Crossing Genetic and Swarm Intelligence Algorithms to Generate Logic Circuits

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Abstract: Genetic Algorithms (GAs) are adaptive heuristic search algorithm based on the evolutionary ideas of natural selection and genetic. The basic concept of GAs is designed to simulate processes in natural system necessary for evolution, specifically those that follow the principles first laid down by Charles Darwin of survival of the fittest. On the other hand, Particle swarm optimization (PSO) is a population based stochastic optimization technique inspired by social behavior of bird flocking or fish schooling. PSO shares many similarities with evolutionary computation techniques such as GAs. The system is initialized with a population of random solutions and searches for optima by updating generations. However, unlike GA, PSO has no evolution operators such as crossover and mutation. In PSO, the potential solutions, called particles, fly through the problem space by following the current optimum particles. PSO is attractive because there are few parameters to adjust. This paper presents hybridization between a GA algorithm and a PSO algorithm (crossing the two algorithms). The resulting algorithm is applied to the synthesis of combinational logic circuits. With this combination is possible to take advantage of the best features of each particular algorithm.

Key–Words: Artificial Intelligence, Computational Intelligence, Evolutionary Computation, Genetic Algorithms, Particle Swarm Optimization, Digital Circuits

1 Introduction

Evolutionary Computation (EC) is a subfield of artificial intelligence, particularly computational intelligence. EC is the general term for several computational techniques which use ideas and get inspiration from natural evolution and adaptation (figure 1)[5]. Evolutionary techniques mostly involve optimization algorithms such as:

- Evolutionary Algorithms:
  - genetic algorithms, evolutionary programming, genetic programming and learning classifier systems.
- Swarm Intelligence:
  - particle swarm optimization, ant colony optimization and bee colony optimization.

In recent decades EC techniques have been applied to the design of electronic circuits and systems, leading to a novel area of research called Evolutionary Electronics (EE) or Evolvable Hardware [8]. EE considers the concept for automatic design of electronic systems. Instead of using human conceived models, abstractions and techniques, EE employs search algorithms to develop implementations not achievable with the traditional design schemes, such as the Boolean methods: Karnaugh or the Quine-McCluskey.

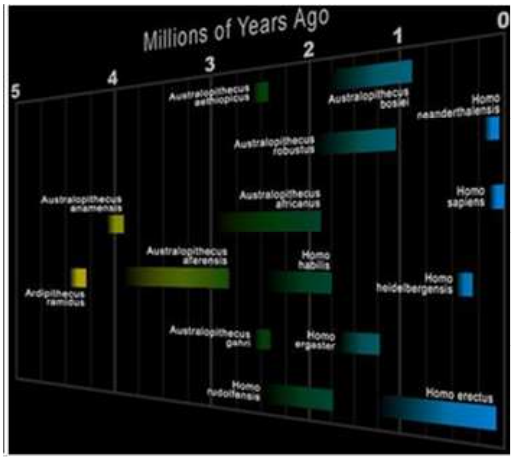

Figure 1: Human evolution timeline [22]

