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# **Currency Total Return Swaps: Valuation and Risk Factor Analysis**

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# **Abstract:**

Currency total return swaps (CTRS) are hybrid derivatives instruments that allow to simultaneously hedge against credit and currency risks. We develop a structural credit risk model to evaluate CTRS premia. Empirical test on a sample of 23,005 price observations from 59 underlying issuers yields an average percentage error of around 10%. This indicates that, beyond interest rate risk, firm-specific factors are major drivers of the variations in the valuation of these instruments. Regression analysis of residuals shows that exchange rate determinants account for up to 40% of model pricing errors – indicating that a currency risk premium affects the CTRS price significantly but only marginally, which confirms the prevalence of credit risk in the pricing of CTRS.

**Keywords:** Credit derivative, credit risk, currency risk

**JEL Classification:** G13, G15, G32

Financial innovation allows investors to trade on new products, thereby exchanging more accurate information on how to determine the equilibrium reward for exposure to various types of risks. Unlike bonds, whose observed price can be contaminated by supply and demand liquidity effects, the simple structure of symmetric financial derivatives such as futures and plain vanilla swaps provides the possibility to identify the fundamental drivers of their marked-to-market valuations. When the swap contract involves several very distinct sources of risk, the analysis can become more complex but remains valuable. In particular, it can shed light on the relative importance of the distinct sources of risk in the determination of market prices. For instance, with a contract that would involve interest rate and currency risk only, an adequate hedging strategy requires identifying the extent to which price fluctuations are only due to interest rate movements versus those that can be attributed to currency-specific risk factors.

In this paper, we study a recent kind of credit derivative involving cash flows denominated in different currencies. A Currency Total Return Swap (CTRS) is an overthe-counter credit derivative in which the buyer pays a floating return on the principal amount of the reference obligation denominated in foreign currency, while the seller pays a floating return on the principal amount denominated in domestic currency. Entering into a CTRS contract therefore allows to simultaneously hedge against default and currency risks. Naturally, the credit risk of the underlying bond instrument drives a large proportion of price fluctuations of such a product, but it is necessary to identify its role through an adequate valuation scheme. For this purpose, our first aim is to derive the analytical pricing of the CTRS and identify the mechanisms through which it is impacted by credit and currency risks.

By construction, CTRS should be more exposed to foreign exchange risk than any other credit derivative as its cash flows directly involve different currencies. Our second and main objective is thus to investigate the extent to which the pricing of this type of credit derivative is affected by currency risk. This contributes to a relatively scarce empirical literature linking credit derivatives valuation with foreign exchange conditions. Skinner and Townend (2002) and Skinner and Diaz (2003) show that the 1998 Asian currency crisis only impacted the prices of credit default swaps (CDS) that were written on Asia-located entities. However, they reject the idea that currency risk might have increased the exposure to default risk. Rather, they attribute the increase in Asian CDS premia to a moral hazard problem based on underestimating the likelihood of issuer's restructuring as a credit event. Carr and Wu (2007) work on Brazilian and Mexican evidence to document that sovereign credit default swaps are affected by currency risk. Zhang *et al.* (2010) establish Granger causality between some CDS indices and exchange rates with the U.S. dollar, but most of their results lose their significance when it comes to the exchange rate with the Euro.

The literature is therefore mixed as to whether credit derivatives are significantly impacted by currency risk, mostly because its impact on the plain vanilla CDS instrument cannot be precisely determined. With our approach, we can quantify very precisely the potential currency exposure by removing the whole impact of idiosyncratic credit risk from the CTRS price. Also, in order to avoid potential contamination from sovereign risk, our work focuses on developed economies as our sample CTRS are written on EMU and UK firms and involve U.S. dollar denominated cash flows. We can attribute most of the residual variation in CTRS prices to currency risk.

Our results shed new light on the pricing of credit derivatives in general, and CTRS in particular. The interest rate and credit risk components explains more than 80% of the variance of CTRS prices in our model Only a small residual fraction, lower

than 10%, results from currency-specific risk factors. As we get very little unexplained variance in prices, our empirical evidence tends to confirm that pure foreign exchange risk has little influence on the price of credit derivatives beyond the impact of sovereign default risk.

The rest of the paper is structured as follows. In the next section we present the valuation framework for CTRS. Implementation of the model to the sample data is detailed in section 3. In section 4 we perform a risk factor analysis that allows to gauge the relative importance of credit and currency risks on CTRS premia. Section 5 concludes. Technical proofs are gathered in the appendix.

The payoffs involved in a CTRS contract are represented in Figure 1.

#### Insert Figure 1 here

Party B in Figure 1 swaps the cash flows received from foreign Libor net of the CTRS premium against the cash flows received from foreign Libor and converted into domestic currency.

### 2.1 Assumptions

Financial markets In the foreign and domestic economies, assets are continuously traded in arbitrage-free and complete markets. Following Amin and Jarrow (1991), the traded in arbitrage-free and complete markets. Following Amin and Jarrow (1991), the unique domestic risk-neutral probability measure  $\mathbb{Q}_d$  is defined such that all discounted unique domestic risk-neutral probability measure  $\mathbb{Q}_d$  is defined such that all discounted<br>traded assets denominated in domestic currency are martingales under  $\mathbb{Q}_d$ . The foreign traded assets denominated in domestic currency are martingales under  $\mathbb{Q}_d$ . The foreign risk-neutral probability measure  $\mathbb{Q}_f$  is defined similarly for the foreign economy.

Foreign and domestic term structures The instantaneous domestic (foreign) riskfree interest rate follows an Ornstein-Uhlenbeck process under  $\mathbb{Q}_d$  ( $\mathbb{Q}_f$ ), that is

$$
dr_{kt} = \alpha_k (\beta_k - r_{kt}) dt + \sigma_k dW_{kt}^k, \quad k \in \{d, f\},
$$

Foreign and domestic term structures The instantaneous domestic (foreign) risk-<br>Foreignes multiplies an Omeioin Dibeniae's process under Q<sub>n</sub> (Q<sub>p</sub>), the is<br> $d\alpha_1 = \alpha_1(\beta_2 - \pi_1)d + \sigma_1d\alpha_2^2a - k \in [d_1f]$ , where  $\beta_3$  repr where  $\mu_X$  represent value of the long-term equilibrium value of the process,  $W_{\text{eff}}^* \geq 0$  is a<br>standard Wiener process under  $Q_X$  is the interest rate value<br>littly. The process  $(W_{\text{eff}}^* \geq 0)$  is a<br>standard Wiener reversion speed and  $\sigma_k$  is the interest rate volatility. The process (<br>standard Wiener process under  $\mathbb{Q}_k$  representing interest rate uncertain<br>denotes domestic (d) or foreign (f) economy. Vasicak (1977) shows that<br>  $W_{kt}, t \geq 0$  reversion speed and  $\sigma_v$  is the interest rate volatility. The process  $\langle W_{k\ell}^k, t\geq 0 \rangle$  is a<br>tandard Wiener process under  $Q_k$  representing interest rate uncertainty. Subscript k<br>denotes domestic  $(d)$  or foreign  $(f)$ standard Wiener process under  $\mathbb{Q}_k$  representing interest rate uncertainty. Subscript  $k$ denotes domestic  $(d)$  or foreign  $(f)$  economy. Vasicek (1977) shows that the time-*t* va<br>for the riskless zero-coupon bond with one monetary unit due at time *T* is given by

$$
P_k(t,T) = a_k(\tau) \exp(-b_k(\tau) r_{kt}), \quad k \in \{d, f\},\
$$

with

$$
a_k(\tau) = \exp\left(\frac{(b_k(\tau) - \tau)(\alpha_k^2 \beta_k - \sigma_k^2/2)}{\alpha_k^2} - \frac{\sigma_k^2 b_k^2(\tau)}{4\alpha_k}\right),
$$
  
