. Deep learning based registration methods, however, can perform registration in a single-shot, which is considerably faster than using iterative methods [2]. Due to the recent successes of deep learning for a wide variety of medical image analysis tasks [3], and the advances in Graphics Processing Unit (GPU) computing that have enabled the training of increasingly large three-dimensional (3D) networks [4], the number of studies using deep learning for medical image registration has increased considerably since 2016 [5].

Although deep learning could have a major impact on the field of medical image registration, there is still a gap between proof-of-concept technical feasibility studies and the application of these methods to "real-world" medical imaging scenarios. It remains unclear to which extent deep learning is suited for challenging coregistration tasks with large inter- and intra-patient variations and potential outliers or foreign objects in the Volume of Interest (VOI). Moreover, deep learning based methods typically require large amounts—i.e., thousands—of well prepared, annotated 3D training images that are rarely available in clinical settings [6].

The present study focuses on the registration of abdominopelvic CT images since these are widely acknowledged to be difficult to register [7]. In abdominopelvic imaging, the conservation-of-mass assumption is typically not valid and, although local-affine diffeomorphic demons have been used in abdominal CT images [8], the transformation is typically not a diffeomorphism. For instance, bladder-filling or bowel peristalsis in the abdomen may vary between images. More specifically, we consider a longitudinal abdominopelvic CT dataset that comprises several images of each patient acquired at distinct time-points. From a clinical perspective, accurate and real-time (< 1 second) deformable registration of longitudinal datasets is a necessary step; for instance, in oncological imaging to provide the reporting radiologist with registered images and in radiation therapy for treatment planning. For radiologists reporting on the most recent of a series of oncologic follow-up CT scans, real-time registration during the reporting session would facilitate comparing scans for changes in disease extent or tumor size, and response assessment. In addition, any add-on of further processing, like automated lesion detection and segmentation for disease follow-up and response assessment, might benefit from fast registration prior to their execution [9–11].

This study proposes a novel incremental training strategy based on simulated deformations to enable training of one of the most used unsupervised single-shot deep learning frameworks (VoxelMorph [12]) for deformable registration of longitudinal abdominopelvic CT images of patients with bone metastases from primary breast cancer. In addition, we assessed the maximum displacements that can be learned by the VoxelMorph framework and the impact of extra-corporeal structures, such as the CT table, clothing and prostheses on the registration performance. The in-

crementally trained VoxelMorph framework was compared against iterative registration using the NiftyReg [13] toolbox that was selected because of its excellent performance on abdominal CT images in a comparative study [14].

The contributions of this work are:

- demonstrating the impact of removing extracorporeal structures before deformable image registration;
- using simulated deformations to partially overcome the limitations of the VoxelMorph framework for the deformable registration of abdominopelvic CT images;
- introducing a novel incremental training strategy tailored to longitudinal datasets that enables deep learning based deformable image registration when dealing with large displacements and limited amounts of training data.

This paper is structured as follows. Section 2 outlines the background of medical image registration, with a particular focus on deep learning based methods. Section 3 presents the characteristics of our longitudinal abdominopelvic CT dataset, as well as the deformable registration framework, the proposed incremental training strategy, and the evaluation metrics used in this study. Section 4 describes the experimental results. Finally, Sections 5 and 6 provide a discussion and concluding remarks, respectively.

# 2. Related work

This section introduces the basic concepts of medical image registration and provides a comprehensive overview about the state-of-the-art of deformable registration using deep learning.

# 2.1. Medical image registration

Medical image registration methods aim to estimate the best solution in the parameter space  $\Omega \subset \mathbb{R}^N$  which corresponds to the set of potential transformations used to align the images, where N is the number of dimensions. Typically,  $N \in \{2,3\}$  in biomedical imaging. Each point in  $\Omega$  corresponds to a different estimate of the transformation that maps a moving image to a fixed image (target). This transformation can be either parametric, i.e., can be parameterized by a small number of variables (e.g., six in case of a 3D rigid-body transformation or twelve for an 3D affine transformation), or non-parametric, i.e., in the case that we seek the displacement of every image element. For most organs in the human body, particularly in the abdomen, many degrees of freedom are necessary to deal with non-linear or local soft-tissue deformations. In global deformable transformation, the number of parameters encoded in a Displacement Vector Field (DVF)  $\phi$  is typically large, e.g., several thousands. Therefore, two-step intensity-based registration approaches are commonly employed in which the first step is a global affine registration and the second step is a local deformable registration using for example B-splines [15].

Traditional medical image registration methods often use iterative optimization techniques based on gradient descent to find the optimal transformation [1,15,16]. Deformable registration can be performed using demons [17], typically based on diffeomorphic transformations parameterized by stationary velocity fields [18]. In addition, global optimization techniques that leverage evolutionary

algorithms [15] and swarm intelligence meta-heuristics can be useful to avoid local minima [19]. Several off-the-shelf, open-source toolboxes are available for both parametric and non-parametric image registration in biomedical research, such as: elastix [20], NiftyReg [13], Advanced Normalization Tools (ANTs) [21], and Flexible Algorithms for Image Registration (FAIR) [22].

# 2.2. Deep learning based registration

Since 2013, the scientific community has shown an increasing interest in medical image registration based on deep learning [5]. Early unsupervised deep learning based registration approaches leveraged stacked convolutional neural networks (CNNs) or autoencoders to learn the hierarchical representations for patches [23,24].

Fully-supervised methods, such as in [25], have focused on learning a similarity metric for multi-modal CT-MRI brain registration according to the patch-based correspondence. Another supervised method based on the Large Deformation Diffeomorphic Metric Mapping (LDDMM) model called Quicksilver was proposed in [26] and tested on brain MRI scans. In this context, Eppenhof and Pluim [27] introduced the simulation of ground truth deformable transformations to be employed during training to overcome the need for manual annotations in the case of a pulmonary CT dataset. Very recently, in [28], a graph CNN was used to estimate global key-point locations and regress the relative displacement vectors for sparse correspondences.

Alternatively, several studies have focused on weaklysupervised learning. For example, Hu et al. [29] proposed a weakly-supervised framework for 3D multimodal registration. This end-to-end CNN approach aimed to predict displacement fields to align multiple labeled corresponding structures for individual image pairs during the training, while only unlabeled image pairs were used as network input for inference. Recently, generative deep models have also been applied to unsupervised deformable registration. Generative Adversarial Networks (GANs) can be exploited as an adversarial learning approach to constrain CNN training for deformable image registration, such as in [30] and [31]. In [32], spatial correspondence problems due to the different acquisition conditions (e.g., inhale-exhale states) in MRI-CT deformable registration, led to changes synthesized by the adversarial learning, which were addressed by reducing the size of the discriminator's receptive fields. In addition, Krebs et al. [33] proposed a probabilistic model for diffeomorphic registration that leverages Conditional Variational Autoencoders.

The current trend in deep learning based medical image registration is moving towards unsupervised learning [5]. The CNN architecture proposed in [2], called RegNet—different from existing work—directly estimates the displacement vector field from a pair of input images; it integrates image content at multiple scales by means of a dual path, allowing for contextual information. Traditional registration methods optimize an objective function independently for each pair of images, which is time-consuming for large-scale datasets. To this end, the differentiable Spatial Transformer Layer (STL) has been introduced that enables CNNs to perform global parametric image alignment without requiring supervised labels [34].

Recently, de Vos et al. [35] proposed a Deep Learning Image Registration (DLIR) framework for unsupervised affine and deformable image registration. This framework consists of a multistage CNN architecture for the coarse-to-fine registration considering multiple levels and image resolutions and achieved comparable performance with respect to conventional image registration while being several orders of magnitude faster. A progressive training method for end-to-end image registration based on a U-Net [36] was devised in [37], which gradually processed from coarse-grained to fine-grained resolution data. The network was

progressively expanded during training by adding higher resolution layers that allowed the network to learn fine-grained deformations from higher-resolution data.

The starting point of the present work was the VoxelMorph framework that was recently introduced for deformable registration of brain Magnetic Resonance Imaging (MRI) images and is considered state-of-the-art [12]. The VoxelMorph framework is fully unsupervised and allows for a clinically feasible real-time solution by registering full 3D volumes in a single-shot. From a research perspective, the framework is flexible to modifications and extensions of the network architecture. VoxelMorph formulates the registration as a parameterized function  $g_{\theta}(\cdot,\cdot)$  learned from a collection of volumes in order to estimate the DVF  $\phi$ . This parameterization  $\boldsymbol{\theta}$  is based on a CNN architecture similar to U-Net [36] which allows for the combination of low- and highresolution features, and is estimated by minimizing a loss function using a training set. The initial VoxelMorph model was evaluated on a dataset of 7829 T1-weighted brain MRI images acquired from eight different public datasets. As extensions of this model, Kim et al. [38] integrated cycle-consistency [39] into VoxelMorph, showing that even image pairs with severe deformations can be registered by improving topology preservation. In addition, the combination of VoxelMorph with FlowNet [40] for motion correction of respiratory-gated Positron Emission Tomography (PET) scans was proposed in [41].

# 3. Materials and methods

# 3.1. Dataset description

The dataset used in this study comprised consecutive CT images of patients with bone metastases originating from primary breast cancer. Breast cancer frequently presents with a mixture of lytic and sclerotic bone metastases, where lytic metastases appear similar to areas of low Hounsfield Unit (HU) attenuation in the bones and sclerotic metastases are more densely calcified than normal bone and have higher HU attenation. Treatment response often causes increasing sclerosis, especially in lytic metastases. However, increasing sclerosis can also be a sign of disease progression, especially in patients with mixed or purely sclerotic metastases at diagnosis, thus causing a diagnostic dilemma [42]. Quantitative assessment of bone metastases and the associated changes in attenuation and bone texture over time thus holds the potential to improve treatment response assessment [9-11]. To enable such assessments, accurate and preferably real-time deformable registration of the consecutive CT images is an important prerequisite.

