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A Fixed-Time Second Order Sliding Mode Observer for a Class of Nonlinear Systems

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***Abstract*— This paper presents a second order fixed time sliding mode observer based on an extension of the super-twisting algorithm. This observer can be applied to a class of nonlinear system with a block-wise representation. The block structure provides a straightforward form to the application of the proposed second order sliding mode algorithm, yielding to finite-time convergence with a settling time independent to the system initial conditions. Finally, as numerical simulation example, the case of a linear induction motor is studied, exposing the efficiency and feasibility of the proposal.**

I. Introduction

The sliding mode (SM) algorithms are applied with the idea to drive the dynamics of a system to a sliding manifold that is an integral manifold with finite reaching time [1]. Generally, this approach exhibits very interesting and desirable features such as the work with reduced observation error dynamics, the possibility to decompose the design problem into two sub problems of the reduced order, the robustness of the closed-loop system in presence of parameter variations and external disturbances and, finite-time stability [2]–[4].

Considering the observation error as a sliding variable, the SM algorithms can be considered as an effective solution to the problem of observers design for nonlinear systems [5], specially when finite-time convergence of the observed states to the real ones is required. An important class of SM observers use the equivalent control method [6] to obtain information of the system by means of continuous equivalent values of the discontinuous observer inputs in SM motion [7]. With this idea, several designs have been proposed as the cascade observers [8], step-by-step observers [9], a SM observer where the estimation of unknown inputs problem has been considered [10], fixed time designs [11], among others.

Another class of SM observers are based on the second order SM feature of the super-twisting algorithm (STA) [12]. Those attractive characteristics of the STA algorithm have been exploited and extended for fixed time convergent methods [13]–[15], adaptive controllers [16]–[21], multivariable structures [22], most of them based on the stability studies presented in [23]–[29]. For the case of observers, a design for mechanical systems is presented in [30] being extended to electrical drives [31], more general forms as in [32] and systems with noisy measurements [33], [34].

All these methods present high performance. However, most of them are presented in scalar form. And, the multivariable structure introduced in [22] converges in finite time but not fixed.

Under that consideration, this paper is aimed to present a SM observer for a class of nonlinear systems based on a fixed time STA with fixed time convergence. This design allows the problem to be solved without the individual selection of each stabilizing input, instead a multivariable function, based on the unit control [2], [35], is used. On the other hand, the fixed time stability [13], [36] ensures the existence of a finite time independent to the initial conditions in which the system converges. Thus, the proposed approach have very attractive features as: fixed time convergence to the observed variables and a fixed parameters number (six for this case), regardless of the state dimension.

The linear induction motor is considered as case study. The effectiveness the proposed observer is demonstrated by means of numerical simulation, showing a good performance of this proposal.

This paper is organized as follows: Section II introduces a multivariable fixed time stable STA . Section III describes the proposed observers. The simulations are presented in Section IV. Finally, in Section V the conclusions are given.

II. Preliminary Result

Let the vectors $x_1, x_2 \in \mathbb{R}^n$. Now, consider the system

$$\begin{aligned} \dot{x}_1 &= -k_1 \frac{x_1}{\|x_1\|^{1/2}} - k_2 x_1 - k_3 x_1 \|x_1\|^{1/2} + x_2 + \Delta_1 \\ \dot{x}_2 &= -k_4 \frac{x_1}{\|x_1\|} - k_5 x_1 - k_6 x_1 \|x_1\|^{1/2} + \Delta_2 \end{aligned} \tag{1}$$

where $k_1, \ldots, k_6 > 0$, and the disturbances are regarded as $\|\Delta_1\| \leq \delta_1 \|x_1\|$ and $\|\Delta_2\| \leq \delta_2$ with $\delta_1, \delta_2 > 0$.