\n
$$
b_k(\tau) = \frac{1 - \exp(-\alpha_k \tau)}{\alpha_k},
$$
  
\n
$$
\tau = T - t.
$$

− *t*.<br>3 U  $\overline{C}$ fusion, *i.e.* 

$$
\frac{d1/S_t}{1/S_t} = (r_{ft} - r_{dt}) dt - \sigma_s dW_{st}^f
$$

the set of  $k$  alue  $y$  and  $\text{dist.}$ Exeriange rate dynamics Under  $\psi_f$  the exchange rate  $\frac{d1}{S_t}$ <br>fusion, *i.e.*<br> $\frac{d1}{S_t} = (r_{ft} - r_{dt}) dt - \sigma_s dW_{st}^f$ <br>where  $\sigma_s$  is the constant volatility of the returns of the e:<br>is the stochastic process representing th where  $\sigma_s$ <br>is the stoc $\left(W_{st}^f, t \geq 0\right)$ <br>Alternative where  $\sigma_s$  is the constant volatility of the returns of the exchange rate,  $(r_{dt}, t \ge 0)$ <br>is the stochastic process representing the instantaneous domestic risk-free rate, and where  $\sigma_s$  is the constant volatility of the returns of the exchange rate,  $(r_{dt}, t \ge 0)$ <br>is the stochastic process representing the instantaneous domestic risk-free rate, and<br> $\left(W_{st}^f, t \ge 0\right)$  is a standard Wiener proce  $\left(W_{st}^f, t \ge 0\right)$  is a standard Wiener process under  $\mathbb{Q}_f$  accounting for the exchange risk.<br>Alternatively, under  $\mathbb{Q}_d$  we have<br> $\frac{dS_t}{S_t} = (r_{dt} - r_{ft}) dt + \sigma_s dW_{st}^d$ <br>where  $\left(W_{st}^d, t \ge 0\right)$  is a standard Wiener  $\mathbb{R}^2$  $W_{st}^j, t \geq 0$ -) is a standard Wiener process under  $\mathbb{Q}_f$  accounting for the exchange risk. Alternatively, under  $\mathbb{Q}_d$  we have

$$
\frac{dS_t}{S_t} = (r_{dt} - r_{ft}) dt + \sigma_s dW_{st}^d
$$
  
hard Wiener process under  $\mathbb{Q}_d$   
6

where  $\left(W_{st}^{d}, t \geq 0\right)$  is a standard Wiener process under  $Q_d$ .

Assets of bond issuer The foreign firm capital structure is comprised of equity nont loss of generality, the face value of debt is normalized<br>ratio, denoted by  $V$ , follows a lognormal diffusion process<br> $\frac{dV_i}{V_i} = r_f dt + \sigma_i dW_{ci}^f$ <br>thatility of returns, and  $(W_{ci}^f, t \ge 0)$  is a standard Wiener<br>ig for outstanding and debt. Without loss of generality, the face value of debt is normalized to 1, and the asset-to-debt ratio, denoted by  $V$ , follows a lognormal diffusion process under  $\mathbb{Q}_f$ 

$$
\frac{dV_t}{V_t} = r_{ft}dt + \sigma_v dW_{vt}^f
$$

-

to 1, and the associeted<br>check ratio, denoted by  $V$ , follows a lognorized diffusion process<br>under Q:<br> $\frac{\partial V_2}{V_3} = r_I dt + \sigma_p dW_{13}^2$ <br>where  $\sigma_s$  is the constant volatility of returns, and<br> $\left(W_{21}^I, t\geq 0\right)$  is a standa under Q<sub>I</sub><br>  $\frac{\partial V_1}{V_1} = r_f \omega t + \sigma_s \omega t V_{1s}^t$ <br>
where  $\sigma_s$  is the constant wishing of refurres, and  $\left(W_{2s}^t, t \ge 0\right)$  is a standard Wiener<br>
process under Q<sub>I</sub> seconding for the hustness risk of the furth. We denote by where  $\sigma_v$ <br>process v<br>correlatic<br>Default<br>first hitti<br>where  $T$ <br>(1997), tl<br>the risk-f<br>where  $\lambda$  s<br>to leave t<br>**Recover**<br>and the r<br>2.2 C. where  $\sigma_v$  is the constant volatility of returns, and  $\left\{\right.$ <br>
reprocess under  $\mathbb{Q}_f$  accounting for the business risk coorrelation coefficient between  $\left(W'_{xi}, t \ge 0\right)$  and  $\left(W'_{f}$ <br> **Default rule** The default boun  $W_{vt}^j, t \geq 0$ is a standard Wiener process under  $\mathbb{Q}_f$  accounting for the business risk of the firm. We denote by  $\rho$  the  $W_{vt}^j, t \geq 0$  $\Big)$  and  $\Big($  $\left(W_{ft}^f, t \geq 0\right)$ J.

correlation coefficient between  $(W_{vt}^t, t \ge 0)$  and  $(W_{ft}^t, t \ge 0)$ .<br>Default rule The default boundary is denoted by  $H_t$  and the default occurs at the **Default rule** The default  $\frac{1}{1}$  first hitting time  $\theta$  defined as The default boundary is denoted by  $H_t$  and the default occurs at the

$$
\theta = \inf \left\{ t \leq T : V_t = H_t \right\},\
$$

accounting for the business risk of the firm. We denote by *p* intimated business risk of the firm. We denote by *p* intimated business for  $W_{tt}^t$  ( $\geq 0$ ) and  $(W_{tt}^t, t \geq 0)$ .<br>
in between  $\{W_{tt}^t \geq T : V_t = H_t\}$ ,<br>
or correlation coefficient between (<br>
Default rule The default bou<br>
first hitting time  $\theta$  defined as<br>  $\theta$ <br>
where T stands for the CTRS<br>
(1997), the default boundary has<br>
the risk-free (foreign) zero-coupe<br>
where  $\lambda < 1$  i  $\theta=\inf\left\{t\leq T: V_t=H_t\right\},$ e $T$  stands for the CTRS contract maturity. Following Briys and de Varenne where  $T$  stands for the CTRS contract maturity. Following Briys and de Varenne  $(1997)$ , the default boundary has an exponential the risk-free (foreign) zero-coupon bond, that is, the risk-free (foreign) zero-coupon bond, that is,

$$
H_t = \lambda P_f\left(t, T\right),
$$

 $H_t = \lambda \, P_f\left(t,T\right)\,,$ e $\lambda < 1$  is a constant representing the critical value below which shareholders decide where  $\lambda < 1$  is a constant repr<br>to leave the firm to creditors. to leave the firm to creditors.

to leave the firm to creditors.<br>Recovery rule Debtholders recover only a fraction  $\epsilon < 1$  of the assets upon default **Recovery rule** Debtholders reand the recovery rate is thus  $\epsilon \lambda$ .