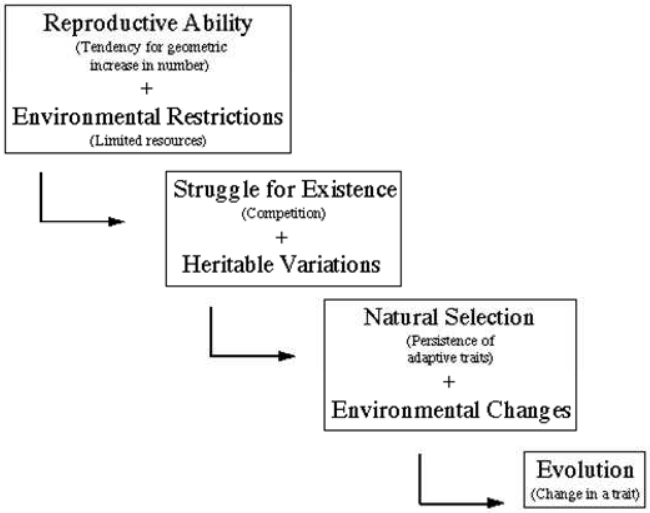

Figure 2: Natural selection by Charles Darwin

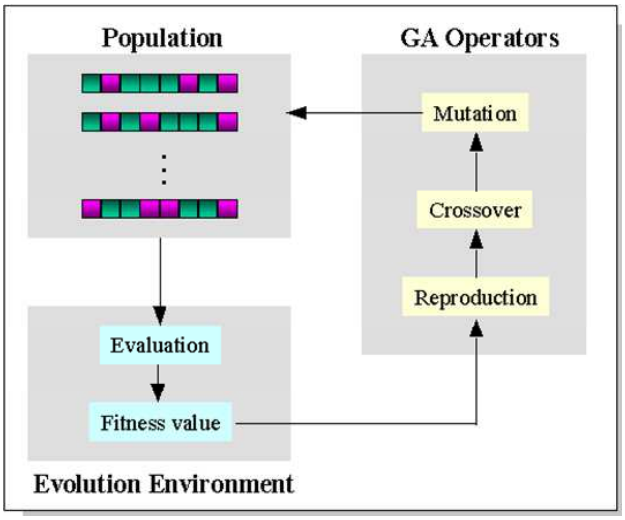

Figure 3: Evolution flow of a Genetic Algorithm [23]

GAs are adaptive heuristic search algorithm based on evolutionary principles and are designed to simulate processes, in natural systems, necessary for evolution, following the principles first laid down by Charles Darwin. Darwin proposed that humans, and in fact all creatures, evolve from other creatures and over time, creatures change to adapt to their environment to survive and thrive (figure 2) [7].

GAs were invented by John Holland in the 1960s and developed by Holland and his students and colleagues at the University of Michigan in the 1960s and the 1970s Holland's GA is a method for moving from one population of "chromosomes" to a new population by using a kind of "natural selection" together with the genetics-inspired operators of crossover, mutation and inversion [2, 4, 6]. Each chromosome consists of genes and the selection operator chooses in the population the chromosomes that will reproduce. Crossover exchanges subparts of two chromosomes, mimicking biological recombination between two organisms. Mutation randomly changes the values of some locations in the chromosome Inversion reverses the order of a contiguous section of the chromosome.

Figure 3 presents the evolution flow of a GA and figures 4 and 5 show examples of crossover and mutation, respectively.

Several papers proposed designing combinational logic circuits using evolutionary algorithms and, in particular, Genetic Algorithms (GAs) [3, 1, 9, 14]. Also hybrid schemes such as Memetic Algorithms (MAs) [19] were proposed. MAs are evolutionary algorithms (EAs) that apply a separate local search process to refine individuals (i.e. that improve their fitness by hill-climbing). Figures 6 and 7 show the algorithms of a MA. Under different contexts and situations, MAs are also known as hybrid EAs or genetic local searchers [18]. The term comes from the Richard Dawkin's term "meme" [17].

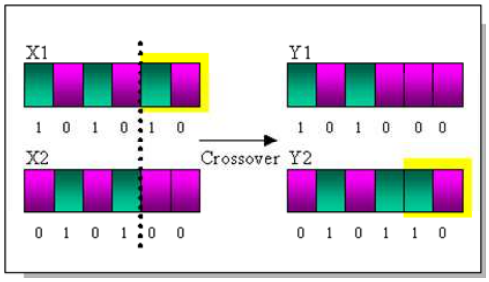

Figure 4: Crossover operator example [23]

Another emerging area of research of Artificial Intelligence is the Swarm Intelligence (SI)[12]. SI is a new computational and behavioral paradigm for solving distributed problems based on self-organization. While its main principles are similar to those underlying the behavior of natural systems consisting of many individuals, such as ant colonies and flocks of birds, SI is continuously incorporating new ideas, algorithms, and principles from the engineering and basic science communities.

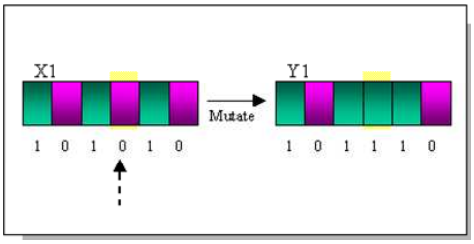

Figure 5: Mutation operator example [23]

Particle swarm optimization (PSO) is a population based stochastic optimization technique developed by Dr. Eberhart and Dr. Kennedy in 1995, inspired by social behavior of bird flocking or fish schooling (figures 8 and 9).

PSO shares many similarities with evolutionary computation techniques such as GAs. The system is initialized with a population of random solutions and searches for optima by updating generations. Figure 10 presents the PSO algorithm. However the PSO has no evolution operators such as crossover and mutation. In PSO, the potential solutions, called particles, fly through the problem space by following the current optimum particles. The detailed information will be given in following sections.

