1 **The need for high-quality oocyte mitochondria at extreme ploidy dictates**

2 **mammalian germline development**

3

4 **Authors**: Marco Colnaghi[1,2], Andrew Pomiankowski[1,2*] & Nick Lane[1,2*]

5

6 **ORCID**

7 0000-0002-5641-9324 (MC)

8 0000-0002-5171-8755 (AP)

9 0000-0002-5433-3973 (NL)

10

11 **Affiliations**:

12 [1]CoMPLEX and [2]Department of Genetics, Evolution and Environment

13 University College London

14 Darwin Building, Gower Street, London WC1E 6BT

15

16 * **Corresponding author**: Andrew Pomiankowski (ucbhpom@ucl.ac.uk)

17

18 One sentence summary (30 words max):

19 Selective transfer of mitochondria in the Balbiani body ensures high-quality oocyte

20 mitochondria at extreme ploidy, explaining many enigmatic features of female germline

21 architecture including germ cell loss.

22

23

24   **ABSTRACT**

25   Selection against deleterious mitochondrial mutations is facilitated by germline processes,

26   lowering the risk of genetic diseases. How selection works is disputed: experimental data

27   are conflicting and previous modelling work has not clarified the issues. Here we develop

28   computational and evolutionary models that compare the outcome of selection at the level

29   of individuals, cells and mitochondria. Using realistic *de novo* mutation rates and germline

30   development parameters from mouse and humans, the evolutionary model predicts the

31   observed prevalence of mitochondrial mutations and diseases in human populations. We

32   show the importance of organelle-level selection, seen in the selective pooling of

33   mitochondria into the Balbiani body, in achieving high-quality mitochondria at extreme

34   ploidy in mature oocytes. Alternative mechanisms debated in the literature, bottlenecks and

35   follicular atresia, are unlikely to account for the clinical data, because neither process

36   effectively eliminates mitochondrial mutations under realistic conditions. Our findings

37   explain the major features of female germline architecture, notably the longstanding

38   paradox of over-proliferation of primordial germ cells followed by massive loss. The near-

39   universality of these processes across animal taxa makes sense in light of the need to

40   maintain mitochondrial quality at extreme ploidy in mature oocytes, in the absence of sex

41   and recombination.

42

43   **Keywords:** Balbiani body, bottleneck, germline, mitochondria, mitochondrial mutation,

44   mtDNA, oogenesis

45

46 **INTRODUCTION**

47

48 In mammals, mitochondrial gene sequences diverge at 10-30 times the mean rate of nuclear

49 genes [1, 2]. This difference is typically ascribed to a faster underlying mutation rate and

50 limited scope for purifying selection on mitochondrial genes, given uniparental inheritance,

51 negligible recombination and high ploidy [3]. At face value, weak selection against

52 mitochondrial mutations might seem to be consistent with the high prevalence of

53 mitochondrial mutations (~1 in 200) [4] and diseases (~1 in 5000 births) [5] in human

54 populations. But it is not consistent with the strong signal of purifying selection [6],

55 evidence of adaptive change [7] and codon bias [8] in mitochondrial genes, nor with the low

56 transmission rate of severe mitochondrial mutations between generations [9-11]. Despite

57 the high rate of sequence divergence, female germline processes apparently facilitate

58 selection against mitochondrial mutations, but the mechanisms are disputed and poorly

59 understood [12].

60

61 Here we develop computational and evolutionary models that compare three hypotheses of

62 germline mitochondrial inheritance and selection: (i) selection at the individual level,

63 facilitated by mitochondrial bottlenecks; (ii) selection at the cell level through follicular

64 atresia, which weeds out primordial germ cells with high mutation load; and (iii) selection at

65 the organelle level through selective transfer of mitochondria into oogonia during

66 development. These modes of selection are not mutually exclusive nor the only ones that

67 operate (a full examination is provided in the Discussion). The objective here is to clearly

68 delineate the major forces involved and the effectiveness of each in controlling mutation

69 accumulation. Our approach incorporates important factors neglected in earlier work, in

70   particular the input of *de novo* mitochondrial mutations and their segregation over multiple

71   rounds of germ-cell division. This provides a realistic model of mutation, segregation and

72   selection allowing the three hypotheses to be tested against the observed levels of

73   mitochondrial mutation and fitness across a variety of species with an emphasis on the

74   detailed clinical reports in human populations [4, 5].

75

76   The idea that mitochondrial mutations are winnowed through a tight germline bottleneck is

77   pervasive in the literature and has long been held to explain sharp changes in mutation load

78   between generations [13-15]. The exact size of the bottleneck is unclear, with estimates

79   from mouse [16-18] and human studies [14, 19-21] spanning two orders of magnitude.

80   Bottlenecks generate variance in mutation loads among the resulting germ cells, and tighter

81   bottlenecks produce greater variance, offering scope for selection against mitochondrial

82   mutations at the level of the individual [22-24]. The problem with this line of thinking is that

83   it ignores two other forces. First, gametes are produced through multiple rounds of cell

84   division, leading to repeated rounds of mitochondrial segregation, which in itself generates

85   considerable variance [25]. Second, bottlenecks induce greater input of *de novo* mutations

86   as more rounds of mitochondrial replication are required to regenerate the extreme ploidy

87   of mitochondrial DNA in mature oocytes. By applying realistic segregation dynamics and

88   mutational input, we evaluate the impact of these forces on the value of bottleneck size on

89   individual fitness.

90

91   Follicular atresia is another force widely considered to be critical in maintaining oocyte

92   quality [26-28] . In humans [29, 30], the number of germ cells declines dramatically in the

93   foetus between mid-gestation (~20 weeks in humans) when there are 7-8 million oocytes,

94   to late gestation when at least two thirds of these are lost, leaving a reserve of 1-2 million at

95   birth [31]. Oocyte loss continues throughout the life of an individual, eventually leading to

96   the depletion of the ovarian pool and loss of reproductive function at menopause [32-34].

97   Similar loss of female germ cells before sexual maturity is evident in mice and several other

98   animal species [35-38]. This attrition has historically been ascribed to cell death during

99   oocyte maturation [39, 40], but more recent findings implicate the apoptotic loss of 'nurse

100 cells' during the genesis of primary oocytes [41]. In either case, differential oocyte loss

101 offers scope for between-cell selection. However, the basis for between-cell selection has

102 long been questioned, on the grounds that it seems unlikely that 70–80% of oocytes have

103 low fitness as a result of mitochondrial mutations [40]. We therefore test whether selection

104 against oocytes with higher loads of mitochondrial mutations during follicular atresia is

105 capable of giving rise to the distribution of mutations observed.

106

107 A more recent interpretation of germ-cell loss links it to the formation of the Balbiani body,

108 a prominent feature of the humans [42, 43] and mouse [41, 44-46] female germline, as well

109 as a range of other vertebrates and invertebrates, with a range of terminology (e.g. fusome,

110 mitochondrial cloud) [41, 44-48]. In the mouse, proliferating germ cells typically form

111 clusters of 5-8 cells that establish cytoplasmic bridges [41, 49]. It is thought that around half

112 the mitochondria from each nurse cell are streamed into the Balbiani body of the primary

113 oocyte, through an active cytoskeletal process that depends in part on the membrane

114 potential of discrete mitochondria [50, 51]. This offers scope for purifying selection through

115 the preferential exclusion of dysfunctional mitochondria. The remaining nurse cells, now

116 denuded of half their mitochondria, undergo apoptosis [41]. Selective transfer and pooling

117 of mitochondria from interconnected cells may occur in other vertebrate and invertebrate

118   systems. We consider the consequence of different strengths of selection at the level of

119   mitochondrial function in the production of the Balbiani body.

120

121   To systematically distinguish between the predictions of these three different hypotheses,

122   under a range of reasonable parameter values, we use a computational model to evaluate

123   the patterns of mutation load generated over a single generation in each case. We then use

124   an evolutionary model to generate equilibrium levels and compare the predictions to the

125   prevalence of mutations and disease from human studies. Our results show that selection at

126   the organelle level through the pooling of high-quality mitochondria into the Balbiani body

127   is a more potent force than germline bottlenecks and follicular atresia and must play a key

128   role in the maintenance of mitochondrial function in the face of pervasive mutational

129   pressure. This analysis also pleasingly clarifies the longstanding paradox of germ-cell over-

130   proliferation followed by massive loss which is a widely conserved feature of the female

131   germline in animal taxa.

132

133   **RESULTS**

134   **Computational model**

135   The computational model follows the distribution of mitochondrial mutations across a

136   single generation, using model parameters derived from human data [29] (**Figure 1**). The

137   zygote is assumed to have around half a million copies of mitochondrial DNA (exact number

138   2^{19}), which are randomly partitioned to the daughter cells at each cell division. The pattern

139   of segregation is in agreement with recent evidence for actin-mediated mixing of

140   mitochondria within cells during mitosis leading to random segregation [52]. We assume

141   independent segregation of mitochondria with one mtDNA per mitochondrion, and do not

142   consider complications that might arise from the packaging of multiple mtDNA copies per

143   mitochondrion [14]. This assumption is supported by evidence that mitochondrial networks

144   fragment into multiple smaller structures at cell division [53, 54] that probably contain one

145   or a few mtDNAs.

146

147   Mitochondrial replication is not active during early embryo development [55], so the mean

148   mitochondrial number per cell approximately halves with each division (**Figure 1B**). In

149   humans, after 12 cell divisions a random group of 32 cells form the primordial germ cells

150   (PGC) [56], which in the model corresponds to a mean of 128 mitochondria per PGC.

151   Mitochondrial replication resumes at this point [29, 55]. Each mtDNA doubles prior to cell

152   division. With probability μ, one of the daughter mitochondria acquires a new deleterious

153   mutation through a copying error. We consider μ in the range 10^{-9} to 10^{-8} to 10^{-7} per base

154   pair per cell division (designated low, standard and high respectively), consistent with the

155   range of estimates for the female germline, and assume no back mutations (see Methods).

156   Point mutations during replication are the dominant form of mutation in mtDNA, so we do

157   not consider damage from other sources such as oxidative damage [57]. Mitotic

158   proliferation of PGCs gives rise to ~8 million oogonia, which are reduced to ~1 million

159   primary oocytes during late gestation (**Figure 1B**) [29, 55]. Proliferation is followed by a

160   quiescent phase during which the mitochondria in primary oocytes are not actively

161   replicated. Mutations accumulate far more slowly during this phase, which persists over

162   decades in humans [55, 58]. For simplicity, we assume no mutational input during this

163   period (not marked in **Figure 1B**). At puberty, the primary oocytes mature through clonal

164   amplification of mitochondria back to the extreme ploidy in mature oocytes (~500,000

165   copies; **Figure 1B**) [59]. The same copying error mutation rate μ is applied during this

166   process.

167

168   We consider three different forms of selection on mitochondria: selection at the level of

169   individuals, cells, or mitochondria. We apply selection at the level of individuals on the

170   zygotic mutation load. Selection at the level of cells or mitochondria is applied during culling

171   at late gestation when primary oocytes are produced. Each of these processes can be

172   captured by modifications of the computational model, allowing easy comparison between

173   them. In order to distinguish between different levels of selection, the model extends earlier

174   work that considered segregational variation of a fixed burden of existing mutations [13, 22-

175   24] but neglected the input of new mutations during PGC proliferation and oocyte

176   maturation, as well as the loss of germ cells during late gestation. The analysis here shows

177   the importance of considering these additional processes governing the population of

178   mitochondria in germline development.

179

180   **Germline bottleneck increases variance but introduces more *de novo* mitochondrial**

181   **mutations**

182

183   The effect of a bottleneck was assessed in the model by allowing b extra rounds of cell

184   division without mitochondrial replication during early embryonic development (e.g., two

185   extra rounds shown in **Figure 2A**). Each additional cell division leads to an average reduction

186   of $(0.5)^{b}$ mitochondria in PGCs compared to the base model. For simplicity we then hold

187   mitochondrial numbers at this lower value through the period of PGC proliferation. This

188   assumption gives greater impact to the bottleneck and is consistent with some views [18].

189   Tighter bottlenecks at this early developmental stage generate greater segregational

190   variance in mutation load between cells (**Figure 2B**). This increase in variance persists and is

191   enhanced through PGC proliferation to the production of primary oocytes and ultimately in

192   mature oocytes (**Figure 2B**). The bottleneck not only creates a wider spread of mutation

193   number per cell, but also the possibility that cells can be mutation free even when initiated

194   from a zygote that contains significant numbers of mutations (**Figure 2B**). Bottlenecks in

195   themselves do not change the mean mutation load, as they occur before the start of

196   mitochondrial replication (i.e. at PGC specification; **Figure 2B**) [55]. But oocyte maturation

197   requires the expansion of mitochondrial number back to half a million. Cells starting with

198   lower numbers must therefore undergo more rounds of mitochondrial replication, and

199   hence will accumulate more *de novo* mutations. So, the mean mitochondrial mutation load

200   in mature oocytes increases with tighter bottleneck size, albeit this effect is small with

201   standard mutation rates ($\mu = 10^{-8}$; **Figure 2B**). Nonetheless, the tension between variance

202   and mean determines the overall selective consequence of the bottleneck.

203

204   The advantage that the bottleneck brings depends on how selection acts against the

205   mutation load carried by an individual. Based on the observed dependence of mitochondrial

206   diseases on mutation load [60-62], in which more serious phenotypes typically manifest

207   only at high mutation loads of >60 % [60-62], it is thought that individual fitness is defined

208   by a concave fitness function, indicative of negative epistasis (**Figure 2C**). This assumes that

209   each additional mitochondrial mutation causes a greater reduction in fitness beyond that

210   expected from independent effects. In other words, low mutation loads have a relatively

211   trivial fitness effect, whereas higher mutation loads produce a steeper decline in fitness.

212

213   The change in mutation load (Δm) over a single generation after individual selection was

214   measured against 5 mean bottleneck sizes ($\bar{B} = 128, 64, 32, 16, 8$), for three initial mutation

215   loads (m_0) and three mutation rates (μ). The bottleneck shows an ambiguous relationship

216   with fitness, dependent on the inherited mutation load (m_0). For the estimated mutation

217   rate ($\mu = 10^{-8}$) there is always an increase in mutation load in individuals who inherit low

218   or medium mutation loads ($m_0 = 0.001, 0.01$; **Figure 2D**). This increase in load ($\Delta m > 0$)

219   becomes more deleterious with a tighter bottleneck (**Figure 2D**). The bottleneck only

220   confers a benefit ($\Delta m < 0$) among individuals who inherit a high mutation load ($m_0 = 0.1$;

221   **Figure 2D**), where the advantage of greater variance outweighs the increase in *de novo*

222   mutation load. If the mutation rate is lower ($\mu = 10^{-9}$), bottlenecks have little effect except

223   when severe, where they again cause an increase in mutation number in individuals with

224   low or medium mutation loads ($m_0 = 0.001, 0.01$; **Figure 2 – figure supplement 1A**). In

225   individuals with high mutation load ($m_0 = 0.1$) only tighter bottlenecks ($\bar{B} = 16, 8$) are

226   beneficial (**Figure 2 – figure supplement 1A**). If the mutation rate is higher ($\mu = 10^{-7}$) the

227   pattern is more extreme, with the accumulation of *de novo* mutations except in individuals

228   with high inherited mutation loads ($m_0 = 0.1$) at the tightest bottleneck size ($\bar{B} = 8$)

229   (**Figure 2 – figure supplement 1B**). In sum: even though bottlenecks generate greater

230   variance, they impose the need for additional rounds of mitochondrial replication during

231   oocyte maturation, resulting in greater *de novo* mutational input. This makes tight

232   bottlenecks advantageous only for rare individuals who inherit high mutation loads, but not

233   for the great majority of the population where the prevalence of mitochondrial mutations is

234   below the limits of detectability, between 0.001 and 0.01 [4, 14].