After informed consent, patients with metastatic breast cancer were recruited into a study designed to characterize the disease at the molecular level, using tissue samples and serial samples of circulating tumor DNA (ctDNA) [43,44]. CT imaging of the chest, abdomen, and pelvis was acquired according to clinical request every 3 – 12 months to assess response to standard-of-care treatment. A subset of 12 patients with bone metastases only were selected, resulting in 88 axial CT images of the abdomen and pelvis. The CT images were acquired using either of two different clinical CT scanner models—the SOMATOM Emotion 16, the SOMATOM Definition AS(+), and the SOMATOM Sensation 16—manufactured by Siemens Healthineers (Erlangen, Germany). The original image size was 512 × 512 pixels with a variable number of slices (median: 302; interquartile range: 35).

On axial images reconstructed with a slice thickness of 2 mm and a pixel spacing ranging from 0.57-0.97 mm using bone window settings, all vertebral bodies of the thoracic and lumbar spine that were depicted completely were segmented semi-automatically by a board certified radiologist with ten years of experience in

clinical imaging, using Microsoft Radiomics (project InnerEye<sup>3</sup>, Microsoft, Redmond, WA, USA). Thus, a series of closely neighboring VOIs was created that spanned the majority of the superior-inferior extent of each scanning volume and was used subsequently to assess the performance of the registration approach. The total number of VOIs delineated for the analyzed dataset was 805 (mean VOIs per scan: 9.15).

# 3.2. Dataset preparation and training set construction

# 3.2.1. Abdominopelvic CT image pre-processing CT table removal

In a manner similar to that of the commonly used data preparation procedure for brain MR images called "skull-stripping" [45], we refined our abdominopelvic CT images to facilitate deformable registration. The CT table could bias the learning process and lead the registration to overfit on the patient table region. Therefore, we developed a fully automatic approach based on region-growing [46] to remove the CT table from the CT images, as well as all extra-corporeal components, such as breast prostheses, clothes and metal objects. Our slice-by-slice approach automatically initialized the growing region,  $\mathcal{R}_G$ , with a 50 × 50-pixel squared seed-region at the center of each slice by assuming that the body was positioned at the center of the CT scanner.

Considering an image I, Eq. (1) defines the homogeneity criterion, P, in terms of the mean value of the region  $\mu_{R_G}$  [46]:

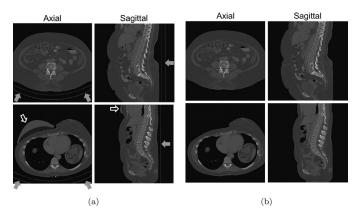
$$\mathsf{P} = \begin{cases} \mathsf{True, if } \; \boldsymbol{p}_{\mathcal{B}} \notin \mathcal{R}_{\mathcal{G}} \wedge |\boldsymbol{I}(\boldsymbol{p}_{\mathcal{B}}) - \mu_{\mathcal{R}_{\mathcal{G}}}| < T_{\mathcal{G}} \\ \mathsf{False, otherwise} \end{cases} \; , \tag{1}$$

where  $\mathbf{p}_{\mathcal{B}} \in \mathcal{B}$  denotes a pixel belonging to the candidate list  $\mathcal{B}$  of the boundary pixels in the growing region  $\mathcal{R}_{G}$ , while  $T_{G}$  is the inclusion threshold. In particular, during the iterations, the 8-neighbors of the current pixel  $\mathbf{p}_{\mathcal{B}}$ , which do not yet belong to  $\mathcal{R}_{G}$ , are included into the candidate list  $\mathcal{B}$ . The similarity criterion,  $\mathsf{P}$ , was based on the absolute difference between the value of the candidate pixels  $\mathbf{I}(\mathbf{p})$  and the mean intensity of the pixels included in  $\mathcal{R}_{G}$  (i.e.,  $\mu_{\mathcal{R}_{G}} = \sum_{\mathbf{q} \in \mathcal{R}_{G}} \mathbf{I}(\mathbf{q})/|\mathcal{R}_{G}|$ . If this difference is lower than  $T_{G}$ , the current pixel  $\mathbf{p}$  under consideration is added to  $\mathcal{R}_{G}$ . The procedure ends when the list  $\mathcal{B}$  is empty. To account for the variability of the different CT scans, the inclusion threshold,  $T_{G}$ , is incrementally increased until  $|\mathcal{R}_{G}|$  reaches a minimum area of 6000 pixels. In more details, the input CT pixel values (expressed in HU) are transformed into the range [0,1] (via a linear mapping) and the value of  $T_{G}$  varies in [0.08,0.4] at 0.02 incremental steps at each iteration. Finally, all automated refinements were carefully verified.

Figure 1 shows two examples of CT table removal. In particular, the sagittal view shows how the CT table was removed along the whole scan (Fig. 1b). In addition, the extra-corporeal parts (i.e., breast prostheses) are discarded in the second example (bottom row).

CT image pre-processing After CT table removal, the following additional data pre-processing steps were performed:

- 1. Affine registration using the NiftyReg toolbox [13] to account for global rotations and translations, as well as differences in the Field-of-View (FOV) between consecutive scans;
- 2. Normalization per scan in [0,1] by means of linear stretching to the 99th percentile:  $\tilde{x}_i = \frac{x_i x_{\min}}{x_{\max} x_{\min}}$  for  $i \in \{x_{\min}, x_{\min} + 1, \dots, x_{\max}\}$ ;
- 3. Downsampling by a factor of 2 with isotropic voxels of 1 mm³, and cropping all volumes to achieve a uniform dimension of  $160 \times 160 \times 256$  voxels. Similar to VoxelMorph [12], isotropic voxel sizes are important to enable accurate deformable registration, which is why most studies resample the volumes.



**Fig. 1.** Two example pairs of input axial and sagittal CT slices from the analyzed dataset: (a) original images; (b) refined images where the CT table and other extracorporeal parts were removed. The CT table and the breast prosthesis are indicated by solid gray and empty white arrows, respectively. Window level and width are set to 400 and 1800 HU, respectively, optimized for spine bone visualization.

With more details, the desired image dimension to which the CT scans were resampled (according to step 3) was determined as follows:

- The resizing factor is computed as:  $f_{\text{resize}} = \text{VoxelSize}_{\text{original}}/\text{VoxelSize}_{\text{desired}}$ , where VoxelSize $_{\text{desired}} = 1 \times 1 \times 1 \text{ mm}^3$  for isotropic voxels.
- The image dimension is determined accordingly:  $ImageDimension_{desired} = 0.5 \cdot ImageDimension_{original} \cdot f_{resize}.$

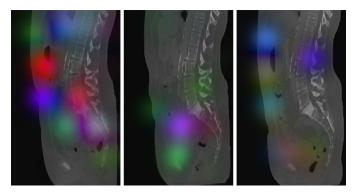
# 3.2.2. Generation of simulated DVFs

It was not possible to directly train a network to register the longitudinal abdominopelvic CT images in our dataset due to the limited amount of available transformation pairs (see Section 3.1), large inter-patient variations, and the often non-diffeomorphic nature of the transformations, e.g., due to the changes in the appearances of normal structures in consecutive CT images caused by bowel peristalsis or bladder filling. Therefore, we developed a simulator that generated random synthetic DVFs and transforms abdominopelvic CT images in a manner similar to that of Sokooti et al. [2] and Eppenhof and Pluim [27]. The resulting deformed CT images can subsequently be used to train or evaluate deep learning based image registration methods.

The synthetic DVF generator randomly selects P initialization points,  $\mathbf{d}_i$  (with  $i = 1, 2, \dots, P$ ), from within the patient volume of a CT image with a minimum distance,  $d_P$ , between these points. In the present study, all DVFs were generated using P = 100 and  $d_P = 40$ . Each point,  $\mathbf{d}_i$ , is composed of three random values between  $-\delta$  and  $\delta$  that correspond to the x, y, and z components of the displacement vector in that point. To ensure that the simulated displacement fields were as realistic as possible, we set  $\delta = 6$  to mimic the typical displacements found between the pre-registered images in our abdominopelvic CT dataset. From clinical radiological experience, displacements in the range between 0 and 50 mm are what would be reasonably expected when a patient is placed on the CT scanner in a consistent way, with identical breathing commands, and with similar FOVs. While -25 mm and +25 mm likely represent the extreme of what might be observed, more conservative displacements in the range of -6 mm and +6 mm are the most common [47]. In addition, we generated a series of DVFs with increasingly large displacements ( $\delta = [0, 1, ..., 25]$ ) for evaluation purposes (see Section 4.2.2).

The resulting vectors were subsequently used to initialize a displacement field,  $\phi_s$ , with the same dimensions as the original CT image. To ensure that the DVF moved neighboring voxels into the

<sup>&</sup>lt;sup>3</sup> https://www.microsoft.com/en-us/research/project/medical-image-analysis/



**Fig. 2.** Randomly selected examples of simulated DVFs (same patient; first three time-points). The displacements—distributed across the whole CT scan in the x, y, and z spatial directions—are encoded by the Red, Green, and Blue (RGB) color channels of an RGB image superimposed on the corresponding sagittal CT image via alpha blending.

same direction, the displacement field was smoothed with a Gaussian kernel with a standard deviation of  $\sigma_s = 0.005$ . Three examples of resulting synthetic DVFs are shown in Fig. 2. Finally, the CT image was transformed using the generated DVF and Gaussian noise with a standard deviation of  $\sigma_n = 0.001$ , which was added to make the transformed CT image more realistic. The resulting deformed CT images had a mean Dice Similarity Coefficient (DSC) of  $0.725 \pm 0.059$ , which corresponded to the initial differences between the real scan pairs in our longitudinal abdominopelvic CT dataset (see Fig. 10). A detailed explanation of DSC can be found in Section 3.4.

