



Article Eliminating Stick-Slip Vibrations in Drill-Strings with a Dual-Loop Control Strategy Optimised by the CRO-SL Algorithm

Jorge Pérez-Aracil^{1,*}, Carlos Camacho-Gómez², Emiliano Pereira¹, Vahid Vaziri³, Sumeet S. Aphale³ and Sancho Salcedo-Sanz¹

- ¹ Department of Signal Processing and Communications, Universidad de Alcalá, Alcalá de Henares, 28805 Madrid, Spain; emiliano.pereira@uah.es (E.P.); sancho.salcedo@uah.es (S.S.-S.)
- ² Department of Information Systems, Universidad Politécnica de Madrid, Campus Sur, 28031 Madrid, Spain; carlos.camacho@upm.es
- ³ School of Engineering, University of Aberdeen, Aberdeen AB24 3UE, UK; vahid.vaziri@abdn.ac.uk (V.V.); s.aphale@abdn.ac.uk (S.S.A.)
- * Correspondence: jorge.perezraracil@uah.es

Abstract: Friction-induced stick-slip vibrations are one of the major causes for down-hole drill-string failures. Consequently, several nonlinear models and control approaches have been proposed to solve this problem. This work proposes a dual-loop control strategy. The inner loop damps the vibration of the system, eliminating the limit cycle due to nonlinear friction. The outer loop achieves the desired velocity with a fast time response. The optimal tuning of the control parameters is carried out with a multi-method ensemble meta-heuristic, the Coral Reefs Optimisation algorithm with Substrate Layer (CRO-SL). It is an evolutionary-type algorithm that combines different search strategies within a single population, obtaining a robust, high-performance algorithm to tackle hard optimisation problems. An application example based on a real nonlinear dynamics model of a drill-string illustrates that the controller optimised by the CRO-SL achieves excellent performance in terms of stick-slip vibrations cancellation, fast time response, robustness to system parameter uncertainties and chattering phenomenon prevention.

Keywords: stick-slip; drill-strings; vibration control; coral reefs optimisation; meta-heuristics

1. Introduction

Stick-slip phenomena occur when, due to a particular confluence of parameters, the bit–rock interaction is such that rather than a constant (ideally synchronous) rotating speed of the top drive and the drill-bit, the drill-bit speed varies between zero and six times the speed of the top drive at the top of the drill-string. This unwanted phenomenon severely impacts the achieved rate of penetration during most drilling operations. In severe cases, this can lead to faster degradation of drill-bits and in rare cases warping or breaking of the drill-string models have been proposed in the literature [2–5]. Consequently, several drill-string models have also been proposed and validated [4,6,7]. The importance of the stick-slip vibrations problem has been widely analysed in [8–11]. In these previous works, researchers focus on understanding of the drill-string dynamics, the bit–rock interaction and the quantification of stick-slip vibrations. The current research aims to reduce the effects of the stick-slip phenomena during the drilling operation.

Vibration control in nonlinear systems is a problem that can be solved by linear and nonlinear controllers [3,12]. These controllers may be designed by using optimisation algorithms [13]. The problem of mitigating stick-slip vibrations in drill-strings is a well-known nonlinear control problem [3]. Some of the more recent and noteworthy approaches include the bit speed and torque independent stick-slip compensator [14], sliding-mode



Citation: Pérez-Aracil, J.; Camacho-Gómez, C.; Pereira, E.; Vaziri, V.; Aphale, S.S.; Salcedo-Sanz, S. Eliminating Stick-Slip Vibrations in Drill-Strings with a Dual-Loop Control Strategy Optimised by the CRO-SL Algorithm. *Mathematics* **2021**, *9*, 1526. https:// doi.org/10.3390/math9131526

Academic Editor: Stevan Dubljevic

Received: 1 June 2021 Accepted: 25 June 2021 Published: 29 June 2021

Publisher's Note: MDPI stays neutral with regard to jurisdictional claims in published maps and institutional affiliations.



Copyright: © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). controllers [15], feedback controllers by including the axial and torsional motions in the numerical model [16], the use of robust controllers based on proportional-derivative feedback control design to keep a constant drill-bit rotation speed [17]. The use of Kalman filter based full-state feedback controllers was proposed in [18]. Sliding-mode controllers have shown very good results in the problem of reducing stick-slip vibration issues [19–21]. This fact arises from the good qualities of this controller, such as: robustness against inaccuracies related to the model and/or unpredicted dynamics. It also has a wide disturbance rejection and broad control bandwidth. It has been recently presented in [15,22] for eliminating stick-slip vibrations. The use of proportional-integral-derivative (PID) motivated linear controllers have also been proposed to address the stick-slip [23].

The complexity of the design of vibration controllers for drill-strings justifies the use of optimisation algorithms; in many cases, these are meta-heuristics approaches. Thus, the problem of stick-slip vibration has been solved by using optimisation algorithms [24,25]. In Reference [24], a torsional vibration control approach based on the genetic algorithm is studied. In [25], the authors show the use of a dynamic programming technique to design the optimal control of nonlinear systems. The Nelder-Mead method has been applied to design the controllers of multiple isolators situated on the same supporting structure [26]. In addition, some variants of the well-known genetic meta-heuristics algorithm have been applied to structural optimisation problems. In [27], the authors proposed a fuzzy control and a genetic algorithm for structural shape optimisation. In [28], the optimisation of 3D trusses was tackled with a Grouping Genetic Algorithm (GGA). In [29], a microgenetic algorithm (μ -GA) was used for impact load identification and characterisation of concrete structures. For the plane stress problem, a variant of the Evolutionary Structural Optimisation (ESO) algorithm was proposed in [30]. Finally, in [31], the GA and among other meta-heuristic methods were implemented to obtain the optimal parameters in the welded beam structure problem. The particle swarm optimisation (PSO) algorithm introduced in [32] is also an important meta-heuristic that has been successfully applied to structural optimisation problems such as in [33], where the so-called democratic-PSO was proposed for truss layout with frequency constraints, or in [34], where optimal sizing design of truss structures was studied. The teaching-learning-based algorithm [35] has also been applied to optimise mechanical design problems [36,37]. The Harmony Search (HS) approach [38] has also been applied to structural optimisation; however, in [39], the authors aimed at two main ideas: firstly, they gathered a large number of meta-heuristics that have been used in structural optimisation; secondly, they reflected about the lack of mathematical background in meta-heuristics basics and the contributions of the HS. In the last decade, a new kind of meta-heuristics based on physics phenomena have been applied to structural optimisation problems. The Big-Bang Big-Crunch algorithm was updated in [40] to a memetic algorithm by mixing it with a local search process called the quasi-Newton method and was proposed to find the optimal weight of the structure. The Colliding Bodies Optimisation [41], the Ray Optimisation [42] or the Charged System Search [43] algorithms were created by A. Kaveh and tested in the welded beam design problem.