235

Follicular atresia cannot be explained by realistic selection against cells with high

mitochondrial mutation loads

In the analysis of bottlenecks above, the culling of ~8 million oogonia to 1 million primary

oocytes at the end of PGC proliferation was assumed to be a random process (**Figure 2A**).

This loss has a minimal effect on the mean and variance of mitochondrial mutations in germ

cells, given the large numbers involved (and no effect at all when averaged over a

population). However, the loss of ~80% of oocytes via follicular atresia during late gestation

has long been puzzling and could arguably reflect selection against cells with higher

mutation loads.

To analyse follicular atresia, cell-level selection was applied to oogonia at the end of PGC

proliferation (**Figure 3A**). PGCs vary in mutation frequency due to both the random

segregation of mutants during the multiple cell divisions of proliferation and the chance

input of new mutations during mtDNA replication. In principle, we assume that between-cell

selection is governed by a negative epistatic fitness function (**Figure 3B**) similar to that

thought to apply at the individual level, and vary selection from linear ($\xi = 1$), weak ($\xi = 2$)

to strong epistasis ($\xi = 5$). Positive epistasis ($\xi < 1$), whereby a single point mutation

produces a steep loss of fitness, but additional mutations have less impact (i.e. mutations

are less deleterious in combination), seems biologically improbable, so we do not consider it

here.

The effect of cell selection during follicular atresia was calculated as the change in mutation

frequency for individuals carrying different mutation loads (m_0) over a single generation,

260   given standard values for *de novo* mutations ($\mu = 10^{-8}$) and bottleneck size ($\bar{B} = 128$).

261   Under strong negative epistasis ($\xi = 5$), only the few cells with very high mutation loads

262   (generated by segregation) are eliminated. Cell-level selection does not reduce mutation

263   load, even for individuals with a high initial frequency of mutations ($m_0 = 0.1$; **Figure 3C**).

264   Cell-level selection is more effective with weak epistasis ($\xi = 2$) or linear selection ($\xi = 1$)

265   as this makes cells with lower mutation loads more visible to selection, and has a greater

266   benefit in individuals carrying higher initial mutation loads (**Figure 3C**). However, in

267   individuals who inherit low or medium mutation load ($m_0 = 0.001, 0.01$) cell selection

268   offers a minimal constraint against mutation input. The only case in which cell selection

269   produces a benefit is with high mutation load ($m_0 = 0.1$) under linear selection ($\xi = 1$)

270   (**Figure 3C**). This pattern holds for a lower mutation rate ($\mu = 10^{-9}$; **Figure 3 – figure**

271   **supplement 1A**), while there is no benefit at all at a higher mutation rate ($\mu = 10^{-7}$; **Figure**

272   **3 – figure supplement 1B**).

273

274   **The Balbiani body pools high-quality mitochondria and restricts *de novo* mutation input**

275   An alternative interpretation of atresia in late gestation lies in the formation of the Balbiani

276   Body. We model the developmental process giving rise to the Balbiani body by assuming

277   that cysts of 8 oogonia form at the end of PGC proliferation (**Figure 4A**). Cells within a cyst

278   are derived from a common ancestor (i.e. via 3 consecutive cell divisions). At the 8-cell

279   stage, intercellular bridges form between the oogonia. These allow cytoplasmic transfer of a

280   proportion of mitochondria (f) from each cell to join the Balbiani body of the single cell

281   destined to become the primary oocyte (**Figure 4A**). The mitochondria that undergo

282   cytoplasmic transfer are sampled at random (without replacement), with different weights

283   for wildtype (p_{wt}) and mutant (p_{mut}) mitochondria, until f have moved to the Balbiani

284   body. The oogonia that donate their cytoplasm to the primary oocyte are now defined as

285   nurse cells, and undergo programmed cell death – atresia (**Figure 4A**).

286

287   The model shows that two benefits accrue from cytoplasmic transfer. The first benefit of

288   mitochondrial transfer into the Balbiani body is that pooling increases the number of

289   mitochondria in primary oocytes. As the proportion of mitochondria transferred increases

290   towards the estimated rate of f = 50% [41], the number of mitochondria in primary oocytes

291   increases 4-fold. Pooling therefore cuts the number of rounds of replication needed to

292   reach the extreme ploidy required by mature oocytes, which decreases the input of new

293   mutations from replication errors during oocyte maturation. This benefit accrues whatever

294   the initial mutation load, and more dramatically with a higher mutation rate (**Figure 4 –**

295   **figure supplement 1**).

296

297   The second benefit arises from selective transfer of mitochondria. Preferential exclusion of

298   mutant mitochondria ($p_{wt} > p_{mut}$), as suggested by experimental evidence [41, 51, 63],

299   lowers the mutation load in primordial oocytes (**Figure 4B**). The difference between p_{wt} and

300   p_{mut} determines the extent to which the mutation load is reduced, with stronger exclusion

301   of mutant mitochondria (lower p_{mut}) reducing the number of mutations when the inherited

302   load is medium or high ($m_0 = 0.01, 0.1$), albeit with a negligible effect at low initial

303   mutation load ($m_0 = 0.001$; **Figure 4C**). The same effect is seen with lower and higher

304   mutation rates (**Figure 4 – figure supplement 2**). Nurse cells retain a higher fraction of

305   mutant mitochondria but undergo apoptosis, removing mutants from the pool of germ cells,

306   and explaining the need for an extreme loss of germ cells during late gestation. This effect

307   acts in concert with pooling leading to a reduction in both the mean and variance of

308   mitochondria mutation load in the cells destined to develop into mature oocytes. (**Figure**

309   **4B**).

310

311   **Evolutionary model**

312   The computational model discussed above gives an indication of the effectiveness of

313   selection at the level of individuals, cells or mitochondria in eliminating mitochondrial

314   mutations across a single generation. To address the long-term balance of mutation

315   accumulation versus selection over many generations, we developed an evolutionary

316   model. This assesses the effectiveness of the three representations of germline

317   development in explaining the observed prevalence of mitochondrial mutation load and

318   disease in human populations (see **Materials and Methods**). This evolutionary model

319   evaluates long-term evolutionary change in an infinite population with non-overlapping

320   generations and is implemented using a number of approximations, which greatly reduce

321   the model complexity (see **Materials and Methods**).

322

323   By iterating the patterns of germline inheritance and selection, the equilibrium mutation

324   distribution was calculated across a range of mutation rates and bottleneck sizes. The

325   accuracy of the three models was then assessed as the likelihood of reproducing the

326   observed levels of mitochondrial mutations in the human population (**Figure 5**). Specifically,

327   we used estimated values of 1/5000 for mitochondrial disease (>60% mutant), 1/200 for

328   carriers of mitochondrial mutants (2-60% mutant) and hence 99.5% of individuals are

329   'mutation free' (i.e. carry <2% mutants, the threshold for detection in these estimates of

330   mutation frequency [4, 5]). Recent deep-sequencing estimates using a mutation detection

331   threshold of >1% [14], show that a minor allele frequency of 1-2% is relatively common in

332   selected human PGCs, but this does not alter earlier population-level estimates of the

333   proportion of carriers not suffering from overt mitochondrial disease, defined as a 2-60%

334   mutation load used here.

335

336   Likelihood heatmaps confirm that selection at the level of individuals or cells alone do not

337   readily approximate the clinical data whatever the bottleneck size (**Figure 5A-B**). Only at a

338   mutation rate $\mu < 0.5 \times 10^{-8}$ do these forms of selection offer explain the observed

339   mutation load and disease frequency in humans at high likelihood, especially when using

340   tighter bottlenecks (**Figure 5A**). These limitations do not apply to the preferential transfer of

341   wildtype mitochondria into the Balbiani body (**Figure 5C-D**). Even intermediate levels of

342   selection against the transfer of mutant mitochondria into the Balbiani body ($p_{mut} = 0.33$,

343   $p_{wt} = 0.67$) generates a high log-likelihood of reproducing the clinical data at the standard

344   mutation rates ($\mu = 10^{-8}$) and bottleneck sizes (> 100 mitochondria per cell) (**Figure 3C**).

345   Stronger selection on transfer probabilities ($p_{mut} = 0.25$, $p_{wt} = 0.75$) can account for the

346   clinical pattern under a wide range of bottleneck sizes and mutation rates (**Figure 5D**).

347

348   **DISCUSSION**

349

350   How selection operates on mitochondria has long been controversial. At the heart of this

351   problem is the paradox that mtDNA accumulates mutations faster than nuclear genes, yet

352   there is evidence that mtDNA is under strong purifying selection. Mitochondrial mutations

353   accumulate through Muller's ratchet, as mtDNA is exclusively maternally inherited, and

354   does not undergo recombination through meiosis [3]. In addition, mitochondrial genes are

355   highly polyploid, which obscures the relationship between genotype and phenotype,

356   hindering the effectiveness of selection on individuals. Despite these constraints,

357   deleterious mitochondrial mutations seem to be eliminated effectively [6-11], facilitated by

358   female germline processes that have long been mysterious. These include: the excess

359   proliferation of primordial germ cells (PGCs) [64]; the germline mitochondrial bottleneck

360   (when mitochondrial numbers are reduced to a disputed minimum in PGCs) [13-15]; the

361   formation of the Balbiani body in primary oocytes [41, 51]; the atretic loss of 70-80% of

362   germ cells during late gestation [31, 39]; the extended oocyte quiescence until puberty or

363   later (during which time mitochondrial activity and replication is suppressed) [58, 65]; and

364   the generation of around half a million copies of mtDNA in mature oocytes [59]. The key

365   question is how do these processes facilitate the maintenance of mitochondrial quality over

366   generations?

367

368   In this study, we introduced a computational model that considers these germline processes

369   from the perspective of mitochondrial proliferation, segregation and selection, using

370   realistic estimates of parameter values, drawn from the human literature [29, 55]. Most

371   work to date [13, 15-18] has focused on the mitochondrial bottleneck as a means of

372   generating variation in mitochondrial content between oocytes and by extension zygotes

373   (**Figure 2B**), furnishing the opportunity for selection to act on individuals in the following

374   generation. These studies have been unable to reconcile serious differences in experimental

375   estimates of mitochondrial numbers during PGC proliferation, inciting inconclusive debates

376   over the tightness of the bottleneck [13, 15-18]. More significantly, this earlier work

377   neglects an important germline feature, the introduction of *de novo* mitochondrial

378   mutations produced by copying errors [66] rather than damage by reactive oxygen species

379   [57, 67]. These accumulate during PGC proliferation and, equally importantly, during the

380   mass-production of mtDNAs in the mature oocyte. Tighter bottlenecks are disadvantageous

381   as they impose the need for more rounds of mitochondrial replication which means a

382   greater input of *de novo* mutations. Our modelling shows that for most individuals the mean

383   mutation load shows little meaningful change (**Figure 2D**), regardless of whether the

384   mutation rate is set low or high (**Figure 2 – figure supplement 1**), and in fact increases with

385   tighter bottleneck size (**Figure 2D**). Most individuals have low mutation loads (~99.5% in

386   human populations [4, 5]), and for them, the normal process of repeated segregation during

387   cell division generates sufficient variance in itself. Any marginal increase in variance caused

388   by bottlenecks is more than offset by increased mutational input. Tighter bottlenecks only

389   benefit individuals who already carry high mutation loads (i.e. $m_0 \geq 0.1$, **Figure 2D**). For

390   them, there is benefit in further reductions in bottleneck size as this increases the fraction

391   of mature oocytes with significantly reduced mutation load (**Figure 2D**). In the modelling,

392   we assumed that the bottleneck size was maintained across the period of PGC proliferation.

393   Some studies have found that from a low number in early development, copy number

394   increases 5-10 fold to production of the oogonia [16, 17]. This would lessen the effect of the

395   bottleneck in general as it would have less effect on segregation.

396

397   These results show that the popular idea that a germline mitochondrial bottleneck

398   facilitates selection against mitochondrial mutations is misconstrued. The value of a

399   bottleneck depends on the unforeseen trade-off between increasing genetic variance and

400   mutation input. In fact, the reduction in mitochondrial copy numbers from zygote to

401   primordial germ cells should be thought of as the reestablishment of a typical copy number

402   at the start of cellular differentiation, which commences after multiple cell divisions *without*

403   mtDNA replication. What counts as a bottleneck are the 'extra' rounds of cell division

404   reducing mitochondrial number below the 'normal' number, and the incremental increase

405   in variance this induces. Most critically, the bottleneck needs to be understood in relation to

406   oogamy, the massively exaggerated mitochondrial content of the female gamete. This is a

407   characteristic of metazoan gametogenesis [59]. Previous work has shown it is beneficial in

408   animals with mutually interdependent organ systems [59]. The extreme ploidy in the zygote

409   allows early rounds of cell division to occur without mitochondrial replication, and hence

410   without *de novo* mutational input. These initial cell divisions generate little between-cell

411   differences, as segregational variance is weak when numbers are high and mitochondria

412   segregate randomly during mitosis [52] (e.g. **Fig 1B** before PGC specification). So at the point

413   of cellular differentiation (~12 cell divisions) there is homogeneity in the mutation load

414   among the different organ systems and no one system is likely to fail, which would

415   massively lower the fitness of the whole organism [59]. This contrasts with organisms that

416   have modular growth, such as plants and morphologically simple metazoa (sponges, corals,

417   placozoa), which neither sequester a recognizable germline distinct from the stem-cell

418   lineage early in development (although recent work challenges this view), nor have oocytes

419   with massively expanded mitochondrial numbers [56, 59, 68-70].

420

421   Follicular atresia is another female germline feature examined in our modelling, in which

422   there is over-proliferation of PGCs followed by ~80% loss early in development, before

423   oocyte maturation [31, 39]. This massive reduction in germ cell number has long been

424   enigmatic. It is unlikely to be random, yet does not obviously serve a selective function, as it

425   seems unlikely that such a high proportion of germ cells could have low fitness [26-28]. The

426   model confirms this intuition. Selection among PGCs at the end of the period of

427   proliferation has little effect in significantly reducing mutation load (**Figure 3C**). Assuming a

428   concave fitness function (**Figure 3B**), which seems reasonable by extension from the

429   severity of mitochondrial diseases [60, 62], between-cell selection is ineffective, as it only

430   eliminates PGCs with very high mutational numbers. This has little effect in constraining the

431   burgeoning of lower mutation loads. Linear selection does better, even if it seems

432   unrealistic, as it will act against a broader range of mutational states. But as with

433   bottlenecks, it is only beneficial in individuals already carrying significant mutation loads (i.e.