# 3.3. Deep learning based deformable image registration

# 3.3.1. The VoxelMorph framework

The VoxelMorph model consists of a CNN that takes a fixed and a moving volume as input, followed by an STL that warps the moving volume using the deformation that is yielded by the CNN (Fig. 3). The model can be trained with any differentiable loss function. Let **F** and **M** be two image volumes defined over an *N*-dimensional spatial domain,  $\Omega \subset \mathbb{R}^N$ . We consider CT images, thus N=3 in our study. More specifically, **F** and **M** were the fixed and moving images, respectively.

Let  $\phi$  be a transformation operator defined by a DVF  ${\bf u}$  that denotes the offset vector from  ${\bf F}$  to  ${\bf M}$  for each voxel:  $\phi={\rm Id}+{\bf u}$ , where Id is the identity transform. We used the following unsupervised loss function:

$$\mathcal{L}(\mathbf{F}, \mathbf{M}; \phi) = \mathcal{L}_{\text{sim}}(\mathbf{F}, \mathbf{M} \circ \phi) + \lambda \mathcal{L}_{\text{smooth}}(\phi), \tag{2}$$

where  $\mathcal{L}_{sim}$  aims to minimize differences in appearance and  $\mathcal{L}_{smooth}$  penalizes the local spatial variations in  $\phi$ , acting as a regularizer weighted by the parameter  $\lambda$ . The employed  $\mathcal{L}_{sim}$  is the local cross-correlation between  $\mathbf{F}$  and  $\mathbf{M} \circ \phi$ , which is more robust to intensity variations found across scans and datasets [48]. Let  $\hat{\mathbf{F}}(\mathbf{p})$  and  $[\hat{\mathbf{M}} \circ \phi](\mathbf{p})$  denote local mean intensity images:  $\hat{\mathbf{F}}(\mathbf{p}) = \frac{1}{\omega^3} \sum_{\mathbf{p}_i \in \mathcal{N}(\mathbf{p})} \mathbf{F}(\mathbf{p}_i)$ , where  $\mathbf{p}_i$  iterates over a local neighborhood,  $\mathcal{N}(\mathbf{p})$ , defining an  $\omega^3$  volume centered on  $\mathbf{p}$ , with  $\omega=9$  in our experiments. The local normalized cross-correlation (NCC) of  $\mathbf{F}$  and  $[\mathbf{M} \circ \phi]$  is defined as:

 $NCC(\mathbf{F}, \mathbf{M} \circ \boldsymbol{\phi})$ 

$$= \sum_{\boldsymbol{p} \in \Omega} \frac{\left(\sum\limits_{\boldsymbol{p}_i \in \mathcal{N}(\boldsymbol{p})} (\boldsymbol{F}(\boldsymbol{p}_i) - \boldsymbol{\hat{F}}(\boldsymbol{p})) ([\boldsymbol{M} \circ \boldsymbol{\phi}](\boldsymbol{p}_i) - [\boldsymbol{\hat{M}} \circ \boldsymbol{\phi}](\boldsymbol{F}))\right)^2}{\left(\sum\limits_{\boldsymbol{p}_i \in \mathcal{N}(\boldsymbol{p})} (\boldsymbol{F}(\boldsymbol{p}_i) - \boldsymbol{\hat{F}}(\boldsymbol{p}))^2\right) \left(\sum\limits_{\boldsymbol{p}_i \in \mathcal{N}(\boldsymbol{p})} ([\boldsymbol{M} \circ \boldsymbol{\phi}](\boldsymbol{p}_i) - [\boldsymbol{\hat{M}} \circ \boldsymbol{\phi}](\boldsymbol{p}))^2\right)}.$$

A higher NCC indicates a better alignment, yielding the loss function:

$$\mathcal{L}_{\text{sim}}(\mathbf{F}, \mathbf{M}; \phi) = -\text{NCC}(\mathbf{F}, \mathbf{M} \circ \phi). \tag{4}$$

Minimizing  $\mathcal{L}_{sim}$  encourages  $\mathbf{M} \circ \boldsymbol{\phi}$  to approximate  $\mathbf{F}$ , but might yield a non-smooth  $\boldsymbol{\phi}$  that is not physically realistic. Thus, a smoother displacement field  $\boldsymbol{\phi}$  is achieved by using a diffusion regularization term on the spatial gradients of displacement  $\mathbf{u}$ :

$$\mathcal{L}_{\text{smooth}}(\phi) = \sum_{\mathbf{p} \in \Omega} ||\nabla \mathbf{u}(\mathbf{p})||^2, \tag{5}$$

and approximate spatial gradients *via* the differences among neighboring voxels.

Figure 3 depicts the CNN used in VoxelMorph, which takes a single input formed by concatenating F and M into a twochannel 3D image. Taking inspiration from U-Net [36], the decoder uses several 32-filter convolutions, each followed by an upsampling layer, to bring the volume back to full-resolution. The gray lines denote the skip connections, which concatenate coarsegrained and fine-grained features. The full-resolution volume is successively refined via several convolutions and the estimated deformation field,  $\phi$ , is applied to the moving image, **M**, via the STL [34]. In our experiments, the input was  $160 \times 160 \times 256 \times 2$  in size. 3D convolutions were applied in both the encoder and decoder paths using a kernel size of 3, and a stride of 2. Each convolution was followed by a Leaky Rectified Linear Unit (ReLU) layer with parameter  $\alpha$ . The convolutional layers captured hierarchical features of the input image pair, used to estimate  $\phi$ . In the encoder, strided convolutions were exploited to halve the spatial dimensions at each layer. Thus, the successive layers of the encoder operated over coarser representations of the input, similar to the image pyramid used in hierarchical image registration approaches.

# 3.3.2. Parameter settings and implementation details

In the present study, the optimized hyperparameter settings suggested by Balakrishnan et al. [12] served as a starting point. We investigated the effect of the LeakyReLU  $\alpha$  parameter on the stability of the training process and found that an  $\alpha$  of 0.5 was optimal for registering abdominopelvic CT images. In all experiments, the regularization parameter,  $\lambda$ , was set to 1.0. One training epoch consisted of 100 steps and took approximately five minutes. The models described in Section 4.1 were trained until convergence (1000 epochs) using a learning rate of  $10 \times 10^{-4}$ , whereas the models described in Section 4.2 were trained using the early stopping monitoring function implemented in the Python programming language using Keras (with a TensorFlow backend) based on 50 validation steps and a patience of 20 epochs. Training was parallelized on four Nvidia GeForce GPX 1080 Ti (Nvidia Corporation, Santa Clara, CA, USA) GPUs (batch size = 4) and evaluation of the trained networks was performed using an Nvidia GeForce GPX 1070 Ti GPU.

# 3.3.3. Incremental training strategy

The VoxelMorph network did not converge when it was naïvely trained on the limited number of abdominopelvic CT scans in the available dataset  $\mathcal{D}$  (only  $76 \times 2 = 152$  possible intra-patient combinations). To overcome this limitation, we developed a novel approach to enforce learning based on simulated deformations (see Section 3.2.2) and incremental learning, rather than basic data augmentation. In our incremental training strategy (Fig. 4), deformed CT images are sequentially presented to the network in chronological mini-batches per patient. Incremental training, compared to naïve data augmentation, enables the network to benefit from the resemblance between consecutive images of a single patient and transfer this knowledge to the next patient by means of physically-driven deformations.

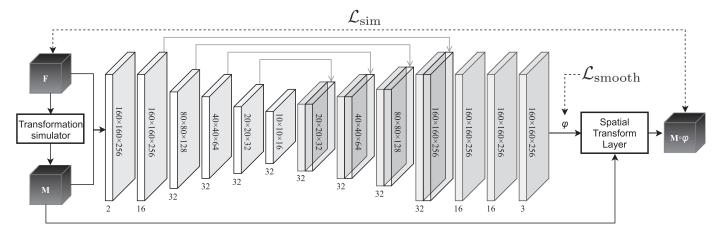


Fig. 3. CNN architecture implementing  $g_{\theta}(\mathbf{F}, \mathbf{M})$  based on VoxelMorph [12]. The spatial resolution of the input 3D volume of each 3D convolutional layer is shown vertically, while the number of feature maps is reported below each layer. The black solid lines denote the operations that involve the input fixed F and moving M volumes, while the black dashed lines represent the arguments of the loss function components  $\mathcal{L}_{sim}$  and  $\mathcal{L}_{smooth}$ .

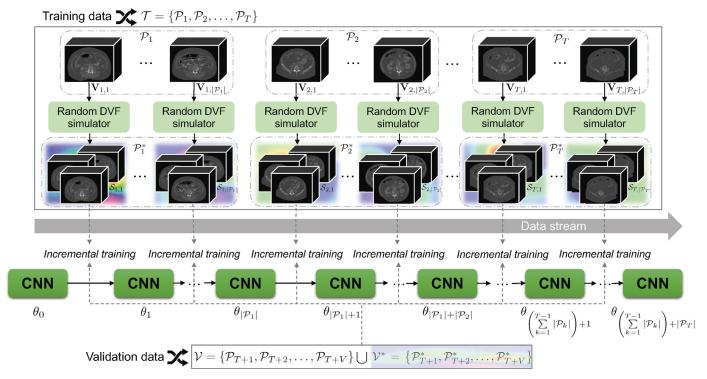


Fig. 4. Workflow of the proposed incremental training strategy:  $\mathcal{T}$  and  $\mathcal{V}$  represent the training and validation sets, respectively. The parameters  $\theta$ , employed in the parameters terized registration functions  $g_{\theta}(\cdot, \cdot)$ , are incrementally learned for each deformed volume included in the training set  $\mathcal{T}$  and tested on the unseen volumes of the validation set  $\mathcal{V}$ . All deformed volumes in  $\mathcal{T}$  and  $\mathcal{V}$  are synthesized using a random DVF simulator. The notation  $\mathbf{V}_{i,j}$  denotes the jth 3D volume for a patient,  $\mathcal{P}_i$  (with  $i \in \{1,2,\ldots D\}$ and D = T + V).