### 2.2 CTRS premium

The floating rate coupon is the yield of the equivalent riskless bond, that is,

$$
Y_f(t_i, t_{i+1}) = -\frac{1}{t_{i+1} - t_i} \ln P_f(t_i, t_{i+1}),
$$

at dates  $t_i$ ,  $i = 1, ..., n$ , which yields

$$
Y_f(t_i, t_{i+1}) = \frac{b_f(t_{i+1} - t_i) r_{ft_i} - \ln a_f(t_{i+1} - t_i)}{t_{i+1} - t_i}
$$

 $\frac{-v_i + r_{ti} - \ln a_f (v_{i+1} - v_i)}{t_{i+1} - t_i}$ <br>ncy at time t is denoted L<br>time T.  $\frac{1}{t}$ <br>ne t Debt value denominated in foreign currency at time t is denoted  $D_f(t)$ . The CTRS is issued at a fixing date  $t_0$  and matures at time  $T$ .

According to the set of assumptions presented above, the no-arbitrage value for the CTRS contract is given by the following proposition (all proofs are reported in the appendix).

**Proposition 1** The premium of the CTRS denoted by  $p_{CTRS}$  satisfies

$$
p_{CTRS} = \frac{F_d(t_0, T) - D_f(t_0)}{\sum_{i=1}^n P_d(t_0, t_i)}
$$

where  $D_f$  (t<sub>0</sub>) is the current value of the reference obligation and

$$
F_d(t_0, T) = \sum_{i=1}^n P_d(t_0, t_i) y_d(t_i, t_{i+1}) + P_d(t_0, T),
$$
  
\n
$$
y_d(t_i, t_{i+1}) = \frac{b_d(t_{i+1} - t_i)}{t_{i+1} - t_i} \left[ (r_d - \beta_d) e^{-\alpha_d t_i} + \beta_d - \frac{\sigma_d^2}{2\alpha_d^2} (1 - e^{-\alpha_d t_i})^2 \right] - \frac{\ln a_d(t_{i+1} - t_i)}{t_{i+1} - t_i}
$$

 $-\frac{t_i}{t_i}$ <br>prov  $\left[\left(r_d - \beta_d\right)e^{-\alpha_d t_i} + \beta_d - \frac{\partial_d}{2\alpha_d^2} \left(1 - e^{-\alpha_d t_i}\right)^2\right] - \frac{\ln a_d \left(t_{i+1} - t_i\right)}{t_{i+1} - t_i}$ <br>
n provides with the no-arbitrage value for the reference obligation<br>
RS valuation.

**Proposition 2** The current value of the reference obligation satisfies

*where D<sub>f</sub>* (a<sub>0</sub>) is the current state of the reference conjugation and  
\n
$$
F_d(t_0, T) = \sum_{i=1}^{n} P_d(t_0, t_i) y_d(t_i, t_{i+1}) + P_d(t_0, T),
$$
\n
$$
y_d(t_i, t_{i+1}) = \frac{b_d(t_{i+1} - t_i)}{t_{i+1} - t_i} \left[ (r_d - \beta_d) e^{-\alpha_d t_i} + \beta_d - \frac{\sigma_d^2}{2\alpha_d^2} (1 - e^{-\alpha_d t_i})^2 \right] - \frac{\ln a_d(t_{i+1} - t_i)}{t_{i+1} - t_i}
$$
\nThe next proposition provides with the no-arbitrage value for the reference obligation and completes the CTRS valuation.  
\nProposition 2 The current value of the reference obligation satisfies  
\n
$$
D_f(t_0) = P_f(t_0, T) \left[ \Phi(z_1^T) - \frac{V}{\lambda} \Phi(-z_1^T) \right]
$$
\n
$$
+ \epsilon \lambda P_f(t_0, T) \left[ \Phi(-z_2^T) + \frac{V}{\lambda} \Phi(-z_1^T) \right]
$$
\n
$$
+ \sum_{i=1}^{n} y_f(t_i, t_{i+1}) P_f(t_0, t_i) \left[ \Phi(z_2^{t_i}) - \frac{V}{\lambda} \Phi(-z_1^{t_i}) \right],
$$
\nwith  
\n
$$
z_1^{t_i} = \frac{\ln \left( \frac{V}{\lambda P(t_0, T)} \right)}{s(t_0, t_i)} + \frac{s(t_0, t_i)}{2}, \quad z_2^{t_i} = z_1^{t_i} - s(t_0, t_i),
$$

,

with

$$
+\sum_{i=1}^{n} y_{f}(t_{i}, t_{i+1}) P_{f}(t_{0}, t_{i}) \phi(z_{2}^{t_{i}}) - \frac{1}{\lambda} \Phi(-z_{1})
$$
  

$$
z_{1}^{t_{i}} = \frac{\ln\left(\frac{V}{\lambda P(t_{0}, T)}\right)}{s(t_{0}, t_{i})} + \frac{s(t_{0}, t_{i})}{2}, \quad z_{2}^{t_{i}} = z_{1}^{t_{i}} - s(t_{0}, t_{i}),
$$
  

$$
8
$$

$$
s(t_0, t_i) = \sqrt{\int_{t_0}^{t_i} \left(\sigma_{P_f}^2(u, t_i) + \sigma_v^2 - 2\rho_{vf}\sigma_v\sigma_{P_f}(u, t_i)\right) du},
$$

$$
\sigma_{P_f}(t, T) = \sigma_f b_f(T - t),
$$
  
*) is defined in a similar fashion as y<sub>d</sub>*  $(t_{i-1}, t_i)$ , and  $\Phi$ 

 $- t$ ),<br>3  $y_d$  ( and  $y_f$  ( $t_i$ −1,  $t_i$ ) is defined in a similar fashion as  $y_d$  ( $t_i$ −1,  $t_i$ ), and  $\Psi$  (.) denotes the standard normal cumulative distribution function.<br>2.3 Sensitivity analysis standard normal cumulative distribution function.

### 2.3 Sensitivity analysis

Table 1 reports the CTRS premium statics for various levels of leverage.

#### Insert Table 1 here

The CTRS premium (reported in basis points) decreases more than exponentially with the asset-to-debt ratio. By contract construction, it displays little sensitivity to domestic interest rate parameters (which only interfere in the discounting of cash flows), but it is significantly affected by the foreign term structure level and slope (which interfere in the determination of cash flows). As expected, the greatest impacts on the CTRS premium stem from the underlying firm credit risk parameters, namely the assetto-debt ratio and volatility as well as the default boundary. The largest sensitivities are observed for the latter two variables, but their importance varies across levels of leverage. When it is low (high asset value  $V$ ), the distance to default is high and the key driver of the CTRS premium is asset volatility. As leverage increases, the default threshold becomes more prevalent, because the likelihood of default increases and  $\lambda$ affects both the probability of default and the expected recovery rate.

# 3 Model implementation

We apply the pricing results obtained in Propositions 1 and 2 to get the fitted prices of a sample of CTRS contracts. This will, in turn, enable us to identify the determinants of price variations related to default, interest rate, and currency risks.

#### 3.1 Sample data

The dataset contains OTC quotations on CTRS issued by ING between September 1, 2005 and March 16, 2007. The reference obligations are written by European firms and are denominated in euro or in British pound while the bank payments are denominated in U.S. dollar. From the bank perspective, the U.S. dollar is the domestic currency and the foreign economy is the reference obligor's.

#### Insert Table 2 here

The database initially contains 125 firms, with 49,135 daily observations. We have restricted our sample to non-financial firms, incorporated in the Economic and Monetary Union (EMU) or in the U.K., and listed on the stock market. The final sample contains 59 firms (listed in Table 2) and 23,005 daily observations.

#### Insert Table 3 here

Table 3 reports the descriptive statistics for the CTRS premia and their breakdown across ratings and currencies. As expected, CTRS premia increase in level and become more volatile as the credit rating deteriorates. U.K. firms tend to have lower premia than the EMU ones, but the difference is not significant.