With the Lyapunov function

$$V = 2k_3 \|x_1\| + k_4 \|x_1\|^2 + \frac{1}{2}\|x_2\|^2 + \nu^T \nu \tag{2}$$

where $\nu = k_1 \frac{x_1}{\|x_1\|^{1/2}} + k_2 x_1 + k_3 x_1 \|x_1\|^{1/2} - x_2$, it is possible to show there exists constants $\gamma_1 = \gamma_1(\theta), \gamma_2 = \gamma_2(\theta) > 0$, $\theta = (k_1, k_2, k_3, k_3, k_4, k_5, k_6, \delta_1, \delta_2)$, such that

$$\dot{V} \leq -\gamma_1 V^{1/2} - \gamma_2 V^{3/2}. \tag{3}$$

Therefore, from (2) – (3), the system (1) is globally fixed time stable [36].

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III. Fixed-Time Second Order Sliding Mode Observer

A. Observer Design

Consider the system written in the following block-wise form:

$$\begin{aligned} \dot{x}_1 &= B_1(x_1)x_2 + f_1(x_1, u) \\ \dot{x}_2 &= B_2(x_1)x_2 + f_2(x_1) \\ y &= x_1 \end{aligned} \tag{4}$$

where $x = [x_1 \quad x_2]^T$ and the vectors $x_1, x_2 \in \mathbb{R}^n$. The matrix $B_1(x_1)$ is considered to be invertible.

Based on the system (4), the following observer is proposed in order to provide a uniform finite estimation of the state x:

$$\begin{aligned} \dot{\hat{x}}_1 &= B_1(x_1)\hat{x}_2 + f_1(x_1, u) + \phi_1(\tilde{x}_1) \\ \dot{\hat{x}}_2 &= B_2(x_1)\hat{x}_2 + f_2(x_1) + B_1^{-1}(x_1)\phi_2(\tilde{x}_1) \end{aligned} \tag{5}$$

where $\hat{x}_1$ and $\hat{x}_2$ are the estimates of x_1 and x_2, respectively and, the observer errors are given by $\tilde{x}_1 = \hat{x}_1 - x_1$ and $\tilde{x}_2 = \hat{x}_2 - x_2$. The observer inputs $\phi_1(\tilde{x}_1)$, and $\phi_2(\tilde{x}_1)$ are defined as

$$\begin{aligned} \phi_1(\tilde{x}_1) =& k_1 \frac{\tilde{x}_1}{\|\tilde{x}_1\|^{1/2}} + k_2\tilde{x}_1 + k_3\tilde{x}_1 \|\tilde{x}_1\|^{1/2} \\ \phi_2(\tilde{x}_1) =& k_4 \frac{\tilde{x}_1}{\|\tilde{x}_1\|} + k_5\tilde{x}_1 + k_6\tilde{x}_1 \|\tilde{x}_1\|^{1/2} \end{aligned} \tag{6}$$

where $k_1, \ldots, k_6 > 0$.

B. Convergence Analysis

To analyze the observer convergence, consider the dynamics of the errors $\tilde{x}_1$ and $\tilde{x}_2$. From (4) and (5) it follows

$$\begin{aligned} \dot{\tilde{x}}_1 &= B_1(x_1)\tilde{x}_2 - \phi_1(\tilde{x}_1) \\ \dot{\tilde{x}}_2 &= B_2(x_1)\tilde{x}_2 - B_1^{-1}(x_1)\phi_2(\tilde{x}_1). \end{aligned} \tag{7}$$

Defining $q = B_1(x_1)\tilde{x}_2$, the system (7) is transformed to

$$\begin{aligned} \dot{\tilde{x}}_1 &= \phi_1(\tilde{x}_1) + q \\ \dot{q} &= \phi_2(\tilde{x}_1) + B(x_1)q \end{aligned} \tag{8}$$

where $B(x_1) = \left[\dot{B}_1(x_1) + B_1(x_1)B_2(x_1)\right] B_1^{-1}(x_1)$.

Considering $\|B(x_1)q\| < \delta$ where $\delta > 0$, with a suitable choice of the gains $k_1, \ldots, k_6$, it follows from (2) – (3) that the system (8) is globally fixed time stable. Therefore, the observer variables converges to the real ones in fixed time.