434    $m_0 \geq 0.1$, **Figure 3C**). We conclude that cell-level selection produces little measurable

435   reduction in mutation load and so is unlikely to be responsible for follicular atresia.

436

437   A more recent explanation of PGC loss relates to the formation of the Balbiani body in

438   primary oocytes [41, 44]. In many metazoa, including clams [46], insects [45, 71], mice [49]

439   and probably humans [44], the over-proliferation of PGCs culminates in their organization

440   into germline cysts of multiple oogonia connected by cytoplasmic bridges [41, 49, 71]. These

441   connections are thought to allow the transfer of mitochondria and other cytoplasmic

442   constituents by active attachment to microtubules, into what becomes the primary oocyte

443   [41]. The surrounding oogonia that transferred their mitochondria, now termed nurse cells,

444   die by apoptosis [41]. The plethora of terms should not mask the key point that nurse cell

445   death accounts for a considerable fraction of the germ cell loss usually ascribed to follicular

446   atresia. We modelled selective mitochondrial transfer into the Balbiani body, perhaps in

447   part reflecting membrane potential [45, 51]. This achieves two complementary benefits: it

448   purges mutations and pools high-quality mitochondria in a single cell. If the germline cyst is

449   composed of eight cells that contribute half of their mitochondria to the Balbiani body, then

450   the primary oocyte gains four times as many mitochondria which have passed through

451   quality control. This also cuts the need for additional rounds of mtDNA copying, and so

452 reducing the input of *de novo* mutations. Selective transfer and pooling lowers the mutation

453 load across a wide range of mutation rates and inherited loads (**Figure 4C, Figure 4 – figure**

454 **supplement 1-2**). This process differs from mitophagy, the main route used in somatic cells

455 for maintaining mitochondrial quality [72, 73], as it not only removes mutant mitochondria,

456 but crucially also increases mitochondrial numbers, a key requirement for prospective

457 gametes. The requirement for pooling of mitochondria to lower the mutation load from

458 copying errors also aligns with experimental observations of active spindle-associated

459 mitochondrial migration to the generative oocyte in the formation of polar bodies during

460 meiosis I of oogenesis [74]. We predict that selection for mitochondrial quality occurs during

461 this process (i.e. polar bodies retain mutant mitochondria) but have not dealt with that

462 explicitly in the model.

463

464 These insights depend in part on the parameter values used in the modelling, many of which

465 are uncertain. We have examined variation around the most representative values drawn

466 from the literature [2, 14, 75, 76], and aimed to be conservative wherever possible. We

467 considered mutation rates across two orders of magnitude, around 10^{-8} per bp as the

468 standard [75] and a similar range of bottleneck sizes ($\bar{B} = 8 - 128$). Strong selective pooling

469 of mitochondria into the Balbiani body predicts the observed prevalence of mitochondrial

470 mutations and diseases in human populations [4, 5] under a wide range of mutation rates

471 and bottleneck sizes (**Figure 5**). Selection at the level of individuals or cells are much more

472 constrained explanations, although we do not rule out some role for these processes (**Figure**

473 **5**). In general, higher mutation rates (10^{-7} per base pair) strengthen the conclusions

474 discussed here (**Figures 2-4 – figure supplement 1-2**) whereas the lowest mutation rates are

475 more commensurate with weaker forms of evolutionary constraint generated by selection

476   on individuals or cells. Plainly, weaker selection approximates best to clinical data when the

477   mutation input tends towards zero (**Figure 5**). However, such low mutation rates are not

478   consistent with the 10-30-fold faster evolution rates of mtDNA compared with nuclear

479   genes [1, 2], or with the strong signatures of purifying [6] and adaptive [7] selection on

480   mitochondrial genes. In the modelling, we ignored the contribution of oxidative damage

481   caused by reactive oxygen species. While this source of mutation is likely low compared

482   with copying errors [57, 66], oxidative mutations may accumulate over female reproductive

483   lifespans [67], perhaps contributing to the timing of the menopause [77]. As primary

484   oocytes contain ~6000 mitochondria [77], expansion up to ~500,000 copies in the mature

485   oocyte will amplify any mutations acquired during oocyte arrest at prophase I, potentially

486   over decades [66]. The metabolic quiescence of oocytes can best be understood in light of

487   the need to repress mitochondrial mutation accumulation during the extended period

488   before reproduction [58, 65].

489

490   We have addressed here a simple paradox at the heart of mitochondrial inheritance. Like

491   Gibbon's *Decline and Fall of the Roman Empire*, mitochondrial DNA is often portrayed as

492   being in continuous and implacable decline through Muller's ratchet [3]; yet like the Empire,

493   which endured for another millennium, mitochondrial DNA has persisted and has been at

494   the heart of eukaryotic cell function for over a billion years [78]. Strong evidence for

495   purifying and adaptive selection implies that the female germline facilitates selection for

496   mitochondrial quality, but the mechanisms have remained elusive. We have modelled

497   segregation and selection of mitochondrial DNA at each stage of germline development, and

498   shown that direct selection for mitochondrial function during transfer into the Balbiani body

499   is the most likely explanation of the observed prevalence of mitochondrial mutations and

500   diseases in human populations. More remarkably, this mitochondria-centric model

501   elucidates the complexities of the female germline. It explains why mature oocytes are

502   crammed with mitochondria [59], whereas sperm mitochondria are typically destroyed,

503   giving rise to two sexes [25]; why germ cells over-proliferate during early germline

504   development; why oogonia organize themselves into germline cysts, forming the Balbiani

505   body; why the majority of germ cells then perish by apoptosis as nurse cells; why primary

506   oocytes enter metabolic quiescence, sometimes for decades; and even why polar bodies

507   channel most of their mitochondria into a single mature oocyte. The need for mitochondrial

508   quality extends to somatic cells, as mitochondria activity is crucial to cellular, tissue and

509   organ functioning in the adult organism [79-81]. Some of the approaches we have adopted

510   here need to be applied to development and whether specific processes have evolved to

511   maintain mitochondria where their function is more critically related to somatic fitness [59,

512   82]. Most fundamentally, this perspective challenges the claim that complex multicellularity

513   requires passage through a single-celled, haploid stage to constrain the emergence of lower-

514   level, selfish genetic elements [82, 83]. This is true for nuclear genes in oocytes, whose

515   quality is maintained by sexual exchange and recombination [83], but is not the case for

516   mitochondria, which are generally transmitted uniparentally, without sexual exchange or

517   recombination. In animals, the oocyte cytoplasm is not derived from a single cell, but

518   instead requires the selective pooling of mitochondrial DNA from clusters of progenitor

519   cells, which together generate high-quality mitochondria at extreme ploidy in mature

520   gametes.

521

522

523 **MATERIALS AND METHODS**

524 **Computational Model**

525   1. Initial conditions

526 We use a computational model implemented in MATLAB (**RRID:SCR_001622**) to follow the

527 distribution of mitochondrial mutations in the female germline over a single generation

528 from zygote to a new set of mature oocytes, as set out in the developmental history given in

529 the main text (**Figure 1A**). The initial state of the system is a zygote containing $M_0 = 2^{19} =$

530 524,288 copies of mtDNA [59, 84], of which m_0 carry a deleterious mutation. Three specific

531 models are considered: bottleneck, follicular atresia and cytoplasmic transfer. A list of terms

532 and parameter values is given in **Table 1**, which also apply in the evolutionary model

533 considered below.

534 **Table 1**

Parameters and variables	Symbols and values
Maximum number of germ cells	$N_{max} = 8,388,608$
mtDNA number in mature oocytes	$M_0 = 2^{19} = 524,288$
Minimum mtDNA ploidy	B
Final number of germ cells	$N_{max}/8 = 1,048,576$
Initial mutation load	m_0
Mutation rate per bp per cell division	μ
Strength of epistatic interactions	ξ
Transfer probability of mutant mtDNA	p_{mut}
Transfer probability of wildtype mtDNA	p_{wt}
Human mitochondrial genome size	$g = 16,569\text{bp}$ [85]

535

536   2. Early embryonic development

537   During early embryonic development, there is no mtDNA replication. The number of cells

538   doubles at each time step. The existing population of mutant and wildtype mtDNA

539   undergoes random segregation into daughter cells according to a binomial distribution –

540   each mtDNA copy has a 50% probability of being assigned to either daughter cell. During

541   this process, the average number of mtDNA copies per cell halves at each time step. There is

542   no mutational input, as we only consider mutations that arise due to replication errors.

543

544   3. PGC proliferation, oogonia cell death and oocyte maturation

545   The early embryonic period lasts for the first 12 cell divisions. A group of 32 cells is selected

546   at random to form the primordial germ cells (PGC). The PGCs then undergo proliferation for

547   a further 18 rounds of cell division, until the maximum number of germ cells is

548   reached, $N_{max} = 32 \times 2^{18} = 8,388,608$. This value is close to the average reported in the

549   literature [29].

550

551   mtDNA replication resumes after cell division 12, at the point of PGC determination. At this

552   point, cells have an average of 128 mtDNA copies. At each following time step, the number

553   of mtDNA copies doubles prior to random segregation into daughter cells. This means that

554   the average number of mtDNA copies per cell is kept constant. New mutations are

555   introduced as errors in mitochondrial replication. During the replication process, the new

556   replica of each wildtype mtDNA copy has a probability of mutation μ/bp. The genome wide

557   mutation rate $U = g \times \mu$ is calculated as genome size ($g = 16,569$ bp [85]) multiplied by μ.

558   This estimate assumes each site contributes equally to selective effects and ignores many

559   subtleties relating to mutation probability and within-cell maintenance processes, but

560   should give a reasonable order of magnitude gauge of the target size of mutational input

561   per cell division. Given n wildtype and m mutant mtDNAs, the number of new mutants

562   Δm resulting from replication errors is obtained by sampling at random from a binomial

563   distribution with n trials with probability U. After replication and mutation and prior to

564   segregation the total number of wildtype and mutant mtDNAs is $2n - \Delta m$ and $2m + \Delta m$

565   respectively. Back mutation to wildtype is not permitted.

566

567   At the end of PGC proliferation, the N_{max} oogonia undergo random cell death, leaving

568    $N_{max}/8 = 1{,}048{,}576$ primary oocytes. This is achieved by sampling the surviving cells at

569   random with uniform weights (i.e., every cell has an equal probability of survival). The

570   primary oocytes do not undergo further cell division or mitochondrial replication during the

571   quiescent period (this is not explicitly modelled). At puberty, oocyte maturation

572   commences. The number of mitochondria per cell is brought back to the original value

573    $M_0 = 2^{19}$ through 12 rounds of replication without cell division. We assume that the

574   number of mtDNA copies doubles at each time step. This introduces new deleterious

575   mutations, which again are randomly drawn from a binomial distribution (as described

576   above).

577

578   4. Specific models of selection

579   We consider three specific models in the main text with modifications to the base model

580   described above.

581

582   The first model adds a bottleneck stage at the time of PGC determination (**Figure 2**). As

583   before, 32 cells are selected at cell division 12 to form the PGCs. These go through b extra

584   rounds of cell division without mtDNA replication. This reduces the mean number of mtDNA

585   copies per cell to $\bar{B} = 128 * (0.5)^b$. The mtDNA replication commences at cell division 14.

586   The PGCs then proliferate as before to produce oogonia that undergo random cell death to

587   produce primary oocytes. The primary oocytes have a reduced number of mtDNA copies,

588   and so must undergo $12 + b$ extra rounds of mtDNA replication in order to regain the

589   original value M_0 mitochondria in mature oocytes. Note that this is an extreme model of the

590   bottleneck, where mtDNA copy number is kept low throughout the period of PGC

591   proliferation, and so maximises the benefit derived from the increase in segregational

592   variation caused by the bottleneck.

593

594   For the model of the bottleneck, we allow selection dependent on individual fitness in

595   relation to their mutation load m among mature oocytes, according to the fitness function

596    $f(m) = 1 - (\frac{m}{M})^5$ (**Figure 2C**). The concave shape of this function accounts for the fact that

597   mitochondrial mutations typically have a detrimental effect on individual fitness only for

598   loads >60%. Changes to the power exponent make little qualitative difference to the

599   outcome of this model (data not shown).

600

601   A second model considers non-random death during the cull of oogonia as these cells

602   transition to being primary follicles (**Figure 3**). Selection in this case is applied at the cell

603   level. Cell fitness is expressed as $f(m) = 1 - (\frac{m}{M})^\xi$, where m is the number of mutant

604   mitochondria. The parameter ξ determines the strength of epistatic interactions (**Figure

605   3B**). As in other models, the number of cells is reduced from $N_{max} = 8,388,608$ to

606    $N_{max}/8 = 1,048,576$. This is achieved by sampling without replacement the surviving cells

607   at random, with weights proportional to cell fitness (i.e., every cell has a probability of

608   survival proportional to its fitness).

609

610   The third model considers that the oogonia are organised in cysts of 8 cells each. These are

611   the descendants of a single cell (*i.e.* three cell divisions prior). One cell is randomly

612   designated as the primary oocyte using the MATLAB function randsample. The Balbiani body

613   of the primary oocyte contains a proportion f of the mtDNA copies of all cells in the cyst.

614   The mitochondria that join the Balbiani body are sampled at random without replacement

615   from each cell with different weights for wildtype (p_{wt}) and mutant (p_{mut}). After

616   mitochondrial transfer to the Balbiani body, nurse cells undergo apoptosis (i.e. all cells

617   except the one designated as the primary oocyte), reducing the total number of oocytes to

618    $N_{max}/8 = 1,048,576.$

619

620   **Evolutionary Model**

621   In order to calculate the equilibrium distribution of a population undergoing the

622   developmental dynamics mentioned in the previous section, we develop an analytical

623   model for the distribution of mitochondrial mutations in an infinite population, with non-

624   overlapping generations. As it was not possible to find an analytical solution, we solved the

625   equations through numerical iterations. The system converges to a unique equilibrium

626   state, independent of the initial conditions.

627

628   The state of the system is described by the vector $p(t) = \{p_0(t), \dots, p_{M(t)}(t)\}$, where

629    $M(t)$ is the number of mtDNA copies per cell at time t. The elements $p_m(t)$ are the

630   frequency of mutation load $m(t)/M(t)$ at time t. The evolution of the system is determined

631 by a set of transition matrices whose elements are the transition probabilities between

632 states. To avoid unnecessary complexity in the evolutionary model, we assume that

633 fluctuations in mitochondrial number per cell due to segregation are negligible (*i.e.* in

634 contrast to the computational model which allows binomial segregation at each division).

635 Therefore, the mtDNA number per cell is constant across the whole population of cells at

636 every time step. That is, during early embryonic development (when there is no mtDNA

637 replication), after t cell divisions, the total number of mitochondria per cell is $M^{(t)} =$

638 $2^{-t}M_0$. Then, during PGC proliferation, the total number of mitochondria per cell is

639 constant. Finally, during oocyte maturation, the number of mitochondria per cell exactly

640 doubles with each mtDNA replication cycle. To aid in calculations, we also set the initial

641 number of mtDNA copies to be proportional to the bottleneck size, *i.e.* $M_0 = 2^{12} \times B$. As

642 the mtDNA number per cell halves at each cell division during early embryonic

643 development, setting M_0 this way allows the mtDNA number to remain an integer. This is

644 important for the modelling procedure, because the dimension of the transition matrixes

645 (which is determined by the mtDNA number) must be an integer.