The concept of modified output, which was firstly introduced in [44], is used in this paper to propose a new control approach for eliminating stick-slip vibrations in drillstrings. The controller is based on a dual-loop linear control scheme. The inner loop, whose feedback signal is a combination of output signals, damps the vibration of the system, eliminating the limit cycle due to nonlinear friction. The outer loop achieves the desired velocity with a fast time response. The performance of the controller is improved by the use of a multi-method ensemble meta-heuristic, the Coral Reefs Optimisation algorithm with Substrate Layer (CRO-SL) [45,46], is adopted. This ensemble method was successfully applied in other engineering problems, such as [47–49]. In [47], the problem of optimal design and location of tuned mass dampers for structures subjected to earthquake ground motions is solved. In [48], the complex problem of design and location of inertial mass dampers for floor based structures subjected to human induced vibration is tackled. In [49], the design of submerged arch structures is approached. All the problems show that CRO-SL can be suitable for obtaining global optimum designs, with affordable computation time in complex vibration control problems. Consequently, the CRO-SL algorithm is applied to find the best configuration of the control parameters, i.e., obtaining the four controller parameters needed to eliminate stick-slip vibrations in a drill-string model with system uncertainties. The objective function to solve the problem is a functional that considers vibration, steady-state error and control effort.

The structure of the remainder of the paper is as follows: Section 2 presents the mathematical model of the drill-string, the bit–rock interaction and the model verification. Section 3 describes the proposed control scheme along with the CRO-SL optimisation algorithm, including the definition of a substrate layerand how this approach can be considered as a multi-method ensemble optimisation algorithm. Section 4 presents the optimisation results as well as the closed-loop results for the drill-string system, where the proposed algorithm's performance is evaluated. Section 5 closes the paper by giving some final conclusions and remarks on this research.

2. System Model

To realistically reproduce the stick-slip phenomena occurring in drill-strings and enable the implementation and testing of various control schemes, a scaled drill-string piece of equipment was set up at the Centre for Applied Dynamics Research, University of Aberdeen [22]. The following subsections describe the two-degrees-of-freedom (DOF) mathematical model that accurately captures the drill-string dynamics. The bit–rock interaction model is also described along with the system parameters on which the presented control design and analysis is based on.

2.1. Mathematical Model

As mentioned above, a 2-DOF model that accurately captures the stick-slip vibrations experienced by the drill-string is adopted. This is to ensure that the model is accurate, adequate and not overcomplicated. There are several works that have adopted a similar 2-DOF model [2,6,7,50].

The model lumps the drill-string components into two discs: (i) The upper disc that represents the top-drive system and (ii) the lower disc that represents the drill bit. Between the upper (top drive) and lower disc (drill bit), the drill-string is placed, mainly composed from a drill pipe and bottom hole assemble (BHA). A simple schematic of this model is shown in Figure 1. As labelled in Figure 1, the input torque that drives the system is denoted by *U*. The angular position of top drive is ϕ_r , its viscous damping is c_r , and the inertia J_r . The pipe, which connects the top drive with the BHA, is modelled by its torsional damping *C* and the torsional stiffness *K*. The torque of friction on the lower disc, which models the interaction between the bit and the rock, is denoted by T_b . The angular position of the BHA is ϕ_b , and its inertia is J_b .

The equation of motion that encapsulates the entire system behaviour is then given by:

$$\ddot{\phi}_r = \frac{U}{J_r} - \frac{C_r + C}{J_r} \dot{\phi}_r + \frac{C}{J_r} \dot{\phi}_b - \frac{K}{J_r} (\phi_r - \phi_b)$$
(1)

$$\ddot{\phi}_b = \frac{C}{J_b} \dot{\phi}_r - \frac{C}{J_b} \dot{\phi}_b + \frac{K}{J_b} (\phi_r - \phi_b) - \frac{T_b}{J_b}$$
(2)

However, to facilitate control design, the new state of the system can be initialised as follows:

$$x = (\dot{\phi}_r, \phi_r - \phi_b, \dot{\phi}_b)^T = (x_1, x_2, x_3)^T$$
(3)

which further simplifies the system equation to:

$$\dot{x}_1 = \frac{U}{J_r} - \frac{C_r + C}{J_r} x_1 + \frac{C}{J_r} x_3 - \frac{K}{J_r} x_2$$
(4)

$$\dot{x}_2 = x_1 - x_3$$
 (5)

$$\dot{x}_3 = \frac{C}{J_b} x_1 - \frac{C}{J_b} x_3 + \frac{K}{J_b} x_2 - \frac{T_b}{J_b}$$
(6)



Figure 1. Schema of the 2-DOF lumped-parameter model of the drill-string.

Equations (3)–(6) can be re-described as the following state-space system:

$$\dot{x} = \begin{bmatrix} -\frac{C_r + C}{J_r} & -\frac{K}{J_r} & \frac{C}{J_r} \\ 1 & 0 & -1 \\ \frac{C}{J_b} & \frac{K}{J_b} & \frac{C}{J_b} \end{bmatrix} x + \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \frac{U}{J_r} + \begin{bmatrix} 0 \\ 0 \\ -1 \end{bmatrix} \frac{T_b}{J_b}.$$
(7)

The problem of drill-string can be modelled as a linear part (Equation (7)) connected with the hard nonlinear model of the bit–rock interaction. This interaction is modelled by the torque T_b in Equation (7). This is explained below.

2.2. Bit-Rock Interaction

It is possible to distinguish three different phases in the bit–rock interaction: (i) stick phase: the drill-bit is not rotation since it is stuck with the rock, (ii) stick-to-slip phase: to begin slipping, the drill-bit has to achieve enough torque, (iii) slip phase: the drill-bit rotates and it is actually drilling [4,15,51,52].

It is important to note that the system is locked between phases (ii) and (iii). The sticking phase ends when the reaction torque reaches the peak value. The slip phase starts when the drill-bit starts to rotate. For $x_3 = 0$, the dry friction is estimated by combining a zero band velocity introduced in [53] and the switch model in [54].