IV. Numerical Simulation Results

This section shows numerical simulations results of the proposed observer for a linear induction motor. The measured variables are the velocity and the currents. The observed variables are the flux and the load torque, introduced as step form. This is motivated, due the difficulty of the flux and torque direct measurement [37].

The model for the induction can be described by equations for the stator current and rotor fluxes in stationary reference frame $\alpha\beta$ as follows:

$$\begin{aligned} \frac{d\Theta}{dt} &= d_1\left(\lambda_{\alpha r} i_{\beta s} - \lambda_{\beta r} i_{\alpha s}\right) - d_2\Gamma - d_3\Theta \\ \frac{d\lambda_{\alpha r}}{dt} &= -\eta_1\lambda_{\alpha r} + \eta_2\Theta\lambda_{\beta r} + \eta_3 i_{\alpha s} \\ \frac{d\lambda_{\beta r}}{dt} &= -\eta_1\lambda_{\beta r} - \eta_2\Theta\lambda_{\alpha r} + \eta_3 i_{\beta s} \\ \frac{di_{\alpha s}}{dt} &= -\eta_4 i_{\alpha s} + \eta_5\lambda_{\alpha r} - \eta_6\Theta\lambda_{\beta r} + \eta_7 v_{\alpha s} \\ \frac{di_{\beta s}}{dt} &= -\eta_8 i_{\beta s} + \eta_9\lambda_{\beta r} + \eta_{10}\Theta\lambda_{\alpha r} + \eta_{11} v_{\beta s} \end{aligned} \tag{9}$$

where $\lambda_{\alpha r}$ and $\lambda_{\beta r}$ are the rotor magnetic-flux-linkage components, respectively; $i_{\alpha s}$ and $i_{\beta s}$ are the stator current components, respectively, $v_{\alpha s}$ and $v_{\beta s}$ are the voltage of α and β axes in the stator, respectively.

For the three-phase linear induction motor in $\alpha\beta$ frame, the voltages are presented of the form

$$v_{\alpha s} = v_s \sin(\omega t) \tag{10}$$

$$v_{\beta s} = -v_s \sin(\omega t). \tag{11}$$

Thus, for this case, the parameters are: $\eta_1 = \frac{R_r}{L_r}$, $\eta_2 = n_p\left(\frac{\pi}{\tau}\right)$, $\eta_3 = \frac{R_r L_m}{L_r}$, $\eta_4 = \frac{R_s}{\left(\frac{{L_s}^2 L_r - L_s {L_m}^2}{L_s L_r}\right)} + \frac{1-\left(\frac{L_s L_r - {L_m}^2}{L_s L_r}\right)}{\left(\frac{L_s L_r - {L_m}^2}{L_s L_r}\right)\frac{R_r}{L_r}}$, $\eta_5 = \frac{L_m R_r}{\left(\frac{L_s L_r - {L_m}^2}{L_s L_r}\right) L_s {L_r}^2}$, $\eta_6 = n_p\left(\frac{\pi}{\tau}\right)\frac{L_m}{\left(\frac{L_s L_r - {L_m}^2}{L_s L_r}\right) L_s L_r}$, $\eta_7 = \frac{1}{\left(\frac{L_s L_r - {L_m}^2}{L_s L_r}\right) L_s}$, $\eta_8 = \eta_4$, $\eta_9 = \eta_5$, $\eta_{10} = \eta_6$, $\eta_{11} = \eta_7$, $d_1 = \frac{3 n_p \pi L_m}{2 L_r \tau M}$, $d_2 = \frac{1}{M}$, $d_3 = \frac{D}{M}$ where R_s and L_s are the resistance and inductance of the stator, respectively. τ is the pole pitch, M is the total mass of the moving element, D is viscous friction, $\Theta = \upsilon$ is the linear velocity and $\Gamma = F_L$ is the external force.