646

647   1. Early embryonic development

648 During early embryonic development, when mitochondrial replication is not active, changes

649 in frequency arise purely from the process of segregation. Let $W^{(t)}$ be a $M^{(t)} + 1 \times M^{(t)} +$

650 1 square matrix, whose elements W_{mn} represent the transition probabilities from a state

651 with m to a state with n mutants:

$$W_{mn}^{(t)} = \binom{m}{n}\binom{M^{(t-1)} - m}{M^{(t)} - n} \Big/ \binom{M^{(t-1)}}{M^{(t)}} \tag{1}$$

652

653   These matrix elements model the probability of transitioning from a state with m mutants

654   and $M - m$ wildtype to a state with n mutants and $M - n$ wild type via the segregation of

655    $2M$ mitochondria into two daughter cells with M mitochondria each.

656

657   After t cell divisions, the average number of mutants per cell is $\overline{m} = 2^{-t}m_0$, and the

658   variance is $Var(t) = \frac{1}{4}[Var(t-1) + 2^{-t}m_0]$. The state of the system is updated as

659    $\vec{p}^{(1)} = \left(\prod_t W^{(t)}\right) \times \vec{p}^{(0)}$.

660

661   2.   PGC proliferation, oogonia cell death and oocyte maturation

662   During PGC proliferation, new mutations are introduced at a rate $U = \mu \times g$. The transition

663   coefficient Q_{mn} from a state with m to a state with n mutants results from the combined

664   effects of replication, mutation and segregation:

665

$$Q_{mn} = \sum_k \binom{M-n}{k-n} U^{k-n}(1-U)^{M-k} \binom{k}{m}\binom{M-k}{M-m} \Big/ \binom{2M}{M} \qquad (2)$$

$$= \sum_k \binom{M-n}{k-n} U^{k-n}(1-U)^{M-k} a_{k,m}$$

666   The coefficient $a_{k,m} = \binom{k}{m}\binom{M-k}{M-m}/\binom{2M}{M}$ models the probability of transitioning from a state

667   with k mutants and $M - k$ wildtype to a state with n mutants and $M - n$ wild type via the

668   segregation of $2M$ mitochondria into two daughter cells with M mitochondria each; the

669   remaining part of the equation models the probability of reaching a state with k mutant

670   mitochondria through replication and mutation of M mitochondria, of which m are mutant

671   (this corresponds to the probability of introducing $k - m$ new mutations). The system is

672   updated $\vec{p}^{(2)} = Q^q \times \vec{p}^{(1)}$, across q rounds of PGC cell division. We then apply particular

673   processes to capture the effects of the bottleneck, follicular atresia and cytoplasmic

674   transfer.

675

676   As before, we model the bottleneck as b extra rounds of segregation before the onset of

677   mtDNA replication, following **Eq(1)** with $q + b$ cell divisions. This has no effect on the mean

678   mutational number but increases mutational variance between the resulting PGCs. The

679   transition between oogonia and primary oocytes occurs at random, and so does not alter

680   the frequency distribution of mutants. Finally, during oocyte maturation, the mtDNA

681   content of each cell doubles at every time step until the initial ploidy M_0 is restored. The

682   transition matrix G_{mn} is analogous to the first term of **Eq(2)**, incorporating replication and

683   mutation, but without segregation (last term of **Eq(2)**):

684

$$G_{mn}^{(t)} = \binom{M^{(t)} - m}{n - m} U^{n-m}(1 - U)^{M-k} \tag{3}$$

685   **Eq(3)** models the probability of transitioning from a state with m to a state with n mutants,

686   which is equivalent to the probability that exactly $n - m$ out of $M^{(t)} - m$ wildtype acquire a

687   deleterious mutation. As the bottleneck reduces mtDNA copy number per cell, there is the

688   need for b extra rounds of replication of mtDNA during oocyte maturation. Hence, the

689   transition coefficient G is applied $b + 12$ times in the bottleneck model, to restore the

690   number of mtDNA copies per oocytes to the original ploidy level M_0: $\vec{p}^{(3)} = \left(\prod_t G^{(t)}\right) \times$

691    $\vec{p}^{(2)}$.

692

693   At the end of the maturation phase, for the bottleneck model, selection is applied on

694   individual fitness using a vector w whose elements w_m are equal to the corresponding

695   fitness: $w_m = f(m) = 1 - \left(\frac{m}{M}\right)^5$. This causes a change in the population mutation load as

696   the system is updated to:

$$\vec{p}^{(3)} = (I\vec{w})\,\vec{p}^{(2)}/\vec{w}^T\,\vec{p}^{(2)} \tag{4}$$

697   where I is the identity matrix.

698

699   In the model of follicular atresia, an extra step is included to reflect selection that operates

700   when the population of oogonia are culled to produce the primary oocytes. This causes a

701   change in the population mutation load analogous to that described in **Eq(4)**, but using the

702   cell fitness function $w_m = f(m) = 1 - \left(\frac{m}{M}\right)^\xi$ instead. This determines the shift in mutation

703   loads that arises from fitness-dependent culling of oogonia. The transition coefficient **Eq(3)**

704   for oocyte maturation is then applied 12 times in the follicular atresia model, to restore the

705   original level of ploidy.

706

707   Finally, in order to model cytoplasmic transfer, a different process is used in the production

708   of primary oocytes. A set of 8 clonally derived cells is selected. The mutation levels of each

709   cell in the cyst is obtained by applying **Eq(3)** three times. Then, 50% of the mitochondria in

710   each cell are pooled into the Balbiani body of the primary oocyte. The probability for a cell

711   with m mutants to contribute n mutants to the Balbiani body is given by:

$$C_{nm} = \binom{m}{n} p_{mut}^n \binom{M-m}{M/2-n} p_{wt}^{M/2-n} /N \tag{5}$$

712

713   Which gives the number of permutations of n mutant and $M/2 - n$ wildtype mtDNA

714   copies, weighted by the probability of transfer p_{mut} and p_t respectively, and divided by a

715   normalisation constant N. As the primary oocyte contains half of mitochondria from 8 cells,

716   it needs to undergo 2 fewer rounds of replication during oocyte maturation. Hence only 10

717   rounds of replication following **Eq(3)** are carried out in this case to restore the original level

718   of ploidy.

719

720   For all three models (bottleneck, follicular atresia and cytoplasmic transfer), the frequency

721   distribution of mutation loads after these steps is used as the starting point for the next

722   generation.

723

724   3.   Evolutionary dynamics and model accuracy

725   The processes described above are iterated until the Kullback-Leibler divergence (a

726   theoretical measure of how two probability distributions differ from each other [86])

727   between the new and the old distribution is smaller than a threshold $\eta = 10^{-9}$. We then

728   assume that the system has reached a stationary state, *e.g.* without significant changes in

729   the overall distribution of mutation loads between generations (mutation-selection

730   balance).

731

732   In order to compare the prediction of the model with the clinical data, we use the

733   equilibrium distribution to calculate the fraction of the population which carries a

734   detectable load of mitochondrial mutations but does not manifest any detrimental

735   phenotype (α_1) and the fraction of individuals affected by mitochondrial disease (α_2) using a

736   threshold of 60% mutation load to discriminate between carrier and disease status.

737   Individuals are assumed to be mutation free beyond the detection threshold of 2% [4].

738

739   The accuracy of the model is evaluated as the logarithm of the probability of reproducing

740   clinical data by sampling the theoretical distribution at random. This is calculated as follows:

741   let X_1 be the number of healthy individuals with detectable mutation load, and X_2 be the

742   number of individuals affected by mitochondrial diseases; N_1 and N_2 the total number of

743   individuals in the two trials; α_1 and α_2 the probability of observing, respectively, a healthy

744   individual with detectable mutation load and an individual affected by mitochondrial

745   disease, according to the prediction of the model. The log-likelihood of observing X_1 and

746   X_2 by random sampling the theoretical distribution is given by

$$\log(\lambda_{tot}(\mu, M, \dots) = log\left[\prod_{i=1}^{2} p(X_i|\alpha_i(\mu, M, \dots))\right]$$

$$= \sum_{i=1}^{2} \log\left[\binom{N_i}{X_i}\alpha_i^{N_i}(1 - \alpha_i)^{N_i - X_i}\right]$$

$$= \sum_{i=1}^{2} log\binom{N_i}{X_i} + N_i\alpha_i + (N_i - X_i)(1 - \alpha_i)$$

(6)

747

748   **Estimation of the deleterious mutation rate**

749   The parameter values for the deleterious mutation rate we investigate reflect data collected

750   from a number of species. Estimates of mtDNA point mutation rates in the crustacean

751   *Daphnia pulex* range between 1.37×10^{-7} and 2.28×10^{-7} per site per generation [87].

752   Assuming this rate applies to humans and there are $\sim$20 cell divisions before oocyte

753 maturation, leads to a range between 0.68×10^{-8} and 1.14×10^{-8} per site, per cell

754 division. Analysis of *Caenorhabditis elegans* mtDNA leads to a similar estimate of

755 $\sim 1.6 \times 10^{-7}$ per site, per generation [88], which corresponds to a rate of 0.8×10^{-8} per

756 site, per cell division. For *Drosophila melanoganster*, the mtDNA mutation rate yields an

757 estimate of 6.2×10^{-8} per site, per generation, and hence $\sim 0.31 \times 10^{-8}$ per site, per cell

758 division [89]. Finally, analysis of human mtDNA point mutation rates give a mutation rate of

759 0.0043 per genome per generation [75], corresponding to $\sim 1.3 \times 10^{-8}$ mutations per site,

760 per cell division.

761

762 These values do not take into account the presence of a number of processes likely to

763 remove mutants and is therefore a conservative estimate. The loss of mutations would

764 mean that the actual mutation rate is higher than the estimates above. But unlike nuclear

765 rates, the compact structure of mtDNA where intergenic sequences are absent or limited to

766 a few bases, means that the rate of point mutations is probably not much higher than the

767 rate of deleterious mutations. Therefore, for this study we consider a broad interval of

768 possible deleterious mutation rates, labelled as low (10^{-9}), standard (10^{-8}) and high

769 (10^{-7}).

770

771   **FIGURE LEGENDS**

772

773   **Figure 1**

774   **Stages in female germline development.**

775   (**A**) Timeline of human oocyte development showing the main stages modelled, with

776   wildtype (blue) and mutant mitochondria (orange). (**B**) Numerical simulation of the base

777   model. Top panel: number of germ cells from specification of the 32 primordial germ cells

778   (PGCs) after 12 cell divisions; proliferation to form 8 million oogonia; random cell death

779   reducing to 1 million primary oocytes; quiescent period (not shown) and finally oocyte

780   maturation at puberty. Middle panel: copy number of mitochondria (i.e. mtDNA); from

781   zygote with ~500,000 copies, which are partitioned at cell division during early embryo

782   development until replication begins (first vertical line) during PGC proliferation; copy

783   number is amplified during oocyte maturation back to ~500,000 copies; dotted line shows

784   the mean mitochondria copy number, with the distribution across oocytes shown in yellow.

785   Note, skew reflects the log-scale. Bottom panel: mean (dotted line) and distribution of

786   mutation load through development. The yellow shaded area shows the 90% quantile.

787   Other parameter values $\mu = 10^{-8}$, $m_0 = 0.1$.

788

789   **Figure 2** with 1 supplement

790   **Model of germline bottleneck and individual selection.**

791   (**A**) A bottleneck with two extra rounds of cell division without replication (cell division 13

792   and 14; after the first vertical line), reducing mitochondria copy number per PGC (by a

793   quarter on average). Two extra rounds of mitochondrial replication are required to

794   regenerate the copy number in mature oocytes. Compared to the base model (**Figure 1**),

795   mean mutation load (dotted line, bottom panel) is slightly higher and variation in load is

796   substantially greater (yellow shaded area, 90% quantile). Parameter values $\mu = 10^{-8}$,

797    $m_0 = 0.1$. (**B**) Violin plots of the distribution of mutations (mean ± SD shown in red) at two

798   developmental stages, PGC specification and mature oocytes, given 5 mean bottleneck sizes

799   ($\bar{B}$) when $m_0 = 0.1$. (**C**) Strength of selection on individual fitness, with a concave fitness

800   function based on clinical data from mitochondrial diseases[27,28]. (**D**) Change in mutation load

801   (Δm) across a single generation for three initial mutation loads (m_0), given 5 mean

802   bottleneck sizes ($\bar{B}$), showing the median (red line) and distribution (box plot IQR with

803   min/max whiskers and outliers).

804

805   **Figure 2 – figure supplement 1**

806   **Bottleneck change in mutation load with different mutation rates.**

807   Change in mutation load (Δm) across a single generation after individual selection with

808   variable mean bottleneck size ($\bar{B}$). This is shown with (**A**) low ($\mu = 10^{-9}$) and (**B**) high

809   ($\mu = 10^{-7}$) mutation rate, for individuals with low ($m_0 = 0.001$), medium ($m_0 = 0.01$) and

810   high ($m_0 = 0.1$) initial mutation loads. Box plots show the median (red line) and distribution

811   (box plot IQR with min/max whiskers and outliers).

812

813   **Figure 3** with 1 supplement

814   **Model of follicular atresia and cell selection.**

815   (**A**) After PGC proliferation, follicular atresia occurs through selective apoptosis of oogonia.

816   (**B**) Cell fitness is assumed to be linear ($\xi = 1$) or follow negative epistasis ($\xi = 2, 5$) in

817   which mutations are more deleterious in combination. (**C**) Change in mutation load, Δm,

818   across a single generation after cell selection, at an intermediate mutation rate ($\mu = 10^{-8}$),

819   for individuals with low ($m_0 = 0.001$), medium ($m_0 = 0.01$) and high ($m_0 = 0.1$) initial

820   mutation loads, for variable levels of epistasis (median (red line) and distribution (box plot

821   IQR with min/max whiskers and outliers)).

822

823   **Figure 3 – figure supplement 1**

824   **Follicular atresia and cell selection change in mutation load with different mutation rates.**

825   Change in mutation load (Δm) across a single generation after cell selection with variable

826   levels of epistasis (ξ). This is shown with (**A**) low ($\mu = 10^{-9}$) and (**B**) high ($\mu = 10^{-7}$)

827   mutation rate, for individuals with low ($m_0 = 0.001$), medium ($m_0 = 0.01$) and high

828   ($m_0 = 0.1$) initial mutation loads. Box plots show the median (red line) and distribution (box

829   plot IQR with min/max whiskers and outliers).

