



*Citation for published version:*

Pucknell, S, Kjeldsen, T, Haxton, T, Jeans, J & Young, A 2020, 'Estimating the probable maximum flood in UK catchments using the ReFH model', *Dams and Reservoirs*, vol. 30, no. 3, pp. 85-90.  
<https://doi.org/10.1680/jdare.20.00015>

*DOI:*

[10.1680/jdare.20.00015](https://doi.org/10.1680/jdare.20.00015)

*Publication date:*

2020

*Document Version*

Peer reviewed version

[Link to publication](#)

The final publication is available at ICE publishing via <https://doi.org/10.1680/jdare.20.00015>

## University of Bath

### Alternative formats

If you require this document in an alternative format, please contact:  
[openaccess@bath.ac.uk](mailto:openaccess@bath.ac.uk)

#### General rights

Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

#### Take down policy

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

## **Estimating the probable maximum flood in UK catchments using the ReFH model**

Date revised: 15/06/2020

### Authors:

Samuel Pucknell BEng<sup>1</sup>

Thomas Rodding Kjeldsen MSc, PhD<sup>1</sup>

Tracey Haxton BSc, MSc, C.WEM, MCIWEM<sup>2</sup>

Jude Jeans C.WEM, MCIWEM, PIEMA<sup>2</sup>

Andrew R. Young BSc (Jt. Hons), MSc, PhD<sup>2</sup>

<sup>1</sup>Department of Architecture and Civil Engineering, University of Bath, BA2 7AY

<sup>2</sup>Wallingford HydroSolutions, Wallingford, OX10 8BB

Corresponding author: Thomas Kjeldsen

Email: trk23@bath.ac.uk

### Document statistics:

Number of words: 2702

Number of figures: 2

Number of tables: 4

## Abstract

This paper presents a first attempt at formulating a complete framework for estimating the probable maximum flood (PMF) in UK catchments using the Revitalised Flood Hydrograph (ReFH) model. The framework translates most of the guidelines developed for the FSR/FEH rainfall-runoff model, but a new method for estimating initial soil moisture in line with the ReFH loss model is proposed. The framework has been tested using both ReFH 2.2 and ReFH 2.3 against previously published PMF results for 15 reservoir catchments and found to provide comparable and credible results.

## Key words

Dams, barrages & reservoirs. Floods & floodworks. Hydrology & water resource.

## List of symbols

Symbol	Meaning	Units
$C_{ini}$	Initial soil moisture depth	mm
$C_{max}$	Maximum soil moisture depth	mm
CWI	Catchment wetness index	mm
$DPR_{CWI}$	Dynamic percentage runoff dependent on CWI	%
$DPR_{RAIN}$	Dynamic percentage runoff dependent on P	%
P	Total design storm depth	mm
PMP	Total depth of a design PMP storm	mm
PR	Percentage runoff	%
SPR	Standard percentage runoff	%
$\Delta PR$	Absolute difference in percentage runoff	%

## 1 Introduction

2 Estimation of the probable maximum flood (PMF) is an important part of reservoir safety  
3 considerations in the United Kingdom for category A dams, where a breach could endanger lives in a  
4 downstream community (ICE, 2015). The current guidelines for estimating PMF, as detailed in the  
5 fourth edition of the Floods and Reservoir Safety publication (ICE, 2015) stipulate that estimates of  
6 PMF should be derived as outlined in Volume 4 of the Flood Estimation Handbook (Institute of  
7 Hydrology, 1999) using the FSR/FEH rainfall-runoff model combined with estimates of the probable  
8 maximum flood (PMP) published as part of the Flood Studies Report (NERC, 1975).