#### 3.2 Estimation procedure

Interest rate parameters Parameters for the interest rate processes are estimated using the extended Kalman filter technique as in Duffee (1999) and Duan and Simonato (1999). Yield curves are collected on a weekly basis (Wednesday observation) with seven different maturities (3 and 6 months, 1, 2, 5, 10 and 20 years). Data for the U.S. rates

are the Constant Maturity Treasury yields from the Federal Reserve of St-Louis. U.K. rates are obtained from the Bank of England, except for the 3 and 6 months maturity which are LIBOR rates. EMU rates are a composite index of French and German rates provided by Bloomberg. This index is well suited with our data since a majority of our sample firms (27 out of 44) are incorporated either in France or in Germany. Results for the Kalman filter estimations are reported in Table 4. Figure 2 provides with a visual inspection of the fit.

#### Insert Table 4 here

#### Insert Figure 2 here

Firm characteristics Parameters V and  $\sigma_v$  are obtained using a method which is similar to Vassalou and Xing (2004)'s iterative procedure. Specifically, we first use the theoretical CDS premium formula to infer a series of  $V$  that is consistent with the observed quotations (5-year maturity CDS premia are obtained from Datastream). Then,  $\sigma_v$  is computed as the standard deviation of the returns on the inferred asset-todebt ratios and  $\rho$  is the correlation coefficient between these returns and the risk-free interest rate. Using this series of V and the computed  $\sigma_v$  and  $\rho$ , parameter  $\lambda$  is calibrated to minimize the squared errors of the theoretical model. This procedure is iterated until minimization of the squared errors. Results are reported in Table 5.

#### Insert Table 5 here

Because the model is using the asset-to-debt ratio (and not assets) as state variable, the estimated volatility levels are relatively lower (4.7% on average for EMU firms). On the other hand, the distance to default (defined as the ratio  $V/H_0$ ) is smaller (1.25 on average for EMU firms). The asset-to-ratio is estimated at 1.97 on average for EMU firms, which corresponds to a leverage ratio of one third — in line with empirical studies on leverage (see e.g. Fan, Titman and Twite, 2010). As expected, correlation between asset-to-debt ratio and risk-free rate is slightly negative.

We use the following recovery rates obtained from Moody's report (Hamilton and Varma, 2006) for the period under study: 57.04%, 49.54% and 45.48% for Aa, A and Baa ratings, respectively.

#### 3.3 Model performance

In tables 6 and 7 we report the in-sample performance of the model. The pricing error is defined as the difference between the theoretical and observed premia. Since the model developed in section 2 essentially captures credit risk, its pricing performance provides a good indication about the relative importance of other sources of risk on CTRS premia.

> Insert Table 6 here Insert Table 7 here

Overall the model tends to slightly undervalue CTRS premia, with a mean error of almost 4 basis points (corresponding to a 11% proportional error). In absolute terms, the RMSE is 5.64% (i.e. 17.35% in proportion). Table 6 shows that the model undervalues CTRS labelled in euro and overvalues those labelled in British pound. This indicates that an exchange risk factor might be missing in the pricing of CTRS. Table 7 shows that the undervaluation slightly increases with the lower ratings, but not when measured by the RMSPE (i.e. the absolute error in proportion).

#### Insert Figure 3 here

Figure 3 plots the time series of theoretical and observed CTRS premia for a subsample of 6 firms (from all rating categories and both currencies). It visually confirms the undervaluation (resp. overvaluation) of CTRS written on EMU (resp. U.K.) firms.

It also illustrates that the pricing error does not appear to be clustered in a particular subperiod. Similar patterns are found for the rest of sample firms (results available upon request).

The next section first investigates the behavior of the credit risk premium relative to the classical credit risk factors. Secondly, we study the residual in order to uncover the presence of an exchange and a liquidity components in the premia that is not captured by the pricing model.

## 4 Risk factor analysis

#### 4.1 Credit risk premium

The aim of this subsection is to confirm that the model is indeed capturing a credit risk premium. According to structural models of credit risk, the credit risk premium should be driven by three important factors: leverage, asset volatility and the risk-free rate. We closely follow the methodology of Ericsson  $et$  al. (2009) and perform the following regression on theoretical CTRS premia

$$
p_{CTRS}(i, t) = \alpha_i + \beta_i^l LEV_{i,t} + \beta_i^v VOL_{i,t} + \beta_i^r r_t + \epsilon_{i,t}
$$

where  $p_{CTRS}(i, t)$  is the theoretical CTRS premium of firm i at time t,  $\alpha_i$  a constant,  $LEV_{i,t}$  the financial leverage,  $VOL_{i,t}$  the asset volatility and  $r_t$  the risk-free rate.

Leverage is proxied by the ratio: book value of debt  $/$  (book value of debt  $+$  market value of equity). Balance sheet data are retrieved from Mergent Online. Asset volatility is proxied by the historical volatility of stock returns, computed from a 250 trading days rolling window. The risk-free rate is proxied by the one-year Libor rate.

Insert Table 8 here

Results are reported in table 8. Estimation is performed for each firm separately, and the reported coefficients are averages across firms coefficients.<sup>1</sup> Following Collinand the reported coefficients are averages across firms coefficients are averages across firms coefficients are computed as follows

$$
\frac{\overline{\beta}\sqrt{N}}{\sigma_{\beta}},
$$

 $\frac{\rho_{\mathbf{V}}}{\sigma_{\beta}},$ e  $\overline{\beta}$  is the mean coefficient for each explanatory variable,  $\sigma_{\beta}$  stands for the standard where  $\overline{\beta}$  is the mean coefficient for each explanatory variable,<br>deviation of these coefficients, and N is the number of firms. deviation of these coefficients, and  $N$  is the number of firms.

Overall the three variables have a high explanatory power on CTRS premia, with an Overall the three variables have a high explanatory power on CTRS premia, with an adjusted  $R^2$  ranging from 60% to 85% depending on rating category – figures comparable adjusted  $R^2$  ranging from 60% to 85% depending on rating category – figures comparable<br>to the ones obtained in Ericsson *et al.* (2009). Financial leverage is globally significant at to the ones obtained in Ericsson *et al.* (2009). Financial leverage is globally significant at the 1% confidence level and has the expected sign. This result is mainly driven by lower<br>rated (Baa) firms. Leverage is only significant for the EMU firms, but the t-statistic for the UK firms is at 1.64, extremely close to the 10% level. Volatility coefficients have the right sign but they are never significantly different from zero at any usual level. This is probably explained by the low variation in the volatility estimates used to compute the premia across the firms. The risk-free rate has the expected negative effect on the premia, and every coefficient is highly significant at the 1% level, whatever the currency or the rating. These regression results confirm that the theoretical model seems to adequately capture the credit risk component in the CTRS premia. The breakdown by credit rating appears to bring higher significance levels. This indicates that the main source of heterogeneity is likely to be found in credit qualities, which suggests that credit risk is the major driver of CTRS prices.

 $^{\rm 1}$  Note that there are 300 more observations than in the dataset, which correspond to missing observed premia that have been interpolated in order to reach a balanced sample. Their exclusion does not alter the estimates.