830

831   **Figure 4** with 2 supplements

832   **Model of cytoplasmic transfer and mitochondria selection.**

833   (**A**) Cytoplasmic bridges form among oogonia in the germline cyst, leading to selective

834   transfer of wild-type mitochondria (blue) to the primary oocyte, leaving mutant

835   mitochondria (red) in nurse cells that then undergo apoptosis. (**B**) Cytoplasmic transfer

836   which selectively pools $f = 50\%$ of mtDNA from 8 germline cyst cells into a single primary

837   oocyte causes a large increase in the number of mitochondria (middle panel) and a large

838   reduction in the mean (dotted line, bottom panel) and distribution of mutation load (yellow

839   shaded area shows the 90% quantile, bottom panel), which persists during oocyte

840   maturation. Pooling of mtDNA requires two fewer rounds of mtDNA replication to

841   regenerate copy number in mature oocytes. Parameter values $\mu = 10^{-8}$, $m_0 = 0.1$. (**C**)

842   Change in mutation load (Δm) across a single generation (median (red line) and distribution

843   (box plot IQR with min/max whiskers and outliers)), for individuals with low ($m_0 = 0.001$),

844   medium ($m_0 = 0.01$) and high ($m_0 = 0.1$) initial mutation loads, with variable strengths of

845   selective transfer (p_{mut}). Parameter value $\mu = 10^{-8}$.

846

847   **Figure 4 – figure supplement 1**

848   **Cytoplasmic transfer and mitochondria selection change in mutation load with different**

849   **mutation rates and proportion of transferred mitochondria (f).**

850   Change in mutation load (Δm) across a single generation, given a variable proportion of

851   transferred mitochondria (f) to the Balbiani body when transfer is non-selective ($p_{mut} =$

852    $p_{wt} = 0.5$). This is shown with (**A**) low ($\mu = 10^{-9}$), (**B**), standard ($\mu = 10^{-8}$) and (**C**) high

853   ($\mu = 10^{-7}$) mutation rate, for individuals with low ($m_0 = 0.001$), medium ($m_0 = 0.01$) and

854   high ($m_0 = 0.1$) initial mutation loads. Box plots show the median (red line) and distribution

855   (box plot IQR with min/max whiskers and outliers).

856

857   **Figure 4 – figure supplement 2**

858   **Cytoplasmic transfer and mitochondria selection change in mutation load with different**

859   **mutation rates and probability of mutant transfer (p_{mut}).**

860   Change in mutation load (Δm) across a single generation, for individuals undergoing

861   cytoplasmic transfer the Balbiani body with variable strength of selection, given a fixed

862   probability of transfer of wildtype mitochondria ($p_{wt} = 0.5$) and a decreasing probability of

863   transfer of mutant mitochondria (p_{mut}). Note the null case is when ($p_{mut} = p_{wt} = 0.5$).

864   This is shown with (**A**) low ($\mu = 10^{-9}$) and (**B**) high ($\mu = 10^{-7}$) mutation rate, for individuals

865   with low ($m_0 = 0.001$), medium ($m_0 = 0.01$) and high ($m_0 = 0.1$) initial mutation loads,

866   and a fixed proportion of transferred mitochondria ($f = 0.5$). Box plots show the median

867   (red line) and distribution (box plot IQR with min/max whiskers and outliers).

868

869   **Figure 5**

870   **Log-likelihood of the models reproducing clinical data of mitochondria mutation load and**

871   **disease frequency.**

872   Heatmaps showing log-likelihood of reproducing the observed mutation load and disease

873   frequency in humans, for equilibrium conditions under the evolutionary model with (**A**)

874   bottleneck and selection on individuals, (**B**) follicular atresia and selection on cells ($\xi = 5$),

875   (**C**) cytoplasmic transfer with intermediate ($p_{mut} = 0.33, p_{wt} = 0.67, f = 0.5$) or (**D**) strong

876   ($p_{mut} = 0.25, p_{wt} = 0.75, f = 0.5$) selective transfer of wildtype mitochondria. Yellow

877   depicts high likelihood; blue, low likelihood. All models are shown for variable bottleneck

878   size (the minimum mitochondria population size at which replication commences) and

879   variable mutation rates.

880

881

889

890 **DECLARATION OF INTERESTS**: none.

891

892 **DATA AND MATERIALS AVAILABILITY**: All code will be posted on Github on publication.

REFERENCES

1.   Lynch M, Koskella B, Schaack S. Mutation pressure and the evolution of organelle genomic architecture. Science. 2006;311:1727-39.
2.   Allio R, Donega S, Galtier N, Nabholz B. Large variation in the ratio of mitochondrial to nuclear mutation rate across animals: Implications for genetic diversity and the use of mitochondrial DNA as a molecular marker. Mol Biol Evol. 2017;34:2762-72.
3.   Rand DM. The units of selection on mitochondrial DNA. Annu Rev Ecol Sys. 2001;32:415-48.
4.   Elliott HR, Samuels DC, Eden JA, Relton CL, Chinnery PF. Pathogenic mitochondrial DNA mutations are common in the general population. Am J Hum Genet. 2008;83:254-60.
5.   Schaefer AM, Blakely EL, He L, Whittaker RG, Taylor RW, Chinnery PF, et al. Prevalence of mitochondrial DNA disease in adults. Ann Neurol. 2008;63:35-9.
6.   Fonseca RR, Johnson WE, Brien SJO, Ramos MJ, Antunes A. The adaptive evolution of the mammalian mitochondrial genome. BMC Genomics. 2008;9:119.
7.   James JE, Piganeau G, Eyre-Walker A. The rate of adaptive evolution in animal mitochondria. Mol Biol Evol. 2016;25:67-78.
8.   Yang Z, Nielsen R. Mutation-selection models of codon substitution and their use to estimate selective strengths on codon usage. Mol Biol Evol. 2008;25:568-79.
9.   Stewart JB, Freyer C, Elson JL, Wredenberg A, Cansu Z, Trufunovic A, et al. Strong purifying selection in transmission of mammalian mitochondrial DNA. PLoS Biol. 2008;6:63-71.
10.   Fan W, Waymire KG, Narula N, Li P, Rocher C, Coskun PE, et al. A mouse model of mitochondrial disease reveals germline selection against severe mtDNA mutations. Science. 2008;319:958-63.
11.   Hill JH, Chen Z, Xu H. Selective propagation of functional mitochondrial DNA during oogenesis restricts the transmission of a deleterious mitochondrial variant. Nat Genet. 2014;46:389-92.
12.   Burr SP, Pezet M, Chinnery PF. Mitochondrial DNA heteroplasmy and purifying selection in the mammalian female germ line. Dev Growth Differ. 2018;60:21-32.
13.   Johnston IG, Burgstaller JP, Havlicek V, Kolbe T, Rulicke T, Brem G, et al. Stochastic modelling, bayesian inference, and new in vivo measurements elucidate the debated mtDNA bottleneck mechanism. eLife. 2015;4:e07464.
14.   Floros VI, Pyle A, Dietmann S, Wei W, Tang WCW, Irie N, et al. Segregation of mitochondrial DNA heteroplasmy through a developmental genetic bottleneck in human embryos. Nat Cell Biol. 2018;20(2):144-51. doi: 10.1038/s41556-017-0017-8.
15.   Stewart JB, Chinnery PF. The dynamics of mitochondrial DNA heteroplasmy : implications for human health and disease. Nat Rev Genet. 2015;16:530-42.
16.   Wai T, Teoli D, Shoubridge EA. The mitochondrial DNA genetic bottleneck results from replication of a subpopulation of genomes. Nat Genet. 2008;40:1484-8.
17.   Cree LM, Samuels DC, de Sousa Lopes SC, Rajasimha HK, Wonnapinij P, Mann JR, Dahl, et al. A reduction of mitochondrial DNA molecules during embryogenesis explains the rapid segregation of genotypes. Nat Genet. 2008;40:249-54.
18.   Cao L, Shitara H, Sugimoto M, Hayashi J, Abe K, Yonekawa H. New evidence confirms that the mitochondrial bottleneck is generated without reduction of mitochondrial DNA content in early primordial germ cells of mice. PLoS Genet. 2009;5:e1000756.

938   19.   Rebolledo-Jaramillo B, Su MS-W, Stoler N, McElhoe JA, Dickins B, Blankenberg D, et
939   al. Maternal age effect and severe germ-line bottleneck in the inheritance of human
940   mitochondrial DNA. Proc Natl Acad Sci U S A. 2014;111(43):15474. doi:
941   10.1073/pnas.1409328111.
942   20.   Guo Y, Li C-I, Sheng Q, Winther JF, Cai Q, Boice JD, et al. Very low-level heteroplasmy
943   mtDNA variations are inherited in humans. J Genet Genomics. 2013;40(12):607-15. Epub
944   2013/12/08. doi: 10.1016/j.jgg.2013.10.003. PubMed PMID: 24377867.
945   21.   Li M, Rothwell R, Vermaat M, Wachsmuth M, Schröder R, Laros JFJ, et al.
946   Transmission of human mtDNA heteroplasmy in the Genome of the Netherlands families:
947   support for a variable-size bottleneck. Genome Res. 2016;26(4):417-26. Epub 2016/02/25.
948   doi: 10.1101/gr.203216.115. PubMed PMID: 26916109.
949   22.   Bergstrom C, Pritchard J. Germline bottlenecks and the evolutionary maintenance of
950   mitochondrial genomes. Genetics. 1998;149(4):2135-46. PubMed PMID: 9691064.
951   23.   Roze D, Rousset F, Michalakis Y. Germline bottlenecks, biparental inheritance and
952   selection on mitochondrial variants: a two-level selection model. Genetics.
953   2005;170(3):1385-99. Epub 2005/05/23. doi: 10.1534/genetics.104.039495. PubMed PMID:
954   15911581.
955   24.   Hadjivasiliou Z, Lane N, Seymour RM, Pomiankowski A. Dynamics of mitochondrial
956   inheritance in the evolution of binary mating types and two sexes. Proc R Soc B Biol Sci.
957   2013;280:20131920.
958   25.   Radzvilavicius AL, Lane N, Pomiankowski A. Sexual conflict explains the extraordinary
959   diversity of mechanisms regulating mitochondrial inheritance. BMC Biol. 2017;14.
960   26.   Krakauer DC, Mira A. Mitochondria and germ-cell death. Nature. 1999;400:125-6.
961   27.   Chu H. P., Liao Y, Novak JS, Hu Z, Merkin JJ, Shymkiv Y, et al. Germline quality
962   control : eEF2K stands guard to eliminate defective oocytes. Dev Cell. 2014;28:561-72.
963   28.   Haig D. Intracellular evolution of mitochondrial DNA (mtDNA) and the tragedy of the
964   cytoplasmic commons. BioEssays. 2016;38:549-55.
965   29.   Albamonte MS WM, Albamonte MI, Jensen F, Espinosa MB, and Vitullo AD. The
966   developing human ovary : immunohistochemical analysis of germ-cell-specific VASA protein,
967   BCL-2 / BAX expression balance and apoptosis. Hum Reprod. 2008;23:1895-901.
968   30.   Kaipia A, Hsueh AJW. Regulation of ovarian follicle atresia. Annual Review of
969   Physiology. 1997;59(1):349-63. doi: 10.1146/annurev.physiol.59.1.349.
970   31.   Townson DH, Combelles CMH. Ovarian Follicular Atresia. Darwish A, editor: InTech;
971   2012.
972   32.   Suganuma N, Kitagawa T, Nawa A, Tomoda Y. Human ovarian aging and
973   mitochondrial DNA deletion. Horm Res. 1993;39:16-21. Epub 1993/01/01. doi:
974   10.1159/000182752. PubMed PMID: 8365704.
975   33.   Galimov ER, Chernyak BV, Sidorenko AS, Tereshkova AV, Chumakov PM. Prooxidant
976   properties of p66shc are mediated by mitochondria in human cells. PLoS One.
977   2014;9(3):e86521-e. doi: 10.1371/journal.pone.0086521. PubMed PMID: 24618848.
978   34.   Cummins JM. The role of mitochondria in the establishment of oocyte functional
979   competence. Eur J Obstet Gynecol Reprod Biol. 2004;115:S23-9. doi:
980   https://doi.org/10.1016/j.ejogrb.2004.01.011.
981   35.   Nezis IP, Stravopodis DJ, Papassideri I, Robert-Nicoud M, Margaritis LH. Stage-
982   specific apoptotic patterns during Drosophila oogenesis. European Journal of Cell Biology.
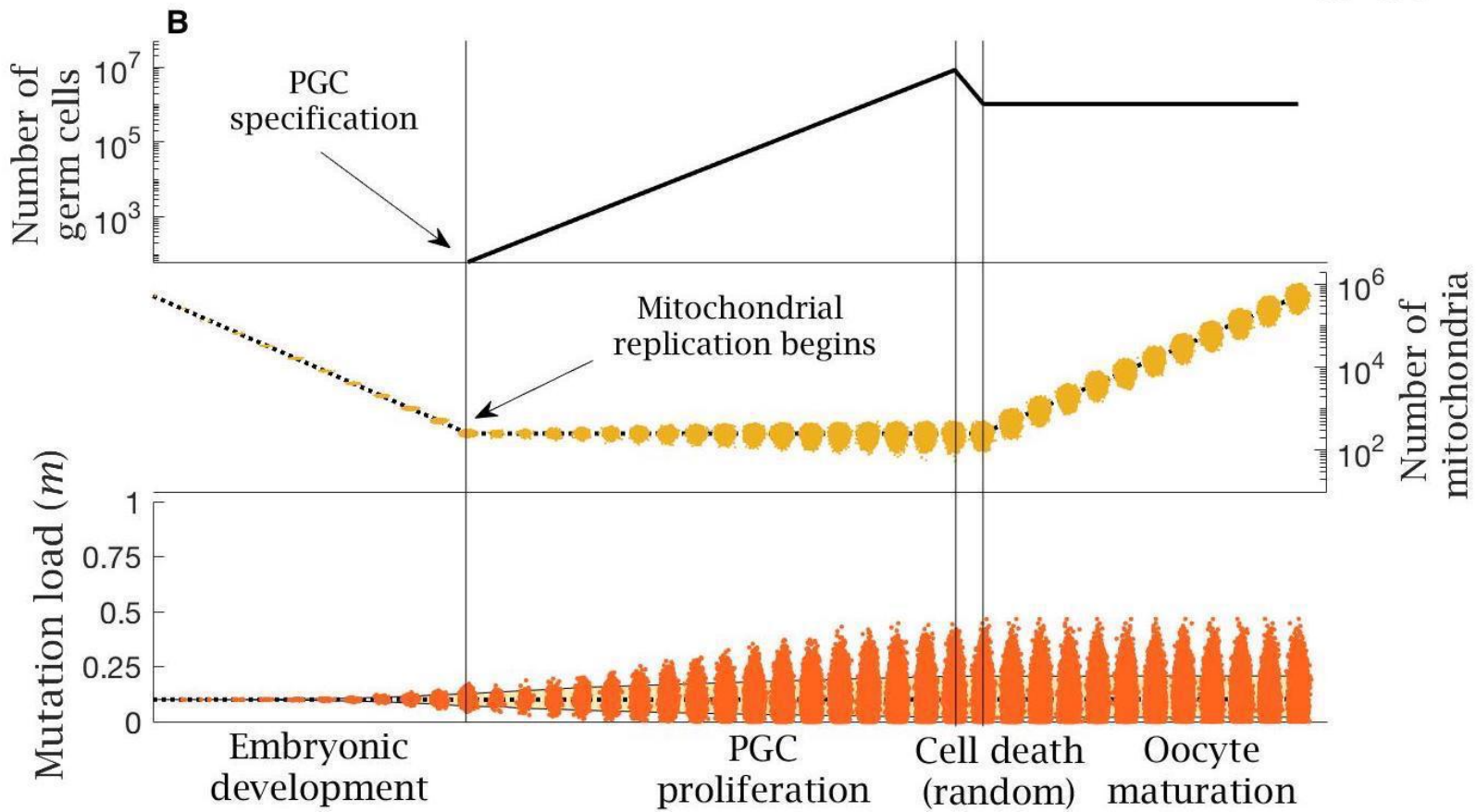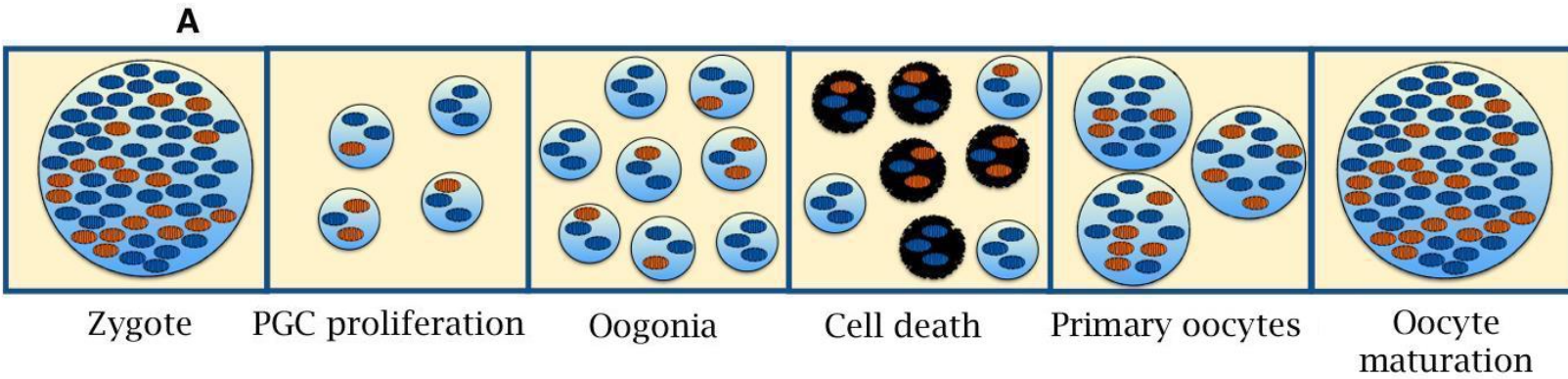983   2000;79(9):610-20. doi: https://doi.org/10.1078/0171-9335-00088.