9 The FSR/FEH rainfall-runoff model is an event-based model converting a rainfall event (observed or  
10 design event) into a corresponding flood hydrograph. The model was first published as part of the  
11 Flood Studies Report (NERC, 1975) and later revised as part of the Flood Estimation Handbook (IH,  
[https://computingservices-my.sharepoint.com/personal/trk23\\_bath\\_ac\\_uk/Documents/Pucknell\\_et\\_al\\_06February2020\\_REV\\_01.docx](https://computingservices-my.sharepoint.com/personal/trk23_bath_ac_uk/Documents/Pucknell_et_al_06February2020_REV_01.docx))

12 1999) to be compatible with electronic catchment descriptors and a revised design rainfall model.  
 13 While the model is still recommended for use in reservoir safety, it has effectively been replaced by  
 14 the Revitalised FSR/FEH rainfall-runoff model (ReFH) for use in most fluvial design flood estimation  
 15 studies. The first release of the ReFH model was limited to estimating events with a return period up  
 16 to 150 years (Kjeldsen 2007). An updated version of the model was proposed by Kjeldsen et al.  
 17 (2013) mainly considering the effects of urban development, and Wallingford HydroSolutions (2017)  
 18 released an updated version of the model, ReFH2, compatible with the FEH13 Depth-Duration-  
 19 Frequency rainfall model (Stewart et al., 2013) enabling simulation of design events up to a return  
 20 period of 1000 years. While design events with return periods between 100-1000 years are  
 21 routinely used in management of fluvial flood risk, they are still far below the requirements of  
 22 10,000 year events and PMF events required for reservoir safety considerations. Simulation of  
 23 design events up to a return period of 10,000 years was enabled within the ReFH2.3 software,  
 24 released in November 2019. Pether and Fraser (2019) highlighted the complexity of the current  
 25 guidelines for design flood estimation for reservoir safety in the UK, involving different methods for  
 26 different return period. MacDonald and Scott (2000) critiqued the use of the FSR/FEH model for use  
 27 in design flood estimation for reservoir safety, and Faulkner and Benn (2016) suggested that a move  
 28 from the FSR/FEH methodology to ReFH might be warranted, but noted that ReFH was designed for  
 29 smaller events and that further research into the applicability for modelling PMF events is required.  
 30 In the light of this discussion, the aim of the current study is to investigate how best to combine the  
 31 ReFH model with PMP rainfall events to generate credible estimates of PMF, and to investigate the  
 32 sensitivity of the resulting PMF estimates to change in key input parameters.

33

#### 34 **The FSR/FEH model**

35 The FSR/FEH model is described in detail by Houghton-Carr (1999) and consists of three  
 36 components: a loss model, a routing model and a baseflow model. The purpose of the loss model is  
 37 to calculate the fraction of the total rainfall volume that is transformed into direct runoff;  
 38 percentage runoff (PR). To simulate a design flood event for a given return period, the loss model  
 39 calculates PR as a combination of a static and two dynamic terms as

$$\begin{aligned}
 PR &= SPR + DPR_{CWI} + DPR_{RAIN} \\
 DPR_{CWI} &= 0.25(CWI - 125) \\
 DPR_{RAIN} &= \begin{cases} 0 & P \leq 40mm \\ 0.45(P - 40)^{0.7} & P > 40 \end{cases}
 \end{aligned}
 \tag{1}$$

40 where  $SPR$  is the static standard percentage runoff (%) often obtained from the SPRHOST  
41 catchment descriptor,  $DPR_{CWI}$  is the dynamic effect from antecedent soil moisture as measured by  
42 the catchment wetness index (CWI), and  $DPR_{RAIN}$  is the dynamic effect from the rainfall magnitude,  
43 depending on the total rainfall volume  $P$ .

44 When simulating a PMF event, the probable maximum precipitation (PMP) event is combined with a  
45 revised version value of  $CWI$  used based on the estimated maximum antecedent rainfall as  
46 described by Houghton-Carr (1999).

47

#### 48 **The ReFH model**

49 The initial ReFH model was developed by Kjeldsen et al. (2005). The model consists of a loss-model,  
50 a routing model and a baseflow model, mirroring the structure of the FSR/FEH rainfall-runoff model.  
51 Development of the ReFH model was motivated by shortcomings of the FSR/FEH model and  
52 benefitted from updates in hydrological modelling methodology and a more comprehensive  
53 database of observed flood events for model calibration. A comprehensive description of the ReFH  
54 model and subsequent updates is provided by Kjeldsen (2007) and Wallingford HydroSolutions  
55 (2019).

