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# Characterization of rockfalls from seismic signal: insights from laboratory experiments

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Abstract. The seismic signals generated by rockfalls can provide information on their dynamics and location. However, the lack of field observations makes it difficult to establish clear relationships between the characteristics of the signal and the source. In this study, scaling laws are derived from analytical impact models to relate the mass and the speed of an individual impactor to the radiated elastic energy and the frequency content of the emitted seismic signal. It appears that the radiated elastic energy and frequencies decrease when the impact is viscoelastic or elasto-plastic compared to the case of an elastic impact. The scaling laws are validated with laboratory experiments of impacts of beads and gravels on smooth thin plates and rough thick blocks. Regardless of the involved materials, the masses and speeds of the impactors are retrieved from seismic measurements within a factor of 3. A quantitative energy budget of the impacts is established. On smooth thin plates, the lost energy is either radiated in elastic waves or dissipated in viscoelasticity when the impactor is large or small with respect to the plate thickness, respectively. In contrast, on rough thick blocks, the elastic energy radiation represents less than 5% of the lost energy. Most of

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the energy is lost in plastic deformation or rotation modes of the bead owing to surface roughness. Finally, we estimate the elastic energy radiated during field scale rockfalls experiments. This energy is shown to be proportional to the boulder mass, in agreement with the theoretical scaling laws.

#### 1. Introduction

Rockfalls represent a major natural hazard in steep landscapes. Because of their unpre-1 2 dictable and spontaneous nature, the seismic monitoring of these gravitational instabilities has raised a growing interest for risks assessment in the last decades. Recent studies 3 showed that rockfalls can be automatically detected and localized with high precision from 4 the seismic signal they generate [Suriñach et al., 2005; Deparis et al., 2008; Dammeier 5 et al., 2011; Hibert et al., 2011, 2014a]. A burning challenge is to obtain quantitative 6 information on the gravitational event (volume, propagation velocity, extension,...) from 7 the characteristics of the associated seismic signal [Norris, 1994; Deparis et al., 2008; Vila-8 josana et al., 2008; Favreau et al., 2010; Dammeier et al., 2011; Hibert et al., 2011, 2014a; 9 Moretti et al., 2012, 2015; Yamada et al., 2012]. 10

Some authors found empirical relationships between the rockfall volume and the max-11imum amplitude of the signal or the radiated seismic energy [Norris, 1994; Hibert et al., 12 2011; Yamada et al., 2012]. The precursory work of Norris [1994] on rockfalls of large 13 volume  $> 10^4$  m<sup>3</sup> at Mount St Helens showed that the maximum amplitude of the emitted 14 signal depends linearly on the rockfall volume. This is in agreement with the observa-15 tions of Yamada et al. [2012] on landslides triggered in Japan by Typhoon Talas in 2011. 16 The authors observed that the integral of the squared signal amplitude measured at 1 17 km from the source varied as the square the landslide volume. In contrast, *Hibert et al.* 18 [2011] showed that the seismic energy emitted by rockfalls is proportional to their volume 19 in the Dolomieu crater of the Piton de la Fournaise volcano, Réunion Island. Moreover, 20 Dammeier et al. [2011] used a statistical approach and estimated the volume V of several 21

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<sup>22</sup> rockfalls in the central Alps from the measurement of the duration  $t_s$ , enveloppe area <sup>23</sup> *EA* and peak amplitude *PA* of the generated seismic signal. For twenty well constrained <sup>24</sup> events, they found the empirical scaling law:  $V \propto t_s^{1.0368} EA^{-0.1248} PA^{1.1446}$ . The volumes <sup>25</sup> estimated with this relation were close to the measured ones but the results were sensitive <sup>26</sup> to the distance of the seismic stations from the events.

Other surveys investigated the ratio of the radiated seismic energy  $W_{el}$  over the potential 27 energy  $\Delta E_p$  lost by the rockfalls from initiation to deposition [Deparis et al., 2008; Hibert 28 et al., 2011, 2014a; Lévy et al., 2015]. Deparis et al. [2008] studied ten rockfalls that 29 occurred between 1992 and 2001 in the french Alps and estimated that the ratio  $W_{el}/\Delta E_p$ 30 was between  $10^{-5}$  and  $10^{-3}$ . *Hibert et al.* [2011, 2014a] observed that the ratios of the 31 seismic energy  $W_{el}$  radiated by the rockfalls in the Dolomieu crater over their potential 32 energy lost  $\Delta E_p$  varied from 5.10<sup>-5</sup> to 2.10<sup>-3</sup>. Finally, Lévy et al. [2015] found  $W_{el}/\Delta E_p \approx$ 33  $1.1.10^{-5} - 2.8.10^{-5}$  for pyroclastic and debris flows that occurred on the Souffrière Hills 34 volcano in Montserrat Island, Lesser Antilles. Most of the aforementioned studies focused 35 on a specific rockfalls site [Norris, 1994; Deparis et al., 2008; Dammeier et al., 2011; Hibert 36 et al., 2011, 2014a; Yamada et al., 2012; Lévy et al., 2015]. It is however difficult to test 37 the developed techniques on other sites because only a few of rockfalls areas are nowadays 38 simultaneously seismically and optically monitored. 39

Because gravitational events are very complex, it is still not clear what parameters controls their seismic emission. The seismic signals generated by rockfalls on the field are partially composed of waves emitted by individual impacts of boulders, triggering high frequencies noise, typically higher than 1 Hz [e.g. *Deparis et al.*, 2008; *Vilajosana et al.*, *2008; Helmstetter and Garambois*, 2010; *Hibert et al.*, 2014b; *Lévy et al.*, 2015] and by

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long period stresses variations owing to the mass acceleration and deceleration over the
topography, responsible for lower frequencies in the signal (< 1 Hz) [e.g. Kanamori and</li> *Given*, 1982; *Favreau et al.*, 2010; *Allstadt*, 2013]. To start the work on understanding the
seismic emission of rockfalls, we focus here on the seismic signal generated by impacts.

The dynamics of impact can be described at first order by the classical model proposed 49 by *Hertz* [1882] that gives the analytical expression of the force of impact of an elastic 50 sphere on a solid elastic surface [see Johnson, 1985]. From the comparison of the impacts 51 forces and durations measured from the emitted seismic signal with that predicted by *Hertz* 52 [1882], Buttle and Scruby [1990] and Buttle et al. [1991] managed to retrieve the diameter 53 of sub-millimetrical particles impacting a thick block. However, their computation was 54 based on the direct compressive wave, measured at the opposite of the impact on the 55 target block. Their configuration can therefore not be exported to field context. Also 56 based on *Hertz* [1882]'s theory, *Tsai et al.* [2012] expressed the long period power spectral 57 density generated by the impacts of sediments on the bed of rivers as a function of the 58 river parameters such the particle size distribution, the impact rate and the bed load flux. 59 From seismic measurements of Burtin et al. [2008] on trans-Himalayan Trisuli River, Tsai 60 et al. [2012] were then able to quantitatively deduce the bed load flux. 61

In this paper, we adopt a similar approach. The basic idea is to derive from *Hertz* [1882]'s model analytical scaling laws relating the radiated elastic energy and the frequencies of the seismic signal generated by an impact to the mass and the speed of the impactor. These laws can then be inverted to deduce the impact parameters from a measurement of the emitted seismic signal. Note that *Tsai et al.* [2012] assumed for their analytical model that the impact duration was instantaneous because they focused on

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signals of long periods compared with this duration. On the contrary, we do not assume an instantaneous impact here because we try here to use the whole spectrum content. Indeed, in order to robustly estimate the impact parameters from the emitted signal using our scaling laws, we need to determine the absolute energy radiated in elastic waves and, therefore, the entire amplitude spectrum of the seismic signal generated by the impact. This implies:

1. to record signal periods much smaller than the impact duration;

2. to know well the elastic properties of the impactor and of the substrate, i.e. their
elastic modulii, their density, the type of mode excited in the substrate after an impact,
its dispersion and how its energy attenuates with increasing distance from the source.

These two conditions are not easy to address in the field because usual sampling times 78 are of the order of the typical impact durations ( $\sim 0.01$  s) and because of the strong 79 heterogeneity of the ground. Therefore, in order to test our analytical scaling laws, we 80 perform controlled laboratory experiments of impacts of spherical beads on thin plates 81 with an ideal smooth surface, then on rough thick blocks i.e., in a context similar to that 82 of the field. A series of impact experiments is also conducted with gravels to quantify 83 how the relations between impacts properties and signal characteristics change when the 84 impactor has a rough surface, which is a more realistic case i.e., closer to what is observed 85 for natural rockfalls. 86

During an impact, a significant part of the impactor's energy can be lost in inelastic processes such as plastic i.e., irreversible, deformation of the impactor or the ground [Davies, 1949] or viscoelastic dissipation in the vicinity of the impact [Falcon et al., 1998]. These losses are not considered in Hertz [1882]'s elastic impact model. In this paper, we use

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analytical models of viscoelastic and elasto-plastic impact to estimate how the frequen-91 cies of the emitted vibration and the radiated elastic energy deviate from that predicted 92 using *Hertz* [1882]'s theory when inelastic dissipation occurs. Using these models, we 93 interpret the discrepancy observed between the measured values in our experiments and 94 those predicted by the elastic model of *Hertz* [1882]. Another advantage of the laboratory 95 experiments is that the total energy lost during the impact can be easily measured from 96 the velocity change of the impactor before and after the impact. We can then establish a 97 quantitative energy budget among the energy radiated in elastic waves and that dissipated 98 in inelastic processes. This allow us to better understand the process of wave generation 99 by an impact and to roughly extrapolate what should be the relative importance of the 100 different loss processes for natural rockfalls. 101

This paper is structured as follows. In section 2, we recall the theory for elastic, vis-102 coelastic and elasto-plastic impacts of a sphere on a plane surface and we derive the 103 analytical scaling laws from this theory. The experimental setup is presented in section 3. 104 In section 4, we test experimentally the scaling laws established in section 2 and retrieve 105 the masses and speeds of the impactors from the measured seismic signals. In addition, 106 107 we establish the energy budget of the impacts among elastic and inelastic losses and observe how this budget varies on smooth thin plates and rough thick blocks when the bead 108 mass and the elastic parameters change. In section 5, the discrepancy of the experimental 109 results with the theory is discussed. Finally, the analytical scaling laws demonstrated in 110 this paper are compared with empirical relations observed in drop experiments of large 111 boulders in a natural context. We identify the issues that should be overcome in order to 112 apply our scaling laws to natural impact situations. 113

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#### 2. Theory: Relations Between Impact Parameters and Seismic Characteristics

The vibration displacement  $\mathbf{u}(\mathbf{r}, t)$  at the distance  $\mathbf{r}$  from an impact is given by the time convolution of the force  $\mathbf{F}(\mathbf{r}_s, t)$  applied to the ground at position  $r_s$  with the Green's function  $\overline{\mathbf{G}}(\mathbf{r}, \mathbf{r}_s, t)$  of the structure where the wave propagates [Aki and Richards, 1980]:

$$\mathbf{u}(\mathbf{r},t) = \bar{\mathbf{G}}(\mathbf{r},\mathbf{r}_s,t) * \mathbf{F}(\mathbf{r}_s,t), \qquad (1)$$

where \* stands for the time convolution product. In our experiments, we only have access to the vibration acceleration in the direction normal to the surface  $a_z(r, t)$ . In the time Fourier domain, this acceleration is given by:

$$\tilde{A}_z(r,f) = -(2\pi f)^2 \tilde{G}_{zz}(r,f) \tilde{F}_z(f), \qquad (2)$$

where f is the frequency and  $\tilde{F}_z(f)$  is the time Fourier transform of the vertical impact 114 force  $F_z(t)$ . The expression of the Green's function  $\tilde{G}_{zz}(r, f)$  is different when the impact 115 duration is greater or smaller than the two-way travel time of the emitted wave in the 116 structure thickness, i.e. for impacts on thin plates and on thick blocks, respectively. A 117 plate of thickness h vibrates normally to its surface because the fundamental  $A_0$  mode of 118 Lamb carries most of the energy [Royer and Dieulesaint, 2000; Farin et al., 2015]. The 119 module of the Green's function of this mode of vibration can be approximated by [e.g. 120 Goyder and White, 1980]: 121

$$|\tilde{G}_{zz}(r,f)| = \frac{1}{8Bk^2} \sqrt{\frac{2}{\pi kr}},$$
(3)

where k is the wave number,  $B = h^3 E_p / 12(1 - \nu_p^2)$  is the bending stiffness and  $E_p$  and  $\nu_p$ are the Young's modulus and the Poisson ratio of the impacted structure, respectively. At low frequencies i.e., for  $kh \ll 1$ , the wave number k is related to the angular frequency  $\omega$  by  $k^4 = \omega^2 \rho_p h/B$ , where  $\rho_p$  is the plate density.

122

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In contrast, an impact on a thick block generates compressive, shear and Rayleigh waves [*Miller and Pursey*, 1955; *Aki and Richards*, 1980]. For kr >> 1 i.e., in far field, the displacement mainly results from Rayleigh waves and the Green's function can be approximated by [*Miller and Pursey*, 1955; *Farin et al.*, 2015]:

131 
$$|\tilde{G}_{zz}(r,f)| \approx \frac{\xi^2 \omega}{2\mu c_P} \frac{\sqrt{x_0(x_0^2 - 1)}}{f'_0(x_0)} \sqrt{\frac{2c_P}{\pi \omega r}},$$
 (4)

132 where  $\mu$  is the shear Lamé coefficient,  $c_P$  is the compressional wave speed,  $\xi = \sqrt{2(1-\nu_p)/(1-2\nu_p)}$ ,  $f_0(x) = (2x^2-\xi^2)^2 - 4x^2\sqrt{(x^2-1)(x^2-\xi^2)}$  and  $x_0$  is the real 134 root of  $f_0$ .

In this section, we derive analytical scaling laws that relate the energy radiated in 135 elastic waves and the characteristic frequencies of the vibration  $\tilde{A}_z(r, f)$  emitted by an 136 impact to the impact parameters (mass m, speed  $V_z$ ). Because the vibration  $\tilde{A}_z(r, f)$  is 137 controlled by the impact force  $\tilde{F}_z(f)$  [equation (2)], the scaling laws are different when 138 the impact is elastic or when viscoelastic dissipation or plastic deformation occur. Let 139 us first recall the expression of the impact force for an elastic impact and how it changes 140 for an inelastic impact. Note that we do not use any elasto-visco-plastic model of impact 141 here because elastic energy radiation, viscoelastic dissipation and plastic deformation are 142 never simultaneously significant in our experiments, even though it could be the case on 143 the field. For example, in certain cases, viscoelastic and plastic losses are negligible and 144 an elastic impact model is sufficient to describe the energy transfer. 145

#### 2.1. Impact Models

# 146 2.1.1. Elastic Impact Model

# 147 2.1.1.1. Hertz's Model

148 *Hertz* [1882] gives the force of elastic contact of a sphere of mass m on a plane as a 149 function of their interpenetration depth  $\delta_z(t)$  (Figure 1a):

$$F_z(t) = -K\delta_z^{3/2}(t), \tag{5}$$

151 where

150

152

$$K = \frac{4}{3}R^{1/2}E^*,\tag{6}$$

with R, the sphere radius and  $1/E^* = (1 - \nu_s^2)/E_s + (1 - \nu_p^2)/E_p$ , where  $\nu_s$ ,  $\nu_p$ ,  $E_s$ ,  $E_p$  are respectively the Poisson's ratios and the Young's moduli of the constitutive materials of the sphere and the impacted plane.

During an impact, the displacement of the center of mass of the sphere is equal to the interpenetration  $\delta_z(t)$ . Neglecting the gravity force, the equation of motion of the sphere is then:

159 
$$m\frac{\mathrm{d}^2\delta_z(t)}{\mathrm{d}t^2} = -K\delta_z^{3/2}(t).$$
(7)

160 The solution of equation (7) is of the form  $\delta_z(t) = \delta_{z0} f(t/T_c)$ . The maximum interpene-161 tration depth  $\delta_{z0}$  and the impact duration  $T_c$  are respectively given by [Johnson, 1985]:

162 
$$\delta_{z0} = \left(\frac{5mV_z^2}{4K}\right)^{2/5},\tag{8}$$

163 and

164 
$$T_c \approx 2.94 \frac{\delta_{z0}}{V_z} \approx 2.87 \left(\frac{16m^2}{9K^2V_z}\right)^{1/5},$$
 (9)

165 where  $V_z$  is the impact speed.

166 The maximum value of the impact force is therefore, according to equation (5):

167 
$$F_0 = K \delta_{z0}^{3/2} = K \left(\frac{5mV_z^2}{4K}\right)^{3/5}, \qquad (10)$$

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168 In the following, the interpenetration depth  $\delta_z(t)$ , the time t and the force  $F_z(t)$  are 169 respectively scaled by  $\delta_{z0}$ ,  $\delta_{z0}/V_z$  and  $F_0$ , that contain all the informations on the impact 170 characteristics.