#### 4.2 Analysis of pricing errors

The theoretical model implies that there is no currency risk component in the CTRS premium. In this section, we investigate the extent to which the CTRS premium effectively contains a currency risk premium. The analysis is performed on the pricing error of the model. The rationale is that the model should have extracted all the credit component, leaving only liquidity effects and a random noise. To test this hypothesis, we regress the pricing error with most of the usual explanatory factors of the exchange rate. The factors are defined as the difference between the domestic and the foreign variables. In order to obtain comparable variables in the two economies, we standardize each variable before computing the difference. Consistently, the pricing error is also standardized. In the absence of a currency risk premium, none of these factors should be significant. The following regressors are used:

The exchange rate volatility If FX risk is priced, then the level of the risk The exchange rate volatility If FX risk is priced, then the level of the risk<br>mium should be related to exchange rate volatility. Nevertheless, since the volatility<br>he USD-GBP or the USD-EUR exchange rate is positively rel premium should be related to exchange rate volatility. Nevertheless, since the volatility of the USD-GBP or the USD-EUR exchange rate is positively related to the volatility of the inverse exchange rate, the sign of the risk premium depends on the domestic currency of the purchaser of the contract. A negative sign would correspond to a dominance of U.K. or Eurozone purchasers, respectively, while a positive sign would be consistent with a larger share of the contracts held in majority by U.S. parties.

The nominal interest rates of the two economies The interest parity theory The nominal interest rates of the two economies The interest parity theory<br>vulates a relation between the interest rates differential and the exchange rate. Thus<br>expect them to have a possible effect on the residual. The d stipulates a relation between the interest rates differential and the exchange rate. Thus we expect them to have a possible effect on the residual. The data used are the 1-year Libor rates.

The price level and the inflation in the two economies The data used are the rate of variation of the monthly Harmonized Index of Consumer Prices from Eurostat for the EMU and U.K. economies and the Consumer Price Index from the Bureau of Labour Statistics for the U.S. economy.

**Money supply** Data are taken from Eurostat for the European economies and from the FED of St-Louis for the U.S. We use the monetary aggregate M2. Macroeconomic data have been linearly interpolated in order to have daily observations.

The price level and the inflation in the two economies . The data used are the of variation of the montaly line<br>moise and the convergence of consumer Price fields from European constrained<br>and the EMU ad UK. consider and Money supply Data are taken from Eurotetat for the European economies and<br>the FED of SI-Lovis for the U.S. We use the monetary aggregate M2. Macrosco-<br>include taken from Euroscopy interpolated in order to have daily obser We also include GDP and the stock market index as control variables to account for the business cycle. GDP data are obtained from Eurostat and the FED websites. The stock market indices are the S&P 500, the Euronext 50 and the FTSE 100. As far as a liquidity variable is concerned, the bid-ask spread on the CTRS premia being unavailable, we include the bid-ask spread on CDS quotations. The underlying working assumption is that demand for CTRS is closely correlated with demand for CDS or, put simply, that the most traded CDS should also be the most traded CTRS.

#### Insert Table 9 here

Table 9 reports the collinearity diagnosis. Correlation levels among explanatory variables are moderate, except maybe for GDP and the stock market index in the British economy. We compute the Variance Inflation Factor for each regressor and find that none of them exceeds  $5 -$  which a commonly accepted criterion for rejecting multicollinearity issues in the regression analysis.

Regressions are performed for each firm separately, one including all the currency risk regressors, one adding the liquidity risk. We also run univariate regressions.

Insert Table 10 to 12 here

Tables 10 to 12 present the coefficients and their respective t-stats for the whole sample and for each currency zone. For the whole sample (Table 10), almost all the factors, with the exception of GDP, are significant at the 1% level, and have the expected sign. When combined together, only inflation and exchange rate volatility lose their significance. Currency risk factors account for 37% of total variance of the pricing error, and the residual pricing error, represented by the constant, does not appear to drift away from zero. Interestingly, the liquidity factor (as we proxy it using CDS bid-ask spread) does not contribute much to explaining pricing errors, as the adjusted R-square marginally increases by one or two percentage points as we include this variable.

Evidence presented in Tables 11 (EMU) and 12 (U.K.) confirm the contribution of each variable to the overall explanation of pricing errors. The significance level of the multiple regression reaches 34 % for EMU firms and 46% for U.K. firms. The major source of the difference between both sub-samples is the role of the exchange rate volatility factor. For EMU firms, it is negative in the single factor regression but switches signs in the multiple one, and becomes weakly significant. We cannot infer any meaningful evidence about the currency risk premium from these results. For the U.K. sample however, there is a strong and robust negative relation between CTRS prices and FX volatility. Such a finding suggests that domestic U.K. investors are in majority long these contracts, inducing the negative sign of the corresponding currency risk premium. The small significance of the EMU premium could be explained by the nationality of the originator (ING) in the CTRS sample, which is primarily active in the EMU zone and thus mitigates the currency premium effect for these contracts, even though such an explanation warrants further investigation.

Overall, these results point to the presence of a currency risk premium, which accounts for a proportion that ranges from one third to one half of the variance in our model pricing errors. However, the pricing model proposed in Section 2, which reflects default and interest rate risk characteristics, makes an 11% proportional error on observed CTRS premia. Therefore, even though the explanatory power is satisfactory and confirms the influence of FX risk on the valuation of these contracts, we conclude that the contribution of a currency risk factor to the total premium is relatively marginal.

# 5 Conclusion

The interaction between default and currency risks is a topic that does not lend itself to an easy analysis. Through this paper, we have made a direct investigation of the relative influence of these two types of risks on the pricing behavior of derivatives that explicitly bear them, namely the CTRS. As a necessary step towards this end, we proposed a pricing approach of this hybrid contract based on the state-of-the-art literature on structural analysis of credit risk derivatives.

The performance of our pricing model, which is the first one that has been developed for such instrument, has been tested on a proprietary and important sample of CTRS data. Our first conclusion is related to the quality of the pricing approach. Even though the asset volatility was indirectly estimated using stock market data, and despite the fact that the CTRS quotes can be contaminated by liquidity issues, the valuation performance of the structural model is more than decent. Such a result, which holds independently of the factors affecting the time variations in the exchange rate risk premium, sheds light on the prevalence of default risk characteristics, mainly at the firm-specific level, over broad macroeconomic risk factors as drivers of a mixed credit-currency derivative.

Our empirical investigation of the determinants of the pricing error has confirmed our initial view. The factors affecting currency risk all have a significant influence on the residual variations of CTRS prices, but this influence is marginal compared to the default component. Thus, after considering a large set of potential drivers of CTRS price variations, we reach quite conclusive evidence that the explained part of the variance is very large when all factors are combined, but this type of contract clearly belongs to the class of credit risk instruments.

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# Appendix

# Proof of proposition 1

Holding a CTRS and the reference obligation is equivalent to a riskless bond. Thus, the CTRS premium verifies

$$
0 = -p_{CTRS} \sum_{i=1}^{n} E_{\mathbb{Q}_f} \left[ \exp \left( - \int_{t_0}^{t_i} r_{fu} du \right) \cdot \frac{S_{t_0}}{S_{t_i}} \right]
$$
  
+ 
$$
\sum_{i=1}^{n} E_{\mathbb{Q}_f} \left[ \exp \left( - \int_{t_0}^{t_i} r_{fu} du \right) \cdot \frac{S_{t_0}}{S_{t_i}} \cdot Y_d(t_i, t_{i+1}) \right]
$$
  
+ 
$$
E_{\mathbb{Q}_f} \left[ \exp \left( - \int_{t_0}^{T} r_{fu} du \right) \cdot \frac{S_{t_0}}{S_{t_i}} \right]
$$
  
- 
$$
D_f(t_0)
$$
  
e following change of probability measure

Introducing the following change of probability measure

$$
\frac{dQ_d}{dQ_f} = \frac{S_{t_0}}{S_t} \exp\left(\int_{t_0}^t (r_{du} - r_{fu}) du\right)
$$
  