Let  $\mathcal{D} = \{\mathcal{P}_1, \mathcal{P}_2, \dots, \mathcal{P}_D\}$  contain all abdominopelvic CT images for each patient  $\mathcal{P}_i = \left\{ \mathbf{V}_{i,1}, \mathbf{V}_{i,2}, \dots, \mathbf{V}_{i,|\mathcal{P}_i|} \right\}$ , where  $i = 1, 2, \dots, D$ and  $|\mathcal{P}_i|$  denotes the patient index and the corresponding number of CT volumes, respectively. The whole dataset,  $\mathcal{D}$ , was split into two disjoint training,  $\mathcal{T} = \{\mathcal{P}_1, \mathcal{P}_2, \dots, \mathcal{P}_T\}$ , and validation,  $\mathcal{V} = \{\mathcal{P}_1, \mathcal{P}_2, \dots, \mathcal{P}_T\}$  $\{\mathcal{P}_{T+1}, \mathcal{P}_{T+2}, \dots, \mathcal{P}_{T+V}, \}$  sets with T+V=D. In our case, D=12with T = 9 and V = 3. Each volume,  $\mathbf{V}_{i,j}$  (with  $j = 1, 2, ..., |\mathcal{P}_i|$ ), was subsequently deformed using K randomly generated DVFs,  $\phi_k$ (see Section 3.2.2), resulting in  $\mathcal{S}_{i,j} = \left\{ \mathbf{V}_{i,j}^{(k)} \right\}_{k=1,\dots,K}$  deformed volumes for the ith patient, with  $i=1,2,\dots,D$ . The set  $\mathcal{T}^* = \left\{ \mathcal{P}_1^*, \mathcal{P}_2^*, \dots, \mathcal{P}_T^* \right\}$ , with  $\mathcal{P}_i^* = \left\{ \mathcal{S}_{i,1}, \mathcal{S}_{i,2}, \dots, \mathcal{S}_{i,|\mathcal{P}_i|} \right\}$ , was used to incrementally train the network such that in each

training iteration the network was trained on a mini-batch con-

taining all deformed volumes,  $S_{i,j}$ . The deformed volumes in the set  $\mathcal{V}^* = \left\{\mathcal{P}^*_{T+1}, \mathcal{P}^*_{T+2}, \dots, \mathcal{P}^*_{T+V}\right\}$  were randomly divided into two equal, independent parts. One part was kept aside for evaluation, and the other part was used to monitor the training process to avoid concept drift (i.e., changes in the data distribution) between the mini-batches over time. After each training iteration, the network weights that resulted in the best performance on this second part of  $\mathcal{V}^*$  were reloaded to initiate the next iteration. If the network did not converge during a certain iteration, the network weights of the previous iteration were reloaded, thereby ensuring that the overall training process could continue and remain stable. To reduce forgetting, the learning rate was decreased linearly from from  $10^{-4}$  (first iteration) to  $10^{-6}$  (last iteration) [49].

The incremental training strategy was evaluated using a 4-fold cross-validation scheme in which all patients in dataset  $\mathcal{D}$  were randomly shuffled while the order of the distinct time-points was preserved in order to account for the longitudinal nature of our dataset. Since D=12,  $\sum_{i=1,2,\dots,D} |\mathcal{P}_i|=88$ , and K=30, a total of 2640

deformed volumes,  $\mathcal{D}^*$ , were generated in this study, of which 2014 were used for training, 323 for monitoring the training process, and 323 for evaluation in each cross-validation round. It should be noted that patients included in the training set were not included in the corresponding validation and test set, i.e., data of one patient cannot belong to both partitions. Cross-validation allows for a better estimation of the generalization ability of our training strategy compared to a hold-out method in which the dataset is partitioned into only one training and evaluation set.

#### 3.4. Evaluation methodology

This section describes the evaluation metrics used to quantify the registration performance of the incrementally trained Voxel-Morph framework and the NiftyReg toolbox [13] that served as a benchmark in this study.

#### 3.4.1. NiftyReg

All deformed abdominopelvic CT images were also registered using the Fast Free-Form Deformation (F3D) algorithm for nonrigid registration in the NiftyReg toolbox (version 1.5.58) [13]. All options were set to default: the image similarity metric used was Normalized Mutual Information (NMI) with 64 bins and the optimization was performed using a three-level multi-resolution strategy with a maximum number of iterations in the final level of 150. Note that the F3D algorithm in the NiftyReg toolbox does not support GPU acceleration, in contrast to the Block Matching algorithm for global (affine) registration in the NiftyReg toolbox that was used to pre-align the CT images in this study (see Section 3.2.1).

# 3.4.2. Evaluation metrics

To quantify image registration performance, we relied on highly accurate delineations of all vertebral bodies of the thoracic and lumbar spine performed by a board-certified radiologist. The rationale for considering these VOIs to determine registration performance was that they spanned the majority of the scanning volume in the superior-inferior direction and were of clinical relevance because of the underlying study on bone metastases.

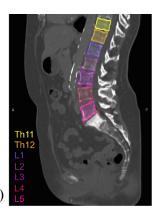
As an evaluation metric, we used the DSC, which is often used in medical image registration [12]. DSC values were calculated using the gold standard regions delineated on the fixed scans  $(\mathcal{R}_{\mathbf{F}})$  and the corresponding transformed regions on the moving scans  $(\mathcal{R}_{\mathbf{M}})$  after application of the estimated DVF  $\phi$ :  $\mathcal{R}_{\mathbf{D}} = \mathcal{R}_{\mathbf{M}} \circ \phi$ (Eq. (6)):

$$\mbox{DSC} = \frac{2 \cdot |\mathcal{R}_{D} \cap \mathcal{R}_{F}|}{|\mathcal{R}_{D}| + |\mathcal{R}_{F}|}. \eqno(6)$$

Since DSC is an overlap-based metric, the higher the value, the better the segmentation results.

For completeness, we also calculated the Structural Similarity Index (SSIM). This metric is commonly used to quantify image quality perceived as variations in structural information [50]. Let X and Y be two images (in our case, F was compared with either M or D for the evaluation), and SSIM combines three relatively independent terms:

- the luminance comparison  $l(\mathbf{X}, \mathbf{Y}) = \frac{2\mu_{\mathbf{X}}\mu_{\mathbf{Y}}+\kappa_{1}}{\mu_{\mathbf{X}}^{2}+\mu_{\mathbf{Y}}^{2}+\kappa_{1}};$  the contrast comparison  $c(\mathbf{X}, \mathbf{Y}) = \frac{2\sigma_{\mathbf{X}}\sigma_{\mathbf{Y}}+\kappa_{2}}{\sigma_{\mathbf{X}}^{2}+\sigma_{\mathbf{Y}}^{2}+\kappa_{2}};$
- the structural comparison  $s(\mathbf{X}, \mathbf{Y}) = \frac{\sigma_{\mathbf{X}}}{\sigma_{\mathbf{Y}}}$



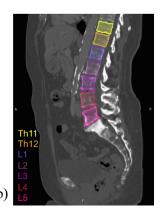


Fig. 5. Sagittal view of two CT images of the same patient: (a) baseline; (b) second time-point. The vertebrae VOIs are displayed using different colors (legend is shown at the bottom-left). Window level and width are set to 400 and 1800 HU, respectively.

where  $\mu_{X}$ ,  $\mu_{Y}$ ,  $\sigma_{X}$ ,  $\sigma_{Y}$ , and  $\sigma_{XY}$  are the local means, standard deviations, and cross-covariance for the images X and Y, while  $\kappa_1, \kappa_2, \kappa_3 \in \mathbb{R}^+$  are regularization constants for luminance, contrast, and structural terms, respectively, exploited to avoid instability in the case of image regions characterized by local mean or standard deviation close to zero. Typically, small non-zero values are employed for these constants; according to Wang et al. [50], an appropriate setting is  $\kappa_1 = (0.01 \cdot L)^2$ ,  $\kappa_2 = (0.03 \cdot L)^2$ ,  $\kappa_3 = \kappa_2/2$ , where L is the dynamic range of the pixel values in F. SSIM is then computed by combining the components described above:

$$SSIM = l(\mathbf{X}, \mathbf{Y})^{\alpha} \cdot c(\mathbf{X}, \mathbf{Y})^{\beta} \cdot s(\mathbf{X}, \mathbf{Y})^{\gamma}, \tag{7}$$

where  $\alpha$ ,  $\beta$ ,  $\gamma > 0$  are weighting exponents. As reported in [50], if  $\alpha = \beta = \gamma = 1$  and  $\kappa_3 = \kappa_2/2$ , the SSIM becomes:

$$SSIM = \frac{(2\mu_{\mathbf{X}}\mu_{\mathbf{Y}} + \kappa_1)(2\sigma_{\mathbf{XY}} + \kappa_2)}{(\mu_{\mathbf{X}}^2 + \mu_{\mathbf{Y}}^2 + \kappa_1)(\sigma_{\mathbf{X}}^2 + \sigma_{\mathbf{Y}}^2 + \kappa_2)}.$$
 (8)

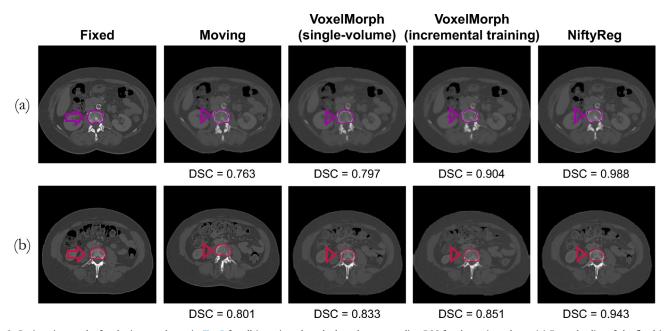
Note that the higher the SSIM value, the higher the structural similarity, implying that the co-registered image, D, and the original image F are quantitatively similar.