56 The most substantial change between ReFH and the original FSR/FEH model is the introduction of a  
57 new loss model concept, which has implications for PMF estimation. The purpose of the loss model  
58 is to estimate the percentage of the total rainfall that is transformed into direct runoff, i.e.  
59 percentage runoff. The ReFH loss model has one parameter,  $C_{max}$  which provides a conceptual  
60 realisation of the maximum soil moisture depth and one boundary condition, the initial soil moisture  
61 depth,  $C_{ini}$ . While  $C_{max}$  stays constant,  $C_{ini}$  is a dynamic boundary condition that can vary between  
62 events. The percentage runoff is calculated as a function of  $C_{max}$ , rainfall depth  $P$  (mm) and  $C_{ini}$  as

$$PR = \frac{C_{ini}}{C_{max}} + \frac{P}{2C_{max}} \quad (2)$$

63 The first term on the right-hand side is a measure of the initial soil moisture while the second  
64 represent the dynamic rainfall effects. Thus, the ReFH model represent the same fundamental  
65 dynamics as the FSR/FEH loss model, relating PR to antecedent soil moisture and rainfall volume.  
66 The model parameter  $C_{max}$  can be estimated either from analysis of observed flood events or via a  
67 regression model linking model parameters to catchment descriptors. Unlike the FSR/FEH model,  
68 the losses in the ReFH model are calculated for each time step of the simulation to account for the  
69 wetting-up of the soil moisture during the flood event.

70

71 **Estimating the Probable maximum flood**

72 The FSR/FEH procedures for estimating PMF requires key input variables to be adjusted to represent  
73 “*ultra conservative assumptions*” (NERC, 1975) reflecting the seriousness of reservoir safety  
74 considerations. Estimation of PMF events using the ReFH model therefore needs to translate these  
75 considerations into equivalent adjustments of ReFH input variables. The following five input  
76 variables are explicitly considered: probable maximum precipitation event, frozen ground, snow  
77 melt, antecedent soil moisture, and reduction in catchment response time. A summary of how the  
78 input factors are considered in the FSR/FEH model and the proposed changes in ReFH are listed in  
79 Table 1.

80

81 Table 1: Guidelines for PMF estimation for the FSR/FEH model and proposed guidelines for the ReFH  
82 model.

Input variable	FSR/FEH	ReFH
Probable maximum precipitation event	Use FSR methodology	Use FSR methodology
Snow melt	42 mm/day	42 mm/day
Reduction in catchment response time	Reduce Time-to-peak by 33%	Reduce Time-to-peak by 33%
Frozen ground	A minimum <i>SPR</i> value of 53%	A minimum PR value of 53%
Antecedent soil moisture	Increase <i>CWI</i>	Increase $C_{ini}$

83

84 It is proposed that no changes are made to the actual PMP design rainfall event and that the snow-  
85 melt ratio of 42 mm/day are both maintained. Similarly, the 33% reduction in Time-to-peak ( $T_p$ ) is  
86 maintained for the ReFH model. Note that a minimum value of  $T_p$  of 1hr is recommended in the  
87 ReFH model for the rural compartment of a catchment, and lower values should be used with  
88 caution. For the urban compartment of a catchment  $T_p$  is scaled by a factor that is less than unity to  
89 represent the enhanced routing of runoff within urban areas. Thus,  $T_p$  in the urban compartment  
90 can be less than 1 (Wallingford HydroSolutions, 2019).

91 Translation of elevated antecedent soil moisture and frozen ground adjustments from the FSR/FEH  
92 model to ReFH are less straight-forward, as the ReFH model is based on a conceptual hydrological

93 model rather than a direct representation of percentage runoff. The FSR suggested accounting for  
94 frozen ground conditions by assuming all soils across the catchment could be categorised WRAP  
95 class 5, i.e. the most impermeable class of soils in the FSR methodology. For the FSR/FEH method  
96 this was translated into a minimum value of  $SPR$  of 53%. While this mostly will result in actual  $PR$   
97 values in excess of 53%, a minimum  $PR$  value of 53% was imposed on the ReFH model. Further  
98 research into representation of frozen soils in the ReFH model is clearly needed.