# 171 2.1.1.2. Hertz-Zener's model for impacts on thin plates

*Hertz* [1882]'s model [equation (8)] is valid provided that the energy radiated in elastic 172 waves during the impact represents a small proportion of the impact energy  $\frac{1}{2}mV_z^{1/2}$ 173 [Hunter, 1957; Johnson, 1985]. This is not the case when the thickness of the impacted 174 structure is around or lower than the diameter of the impactor, i.e. for impacts on thin 175 plates and membranes [e.g. Zener, 1941; Farin et al., 2015]. When the energy lost in 176 plate vibration during the impact is not negligible, Zener [1941] proposed a more exact 177 description than *Hertz* [1882]'s model of the interaction between the sphere and the plate's 178 surface. One has to distinguish the sphere displacement z, given by: 179

180 
$$m\frac{\mathrm{d}^2 z(t)}{\mathrm{d}t^2} = -F_z(t), \qquad (11)$$

181 from the plate's surface displacement  $u_z$  at the position of the impact, whose time deriva-182 tive is:

183 
$$\frac{\mathrm{d}u_z(t)}{\mathrm{d}t} = Y_{el}F_z(t),\tag{12}$$

where  $Y_{el}$  is the real part of the time derivative of the Green's function at the impact position  $\Re (dG_{zz}(r_0, t)/dt)$ , i.e. the radiation admittance. This function is given by [Goyder and White, 1980] for plates:

187 
$$Y_{el} = \frac{1}{8\sqrt{B\rho_p h}},\tag{13}$$

188 with B, the bending stiffness and h, the plate thickness. In these equations, the impact 189 force  $F_z(t)$  follows *Hertz* [1882]'s theory [equation (5)].

The difference of equation (11) and the derivative of equation (12) gives the following equation for the relative movement of the sphere and of the substrate i.e., the interpenetration  $\delta_z(t) = z(t) - u_z(t)$ , in dimensionless form with  $\delta^* = \delta_z/\delta_{z0}$  and  $t^* = V_z t/\delta_{z0}$ :

193 
$$\frac{\mathrm{d}^2\delta^*}{\mathrm{d}t^{*2}} = -\frac{5}{4}\left(\delta^{*3/2} + \lambda_Z \frac{\mathrm{d}\delta^*}{\mathrm{d}t^*}\delta^{*1/2}\right),\tag{14}$$

194 with

195 
$$\lambda_Z \approx 0.175 \frac{E^{*2/5}}{\rho_s^{1/15} \sqrt{B\rho_p h}} m^{2/3} V_z^{1/5}.$$
(15)

In equation (14), we retrieve the impact model of *Hertz* [1882] [equation (7)] with a corrective term that depends on the parameter  $\lambda_Z$ . This corrective term becomes negligible when the thickness h of the structure is much larger than the diameter d of the impactor because the parameter  $\lambda_Z$  tends towards 0 [Zener, 1941]. Therefore, for impacts on elastic half-spaces i.e., on thick blocks, the corrective term disappears and the model of Zener [1941] [equation (14)] matches with that of *Hertz* [1882] [equation (7)]. As a consequence, this model is only relevant for impacts on thin plates.

Equation (14) is solved numerically for different values of  $\lambda_Z$  with the initial conditions  $\delta^*(0) = 0$  and  $\frac{d\delta^*}{dt^*}(0) = 1$ . The impact force  $F_z(t)/F_0 = \delta^{*3/2}$  is shown on Figure 1b. When  $\lambda_Z$  increases i.e., when *m* and  $V_z$  increase, the force profile looses its symmetry with respect to its maximum, its amplitude decreases and its duration increases. For an inelastic coefficient  $\lambda_Z = 0.25$ , the force is only slightly affected. Practically,  $\lambda_Z$  is always smaller than 0.5 in our experiments.

#### 209 2.1.2. Viscoelastic Impact Model

210 Viscoelastic dissipation is related to the viscosities of the materials involved in the 211 impact and can be described as a heat loss. Viscoelastic solids are often represented by

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a spring and a dashpot in parallel (Kelvin-Voigt model). Hertz [1882]'s theory has been extended to viscoelastic impacts, adding a force  $F_{diss}(t)$  in equation (7) to model viscous dissipation [Kuwabara and Kono, 1987; Falcon et al., 1998; Ramírez et al., 1999]:

215 
$$F_{diss}(t) = -\frac{3}{2}DK\frac{\mathrm{d}\delta_z(t)}{\mathrm{d}t}\delta_z^{1/2}(t), \qquad (16)$$

with D, a characteristic time depending on the materials viscosities and elastic constants
[Hertzsch et al., 1995; Brilliantov et al., 1996; Ramírez et al., 1999]. The expression of D
is only given in the literature in case when the sphere and the plane have the same elastic
parameters E and v:

220 
$$D = \frac{2}{3} \frac{\chi^2}{(\chi + 2\eta)} \frac{(1 - \nu^2)(1 - 2\nu)}{E\nu^2},$$
 (17)

where  $\chi$  and  $\eta$  are the bulk and shear viscosities, respectively. We can not measure these two last parameters in our experiments and they are not tabulated in our frequencies range of interest, therefore D will be an adjustable parameter.

# 224 The dimensionless equation of motion for a viscoelastic impact is then:

225 
$$\frac{\mathrm{d}^2\delta^*}{\mathrm{d}t^{*2}} = -\frac{5}{4}\left(\delta^{*3/2} + \alpha \frac{\mathrm{d}\delta^*}{\mathrm{d}t^*}\delta^{*1/2}\right),\tag{18}$$

which is the same expression as for *Zener* [1941]'s model [equation (14)] but with a different parameter:

228 
$$\alpha = \frac{3}{2} D \frac{V_z}{\delta_{z0}} \simeq 1.4 D \frac{E^{*2/5}}{\rho_s^{1/15}} \frac{V_z^{1/5}}{m^{1/3}},$$
 (19)

the viscoelastic parameter [Ramírez et al., 1999]. For α = 0 (i.e., D = 0), equation (18)
matches with equation (7) for elastic impacts.

Because equations (14) and (18) are identical, when  $\alpha$  increases the force profile varies exactly the same way as when  $\lambda_Z$  increases in Zener [1941]'s model (Figure 1b). However,

note that the corrective terms to *Hertz* [1882]'s model in the viscoelastic and *Zener* [1941]'s 233 models have a different physical origin. The viscoelastic corrective term is due to the fact 234 that the impactor and the ground have an intrinsic viscosity [Falcon et al., 1998]. This 235 term is stronger when the mass m, or diameter d, of the sphere decreases [equation (19)]. 236 On the contrary, the corrective term of *Zener* [1941]'s model comes from the fact that a 237 larger amount of the impactor's kinetic energy is transferred into plate vibration during 238 the impact when the sphere's diameter d is large compared to the plate thickness h [Zener, 239 1941] [equation (15)]. We can therefore assume that the viscoelastic and Zener [1941]'s 240 impact models are never simultaneously effective. 241

# 242 2.1.3. Elasto-plastic Impact Model

Plastic (i.e. not reversible) deformations result from irreversible structural modifications 243 which occur when the pressure on the contact area  $P(t) = F_z(t)/2\pi R\delta_z(t)$  reaches the 244 dynamic yield strength  $P_Y = 3Y_d$  of the material, where  $Y_d$  is the dynamic yield stress of 245 the softest material [Crook, 1952; Johnson, 1985]. Plastic deformation can be evidenced 246 by the apparition of a crater at the impact position. The energy lost to create this crater 247 modifies the shape of the impact force with respect to the case of an elastic or viscoelastic 248 impact. A model was proposed by Troccaz et al. [2000] to describe the evolution of the 249 impact force when the limit of elastic behavior is exceeded. This model is based on the 250 hypothesis that only the sphere or the structure deforms plastically. Such an impact is 251 composed of three successive phases: 252

253 1. The impact is elastic while  $P(t) < P_Y$  and the impact force F(t) follows equation 254 (5);

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255 2. When  $P(t) \ge P_Y$  the deformation is fully plastic and the force expression becomes 256  $F_z(t) = -2\pi R P_Y \delta_z(t)$  until the force reaches a maximum  $F_{max}$ , which is smaller than the 257 maximum value  $F_0$  for an elastic impact;

3. The rebound is elastic with  $F_z(t) = F_{max} \left( (\delta_z(t) - \delta_r) / (\delta_{max} - \delta_r) \right)^{3/2}$ , where  $\delta_{max}$ is the maximum interpenetration reached and  $\delta_r$  is the residual deformation after plastic deformation, that is neglected (i.e., considered to be 0) in the following.

261 The dimensionless equation of motion during plastic deformation (phase 2) is then, if 262  $\delta_z(t)$  and time t are respectively scaled by  $\delta_{z0}$  and  $\delta_{z0}/V_z$ :

263 
$$\frac{\mathrm{d}^2\delta^*}{\mathrm{d}t^{*2}} = -\frac{5}{4}\frac{P_Y}{P_0}\delta^*,\tag{20}$$

where  $P_0$  is the maximum stress during Hertz's elastic impact:

265 
$$P_0 = \frac{K\delta_{z0}^{3/2}}{2\pi R\delta_{z0}} = \frac{2}{3\pi} \left(\frac{5}{4}\right)^{1/5} \rho_s^{1/5} E^{*4/5} V_z^{2/5}.$$
 (21)

Equation (20) depends only on the stresses ratio  $P_Y/P_0$  that is independent of the impactor mass m. When this ratio is greater or equal to 1, the impact is purely elastic. The amplitude of the impact force decreases as the stresses ratio  $P_Y/P_0$  decreases (Figure 1c). Both the duration of the impact and the time to reach the maximum amplitude increase for an elasto-plastic impact with respect to the elastic case.

### 2.2. Analytical Scaling Laws

The seismic signal generated by an impact can be characterized by the radiated elastic energy  $W_{el}$  and by a frequency. Here we relate analytically these seismic characteristics with the mass m and the speed  $V_z$  of the impactor using the impact models presented above.

#### 275 2.2.1. Radiated Elastic Energy

The energy  $W_{el}$  radiated in elastic waves is the work done by the impact force  $F_z(t)$ during the impact, i.e.,

278 
$$W_{el} = \int_{-\infty}^{+\infty} F_z(t) \frac{\mathrm{d}u_z(t)}{\mathrm{d}t} \mathrm{d}t = \int_{-\infty}^{+\infty} |\tilde{F}_z(f)|^2 \tilde{Y}_{el}(f) \mathrm{d}f, \qquad (22)$$

according to Parceval's theorem, where  $\frac{du_z(t)}{dt}$  is the vibration speed at the impact position [equation (12)] and  $\tilde{Y}_{el}(f)$  is the time Fourier transform of the radiation admittance.

The radiated elastic energy  $W_{el}$  is different for impacts on thin plates and on thick blocks because the radiation admittance  $\tilde{Y}_{el}(f)$  has a different expression. Developing equation (22), we obtain in Table 1 analytical expressions for the elastic energy  $W_{el}$  radiated during an impact on thin plates and thick blocks, as a function of the impact parameters (see Appendix A for details on the calculations). On thin plates,

286 
$$W_{el} = a_1 C_{plate} m^{5/3} V_z^{11/5}$$
(23)

287 and, on thick blocks,

$$W_{el} = a_2 C_{block} m V_z^{13/5}, (24)$$

where coefficients  $a_1$  and  $a_2$  depends only on the elastic parameters (see Table 1). In these 289 expressions,  $C_{plate} = \int_{-\infty}^{+\infty} |g(t^*)|^2 dt^*$  and  $C_{block} = \int_{0}^{+\infty} f^{*2} |\tilde{g}(f^*)|^2 df^*$ , where  $|g(t^*)| = \int_{0}^{+\infty} |g(t^*)|^2 df^*$ 290  $|F_z(t)|/F_0$  with  $t^* = V_z t/\delta_{z0}$  and where  $\tilde{g}(f^*)$  is the time Fourier transform of  $g(t^*)$ . For 291 an elastic impact i.e., with  $F_z(t)$  given by equation (5), we obtain  $C_{plate} \simeq 1.21$  and  $C_{block} \simeq$ 292 0.02. The function  $g(t^*)$  has a lower amplitude when the impact is inelastic compared to 293 the case of an elastic impact (Figures 1b and 1c). Therefore, both coefficients  $C_{plate}$  and 294  $C_{block}$  decrease when the viscoelastic parameter  $\alpha$  increases and when the stresses ratio 295  $P_Y/P_0$  decreases (Figures 2a and 2b). Moreover, on thin plates  $C_{plate}$  also decreases when 296 the parameter  $\lambda_Z$  increases (Figure 2a). As a consequence, less energy is radiated in the 297

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298 form of elastic waves when the impact is inelastic with respect to the case of an elastic
299 impact.

On thick blocks, the radiated elastic energy  $W_{el}$  is proportional to the impactor's mass m for a given impact speed  $V_z$  [equation (24)]. Moreover, the ratio of  $W_{el}$  over the impact energy  $E_c = \frac{1}{2}mV_z^2$  varies as  $V_z^{3/5}$  and is independent of the sphere mass m, which is in agreement with Hunter [1957]'s findings.

It is important to note that the analytical expressions for the radiated elastic energy  $W_{el}$ in Table 1 are only controlled by the impact force  $F_z$  and by the rheological parameters of the impactor and the substrate in the vicinity of the impact but do not depend on wave dispersion and viscous dissipation during wave propagation within the substrate.

# 308 2.2.2. Characteristic Frequencies

The frequency content of the seismic signal emitted by an impact can give information on the impact duration. To describe the amplitude spectrum  $|\tilde{A}_z(r, f)|$  of the acceleration vibration, we can either measure:

1. A mean frequency  $f_{mean}$  that is less sensitive to the signal to noise ratio than the frequency for which the amplitude spectrum is maximum [*Vinningland et al.*, 2007a, b]:

314 
$$f_{mean} = \frac{\int_0^{+\infty} |\tilde{A}_z(r, f)| f \mathrm{d}f}{\int_0^{+\infty} |\tilde{A}_z(r, f)| \mathrm{d}f},$$
 (25)

315 2. The bandwidth  $\Delta f$ :

316 
$$\Delta f = 2\sqrt{\frac{\int_{0}^{+\infty} |\tilde{A}_{z}(r,f)| f^{2} \mathrm{d}f}{\int_{0}^{+\infty} |\tilde{A}_{z}(r,f)| \mathrm{d}f}} - f_{mean}^{2}}.$$
 (26)

Regardless of the complexity (fracturation, layers, ...) of the substrate where the waves emitted by the impact propagate, it is important to notice that the mean frequency  $f_{mean}$  and the bandwidth  $\Delta f$  are always inversely proportional to the duration of the

impact, which is given by the force history at the position of the impact. Here, we 320 normalize these frequencies by Hertz [1882]'s impact duration  $T_c$ . The coefficients of 321 proportionality between  $f_{mean}$ ,  $\Delta f$  and  $1/T_c$  are estimated for elastic, viscoelastic and 322 elasto-plastic impacts by computing a synthetic spectrum  $|\tilde{A}_z(r, f)|$  using equation (2) 323 with the forces represented in Figures 1b and 1c for different values of  $\alpha$  and  $P_Y/P_0$ . The 324 frequencies for an elastic impact i.e., for  $\alpha = 0$  and  $P_Y/P_0 = 1$ , are given in Table 2. Both 325 frequencies  $f_{mean}$  and  $\Delta f$  are smaller when the impact is inelastic compared to the case 326 of an elastic impact (Figure 3). They decrease by ~ 5% when  $\alpha$  increases from 0 to 0.5 327 and by ~ 25% when the stresses ratio  $P_Y/P_0$  decreases from 1 to 0.5. 328

When normalized by  $T_c$ , the characteristic frequencies are also affected by wave disper-329 sion and viscous attenuation of energy during propagation i.e. by the Green's function of 330 the structure. These propagation effects are independent of the profile of the impact force, 331 i.e. of the fact that the impact is elastic or inelastic. For the computation of the charac-332 teristic frequencies on thick blocks, we used for simplicity the far field approximation of 333 the Green's function of Rayleigh waves [equation (4)]. This approximation is correct for 334 impacts on homogeneous media such that investigated in the laboratory experiments of 335 section 4. In the field, however, the propagation medium is much more complex and other 336 modes with a different dispersion could develop. In this case, the frequencies normalized 337 by  $T_c$  shown in Table 2 could change. Active or passive seismic surveys can allow to eval-338 uate locally the Green's function of a specific site. This Green's function can then be used 339 in equations (25) and (26) to estimate how much the normalized frequencies divert from 340 that computed using the Green's function of Rayleigh waves. This is however beyond the 341 scope of the paper. In addition to dispersion, viscous attenuation of energy during prop-342

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agation can have a significant influence on the measured frequency on the field, especially 343 for high frequencies. [Gimbert et al., 2014] investigated the amplitude spectrum gener-344 ated by the turbulent flow in rivers and showed that its central frequency can decrease 345 by a factor of 10 when the distance r from the source increases from 5 m to 600 m, for 346 a quality factor Q = 20. To quantify the effect of viscous attenuation on frequencies in 347 our impact experiments, we multiply the synthetic spectrum in equations (25) and (26)348 by the factor exp  $(-\gamma(\omega)r)$ , where  $1/\gamma(\omega)$  represents the characteristic distance of energy 349 attenuation. In our experiments, the propagation media are homogeneous and we record 350 the seismic signals close to the impacts, from r = 2 cm to about r = 30 cm. In this range 351 of distances r and for the substrates investigated in section 4, we estimate that the char-352 acteristic frequencies  $f_{mean}$  decreases and  $\Delta f$  increases by less than 5% when r increases, 353 which is negligible. However, for every practical applications, it is crucial to evaluate wave 354 dispersion and viscous attenuation during propagation and correct the measured seismic 355 signal from these effects before computing its energy  $W_{el}$  and its frequencies  $f_{mean}$  and 356  $\Delta f$ . This correction is systematically performed in our experiments. 357

#### 358 2.2.3. Inverse Scaling Laws

We can invert the scaling laws derived in this section for the radiated elastic energy  $W_{el}$  and for the frequencies  $f_{mean}$  and  $\Delta f$  (Tables 1 and 2) to express the mass m and the impact speed  $V_z$  as functions of the radiated elastic energy  $W_{el}$  and a characteristic frequency  $f_c$  of the seismic signal that is either  $f_{mean}$  or  $\Delta f$ .