984   36.   Rodrigues P, Limback D, McGinnis LK, Plancha CE, Albertini DF. Multiple mechanisms
985   of germ cell loss in the perinatal mouse ovary. Reproduction. 2009;137(4):709-20.
986   37.   Saidapur SK. Follicular atresia in the ovaries of nonmammalian vertebrates.
987   International review of cytology. 1978;54:225-44.
988   38.   Morita Y, Tilly JL. Oocyte apoptosis: like sand through an hourglass. Developmental
989   biology. 1999;213(1):1-17.
990   39.   Tilly JL. Commuting the death sentence: how oocytes strive to survive. Nat Rev Mol
991   Cell Biol. 2001;2:838-48.
992   40.   Perez GI, Trbovich AM, Gosden RG, Tilly JL. Mitochondria and the death of oocytes.
993   Nature. 2000;403(6769):500-1. doi: 10.1038/35000651.
994   41.   Lei L, Spradling AC. Mouse oocytes differentiate through organelle enrichment from
995   sister cyst germ cells. Science. 2016;252:95-9.
996   42.   Motta PM, Nottola SA, Makabe S, Heyn R. Mitochondrial morphology in human fetal
997   and adult female germ cells. Human Reproduction. 2000;15(suppl_2):129-47. doi:
998   10.1093/humrep/15.suppl_2.129.
999   43.   Hertig AT. The primary human oocyte: some observations on the fine structure of
1000 Balbiani's vitelline body and the origin of the annulate lamellae. American Journal of
1001 Anatomy. 1968;122(1):107-37.
1002 44.   Kloc M, Bilinski S, Etkin LD. The Balbiani body and germ cell determinants: 150 years
1003 later. Curr Top Dev Biol. 2004;59:1-36.
1004 45.   Tworzydlo W, Kisiel E, Jankowska W, Witwicka A, Bilinski SM. Exclusion of
1005 dysfunctional mitochondria from Balbiani body during early oogenesis of Thermobia. Cell
1006 Tissue Res. 2016;366(1):191-201. Epub 2016/05/10. doi: 10.1007/s00441-016-2414-x.
1007 PubMed PMID: 27164893.
1008 46.   Reunov A, Alexandrova Y, Reunova Y, Komkova A, Milani L. Germ plasm provides
1009 clues on meiosis: the concerted action of germ plasm granules and mitochondria in
1010 gametogenesis of the clam Ruditapes philippinarum. Zygote. 2019;27(1):25-35. Epub
1011 2018/12/07. doi: 10.1017/S0967199418000588.
1012 47.   Larkman AU. The fine structure of mitochondria and the mitochondrial cloud during
1013 oogenesis on the sea anemone Actinia. Tissue and Cell. 1984;16:393-404.
1014 48.   Heasman J, Quarmby J, Wylie CC. The mitochondrial cloud of Xenopus oocytes: The
1015 source of germinal granule material. Developmental Biology. 1984;105(2):458-69. doi:
1016 https://doi.org/10.1016/0012-1606(84)90303-8.
1017 49.   Pepling ME, Wilhelm JE, Hara AL, Gephardt GW, Spradling AC. Mouse oocytes within
1018 germ cell cysts and primordial follicles contain a Balbiani body. Proc Natl Acad Sci U S A.
1019 2007;104(1):187. doi: 10.1073/pnas.0609923104.
1020 50.   Zhou RR, Wang B, Wang J, Schatten H, Zhang YZ. Is the mitochondrial cloud the
1021 selection machinery for preferentially transmitting wild-type mtDNA between generations?
1022 Rewinding Müller's ratchet efficiently. Curr Genet. 2010;56:101-7.
1023 51.   Bilinski SM, Kloc M, Tworzydlo W. Selection of mitochondria in female germline cells:
1024 is Balbiani body implicated in this process? J Assist Reprod Genet. 2017;34:1405-12.
1025 52.   Moore AS, Coscia SM, Simpson CL, Ortega FE, Wait EC, Heddleston JM, et al. Actin
1026 cables and comet tails organize mitochondrial networks in mitosis. Nature.
1027 2021;591(7851):659-64. doi: 10.1038/s41586-021-03309-5.
1028 53.   Taguchi N, Ishihara N, Jofuku A, Oka T, Mihara K. Mitotic phosphorylation of
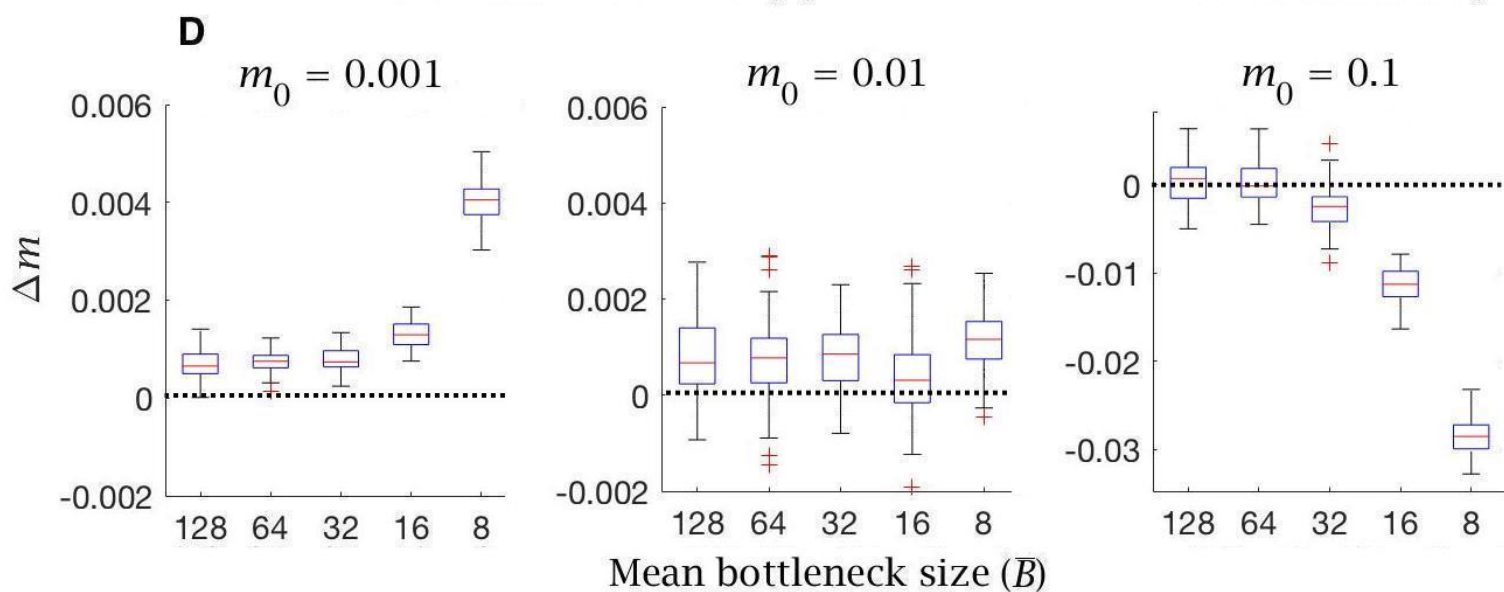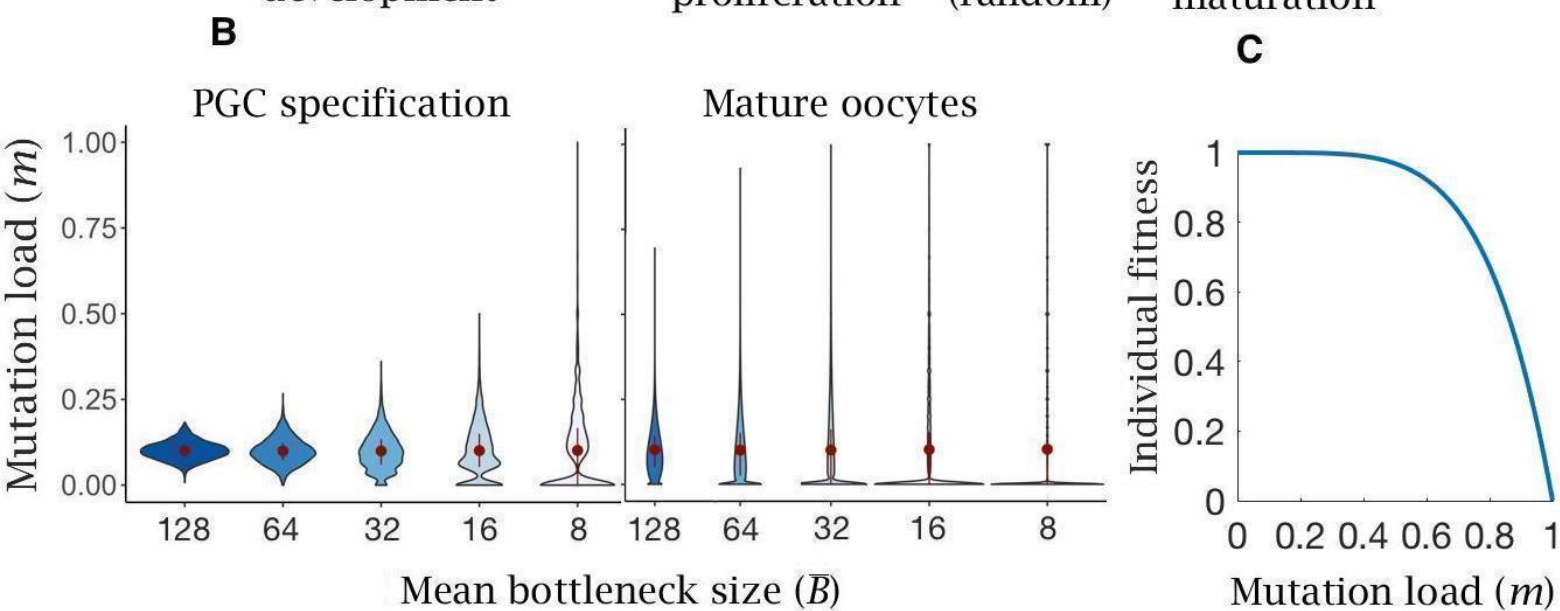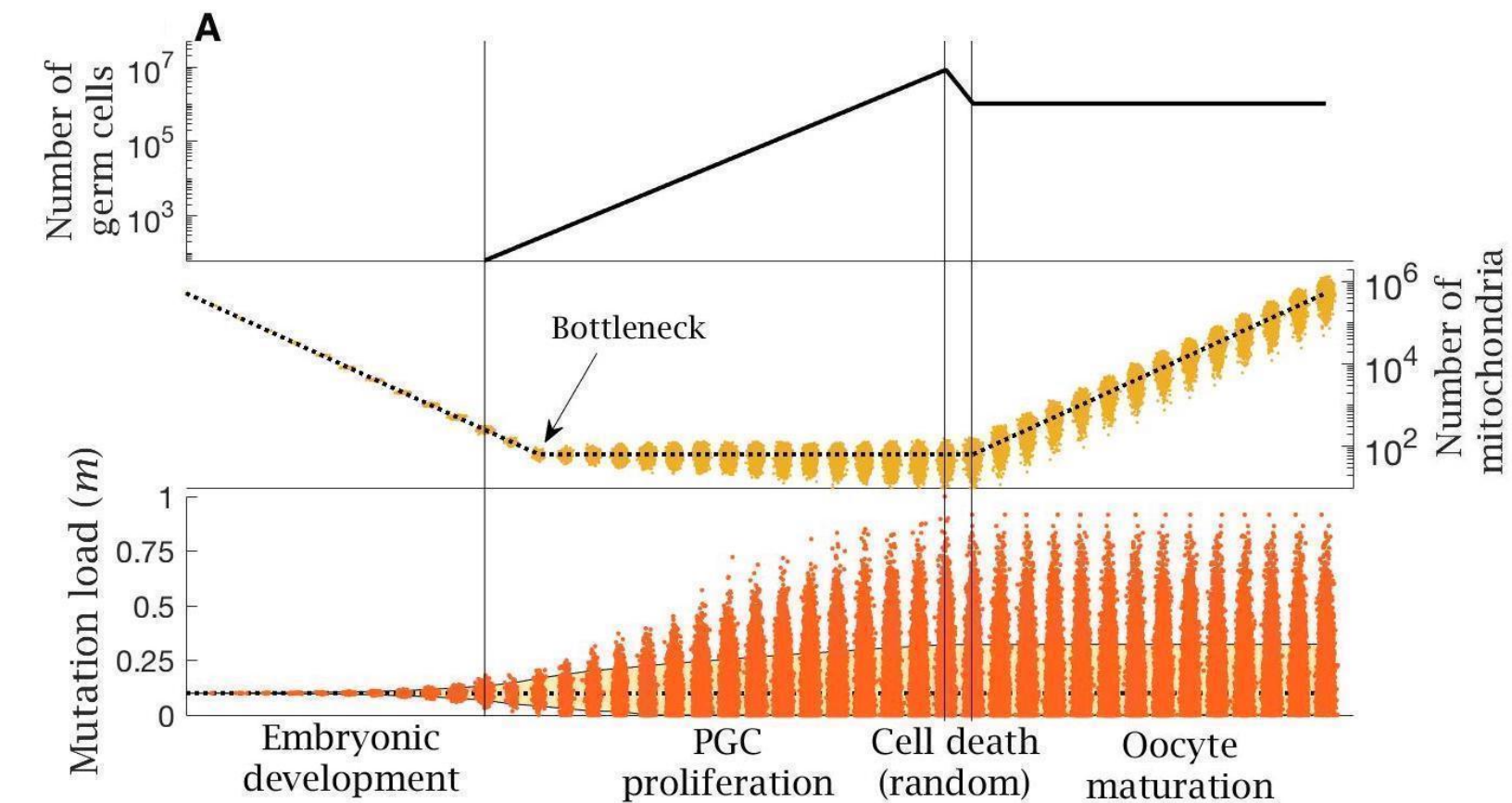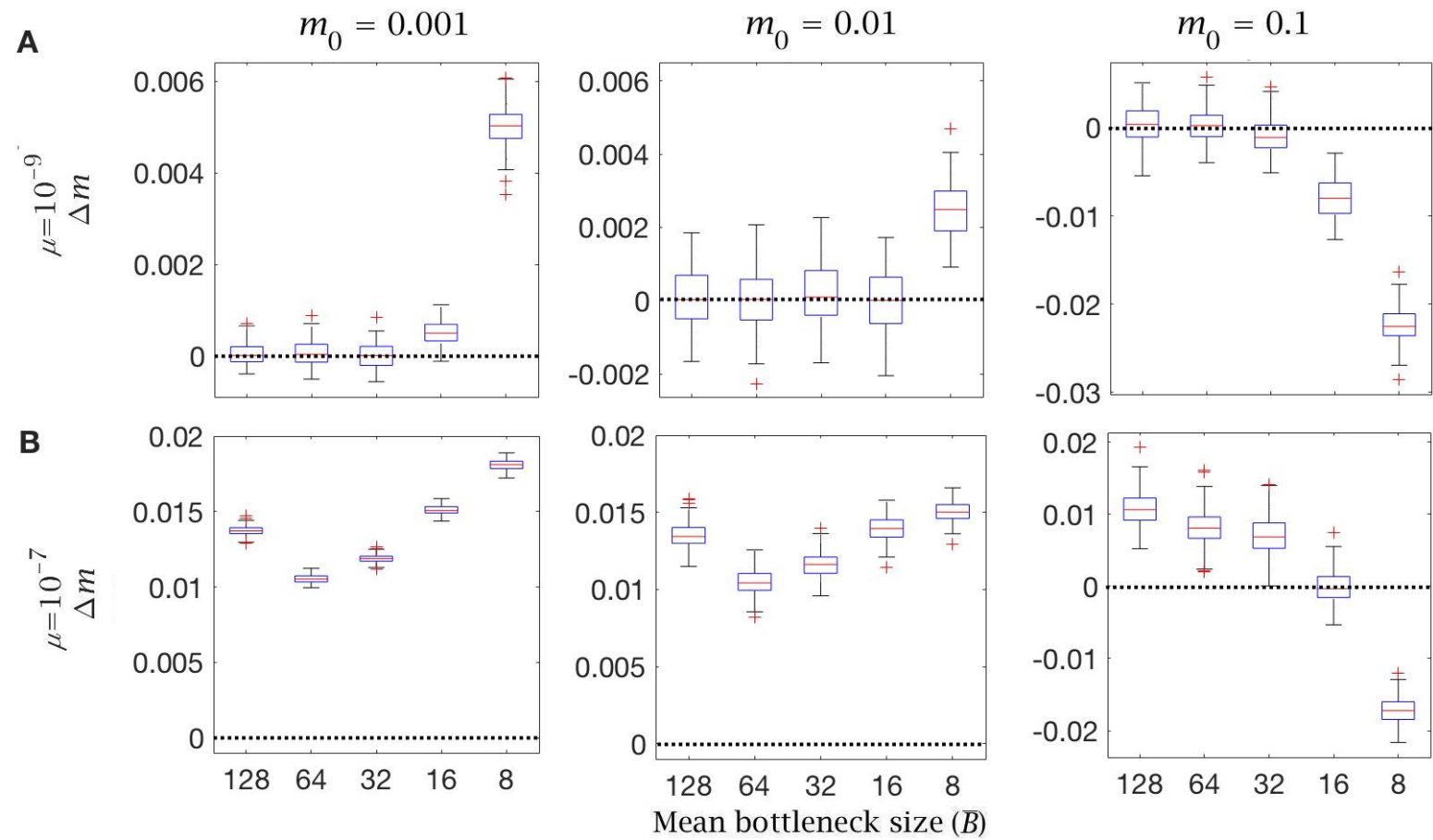1029 dynamin-related GTPase Drp1 participates in mitochondrial fission. J Biol Chem.