For the observer design, the availability of continuous measurements of motor speed and currents is assumed. In addition the mechanic load Γ is considered as an unknown and slowly-varying perturbation to be estimated, that is $\dot{\Gamma} = 0$. Thus, the system (9) can be and, the blocks are $x_1 = [\Theta \quad i_{\alpha s} \quad i_{\beta s}]^T$ and, $x_2 = [\lambda_{\alpha r} \quad \lambda_{\beta r} \quad \Gamma]^T$, with $u = [v_{\alpha s} \quad v_{\beta s}]^T$. Here $B_1(x_1) = \begin{bmatrix} d_1 i_{\beta s} & d_1 i_{\alpha s} & -d_2 \\ \eta_5 & -\eta_6\Theta & 0 \\ \eta_{10}\Theta & \eta_9 & 0 \end{bmatrix}$, $f_1(x_1, u) = \begin{bmatrix} -d_3\Theta \\ \eta_7 v_{\alpha s} - \eta_4 i_{\alpha s} \\ \eta_{10}\Theta \end{bmatrix}$, $B_2(x_1) = \begin{bmatrix} -\eta_1 & \eta_2\Theta & 0 \\ -\eta_2\Theta & -\eta_1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ and, $f_2(x_1) = \begin{bmatrix} \eta_3 i_{\alpha s} \\ \eta_3 i_{\beta s} \\ 0 \end{bmatrix}$.

$B_1^{-1}(x_1)$ is the inverse of the matrix $B_1(x_1)$ and is given by $B_1^{-1}(x_1) = \begin{bmatrix} 0 & \frac{\eta_9}{\eta_6\eta_{10}\Theta^2 + \eta_5\eta_9} & \frac{\eta_6\Theta}{\eta_6\eta_{10}\Theta^2 + \eta_5\eta_9} \\ 0 & -\frac{\eta_{10}\Theta}{\eta_6\eta_{10}\Theta^2 + \eta_5\eta_9} & \frac{\eta_5}{\eta_6\eta_{10}\Theta^2 + \eta_5\eta_9} \\ -\frac{1}{d_2} & \frac{d_1(\eta_9 i_{\beta s} + \eta_{10} i_{\alpha s}\Theta)}{d_2(\eta_6\eta_{10}\Theta^2 + \eta_5\eta_9)} & -\frac{d_1(\eta_5 i_{\alpha s} - \eta_6 i_{\beta s}\Theta)}{d_2(\eta_6\eta_{10}\Theta^2 + \eta_5\eta_9)} \end{bmatrix}$.

For three-phase linear induction motor the parameter are presented as [38]:

Three-phase linear			
H.P.	4	V_s	180 (V)
f	60 (Hz)	n_p	2
R_s	5.3685 (Ω)	R_r	3.5315 (Ω)
L_s	0.02846(H)	L_r	0.02846 (H)
L_m	0.02419 (H)	M	2.78 (kg)
D	36.0455 (Kg/s)	τ	0.027 (m)
$I_{\max}$	14.2 (A)		
μ_1	1	μ_2	1
m_{11}	640	m_{12}	640
m_{13}	45	m_{21}	64000
m_{22}	64000	m_{23}	20

The observer gains are chosen as $k_1 = 5$, $k_2 = 10$, $k_3 = 2$, $k_4 = 10$, $k_5 = 5$ and $k_6 = 1$. The simulation results are shown in the following figures:

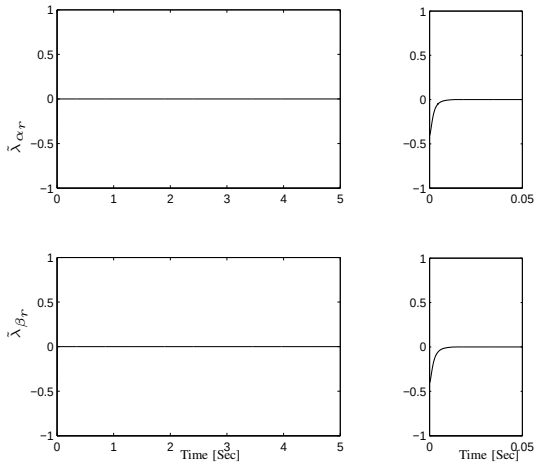

Fig. 1. Error of rotor flux $\tilde{\lambda}_{\alpha_r}$ and $\tilde{\lambda}_{\beta_r}$ of TLIM.