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363 On thin plates,  $W_{el} = a_1 C_{plate} m^{5/3} V_z^{11/5}$ ,  $f_{mean} = 0.75/T_c$  and  $\Delta f = 0.72/T_c$ , then, 364 developing the expression of  $T_c$  [equation (9)], we obtain:

365 
$$m = c_1 \left( \frac{E^{*2}}{(a_1 C_{plate})^{3/11} \rho_s^{1/3}} \right)^{11/16} \frac{W_{el}^{3/16}}{f_c^{33/16}}$$
(27)

366 and

367 
$$V_z = c_2 \left(\frac{\rho_s^{1/3}}{a_1 C_{plate} E^{*2}}\right)^{5/16} W_{el}^{5/16} f_c^{25/16}, \tag{28}$$

where  $c_1 \approx 0.046$  or 0.05 and  $c_2 \approx 10.8$  or 10.1 if  $f_c$  is  $f_{mean}$  or  $\Delta f$ , respectively. The coefficient  $a_1$  is given in Table 1.

370 On thick blocks, the inversion of the relations  $W_{el} = a_2 C_{block} m V_z^{13/5}$ ,  $f_{mean} = 1/T_c$  and 371  $\Delta f = 0.6/T_c$  gives:

372 
$$m = c_3 \left( \frac{E^{*6/5}}{(a_2 C_{block})^{3/13} \rho_s^{1/5}} \right)^{13/16} \frac{W_{el}^{3/16}}{f_c^{39/16}}$$
(29)

373 and

374 
$$V_z = c_4 \left(\frac{\rho_s^{1/5}}{a_2 C_{block} E^{*6/5}}\right)^{5/16} W_{el}^{5/16} f_c^{15/16}, \tag{30}$$

where  $c_3 \approx 4.88$  or 4.7 and  $c_4 \approx 0.018$  or 0.02 if  $f_c$  is  $f_{mean}$  or  $\Delta f$ , respectively. The value of  $a_2$  is given in Table 1.

The physical characteristics of an impact can then be theoretically deduced from the generated seismic signal. With a continuous recording the seismic signals emitted by rockfalls, such that performed in Dolomieu crater, Réunion Island [e.g. *Hibert et al.*, 2014a], the relations (27) to (30) could be very useful for risks assessment related to these events. Note that the estimation of the impact parameters m and  $V_z$  requires a prior evaluation of the elastic properties  $\rho_i$ ,  $E_i$  and  $\nu_i$  of the impactor and the ground. It should also be noticed that m and  $V_z$  strongly depend on the frequency  $f_c$ . For example

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on blocks, if the characteristic frequency is underestimated by a factor of 2, the mass m will be overestimated by a factor of  $2^{39/16} \simeq 5.4$ . It is therefore necessary to record the entire frequency spectrum to obtain a good estimation of the impact parameters. Because of temporal aliasing during signal sampling, an ideal sampling frequency should be higher than two times the highest frequency of the spectrum, that should be at least  $f_{mean} + \Delta f/2$ . According to Table 2, the sampling frequency should then be at minimum  $3/T_c$ .

In section 4.3, the scaling laws presented in Tables 1 and 2 are tested with impacts experiments. Moreover, the masses m and the speeds  $V_z$  of the impactors in the experiments are retrieved from the measured seismic signals using equations (27) to (30) and they are compared with their real values.

#### 2.3. Energy Budget and Coefficient of Restitution

Another objective of this paper is to establish an energy budget of the impacts. To that way, we compare the radiated elastic energy  $W_{el}$  to the total energy lost during the impact  $\Delta E_c$ . From a practical point of view, the total energy lost by a spherical bead rebounding normally and without rotation can be easily measured from the difference of the bead kinetic energy before and after the impact:

400 
$$\Delta E_c = \frac{1}{2}mV_z^2(1-e^2), \qquad (31)$$

where e is the normal coefficient of restitution, that is the ratio of the bead vertical speeds after and before the impact, respectively V' and  $V_z$  [e.g. *Tillett*, 1954; *Hunter*, 1957; *Reed*, 1985; *Falcon et al.*, 1998; *McLaskey and Glaser*, 2010].

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 $\Delta E_c$  is the sum of the energy radiated in elastic waves  $(W_{el})$ , lost in viscoelastic dissipation in the vicinity of the contact  $(W_{visc})$  and dissipated by all other processes  $(W_{other})$ . These other losses can be due to plastic deformation [*Davies*, 1949], surface forces between the sphere and the surface, as e.g. electrostatic forces [*Israelachvili*, 2002], or in general grain scale interactions [*Duran*, 2010; *Andreotti et al.*, 2013]:

$$\Delta E_c = W_{el} + W_{visc} + W_{other}.$$
(32)

In our impacts experiments, the radiated elastic energy  $W_{el}$  is deduced from a measurement of the generated seismic signal. Here we present an analytical expression for the energy  $W_{visc}$  that will be used later to estimate the losses related to viscoelastic dissipation.

#### 414 2.3.1. Energy Lost by Viscoelastic Dissipation

The energy  $W_{visc}$  lost by viscoelastic dissipation in the vicinity of the impact results from the work done by the viscoelastic force  $F_{diss} = -\frac{3}{2}DK\frac{d\delta_z(t)}{dt}\delta_z^{1/2}(t)$  during the impact:

417 
$$W_{visc} = \int_0^{+\infty} F_{diss}(t) \cdot \frac{\mathrm{d}\delta_z(t)}{\mathrm{d}t} \mathrm{d}t.$$
(33)

418 Using the dimensionless variables  $\delta^* = \delta_z/\delta_{z0}$  and  $t^* = V_z t/\delta_{z0}$  and the viscoelastic pa-419 rameter  $\alpha = \frac{3}{2}DV_z/\delta_{z0}$ , we can show that:

$$W_{visc} = C_{visc} m V_z^2, \tag{34}$$

421 where  $C_{visc} = \int_0^{+\infty} \left(\frac{\mathrm{d}\delta^*}{\mathrm{d}t^*}\right)^2 \delta^{*1/2} \mathrm{d}t^*$  is a function of  $\alpha$  only (Figure 2c). For an elastic 422 impact, no work is done by the viscoelastic force because  $C_{visc} = 0$ . The expression of 423  $W_{visc}$  is independent of the fact that the impact is on a plate or on a block because it 424 concerns the energy dissipated in the impact region.

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The proportion of total energy  $E_c$  dissipated by viscoelasticity can be developed in powers of the mass m and the impact speed  $V_z$  using the third order Taylor series  $C_{visc} \approx$  $1.24\alpha - 1.51\alpha^2 + 0.86\alpha^3$  and the expression of  $\alpha$  in equation (19):

428 
$$\frac{W_{visc}}{E_c} = 2C_{visc} \approx 3.47x - 5.92x^2 + 4.72x^3 + O(x^3), \tag{35}$$

429 where  $x = DE^{*2/5}\rho_s^{-1/15}m^{-1/3}V_z^{1/5}$ , which is in agreement with the viscoelastic impact 430 models of *Kuwabara and Kono* [1987] and *Ramírez et al.* [1999].

# 431 2.3.2. Total Energy Lost

Finally, if we assume that the sole energy dissipation processes are elastic waves radiation and viscoelastic dissipation and that other energy dissipation processes (e.g. plastic deformation) are negligible, the proportion of the lost energy  $\Delta E_c$  radiated in elastic waves is, on plates:

436 
$$\frac{W_{el}}{\Delta E_c} = \frac{a_1 C_{plate} m^{2/3} V_z^{1/5}}{a_1 C_{plate} m^{2/3} V_z^{1/5} + C_{visc}},$$
(36)

437 and the proportion of the lost energy  $\Delta E_c$  dissipated in viscoelasticity is:

438 
$$\frac{W_{visc}}{\Delta E_c} = \frac{C_{visc}}{a_1 C_{plate} m^{2/3} V_z^{1/5} + C_{visc}}.$$
 (37)

439 In these expressions, at first order  $C_{visc} \propto m^{-1/3}$  [equation (35)]. Therefore, when the 440 mass m of the impactor increases, the proportion of the lost energy  $\Delta E_c$  radiated in 441 elastic waves should tends towards 100% and that lost by viscoelastic dissipation should 442 tends toward 0%. The transition from a viscoelastic impact (for small masses) towards an 443 elastic impact (for large masses) occurs when  $a_1 C_{plate} m^{2/3} V_z^{1/5} = C_{visc}$ , i.e. for a critical 444 mass  $m_c \approx 8D \sqrt{B\rho_p h}$ .

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445 On blocks, we get:

446

448

$$\frac{W_{el}}{\Delta E_c} = \frac{a_2 C_{block} V_z^{3/5}}{a_2 C_{block} V_z^{3/5} + C_{visc}},$$
(38)

447 and

$$\frac{W_{visc}}{\Delta E_c} = \frac{C_{visc}}{a_2 C_{block} V_z^{3/5} + C_{visc}}.$$
(39)

For large masses m, the ratio  $W_{el}/\Delta E_c$  becomes independent of m and tends towards 100% because  $C_{visc}$  is negligible. When m decreases, the ratio  $W_{el}/\Delta E_c$  decreases and the ratio  $W_{visc}/\Delta E_c$  increases.

This model is somewhat ideal because the energy dissipated by other processes such as plastic deformation are not negligible when the impactor's mass m is large, in particular when the contact surface is rough. As a consequence, the ratio  $W_{el}/\Delta E_c$  practically never reaches 100% when m increases (see section 4.4.2).

The validity of theoretical scaling laws established in this section for the radiated elastic energy, the frequencies and the lost energy is tested in section 4 with simple impact experiments. Prior to this, the experimental setup is presented in the next section.

#### 3. Experimental Setup

We conduct laboratory experiments of beads and gravels impacts on horizontal hard substrates. The generated seismic vibration is recorded on the surface by mono-component piezoelectric charge shock accelerometers (type 8309, *Brüel & Kjaer*). The response of the sensors is flat between 1 Hz and 54 kHz. The impactor is initially held by a screw and dropped without initial velocity and rotation to ensure reproducibility (Figure 4a). The height of fall *H* varies between 2 cm and 40 cm. The impact speed  $V_z$  is calculated assuming a fall without air friction:  $V_z = \sqrt{2gH}$ , with *g* the gravitational acceleration.

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We drop spherical beads of steel, glass and polyamide (Figure 4b) of diameter *d* ranging from 1 mm to 20 mm to observe the influence of the mass and of the elastic parameters on the results. We conduct the same experiments with granite gravels of irregular shapes and of similar size and mass than the beads to test if the analytical scaling laws established for spheres impacts are still valid if the impactor is not spherical. The properties of the impactors used in the experiments are shown in Table 3.

Four target substrates are used: (i) a smooth PMMA plate of dimensions  $120 \times 100 \times 1$ 472 cm<sup>3</sup>, (ii) a circular 1 cm-thick smooth glass plate of radius 40 cm, (iii) a rough marble block 473 of dimensions  $20 \times 20 \times 15$  cm<sup>3</sup> and (iv) a rough concrete pillar of dimensions  $3 \times 1.5 \times 0.6$ 474 m<sup>3</sup>. The seismic vibration is recorded at different distances from the impacts to measure 475 waves group speed  $v_g = \partial \omega / \partial k$  and phase speed  $v_\phi = \omega / k$  of the direct wave front in these 476 substrates. These characteristics and the elastic parameters of the investigated structures 477 are summarized in Table 4. Note that we assume that the rheological properties  $E_p$ ,  $\nu_p$ 478 and  $\rho_p$  of the substrates at the position of the impact are the same than that within 479 the substrates, where the waves propagate. This hypothesis is valid for the homogeneous 480 solids investigated here but it may not be correct in the fractured and layered media 481 encountered in the field, whose elastic properties vary with depth. In any cases, it is 482 necessary to determine these properties in order to quantify the radiated elastic energy 483  $W_{el}$  and to deduce thereafter the impact parameters m and  $V_z$  from the seismic signal. 484

# 4. Experimental Results

# 4.1. Methods to Estimate the Radiated Elastic Energy

Let us first describe the signals recorded in our experiments of bead impacts on the different substrates and how we compute the radiated elastic energy  $W_{el}$  in each case. 487 A bouncing bead generates a series of short and impulsive acoustic signals (Figures 5a, 488 5b, 6a and 6b). The bead can rebound more than 50 times on the smooth glass plate 489 while it rebounds only 2 or 3 times on the concrete block owing to surface roughness 490 (Figures 5b and 6a). We estimate the coefficient of normal restitution  $e = \sqrt{H'/H}$  from 491 the time of flight  $\Delta t$  between the successive rebounds because the rebound height is given 492 by  $H' = g\Delta t^2/8$  [Falcon et al., 1998; Farin, 2015]. The total energy lost during an impact 493 is then given by  $1 - e^2$  [see equation (31)].

The PMMA and glass plates and the concrete block are sufficiently large to measure most of the first wave arrival before the return of the first reflections off the lateral sides (Figures 5c, 5f and 6e). In these cases, we estimate the radiated elastic energy  $W_{el}$  from the energy flux crossing a surface surrounding the impact, as detailed in *Farin et al.* [2015] i.e., for plates:

499 
$$W_{el} = 2rh\rho_p \int_0^{+\infty} v_g(\omega) |\tilde{V}_z(r,\omega)|^2 \exp\left(\gamma(\omega)r\right) d\omega, \tag{40}$$

500 and for blocks:

501 
$$W_{el} = 2\rho_p r v_g c_P \pi_R^{surf}(r) \frac{\beta (f_0'(x_0))^2}{2\pi \xi^4 (x_0^2 - 1)} \int_0^{+\infty} |\tilde{V}_z(r, \omega)|^2 \omega^{-1} \exp\left(\gamma(\omega)r\right) d\omega.$$
(41)

In these expressions,  $v_g$  is the group speed,  $|\tilde{V}_z(r,\omega)|$  is the time Fourier transform of the vertical vibration speed at the surface and  $\pi_R^{surf}(r)$  is the percentage of Rayleigh waves in the signal at the surface at distance r from the impact [Farin et al., 2015]. The factor exp  $(\gamma(\omega)r)$  compensates viscoelastic dissipation with distance. The characteristic distance of energy attenuation  $1/\gamma(\omega)$  is estimated experimentally for every substrates (Table 4) [see Farin et al., 2015, for details]. The coefficient  $\beta$  depends only on the Poisson's ratio  $\nu_p$  (see Figure 17 in Appendix A).

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Because the substrates size is limited, wave reflections off the boundaries are recorded by 509 the sensors. Side reflections are strongly attenuated in PMMA which is a more damping 510 material than glass, concrete and marble (Figure 5c). On contrary, the wave is reflected 511 many times in the glass plate and in the two blocks and its averaged amplitude decreases 512 exponentially with time owing to viscous dissipation during wave propagation (Figures 5d, 513 6c and 6d). An adjustment of an exponential curve on the squared signal, filtered below 514 2000 Hz, allows us to quantify the characteristic decay time of energy  $\tau$  in the substrate 515 (Table 4) [see Appendix B of *Farin et al.*, 2015, for details on the experimental procedure]. 516 This situation is referred to as a diffuse field in the literature [e.g. Weaver, 1985; Mayeda 517 and Malagnini, 2010; Sánchez-Sesma et al., 2011]. In this case, we can estimate the 518 radiated elastic energy  $W_{el}$  from the reflected coda. Indeed, in diffuse field approximation, 519 the squared normal vibration speed averaged over several periods decreases exponentially: 520

521 
$$\overline{v_z(t)^2} = \overline{v_z(t=0)^2} \exp\left(-\frac{t}{\tau}\right),\tag{42}$$

where t = 0 is the instant of the impact. Knowing the characteristic time  $\tau$ , we extrapolate the vibration speed at the instant t = 0 and deduce the radiated elastic energy  $W_{el}$  from [*Farin et al.*, 2015]:

525 
$$W_{el} \approx \left(1 + \left(\frac{\mathcal{H}}{\mathcal{V}}\right)_{\text{diffuse}}^2\right) \rho_p V \overline{v_z(t=0)^2},\tag{43}$$

where V is the block volume and  $\left(\frac{\mathcal{H}}{\mathcal{V}}\right)_{\text{diffuse}}$  is the ratio of horizontal to vertical amplitude at the surface of the structure in diffuse field approximation. On thin plates,  $\left(\frac{\mathcal{H}}{\mathcal{V}}\right)_{\text{diffuse}} \simeq 0$ . On a thick block of Poisson's ratio  $\nu_p$ , Sánchez-Sesma et al. [2011] give  $\left(\frac{\mathcal{H}}{\mathcal{V}}\right)_{\text{diffuse}} \approx 1.245 +$ 0.348 $\nu_p$ . Due to statistical assumptions, the diffuse method leads to larger uncertainties on the results compared to that based on the energy flux [Farin et al., 2015]. However,

it is the only method that can be applied when the first arrival can not be distinguishedfrom its side reflections, as for example in the marble block (Figure 6f).

#### 4.2. Comparison with Synthetic Signals

We compare the measured vibration acceleration  $a_z(r,t)$  with a synthetic signal which is the time convolution of *Hertz* [1882]'s force of elastic impact (Figure 1b with  $\alpha = 0$ ) with the Green's function [equations (3) and (4)] (Figures 5e to 5h and 6e to 6h).