99 In both the FSR/FEH and the ReFH models, percentage runoff is determined by the antecedent soil  
100 moisture and total rainfall. In this study the necessary upward adjustment of the initial soil moisture  
101 of the ReFH model was estimated by first considering the absolute difference (increase)  $\Delta PR$   
102 between the percentage runoff as derived for a T-year event and for the PMF when using the  
103 FSR/FEH method (eq. 1) combined with the PMP event. This difference represents the effect of the  
104 frozen ground adjustment and increased catchment wetness (CWI) when simulating the PMF event.  
105 Next, the absolute difference in percentage runoff  $\Delta PR$  is added directly to the percentage runoff  
106 derived from the ReFH model (Eq. 2). Finally, the corresponding value of  $C_{ini}$  (denoted  $C_{ini}^{PMF}$ ) is  
107 calculated by re-arranging the ReFH loss model as

$$C_{ini}^{PMF} = (PR_{ReFH} + \Delta PR)C_{max} - \frac{1}{2}PMP \quad (3)$$

108 where PMP is the total depth of the PMP event. The procedure outlined above will occasionally  
109 result in adjusted values of  $C_{ini}^{PMF}$  that cause estimates of percentage runoff in excess of 100%. This  
110 is clearly untenable and in such cases the percentage runoff was capped at 100%.

111

## 112 **Case study**

113 The Institute of Hydrology Report 114 (IH 114) by Reed and Field (1992) provided estimates of PMF  
114 for 15 reservoir catchment, evenly distributed across upland areas of the UK. A summary of the  
115 catchments is provided in Table 2, including key catchment descriptors such as catchment area,  
116 standard annual average rainfall (1960-1990), and BFIHOST extracted from the FEH Service (CEH,  
117 2018). Note that the IH114 study was conducted before the availability of digital FEH catchment  
118 descriptors, and therefore the catchment areas originally published in IH114 differs slightly from the  
119 areas reported in Table 1 but are within 8% (apart from one catchment) which is considered a  
120 reasonable deviation. For each catchment Reed and Field (1992) estimated PMF both including and

121 excluding reservoir effects. In this study the comparison is based on the PMF excluding reservoir  
 122 effects.

123 Table 2: Details of 15 reservoired catchments from Reed and Field (1992)

Catchment	Area (km <sup>2</sup> )	SAAR (mm)	BFIHOST	Region
Loch Craisg	0.74	1156	0.3660	Scotland
Little Denny	0.98	1247	0.5110	Scotland
Loch Gleann	1.21	1763	0.3760	Scotland
Parkhill House	1.21	780	0.7210	Scotland
Leperstone	1.22	1517	0.6090	Scotland
Higher Naden	3.9	1479	0.4080	England
Lower Carriston	3.94	808	0.5890	Scotland
Nanpantan	4.28	717	0.3510	England
Upper Neuadd	5.74	2243	0.3220	Wales
Crafnant	6.2	2142	0.4190	Wales
Usk	13.5	1694	0.3700	Wales
Colt Crag	18.05	784	0.2910	England
Loch Kirbister	20.73	1068	0.4690	Scotland
Staunton Harold	26.3	671	0.5070	England
Roadford	34.69	1146	0.4160	England