=  $\exp\left(-\int_{t_0}^t \frac{\sigma_s^2}{2} du - \int_{t_0}^t \sigma_s dW_{su}^f\right),$ 

we get

$$
\frac{dQ_d}{dQ_f} = \frac{S_{t_0}}{S_t} \exp\left(\int_{t_0}^t (r_{du} - r_{fu}) du\right)
$$
\n
$$
= \exp\left(-\int_{t_0}^t \frac{\sigma_s^2}{2} du - \int_{t_0}^t \sigma_s dW_{su}^f\right),
$$
\nwe get\n
$$
E_{Q_f} \left[\exp\left(-\int_{t_0}^{t_i} r_{fu} du\right) \cdot \frac{S_{t_0}}{S_{t_i}}\right] = E_{Q_d} \left[\exp\left(-\int_{t_0}^{t_i} r_{du} du\right)\right] = P_d(t_0, t_i)
$$
\n
$$
E_{Q_f} \left[\exp\left(-\int_{t_0}^{t_i} r_{fu} du\right) \cdot \frac{S_{t_0}}{S_{t_i}} \cdot Y_d(t_i, t_{i+1})\right] = E_{Q_d} \left[\exp\left(-\int_{t_0}^{t_i} r_{du} du\right) \cdot Y_d(t_i, t_{i+1})\right]
$$
\nUsing the domestic forward-neutral probability measure  $Q_{dt_i}$ , we can write\n
$$
E_{Q_d} \left[\exp\left(-\int_{t_0}^{t_i} r_{du} du\right) \cdot Y_d(t_i, t_{i+1})\right] = P_d(t_0, t_i) E_{Q_{dt_i}} \left[Y_d(t_i, t_{i+1})\right].
$$
\nDefine  $y_d(t_i, t_{i+1}) = E_{Q_{dt_i}} \left[Y_d(t_i, t_{i+1})\right]$ . We obtain\n
$$
y_d(t_i, t_{i+1}) = \frac{b_d(t_{i+1} - t_i) E_{Q_{dt_i}}(r_{dt_i}) - \ln a_d(t_{i+1} - t_i)}{t_{i+1} - t_i}.
$$
\nUnder the forward neutral measure, the spot rate mean equals the current instantaneous forward rate. Hence\n
$$
E_{Q_{dt_i}}(r_{dt_i}) = (r_d - \beta_d) e^{-\alpha_d t_i} + \beta_d - \frac{\sigma_d^2}{2\alpha_d^2} \left(1 - e^{-\alpha_d t_i}\right)^2.
$$

Using the domestic forward-neutral probability measure 
$$
\mathbb{Q}_{dt_i}
$$
, we can write  
\n
$$
E_{\mathbb{Q}_d} \left[ \exp \left( - \int_{t_0}^{t_i} r_{du} du \right) \cdot Y_d(t_i, t_{i+1}) \right] = P_d(t_0, t_i) E_{\mathbb{Q}_{dt_i}}[Y_d(t_i, t_{i+1})].
$$
\nDefine  $y_d(t_i, t_{i+1}) = E_{\mathbb{Q}_{dt_i}}[Y_d(t_i, t_{i+1})]$ . We obtain

$$
\begin{aligned}\n\mathbf{y}_{t_0} &= \int_{t_0}^{t_0} \left[ Y_d \left( t_i, t_{i+1} \right) \right] \quad \text{and} \quad \mathbf{y}_{dt_i} \in \mathbb{R}^n, \\
\mathbf{y}_{t_0} &= \int_{t_0}^{t_0} \left[ Y_d \left( t_i, t_{i+1} \right) \right] \quad \text{We obtain} \\
\mathbf{y}_{t_0} &= \int_{t_0}^{t_0} \left( t_i, t_{i+1} \right) \quad \text{and} \quad \mathbf{y}_{t_0} \left( t_{i+1} - t_i \right) \quad \text{and} \quad \mathbf{y}_{t_0} \left( t_{i+1} - t_i \right) \\
\mathbf{y}_{t_0} &= \int_{t_0}^{t_0} \left( t_i, t_{i+1} \right) \quad \text{and} \quad \mathbf{y}_{t_0} \left( t_{i+1} - t_i \right) \quad \text{and} \quad \mathbf{y}_{t_0} \left( t_{i+1} - t_i \right) \\
\mathbf{y}_{t_0} &= \int_{t_0}^{t_0} \left( t_i, t_{i+1} \right) \quad \text{and} \quad \mathbf{y}_{t_0} \left( t_i, t_{i+1} \right) \quad \text{and} \quad \mathbf{y}_{t
$$

Using the domestic forward-neutral probability measure  $Q_{at_i}$ , we can write<br>  $E_{\mathbb{Q}_d} \left[ \exp \left( - \int_{t_0}^{t_i} r_{du} du \right) \cdot Y_d(t_i, t_{i+1}) \right] = P_d(t_0, t_i) E_{\mathbb{Q}_{dt_i}} [Y_d(t_i, t_{i+1})$ <br>
Define  $y_d(t_i, t_{i+1}) = E_{\mathbb{Q}_{dt_i}} [Y_d(t_i, t_{i+1})]$ . We ob  $\frac{t_{i,j} - t_{i,j} - t_{i,j}}{t_{i+1} - t_i}$ <br>the spot rate mean equals the curre  $\frac{1}{2}$ <br> $\frac{1}{2}$ Under the forward neutral measure, the spot rate mean equals the current instantaneous forward rate. Hence

$$
E_{\mathbb{Q}_{dt_i}}(r_{dt_i}) = (r_d - \beta_d) e^{-\alpha_d t_i} + \beta_d - \frac{\sigma_d^2}{2\alpha_d^2} (1 - e^{-\alpha_d t_i})^2.
$$
  
22

Therefore

$$
p_{CTRS} = \frac{F_d(t_0, T) - D_f(t_0)}{\sum_{i=1}^n P_d(t_0, t_i)},
$$

with

$$
p_{CTRS} = \frac{P_d(v_0, 1) - D_f(v_0)}{\sum_{i=1}^n P_d(t_0, t_i)},
$$
  

$$
F_d(t_0, T) = \sum_{i=1}^n P_d(t_0, t_i) y_d(t_i, t_{i+1}) + P_d(t_0, T),
$$

which completes the proof.

# Proof of proposition 2

The value at inception of the reference obligation paying floating coupons is given by

$$
D_f(t_0) = \sum_{i=1}^{n} E_{\mathbb{Q}_f} \left[ \exp \left( - \int_{t_0}^{t_i} r_{fu} du \cdot Y_f(t_i, t_{i+1}) \cdot 1_{\theta > t_i} \right) \right]
$$
  
+ 
$$
E_{\mathbb{Q}_f} \left[ \exp \left( - \int_{t_0}^{T} r_{fu} du \cdot 1_{\theta > T} \right) \right]
$$
  
+ 
$$
\epsilon \lambda E_{\mathbb{Q}_f} \left[ \exp \left( - \int_{t_0}^{\theta} r_{fu} du \cdot P_f(0, T) \cdot 1_{\theta < T} \right) \right].
$$
  
 Detailed calculations for these three terms can be found, in the context of domestic bonds, in Brigs and de Varenne (1997) and in François and Hübner (2004).

−<br>−<br>− bonds, in Briys and de Varenne (1997) and in François and Hübner (2004).

# Figures



Figure 1: Currency Total Return Swap payoffs.