1030 2007;282(15):11521-9. Epub 2007/02/16. doi: 10.1074/jbc.M607279200. PubMed PMID:
1031 17301055.
1032 54.   Park YY, Cho H. Mitofusin 1 is degraded at G2/M phase through ubiquitylation by
1033 MARCH5. Cell Div. 2012;7(1):25. Epub 2012/12/21. doi: 10.1186/1747-1028-7-25. PubMed
1034 PMID: 23253261; PubMed Central PMCID: PMCPMC3542011.
1035 55.   Dumollard R, Duchen M, Carroll J. The role of mitochondrial function in the oocyte
1036 and embryo. Curr Top Dev Biol. 2007;77:21-49.
1037 56.   Extavour CG, Akam M. Mechanisms of germ cell specification across the metazoans:
1038 epigenesis and preformation. Development. 2003;130:5869-84.
1039 57.   Stewart JB, Larsson N-G. Keeping mtDNA in shape between generations. PLoS Genet.
1040 2014;10(10):e1004670-e. doi: 10.1371/journal.pgen.1004670. PubMed PMID: 25299061.
1041 58.   Allen J, de Paula W. Mitochondrial genome function and maternal inheritance.
1042 Biochem Soc Trans. 2013;41:1298-304.
1043 59.   Radzvilavicius AL, Hadjivasiliou Z, Pomiankowski A, Lane N. Selection for
1044 mitochondrial quality drives evolution of the germline. PLoS Biol. 2016;14:e2000410.
1045 60.   Rossignol R, Faustin B, Rocher C, Malgat M, Mazat JP, Letellier T. Mitochondrial
1046 threshold effects. Biochem J. 2003;370:751-62.
1047 61.   Kopinski PK, Janssen KA, Schaefer PM, Trefely S, Perry CE, Potluri P, et al. Regulation
1048 of nuclear epigenome by mitochondrial DNA heteroplasmy. Proc Natl Acad Sci U S A.
1049 2019;116(32):16028-35. Epub 2019/06/30. doi: 10.1073/pnas.1906896116. PubMed PMID:
1050 31253706; PubMed Central PMCID: PMCPMC6689928.
1051 62.   Wallace DC, Chalkia D. Mitochondrial DNA genetics and the heteroplasmy
1052 conundrum in evolution and disease. Cold Spring Harb Perspect Biol. 2013;5:a021220.
1053 63.   Chen Z, Wang ZH, Zhang G, Bleck CKE, Chung DJ, Madison GP, et al. Mitochondrial
1054 DNA segregation and replication restrict the transmission of detrimental mutation. J Cell
1055 Biol. 2020;219(7). Epub 2020/05/07. doi: 10.1083/jcb.201905160. PubMed PMID:
1056 32375181; PubMed Central PMCID: PMCPMC7337505.
1057 64.   Pepling ME. From primordial germ cell to primordial follicle: mammalian female
1058 germ cell development. Genesis. 2006;44(12):622-32. doi: 10.1002/dvg.20258.
1059 65.   de Paula WBM, Lucas CH, Agip A-NA, Vizcay-Barrena G, Allen JF. Energy, ageing,
1060 fidelity and sex: oocyte mitochondrial DNA as a protected genetic template. Philos Trans R
1061 Soc B. 2013;368(1622):20120263. doi: 10.1098/rstb.2012.0263.
1062 66.   Arbeithuber B, Hester J, Cremona MA, Stoler N, Zaidi A, Higgins B, et al. Age-related
1063 accumulation of de novo mitochondrial mutations in mammalian oocytes and somatic
1064 tissues. PLOS Biol. 2020;18(7):e3000745. doi: 10.1371/journal.pbio.3000745.
1065 67.   Trifunovic A, Hansson A, Wredenberg A, Rovio AT, Dufour E, Khvorostov I, et al.
1066 Somatic mtDNA mutations cause aging phenotypes without affecting reactive oxygen
1067 species production. Proc Natl Acad Sci U S A. 2005;102(50):17993-8. Epub 2005/12/08. doi:
1068 10.1073/pnas.0508886102. PubMed PMID: 16332961; PubMed Central PMCID:
1069 PMCPMC1312403.
1070 68.   Lanfear L. Do plants have a segregated germline? PLoS Biol. 2018;16:e2005439.
1071 69.   Extavour CG. Evolution of the bilaterian germ line: lineage origin and modulation of
1072 specification mechanisms. Integrative and comparative biology. 2007;47(5):770-85.
1073 70.   Blackstone NW, Jasker BD. Phylogenetic considerations of clonality, coloniality, and
1074 mode of germline development in animals. Journal of Experimental Zoology Part B:
1075 Molecular and Developmental Evolution. 2003;297(1):35-47.

71. Cox RT, Spradling AC. A Balbiani body and the fusome mediate mitochondrial inheritance during *Drosophila* oogenesis. Development. 2003;130(8):1579. doi: 10.1242/dev.00365.

72. Twig G, Elorza A, Molina AJA, Mohamed H, Wikstrom JD, Walzer G, et al. Fission and selective fusion govern mitochondrial segregation and elimination by autophagy. EMBO J. 2008;27(2):433-46. doi: 10.1038/sj.emboj.7601963.

73. Kim I, Rodriguez-Enriquez S, Lemasters JJ. Selective degradation of mitochondria by mitophagy. Arch Biochem Biophys. 2007;462(2):245-53. doi: https://doi.org/10.1016/j.abb.2007.03.034.

74. Dalton CM, Carroll J. Biased inheritance of mitochondria during asymmetric cell division in the mouse oocyte. J Cell Sci. 2013;126(13):2955-64. Epub 2013/05/09. doi: 10.1242/jcs.128744. PubMed PMID: 23659999.

75. Sigurdardottir S, Helgason A, Gulcher JR, Donnelly P. The mutation rate in the human mtDNA control region. Am J Hum Genet. 2000;66:1599-609.

76. Stewart JB, Chinnery PF. The dynamics of mitochondrial DNA heteroplasmy: implications for human health and disease. Nat Rev Genet. 2015;16(9):530-42. Epub 2015/08/19. doi: 10.1038/nrg3966. PubMed PMID: 26281784.

77. Shoubridge EA, Wai T. Mitochondrial DNA and the mammalian oocyte. Curr Top Dev Biol. 2007;77:87-111. Epub 2007/01/16. doi: 10.1016/s0070-2153(06)77004-1. PubMed PMID: 17222701.

78. Lane N. Power, Sex, Suicide: Mitochondria and the Meaning of Life: Oxford University Press; 2005.

79. Pereira CV, Gitschlag BL, Patel MR. Cellular mechanisms of mtDNA heteroplasmy dynamics. Critical Reviews in Biochemistry and Molecular Biology. 2021:1-16.

80. Carelli V, Maresca A, Caporali L, Trifunov S, Zanna C, Rugolo M. Mitochondria: biogenesis and mitophagy balance in segregation and clonal expansion of mitochondrial DNA mutations. The international journal of biochemistry & cell biology. 2015;63:21-4.

81. Diot A, Morten K, Poulton J. Mitophagy plays a central role in mitochondrial ageing. Mammalian Genome. 2016;27(7):381-95.

82. Buss L. The Evolution of Individuality: Princeton University Press; 1987.

83. Maynard Smith J, Szathmáry E. The Major Transitions in Evolution: Oxford University Press; 1995.

84. Reynier P, May-Panloup P, Chretien M, Morgan C, Jean M, Savagner F, et al. Mitochondrial DNA content affects the fertilizability of human oocytes. Molecular human reproduction. 2001;7(5):425-9.

85. Palca J. The other human genome. Science. 1990;249:1104-5.

86. Kullback S, Leibler RA. On Information and Sufficiency. Ann Math Statist. 1951;22(1):79-86. doi: 10.1214/aoms/1177729694.

87. Xu S, Schaack S, Seyfert A, Choi E, Lynch M, Cristescu ME. High mutation rates in the mitochondrial genomes of *Daphnia pulex*. Mol Biol Evol. 2012;29(2):763-9. Epub 2011/10/13. doi: 10.1093/molbev/msr243. PubMed PMID: 21998274.

88. Denver DR, Morris K, Lynch M, Vassilieva LL, Thomas WK. High Direct Estimate of the Mutation Rate in the Mitochondrial Genome of *Caenorhabditis elegans*. Science. 2000;289(5488):2342. doi: 10.1126/science.289.5488.2342.

89. Haag-Liautard C, Coffey N, Houle D, Lynch M, Charlesworth B, Keightley PD. Direct estimation of the mitochondrial DNA mutation rate in *Drosophila melanogaster*. PLoS Biol. 2008;6(8):e204. doi: 10.1371/journal.pbio.0060204. PubMed PMID: 18715119.