The advantages of the PSO, relatively to the GA, is that the PSO is easier to implement and involves fewer parameters to adjust.

This paper studies the combination of these two techniques applied to combinational logic circuit synthesis. Bearing these ideas in mind, the organization of this article is as follows. Section 2 presents a brief overview of the GA. Section 3 presents the PSO, while section 4 exhibits the simulation results. Finally, section 5 outlines the main conclusions and addresses perspectives towards future developments.

2 The Genetic Algorithm

In this section we present the GA developed in the study, in terms of the circuit encoding as a chromosome, the genetic operators and fitness functions.

2.1 Problem Definition

A GA strategy is adopted to design combinational logic circuits. The circuits are specified by a truth table and the goal is to implement a functional circuit with the least possible complexity [20, 21]. Two sets of logic gates have been defined, as shown in Table 1, namely Gset 6, with six logic gates and Gset 4, with four logic gates. The WIRE means a direct connection (i. e., without any logic gate).

Gate Set	Logic gates
Gset 6	{AND,OR,XOR,NOT, NAND,NOR,WIRE}
Gset 4	{AND,OR,XOR,NOT,WIRE}

Table 1: Gate sets

For each gate set the GA searches the solution space, based on a simulated evolution aiming the survival of the fittest strategy. In general, the best individuals of any population tend to reproduce and survive, thus improving successive generations. However, inferior individuals can, by chance, survive and also reproduce [10]. In our case, the individuals are digital circuits, which can evolve until the solution is reached (in terms of functionality and complexity).

2.2 Circuit encoding

In the GA scheme the each circuit is encoded as a rectangular matrix **A** of logic cells as represented in figure 11.

The three genes: $<$*input1*$>$ $<$*input2*$>$ $<$*gate type*$>$ represent each cell, where *input1* and *input2* are one of the circuit inputs, if the cell is in the first column of the matrix, or, one of the outputs of a previous cell, if the cell is not in the first column of the matrix. The *gate type* is one of the elements adopted in the gate set. The chromosome is formed by as many triplets of this kind as the matrix size demands. For example, the chromosome that represents a 3×3 matrix is depicted in figure 12.

2.3 The genetic operators

The initial population of circuits (strings) is generated at random. The search is then carried out among this population. The three different operators used are reproduction, crossover and mutation, as described in the sequel.

In what concern the reproduction operator, the successive generations of new strings are reproduced on the basis of their fitness function. In this case, it is

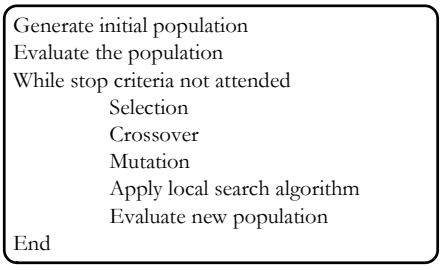

Figure 6: The memetic algorithm

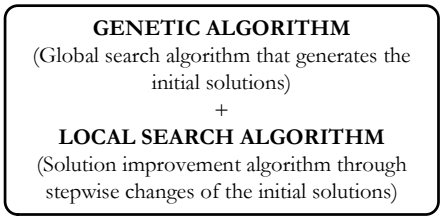

Figure 7: GA and a local search algorithm

used a tournament selection to select the strings from the old population, up to the new population.

For the crossover operator, the strings in the new population are grouped together into pairs at random. Single point crossover is then performed among pairs. The crossover point is only allowed between cells to maintain the chromosome integrity.

The mutation operator changes the characteristics of a given cell in the matrix. Therefore, it modifies the gate type and the two inputs, meaning that a completely new cell can appear in the chromosome. Moreover, it is applied an elitist algorithm and, consequently, the best solutions are always kept for the next generation.

To run the GA we have to define the number of individuals to create the initial population P. This population is always the same size across the generations, until the solution is reached.

The crossover rate *CR* represents the percentage of the population P that reproduces in each generation. Likewise, the mutation rate *MR* is the percentage of the population P that can mutate in each generation.

2.4 The Fitness Function

The initial population of circuits (strings) is generated at random. The search is then carried out among this population. The three different operators used are reproduction, crossover and mutation, as described in the sequel.