Figure 1: Currency Total Return Swap payons.<br>  $\epsilon$  exchange rate at time t, and  $p_{CTRS}$  is the CTRS<br>
is is payments and pays  $\epsilon \lambda$  at maturity.<br>
24  $S_t$  stands for the exchange rate at time t, and  $p_{CTRS}$  is the CTRS premia. In case of default, party A stops its payments and pays  $\epsilon \lambda$  at maturity.



U.K. yield curve

Figure 2: Observed and filtered yields for the U.S., European and British economies. Figure 2: Observed and intered yields for the U.S., European and British economies.<br>The starred lines represent the filtered yields and the continuous line the observed yields.<br>25 The starred lines represent the filtered yields and the continuous line the observed yields.



Figure 3: Time series of theoretical versus observed CTRS premia.

Figure 3: Time series of theoretical versus observed CTRS premia.<br>
stical premia are plotted with the dotted line and observed premia with the c<br>
26 Theoretical premia are plotted with the dotted line and observed premia with the continuous line.

# Tables

Asset value	$\bar{V}$	$\overline{\mathbf{3}}$	2.5	$\sqrt{2}$	$1.5\,$	$\mathbf{1}$
	$p_{CTRS}$	0.13	0.8	6.17	49.51	346.74
$\label{dil1} {\rm Dom\, estic}$	$\beta_d$	$+0.00$	$+0.003$	$+0.02$	$+0.17$	$+1.20$
interest rates		$(+0.35)$	$(+0.35)$	$(+0.35)$	$(+0.35)$	$(+0.35)$
	$\beta_d, r_d$	$+0.00$	$+0.006$	$+0.04$	$+0.35$	$+2.47$
		$(+0.71)$	$(+0.71)$	$(+0.71)$	$(+0.71)$	$(+0.71)$
	$\sigma_d$	$-0.00$	$-0.00$	$-0.00$	$-0.001$	$-0.006$
		$(-0.002)$	$(-0.002)$	$(-0.002)$	$(-0.002)$	$(-0.002)$
	$\alpha_d$	$+0.00$	$+0.00$	$+0.01$	$+0.06$	$+0.43$
		$(+0.12)$	$(+0.12)$	$(+0.12)$	$(+0.12)$	$(+0.12)$
Foreign	$\bar{\beta}_f$	$-0.02$	$-0.10$	$-0.67$	$-3.99$	$-14.23$
interest rates		$(-12.36)$	$(-12.70)$	$(-10.85)$	$(-8.06)$	$(-4.10)$
	$\beta_f, r_f$	$-0.02$	$-0.15$	$-0.99$	$-6.03$	$-22.63$
		$(-18.06)$	$(-18.65)$	$(-16.10)$	$(-12.18)$	$(-6.53)$
	$\sigma_f$	$+0.006$	$+0.01$	$+0.03$	$+0.11$	$+0.15$
		$(+4.25)$	$(+1.19)$	$(+0.50)$	$(+0.23)$	$(+0.04)$
	$\alpha_f$	$-0.005$	$-0.022$	$-0.13$	$-0.74$	$-2.52$
		$(-3.88)$	$(-2.73)$	$(-2.11)$	$(-1.50)$	$(-0.73)$
Firm	$\bar{V}$	$-0.07$	$-0.50$	$-3.47$	$-22.91$	$-105.78$
characteristics		$(-56.70)$	$(-61.62)$	$(-56.28)$	$(-46.27)$	$(-30.51)$
	$\sigma_v$	$+0.31$	$+1.40$	$+6.02$	$+20.64$	$+24.69$
		$(+240.42)$	$(+173.68)$	$(+97.47)$	$(+41.69)$	$(+7.12)$
	$\rho$	$+0.00$	$+0.002$	$+0.01$	$+0.05$	$+0.06$
		$(+0.30)$	$(+0.27)$	$(+0.18)$	$(+0.09)$	$(+0.02)$
	$\epsilon$	$-0.01$	$-0.08$	$-0.58$	$-4.48$	$-27.56$
		$(-8.10)$	$(-9.38)$	$(-9.42)$	$(-9.05)$	$(-7.95)$
	$\lambda$	$+0.18$	$+1.01$	$+5.78$	$+29.14$	$+91.36$
		$(+136.02)$	$(+125.58)$	$(+93.64)$	$(+58.86)$	$(+26.34)$

Table 1: Comparative statics of the CTRS premium.

The numbers reported are the absolute changes in the CTRS premium after a 10% change in the parameter value. In parenthesis are reported the percentage variations of the premia. Base case parameters are:  $r_d = .02$ ,  $\alpha_d = .25$ ,  $\beta_d = .04$ ,  $\sigma_d = .005$ ,  $r_f = .03$ ,  $\alpha_f = .04$ ,  $\beta_{\rm s} = .045$ ,  $\sigma_{\rm t} = .005$ ,  $\sigma_{\rm t} = .15$ ,  $\alpha_{\rm t} = .05$ ,  $\epsilon = .5$  and  $\lambda = 1$  $\beta_f = .045, \sigma_f = .005, \sigma_v = .15, \rho = .05, \epsilon = .5 \text{ and } \lambda = 1.$ 



Table 2: List of sample firms.

	Number	Number	CTRS premium				
	of firms	of observations	Mean (bps)	$\mathrm{Std}\,$ dev. $(\%)$			
Panel A: Whole sample							
Аll	59	23,005	33.89	17.97			
Aa	3	1,178	14 34	7.06			
A	27	9,665	26.30	11.63			
Baa	33	12,155	42 24	18.56			
Panel B. EMU firms							
All	44	17,273	34.64	17.93			
Aa	$\overline{2}$	790	18 23	5.09			
A	22	7,762	27.38	12 30			
Baa	24	8,710	43.12	18.83			
	Panel C: U.K. firms						
All	15	5,732	31.65	17.87			
Aа	$\mathbf{1}$	388	6.42	2.21			
A	5	1,903	21.71	6.42			
Baa	9	3,441	40.00	17.68			

Table 3: Descriptive statistics of CTRS premia.

The number of firms and observations do not add up to the total since four firms were downgraded from A to Baa during the sample period: Compagnie de Saint-Gobain, Daimler, Hellenic Telecom and Telefonica.



Panel B: Filter performance									
		U.S.			EMU		U.K.		
	Measurement	Mean		Measurement	Mean		Measurement	Mean	
	error	error	RMSE	error	error	RMSE	error	error	RMSE
Maturity	variance	(bps)	(bps)	variance	(bps)	(bps)	variance	(bps)	(bps)
3 months	14.81	$-14.45$	16.67	34.63	$-32.24$	32.52	20.21	15.3	15.57
6 months	5.20	3.26	4.61	17.68	$-15.72$	16.27	7.86	0.36	6.74
1 year	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
2 years	10.60	$-6.68$	9.27	8.74	3.29	6.54	5.93	$-0.35$	4.71
5 years	15 13	$-7.83$	14.54	15.14	$-0.88$	12.40	9.92	2.77	7.45
10 years	18.71	1.47	14.80	16.99	$-2.07$	14.14	12.98	3 4 8	10.04
20 years	20.65	25.95	26.56	20.32	$-2.55$	17.17	15.03	$-4.5$	13.2

Table 4: Kalman filter estimation of interest rates parameters.

The risk-neutral dynamics for the instantaneous spot rate are  $a r_k t = \alpha_k (\beta_k - r_k t) a t + W_{kt}$ . For each currency area, parameters are estimated using the extended Kalman filter the weekly yield curves observed between August 31  $\sigma_k dW_{kt}$ . For each currency area, parameters are estimated using the extended Kalman filter<br>on the worlds widd current because here are not always 21, 2005 and Marsh, 16,2007. In Banal on the weekly yield curves observed between August 31, 2005 and March, 16 2007. In Panel A, standard deviations of the estimates are shown in parenthesis. In Panel B, the errors are defined as the difference between the actual and the fitted rates. Measurement error variance is multiplied by  $10^4$ . Mean errors and RMSE are reported in basis points.