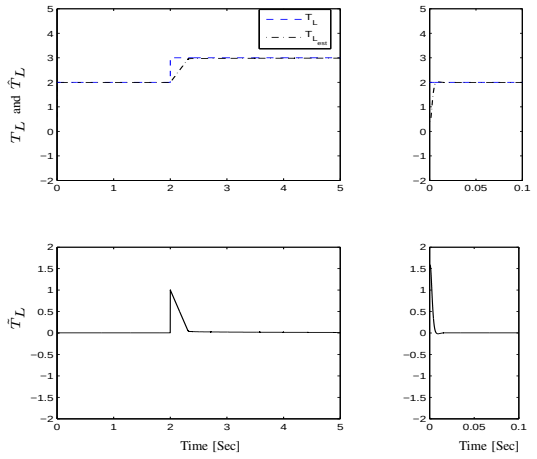

Fig. 2. Load torque estimated $\hat{T}_L$ and error of load torque $\tilde{T}_L$ of TLIM.

In Figure 1 the time evolution of the rotor flux $\tilde{\lambda}_{\alpha_r}$ and $\tilde{\lambda}_{\beta_r}$ errors of induction motors are shown, while Fig. 2 presents the time evolutions of the estimated load torque $\hat{T}_L$ and the load estimation error $\tilde{T}_L$ of induction motors cases.

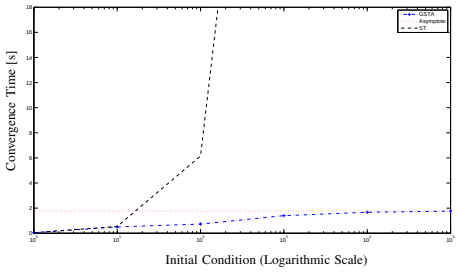

Fig. 3. Convergence time of both observers by growing initial condition norm.

The Figure 3 presents a comparison of the proposed observer with another which uses the mutivariable STA [22], that means fixing $k_3 = 0$ and $k_6 = 0$ in (6). Here is highlighted that the convergence time for the multivariable STA grows unboundedly with the norm of the initial condition, while the convergence time of the proposed observer is asymptotically bounded by a constant for growing initial condition's norm.

V. CONCLUSIONS

In this work a fixed time convergent observer was proposed. The scheme was applied to the model on the stationary frame $\alpha\beta$ for induction motors. The flux and load torque were estimated, all of them are shown to give appreciable results in order of convergence time to estimate the rotor flux and the load torque.

REFERENCES

[1] S. V. Drakunov and V. I. Utkin, "Sliding mode control in dynamic systems," *International Journal of Control*, vol. 55, pp. 1029–1037, 1992.

[2] V. I. Utkin, *Sliding Modes in Control and Optimization*. Springer Verlag, 1992.

[3] V. I. Utkin, J. Guldner, and J. Shi, *Sliding Mode Control in Electro-Mechanical Systems, Second Edition (Automation and Control Engineering)*, 2nd ed. CRC Press, 5 2009.

[4] R. A. DeCarlo, S. Zak, and S. V. Drakunov, *The Control Handbook: a Volume in the Electrical Engineering Handbook Series, Chapter 50, Variable Structure, Sliding Mode Controller Design,*. CRC Press, Inc., 2011.

[5] C. M. Walcott, B.L. and S. Zak, "Comparative study of nonlinear state observation techniques," *Int. J. Control*, vol. 45, pp. 2109–2132, 1987.