When $x_3 = 0$, the dry friction is approximated by combining a zero band velocity introduced in [53] and the switch model in [54]. This is as follows:

$$T_{b} = \left\{ \begin{array}{ll} \tau_{r}, & \text{if} |x_{3}| < \zeta \quad \text{and} \quad |\tau_{r}| \leq \tau_{s} \\ \tau_{s} \cdot sgn(\tau_{r}), & \text{if} |x_{3}| < \zeta \quad \text{and} \quad |\tau_{r}| > \tau_{s} \\ \mu_{b} \cdot R_{b} \cdot W_{ob} \cdot sgn(x_{3}), & \text{if} |x_{3}| \geq \zeta \end{array} \right\},$$
(8)

where *sgn* stands for the *sign* function,

$$sgn(x) = \left\{ egin{array}{ccc} 1 & x > 0 \\ 0 & x = 0 \\ -1 & x < 0 \end{array}
ight.$$

The frictional torque when the drill–bit interaction occurs can be formulated as $\tau_r = C(x_1 - x_3) + K(x_2)$, which is the reaction torque, whilst $\tau_s = \mu_{sb}R_bW_{ob}$ is the friction torque, μ_{sb} is the static friction coefficient, W_{ob} is the Weight on Bit (WOB), R_b is the bit radius. A set of drill-string realistic simulation parameters was obtained in [2,22], and these parameters are tabulated in Table 1.

Table 1. The basic realistic drill-string physical parameters for the model.

Parameters	Values	
Jr	13.93 kg \cdot m ²	
J_b	$1.1378 \text{ kg} \cdot \text{m}^2$	
С	$0.005 \text{ N} \cdot \text{m} \cdot \text{s/rad}$	
K	$10 \text{ N} \cdot \text{m/rad}$	
C_r	$11.38 \text{ N} \cdot \text{m} \cdot \text{s/rad}$	
μ_{sb}	0.0843	
μ_{cb}	0.0685	
R_b	0.0492 m	
γ_b	0.3	
$ u_f$	0.1935	
ζ	10^{-4}	

3. Control Design and Parameter Optimisation

The problem of control of stick-slip oscillations in drill-strings bears some similarity to the problem of control of one-link flexible manipulators. It is clear that as the sensors and actuators for these systems (flexible robot and drill-string) are not physically located at the same spot (not co-located). Therefore, these systems are non-minimum phase in nature. Moreover, the Coulomb friction present in the joint of the robotic manipulator can be treated as a complication similar to the drill-string's nonlinear friction in the bit–rock interaction model (presented in Equation (8)). In the case of the flexible manipulator, modified outputs, like the reflected tip position in one-link flexible manipulators [44,55], have been proposed in the past in order to solve this seemingly complicated problem. These modified outputs have been used to propose simple control schemes, which achieves the objectives of tracking and vibration control [44,55,56]. In addition, these controllers guarantee the stability of the highly unconsidered vibration mode (spillover).

The proposed linear control is inspired by the aforementioned controllers applied to flexible robotic manipulators, where the objective is to cancel the vibrations at the tip with an actuator placed at the joint. The proposed controller is shown in Figure 2. Note that there are two nested loops. The first one is used to stabilise the system, cancelling the vibration of drill-string, which is due to the vibration modes of the linear part and the nonlinear dynamics of the bit–rock interaction.

The controlled input of the inner loop (U_{IL}) is as follows:

$$U_{IL} = \frac{\beta}{\alpha} (\phi_r - \phi_b) - \frac{1}{\alpha} \dot{U}_{IL}, \qquad (9)$$

where α and β are the parameters used to obtain the modified output of the drill-string. The objective of the outer loop is to achieve a desired velocity of the top drive. Thus, if the inner loop (9) cancels the vibration, the outer loop can achieve the desired velocity of BHA. This outer loop is as follows:

$$U_{OL} = P(\dot{\phi}_{r,ref} - \dot{\phi}_r) + I(\phi_{r,ref} - \phi_r), \tag{10}$$

where *P* and *I* are the proportional and integral constants of the tracking controller. The proposed control law can then be written as follows:

$$U = U_{IL} + U_{OL}.$$
 (11)



Figure 2. The adopted dual-loop control scheme. The inner loop consists of a damping controller, which uses the modified output $x_2 C_d$, and the outer loop consists of a tracking controller (proportional and integral).

The optimal control parameters are tuned according to a functional, which considered the following issues:

- J_1 : The steady-state error between the desired (top-drive) and achieved (drill-bit) angular velocity $(\dot{\phi}_r \dot{\phi}_{r,ref})$.
- J_2 : The residual vibration $(\dot{\phi}_b \dot{\phi}_r)$.
- J_3 : The settling time of the variables $\dot{\phi}_b$ and $\dot{\phi}_r$

• *J*₄: The control effort from a determined value of time, which rejects solutions with chattering.

The functional is defined as follows:

$$J(\mathbf{z}) = \gamma_1 J_1 + \gamma_2 J_2 + \gamma_3 J_3 + \gamma_4 J_4,$$
(12)

where γ_1 , γ_2 , γ_3 , and γ_4 are the terms that ponderate each sub-functional. These sub-functionals are as follows:

$$J_{1} = \left| \dot{\phi}_{r,ref} - \dot{\phi}_{r}(t_{f}) \right|,$$

$$J_{2} = \max_{t \in (t_{i}, t_{f})} |\dot{\phi}_{b}(t) - \dot{\phi}_{r}(t)|,$$

$$J_{3} = t_{set,r} + t_{set,b},$$

$$I_{4} = \frac{1}{N} \sum_{t=t_{set,r}}^{t_{f}} (U(t) - U_{OL}),$$
(13)

where t_i is the time at which the controller is engaged, t_f is the final value of time considered in simulations and N is the number of samples considered between t_f and t_i . The variables $t_{set,r}$ and $t_{set,b}$ are the settling time of $\dot{\phi}_r$ and $\dot{\phi}_b$ after the value of t_i and considering a final value equal to $\dot{\phi}_{r,ref}$ with an error of ± 4 %. The variable z is defined by the controller parameters: P, I, β and α . Note that the initial conditions of Equation (7) are considered in J_2 , where the max_{$t \in (t_i, t_f)$} $|\dot{\phi}_b(t) - \dot{\phi}_r(t)|$ depends on the system response before t_i . The functional J_1 and J_4 consider the values of $\dot{\phi}_r$ and U after $t_{set,r}$.

Due to the nonlinear nature of the system, control parameter tuning is not straightforward. Thus, a suitable optimisation algorithm can be used in order to automate the process, ensure stable results and significantly improve the control performance. The Coral Reef Optimisation (CRO) is a meta-heuristic algorithm for optimisation that has been recently proposed as a highly-effective algorithm for such problems [48,57–59]. This work uses an improved version of the CRO algorithm to generate the controller parameters namely β , α , P and I.

Coral Reefs Optimisation Algorithm with Substrate Layer: A Multi-Method Ensemble Approach

The CRO-SL is a further version of the original CRO [57], which was founded on the processes that occur in a coral reef, including reproduction, fight for space or depredation [46]. The basics can be shown in the pseudo-code below, Algorithm 1, with the different CRO phases where the individuals (also called corals) are initialised in the population (or reef), along with all the operators applied to guide the search.