124

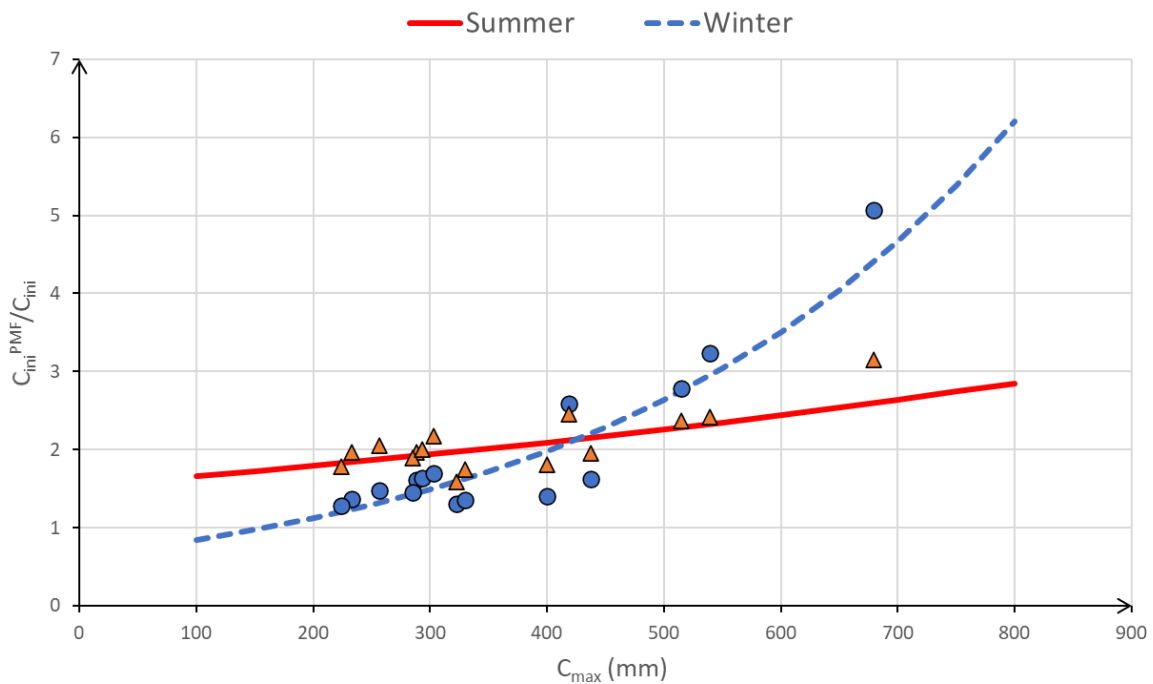
125 For each of the 15 catchments, the ReFH model parameters were estimated based on the extracted  
 126 catchment descriptors (Table 2) and the PMP design rainfall events developed according to the  
 127 procedures outlined in the FEH Volume 4. Both the summer and winter PMP were calculated for  
 128 each catchment. Snowmelt contribution was added to the winter PMP design rainfall events.

129 The four parameters for the ReFH2 model were estimated using the catchment descriptor  
 130 equations. The estimated value of  $Tp$  was reduced by 33% in accordance with the PMF guidelines  
 131 (Table 1), noticing a minimum value of 1hr.

132 Next, the initial soil moisture  $C_{ini}^{PMF}$  required by the ReFH model for simulating the PMF is estimated  
 133 for each catchment using the procedure outlined above. For each catchment the difference  $\Delta PR$  is  
 134 calculated representing the difference between the values of  $PR$  when using the FSR/FEH loss model  
 135 for PMF calculation and return period calculations. Figure 1 shows the ratio between the adjusted  
 136 ( $C_{ini}^{PMF}$ ) and the initial (default) values of  $C_{ini}$  (derived from catchment descriptors) for each of the 15



137 catchment for both summer and winter events plotted against  $C_{max}$  as estimated from catchment  
 138 descriptors.



139  
 140 Figure 1: Observed and predicted values of  $C_{ini}^{PMF} / C_{ini}$  plotted as a function of  $C_{max}$  for 15  
 141 catchments (summer and winter).

142 To enable prediction of the ratio  $C_{ini}^{PMF} / C_{ini}$  for any given catchment, a general relationship between  
 143 the ratio and  $C_{max}$  is proposed in the form of an exponential function for both the summer and  
 144 winter observations as

$$C_{ini}^{PMF} / C_{ini} = a \times \exp\left(b \frac{C_{max}}{1000}\right) \quad (4)$$

145 The two parameters  $a$  and  $b$  are estimated using the method of least squares for both the summer  
 146 and winter season. The outlier on the right-hand side of Figure 1, *Parkhill House*, has a higher value  
 147 of  $C_{max}$  than the bulk of the catchments, representing the high value of BFIHOST. Separate sets of  
 148 regression models were estimated with and without including this catchment, and the resulting  
 149 parameters are summarised in Table 3.