[6] V. I. Utkin, "Equations of sliding mode in discontinuous systems," *Automation and Remote Control*, vol. I, II, no. 12, pp. 211–219, 1972.

[7] S. V. Drakunov, "Sliding-mode observers based on equivalent control method," in *Decision and Control, 1992., Proceedings of the 31st IEEE Conference on*, 1992, pp. 2368 –2369 vol.2.

[8] S. A. Krasnova, V. A. Utkin, and Y. V. Mikheev, "Cascade design of state observers," *Automation and Remote Control*, vol. 62, pp. 207–226, 2001.

[9] T. Floquet and J. P. Barbot, "Super twisting algorithm-based step-by-step sliding mode observers for nonlinear systems with unknown inputs," *International Journal of Systems Science*, vol. 38, no. 10, pp. 803–815, 2007.

[10] F. J. Bejarano and L. Fridman, "High order sliding mode observer for linear systems with unbounded unknown inputs," *International Journal of Control*, vol. 9, pp. 1920–1929, 2010.

[11] J. D. Sánchez-Torres, A. G. Loukianov, J. A. Moreno, and S. V. Drakunov, "An equivalent control based sliding mode observer using high order uniform robust sliding operators," in *American Control Conference (ACC), 2012*, June 2012, pp. 6160–6165.

[12] A. Levant, "Sliding order and sliding accuracy in sliding mode control," *International Journal of Control*, vol. 58, no. 6, pp. 1247–1263, 1993.

[13] E. Cruz-Zavala, J. A. Moreno, and L. Fridman, "Uniform second-order sliding mode observer for mechanical systems," in *Variable Structure Systems (VSS), 2010 11th International Workshop on*, june 2010, pp. 14 –19.

[14] E. Cruz-Zavala, J. Moreno, and L. Fridman, "Uniform robust exact differentiator," *Automatic Control, IEEE Transactions on*, vol. 56, no. 11, pp. 2727–2733, Nov 2011.

[15] E. Cruz-Zavala, J. A. Moreno, and L. Fridman, "Uniform sliding mode controllers and uniform sliding surfaces," *IMA Journal of Mathematical Control and Information*, vol. 29, no. 4, pp. 491–505, 2012.

[16] A. Dávila, J. Moreno, and L. Fridman, "Variable gains super-twisting algorithm: A Lyapunov based design," in *American Control Conference (ACC), 2010*, June 2010, pp. 968–973.

[17] Y. Shtessel, J. Moreno, F. Plestan, L. Fridman, and A. Poznyak, "Super-twisting adaptive sliding mode control: A Lyapunov design," in *Decision and Control (CDC), 2010 49th IEEE Conference on*, Dec 2010, pp. 5109–5113.

[18] Y. B. Shtessel, F. Plestan, and M. Taleb, "Lyapunov design of adaptive super-twisting controller applied to a pneumatic actuator," in *Proceedings of the 18th IFAC World Congress*, 2011.

[19] T. Gonzalez, J. A. Moreno, and L. Fridman, "Variable gain super-twisting sliding mode control," *Automatic Control, IEEE Transactions on*, vol. 57, no. 8, pp. 2100–2105, Aug 2012.

[20] C. Evangelista, P. Puleston, F. Valenciaga, and L. Fridman, "Lyapunov-designed super-twisting sliding mode control for wind energy conversion optimization," *Industrial Electronics, IEEE Transactions on*, vol. 60, no. 2, pp. 538–545, Feb 2013.

[21] V. I. Utkin and A. S. Poznyak, "Adaptive sliding mode control with application to super-twist algorithm: Equivalent control method," *Automatica*, vol. 49, no. 1, pp. 39 – 47, 2013.

[22] I. Nagesh and C. Edwards, "A multivariable super-twisting sliding mode approach," *Automatica*, vol. 50, no. 3, pp. 984 – 988, 2014.

[23] J. A. Moreno and M. Osorio, "A Lyapunov approach to second-order sliding mode controllers and observers," in *Decision and Control, 2008. CDC 2008. 47th IEEE Conference on*, dec. 2008, pp. 2856 –2861.