#### 4. Experimental results

Figure 5 shows a typical example of two CT images (baseline and second time-point) and VOIs from the same patient from the abdominopelvic CT dataset D. Figure 6a shows an example of deformable registrations achieved using VoxelMorph and NiftyReg in which the moving image was a simulated deformed image (see Section 3.2.2). Similarly, Fig. 6b shows an example of a real registration pair from the longitudinal abdominopelvic CT dataset in which the fixed image was the first time-point (Fig. 5a) and the moving image was the second time-point (Fig. 5b). Interestingly, the improvement achieved by the proposed incremental training procedure with respect to single-volume training can be appreciated in the VoxelMorph registrations in both Fig. 6a and b.

# 4.1. Impact of CT table removal

The effect of the removal of the CT table and extracorporeal structures described in Section 3.2.1 on the image registration performance is shown in Fig. 7. This figure shows the registration performance of a VoxelMorph network trained and tested on original images compared to one trained and tested on refined images in which the CT table and extracorporeal structures were removed. To this end, 250 DVFs with a maximum displacement of 5 mm were



**Fig. 6.** Registration results for the images shown in Fig. 5 for all investigated methods and corresponding DSC for the entire volume. (a) Example slice of the fixed image at the level of the third lumbar vertebra (L3) is shown in the top row on the left and the moving image is a *simulated* deformation of the same volume as used during our incremental training procedure; the right edge of the VOI outlining vertebra L3 shows gradual improvement using different registration methods from left to right (arrowheads) when compared to the fixed image (arrow) corresponding to increasing DSC for the entire volume. (b) A second example slice of a fixed image is shown at the level of the fifth lumbar vertebra (L5) together with a *real* moving image of the same patient, respectively. Again, the right edge of the VOI outlining vertebra L3 shows gradual improvement using different registration methods from left to right (arrowheads) when compared to the fixed image (arrow). Window level and width were set to 400 and 1800 HU, respectively.

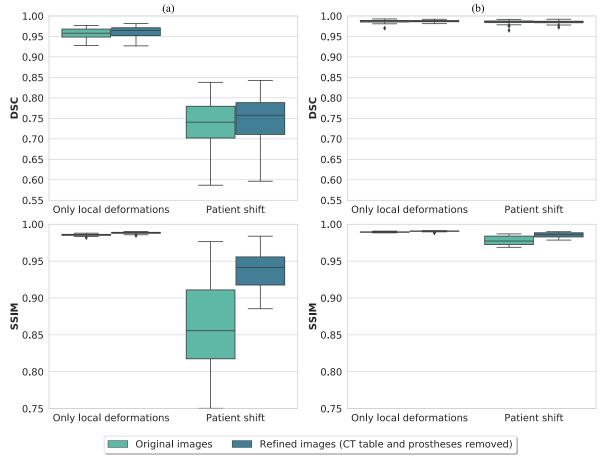


Fig. 7. DSC and SSIM of original and refined CT images registered using: (a) VoxelMorph and (b) NiftyReg.

randomly simulated such that the initialization points were sampled only from within the patient volume, i.e., the CT table was not deformed. These DVFs were used to deform an original CT scan  $(\mathbf{V}_{9,1} \text{ from } \mathcal{P}_9)$  and corresponding refined CT scan, i.e., the CT table, clothing, and prosthesis were removed. An additional test dataset was created by deforming the original and refined CT scan using both local deformations and a random global translation in the x, y, and z directions between -2 mm and 2 mm to simulate a small patient shift with respect to the CT table. Two instances of the VoxelMorph framework were trained on the original and refined datasets, respectively, and tested using 50 held-out deformed CT images without and with additional global patient shift (Fig. 7a). As a benchmark, all original and refined testing CT images were also registered using NiftyReg (Fig. 7b). Statistical analysis was performed using a paired Wilcoxon signed-rank test, with the null hypothesis that the samples came from continuous distributions with equal medians. In all tests, a significance level of 0.05 was set [51].

Figure 7 a shows that the VoxelMorph framework achieved significantly higher DSC values when registering refined CT images compared to original CT images for both local deformations (p < 0.005) and global patient shifts (p < 0.0005). Similarly, the SSIM of the refined images registered using the VoxelMorph framework was higher for both local deformations and global patient shifts (both p < 0.0005). No difference between original and refined CT images was observed in the DSC values of registrations performed using NiftyReg (Fig. 7b), although the SSIM of the refined images registered using NiftyReg showed significant improvements over the original images (both p < 0.0005). Therefore, we can argue that the experiments introducing  $\pm 2$  mm global displacements re-

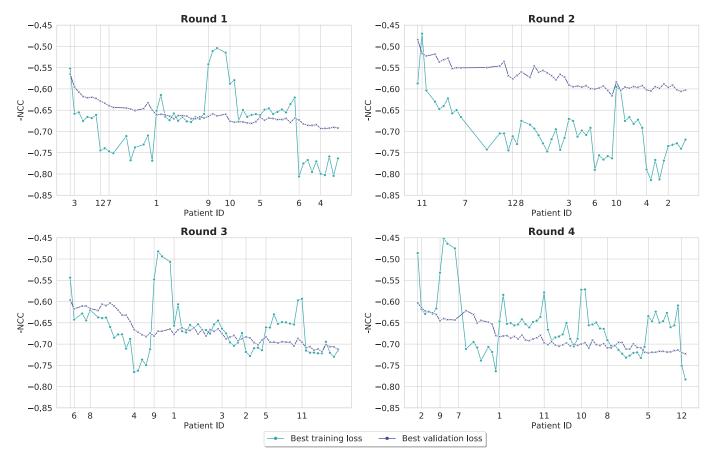
**Table 1** Computational performance of the deformable registration methods in terms of processing times (mean  $\pm$  standard deviation).

Method VoxelMorph	Configuration all registrations	<b>Processing time</b> [s] $0.33 \pm 0.015$
NiftyReg	Local deformations (original CT scans)	$109\pm12$
NiftyReg	Local deformations (refined CT scans)	$105\pm14$
NiftyReg	Local deformations + patient shift (original CT scans)	$106\pm12$
NiftyReg	Local deformations + patient shift (refined CT scans)	105 ± 5

vealed the limitations of VoxelMorph in such a setting. These experiments showed the sensitivity of VoxelMorph to small global misalignments that are not well represented in the training data, and shows that removing the CT table and other extracorporeal structures aids in improving the final outcome in such cases.

# 4.1.1. Computational performance

Table 1 shows the computational times required to register one image pair using the VoxelMorph framework and NiftyReg. The CT table removal procedure resulted in slightly shorter registration times when using the NiftyReg toolbox (on average 105 s) compared to registering original images with and without a patient shift (on average 106 s and 109 s, respectively). The image preprocessing, including CT table removal, was not taken into account



**Fig. 8.** Incremental training process: monitoring the best training and validation image similarity errors (NCC) achieved in each training iteration. The patient IDs represent the randomly initialized order in which the simulated deformed volumes  $S_{i,j} = \left\{ \mathbf{V}_{i,j}^{(k)} \right\}_{k=1,\dots,K}$  (for the jth scan from the ith patient, with  $j=1,2,\dots,|\mathcal{P}_i|$  and  $i=1,2,\dots,D$ ) were used during incremental training in each round.

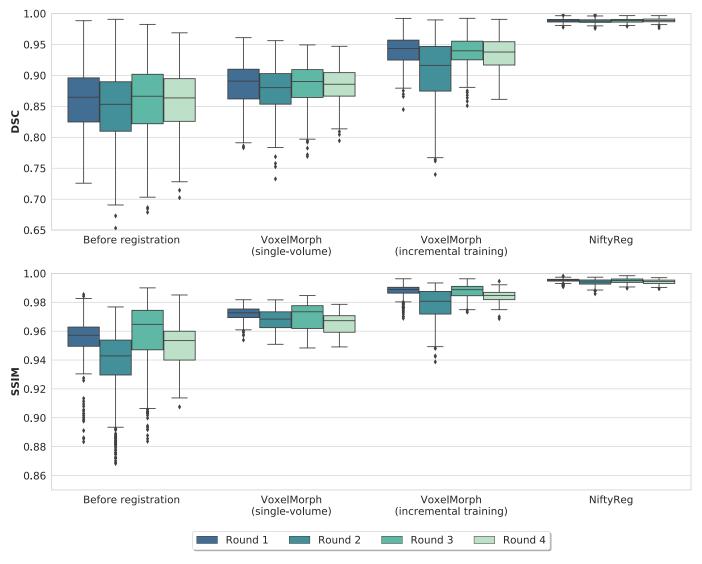


Fig. 9. Registration performance on simulated deformations.

in the computation time since it is independent of the used image registration approach.

# higher (Fig. 8) and the registration performance was lower (see Figs. 9 and 10).

# 4.2. Quantitative evaluation of the incremental training strategy

In the proposed incremental training strategy, a network was trained on all deformed volumes included in a mini-batch  $\mathcal{S}_{i,j}$  until its performance on the validation set  $\mathcal{V}^*$  no longer improved, after which the best performing network weights were reloaded to initiate the next training iteration. Figure 8 shows the resulting best training and validation errors achieved during each training iteration of the different cross-validation rounds. Although the training errors sometimes varied greatly between iterations, the network performance on the validation set,  $\mathcal{V}^*$ , gradually improved during incremental training.