Algorithm 1 Pseudo-code for the original CRO

Require: Valid configuration of parameters controlling the CRO algorithm **Ensure:** A single individual with near-optimal value of its *fitness*

- 1: Initialize the corals and the reef
- 2: for each iteration of the experiment do
- 3: Update values of the algorithm parameters
- 4: Sexual reproduction processes for new individuals (also larvae)
- 5: Settlement of new larvae
- 6: Predation of some of the weakest
- 7: The new population is ready for the next generation
- 8: end for
- 9: Return the best individual (final solution) from the reef

As has been mentioned before, the CRO-SL is an improved version of the CRO, firstly proposed in [60] and further developed in [45]. It is considered as a low-level ensemble method for optimisation, which combines several search processes in parallel over different subpopulations and with information exchange between them, leading to extremely good search capabilities. The CRO-SL has the same structure as shown in the pseudo code of the basic CRO, but including substrate layers or subpopulations, wherein each one is implementing a different search procedure or strategy. A substrate may represent different models, operators, parameters, constraints, repairing functions, etc., though this version, which represents different search operators, has been the most successful version so far. Thus, the CRO-SL is an ensemble approach that promotes cooperative co-evolution. The use of CRO-SL as a cooperative multi-method ensemble has been successfully tested in different applications and problems, such as battery scheduling and topology design in micro-grids [58,61], medical image registration [59], antenna design [62] and vibration cancellation problems in buildings [47] and open floors [48]. This wide application demonstrates the potency of the CRO-SL and deems it an ideal candidate for optimising controller parameters for eliminating stick-slip vibrations in drill-strings. Details of the overall CRO-SL algorithm and the mechanism to include substrate layers is well-reported in [45].

Although different search strategies have been defined at the practitioner's discretion, this work has taken into account a five-substrate construct of the CRO-SL. They are briefly described below:

 Harmony Search (HS): It is a metaheuristic method based on stochastic optimisation [38]. It imitates the process found in music improvisation, which searches for better harmony. There are two parameters that determine the way in which new larvae are generated: (i) Harmony Memory Considering Rate (HMCR), which ranges from zero to one. If a uniformly spawned value is above the value of HMCR, then the encoded parameter value is uniformly drawn from the values in the coral, (ii) Pitch Adjusting Rate (PAR), which ranges from zero to one, which sets the probability of choosing a neighbour value of the current larva.

- 2. Differential Evolution (DE): It is an Evolutionary Algorithm (EA), which has good abilities for global search [63]. The new larvae can be generated either by the mutation or crossover process. For a randomly selected encoded parameter, if a uniformly generated value is above the Crossover Probability (CR) value, which ranges from zero to one, the new value is obtained by $x'_i = x^1_i + F(x^2_i x^3_i)$, in which *F* is the evolution factor. Otherwise, the value is crossed with the randomly selected encoded parameter.
- 3. Classical 2-points crossover (2Px): The crossover operator is the most used exploration mechanism in genetic and evolutionary algorithms [64] since its combination with an efficient mutation process allows achieving a suitable balance between exploration and exploitation. 2Px selects two random parents and exchanges the genetic material in-between two random points on them. Despite that each substrate is linked to a searching process, when another parent must be picked, the selection is not limited to their substrate, but it can be chosen from any part of the population instead. The reason is to contribute to genetic information exchange among substrates so they can easily cooperate.
- 4. Multi-points crossover (MPx): This search method is a generalisation of the 2Px. In this case, *k* points are selected in the parents. In this work, due to the dimensionality of the problem, the value of *k* has been chosen to be three. Thus, a binary vector decides whether the parts of each parent are exchanged or not for the new offspring generation.
- 5. Gaussian Mutation (GM): The Gaussian Mutation is a noisy search method based on adding random values from the Gaussian distribution to the encoded parameter values, thus generating an offspring. The standard deviation σ value in this work is linearly decreasing during the run, from $0.2 \cdot (A B)$ to $0.02 \cdot (A B)$, where [B, A] is the domain search. The Gaussian probability density function is:

$$f_{G(0,\sigma^2)}(x) = \frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{x^2}{2\sigma^2}}$$

With the aim of exploring the search space at the beginning of the optimisation process and exploiting it at the end, the parameter σ is adapted during the simulation.

4. Computational Evaluation

This section presents the computational evaluation of the proposed control algorithm for stick-slip vibrations cancellation, optimised with the CRO-SL algorithm. The open-loop parameters of the drill-string system are given in Table 1. The torsional stiffness (*K*) is considered as a variable parameter and the velocity reference ($\dot{\phi}_{r,ref}$) is selected to be within 2 and 5 rad/s (acceptable practical range). The system is simulated for 40 s in an open-loop after which the loop is closed and the proposed dual-loop control scheme is engaged. The value of the control input (*U*) in Equation (11) is limited to $U \in [20, 80]$ N·m. This is to ensure that the control input lies within the practical limits [7,22].

The CRO-SL algorithm searches for the best solution in terms of Equation (12) for $K \in \{5, 10, 20\}$ N·m/rad and $\dot{\phi}_{r,ref} \in \{2, 3, 4, 5\}$. The values of torque needed to obtain this velocity are $U \in \{30.2, 41.42, 52.65, 63.9\}$ N·m. The parameters of Equations (12) and (13) are:

- $\gamma_1 = 1, \gamma_2 = 0.5, \gamma_3 = 0.25 \text{ and } \gamma_3 = 2;$
- $t_i = 40 \text{ s and } t_f = 120 \text{ s};$
- *N* is the result of using a 0.001 s of sampling time. The simulation is carried out by a fourth-order ordinal differential equation solver (Runge–Kutta) with fixed time of 0.001 s (i.e., $N = (120 40)/(0.001 = 80 \times 10^3)$;
- The input torque is, as mentioned earlier, limited to *U* ∈ [20, 80] N·m. The CRO-SL parameters used in the experiments are shown in Table 2.

Parameter	Description	Value
Reef	Reef size	120
F _b	Frequency of broadcast spawning	97%
Substrates	HS, DE, 2Px, MPx, GM	5
\mathcal{N}_{att}	Number of tries for larvae settlement	3
F _a	Percentage of asexual reproduction	5%
F _d	Fraction of corals for depredation	5%
P_d	Probability of depredation	5%
α	Maximum number of iterations	50

Table 2. Parameters values used in the CRO-SL.

The optimisation results obtained with the CRO-SL are presented in Figure 3. Figure 3a shows the ratio for which each substrate generates the best larva in the CRO-SL approach.