The calculation of F in (1) is divided in two parts, namely f_1 and f_2, where f_1 measures the functionality and f_2 measures the simplicity. In a first phase, we compare the output $\mathbf{Y}$ produced by the GA-generated circuit with the required values $\mathbf{Y}_R$, according to the truth table, on a bit-per-bit basis. By other words, f_{11} is incremented by *one* for each correct bit of the output until f_{11} reaches the maximum value f_{10}, that occurs, when we have a functional circuit. Once the circuit is functional, in a second phase, the GA tries to generate circuits with the least number of gates. This means that the resulting circuit must have as much genes $<$*gate type*$>$ $\equiv$ $<$*wire*$>$ as possible. Therefore, the index f_2, that measures the simplicity (the number of null operations), is increased by *one* (*zero*) for each *wire* (*gate*) of the generated circuit, yielding:

$$f_{10} = 2^{ni} \times no \tag{1a}$$

$$f_{11} = f_{11} + 1 \; if \; bit \; i \; of \; \mathbf{Y} = bit \; i \; of \; \mathbf{Y_R}, \quad i = 1, ..., f_{10} \tag{1b}$$

$$f_2 = f_2 + 1 \; if \; gate \; type = wire \tag{1c}$$

$$F = \begin{cases} f_1, & F < f_{10} \\ f_1 + f_2, & F \geq f_{10} \end{cases} \tag{1d}$$

where *ni* and *no* represent the number of inputs and outputs of the circuit.

3 Particle Swarm Optimization

In the literature about PSO the term 'swarm intelligence' appears rather often and, therefore, we begin by explaining why this is so.

Non-computer scientists (ornithologists, biologists and psychologists) did early research, which led into the theory of particle swarms. In these areas, the term 'swarm intelligence' is well known and characterizes the case when a large number of individuals are able of accomplish complex tasks. Motivated by these facts, some basic simulations of swarms were abstracted into the mathematical field. The usage of swarms for solving simple tasks in nature became an

Figure 8: Bird flock [24]

Figure 9: Fish schooling [25]

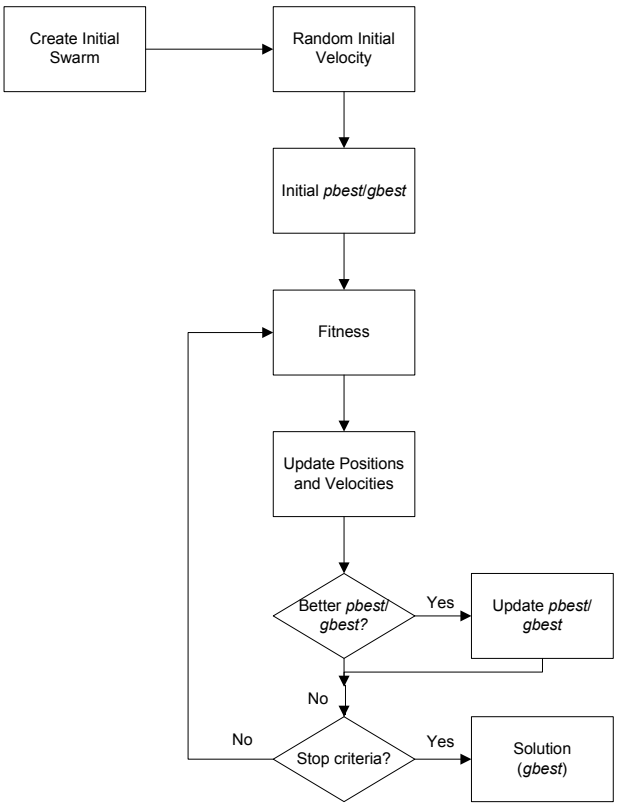

Figure 10: Particle Swarm Optimization Algorithm

intriguing idea in algorithmic and function optimization.

Eberhart and Kennedy were the first to introduce the PSO algorithm [11], which is an optimization method inspired in the collective intelligence of swarms of biological populations, and was discovered through simplified social model simulation of bird flocking, fishing schooling and swarm theory.

3.1 Parameters

In the PSO, instead of using genetic operators, as in the case of GAs, each particle (individual) adjusts its flying according with its own and its companions experiences. Each particle is treated as a point in a D-dimensional space and is manipulated as described below in the original PSO algorithm:

$$v_{id} = v_{id} + c_1 rand()(p_{id} - x_{id}) + c_2 rand()(p_{gd} - x_{id}) \quad (2)$$

$$x_{id} = x_{id} + v_{id} \quad (3)$$

where c_1 and c_2 are positive constants and *rand*() is a random function in the range [0,1], $X_i = (x_{i1}, x_{i2}, \ldots, x_{iD})$ represents the ith particle, $P_i = (p_{i1}, p_{i2}, \ldots, p_{iD})$ is the best previous position (the position giving the best fitness value) of the particle, the symbol g represents the index of the best particle among all particles in the population, and $V_i = (v_{i1}, v_{i2}, \ldots, v_{iD})$ is the rate of the position change (velocity) for particle i.