Another interesting phenomenon that can be observed in Fig. 8 is that the best training errors achievable when training on a specific mini-batch tended to differ between patients. For example, training errors increased when training on simulated deformed scans of patients  $\mathcal{P}_5$  or  $\mathcal{P}_9$ . Since both of these patients were, by chance, included in the validation and test sets of round 2, this also explains why the validation errors in round 2 were generally

# 4.2.1. Deformable registration performance

Since the VoxelMorph network did not converge when training on either the whole dataset  $\mathcal{D}$  or on the simulated dataset  $\mathcal{T}^*$ , the effectiveness of the proposed incremental training strategy in learning features from multiple patients was compared to training a network on 1000 simulated deformed scans derived from a single volume ( $\mathbf{V}_{9,1}$  from  $\mathcal{P}_9$ ). All trained networks were subsequently used to register simulated deformed scans from the independent test set back onto their original volumes (Fig. 9). In all cross-validation rounds, the incremental training strategy resulted in better registration performance compared to training on a single volume, with mean DSC values of  $0.929 \pm 0.037$  and 0.883  $\pm$  0.033, and mean SSIM values of 0.984  $\pm$  0.009 and 0.969  $\pm$ 0.007, respectively. The deformable registrations performed using NiftyReg resulted in the best registration results, with a mean DSC of  $0.988 \pm 0.003$  and a mean SSIM of  $0.995 \pm 0.002$ , although it should be noted that this registration method was about 300 times slower than one forward pass through the VoxelMorph framework (Table 1).

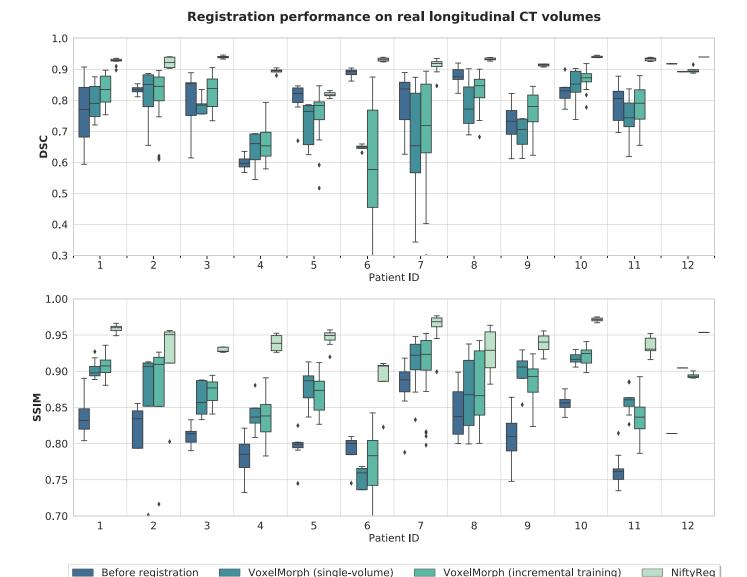


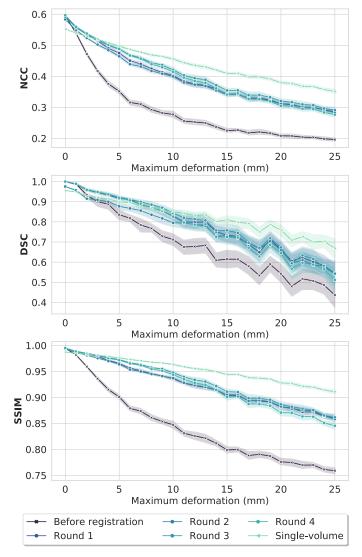
Fig. 10. Registration performance on real longitudinal CT images per patient. The incremental training strategy combined all cross-validation rounds.

To evaluate the impact of the inter- and intra-patient variations on the longitudinal abdominopelvic CT dataset,  $\mathcal{D}$ , on the registration performance, all trained networks were also used to register real scan pairs, i.e., mapping sequential time-points back onto the reference scan (time-point 0). Figure 10 shows the DSC and SSIM values between the real scan pairs before registration, after registration using the VoxelMorph framework trained on single volume or incrementally, and NiftyReg. The differences between the scan pairs before registration greatly varied between patients, with DSC and SSIM values ranging from 0.567 to 0.920 and from 0.693 and 0.918, respectively. Although the VoxelMorph networks were trained using only simulated deformations, the incrementally trained networks improved the DSC between the real scan pairs for 6 out of the 12 patients, whereas the network trained on a single volume improved the DSC for 4 out of the 12 patients (Fig. 10). Furthermore, all VoxelMorph-based models improved the SSIM between the real scan pairs for all patients except patient  $\mathcal{P}_6$ . However, it should be noted that none of the networks trained in this study achieved registration results comparable to NiftyReg.

#### 4.2.2. Large displacements

In addition to variations between patients, mapping large displacements may also form a challenge for deep learning based deformable registration methods. In order to evaluate the effect of the size of the displacements on the registration performance of the networks trained in this study, an additional test set was created by simulating K DVFs  $\phi_k$  ( $k=1,\ldots,K$ ) with maximum displacements ranging from 0 mm (i.e., no deformation) to 25 mm (i.e., structures moving across the entire abdominal and pelvic regions) in steps of 1 mm, with K=30 in each step. These DVFs were used to deform the same volume that was used to generate the training data to train the single-volume network ( $\mathbf{V}_{9,1}$  from  $\mathcal{P}_9$ ), after which the deformed images were mapped back onto the original volume using the trained VoxelMorph networks and NiftyReg.

Figure 11 shows the mean NCC (see Eq. (3)), DSC, and SSIM values for the full range of maximum displacements. The network trained on a single-volume ideally represents the "best possible" (although clinically unrealistic) scenario in which the network was trained and tested on the same volume. This network thus performed better on larger displacements, whereas the incrementally



**Fig. 11.** Registration performance on increasingly large displacements in terms of NCC, DSC, and SSIM.

trained networks performed better for small deformations up to 5 mm.

# 5. Discussion

In recent years, an increasing number of studies have focused on using deep neural networks for deformable image registration because such methods offer fast or nearly real-time registration [2,12,26,27,29,35,37]. However, their application to abdominopelvic CT images remains limited because of the large intra- and inter-patient variations, the not fully diffeomorphic nature of the deformations, and the limited availability of large numbers of well-annotated images for training.

In the present study, we demonstrated that removing extracorporeal structures aids deformable registration of abdominopelvic CT images when using both traditional and deep learning approaches. Along with the registration of multiple CT scans over time, in which the table design and shape may differ and affect the registration process, the devised method based on regiongrowing [46] could also be valuable for multimodal image registration tasks because the scanner table is not visible on MRI and PET [52]. Another practical use case could be radiation treatment-planning, in which the CT table influences the dose distribution

since the table used during imaging typically has different beam attenuation characteristics compared to the treatment table [53].

To address the remaining challenges of our abdominopelvic CT dataset, we generated training data for our network by synthetically deforming the CT images. Such synthetically deformed images can be employed for different purposes: (i) training a neural network for deformable image registration on a relatively small clinical dataset; and (ii) evaluation, e.g., testing the ability of a network to register increasingly large displacements. Synthetic DVFs have already been successfully used for supervised learning of deformable image registration [2,27]. Therefore, a promising direction is to develop more advanced DVF generation strategies and/or synthesize label maps and gray-scale images that expose a network to different anatomical structures and contrasts during training, such as in [54]. As a future development, we plan to introduce an additional penalty term into the loss function of our registration method to exploit the known simulated DVFs during training, which would allow the training process to gradually transition from semi-supervised to unsupervised learning. In addition, we aim to investigate multi- or mixed-scale network architectures [55] for unsupervised medical image registration.

To exploit the longitudinal nature of our abdominal CT dataset and enable training on small amounts of training data, we propose a novel incremental strategy based on simulated deformations. With this incremental training strategy, we managed to overcome the limitations of a well-known unsupervised deep learning framework for deformable image registration (VoxelMorph [12]). Without our novel training strategy it was simply not possible to train any network for deformable registration of our original clinical dataset. However, the performance of our deep learning-based approach was not as good as the non-deep learning-based method (NiftyReg [13]) that was used as a benchmark. Such performance issues that arise when applying deep learning based registration methods to clinically realistic image datasets is a well-established problem in the research community, but remains relatively unaddressed in the scientific literature. We feel that it is very important to highlight the remaining challenges in the field. These advances will facilitate further improvement of deep learning-based image registration algorithms and will eventually enable them to be used for registering more challenging, real clinical datasets with large deformations and variations between patients.

Our results are in agreement with recent literature that suggests that iterative and discrete registration methods are still outperforming deep learning based registration methods in challenging registration tasks in the abdominal area. An example is the recent work by Heinrich [56], who trained a state-of-the-art weakly-supervised deep learning approach called Label-Reg [29] on abdominal CT for inter-patient alignment and achieved an average DSC of only 0.427, which is still substantially worse than NiftyReg with a DSC of 0.561, thus suggesting further research. Importantly, the number of training samples available in our study was indeed small, but we managed to overcome this problem by using simulated deformations, which also has the important advantage of not needing any ground truth displacement fields to train the network in a supervised manner.

In other domains, incremental learning strategies have already shown potential for image classification [57] and medical image segmentation [58], although the so-called catastrophic forgetting [59] still remains a challenge. The incremental training of neural networks for longitudinal image registration could, therefore, benefit from introducing a penalty term into the loss function to balance the registration performance on new images while minimizing forgetting of previous images.

In the long term, parameter-efficient, single-shot deep learning solutions for deformable image registration would enable the development of novel end-to-end approaches, such as task-adapted

image reconstruction [60]. From a clinical perspective, automated registration of longitudinal imaging data is a prerequisite for exploiting the full potential of standard-of-care CT images for treatment response assessment in patients with bone metastases. A successful approach might find potential applications in the most frequently occurring malignancies that have a tendency to metastasize to bone, i.e., prostate, lung, and breast cancer [61].