Figure 3. Evolution of different quality parameters in the CRO-SL; (**a**) evolution of the number of larvae that are finally allocated into the reef as new solutions; (**b**) ratio of times that each substrate produces the best larva in each iteration of the CRO-SL algorithm; (**c**) evolution of the best solution within the CRO-SL.

It is possible to see how DE is the one exploration operator that contributes the most to the CRO-SL search. The contribution of the GM and 2Px are also significant, but they decrease during the search. Figure 3b shows the number of larvae that are produced in the reef for each iteration, as new solutions. Figure 3c shows the evolution of the best solution within the CRO-SL. It is important to note that around 20 iterations, the proposed approach achieves the optimal solution. The final value of the functional (Figure 3c) is J = 8.1560, which corresponds with K = 10 N·m and $\dot{\phi}_{r,ref} = 5$ rad/s. The controller parameters are shown in Table 3.

Table 3. Optimal control parameters obtained by means of CRO-SL.

Optimal Control Parameters					
Р	Ι	β	α		
$3.33 imes10^4$	$3.51 imes 10^4$	$9.15 imes10^4$	$25 imes 10^{-4}$		

The next subsection shows the performance in terms of stick-slip vibrations cancellation, fast time response, robustness to system parameter uncertainties and chattering phenomenon prevention.

Results

First of all, the closed-loop system configured with the above shown parameters is simulated to generate time responses for the nominal conditions ($K = 10 \text{ N} \cdot \text{m/rad}$ and a $\dot{\phi}_{r,ref} = 2.5 \text{ rad/s}$). The controller starts at 40 s, the value of t_i used in optimal design.

Two values of restrictions for control input torque are used. The first one corresponds to $U \in [20, 80]$ N·m, which is the restriction used in the optimisation process. The second one is a naive selection corresponding to $U \in [-100, 100]$ N·m. Figure 4 shows the angular velocity of the top-drive, drill-bit and input torque signal against the time variable. It is clear after some careful understanding of the system that negative values of control input torque require the top-drive to rotate in the opposite direction to the standard drilling. This is, in practice, an unacceptable scenario as physically reversing the motor's direction of rotation is an almost impossible task on the field. However, it is likely that this might be possible or even required in some scenarios (drill-bit retrieval). The objective of these experiments is to show that the controlled system optimised with the CRO-SL scheme is stable in both scenarios.



Figure 4. Time histories of the angular velocity of the top-drive, drill-bit and input torque signal for a desired velocity (2.5 rad/s) and $K = 10 \text{ N} \cdot \text{m/rad}$: (a) angular velocity of the top-drive and drill-bit when $U \in [20, 80] \text{ N} \cdot \text{m}$; (b) angular velocity of the top-drive and drill-bit when $U \in [-100, 100] \text{ N} \cdot \text{m}$; (c) input torque when $U \in [20, 80] \text{ N} \cdot \text{m}$; (d) input torque when $U \in [-100, 100] \text{ N} \cdot \text{m}$.

Figure 5 shows how the controller of Figure 2 can eliminate the limit cycle of the stick-slip. The controller starts at t = 75 s in order to guarantee that the limit cycle is in steady-state for all the reference values ($\dot{\phi}_{r,ref}(t)$) when $U \in [20, 80]$ N·m (see Figure 5e). Figure 5a,b shows the stick-slip limit cycle in an open-loop for U = 36 N·m and its corresponding 2D phase-plane portrait, respectively. Figure 5c shows the corresponding 3D perspective with respect to time in order to better clarify the transient response. Figure 5d shows the motor torque U. In this example, the open loop torque is U = 36 N·m. The controller is turned on at t = 75 s, and the control input undergoes a brief period of transients, with its permanent value equal to U = 36 N·m. Figure 5e shows how the controller can stabilise the stick-slip for $U \in [30, 69.5]$ N·m. It is important to highlight that desired velocity can be achieved from any initial value of input torque in an open loop.



Figure 5. The red line and the blue line stand for uncontrolled and scheme controlled, respectively. (**a**–**c**) The time-history, 2D and 3D phase-portraits, respectively. (**d**) The control input versus time. (**e**) The complete bifurcation diagram showing all types of behaviour.

An additional robustness analysis is carried out. Figure 6a shows the value of the functional (*J*) as a function of the desired velocity and stiffness value. Figure 6a shows that the maximum value of *J* is achieved for $K = 10 \text{ N} \cdot \text{m/rad}$ and a $\dot{\phi}_{r,ref} = 5 \text{ rad/s}$. In addition, the most unfavourable case for each value of *K* is the maximum value of the desired velocity. Then, three examples are plotted in order to show how the stick-slip limit cycle is cancelled. In these examples, like in Figure 5, the controller starts at t = 75 s in order to guarantee that this vibration is in a steady-state for all the cases. Thus, Figure 6b–d shows how the controlled system eliminates the stick-slip vibrations for *K* equal to 5, 10 and 20 N·m/rad, respectively. Note that, although a large torque control input is needed, after the settling time, all time responses are the same, showing that the controller effectively eliminates the stick-slip vibrations for all these cases. In addition, Figure 6e–g shows the input torque when $U \in [20, 80]$ N·m for *K* equal to 5, 10 and 20 N·m/rad, respectively.





Figure 6. Robustness analysis: (a) value of the functional (*J*) for different values of the desired velocity and stiffness values; (b) angular velocity of the top-drive and drill-bit for $K = 5 \text{ N} \cdot \text{m/rad}$; (c) angular velocity of the top-drive and drill-bit for $K = 10 \text{ N} \cdot \text{m/rad}$; (d) angular velocity of the top-drive and drill-bit for $K = 20 \text{ N} \cdot \text{m/rad}$; (e) input torque when $U \in [20, 80] \text{ N} \cdot \text{m}$ for $K = 5 \text{ N} \cdot \text{m/rad}$; (f) input torque when $U \in [20, 80] \text{ N} \cdot \text{m}$ for $K = 10 \text{ N} \cdot \text{m/rad}$; (g) input torque when $U \in [20, 80] \text{ N} \cdot \text{m}$ for $K = 20 \text{ N} \cdot \text{m/rad}$.

Finally, a final case is simulated in order to show the problem of the control effort (chattering phenomenon), which is avoided by including J_4 (see Equations (12) and (13)), justifying the use of the optimisation algorithm. Thus, the tuning of P, I, β and γ is carried out according to the following practical guide: (i) increases the values of P and I in order to achieve a good time response for the top-drive, (ii) modified β in order to reduce the oscillation between drill-bit and top-drive angular velocities and (iii) tune a small, but not equal to zero, value for α , in order to avoid possible practical problems with offset in x_2 . The control parameters are shown in Table 4.