A good agreement is observed in terms of amplitude and frequencies on the PMMA 536 plate but the agreement is less satisfactory on the other substrates. On glass, only the 537 beginning of the signal is well reproduced by the theory (Figure 5f). A resonance of 538 the accelerometer coupled to the glass plate for 38 kHz could explain why the recorded 539 vibration lasts longer than the synthetic one (Figure 5f). This effect clearly appears on the 540 Fourier transform of the signal with a peak of energy around 38 kHz (Figure 5h). Using a 541 laser Doppler vibrometer that measures the exact surface vibration speed but with a much 542 lower sensitivity than the accelerometers, we determined that the resonance overestimates 543 the vibration energy by a factor of 4. To compensate this effect, we divide the measured 544 radiated elastic energy  $W_{el}$  by this factor. On concrete, the synthetic is significantly 545 different than the recorded signal in terms of higher amplitude and frequencies (Figures 546 6f and 6h). The impact may be not completely normal to the surface owing to the surface 547 roughness, and this could reduce the energy on the normal component, as discussed later 548 in section 5. On marble, the frequencies of the measured signal are close to that of the 549 synthetic one but the amplitude is higher than in theory, probably because side reflections 550 arrive before the end of the first arrival (Figures 6e and 6g). This has no consequence on 551 the estimation of the radiated elastic energy  $W_{el}$  for this block because we use the diffuse 552

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method [equation (43)]. Note that the peaks of energy for f > 50 kHz in the synthetic spectrum on the concrete and marble block are not visible in the recordings, because the accelerometers are not sensitive in this frequency range (see Appendix B).

# 4.3. Experimental Test of the Analytical Scaling Laws

# 556 4.3.1. Radiated Elastic Energy

Regardless of the bead material, the measured radiated elastic energy  $W_{el}$  on the PMMA and glass plates matches well with the theoretical energy  $W_{el}^{th}$  predicted in equation (23) for an elastic impact, with  $C_{plate} = 1.21$  (Figure 7). For the smallest and the largest beads investigated, however, the data points separate from the theoretical line and the discrepancy can reach a factor of 5. This is clearer for steel beads (Figures 7c and 7g) and for glass beads on the glass plate (Figure 7e).

563 On blocks, the theory predicts that  $W_{el}^{th} \propto m V_z^{13/5}$  (equation (24) and Table 1). The 564 experimental data of beads impacts on the concrete and marble blocks follow qualitatively 565 this law (Figure 8). In most of the experiments, however, the measured energy  $W_{el}$  is lower 566 than in theory. Moreover, on concrete, the measured radiated elastic energy  $W_{el}$  separates 567 from the theoretical trend for the smallest and the largest beads investigated (Figures 8a, 568 8b and 8c). The discrepancy with the theory on Figures 7 and 8 is interpreted in the 569 discussion.

Surprisingly, the elastic energy  $W_{el}$  radiated by the impacts of granite gravels follows well the scaling law in  $m^{5/3}V_z^{11/5}$  on plates (Figures 7d and 7h) and in  $mV_z^{13/5}$  on blocks (Figures 8d and 8h). The measured energy  $W_{el}$  is however smaller than in theory, by a factor of 2 on plates and up to 10 times smaller on blocks. The experiments with gravels show that Hertz's analytical model of elastic impact, established for spheres, can also

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575 describe at first order the impact dynamics of impactors with a complex shape. As a 576 consequence, we expect that it may also be applied for natural rockfalls.

# 577 4.3.2. Characteristics Frequencies

We compute the mean frequency  $f_{mean}$  and the bandwidth  $\Delta f$  using equations (25) and 578 (26), respectively (Figure 9). Note that the seismic signals generated by bead impacts in 579 our experiments contain much higher frequencies (1 Hz - 100 kHz) than those recorded 580 for natural rockfalls (1 Hz - 50 Hz) [e.g. Deparis et al., 2008; Hibert et al., 2011]. This is 581 because the bead diameters are in average smaller than the diameter of natural boulders, 582 that could be from a few millimeters to a few meters large. In addition, the sampling 583 frequency is much higher and high frequencies are much less attenuated in our experiments 584 than on the field. 585

On the glass plate, as the accelerometers are not sensitive to frequencies larger than 586 50 kHz, the frequencies computed with these sensors saturate to about 40 kHz for the 587 smallest beads i.e., the smallest impact durations  $T_c$  (black crosses on Figures 9c and 588 9d). Therefore, the accelerometers type 8309 are used only for the impacts that generate 589 energy below 50 kHz. For the signals of higher frequencies, we use in parallel piezoelectric 590 ceramics (MICRO-80, Physical Acoustics Corporation) sensitive between 100 kHz to 1 591 MHz. These last sensors can however not be used to quantify the radiated elastic energy 592  $W_{el}$  since they are not very sensitive to frequencies lower than 100 kHz. 593

Regardless of the bead material, the frequencies of the signals generated by impacts on PMMA, glass and marble collapse well within  $\pm 20\%$  with the theoretical scaling laws of Table 2 as a function of the duration of impact  $T_c$  (Figures 9a to 9d, 9g and 9h). The agreement is better for the frequency bandwidth  $\Delta f$  than for the mean frequency

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598  $f_{mean}$ . The agreement is also very satisfactory for the granite gravels of complex shape, 599 even though the theoretical values of the frequencies were computed using Hertz's impact 600 model for a sphere (see section 2.2.2).

In concrete, the wavelength  $c_R/f \approx 1$  cm for frequencies around 40 kHz, which is of the order of the size of the heterogeneities. High frequencies f > 40 kHz are therefore strongly attenuated during wave propagation in this block. This could explain the discrepancy with the theory for these frequencies on Figure 9e.

#### 4.3.3. Estimating Impact Properties from the Seismic Signal

We use equations (27) to (30) with the coefficients for an elastic impact  $C_{plate} = 1.21$ 606 and  $C_{block} = 0.02$  to retrieve the mass m and the impact speed  $V_z$  of the impactors in 607 our experiments. The agreement with the real values is correct, within a factor of 2 for 608 the mass m (Figure 10a) and within a factor of 3 for the impact speed  $V_z$  (Figure 10b), 609 both on smooth thin plates and rough thick blocks. For impacts of rough gravels on the 610 two plates, the predicted values are still close to the real ones, with a factor of 1.5, even 611 when inelastic dissipation occurs. The underestimation of m and  $V_z$  in certain cases is 612 consistent with the aforementioned discrepancy of the radiated energy  $W_{el}$  with theory 613 (Figures 7 and 8). 614

It is therefore possible to have an estimation of the mass m and the impact speed  $V_z$  of an impactor on a plate and on a block from the characteristics of the generated seismic signal, with less than an order of magnitude from the real values, using only *Hertz* [1882]'s analytical model of elastic impact. This method only requires to know the elastic parameters of the involved materials.

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# 4.4. Energy Budget of the Impacts

Inelastic losses during an impact can reduce the energy radiated in the form of elastic waves  $W_{el}$  compared to that predicted by *Hertz* [1882]'s model (see section 2.2.1). This may explain part of the discrepancy observed between the measured radiated elastic energy  $W_{el}$  and its theoretical value  $W_{el}^{th}$  on Figures 7 and 8, and consequently between the values of the masses m and speeds  $V_z$  inverted from seismic signals and their real values on Figure 10. In order to interpret these discrepancies, we establish in this section an energy budget of the impacts.

For that purpose, we compare on Figures 11 and 13 the measured radiated elastic energy  $W_{el}$  (empty symbols) with the total energy lost during the impact  $\Delta E_c$ , estimated with the coefficient of restitution e (full symbols). The difference  $\Delta E_c - W_{el}$  is likely lost in inelastic processes, such as viscoelastic dissipation or plastic deformation. This allows us to establish an energy budget of the impacts (Figures 12 and 14).

Furthermore, we also compare the measured radiated energy  $W_{el}$  with the theoretical one – noted  $W_{el}^{th}$ , red line on Figures 11 and 13 –, predicted by the scaling law in Table 1 for an elastic impact, with  $C_{plate} = 1.21$  and  $C_{block} = 0.02$ , respectively. Note that on plates, we take into account the dependence of  $C_{plate}$  coefficient to  $\lambda_Z$  parameter for large beads (see section 2.1.1.2 and Figure 2a). The corrected theoretical elastic energy on plates is noted  $W_{el}^{th'}$  on Figure 11. The discrepancy with theory is discussed in section 5.1.

# 639 4.4.1. Energy Budget on Smooth Thin Plates

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640 On smooth thin plates, the energy  $\Delta E_c$  lost by the bead during an impact is mostly 641 radiated in elastic waves  $(W_{el})$  or dissipated by viscoelasticity during the impact  $(W_{visc})$ 642 (Figures 11 and 12).

More energy is radiated in elastic waves as the bead mass m and the ratio of the bead 643 diameter d on the plate thickness h increase, regardless of the elastic parameters (empty 644 symbols on Figures 11 and 12). For the smallest beads investigated, only 0.1% to 0.3%645 of the impact energy  $E_c$  is radiated in elastic waves. In contrast, the impact energy  $E_c$ 646 can be almost entirely converted into elastic waves when the bead diameter d is greater 647 than the plate thickness h (Figure 11c). For large beads, the measured ratio of  $W_{el}/E_c$ 648 is close to the theoretical ratio  $W_{el}^{th'}/E_c$  (full red line on Figure 11), but diverges as the 649 bead diameter d decreases. 650

We adjust the viscoelastic parameter D in equation (35) to match the theoretical expression of the lost energy ratio  $\Delta E_c/E_c = W_{el}^{th'}/E_c + W_{visc}/E_c$  (thick green line on Figure 11) with the variation of  $1 - e^2$  (full symbols). The agreement is found to be the best for values of D ranging from 35 ns to 580 ns (Table 5).

The adjustment of D with experimental data allows us to quantify the viscoelastic 655 energy  $W_{visc}$  (blue line on Figure 11). More energy is lost by viscoelastic dissipation 656 as the bead mass m and the ratio d/h decrease and this is almost the sole process of 657 energy loss when the bead diameter d is smaller than 0.2h (Figure 12). The transition 658 from a viscoelastic impact towards an elastic impact is observed for the critical mass 659  $m_c \approx 8D\sqrt{B\rho_p h}$ , as predicted in section 2.3.2 (at the crossing between the red and blue 660 lines on Figure 11). Interestingly, a bouncing bead loses less of its initial energy  $E_c$  for 661 masses m close to the critical mass  $m_c$ . 662

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For the largest beads of glass and steel, some energy is likely lost in plastic deformation of the softer material involved (Figure 12). As a matter of fact, we observed small indentations on the surface of the plates after the impacts of these beads but not for polyamide beads.

Note that the energy budget is very different for impacts of rough gravels on the same plates. Indeed, the ratio  $W_{el}/E_c$  is  $3.3\% \pm 1.8\%$  regardless of the gravel mass m. Moreover, about  $33\% \pm 17\%$  of the initial energy is lost in translational energy of rebound and  $13\% \pm 11\%$  is converted into rotational energy of the gravel. As a matter of fact, half of the gravel's initial energy is in average lost in plastic deformation. (see Appendix C for more details).

## 673 4.4.2. Energy Budget on Rough Thick Blocks

On the rough thick blocks, the energy budget is very different than on the smooth plates (Figures 13 and 14). Indeed, a much smaller proportion of energy seem to be lost in elastic waves and in viscoelastic dissipation. The rest is likely dissipated by other processes such as plastic deformation, adhesion or rotational modes of the bead owing to surface roughness.

The measured radiated elastic energy  $W_{el}$  represents only from 0.01% to 2% of the impact energy  $E_c$ , regardless of the bead mass m (empty symbols on Figure 13). Theory predicts that the ratio  $W_{el}^{th}/E_c$  is independent of the mass m (red line). However, the measured ratio  $W_{el}/E_c$  slightly increases with bead mass m on concrete and decreases on marble for different reasons explained in the discussion.

684 Contrary to plates, it is difficult here to determine what proportion of the lost en-685 ergy  $\Delta E_c$  is dissipated by viscoelasticity and what proportion is lost in other processes.

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However, one remarks that  $1 - e^2$  increases when the mass m decreases (full symbols 686 on Figure 13). This variation may be due to viscoelastic dissipation which is stronger 687 when the bead mass m decreases [equation (35)]. We make the strong assumption that 688 the percentage of energy lost in other processes  $W_{other}/E_c$  is constant and independent 689 of the bead mass m. We then adjust the viscoelastic coefficient D (Table 5) to fit 690  $\Delta E_c/E_c = W_{el}^{th}/E_c + W_{visc}/E_c + W_{other}/E_c$  (thick green line on Figure 13) with the vari-691 ation of  $1 - e^2$  (full symbols). This allows to quantify the energy  $W_{visc}$  lost in viscoelastic 692 dissipation (blue line). 693

In the case where no other energy losses than elastic waves radiation or viscoelastic 694 dissipation occur, we predicted that the ratios  $W_{el}/\Delta E_c$  and  $W_{visc}/\Delta E_c$  should increase 695 and tend towards 100% when the mass m increases and decreases, respectively [equations 696 (38) and (39)]. Here, elastic waves radiation and viscoelastic dissipation follow the same 697 dependence on the mass than that predicted but represent respectively from 0.03% to 698 5% and from 2% to 40 % of the lost energy  $\Delta E_c$  only (Figure 14). For impacts on rough 699 substates as the two blocks investigated here, but also on the field, it is therefore important 700 to take into account the energy  $W_{other}$  lost in other processes. In our experiments, this 701 energy seems to be an increasing percentage of the lost energy  $\Delta E_c$ , from 50% to more 702 than 99%, as the bead mass m increases (Figure 14). 703

# 704 4.4.3. Evaluation of the Energy Budget for Natural Rockfalls

The energy budget of impacts on rough blocks in our laboratory experiments can be used to extrapolate that of natural rockfalls. On the field, the impactors masses varies from a few grams to a few tons and drop heights varies from a few centimeters to several tens of meters. Owing to strong energy dissipation in such complex media, only impacts of

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large masses can be detected by seismic methods. Viscoelastic dissipation should therefore 709 be negligible in most situations encountered on the field. For example, we can estimate 710 the energy lost in viscoelastic dissipation for a granite gravel of m = 100 g impacting the 711 ground with impact speed  $V_z = 10 \text{ m s}^{-1}$  using equation (35) with the coefficient D = 80 ns712 of glass, which has similar properties than granite, and a typical Young's modulus  $E_p = 10$ 713 MPa for the ground [Geotechdata.info, 2013]. It results that the viscoelastic energy  $W_{visc}$ 714 represents only 0.04% of the impact energy  $E_c$ , which is negligible. Moreover, it should 715 be even smaller for larger masses m. The energy  $W_{plast}$  dissipated in plastic deformation 716 of the ground or of the impactor is expected to be much more significant on the field 717 than in our laboratory experiments and even more so when the mass m increases because 718 large stresses are applied on damaged materials with a low yield stress. For such impacts 719 with a rough contact, the energy  $W_{plast}$ , in addition to other energy lost in rotation and 720 translational modes of the impactor, should then represent almost all of the lost energy 721  $\Delta E_c$  (see Appendix C). Consequently, the ratio of the radiated elastic energy over the lost 722 energy  $W_{el}/\Delta E_c$  may not exceed a few percents. For example, for impacts of beads on 723 the rough concrete block, for which plastic deformation is significant, the ratio  $W_{el}/\Delta E_c$ 724 seems to saturate to  $2\% \pm 1\%$  for  $m \simeq 1$  g and then decreases (Figure 14a). 725

#### 5. Discussion

## 5.1. Discrepancy from Hertz's Model

The characteristic frequencies of the signal generated by an impact do not significantly deviate from *Hertz* [1882]'s prediction when the impact is inelastic (Figure 9). On the contrary, in some experiments, the measured radiated elastic energy  $W_{el}$  diverges from that (noted  $W_{el}^{th}$ ) given by the scaling laws in Table 1 (Figures 7 and 8). As a consequence,

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the masses m and speeds  $V_z$  retrieved from the measured signal in our experiments using the elastic model deviate from their real values (Figure 10). Let us discuss here the observed discrepancy.

## 733 5.1.1. Small Bead Diameters

On smooth thin plates, for small bead diameters, viscoelastic dissipation is the major energy loss process (Figure 12). For a steel bead of diameter 1 mm impacting the glass plate, using equation (19) with D = 35 ns (see Table 5), the coefficient  $C_{plate}$  is found to be equal to 1.15 instead of 1.21 for an elastic impact (see Figure 2a). Thus, the viscoelastic impact theory predicts that the radiated elastic energy  $W_{el}^{th}$  should be only of 5% smaller than for an elastic impact, which is negligible compared with the observed difference of 73% (Figure 7g).

The major source of discrepancy is probably due to the fact that our sensors are band 741 limited up to 50 kHz. Indeed, for the 1-mm bead, 50% of the radiated energy is in theory 742 higher than 50 kHz (see Appendix B). The remaining 23% may be lost in adhesion of the 743 bead on the plate during the impact. In addition, some energy may be lost in electro-744 staticity or capillarity, which are greater for the smallest beads [Andreotti et al., 2013]. 745 The discrepancy is totally explained by the limited bandwidth of the accelerometers for 746 a steel bead of diameter d = 2 mm on the glass plate: about 30% of the energy is over 747 50 kHz and the measured energy  $W_{el}$  is 35% smaller than  $W_{el}^{th}$  (Figure 7g). Similarly, on 748 concrete, for a steel bead of diameter d = 2 mm, the theory predicts that only 17% of 749 the radiated elastic energy is below 50 kHz. As a consequence, the measured energy  $W_{el}$ 750 represents only 17% of the theoretical energy  $W_{el}^{th}$  (Figure 8c). For greater bead diameters, 751 both measured and theoretical energies are contained below 50 kHz and the agreement 752

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with elastic theory is better (Figures 7 and 8). In contrast, on marble the radiated elastic energy is closer to the theory for the smallest beads (Figures 13d to 13f). For small bead diameters, less wave reflections occur within the block and the measured energy may therefore be overestimated because the diffuse field is not completely set [*Farin et al.*, 2015].