1123

A

Zygote | PGC proliferation | Oogonia | Cell death | Primary oocytes | Oocyte maturation

B

Number of germ cells

10^7

10^5

10^3

PGC specification

Mitochondrial replication begins

Number of mitochondria

10^6

10^4

10^2

Mutation load (m)

1

0.75

0.5

0.25

0

Embryonic development | PGC proliferation | Cell death (random) | Oocyte maturation

A

Number of germ cells

Bottleneck

Number of mitochondria

Mutation load (m)

Embryonic development   PGC proliferation   Cell death (random)   Oocyte maturation

B

PGC specification   Mature oocytes

Mutation load (m)

Mean bottleneck size ($\bar{B}$)

C

Individual fitness

Mutation load (m)

D

$m_0 = 0.001$ $m_0 = 0.01$ $m_0 = 0.1$

Δm

Mean bottleneck size ($\bar{B}$)

A

Number of germ cells

Number of mitochondria

Mutation load (m)

Embryonic development

PGC proliferation

Selective atresia

Oocyte maturation

B

Cell fitness

Mutation load (m)

ξ
1
2
5

C

$m_0 = 0.001$

$m_0 = 0.01$

$m_0 = 0.1$

Δm

Epistasis (ξ)

A

$m_0 = 0.001$ $m_0 = 0.01$ $m_0 = 0.1$

$\mu = 10^{-9}$
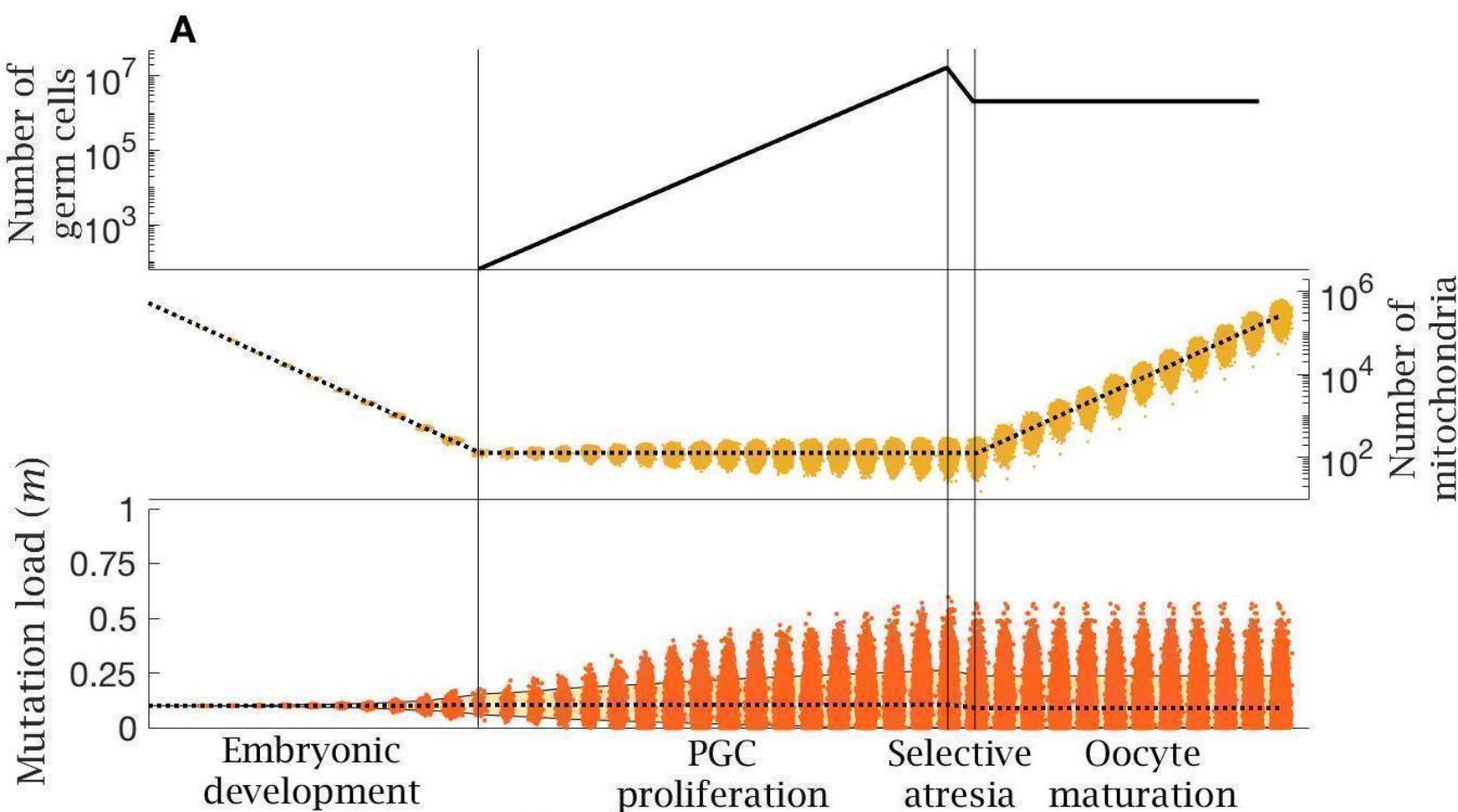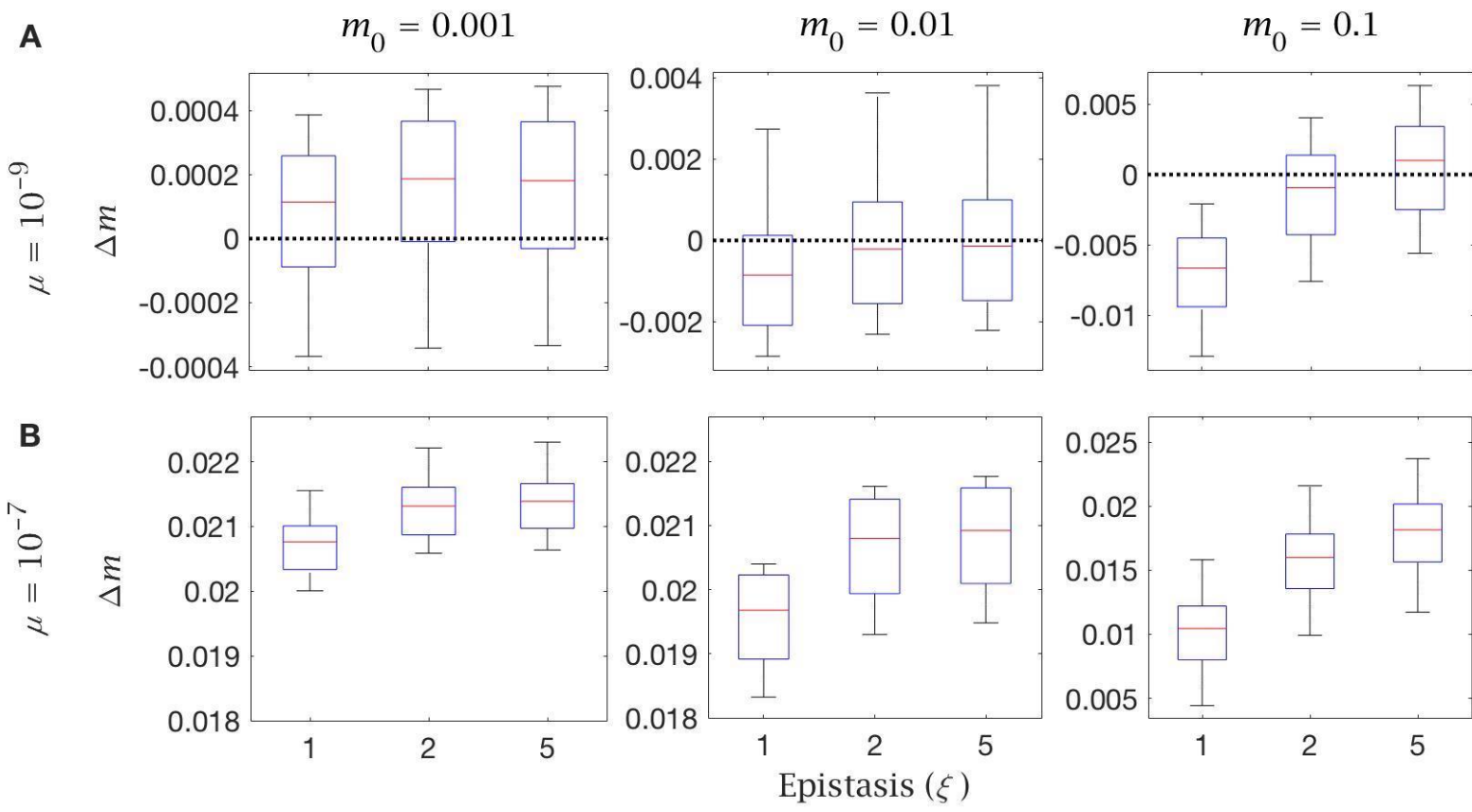
Δm

B

$\mu = 10^{-7}$

Δm

Epistasis (ξ)

A

Germline cyst Cytoplasmic transfer Nurse cell death

B

Number of germ cells

10^7

10^5

10^3

Number of mitochondria

10^6

10^4

10^2

Mutation load (m)

1

0.75

0.5

0.25
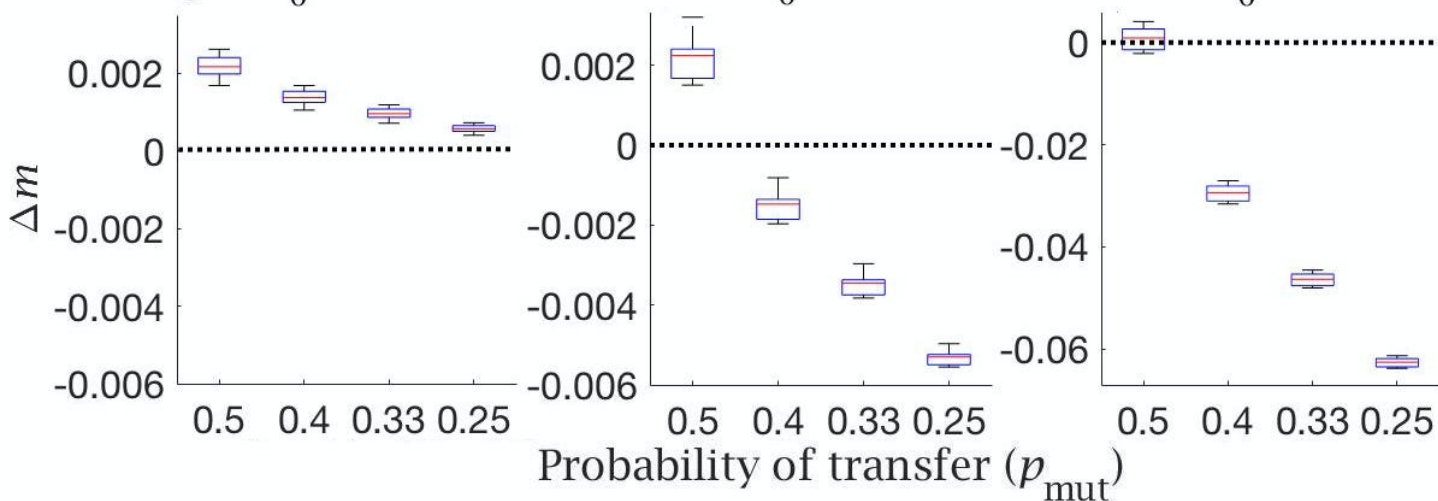
0
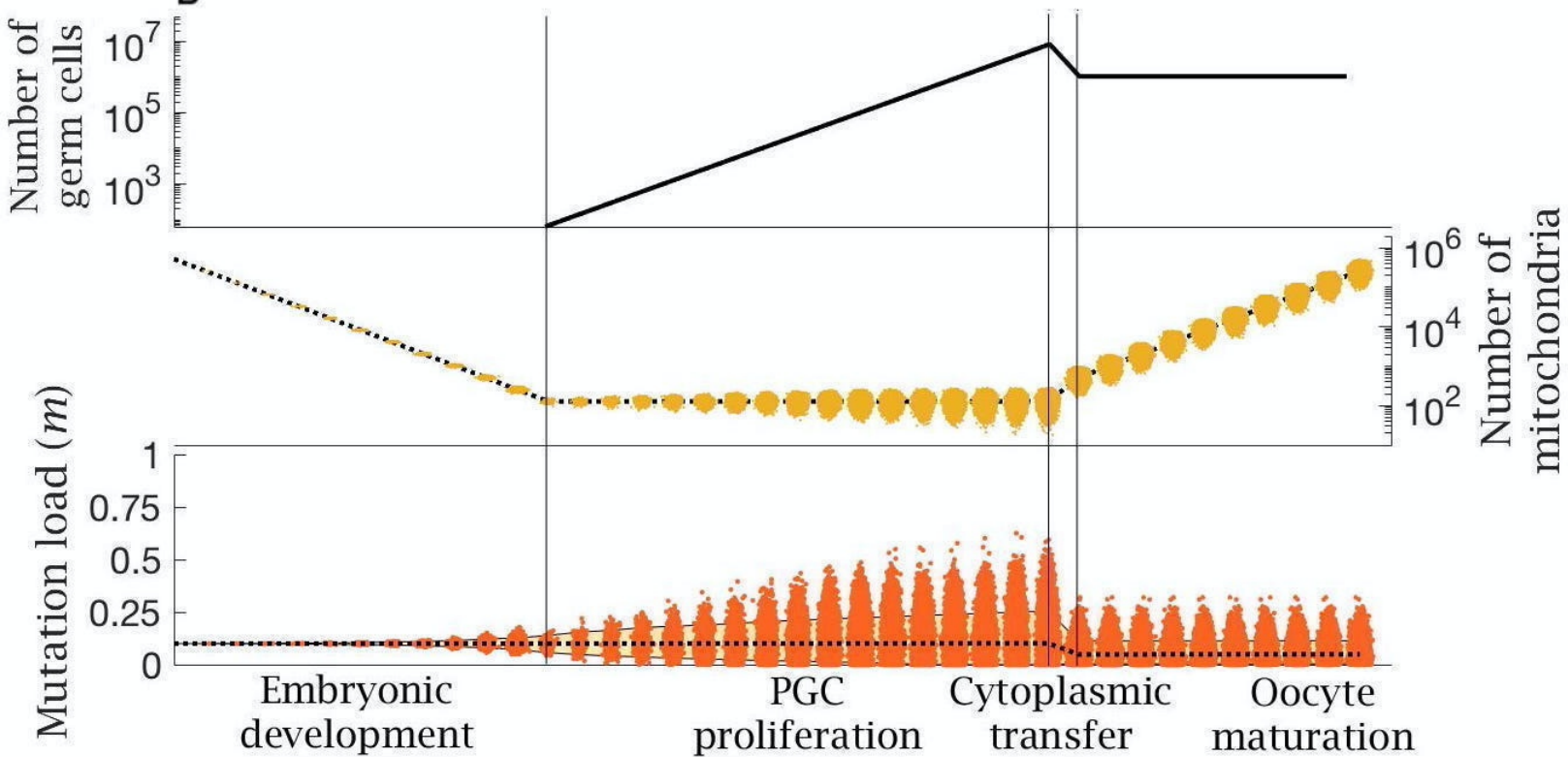
Embryonic development · PGC proliferation · Cytoplasmic transfer · Oocyte maturation

C

$m_0 = 0.001$ $m_0 = 0.01$ $m_0 = 0.1$

Δm

0.002

0

−0.002

−0.004

−0.006

0.002

0

−0.002

−0.004

−0.006

0

−0.02

−0.04

−0.06

0.5 0.4 0.33 0.25 0.5 0.4 0.33 0.25 0.5 0.4 0.33 0.25

Probability of transfer (p_{mut})

Proportion of transferred mitochondria (f)

A

$m_0 = 0.001$

$m_0 = 0.01$

$m_0 = 0.1$

$\mu=10^{-9}$
Δm

B

$\mu=10^{-7}$
Δm

Probability of transfer (p_{mut})

A Between-individual selection

B Between-cell selection

C Selective transfer (intermediate)

D Selective transfer (strong)