Non-Optimal Control Parameters					
Р	Ι	β	α		
$5.00 imes10^4$	$5.00 imes10^4$	$9.00 imes10^4$	$30.00 imes 10^{-4}$		

Table 4. Control parameters for the non-optimised case.

Figure 7 shows the time histories for the angular velocity of the top-drive, drill-bit and input torque signal for a desired velocity of 2.5 rad/s and $K = 10 \text{ N} \cdot \text{m/rad}$ (i.e., the nominal conditions). Note that the time responses of the top-drive and the drill-bit are good and comparable with Figure 4. However, the control effort (chattering phenomenon) for both cases is not admissible because it can damage the actuator. In addition, the design of this controller for a wider range of *K* (parameter uncertainty) and desired velocities is not obvious. This justifies the use of CRO-SL, which simplifies and improves the control parameter selection, consequently resulting in improved closed-loop performance.



Figure 7. Non-optimised design: time histories of the angular velocity of the top-drive, drill-bit and input torque signal for a desired velocity (2.6 rad/s) and $K = 10 \text{ N}\cdot\text{m/rad.}$ (**a**) angular velocity of the top-drive and drill-bit when $U \in [20, 80] \text{ N}\cdot\text{m}$; (**b**) Angular velocity of the top-drive and drill-bit when $U \in [-100, 100] \text{ N}\cdot\text{m}$; (**c**) input torque when $U \in [20, 80] \text{ N}\cdot\text{m}$; (**d**) input torque when $U \in [-100, 100] \text{ N}\cdot\text{m}$.

5. Conclusions

This work proposes a dual-loop control strategy to alleviate stick-slip vibration problems in drill-string applications. The inner loop controller is based on the concept of modified output, which has been used in the past to control non-collated systems. The results show that the combination of both velocities, the top-drive and the drill-bit, can eliminate the limit circle of the nonlinear system. The outer loop is used to achieve the desired drill-bit velocity within a low settling time and without steady-state error. The advantages of optimising the controller parameters have also been shown in this work. The controller has been optimally tuned by using a multi-method ensemble meta-heuristic approach, the Coral Reefs Optimisation algorithm with Substrate Layers (CRO-SL). A functional function is defined in this work, which involves: (i) steady-state error, (ii) the residual vibration, (iii) the settling time and (iv) the control effort. Thus, the optimised controller is robust to parameter systems uncertainties, control input torque limitations and different tip velocities references, eliminating the chattering phenomenon in the control effort. Therefore, this dual-loop strategy, together with the optimisation procedure defined by the functional, has big potential in drill-string applications.

Author Contributions: Conceptualisation, E.P., S.S.A., J.P.-A., V.V., S.S.-S. and C.C.-G.; methodology, S.S.A., E.P., S.S.-S., J.P.-A., V.V.; software, J.P.-A., C.C.-G.; validation, S.S.A., E.P., S.S.-S., V.V. and J.P.-A.; formal analysis, J.P.-A., E.P., S.S.A, V.V.; investigation, J.P.-A., S.S.A., E.P., S.S.-S., C.C.-G. and V.V.; resources, S.S.A., V.V. and E.P.; data curation, J.P.-A., C.C.-G., E.P. and S.S.-S.; writing—original draft preparation, J.P.-A., E.P., S.S.-S. and S.S.A.; writing—J.P.-A., E.P., S.S.-S. and S.S.A.; visualisation, J.P.-A., E.P. and S.S.A.; supervision, S.S.-S., S.S.A. and E.P.; project administration, S.S.-S., S.S.A. and E.P.; funding acquisition, S.S.-A. All authors have read and agreed to the published version of the manuscript.

Funding: This work was partially supported by the Spanish Ministerial Commission of Science and Technology (MICYT) through project number TIN2017-85887-C2-2-P.

Data Availability Statement: Not applicable.

Acknowledgments: The authors would like to thank Marian Wiercigroch and Vahid Vaziri from the Centre for Applied Dynamics Research, University of Aberdeen, for providing the realistic drill-string parameters used in this work.

Conflicts of Interest: The authors declare no conflict of interest. The funders had no role in the design of the study; in the collection, analyses, or interpretation of data; in the writing of the manuscript, or in the decision to publish the results.

References

- 1. Brett, J.F. The genesis of bit-induced torsional drillstring vibrations. SPE Drill. Eng. 1992, 7, 168–174. [CrossRef]
- Hamaneh, S.V.V. Dynamics and Control of Nonlinear Engineering Systems. Ph.D. Thesis, University of Aberdeen, Aberdeen, UK, 2015.
- 3. Vromen, T.; Dai, C.-H.; van de Wouw, N.; Oomen, T.; Astrid, P.; Nijmeijer, H. Robust output-feedback control to eliminate stick-slip oscillations in drill-string systems. *IFAC Pap.* **2015**, *48*, 266–271. [CrossRef]
- Navarro-López, E.M. An alternative characterization of bit-sticking phenomena in a multi-degree-of-freedom controlled drillstring. Nonlinear Anal. Real World Appl. 2009, 10, 3162–3174. [CrossRef]
- 5. Oladunjoye, I.O.; Vaziri, V.; Ing, J.; Aphale, S.S. Severity analysis of stick-slip bifurcation in drill-string dynamics under parameter variation. *Afr. Model. Simul.* 2016. [CrossRef]
- Navarro-López, E.M.; Cortés, D. Avoiding harmful oscillations in a drillstring through dynamical analysis. J. Sound Vib. 2007, 307, 152–171. [CrossRef]
- 7. Kapitaniak, M.; Hamaneh, V.V.; Chávez, J.P.; Nandakumar, K.; Wiercigroch, M. Unveiling complexity of drill-string vibrations: Experiments and modelling. *Int. J. Mech. Sci.* 2015, 101, 324–337. [CrossRef]
- Sugiura, J.; Jones, S. Real-time stick-slip and vibration detection for 8 1/2"-hole-size rotary steerable tools in deeper wells and more aggressive drilling. In Proceedings of the AADE National Technical Conference, Houston, TX, USA, 10–12 April 2007.
- 9. Tucker, W.; Wang, C. On the effective control of torsional vibrations in drilling systems. J. Sound Vib. 1999, 224, 101-122. [CrossRef]
- 10. Sugiura, J. The use of the near-bit vibration sensor while drilling lead to optimized rotary-steerable drilling in push-and point-the-bit configurations. In Proceedings of the SPE Asia Pacific Oil and Gas Conference and Exhibition, Perth, Australia, 20–22 October 2008.
- Robnett, E.; Hood, J.; Heisig, G.; Macpherson, J. Analysis of the stick-slip phenomenon using downhole drillstring rotation data. In Proceedings of the SPE/IADC Drilling Conference, Amsterdam, The Netherlands, 9–11 March 1999.
- 12. Vaziri, V.; O, I.; Kapitaniak, M.; Aphale, S.S.; Wiercigroch, M. Parametric Analysis of a Sliding-Mode Controller to Suppress Drill-String Stick-Slip Vibration. *Meccanica* 2020, *55*, 2475–2492. [CrossRef]
- 13. Baradaran-Nia, M.; Afizadeh, G.; Khanmohammadi, S.; Azar, B.F. Optimal sliding mode control of single degree-of-freedom hysteretic structural system. *Commun. Nonlinear Sci. Numer. Simul.* **2012**, *17*, 4455–4466. [CrossRef]
- 14. Sassan, A.; Halimberdi, B. Design of a controller for suppressing the stick-slip oscillations in oil well drillstring. *Res. J. Recent Sci.* **2013**, *2*, 78–82.