Expression (1) represents the flying trajectory of a population of particles. Equation (2) describes how the velocity is dynamically updated and equation (3) the position update of the "flying" particles. Equation (2) is divided in three parts, namely the momentum, the cognitive and the social parts. In the first part the velocity cannot be changed abruptly: it is adjusted based on the current velocity. The second part represents the learning from its own flying experience. The third part consists on the learning group flying experience [13, 15].

The first new parameter added into the original PSO algorithm is the inertia weight. The dynamic equation of PSO with inertia weight is modified to be:

$$v_{id} = w v_{id} + c_1 rand()(p_{id} - x_{id}) + c_2 rand()(p_{gd} - x_{id}) \quad (4)$$

$$x_{id} = x_{id} + v_{id} \quad (5)$$

where w constitutes the inertia weight that introduces a balance between the global and the local search abilities. A large inertia facilitates a global search while a small inertia weight facilitates the local search.

Another parameter, called constriction coefficient k, is introduced with the hope that it can insure a PSO to converge. A simplified method of incorporating it appears in equation (3), where k is function of c_1 and c_2 as presented in equation (8).

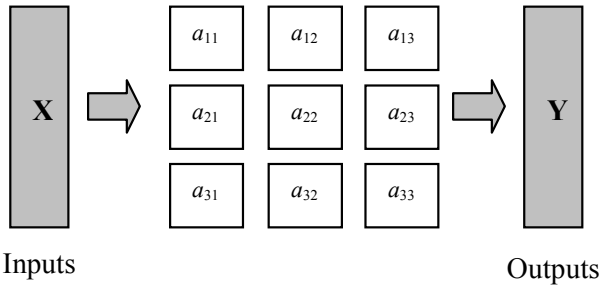

Figure 11: A 3×3 matrix **A** representing a circuit with input **X** and output **Y**

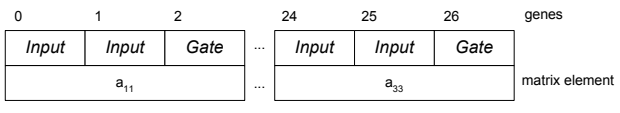

Figure 12: Chromosome for the matrix of figure 11

$$v_{id} = k[v_{id} + c_1 randp_{id} - x_{id} + c_2 randp_{gd} - x_{id}] \quad (6)$$

$$x_{id} = x_{id} + v_{id} \quad (7)$$

$$k = 2\left(2 - \phi - \sqrt{\phi^2 - 4\phi}\right)^{-1}, \Phi = c_1 + c_2, \Phi > 4 \quad (8)$$

3.2 Topologies

There are two different PSO topologies, namely the global version and the local version. In the global version of PSO, each particle flies through the search space with a velocity that is dynamically adjusted according to the particle's personal best performance achieved so far and the best performance achieved up to the moment by all particles. On the other hand, in the local version of PSO, each particle's velocity is adjusted according to its personal best and the best performance achieved so far within its neighborhood. The neighborhood of each particle is generally defined as topologically nearest particles to the particle at each side.

3.3 Algorithm

PSO is an evolutionary algorithm simple in concept, easy to implement and computationally efficient. Figures 13 and 14 present the generic genetic algorithm and the original procedure for implementing the PSO algorithm, respectively.

1. Initialize the population
2. Calculate the fitness of each individual in the population
3. Reproduce selected individuals to form a new population
4. Perform evolutionary operations such as crossover and mutation on the population
5. Loop to step 2 until some condition is met

Figure 13: Generic genetic algorithm

The different versions of the PSO algorithms are: the real-valued PSO, which is the original version of PSO and is well suited for solving real-value problems; the binary version of PSO, which is designed to solve binary problems; and the discrete version of

1. Initialize population in hyperspace
2. Evaluate fitness of individual particles
3. Modify velocities based on previous best and global (or neighborhood) best
4. Terminate on some condition
5. Go to step 2

Figure 14: PSO algorithm

PSO, which is good for solving the event-based problems. To extend the real-valued version of PSO to binary/discrete space, the most critical part is to understand the meaning of concepts such as trajectory and velocity in the binary/discrete space.