This emphasize the importance for future applications to use seismic sensors sensitive in the widest frequency range as possible. In cases where we can not measure the highest frequencies of the seismic vibration generated by an impact, note that it is possible to retrieve the momentum  $mV_z$  of the impactor from the low frequency content of measured amplitude spectrum (see Appendix D).

## 763 5.1.2. Large Bead Diameters

On smooth thin plates, the divergence of the measured radiated elastic energy  $W_{el}$  from the theoretical one  $W_{el}^{th}$  for large bead diameters is partly compensated when we take into account the decrease of the coefficient  $C_{plate}$  when the parameter  $\lambda_Z$  increases (Figures 2a and 11). However, in some experiments,  $W_{el}$  is still smaller than the theory when the bead diameter d is larger than the plate thickness h (Figures 11c, 11d and 11f). This difference may be due to plastic deformation which is more likely to occur for the largest beads investigated.

## 771 5.1.3. Impacts with a Rough Contact

Two complementary effects can explain the discrepancy of the measured radiated elastic energy with theory for impacts of spherical beads on the two rough blocks and for impacts of gravels (Figures 7d, 7h and 8).

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First, plastic deformation is a likely cause for measuring a smaller radiated elastic energy 775 than in theory on the blocks. If  $P_Y/P_0 = 0.6$  in the elasto-plastic model, the radiated 776 elastic energy predicted in Table 1 is two times smaller than for an elastic impact because 777 the coefficient  $C_{block} \approx 0.01$  instead of 0.02 (Figure 2b). This factor of 2 corresponds to 778 that observed between the measured energy  $W_{el}$  and the theoretical one  $W_{el}^{th}$  for impacts of 779 glass and steel beads on the concrete block (Figures 8a and 8c). Measuring the discrepancy 780 of the radiated elastic energy from elastic theory could then be a mean to estimate the 781 dynamic yield strength  $P_Y$  of a material. For example, for a steel bead of diameter d = 5782 mm dropped from height H = 10 cm on concrete, the maximum stress is  $P_0 \approx 300$  MPa 783 and, if  $P_Y/P_0 = 0.6$ , the dynamic yield strength would be  $P_Y \approx 180$  MPa, which is greater 784 than the typical values of  $P_Y$  for concrete [20-40 MPa, The Engineering Toolbox, 2014] 785 but of the same order of magnitude. 786

An additional process can accommodate the discrepancy. If a spherical bead impacts a 787 rough surface or as a gravel impacts a flat surface, the equivalent radius of contact may 788 be smaller than the radius of the impactor (Figure 15). Table 1 shows that the radiated 789 elastic energy  $W_{el}$  increases with the impactor radius R as  $R^5$  on plates and as  $R^3$  on 790 blocks. Then, if the radius of contact R is only 1.15 smaller on plates, the theoretical 791 radiated elastic energy  $W_{el}$  is two times smaller, and this explain the discrepancy observed 792 for gravels on the plates (Figures 7d and 7h). On blocks, if the effective radius of contact R793 is 2.1 times smaller, the radiated elastic energy  $W_{el}$  is 10 times smaller, that could explain 794 the small energy values measured on the marble block (Figures 8e to 8h). The radius of 795 contact R should be even smaller when gravels impacts the rough blocks and the radiated 796 elastic energy  $W_{el}$  is then smaller (Figures 8d and 8h). By comparison, the characteristic 797

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frequencies  $f_{mean}$  and  $\Delta f$  are inversely proportional to the radius R (because  $T_c \propto R$ ) and are therefore less affected by a change in this radius than the radiated elastic energy  $W_{el}$ . This is visible on Figure 9 because the frequencies of the signal emitted by gravels are close to that of spherical beads.

As the effective radius of contact decreases for a given mass m, the stresses are con-802 centrated on a smaller area during the impact and plastic deformation is more likely to 803 occur (see Appendix C). Interestingly, even though the energy lost in plastic deformation 804 is very important for impacts of gravels and on the rough blocks, the measured radiated 805 elastic energy  $W_{el}$  and frequencies  $f_{mean}$  and  $\Delta f$  still follow well the scaling laws in mass 806 m and impact speed  $V_z$  predicted using Hertz's model of impact of a sphere on a plane 807 (Figures 7, 8 and 9). Therefore, we expect that Hertz's model should be still valid at 808 first order on the field and, consequently, that the radiated elastic energy  $W_{el}$  should be 809 proportional to  $mV_z^{13/5}$  and that the characteristic frequencies  $f_{mean}$  and  $\Delta f$  should be 810 proportional to  $1/T_c \propto m^{-1/3} V_z^{1/5}$ . The problem is however to determine the coefficients 811 of proportionality in these relations because they depend on the rheological parameters 812 of the impactor and the ground (Table 1), on the fact that is impact is elastic or inelastic 813 (Figures 2 and 3) and on the roughness of contact, which are each extremely difficult to 814 estimate practically. A solution may be to calibrate the coefficients of proportionality of 815 816 these relations on a given site by dropping some boulders of known mass m and estimating their impact speed  $V_z$ . Once calibrated, these laws can be inverted as in section 2.2.3 817 and used to retrieve the masses m and impact speeds  $V_z$  of other rockfalls on the same 818 site from the generated seismic signals. The advantage of this method is that it is not 819 necessary to know the elastic parameters of the ground. Even so, energy attenuation as a 820

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function of frequency during wave propagation within the substrate need to be evaluatedin order to correct the measured signals.

#### 5.2. Errors on the Estimation of the Masses and Impact Speeds

Here we comment the errors on our estimation of the impactors masses from measured 823 seismic signals in Figure 10. These errors are greater than that of *Buttle et al.* [1991] 824 who managed to size sub-millimetric particles in a stream with a standard deviation less 825 than 10%. However, their estimations were based on the impact force and duration on 826 the direct compressive wave, measured at the opposite of the impact on the target block. 827 Practically, this method is difficult to apply on the field because seismic stations are at 828 the surface. Furthermore, the force and duration of the impact are more complicated 829 to estimate from the seismic signal than the radiated elastic energy and the frequencies 830 because it requires a deconvolution process that induce additional errors [e.g., McLaskey 831 and Glaser, 2010]. Our method has the advantage to be not intrusive and in principle 832 exportable to field problems. 833

## 5.3. Application to Natural Rockfalls

*Dewez et al.* [2010] conducted field scale drop experiments of individual basalt boulders on a rock slope in Tahiti, French Polynesia. The main objective of this study was to estimate hazards associated with rockfalls in a volcanic context. Boulders trajectory was optically monitored using two cameras with 50 frames per seconds. A photogrammetry technique then allowed the authors to compute the position of each boulder in time with an error smaller than the boulder radius [*Dewez et al.*, 2010]. In parallel, the seismic signal generated by boulders impacts on the ground was recorded with a sampling frequency of

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100 Hz by a board band seismometer type *STS* located a few tens of meters away. Here we want to observe how the elastic energy radiated by boulder impacts scales with the boulder's mass and speed in this natural context.

## 5.3.1. Comparison of Field Measurements with Hertz's Prediction

The waves generated by the impacts propagate in a very damaged and complex medium 845 that may involve several layers of different density. In this medium, viscous attenuation 846 of energy can be very strong, especially for high frequencies. For example, waves of 847 frequency 100 Hz only propagate in the first centimeters or meters deep below the surface. 848 Knowing the attenuation as a function of frequency, and assuming some sensitivity / 849 noise level for the sensor, it is possible to correct for this attenuation for all frequencies 850 where the amplitude is above the noise level. The corrected amplitude spectrum should 851 then be equivalent to the emitted spectrum, assuming that all the frequencies have been 852 recorded. The attenuation of energy as a function of frequency can be evaluated, for 853 example, by measuring the signal emitted by a given impact at different distances, as we 854 did in our laboratory experiments [Farin et al., 2015]. Unfortunately, no estimation of 855 the attenuation has been conducted in this field study. We therefore assume a classical 856 attenuation model of energy with distance r and multiply the measured signals by the 857 factor exp  $(\gamma(f)r)$ , with  $\gamma(f) = \pi f/Qc_R$  [Aki and Richards, 1980]. We use the quality 858 factor Q = 10, which is of the order of the values obtained by *Ferrazzini and Aki* [1992] 859 in the similar context of Kilauea volcano in Hawaï. 860

We first focus on the seismic signals emitted by the impacts of a boulder of mass m = 326kg at  $r \simeq 30$  m from the seismometer (Figure 16a). The signals have a short duration  $\sim 0.8$  s and are impulsive, as the ones generated by bead impacts (e.g., Figure 6c). The

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impacts excite a frequency range from ~ 10 Hz to 40 Hz (Figure 16b). Most of the recorded seismic spectra lies between 10 Hz and 20 Hz with a peak frequency  $f_{peak} \approx 15.5$ Hz, a mean frequency  $f_{mean} \approx 18.4$  Hz and a bandwidth  $\Delta f \approx 18.3$  Hz (Figures 16b and 16c).

We compare the measured spectrum with a synthetic amplitude spectrum predicted 868 by Hertz [1882]'s theory of impact using equation (2). The Green's function used in the 869 computation depends on the excited mode. Departs et al. [2008], Dammeier et al. [2011] 870 and Lévy et al. [2015] showed that rockfall events generate principally Rayleigh surface 871 waves. Rayleigh waves develop in far field, i.e. for kr >> 1, where  $k = 2\pi f/c_R$  is the 872 wave number [Miller and Pursey, 1954; Gimbert et al., 2014; Farin et al., 2015]. In the 873 Piton de la Fournaise volcano, Reunion Island, where the ground has a similar structure 874 as in Tahiti, the phase speed  $c_R$  is 800 m s<sup>-1</sup> [*Hibert et al.*, 2011]. We use here the same 875 phase speed  $c_R$  and estimate that kr >> 1 when the frequency f is greater than about 4 876 Hz. Since the recorded seismic energy is mostly between 10 Hz to 40 Hz, we can therefore 877 reasonably use the far field Green's function of Rayleigh waves of equation (4) convolved 878 with *Hertz* [1882]'s impact force to compute the synthetic spectrum (Figure 16c). 879

The characteristics of the impactor are R = 0.35 m, m = 326 kg and  $V_z = 11$  m s<sup>-1</sup>. We assume a typical Young's modulus  $E_p = 10$  MPa for a loose soil such that observed on the slope [*Geotechdata.info*, 2013]. *Hertz* [1882]'s elastic theory then predicts that the duration of impact should be  $T_c \simeq 0.035$  s [equation (9)]. For Rayleigh surface waves, the mean frequency should therefore be  $f_{mean} = 1/T_c \simeq 28$  Hz and the bandwidth  $\Delta f = 0.6/T_c \simeq 17$  Hz, which are close to the measured values (Table 2 and Figure 16c).

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The amplitude of the synthetic spectrum is similar to that of the measured spectrum except around 15 Hz where a peak of energy is observed in the measured spectrum (Figure 16c). The peak of energy may be due to a resonance around 15 Hz of the seismometer or of the first sediment layers because it is observed on every measured spectra [*Schmandt et al.*, 2013; *Farin*, 2015]. The shape of the measured and synthetic spectrum is very different. This may be due to plastic deformation, which is very important for impacts on loose and fractured soil.

## <sup>893</sup> 5.3.2. Elastic Energy Radiated by Boulders Impacts

Despite the discrepancy between the theory and the measurement, we observe how the elastic energy  $W_{el}$  radiated by the impacts of all boulders depends on the boulder mass m and impact speed  $V_z$ . The calculation of  $W_{el}$  is based on the integration of the energy flux over a cylinder surrounding the impacts [*Hibert et al.*, 2011; *Farin et al.*, 2015]:

898 
$$W_{el} = 4\pi r h \rho c_R \int_0^{+\infty} |\tilde{V}(r,f)|^2 \exp(\gamma(f)r) \, \mathrm{d}f,$$
(44)

where  $h = c_R/f$  is the Rayleigh wavelength and  $|\tilde{V}(r, f)|^2 = |\tilde{V}_X(r, f)|^2 + |\tilde{V}_Y(r, f)|^2 + |\tilde{V}_Y(r, f)|^2$  is the sum of the squared time Fourier transforms of the vibration speeds in the three directions of space  $v_X(r, t)$ ,  $v_Y(r, t)$  and  $v_Z(r, t)$ , respectively. The coefficient  $\gamma(f) = \pi f/Qc_R$  is the same than that used to compute the synthetic spectrum in the previous section, with  $c_R = 800 \text{ m s}^{-1}$  and Q = 10.

The nature of the contact between the boulder and the ground during the impact plays a crucial role on the transfer of the seismic energy. Therefore, we separated the "hard" impacts, occurring on outcropping rock, from the "soft" impacts, occurring on loose soil or on grass (Figures 16d to 16g). The measured radiated elastic energy  $W_{el}$  seems to be proportional to the mass m as predicted analytically for impacts on thick blocks (Table 1

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and Figure 16d). This dependance is clearer for "soft" impacts. However, the measured 909 radiated elastic energy  $W_{el}$  does not scale well with the parameter  $mV_z^{13/5}$  derived from 910 Hertz's theory (Figure 16e). We adjust the power a of parameter  $mV_z^a$  to obtain a better fit 911 with  $W_{el}$ . The best fit is observed for power  $a \simeq 0.5$ , i.e. with a much weaker dependence 912 on the impact speed  $V_z$  than in theory, with  $W_{el} \propto V_z^{0.5}$  rather than  $W_{el} \propto V_z^{13/5}$  (Figure 913 16f). The scaling law in  $V_z^{0.5}$  may be biased because boulders systematically impacted 914 loose soil when they reached high speeds  $V_z$  while they often impacted outcropping rocks 915 for lower speeds  $V_z$ . The energy transfer is lower for "loose" impacts than for "hard" 916 impacts and this may then leads to the observed weaker dependence in  $V_z$  (Figure 16g). 917 As a matter of fact, the mean ratio of the radiated elastic energy  $W_{el}$  over the kinetic 918 energy  $\Delta E_c$  lost during the impacts is one order of magnitude higher for "hard" impacts 919 than for "soft" impacts (Figure 16g). Interestingly, the ratio  $W_{el}/\Delta E_c$  is between  $10^{-4}$ 920 and  $10^{-1}$ , which is in agreement with the values observed by *Hibert et al.* [2011]. 921

No clear dependence on m and  $V_z$  was observed for the characteristic frequencies of the signal  $f_{mean}$  and  $\Delta f$ . These frequencies are between 10 Hz and 30 Hz, regardless of the contact quality i.e., of the fact that the impact is "hard" or "soft" [see Figure 92 in Chapter 4 of *Farin*, 2015].

An explanation for the discrepancy between observed and theoretical elastic energy  $W_{el}$ and for the fact that we did not observe any trend for the frequencies may be that we can not record frequencies higher than 50 Hz because the sampling frequency is 100 Hz. Impacts of boulders are expected to generate waves of higher frequencies. For example, *Helmstetter and Garambois* [2010] dropped a boulder of similar dimensions on the Séchilienne rockslide site in the French Alps. Seismic signals generated by the impacts

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were sampled at 250 Hz by several seismic stations located a few tens of meters away. 932 In the spectrogram of these signals, energy is visible up to 100 Hz. As we previously 933 observed in laboratory experiments, when we do not measure the highest frequencies of 934 the generated signal, the discrepancy between the theory and the measurement increases 935 (e.g. for small masses m in Figures 8a to 8c). An other possibility is that the factor 936  $\exp(\gamma(f)r)$ , with  $\gamma(f) = \pi f/Qc_R$ , may be too simple to describe the wave propagation is 937 such a damaged medium. Indeed, multiple modes with different dispersion relations can 938 be excited in different frequencies range in such layered media. However, the data are not 939 sufficient to determine how wave disperse and attenuate within the ground on this specific 940 site. 941

Owing to the large scattering of the seismic data, it is difficult to neither validate 942 nor invalidate the applicability on the field of the analytical scaling laws developed in this 943 paper. However, this study highlights several challenges that need to be addressed in order 944 to be able to retrieve the impacts parameters in future seismic studies of boulder impacts. 945 If the radiated elastic energy or the characteristics frequencies of the emitted signals are 946 underestimated, this will lead to either overestimate or underestimate the masses and 947 impact speed, as evidenced in our laboratory experiments (Figure 10). Therefore, one 948 should measure as much as possible the entire energy spectrum emitted by the impacts 949 and, to do so, use a high sampling frequency, ideally greater than  $3/T_c$  (see section 2.2.2). 950 Moreover, because energy at high frequencies attenuate very rapidly in fractured media, 951 one should record the signal a close as possible from the impacts. Finally, one should have 952 a good knowledge of the elastic properties of the impactor and the ground in the vicinity 953 of the impact, as well as within the ground i.e., its how it disperses and attenuates the 954

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955 frequencies. This could be achieved using several seismic stations recording at different956 distances from the source.