#### 6. Conclusions

In this work, we proposed a novel incremental training strategy based on simulated deformations to overcome the limitations of a well-known unsupervised deep learning framework for deformable image registration (VoxelMorph), in which we exploited the longitudinal properties of our abdominal CT dataset. Although our deformable image registration method did not outperform the non-deep learning based NiftyReg toolbox in terms of DSC or SSIM, the registrations were approximately 300 times faster. In addition, we demonstrated that removing the CT table and additional extracorporal components allows for better deformable image registration performance using both deep learning and non-deep learning based methods. Future research should focus on developing more advanced DVF simulation, label map or image synthesis techniques, as well as exploring different (semi-supervised) training strategies and investigating multi- or mixed-scale network architectures that are well-suited for registration purposes.

# **Declaration of Competing Interest**

All authors in this paper do not have any conflict of interest.

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#### References

- [1] J.P.W. Pluim, J.B.A. Maintz, M.A. Viergever, Image registration by maximization of combined mutual information and gradient information, IEEE Trans. Med. Imaging 19 (8) (2000) 809–814, doi:10.1109/42.876307.
- [2] H. Sokooti, B. de Vos, F. Berendsen, B.P. Lelieveldt, I. Išgum, M. Staring, Nonrigid image registration using multi-scale 3D convolutional neural networks, in: Proc. International Conference on Medical Image Computing and Computer-Assisted Intervention (MICCAI), Springer, 2017, pp. 232–239, doi:10. 1007/978-3-319-66182-7-27.

- [3] G. Litjens, T. Kooi, B.E. Bejnordi, A.A.A. Setio, F. Ciompi, M. Ghafoorian, J.A. Van Der Laak, B. Van Ginneken, C.I. Sánchez, A survey on deep learning in medical image analysis, Med. Image Anal. 42 (2017) 60–88, doi:10.1109/TMI.2014. 2303821.
- [4] D. Shen, G. Wu, H.-I. Suk, Deep learning in medical image analysis, Annu. Rev. Biomed. Eng. 19 (2017) 221–248, doi:10.1146/annurev-bioeng-071516-044442.
- [5] G. Haskins, U. Kruger, P. Yan, Deep learning in medical image registration: a survey, Mach. Vis. Appl. 31 (1) (2020) 8, doi:10.1007/s00138-020-01060-x.
- [6] C. Han, K. Murao, T. Noguchi, Y. Kawata, F. Uchiyama, L. Rundo, H. Nakayama, S. Satoh, Learning more with less: conditional PGGAN-based data augmentation for brain metastases detection using highly-rough annotation on MR images, in: Proc. ACM International Conference on Information and Knowledge Management (CIKM), 2019, pp. 119–127, doi:10.1145/3357384.3357890.
- [7] Z. Xu, C.P. Lee, M.P. Heinrich, M. Modat, D. Rueckert, S. Ourselin, R.G. Abramson, B.A. Landman, Evaluation of six registration methods for the human abdomen on clinically acquired CT, IEEE Trans. Biomed. Eng. 63 (8) (2016) 1563–1572, doi:10.1109/TBME.2016.2574816.
- [8] M. Freiman, S.D. Voss, S.K. Warfield, Abdominal images non-rigid registration using local-affine diffeomorphic demons, in: Proc. International MICCAI Workshop on Computational and Clinical Challenges in Abdominal Imaging, Springer, 2011, pp. 116–124, doi:10.1007/978-3-642-28557-8\_15.
- [9] T.E. Yankeelov, D.A. Mankoff, L.H. Schwartz, F.S. Lieberman, J.M. Buatti, J.M. Mountz, et al., Quantitative imaging in cancer clinical trials, Clin. Cancer Res. 22 (2) (2016) 284–290, doi:10.1158/1078-0432.CCR-14-3336.
- [10] M.D. Blackledge, D.J. Collins, N. Tunariu, M.R. Orton, A.R. Padhani, M.O. Leach, D.-M. Koh, Assessment of treatment response by total tumor volume and global apparent diffusion coefficient using diffusion-weighted MRI in patients with metastatic bone disease: a feasibility study, PLoS One 9 (4) (2014), doi:10.1371/journal.pone.0091779.
- [11] C. Reischauer, R. Patzwahl, D.-M. Koh, J.M. Froehlich, A. Gutzeit, Texture analysis of apparent diffusion coefficient maps for treatment response assessment in prostate cancer bone metastases a pilot study, Eur. J. Radiol. 101 (2018) 184–190, doi:10.1016/j.ejrad.2018.02.024.
- [12] G. Balakrishnan, A. Zhao, M.R. Sabuncu, J. Guttag, A.V. Dalca, VoxelMorph: a learning framework for deformable medical image registration, IEEE Trans. Med. Imaging (2019), doi:10.1109/TMI.2019.2897538.
- [13] M. Modat, G.R. Ridgway, Z.A. Taylor, M. Lehmann, J. Barnes, D.J. Hawkes, N.C. Fox, S. Ourselin, Fast free-form deformation using graphics processing units, Comput. Methods Programs Biomed. 98 (3) (2010) 278–284, doi:10.1016/ j.cmpb.2009.09.002.
- [14] C.P. Lee, Z. Xu, R.P. Burke, R. Baucom, B.K. Poulose, R.G. Abramson, B.A. Landman, Evaluation of five image registration tools for abdominal CT: pitfalls and opportunities with soft anatomy, in: Medical Imaging 2015: Image Processing, vol. 9413, International Society for Optics and Photonics, 2015, p. 94131N.
- [15] S. Klein, M. Staring, J.P. Pluim, Evaluation of optimization methods for nonrigid medical image registration using mutual information and B-splines, IEEE Trans. Image Process. 16 (12) (2007) 2879–2890, doi:10.1109/TIP.2007.909412.
- [16] J. Bernon, V. Boudousq, J. Rohmer, M. Fourcade, M. Zanca, M. Rossi, D. Mariano-Goulart, A comparative study of Powell's and Downhill Simplex algorithms for a fast multimodal surface matching in brain imaging, Comput. Med. Imaging Graph. 25 (4) (2001) 287–297, doi:10.1016/S0895-6111(00)00073-2.
- [17] J. Thirion, Image matching as a diffusion process: an analogy with Maxwell's demons, Med. Image Anal. 2 (3) (1998) 243–260, doi:10.1016/S1361-8415(98) 80022-4
- [18] T. Vercauteren, X. Pennec, A. Perchant, N. Ayache, Diffeomorphic demons: efficient non-parametric image registration, NeuroImage 45 (1) (2009) S61–S72, doi:10.1016/j.neuroimage.2008.10.040.
- [19] L. Rundo, A. Tangherloni, C. Militello, M.C. Gilardi, G. Mauri, Multimodal medical image registration using particle swarm optimization: a review, in: Proc. Symposium Series on Computational Intelligence (SSCI), IEEE, 2016, pp. 1–8, doi:10.1109/SSCI.2016.7850261.
- [20] S. Klein, M. Staring, K. Murphy, M.A. Viergever, J.P. Pluim, elastix: a toolbox for intensity-based medical image registration, IEEE Trans. Med. Imaging 29 (1) (2009) 196–205, doi:10.1109/TMI.2009.2035616.
- [21] N.J. Tustison, P.A. Cook, A. Klein, G. Song, S.R. Das, J.T. Duda, et al., Large-scale evaluation of ANTs and FreeSurfer cortical thickness measurements, NeuroImage 99 (2014) 166–179, doi:10.1016/j.neuroimage.2014.05.044.
- [22] J. Modersitzki, FAIR: Flexible Algorithms for Image Registration, Vol. 6, Society for Industrial and Applied Mathematics (SIAM), Philadelphia, PA, USA, 2009.
- [23] G. Wu, M. Kim, Q. Wang, Y. Gao, S. Liao, D. Shen, Unsupervised deep feature learning for deformable registration of MR brain images, in: Proc. International Conference on Medical Image Computing and Computer-Assisted Intervention (MICCAI), in: LNCS, vol. 8150, Springer, 2013, pp. 649–656, doi:10.1007/978-3-642-40763-5\_80.
- [24] G. Wu, M. Kim, Q. Wang, B.C. Munsell, D. Shen, Scalable high-performance image registration framework by unsupervised deep feature representations learning, IEEE Trans. Biomed. Eng. 63 (7) (2016) 1505–1516, doi:10.1109/TBME. 2015.2496253.
- [25] X. Cheng, L. Zhang, Y. Zheng, Deep similarity learning for multimodal medical images, Comput. Methods Biomech. Biomed. Eng. Imaging Vis. 6 (3) (2018) 248–252, doi:10.1080/21681163.2015.1135299.
- [26] X. Yang, R. Kwitt, M. Styner, M. Niethammer, Quicksilver: fast predictive image registration—a deep learning approach, NeuroImage 158 (2017) 378–396.
- [27] K.A. Eppenhof, J.P. Pluim, Pulmonary CT registration through supervised learning with convolutional neural networks, IEEE Trans. Med. Imaging 38 (5) (2019) 1097–1105, doi:10.1109/TMI.2018.2878316.