- 15. Liu, Y. Suppressing stick-slip oscillations in underactuated multibody drill-strings with parametric uncertainties using sliding-mode control. *IET Control. Theory Appl.* **2014**, *9*, 91–102. [CrossRef]
- Sairafi, F.A.; Ajmi, K.A.; Yigit, A.; Christoforou, A. Modeling and control of stick slip and bit bounce in oil well drill strings. In Proceedings of the SPE/IADC Middle East Drilling Technology Conference and Exhibition, Abu Dhabi, United Arab Emirates, 26–28 January 2016.
- 17. Lin, W.; Liu, Y. Proportional-derivative control of stick-slip oscillations in drill-strings. In Proceedings of the International Conference on Engineering Vibration, Sofia, Bulgaria, 4–7 September 2017.
- Hong, L.; Girsang, I.P.; Dhupia, J.S. Identification and control of stick-slip vibrations using kalman estimator in oil-well drill strings. J. Pet. Sci. Eng. 2016, 140, 119–127. [CrossRef]
- Navarro-López, E.M.; Cortés, D. Sliding-mode control of a multi-dof oilwell drillstring with stick-slip oscillations. In Proceedings of the American Control Conference, ACC'07, New York, NY, USA, 11–13 July 2007; IEEE: Piscataway, NJ, USA, 2007; pp. 3837–3842.
- 20. Biel, D.; Fossas, E.; Guinjoan, F.; Alarcón, E.; Poveda, A. Application of sliding-mode control to the design of a buck-based sinusoidal generator. *IEEE Trans. Ind. Electron.* 2001, *48*, 563–571. [CrossRef]
- 21. Hernandez-Suarez, R.; Puebla, H.; Aguilar-Lopez, R.; Hernandez-Martinez, E. An integral high-order sliding mode control approach for stickslip suppression in oil drillstrings. *Pet. Sci. Technol.* **2009**, *27*, 788–800. [CrossRef]
- 22. Vaziri, V.; Kapitaniak, M.; Wiercigroch, M. Suppression of drill-string stick-slip vibration by sliding mode control: Numerical and experimental studies. *Eur. J. Appl. Math.* **2018**, *29*, 1–21. [CrossRef]
- Ritto, T.; Ghandchi-Tehrani, M. Active control of stick-slip torsional vibrations in drill-strings. J. Vib. Control. 2019, 25, 194–202. [CrossRef]
- 24. Feng, T.; Zhang, H.; Chen, D. Dynamic Programming Based Controllers to Suppress Stick-Slip in A Drilling System. In Proceedings of the 2017 American Control Conference (ACC), Seattle, WA, USA, 24–26 May 2017.
- 25. Ke, C.; Song, X.Y. Control of Down-Hole Drilling Process Using a Computationally Efficient Dynamic Programming Method. J. Dyn. Din. Systms Meas. Control Trans. ASME 2018, 140. [CrossRef]
- Pérez-Aracil, J.; Pereira, E.; Aphale, S.S.; Reynolds, P. Vibration Isolation and Alignment of Multiple Platforms on a Non-Rigid Supporting Structure. *Actuators* 2020, 9, 108. [CrossRef]
- 27. Soh, C.K.; Yang, J. Fuzzy controlled genetic algorithm search for shape optimization. *ASCE J. Comput. Civ. Eng.* **1996**, *10*, 143–150. [CrossRef]
- 28. Togan, V.; Daloglu, A.T. Optimization of 3D trusses with adaptive approach in genetic algorithms. *Eng. Struct.* **2006**, 28, 1019–1027. [CrossRef]
- 29. Yan, G.; Zhou, L. Impact load identification of composite structure using genetic algorithms. J. Sound Vib. 2009, 319, 869–884. [CrossRef]
- 30. Simonetti, H.L.; Almeida, V.S.; de Neto, L. A smooth evolutionary structural optimization procedure applied to plane stress problem. *Eng. Struct.* 2014, *75*, 248–258. [CrossRef]
- 31. Deb, K. Optimal design of a welded beam via genetic algorithms. AIAA J. 1991, 29, 2013–2015. [CrossRef]
- 32. Kennedy, J.; Eberhart, R.C. Particle swarm optimization. In Proceedings of the IEEE International Conference on Neural Networks, Perth, Australia, 27 November–1 December 1995; Volume IV, pp. 1942–1948.
- Kaveh, A.; Zolghadr, A. Democratic PSO for truss layout and size optimization with frequency constraints. *Comput. Struct.* 2014, 130, 10–21. [CrossRef]
- Schutte, J.J.; Groenwold, A.A. Sizing design of truss structures using particle swarms. *Struct. Multidiscip. Optim.* 2003, 23, 261–269. [CrossRef]
- 35. Rao, R.V.; Savsani, V.J.; Vakharia, D.P. Teaching?earning-based optimization: A novel optimization method for continuous non-linear large scale problems. *Inf. Sci.* 2011, 183, 1–15. [CrossRef]
- Rao, R.V.; Savsani, V.J.; Vakharia, D.P. Teaching-learning-based optimization: A novel method for constrained mechanical design optimization problems. *Comput. Aided Des.* 2011, 43, 303-315. [CrossRef]
- Degertekin, S.O.; Hayalioglu, M.S. Sizing truss structures using teaching-learning based optimization. *Comput. Struct.* 2013, 119, 177–188. [CrossRef]
- Geem, Z.W.; Kim, J.H.; Loganathan, G.V. A new heuristic optimization algorithm: Harmony Search. Simulation 2001, 76, 60–68. [CrossRef]
- 39. Saka, M.P.; Hasancebi, O.; Geem, Z.W. Metaheuristics in structural optimization and discussions on harmony search algorithm. *Swarm Evol. Comput.* **2016**, *28*, 88–97. [CrossRef]
- Kaveh, A.; Mahdavi, V.R. Optimal design of structures with multiple natural frequency constraints using a hybridized BB-BC/Quasi-Newton algorithm. *Period. Polytech. Civ. Eng.* 2013, 57, 27–38. [CrossRef]
- 41. Kaveh, A.; Mahdavi, V.R. Colliding bodies optimization: A novel meta-heuristic method. *Comput. Struct.* **2014**, *139*, 18–27. [CrossRef]
- 42. Kaveh, A.; Khayatazad, M. A new meta-heuristic method: Ray Optimization. Comput. Struct. 2012, 112, 283–294. [CrossRef]
- 43. Kaveh, A.; Talatahari, S.A. Novel heuristic optimization method: Charged system search. Acta Mech. 2010, 213, 267–289. [CrossRef]
- 44. Wang, D.; Vidyasagar, M. Passive control of a stiff flexible link International. J. Robot. Res. **1992**, 11, 572–578. [CrossRef]