#### 6. Conclusions

We developed analytical scaling laws relating the characteristics of the acoustic signal 957 generated by an impact on a thin plate and on a thick block (radiated elastic energy, fre-958 quencies) to the parameters of the impact: the impactor mass m and speed before impact 959  $V_z$  and the elastic parameters. These laws were validated with laboratory experiments of 960 impacts of spherical beads of different materials and gravels on thin plates with a smooth 961 962 surface, which is an ideal case, and on rough thick blocks, which are closer to the case of the field. Viscoelastic and elasto-plastic dissipation occurred in the range of masses and 963 impact speeds investigated. In these experiments, the radiated elastic energy is estimated 964 from vibration measurements, independently of the other processes of energy dissipation. 965 A number of conclusions can be drawn from our results: 966

1. The impactor mass m and speed  $V_z$  can be estimated from two independent pa-967 rameters measurable on the field of the seismic signal: the radiated elastic energy and a 968 characteristic frequency, using equations (27) to (30). The estimations of m and  $V_z$  are 969 close to the real values within a factor of 2 and 3, respectively, even when the impactor 970 has a complex shape. If the radiated elastic energy is underestimated (respectively, over-971 estimated) by a factor of 10, the mass m and the impact speed  $V_z$  are underestimated 972 (respectively, overestimated) by a factor of 1.5 and 2, respectively. We noted that the 973 radiated elastic energy is smaller when the surface roughness increases because the ra-974 dius of contact is smaller. However, the signal characteristics measured during impacts of 975

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976 rough impactors on rough surfaces follows well the scaling laws established for impacts of977 spherical beads on a plane surface.

978 2. We also established a quantitative energy budget of the impacts on the plates and979 blocks investigated and we estimated what should be this budget for naturals rockfalls:

(i) On the smooth plates, elastic waves and viscoelastic dissipation are the main
processes of energy losses. Viscoelastic dissipation is major for impactors of diameter
less than 10% of the plate thickness while elastic waves radiation represents only from
0.1% to 0.3% of the impact energy. When the bead diameter increases, the energy lost in
viscoelastic dissipation decreases while the energy radiated in elastic waves increases. For
beads of diameter larger than the plate thickness, almost all of the energy is radiated in
elastic waves.

(ii) On the rough blocks, elastic dissipation represents only between 0.03% and 5%
of the lost energy. In contrast, energy lost in other processes such as plastic deformation
increases with the bead mass from 50% to more than 99% of the lost energy because of
surface roughness. The energy dissipated in viscoelasticity decreases from 50% to 2% of
the lost energy as the bead mass increases.

(iii) Most of the energy lost during a natural rockfall should be dissipated in plastic deformation or in translational or rotational modes of the impactors. Plastic or in general irreversible dissipation reduces the energy radiated in elastic waves and is difficult to quantify. That said, regardless of the impactor mass and speed, the energy radiated in elastic waves may not be more than a few percent of the impact energy. Energy lost in viscoelastic dissipation should be negligible in the range of masses detected by seismic stations on the field.

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The impacts experiments with rough impactors on rough substrates demonstrated that 999 Hertz's model can be used to describe at first order the dynamics of an impact when the 1000 contact surface is not plane. Thus, we expect that the simple analytical relations derived 1001 in this paper between the characteristics of the impact and that of the emitted signal can 1002 allow us to better understand the process of elastic waves generation by impacts on the 1003 field. The major limitation for estimating the impact properties from the signal on the 1004 field would certainly be the fact that a great part of the radiated energy is lost in high 1005 frequencies during wave propagation in highly fractured media. Therefore, we encourage 1006 future seismic studies of rockfalls to record signals as close as possible to the impacts and 1007 to use a high frequency sampling. In addition, it is important to correct measured seismic 1008 signals from wave dispersion and attenuation within the substrate. If these conditions are 1009 fulfilled, the scaling laws derived in this study should provide estimates of the order of 1010 magnitude of the masses and speeds of the impactors. Finally, in addition to direct field 1011 applications, the scaling laws developed for plates can be also useful in the industry as a 1012 1013 non-intrusive technique to estimate the size and speed of particles in a granular transport and in shielding problems. 1014

# Appendix A: Demonstration of the Analytical Scaling Laws for the Radiated Elastic Energy

The objective of this Appendix is to demonstrate the analytical scaling laws showed in Table 1 for the radiated elastic energy  $W_{el}$  as a function of the impactor's mass m and speed  $V_z$  for thin plates and thick blocks.

1018 The radiated elastic energy is defined by:

1019 
$$W_{el} = \int_{-\infty}^{+\infty} |F_z(t)|^2 Y_{el}(t) dt = 2 \int_0^{+\infty} |\tilde{F}_z(f)|^2 \tilde{Y}_{el}(f) df,$$
(A1)

1020 with  $\tilde{Y}_{el}(f)$  the radiation admittance, that has a different expression on thin plates and 1021 on thick blocks.

# A1. Thin Plates

1022 On thin plates,  $\tilde{Y}_{el}(f)$  is independent of frequency f and is given by:

1023 
$$Y_{el} = \frac{1}{8\sqrt{B\rho_p h}}.$$
 (A2)

1024 where B is the bending stiffness and  $\rho_p$  and h are the plate density and thickness, respec-1025 tively.

1026 Therefore,

1027

$$W_{el} = \frac{1}{8\sqrt{B\rho_p h}} \frac{F_0^2 \delta_{z0}}{V_z} \int_{-\infty}^{+\infty} |g(t^*)|^2 \mathrm{d}t^*, \tag{A3}$$

1028 with  $t^* = \delta_{z0}t/V_z$  and where  $g(t^*)$  is the shape function represented on Figures 1b and 1c. 1029 The integral in this equation is noted  $C_{plate}$  and depends on the inelastic parameters  $\alpha$ 1030 and  $P_Y/P_0$  i.e., of the fact that the impact is elastic, viscoelastic or elasto-plastic (Figures 1031 2a and 2b). For an elastic impact,  $C_{plate} = 1.21$ .

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Developing  $F_0$  and  $\delta_{z0}$  as functions of the impact parameters using their expressions in equations (5) and (8), respectively, we get:

1034 
$$\frac{F_0^2 \delta_{z0}}{V_z} = \left(\frac{4}{3}\right)^{1/3} \left(\frac{5}{4}\right)^{8/5} \pi^{-1/15} \rho_s^{-1/15} E^{*2/5} m^{5/3} V_z^{11/5}.$$
 (A4)

1035 Finally, equations (A3) and (A4) give the scaling law relating the radiated elastic energy 1036  $W_{el}$  to the impact parameters on thin plates:

1037 
$$W_{el} = a_1 C_{plate} m^{5/3} V_z^{11/5}, \tag{A5}$$

1038 with  $a_1 \approx 0.18 E^{*2/5} / (\rho_s^{1/15} \sqrt{B \rho_p h}).$ 

# A2. Thick Blocks

1039 On thick blocks, the radiation admittance  $\tilde{Y}_{el}(f)$  was computed in time Fourier domain 1040 by *Miller and Pursey* [1955]:

1041 
$$\tilde{Y}_{el}(f) = \frac{2\pi\xi^4 \beta f^2}{\rho_p c_P^3},$$
 (A6)

1042 where  $\xi = \sqrt{2(1 - \nu_p)/(1 - 2\nu_p)}$ ,  $c_P$  is the compressive wave speed and  $\beta$  is the imaginary 1043 part of

1044 
$$\int_{0}^{X} \frac{x\sqrt{x^{2}-1}}{f_{0}(x)} \mathrm{d}x,$$
 (A7)

with  $f_0(x) = (2x^2 - \xi^2)^2 - 4x^2\sqrt{(x^2 - 1)(x^2 - \xi^2)}$  and X, a real number greater than the positive real root of  $f_0$ . The coefficient  $\beta$  depends only on the Poisson's ratio  $\nu_p$  (Figure 1047 17, see the Appendix of *Farin et al.* [2015] for details on the computation of  $\beta$ ).

1048 Therefore,

1049

$$W_{el} = \frac{4\pi\xi^4\beta}{\rho_p c_P^3} \frac{F_0^2 V_z}{\delta_{z0}} \int_0^{+\infty} f^{*2} |\tilde{g}(f^*)|^2 \mathrm{d}f^*, \tag{A8}$$

1050 with  $f^* = V_z f / \delta_{z0}$  and  $\tilde{g}(f^*)$  is the time Fourier transform of the function  $g(t^*)$  represented

1051 on Figures 1b and 1c. We note  $C_{block}$  the integral in this equation.  $C_{block}$  depends on the D R A F T September 11, 2015, 6:01pm D R A F T

inelastic parameters  $\alpha$  and  $P_Y/P_0$  (Figures 2a and 2b). With an impact force  $F_z(t)$  given by *Hertz* [1882]'s elastic theory i.e., for  $\alpha = 0$  and  $P_Y/P_0 = 1$ , we have  $C_{block} = 0.02$ .

1054 If we develop  $F_0$  and  $\delta_{z0}$  as functions of the impact parameters, we get:

1055 
$$\frac{F_0^2 V_z}{\delta_{z0}} = \frac{4}{3} \left(\frac{5}{4}\right)^{4/5} \pi^{-1/5} \rho_s^{-1/5} E^{*6/5} m V_z^{13/5}.$$
 (A9)

1056 Finally, inserting equation (A9) into equation (A8) we obtain the analytical expression of 1057 the radiated elastic energy  $W_{el}$  on thick blocks:

1058 
$$W_{el} = a_2 C_{block} m V_z^{13/5}, \tag{A10}$$

1059 with the coefficient  $a_2 \approx 15.93 \xi^4 \beta E^{*6/5} / (\rho_p \rho_s^{1/5} c_P^3)$ .

# Appendix B: Cumulative Distribution of Energy

1060 In this Appendix, we show how the radiated elastic energy radiated by impacts is1061 distributed over the frequencies.

The cumulative distribution of the radiated elastic energy shows that impacts generate 1062 signals with higher frequencies as the bead diameter d decreases, regardless of the structure 1063 (Figure 18). It is clear that the sensors used in our experiments do not measure energy for 1064 frequencies higher than 50 kHz. This is not a problem for impacts on the PMMA plate 1065 and for beads of diameter d larger than 5 mm because all of the radiated elastic energy is 1066 in theory below 50 kHz (Figure 18a). However, for impacts of beads of 1 mm in diameter 1067 on glass, concrete and marble, more than 50% of the energy is for frequencies higher than 1068 50 kHz (Figures 18b to 18d). Some of the radiated energy may not be measured for the 1069 smallest beads investigated. Note that for experiments on the glass plate and on the 1070 concrete and marble blocks, the profile of the cumulative energy is steep and saturates 1071

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1072 to a given frequency  $f \approx 38$  kHz,  $f \approx 30$  kHz and  $f \approx 40$  kHz, respectively, as the bead 1073 diameter d decreases (Figures 18b to 18d).

### Appendix C: Influence of the Impactor Shape on the Energy Budget

1074 In this Appendix, we investigate the energy budget of impacts of gravels on the glass1075 plate.

When a spherical bead is dropped without initially speed and rotation on a smooth sur-1076 face it rebounds almost vertically and without spin. In contrast, a rough gravel rebounds 1077 to a much smaller height and can reach a large horizontal distance x with a high rotation 1078 speed  $\omega_r$  up to about 400 rad s<sup>-1</sup>, depending on the face it lands on (Figure 19a). For these 1079 complex impactors, the kinetic energy converted in translational and rotational modes is 1080 therefore not negligible. The translational kinetic energy of rebound is  $E'_c = \frac{1}{2}mV'^2$  where 1081  $V' = V'_x \mathbf{u}_x + V'_z \mathbf{u}_z$  is the rebound speed in the cartesian frame  $(0, \mathbf{u}_x, \mathbf{u}_z)$ .  $V'_x \approx 0 \text{ cm s}^{-1}$ 1082 for spherical beads but varies from 5 cm s<sup>-1</sup> to 40 cm s<sup>-1</sup> for gravels. The rotation energy 1083 is  $E_{\omega} = \frac{1}{2}I\omega_r^2$ , where I is the moment of inertia of the gravel, given by  $I = \frac{2}{5}mR^2$  if we 1084 assume that the gravel is spherical with an equivalent radius R. From camera recordings, 1085 we estimate that  $32\% \pm 17\%$  of the impact energy  $E_c$  is converted into translational energy 1086 of rebound  $E'_c$  and that  $13\% \pm 11\%$  is converted into rotational energy  $E_{\omega}$ . Regardless of 1087 the shape and mass m of the gravel, less energy is converted into translational energy  $E'_c$ 1088 as its rotates faster after the impact (Figure 19b). The percentage of energy radiated in 1089 elastic waves  $W_{el}/E_c$  is  $3.3\% \pm 1.8\%$  and seems independent of the energy converted in 1090 translation energy  $E'_c/E_c$  or in rotational modes  $E_{\omega}/E_c$  (Figures 19c and 19d). 1091

In section 4.4.1, we adjusted the inelastic parameter D on the variation of the coefficient of restitution e to estimate the energy lost in viscoelastic dissipation (Figure 12). This

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is not possible for gravels because of the large dispersion in the results. As granite has 1094 similar elastic properties than glass, we assume that D is the same than for glass beads 1095 impacts on the glass plate i.e., D = 80 ns (see Table 5). Therefore, the viscoelastic 1096 dissipation  $W_{visc}$  for impacts of gravels on the glass plate may represent  $3.7\% \pm 1\%$  of  $E_c$ . 1097 The rest of the energy  $(48\% \pm 14\%)$  is lost to deform plastically the gravel and or the 1098 glass plate. This is therefore the main process of energy dissipation for gravels impacts. 1099 The proportion of energy radiated in elastic waves  $W_{el}/E_c$  seems to decrease when 1100 more energy is lost in plastic deformation (Figure 19e), which is in agreement with the 1101 elasto-plastic model (Figure 2a). 1102

## Appendix D: Determining Impactor Momentum from Low Frequencies

In some experiments on Figure 10, the estimations of m and  $V_z$  are affected because the highest frequencies of the generated vibration are not measured by the sensors or because of a resonance. The purpose of this Appendix is to show that we can use the low frequencies content of the signal to estimate the momentum  $mV_z$  of the impactor.

For frequencies  $f \sim 0$  Hz, we assume as *Tsai at al.* [2012] that the impact duration  $T_c$ is instantaneous relative to the frequencies of interest. The time Fourier transform  $\tilde{F}(f)$ of the *Hertz* [1882] force F(t) then becomes constant in frequency:

1110 
$$\tilde{F}(f) = \int_{-\infty}^{+\infty} F(t) \exp(-ift) dt \sim \int_{-\infty}^{+\infty} F(t) dt.$$
(D1)

1111 where, if we normalize the force F(t) by its maximum value  $F_0$  and time t by the impact 1112 duration  $T_c$  and develop their respective expressions [equations (9) and (10)],

1113 
$$\int_{-\infty}^{+\infty} F(t) dt \approx 2mV_z.$$
 (D2)

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1114 The amplitude spectrum of the vibration acceleration can then be approximated by 1115 [Aki and Richards, 1980]:

1116 
$$|\tilde{A}_z(r, f \to 0)| \sim 2mV_z(2\pi f)^2 |\tilde{G}_{zz}(r, f)|.$$
 (D3)

Using the expression of the Green's function  $|\tilde{G}_{zz}(r, f)|$  given by equations (3) and (4) on plates and blocks, respectively, we show that:

1119 
$$|\tilde{A}_z(r, f \to 0)| \sim a f^b, \tag{D4}$$

1120 with  $a \approx 0.73 m V_z \frac{1}{B\sqrt{r}} (\frac{B}{\rho_p h})^{5/8}$  and b = 3/4 on plates and  $a \approx 100 m V_z \frac{\xi^2}{\mu c_P} \frac{\sqrt{x_0(x_0^2 - 1)}}{f'_0(x_0)} \sqrt{\frac{2c_P}{\pi r}}$ 1121 and b = 5/2 on blocks.

In order to determine the momentum  $mV_z$  of a steel bead of diameter 5 mm dropped from height 10 cm on the glass plate and on the concrete block, we adjust the power law (D4) with the measured spectra  $|\tilde{A}_z(r, f)|$  for frequencies f < 10 kHz (Figure 20). The obtained momentum is  $mV_z \approx 6.9 \cdot 10^{-4}$  kg m s<sup>-1</sup> on glass plate and  $mV_z \approx 6.33 \cdot 10^{-4}$ kg m s<sup>-1</sup> on the concrete block, which is in good agreement with the real momentum  $mV_z \approx 6.85 \cdot 10^{-4}$  kg m s<sup>-1</sup>. Finally, if either m or  $V_z$  is known, this method can be used to estimate the other parameter.