- [28] I.Y. Ha, L. Hansen, M. Wilms, M.P. Heinrich, Geometric deep learning and heatmap prediction for large deformation registration of abdominal and thoracic CT, in: International Conference on Medical Imaging with Deep Learning (MIDL), London, United Kingdom, 2019, pp. 1–5. https://openreview.net/ forum?id=BleGntORtE
- [29] Y. Hu, M. Modat, E. Gibson, W. Li, N. Ghavami, E. Bonmati, G. Wang, S. Bandula, C.M. Moore, M. Emberton, et al., Weakly-supervised convolutional neural networks for multimodal image registration, Med. Image Anal. 49 (2018) 1–13, doi:10.1016/j.media.2018.07.002.
- [30] Y. Hu, E. Gibson, N. Ghavami, E. Bonmati, C.M. Moore, M. Emberton, T. Vercauteren, J.A. Noble, D.C. Barratt, Adversarial deformation regularization for training image registration neural networks, in: Proc. International Conference on Medical Image Computing and Computer-Assisted Intervention (MICCAI), in: LNCS, vol. 11070, Springer, 2018, pp. 774–782, doi:10.1007/ 978-3-030-00928-1 87.
- [31] P. Yan, S. Xu, A.R. Rastinehad, B.J. Wood, Adversarial image registration with application for MR and TRUS image fusion, in: Proc. International Workshop on Machine Learning in Medical Imaging (MLMI), in: LNCS, vol. 11046, Springer, 2018, pp. 197–204, doi:10.1007/978-3-030-00919-9\_23.
- [32] C. Tanner, F. Ozdemir, R. Profanter, V. Vishnevsky, E. Konukoglu, O. Goksel, Generative adversarial networks for MR-CT deformable image registration, arXiv preprint arXiv:1807.07349(2018).
- [33] J. Krebs, H. Delingette, B. Mailhé, N. Ayache, T. Mansi, Learning a probabilistic model for diffeomorphic registration, IEEE Trans. Med. Imaging 38 (2019), doi:10.1109/TMI.2019.2897112.
- [34] M. Jaderberg, K. Simonyan, A. Zisserman, et al., Spatial transformer networks, in: Proc. Advances in Neural Information Processing Systems (NIPS), 2015, pp. 2017–2025.
- [35] B.D. de Vos, F.F. Berendsen, M.A. Viergever, H. Sokooti, M. Staring, I. Išgum, A deep learning framework for unsupervised affine and deformable image registration, Med. Image Anal. 52 (2019) 128–143, doi:10.1016/j.media.2018.11.010.
- [36] O. Ronneberger, P. Fischer, T. Brox, U-Net: convolutional networks for biomedical image segmentation, in: Proc. Conference on Medical Image Computing and Computer-Assisted Intervention (MICCAI), in: LNCS, vol. 9351, Springer, 2015, pp. 234–241, doi:10.1007/978-3-319-24574-4\_28.
- [37] K.A. Eppenhof, M.W. Lafarge, J.P. Pluim, Progressively growing convolutional networks for end-to-end deformable image registration, in: Medical Imaging 2019: Image Processing, vol. 10949, International Society for Optics and Photonics, 2019, p. 109491C, doi:10.1117/12.2512428.
- [38] B. Kim, J. Kim, J.-G. Lee, D.H. Kim, S.H. Park, J.C. Ye, Unsupervised deformable image registration using cycle-consistent CNN, in: Proc. International Conference on Medical Image Computing and Computer-Assisted Intervention (MICCAI), in: LNCS, vol. 11769, Springer, 2019, pp. 166–174, doi:10.1007/978-3-030-32226-7\_19.
- [39] J.-Y. Zhu, T. Park, P. Isola, A.A. Efros, Unpaired image-to-image translation using cycle-consistent adversarial networks, in: Proc. IEEE International Conference on Computer Vision (ICCV), 2017, pp. 2223–2232, doi:10.1109/ICCV.2017.244.
- [40] A. Dosovitskiy, P. Fischer, E. Ilg, P. Hausser, C. Hazirbas, V. Golkov, P. Van Der Smagt, D. Cremers, T. Brox, FlowNet: learning optical flow with convolutional networks, in: Proc. Conference on Computer Vision and Pattern Recognition (CVPR), IEEE, 2015, pp. 2758–2766, doi:10.1109/ICCV.2015.316.
- [41] T. Li, M. Zhang, W. Qi, E. Asma, J. Qi, Motion correction of respiratory-gated PET image using deep learning based image registration framework, in: Proc. 15th International Meeting on Fully Three-Dimensional Image Reconstruction in Radiology and Nuclear Medicine, vol. 11072, International Society for Optics and Photonics, 2019, p. 110720Q, doi:10.1117/12.2534851.
- [42] J.E. Burns, J. Yao, T.S. Wiese, H.E. Muñoz, E.C. Jones, R.M. Summers, Automated detection of sclerotic metastases in the thoracolumbar spine at CT, Radiology 268 (1) (2013) 69–78, doi:10.1148/radiol.13121351.
- [43] F. Mouliere, D. Chandrananda, A.M. Piskorz, E.K. Moore, J. Morris, L.B. Ahlborn, et al., Enhanced detection of circulating tumor DNA by fragment size analysis, Sci. Trans. Med. 10 (466) (2018) eaat4921, doi:10.1126/scitranslmed.aat4921.

- [44] A.B. Gill, L. Rundo, J. Wan, D. Lau, J.P. Zawaideh, R. Woitek, et al., Correlating radiomic features of heterogeneity on CT with circulating tumor DNA in metastatic melanoma, Cancers 12 (12) (2020) 3493, doi:10.3390/cancers12123493.
- [45] O. Gambino, E. Daidone, M. Sciortino, R. Pirrone, E. Ardizzone, Automatic skull stripping in MRI based on morphological filters and fuzzy c-means segmentation, in: Proc. Annual International Conference of the IEEE Engineering in Medicine and Biology Society (EMBS), IEEE, 2011, pp. 5040–5043, doi:10.1109/ IEMBS.2011.6091248.
- [46] L. Rundo, C. Militello, S. Vitabile, C. Casarino, G. Russo, M. Midiri, M.C. Gilardi, Combining split-and-merge and multi-seed region growing algorithms for uterine fibroid segmentation in MRgFUS treatments, Med. Biol. Eng. Comput. 54 (7) (2016) 1071–1084, doi:10.1007/s11517-015-1404-6.
- [47] R. Castillo, E. Castillo, R. Guerra, V.E. Johnson, T. McPhail, A.K. Garg, T. Guerrero, A framework for evaluation of deformable image registration spatial accuracy using large landmark point sets, Phys. Med. Biol. 54 (7) (2009) 1849, doi:10. 1088/0031-9155/54/7/001.
- [48] B.B. Avants, C.L. Epstein, M. Grossman, J.C. Gee, Symmetric diffeomorphic image registration with cross-correlation: evaluating automated labeling of elderly and neurodegenerative brain, Med. Image Anal. 12 (1) (2008) 26–41, doi:10.1016/j.media.2007.06.004.
- [49] P. Goyal, P. Dollár, R. Girshick, P. Noordhuis, L. Wesolowski, A. Kyrola, A. Tulloch, Y. Jia, K. He, Accurate, large minibatch SGD: training ImageNet in 1 hour, arXiv preprint arXiv:1706.02677(2017).
- [50] Z. Wang, A.C. Bovik, H.R. Sheikh, E.P. Simoncelli, Image quality assessment: from error visibility to structural similarity, IEEE Trans. Image Process. 13 (4) (2004) 600–612, doi:10.1109/TIP.2003.819861.
- [51] F. Wilcoxon, Individual comparisons by ranking methods, Biom. Bull. 1 (6) (1992) 196–202, doi:10.2307/3001968.
- [52] Y.-M. Zhu, S.M. Cochoff, R. Sukalac, Automatic patient table removal in CT images, J. Digit. Imaging 25 (4) (2012) 480–485, doi:10.1007/s10278-012-9454-x.
- [53] E. Spezi, A.L. Angelini, F. Romani, A. Guido, F. Bunkheila, M. Ntreta, A. Ferri, Evaluating the influence of the Siemens IGRT carbon fibre tabletop in head and neck IMRT, Radiother. Oncol. 89 (1) (2008) 114–122, doi:10.1016/j.radonc. 2008.06.011.
- [54] M. Hoffmann, B. Billot, J. Eugenio Iglesias, B. Fischl, A.V. Dalca, Learning image registration without images, arXiv preprint arXiv:2004.10282(2020).
- [55] D.M. Pelt, J.A. Sethian, A mixed-scale dense convolutional neural network for image analysis, Proc. Natl. Acad. Sci. 115 (2) (2018) 254–259, doi:10.1073/pnas. 1715832114.
- [56] M.P. Heinrich, Closing the gap between deep and conventional image registration using probabilistic dense displacement networks, in: Proc. International Conference on Medical Image Computing and Computer-Assisted Intervention (MICCAI), Springer, 2019, pp. 50–58, doi:10.1007/978-3-030-32226-7\_6.
- [57] F.M. Castro, M.J. Marín-Jiménez, N. Guil, C. Schmid, K. Alahari, End-to-end incremental learning, in: Proc. European Conference on Computer Vision (ECCV), in: LNCS, vol. 11216, Springer, 2018, pp. 233–248, doi:10.1007/978-3-030-01258-8\_15.
- [58] M. Ben naceur, R. Saouli, M. Akil, R. Kachouri, Fully automatic brain tumor segmentation using end-to-end incremental deep neural networks in MRI images, Comput. Methods Programs Biomed. 166 (2018) 39–49, doi:10.1016/j. cmpb.2018.09.007.
- [59] S.-W. Lee, J.-H. Kim, J. Jun, J.-W. Ha, B.-T. Zhang, Overcoming catastrophic forgetting by incremental moment matching, in: Proc. Advances in Neural Information Processing Systems (NIPS), 2017, pp. 4652–4662.
- [60] J. Adler, S. Lunz, O. Verdier, C.-B. Schönlieb, O. Öktem, Task adapted reconstruction for inverse problems, arXiv preprint arXiv:1809.00948(2018).
- [61] F. Macedo, K. Ladeira, F. Pinho, N. Saraiva, N. Bonito, L. Pinto, F. Gonçalves, Bone metastases: an overview, Oncol. Rev. 11 (1) (2017), doi:10.4081/oncol. 2017.321.