Table 5: Firms parameters estimates.

The dynamics of the firm asset-to-debt ratio are given by  $dV_t = r_t V_t dt + \sigma_v V_t dW_t$ . Volatil-**Table 5:** Firms parameters estimates.<br>The dynamics of the firm asset-to-debt ratio are given by  $dV_t = r_t V_t dt + \sigma_v V_t dW_t$ . Volatility  $\sigma_v$  is reported in percentage.  $H_0$  stands for the initial level of the default boundary The dynamics of the firm asset-to-debt ratio are given by  $dV_t = r_t V_t dt + \sigma_v V_t dW_t$ . Volatility  $\sigma_v$  is reported in percentage.  $H_0$  stands for the initial level of the default boundary and is defined as  $H_0 = \lambda P_f (0, T)$  with assets and the risk-free rate. Parameters have been estimated using the iterative procedure on ity  $\sigma_v$  is reported in percentage.  $H_0$  stands for<br>defined as  $H_0 = \lambda P_f (0, T)$  with  $T = 5$  years. Consects and the risk-free rate. Parameters have b CDS data between  $09/01/2005$  and  $03/16/2007$ .

Theoretical premia												
				Currency								
	AЦ				Euro			Pound				
	Average	Min	Max	Average	Min	Max	Average	Min	Max			
$p_{CTRS}$	30.95	2.80	113 31	29.58	2.80	93.59	34.98	4.09	113 31			
				Performance								
					All	Euro	Pound					
	Mean error (bps)				$-3.96$	$-6.32$	3 1 4					
		(std)			(6.13)	(4.31)	(5.25)					
		RMSE (bps)			5.64	6.33	3.57					
	$(\text{std})$				(4.64)	(4.31)	(4.97)					
			Mean proportional error $(\%)$		$-10.55$	$-18.43$	13.19					
	$(\text{std})$				(18.04)	(7.44)	(19.74)					
		RMSPE $(\%)$			1735	18.45	14.04					
	$(\text{std})$				(11.65)	(7.38)	(19.14)					
		Observations			23,005	17,273	5,732					

Table 6: Model performance: Overall and per currency.

Table 6: Model performance: Overall and per currency.<br>
Error is defined as the difference between the theoretical and observed premia. RMSE<br>
measures the pricing error in absolute terms. Proportional error is mean error di Error is defined as the difference between the theoretical and observed premia. RMSE measures the pricing error in absolute terms. Proportional error is mean error divided by observed proportional Experiment (RMSPE) measur observed premium. Root Mean Squared Proportional Error (RMSPE) measures the proportional error is defined as<br>measures the pricing e<br>observed premium. Roo error in absolute terms.





e between the theoretical and o<br>dute terms. Proportional error is<br>red Proportional Error (RMSPE) n Error is defined as the difference between the theoretical and observed premia. RMSE measures the pricing error in absolute terms. Proportional error is mean error divided by observed premium. Root Mean Squared Proportional Error (RMSPE) measures the proportional error in absolute terms.



Table 8: Credit factors regression results.

erage coefficients of the regression hesis.<br>
34 Reported coefficients are the average coefficients of the regression performed on each firm. Corresponding t-stats are in parenthesis.



Table 9: Collinearity diagnosis.

elation matrix among ex<br>
n Factor (VIF) associate<br>
35 In panel A, Table 9 reports the correlation matrix among explanatory variables. In panel B, Table 9 reports the Variance Inflation Factor (VIF) associated to each of the explanatory variables.

Constant	0.00	$-0.18***$	$0.00***$	0.00	$0.00**$	0.00	0.00	$0.00*$	$-0.00$	$-0.47***$
	(0.94)	$(-3.10)$	(2.71)	(0.63)	(2.07)	(0.54)	(1.36)	(1.83)	$(-0.25)$	$(-4.84)$
Libor	$-0.37***$	$-0.36***$	$-0.44***$							
	$(-7.31)$	$(-7.62)$	$(-7.86)$							
Inflation	0.01	0.01		$0.03***$						
	(0.48)	(0.96)		(2.37)						
Money supply	$0.79***$	$0.70***$			$1.37***$					
	(3.41)	(3.14)			(6.91)					
Prices	$0.18**$	$0.17**$				$0.34***$				
	(2.11)	(2.07)				(4.57)				
$\operatorname{GDP}$	$1.05***$	$1.02***$					0.23			
	(4.83)	(4.87)					(1.50)			
Index	$0.20***$	$0.17***$						$0.45***$		
	(3.11)	(2.79)						(5.49)		
FX volatility	$-0.12$	$-0.11$							$-0.16***$	
	$(-1.54)$	$(-1.58)$							$(-4.43)$	
Liquidity		$0.06***$								$0.16***$
		(3.45)								(4.90)
$R^2$	0.37	0.38	0.11	0.01	0.04	0.05	0.05	0.05	0.10	0.07

Table 10: Pricing errors regression - Whole sample.

Forthermore, and the CTRS modents of regressions performed on each firm.<br>
Siss. Dependent variable is the standardized pricing error on the CTRS model. Reported coefficients are the average coefficients of regressions performed on each firm. The corresponding t-stats are reported in parenthesis.



# Table 11: Pricing errors regression - EMU firms.

andardized pricing error on the CTRS months of regressions performed on each firm.<br>
is. Dependent variable is the standardized pricing error on the CTRS model. Reported coefficients are the average coefficients of regressions performed on each firm. The corresponding t-stats are reported in parenthesis.

Constant	0.00	$-0.32***$	0.00	0.00	0.00	$-0.00$	0.00	0.00	$-0.00$	$-0.88***$
	(0.43)	$(-3.71)$	(1.58)	(0.88)	(1.15)	$(-0.97)$	(1.33)	(1.49)	$(-0.44)$	$(-6.22)$
Libor	$-0.14***$	$-0.14***$	$-0.10$							
	$(-2.53)$	$(-2.65)$	$(-1.53)$							
Inflation	$0.03\,$	$0.03*$		$-0.01$						
	(1.45)	(1.66)		$(-0.23)$						
Money Supply	$0.71***$	$0.67***$			0.21					
	(4.86)	(4.47)			(0.97)					
Prices	$-0.71***$	$-0.68***$				$-0.43***$				
	$(-5.54)$	$(-5.50)$				$(-4.50)$				
$\operatorname{GDP}$	2 62***	247***					$-0.04$			
	(5.48)	(5.37)					$(-0.20)$			
Index	$-0.22***$	$-0.25***$						$0.26**$		
	$(-2.40)$	$(-2.71)$						(1.98)		
FX volatility	$-0.77***$	$-0.71***$							$-0.32***$	
	$(-6.07)$	$(-5.85)$							$(-12.44)$	
Liquidity		$0.11***$								$-0.30***$
		(3.57)								(5.30)
$R^2$	0.46	0.48	0.06	0.01	0.01	0.03	0.04	0.04	0.11	0.10

Table 12: Pricing errors regression - U.K. firms.

andardized pricing error on the CTRS metas of regressions performed on each firm.<br>s. Dependent variable is the standardized pricing error on the CTRS model. Reported coefficients are the average coefficients of regressions performed on each firm. The corresponding t-stats are reported in parenthesis.