# Notation

 $c_P, c_R$  Compressional and

Rayleigh waves speed

 $\begin{array}{c} ({\rm m}\ {\rm s}^{-1})\\ D \quad {\rm Viscoelastic} \ {\rm coeffi-} \end{array}$ 

 $\begin{array}{c} \text{cient (s)} \\ d, R \quad \text{Bead diameter and} \end{array}$ 

radius (m)

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$E_c$	Initial kinetic en-
$E_s, E_p, \nu_s, \nu_p$	ergy (J) Young's modulii (Pa)
	and Poisson's coef-
	ficients of the sphere and
<b></b>	the plane

 $E^*$  Equivalent Young's

e Coefficient of resti-

 $\begin{array}{c} {\rm tution} \ (\mbox{-}) \\ {\bf F}, \ F_z \quad {\rm Force} \ \ {\rm and} \ \ {\rm normal} \end{array}$ 

force (N)  $F_0, P_0$  Maximum force and

stress of elastic im-

$F_{max},  \delta_{max}$	pact (N; Pa) Maximum force and
	penetration depth
	of inelastic impact
$f,\omega$	(N) Frequency and an-
	gular frequency $(s^{-1})$
$f_{peak}, f_{mean}, \Delta f$	Peak, mean fre-
	quencies and band-

width (Hz) g Acceleration of grav-

itation (m s<sup>-2</sup>) H Height of fall (m)

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h Plate thickness (m)

K Parameter in Hertz

[1882]'s theory k Wave number  $(m^{-1})$ 

- V Volume  $(m^3)$
- m Mass (kg)
- r Distance from the

 $\begin{array}{l} \text{impact (m)} \\ T_c \quad \text{Impact duration (s)} \end{array}$ 

- t Time (s)
- $\mathbf{u}_i$  Normalized vector

 $\begin{array}{c} \qquad \qquad \text{ of the direction } i \\ v_i, \, a_i \quad \text{Vibration speed and} \end{array}$ 

acceleration in the

direction  $\mathbf{u}_i$  (m

$$s^{-1}; m s^{-2})$$

 $\tilde{V}_i, \tilde{A}_i$  Time Fourier trans-

form of  $v_i$  and  $a_i$ ,

respectively (m; m

$$s^{-1})$$

 $V_z, V'$  Impact speed and

speed after rebound

$$(m s^{-1})$$
  
 $v_g, v_\phi$  Group and phase

velocities (m  $s^{-1}$ )

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$W_{el}, \Delta E_c$	Radiated elastic en-
	ergy and total en-
$W^{th}_{el},W^{th'}_{el}$	ergy lost (J) Theoretical radi-
	ated elastic energy
	predicted by $Hertz$ [1882]'s and
	Zener [1941]'s mod-
$W_{visc}, W_{other}, E'_c, E_{\omega}$	els (J) Energy lost in vis-
	coelastic dissipa-
	tion, in other pro-
	cesses, kinetic energy of
	rebound and rota-
x,y,z	tion (J) Coordinates in the
	cylindric reference
	frame of the block
$Y_d, P_d$	(m) Dynamic yield stress
	and dynamic yield
$\alpha$	strength (Pa) Viscoelastic param-
	eter (-)

with distance  $(m^{-1})$ 

 $\delta_z, \, \delta_{z0}$  Penetration depth

and maximum of

this depth during

the impact (m)  $\lambda_Z$  Zener [1941]'s pa-

rameter (-)  $\rho_s, \rho_p$  Densities of the

sphere and the plane

 $\begin{aligned} & (\text{kg m}^3) \\ & \tau & \text{Characteristic time} \\ & \text{of energy attenu-} \\ & \text{ation within the} \\ & \text{xtructure (s)} \\ & \chi, \eta & \text{Bulk and shear} \\ & \nu \text{iscosities (Pa s)} \\ & \omega_r & \text{Rotation speed (rad)} \end{aligned}$ 

 $s^{-1}$ )

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	Plates	Blocks
$W_{el}$	$a_1 C_{plate} m^{5/3} V_z^{11/5}$	$a_2 C_{block} m V_z^{13/5}$
VV el	$a_1 C_{plate} M^{-1} V_z$ $a_3 C_{plate} R^5 H^{11/10}$	$a_4 C_{block} R^3 H^{13/10}$
$W_{visc}$	$C_{visc}m$	$V_z^2$
VV visc	$a_5 \cup_{visc} r$	
	$a_1 \approx 0.18 \frac{E^{*2/5}}{\rho_s^{1/15} \sqrt{B\rho_p h}}$	$a_2 \approx 15.93 \frac{\xi^4 \beta E^{*6/5}}{\rho_p \rho_s^{1/5} c_P^3}$
	$a_3 = (2g)  (\overline{3}\pi\rho_s)  (a_1)$	$a_4 = (2g)^{13/10} \frac{4}{3} \pi \rho_s a_2$
	$a_5 = 2g \frac{4}{3}$	$\frac{1}{3}\pi\rho_s$

Table 1. Scaling laws for the radiated elastic energy and the energy dissipated in viscoelasticity.<sup>a</sup>

<sup>a</sup> Radiated elastic energy  $W_{el}$  and energy  $W_{visc}$  dissipated in viscoelasticity for plates of thickness h and blocks as a function of the impact parameters. The coefficients  $a_i$  depend only on the elastic parameters of the impactor and of the structure. The parameter  $\beta$  is a function of the Poisson's ratio  $\nu_p$  only (see Figure 17 of Appendix A). The coefficients  $C_{plate}$  and  $C_{block}$  are represented on Figure 2.

Table 2.	Characteristics	frequencies <sup>a</sup>
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	$f_{mean}$	$\Delta f$
plates	$0.75/T_{c}$	$0.72/T_{c}$
blocks	$1/T_c$	$0.6/T_{c}$

<sup>a</sup> Theoretical mean frequency  $f_{mean}$  and bandwidth  $\Delta f$ , as respectively defined by equations (25) and (26), of the acoustic signal generated by an elastic impact on a thin plate and on a thick block.

**Table 3.** Characteristics of the impactors used in experiments: density  $\rho_s$ , Young's modulus

$E_s$ , Poisson's ratio $\nu_s$ , diameter d and mass m.							
	material	$\rho_s$ (kg m <sup>-3</sup> )	$E_s$	$\nu_s$	d	m	
	materiar	$(\mathrm{kg} \mathrm{m}^{-3})$	(GPa)	-	(mm)	(g)	
	$_{\mathrm{glass}}$	2500	74	0.2	1 - 20	$1.3.10^{-3} - 10$	
spherical beads	polyamide	1140	4	-	-	$6.10^{-4} - 4.8$	
	steel	7800	203	0.3	1 - 20	$4.1.10^{-3} - 33$	
gravels	granite	3600	60	0.27	$\approx 4-28$	0.08 - 18	

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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$						1			
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	matorial		$ ho_p$		$ u_p$	$\gamma$	τ	$v_g$	$v_{\phi}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	material		$(\mathrm{kg} \mathrm{m}^{-3})$	(GPa)	-	(1/m)	(s)	$(m \ s^{-1})$	( /
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	alorg	kh < 1	2500	74	0.2	$0.014 f^{1/6}$	$2 \circ f^{-2/3}$	$18.6f^{1/2}$	$9.3f^{1/2}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	glass	kh > 1	2000	14	0.2	$8.5 \times 10^{-5} f^{2/3}$	<b>J</b> .0 <i>j</i>	3100	3100
$\frac{kh > 1}{\text{concrete} - 2300  16.3  0.4  2.3.10^{-5}f  28f^{-1}  1530  1530}$	риил	kh < 1	1120	2.4	0.27	1		$11.7f^{1/2}$	$5.8f^{1/2}$
<i>v v</i>	I WIWIA	kh > 1	1100	2.4	0.57	$4.8 \times 10^{-3} f^{2/3}$	$0.15 f^{-2/3}$	1400	1400
marble - 2800 26 $0.3$ $2.5.10^{-5}f$ $23.1f^{-1}$ 1750 1750	concrete	-	2300	16.3	0.4	$2.3.10^{-5}f$	$28f^{-1}$	1530	1530
	marble	-	2800	26	0.3	$2.5.10^{-5}f$	$23.1f^{-1}$	1750	1750

Table 4. Characteristics of the materials used in experiments<sup>a</sup>

<sup>a</sup> Density  $\rho_p$ , Young's modulus  $E_p$ , Poisson's ratio  $\nu_p$ , characteristic distance  $1/\gamma$  and time  $\tau$  of energy attenuation, group velocity  $v_g$  and phase velocity  $v_{\phi}$  (that depend on the frequency f (in Hz)) [see the supplementary materials of *Farin et al.*, 2015, for details on the measurement of  $\gamma$  and  $\tau$ ].

**Table 5.** Viscoelastic constant D (in ns)<sup>a</sup>.

	<b>X</b>	/			
substrate		PMMA	glass	concrete	marble
	$_{\rm glass}$	230	80	100	180
bead	polyamide	580	550	300	300
	steel	190	35	200	200

<sup>a</sup> Value of the viscoelastic constant D appearing in equation (19) and adjusted on experimental data for impacts of spherical beads of different material (rows) on the different substrates (columns). X - 72

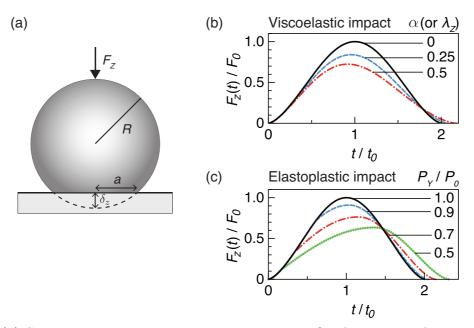


Figure 1. (a) Schematic showing the penetration depth  $\delta_z$  of a sphere of radius R on a plane surface during an impact. Geometrically, the surface of contact is a circle of radius a. (b) and (c) Normalized force of impact  $F_z(t/t_0)/F_0$  for (b) different values of the viscoelastic parameter  $\alpha$  (or  $\lambda_Z$  for Zener [1941]'s theory; see section 2.1.1.2) and for (c) different values of the stresses ratio  $P_Y/P_0$ .  $F_0$  and  $t_0 = T_c/2$  are respectively the force and the time at maximal compression during an elastic impact i.e., for  $\alpha = 0$  and  $P_Y/P_0 = 1$ .

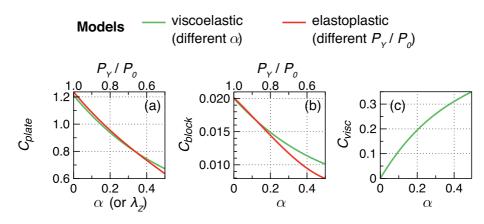


Figure 2. (a), (b) and (c) Values of the constants (a)  $C_{plate}$ , (b)  $C_{block}$  and (c)  $C_{visc}$  as a function of the inelastic parameters  $\alpha$  for a viscoelastic impact (or  $\lambda_Z$  for Zener [1941]'s theory) (green) and  $P_Y/P_0$  for an elasto-plastic impact (red).

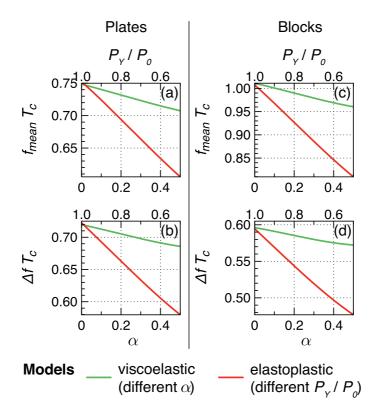


Figure 3. Theoretical values of the (a), (c) mean frequency  $f_{mean}$  and (b), (d) bandwidth  $\Delta f$  for (a) and (b) thin plates and (c) and (d) thick blocks, as a function of the inelastic parameters  $\alpha$  (green) and  $P_Y/P_0$  (red). All frequencies are multiplied by *Hertz* [1882]'s impact duration  $T_c$  to be dimensionless.

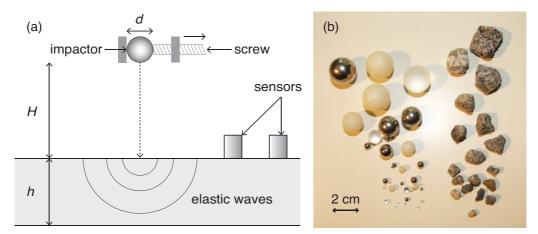


Figure 4. (a) Scheme of the experimental setup. An impactor of diameter d is initially held by a screw and dropped without initial speed or rotation on a hard structure of thickness h. The height of fall H varies from 2 cm to 30 cm. The impact generates elastic waves, recorded by an array of accelerometers. (b) Spherical beads of glass, polyamide and steel and granite gravels used as impactors in the experiments.

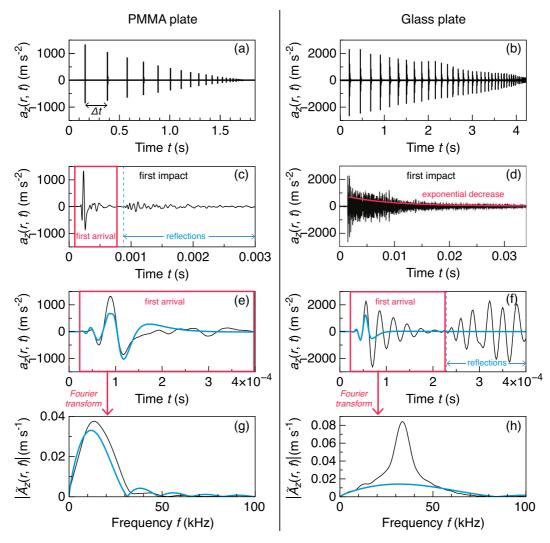


Figure 5. (a) and (b) Acceleration signal  $a_z(r,t)$  generated by the successive impacts of a steel bead of diameter d = 5 mm, dropped from height H = 10 cm on (a) the PMMA plate and (b) the glass plate. The time of flight  $\Delta t$  between two impacts is equal to the duration between two peaks. (c) and (d) Zoom on the signal of the first rebound, filtered below 100 kHz. The coda envelope decreases exponentially with time in the glass plate (red line). (c),(e) and (f) The first arrival is delimited by a red frame and the first reflections off the plate lateral sides arrive at the right of the blue dashed line. The arrival time of the reflections is computed knowing the wave speed and the distance between the sensor and the substrate sides. (g) and (h) The time Fourier transform of the first arrival gives the amplitude spectrum  $|\tilde{A}_z(r, f)|$  as a function of the frequency f. The thick blue line in Figures (e) to (h) represents the synthetic signal and **pupplituderspectrum obtained bySequencesion of Honts**, [1682] pmforce of impact with the Gategar's function.

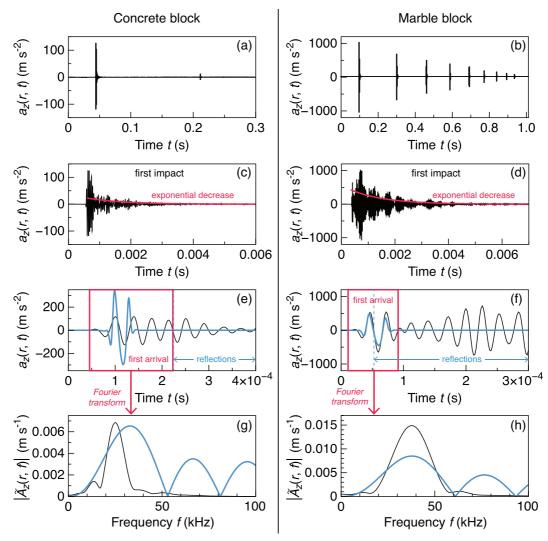


Figure 6. (a) and (b) Acceleration signal  $a_z(r,t)$  generated by the successive impacts of a steel bead of diameter d = 5 mm, dropped from height H = 10 cm on (a) the concrete block and (b) the marble block. (c) and (d) Zoom on the signal of the first rebound, filtered below 100 kHz. The coda envelope decreases exponentially with time (red line). (e) and (f) The first arrival is delimited by a red frame and the first reflections off the plate lateral sides arrive at the right of the blue dashed line. The arrival time of the reflections is computed knowing the wave speed and the distance between the sensor and the substrate sides. (g) and (h) The time Fourier transform of the first arrival gives the amplitude spectrum  $|\tilde{A}_z(r, f)|$  as a function of the frequency f. The thick blue line in Figures (e) to (h) represents the synthetic signal and amplitude spectrum obtained by convolution of *Hertz* [1882]'s force of impact with the Green's

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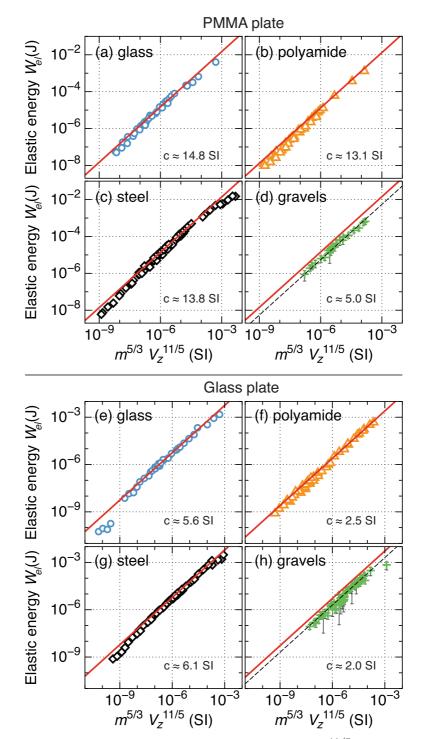


Figure 7. Radiated elastic energy  $W_{el}$  as a function of  $m^{5/3}V_z^{11/5}$  for impacts of (a)-(e) glass, (b)-(f) polyamide and (c)-(g) steel beads and (d)-(h) gravels on (a) to (d) the PMMA plate and on (e) to (h) the glass plate. The red line corresponds to the theoretical energy  $W_{el}^{th}$  given in Table 1 for an elastic impact i.e., with  $C_{plate} = 1.21$ . The black dashed line is a fit to the data of the law  $W_{el} = cm^{5/3}V_z^{11/5}$ , with coefficient c indicated in International System Units (SI). In PhostAcEseT, this line collapses with the determination on a series of 20 experiments and are symbols sized.