Kennedy and Eberhart [4] use velocity as a probability to determine whether x_{id} (a bit) will be in one state or another (zero or one). The particle swarm formula of equation (2) remains unchanged, except that now p_{id} and x_{id} are integers in [0.0,1.0] and a logistic transformation $S(v_{id})$ is used to accomplish this modification. The resulting change in position is defined by the following rule:

$$if\ rand() < S(v_{id})]\ \ then\ x_{id} = 1; \quad else\ x_{id} = 0; \quad (9)$$

where the function $S(v)$ is a sigmoid limiting transformation.

4 Combination of the GA and the PSO algorithms

The algorithm developed in the present work combines a GA with a PSO. The GA is executed in first place and is followed by the PSO as shown in figure 15. The interlacing of the algorithms is repeated until the solution is found. The number of generations of each algorithm ($n1$ for the GA and $n2$ for the PSO) is initially defined at the moment of running the simulations.

4.1 Experiments and Simulation Results

Reliable execution and analysis of a EA usually requires a large number of simulations to provide a reasonable assurance that stochastic effects have been properly considered. Therefore, we developed n = 20 simulations for each case under analysis.

The experiments consist on running the combination of algorithms to generate a typical combinational logic circuit, namely a 2-to-1 multiplexer ($M2-1$) and a 4-bit parity checker (*PC4*), using the fitness

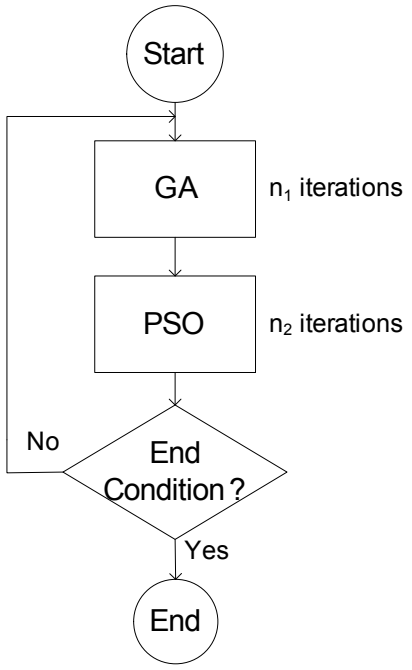

Figure 15: Flowchart of the developed algorithm

function described previously and the two gate sets presented in table 1.

- the $M2-1$ circuit, has 3 inputs **X** = $\{S_0, I_1, I_0\}$ and 1 output $\mathbf{Y}_R$ = {O}. The matrix **A** size is 3 × 3, and CL = 27. Since the 2-to-1 multiplexer has *ni* = 3 and *no* = 1, it results f_{10} = 8 and $F \geq 12$,

- the $PC4$ circuit, has 4 inputs **X** = $\{A_3, A_2, A_1 A_0\}$ and 1 output $\mathbf{Y}_R$ = {P}. The matrix **A** size is 4 × 4, and the length of each string representing a circuit (*i.e.*, the chromosome length) is CL = 48. In this case *ni* = 4 and *no* = 1, resulting f_{10} = 16 and $F \geq 24$.

Table 2 presents the Boolean truth Tables for the circuits under study.

Having a superior performance means achieving solutions with a smaller average number of generations *Av*(N) and a smaller standard deviation of the number of generations $S(N)$ to achieve the solution in order to reduce the stochastic nature of the algorithm.

Figures 16 - 19 depict the average number of generations *Av*(N) and the standard deviation of the number of generations to achieve the solution $S(N)$ with $0 \leq n1, n2 \leq 6$ for the $M2-1$ circuit, using the Gsets 6 and 4, respectively.

Figures 20 - 23 show the average number of generations *Av*(N) and the standard deviation of the number of generations to achieve the solution $S(N)$ with

$PC4$

A_3	A_2	A_1	A_0	P
0	0	0	0	0
0	0	0	1	1
0	0	1	1	0
0	0	1	0	1
0	1	1	0	0
0	1	1	1	1
0	1	0	1	0
0	1	0	0	1
1	1	0	0	0
1	1	0	1	1
1	1	1	1	0
1	1	1	0	1
1	0	1	0	0
1	0	1	1	1
1	0	0	1	0
1	0	0	0	1

$M2-1$

S_0	I_1	I_0	O
0	0	0	0
0	0	1	1
0	1	1	1
0	1	0	0
1	1	0	1
1	1	1	1
1	0	0	0
1	0	0	0

Table 2: Circuit truth tables

$0 \leq n1, n2 \leq 6$ for the $PC4$ circuit, using Gsets 6 and 4, respectively.