150

151

152 Table 3: Model parameters for Eq. (4) estimated

	Summer		Winter	
	<i>a</i>	<i>b</i>	<i>a</i>	<i>b</i>
Incl. outlier	1.3695	1.1166	0.5522	3.2205
Excl. outlier	1.5368	0.7717	0.6339	2.8515

153

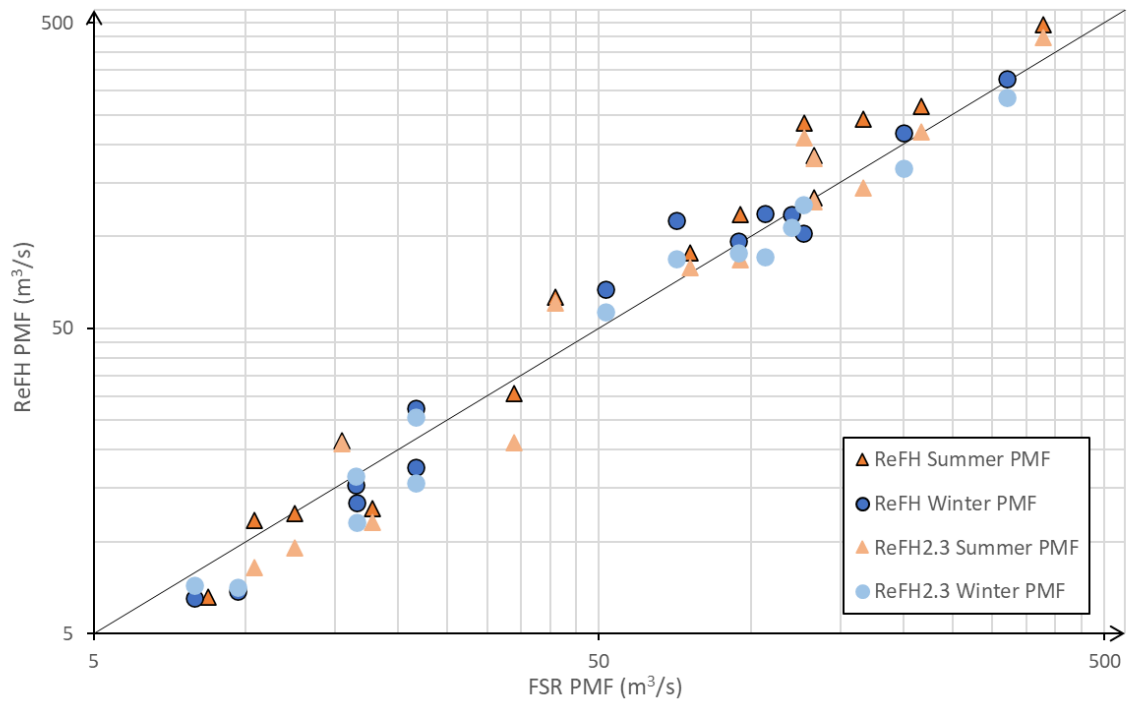
154 Using the set of model parameters derived without considering the data from the outlier yields a  
155 less step curve as  $C_{max}$  increases. This relationship is considered more cautious for use in  
156 extrapolations beyond the calibration range, and is therefore taken forward in the rest of this study.

157 Finally, the summer and winter PMF events are simulated using the ReFH model with PMP design  
158 rainfall events and the adjusted  $C_{ini}$  values. For each catchment the peak flow values of both the  
159 summer and winter PMF were extracted. A summary of the PMF peak flow events obtained from  
160 the adjusted ReFH model as well as the PMF estimates obtained for the same catchments by Reed  
161 and Field (1992) are shown in Table 4 and on Figure 2. The methodology has been developed and  
162 tested using the ReFH2.2 model and repeated using the ReFH2.3 model, which was released in  
163 November 2019. The PMF values derived using the ReFH2.3 model are also presented in Figure 2,  
164 which illustrates that the results are very similar to those derived using both ReFH2.2 and ReFH2.3.

165

166

### FSR PMF vs ReFH PMF



167

168 Figure 2: Comparison of PMF as estimated by the ReFH2 model (y-axis) and the FSR/FEH method (x-  
169 axis) for both summer (triangle) and winter (circle) events. ReFH2.3 results are presented for  
170 comparison.