[24] J. A. Moreno, "A linear framework for the robust stability analysis of a generalized super-twisting algorithm," in *Electrical Engineering, Computing Science and Automatic Control,CCE,2009 6th International Conference on*, Jan 2009, pp. 1–6.

[25] A. Dávila, J. A. Moreno, and L. Fridman, "Optimal lyapunov function selection for reaching time estimation of super twisting algorithm," in *Decision and Control, 2009 held jointly with the 2009 28th Chinese Control Conference. CDC/CCC 2009. Proceedings of the 48th IEEE Conference on*, Dec 2009, pp. 8405–8410.

[26] A. Polyakov and A. Poznyak, "Reaching time estimation for "super-twisting" second order sliding mode controller via lyapunov function designing," *Automatic Control, IEEE Transactions on*, vol. 54, no. 8, pp. 1951–1955, Aug 2009.

[27] J. A. Moreno, "Lyapunov approach for analysis and design of second order sliding mode algorithms," in *Sliding Modes after the First Decade of the 21st Century*, ser. Lecture Notes in Control and Information Sciences, L. Fridman, J. Moreno, and R. Iriarte, Eds. Springer Berlin Heidelberg, 2012, vol. 412, pp. 113–149.

[28] J. A. Moreno and M. Osorio, "Strict Lyapunov functions for the super-twisting algorithm," *Automatic Control, IEEE Transactions on*, vol. 57, no. 4, pp. 1035–1040, April 2012.

[29] V. Utkin, "On convergence time and disturbance rejection of super-twisting control," *Automatic Control, IEEE Transactions on*, vol. 58, no. 8, pp. 2013–2017, Aug 2013.

[30] J. Davila, L. Fridman, and A. Levant, "Second-order sliding-mode observer for mechanical systems," *Automatic Control, IEEE Transactions on*, vol. 50, no. 11, pp. 1785–1789, Nov 2005.

[31] G. J. Rubio, J. D. Sanchez-Torres, J. M. Canedo, and A. G. Loukianov, "HOSM block control of SPIM," in *Electrical Engineering, Computing Science and Automatic Control (CCE), 2012 9th International Conference on*, Sept 2012, pp. 1–6.

[32] J. A. Moreno, "On discontinuous observers for second order systems: Properties, analysis and design," in *Advances in Sliding Mode Control*, ser. Lecture Notes in Control and Information Sciences, B. Bandyopadhyay, S. Janardhanan, and S. K. Spurgeon, Eds. Springer Berlin Heidelberg, 2013, vol. 440, pp. 243–265.

[33] L. Fraguela, M. Angulo, J. Moreno, and L. Fridman, "Design of a prescribed convergence time uniform robust exact observer in the presence of measurement noise," in *Decision and Control (CDC), 2012 IEEE 51st Annual Conference on*, Dec 2012, pp. 6615–6620.

[34] M. Angulo, J. Moreno, and L. Fridman, "The differentiation error of noisy signals using the generalized super-twisting differentiator," in *Decision and Control (CDC), 2012 IEEE 51st Annual Conference on*, Dec 2012, pp. 7383–7388.

[35] C. M. Dorling and A. S. I. Zinober, "Two approaches to hyperplane design in multivariable variable structure control systems," *International Journal of Control*, vol. 44, no. 1, pp. 65–82, 1986.

[36] A. Polyakov, "Nonlinear feedback design for fixed-time stabilization of linear control systems," *IEEE Transactions on Automatic Control*, vol. 57, no. 8, pp. 2106–2110, 2012.

[37] I. Kanellakopoulos, P. T. Krein, and F. Disilvestro, "Nonlinear flux-observer-based control of induction motors," in *American Control Conference, 1992*, june 1992, pp. 1700 –1705.

[38] I. Boldea and S. Nasar, *Linear Electric Actuators and Generators*. Cambridge University Press, 1997.