Analyzing the charts is possible to see the advantage of combining the two algorithms particularly in respect to the average number of generations *Av*(N).

We verify the existence of an optimal locus from ($n1$, $n2$)= (2,4) up to ($n1$, $n2$) = (4,2).

5 CONCLUSIONS

The main conclusion of this study is that the combination of the evolutionary algorithm with the swarm intelligence algorithm leads to superior results than the execution of the same algorithms individually.

With this hybrid algorithm it is possible to take advantage of the benefits of each algorithm.

Future research will address the automatic adjust, during the execution, of the number of iterations $n1$ and $n2$ of each evolutionary algorithm.

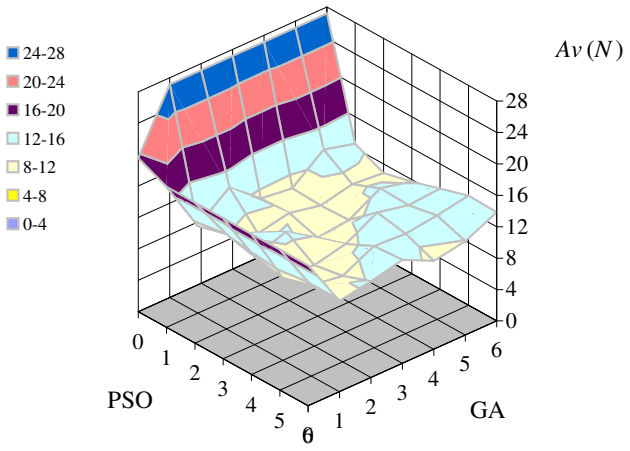

Figure 16: Average number of generations *Av*(*N*) for the $M2-1$ circuit using Gset 6

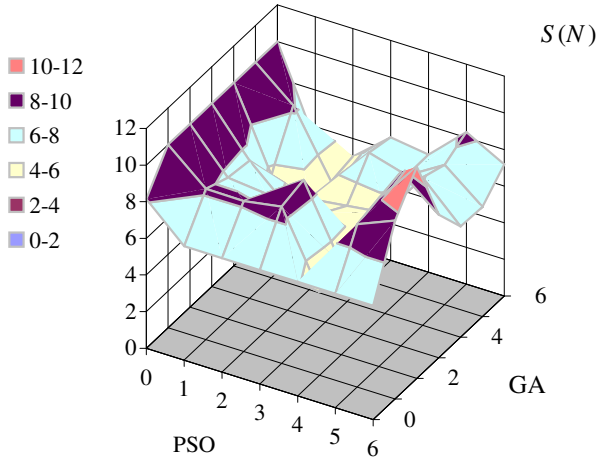

Figure 17: Standard deviation of the number of generations to achieve the solution *S*(*N*) for the $M2-1$ circuit using Gset 6

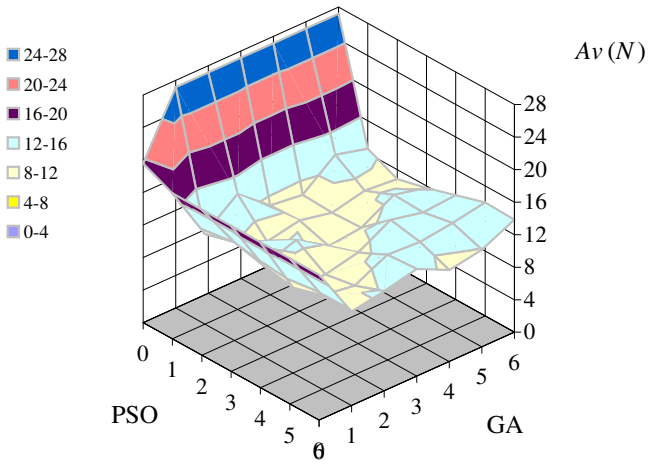

Figure 18: Average number of generations *Av*(*N*) for the $M2-1$ circuit using Gset 4