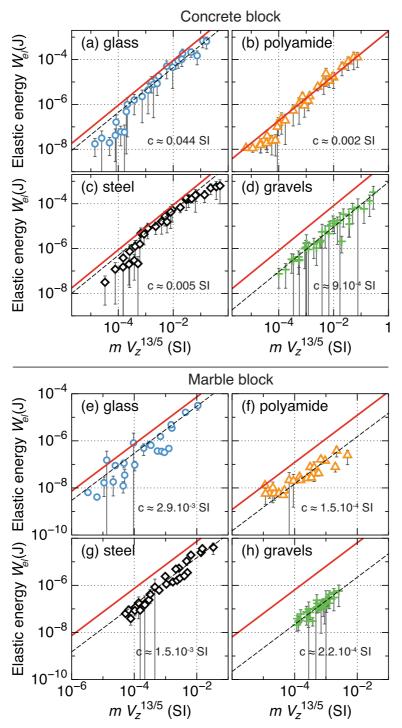


Figure 8. Radiated elastic energy  $W_{el}$  as a function of  $mV_z^{13/5}$  for impacts of (a)-(e) glass, (b)-(f) polyamide and (c)-(g) steel beads and (d)-(h) gravels on (a) to (d) the concrete block and on (e) to (h) the marble block. The red line corresponds to the theoretical energy  $W_{el}^{th}$  given in Table 1 for an elastic impact i.e., with  $C_{block} = 0.02$ . The black dashed line is a fit to the data of the law  $W_{el} = cmV_z^{13/5}$ , with coefficient c indicated in International System Units (SI).

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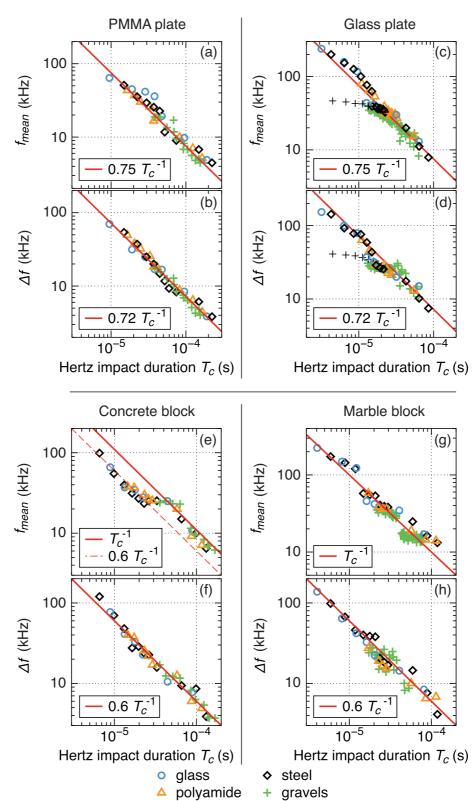


Figure 9. (a), (c), (e) and (g) Mean frequency  $f_{mean}$  and (b), (d), (f) and (h) bandwidth  $\Delta f$ as a function of *Hertz* [1882]'s impact duration  $T_c$  [equation (9)] for impacts of glass, polyamide and steel beads and granite gravels on (a) and (b) the PMMA plate, (c) and (d) the glass plate, fe)<sub>RapdF</sub>(f) the concrete block agelp(ghger) [h), the function of the red line corresponds to the theoretical prediction (Table 2) and the red dashed line in (e) is a fit to the data. The black crosses on Figures (c) and (d) correspond to the frequencies of the signals generated by steel beads measured with the accelerometers type 8309, that resonate around 38 kHz on the glass

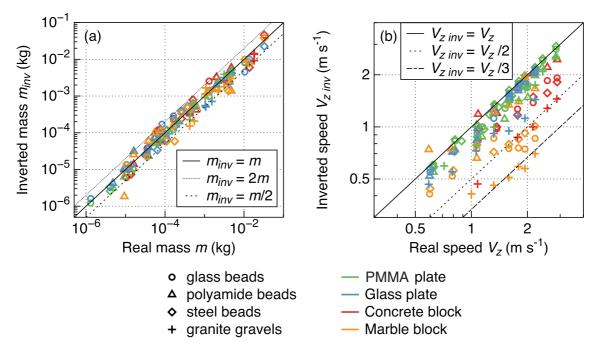


Figure 10. (a) Mass  $m_{inv}$  inverted from signal bandwidth  $\Delta f$  and radiated elastic energy  $W_{el}$ using equations (27) for plates and (29) for blocks as a function of the real mass m. (b) Impact speed  $V_{zinv}$  inverted using equations (28) for plates and (30) for blocks as a function of the real impact speed  $V_z$ . The black full line is a perfect fit.

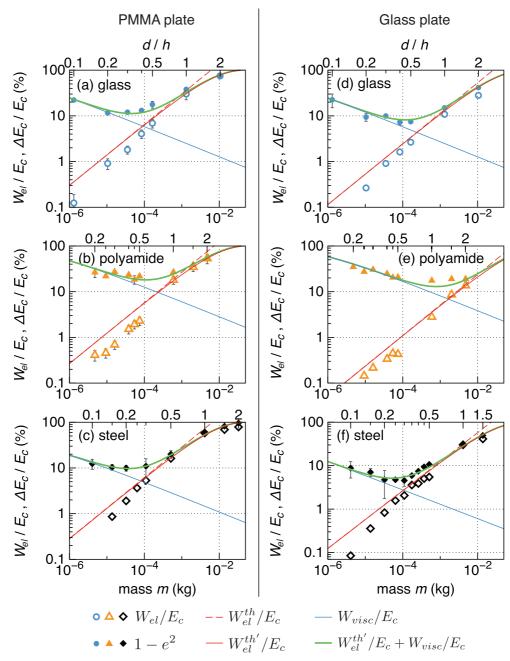


Figure 11. Ratio of the measured radiated elastic energy  $W_{el}$  over the impact energy  $E_c = \frac{1}{2}mV_z^2$  (empty symbols) and measured lost energy ratio  $\Delta E_c/E_c = 1 - e^2$  (full symbols) as a function of bead mass m and of the ratio of the bead diameter d on the plate thickness h for impacts of (a)-(d) glass, (b)-(e) polyamide and (c)-(f) steel beads on (a) to (c) the PMMA plate and on (d) to (f) the glass plate. The red dashed line corresponds to the theoretical ratio  $W_{el}^{th}/E_c$  with  $W_{el}^{th}$  in equation (23) for an elastic impact i.e., with  $C_{plate} = 1.21$ . The red full line is the energy ratio  $W_{el}^{th'}/E_c$  corrected with  $C_{plate}$  dependence on parameter  $\lambda_Z$ , the blue line is the  $V_{el}$  for  $V_{el}^{th'}/E_c$  and  $W_{visc}/E_c$ .

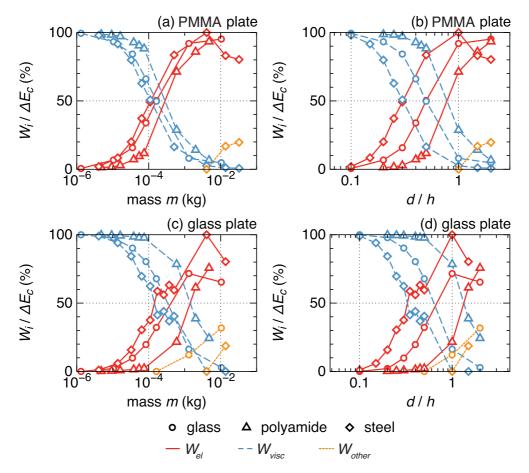


Figure 12. Percentage of the total energy lost in elastic waves  $W_{el}/\Delta E_c$  (red full line), by viscoelastic dissipation  $W_{visc}/\Delta E_c$  (blue dashed line) and by other processes  $W_{other}/\Delta E_c$  (orange dotted line) as a function of (a)-(c) the bead mass m and (b)-(d) the ratio of the bead diameter dover the plate thickness h for impacts of glass (circles), polyamide (triangles) and steel (diamonds) beads dropped from height H = 10 cm on (a)-(b) the PMMA plate and on (c)-(d) the glass plate.

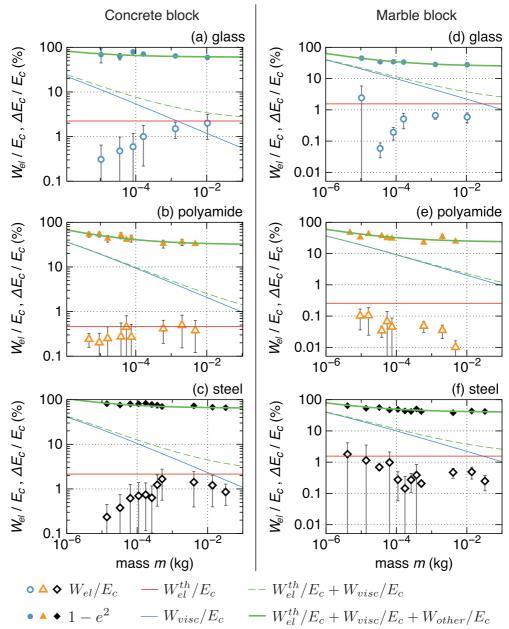


Figure 13. Ratio of the measured radiated elastic energy  $W_{el}$  over the impact energy  $E_c = \frac{1}{2}mV_z^2$  (empty symbols) and measured lost energy ratio  $\Delta E_c/E_c = 1 - e^2$  (full symbols) as a function of bead mass m for impacts of (a)-(d) glass, (b)-(e) polyamide and (c)-(f) steel beads on (a) to (c) the concrete block and on (d) to (f) the marble block. The red line represents the theoretical ratio  $W_{el}^{th}/E_c$  with  $W_{el}^{th}$  in equation (24) with  $C_{block} = 0.02$ . The blue line is the viscoelastic energy ratio  $W_{visc}/E_c$  [equation (35)]. The dashed green line is the theoretical lost energy ratio  $W_{el}^{th}/E_c + W_{visc}/E_c$ . The thick green line is the same ratio plus the percentage  $W_{other}/E_c$  of energy lost in other processes, which is assumed independent of the bead mass m D R A F T September 11, 2015, 6:01pm D R A F T (see text).

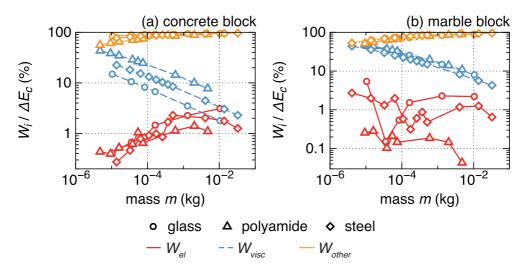


Figure 14. Percentage of the total energy lost in elastic waves  $W_{el}/\Delta E_c$  (red full line), by viscoelastic dissipation  $W_{visc}/\Delta E_c$  (blue dashed line) and by other processes  $W_{other}/\Delta E_c$  (orange dotted line) as a function of the bead mass m for impacts of glass (circles), polyamide (triangles) and steel (diamonds) beads dropped from height H = 10 cm on (a) the concrete block and on (b) the marble block.

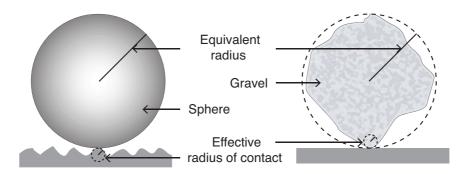


Figure 15. Schematic of the contacts between a sphere and a rough surface and between a rough gravel and a flat surface.

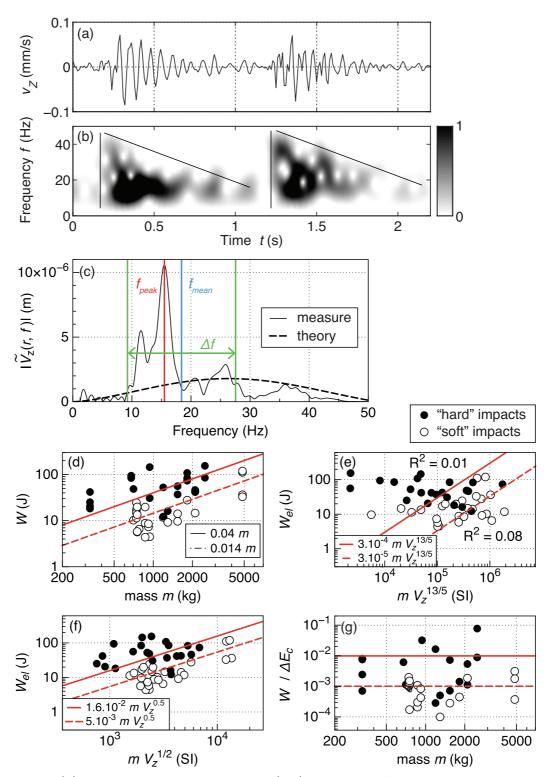
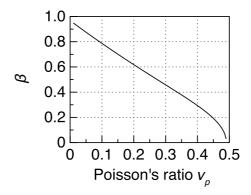


Figure 16. (a) Vertical vibration speed  $v_z(r,t)$  generated by two successive impacts of a boulder of mass m = 326 kg on the rock slope. (b) Spectrogram of the signal in (a). Darker shape represents higher energy (normalized). The black lines highlight the triangular shape of the spectrograms. (c) Amplitude spectrum  $|\tilde{V}_z(r, f)|$  for the first impact, with the peak  $f_{peak}$  and **Indur**  $f_{medn}^{F}$  frequencies and the **September**  $\Delta f_{..}$ , **Dested 5n01pp** in the first spectrum computed with the convolution of Hertz [1882]'s force of elastic impact with the Green's function of Rayleigh waves. (d) to (f) Radiated elastic energy  $W_{el}$  for different boulders documented in Tahiti as a function of (d) the mass m and of parameters (e)  $mV_z^{13/5}$  and (f)  $mV_z^{0.5}$ , with associated



**Figure 17.** Coefficient  $\beta$  defined by equation (A7) as a function of the Poisson ratio  $\nu_p$ .

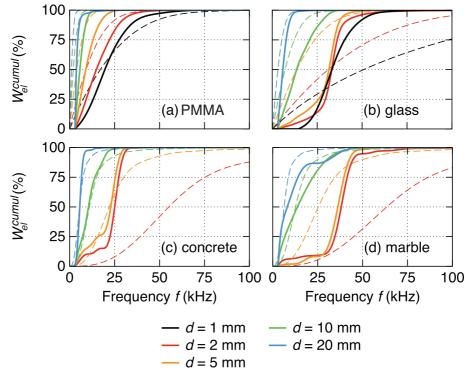


Figure 18. Cumulated radiated elastic energy  $W_{el}^{cumul}$  for the impact of steel beads of different diameters d (different colors) on (a) the PMMA plate, (b) the glass plate, (c) the concrete block and (d) the marble block, as a function of frequency f. Full line: experiments, dashed line: synthetics obtained with the convolution of the Green function with *Hertz* [1882]'s force of elastic impact.

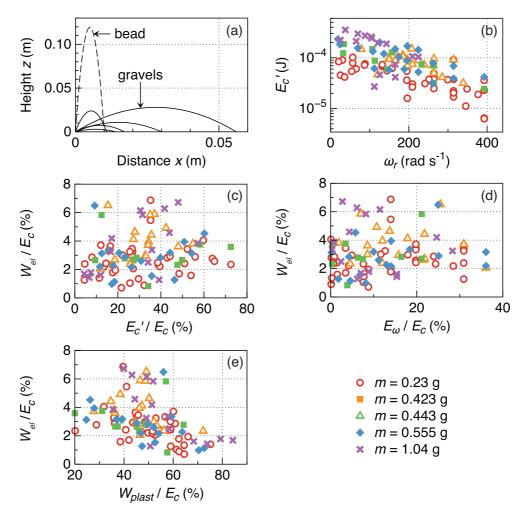


Figure 19. (a) Different rebound trajectories followed by the same gravel of mass m = 0.23g dropped from height H = 10 cm several times on the glass plate (full lines) and one rebound trajectory followed a spherical bead of diameter d = 4 mm dropped from the same height H(dashed line). Gravels of different masses m (different symbols) are dropped without initial spin from height H = 10 cm on the glass plate. (b) Translational kinetic energy  $E'_c$  of the gravels after rebound as a function of their rotation speed  $\omega_r$  after rebound. (c) to (e) Percentage of impact energy lost in elastic waves  $W_{el}/E_c$  as a function of the percentage of the impact energy  $E_c$  converted (c) in rebound translational energy  $E'_c$ , (d) in rotational energy  $E_{\omega}$  and (e) in plastic deformation  $W_{plast}$ .

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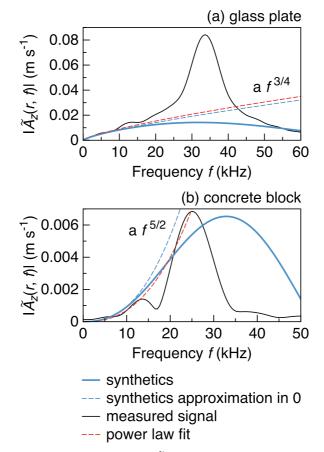


Figure 20. Measured amplitude spectrum  $|\tilde{A}_z(r, f)|$  (black line) and synthetic spectrum (thick blue line) for the impact of a steel bead of diameter 5 mm on (a) the glass plate and (b) the concrete block. The blue dashed line is the power law approximation for low frequencies of the synthetic spectrum. The red dashed line is an adjustment of the low frequencies content of the measured spectrum with the power law.