- 45. Salcedo-Sanz, S.; Camacho-Gómez, C.; Molina, D.; Herrera, F. A Coral Reefs Optimization algorithm with substrate layers and local search for large scale global optimization. In Proceedings of the IEEE Congress on Evolutionary Computation (CEC), Vancouver, BC, Canada, 24–29 July 2016; pp. 1–8.
- 46. Salcedo-Sanz, S. A review on the coral reefs optimization algorithm: New development lines and current applications. *Prog. Artif. Intell.* **2017**, *6*, 1–15. [CrossRef]
- 47. Camacho-Gómez, S.S.C.; Magdaleno, A.; Pereira, E.; Lorenzana, A. Structures vibration control via Tuned Mass Dampers using a co-evolution Coral Reefs Optimization algorithm. *J. Sound Vib.* **2017**, *393*, 62–75.
- 48. Camacho-Gómez, C.; Wang, X.; Pereira, E.; Díaz, I.M.; Salcedo-Sanz, S. Active vibration control design using the Coral Reefs Optimization with Substrate Layer algorithm. *Eng. Struct.* **2018**, *157*, 14–26. [CrossRef]
- 49. Pérez-Aracil, J.; Camacho-Gómez, C.; Hernández-Díaz, A.M.; Pereira, E.; Salcedo-Sanz, S. Submerged Arches Optimal Design with a Multi-Method Ensemble Meta-Heuristic Approach. *IEEE Access* 2020, *8*, 215057–215072. [CrossRef]
- 50. Mihajlovic, N.; Veggel, A.V.; de Wouw, N.V.; Nijmeijer, H. Analysis of friction-induced limit cycling in an experimental drill-string system. *J. Dyn. Syst. Meas. Control* 2004, 126, 709–720. [CrossRef]
- Navarro-López, E.M.; Suárez, R. Practical approach to modelling and controlling stick-slip oscillations in oilwell drillstrings. In Proceedings of the 2004 IEEE International Conference, Paris, France, 20–24 June 2004; IEEE: Piscataway, NJ, USA, 2004; Volume 2, pp. 1454–1460.
- 52. Navarro-López, E.M.; Licéaga-Castro, E. Non-desired transitions and sliding-mode control of a multi-dof mechanical system with stick-slip oscillations. *Chaos Solitons Fractals* 2009, *41*, 2035–2044. [CrossRef]
- 53. Armstrong-Hélouvry, B.; Dupont, P.; Wit, C.C.D. A survey of models, analysis tools and compensation methods for the control of machines with friction. *Automatica* **1994**, *30*, 1083–1138. [CrossRef]
- 54. Leine, R.; Campen, D.V.; Kraker, A.D.; Steen, L.V.D. Stickslip vibrations induced by alternate friction models. *Nonlinear Dyn.* **1998**, *16*, 41–54. [CrossRef]
- Liu, L.Y.; Yuan, K. Noncollocated passivity-based PD control of a single-link flexible manipulator. *Robotica* 2003, 21, 117–135. [CrossRef]
- 56. Ryu, J.H.; Kwon, D.S.; Hannaford, B. Control of a flexible manipulator with noncollocated feedback: Time-domain passivity approach. *IEEE Trans. Robot.* 2004, 20, 776–778. [CrossRef]
- 57. Salcedo-Sanz, S.; Del Ser, J.; Landa-Torres, I.; Gil-López, S.; Portilla-Figueras, J.A. The Coral Reefs Optimization algorithm: A novel metaheuristic for efficiently solving optimization problems. *Sci. World J.* **2014**, *2014*, 739768. [CrossRef] [PubMed]
- 58. Jiménez-Fernández, S.; Camacho-Gómez, C.; Mallol-Poyato, R.; Fernández, J.C.; Ser, J.D.; Portilla-Figueras, A.; Salcedo-Sanz, S. Optimal microgrid topology design and siting of distributed generation sources using a multi-objective substrate layer Coral Reefs Optimization algorithm. *Sustainability* 2019, 11, 169. [CrossRef]
- 59. Bermejo, E.; Chica, M.; Damas, S.; Salcedo-Sanz, S.; Cordón, O. Coral Reef Optimization with ubstrate layers for medical image registration. *Swarm Evol. Comput.* 2018, 42, 138–159. [CrossRef]
- 60. Salcedo-Sanz, S.; noz-Bulnes, J.M.; Vermeij, M. New Coral Reefs-based Approaches for the Model Type Selection Problem: A Novel Method to Predict a Nation's Future Energy Demand. *Int. J. Bio-Inspired Comput.* **2017**, *10*, 145–158. [CrossRef]
- Salcedo-Sanz, S.; Camacho-Gómez, C.; Mallol-Poyato, R.; Jiménez-Fernández, S.; Del Ser, J. A novel Coral Reefs Optimization algorithm with substrate layers for optimal battery scheduling optimization in micro-grids. *Soft Comput.* 2016, 20, 4287–4300. [CrossRef]
- Sánchez-Montero, R.; Camacho-Gómez, C.; López-Espí, P.L.; Salcedo-Sanz, S. Optimal design of a planar textile antenna for Industrial Scientific Medical (ISM) 2.4 GHz Wireless Body Area Networks (WBAN) with the CRO-SL Algorithm. *Sensors* 2018, 18, 1982. [CrossRef] [PubMed]
- 63. Price, K.; Storn, R.; Lampinen, J. Differential Evolution—A Practical Approach to Global Optimization; Springer: Berlin, Germany, 2005.
- 64. Eiben, A.E.; Smith, J.E. Introduction to Evolutionary Computing; Springer: Berlin/Heidelberg, Germany, 2003.