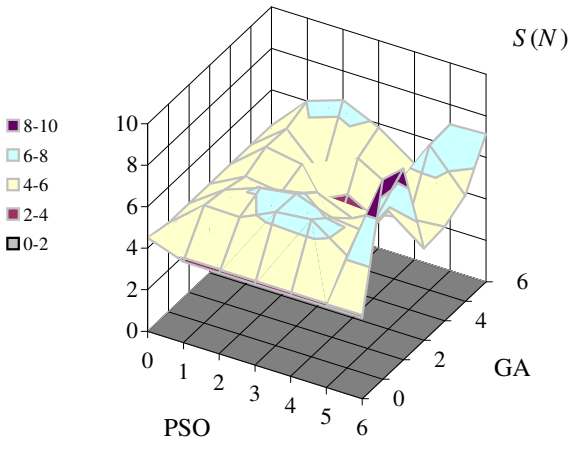

Figure 19: Standard deviation of the number of generations to achieve the solution *S*(*N*) for the $M2-1$ circuit using Gset 4

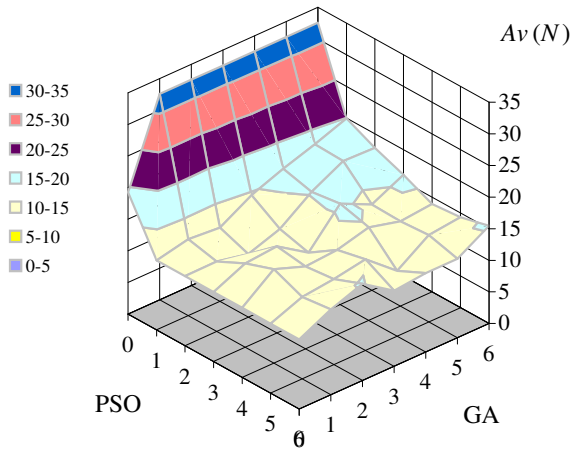

Figure 20: Average number of generations *Av*(*N*) for the $PC4$ circuit using Gset 6

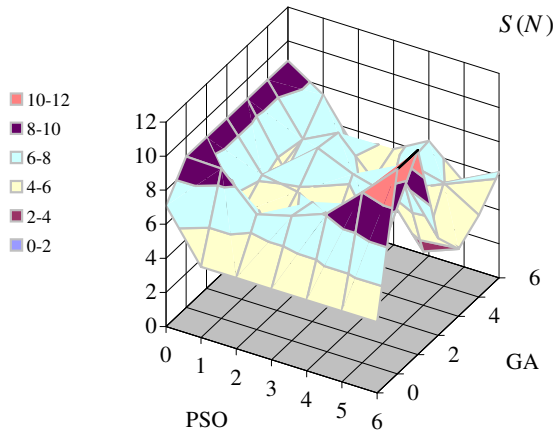

Figure 21: Standard deviation of the number of generations to achieve the solution *S*(*N*) for the $PC4$ circuit using Gset 6

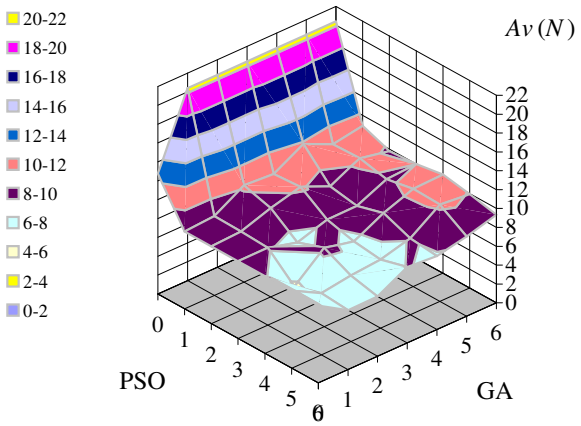

Figure 22: Average number of generations *Av*(*N*) for the $PC4$ circuit using Gset 4

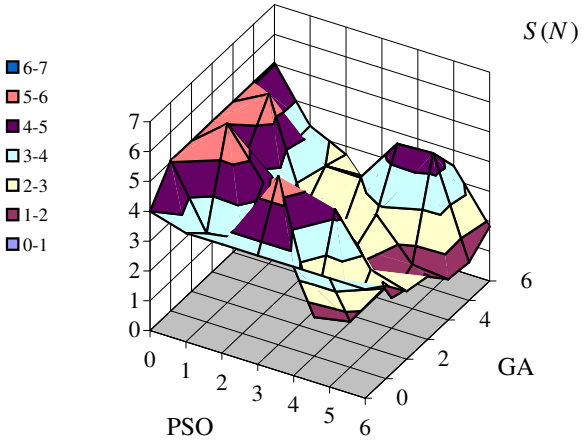

Figure 23: Standard deviation of the number of generations to achieve the solution *S*(*N*) for the $PC4$ circuit using Gset 4

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