171

172

173 Table 4: Estimates of summer and winter PMF obtained from the ReFH2.2 and the FSR/FEH models  
174 for all 15 test catchments

Catchment	ReFH2 PMF (m <sup>3</sup> /s)	ReFH2 PMF Season	Summer event as % of PMF	Winter event as % of PMF	FSR PMF (m <sup>3</sup> /s)	FSR PMF Season
Loch Craisg	11.8	S	100	56	10.4	S
Little Denny	12.4	S	100	56	12.5	S
Loch Gleann	21.4	S	100	72	15.51	W
Parkhill House	6.6	S	100	65	8.4	S
Leperstone	13.4	W	96	100	17.8	S
Higher Naden	88.2	S	100	76	75.6	S
Lower Carriston	30.7	S	100	57	33.9	S
Nanpantan	63.5	S	100	43	40.9	S
Upper Neuadd	133.4	S	100	88	133.3	S
Crafnant	117.9	S	100	82	95.1	S
Usk	267.2	S	100	82	217.4	S
Colt Crag	234.7	S	100	48	127.2	S
Loch Kirbister	184.8	S	100	55	133.2	S
Staunton Harold	242.4	S	100	49	166.4	S
Roadford	493.6	S	100	67	377.8	S

175

176 Figure 2 shows a direct comparison of final estimates of both summer and winter PMF from the FSR  
177 and ReFH model. In general, there is a good agreement between PMF estimates obtained by the  
178 two methods.

179

## 180 Discussion

181 The estimation of the probable maximum flood is a challenging problem as it requires numerous  
182 assumptions to be made concerning the flood producing mechanisms which cannot easily be  
183 validated against observed flood events. The procedures proposed in this paper should not be  
184 viewed as an authoritarian guide to estimation of PMF using the ReFH model. Rather, they  
185 constitute a first attempt at formulating and testing a new framework allowing the ReFH model to  
186 be used for PMF estimation, and that the resulting estimates are compatible with the existing  
187 methods. The results demonstrate that it is credible to finally move away from the FSR/FEH model  
188 for reservoir risk assessment towards adopting the ReFH model. Such a move would unify the  
189 design flood estimation methods in the UK within a common framework, and also allow the  
190 reservoir safety flood modelling to benefit from methodological developments made since the

191 inception of the FSR model more than 50 years ago. The initial work was undertaken using ReFH 2.2  
192 but initial tests using the more recent ReFH 2.3 model have confirmed the consistency of the  
193 method.

194

## 195 **References**

196 Faulkner, D. and Benn, J. (2016) Reservoir flood estimation: Time for a re-think. *In Dams–Benefits*  
197 *and Disbenefits; Assets or Liabilities?* Proceedings of the 19th Biennial Conference of the British Dam  
198 Society held at Lancaster University from 7–10 September 2016 (pp. 87-100). ICE Publishing.

199 Kjeldsen, T.R. (2007) The revitalised FSR/FEH rainfall-runoff method. *Flood Estimation Handbook*  
200 *Supplementary Report No. 1*, Centre for Ecology & Hydrology, Wallingford.

201 Kjeldsen, T.R., Miller, J.D. and Packman, J.C., 2013. Modelling design flood hydrographs in  
202 catchments with mixed urban and rural land cover. *Hydrology Research*, 44(6), pp.1040-1057.

203 Kjeldsen, T.R., Stewart, E.J., Packman, J.C., Folwell, S.S. and Bayliss, A.C. (2005) Revitalisation of the  
204 FSR/FEH rainfall-runoff method. *Final Report to DEFRA/EA project FD1913*.

205 Institution of Civil Engineers (2015) *Floods and Reservoir Safety*, 4<sup>th</sup> Edition, ICE Publishing, London,  
206 71 pages.

207 Natural Environment Research Council (1975) *Flood Studies Report*, 5 Volumes, London.

208 Pether, R. and Fraser, R. (2019) A quick reference table for extreme flood hydrology methods in at  
209 UK dams. *Dams and Reservoirs*, 29(1), 41-42.

210 Reed, D.W. and Field, E.K. (1992) Reservoir flood estimation: another look. *Institute of Hydrology*  
211 *Report 114*, Institute of Hydrology, Wallingford.

212 Stewart E.J., Jones D.A., Svensson C., Morris D.G., Dempsey P., Dent, J.E., Collier C.G. and Anderson  
213 C.W. 2013. Reservoir Safety – Long return period rainfall. R&D Technical Report WS 194/2/39/TR  
214 (two volumes), *Joint Defra/EA Flood and Coastal Erosion Risk Management R&D Programme*.

215 Wallingford HydroSolutions. (2019) ReFH2 Technical Guide <https://refhdocs.hydrosolutions.co.uk>

216