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# Molecular dynamics of a binary mixture of twist-bend nematic liquid crystal dimers studied by dielectric spectroscopy

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We report a comprehensive dielectric characterization of a liquid crystalline binary mixture composed of the symmetric mesogenic dimer CB7CB and the nonsymmetric mesogenic dimer FFO9OCB. In addition to the high-temperature nematic phase, such a binary mixture shows a twist-bend nematic phase at room temperature which readily vitrifies on slow cooling. Changes in the conformational distribution of the dimers are reflected in the dielectric permittivity and successfully analyzed by means of an appropriate theoretical model. It is shown that the dielectric spectra of the mixture reflect the different molecular dipole properties of the components, resembling in the present case the characteristic dielectric spectra of nonsymmetric dimers. Comparison of the nematic and twist-bend nematic phases reveals that molecular dynamics are similar despite the difference in the molecular environment.

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## I. INTRODUCTION

Liquid crystal dimers consisting of two promesogenic groups joined by a flexible methylene chain containing an odd number of carbon atoms have been the focus of intense research activity over the last few years [1–15]. It was found that these compounds, of which 1'',7''-bis(4-cyanobiphenyl-4'-yl) heptane, CB7CB, is the most studied, show a first order nematic-nematic phase transition. The low-temperature nematic phase is the so-called twist-bend nematic,  $N_{TB}$ . In this phase, formed by achiral molecules, the director exhibits periodic twist and bend deformations forming a conical helix having doubly degenerate domains of opposite handedness. Although initially described for dimers of the CBnCB family, the discovery of a low temperature nematic phase boosted research in the area, and a number of materials combining different mesogenic units linked by chains have been identified which exhibit the  $N_{TB}$  phase [16–18] and its chiral counterpart [19,20]. It is now recognized that molecular curvature plays a crucial role in stabilizing the twist-bend nematic phase. For liquid crystal dimers the nature of the links between the flexible spacer composed of methylene groups and the mesogenic groups, together with the length of the spacer, play a key role. For example, methylene as opposed to ether links provides a better stabilization of the  $N_{TB}$  phase and shorter rather than longer odd spacers also tend to stabilize the phase. The low-energy gaps between the conformers generated by the flexible spacer result in a distribution of energetically favored molecular conformations, promoting a preferred bent shape for molecules having linking chains with an odd number of carbon atoms. This also causes a drastic reduction of the bend elastic constant in the conventional nematic phase

[21] above the twist-bend nematic phase. According to the Landau-like theory developed by Dozov [22], the transition to the twist-bend nematic phase occurs when the bend elastic constant vanishes. However, the ultimate physical mechanism causing the director modulation remains controversial. A flexoelectric coupling between bend deformation and electric polarization [23,24] or purely elastic distortions of the director due to molecular curvature [22] are considered to be possible causes behind the formation of such twist-bend nematic deformations. Indeed Monte Carlo simulations of rigid, apolar bent molecules show that this system can still form the twist-bend nematic phase and that the transition is driven by molecular shape alone [25]. The latest theoretical approaches point towards the primary role of the molecular shape through steric interactions for the appearance of the  $N-N_{TB}$  transition [26,27].

The presence of polar groups in the mesogenic units of the dimers can be used to explore the evolution of the conformational population distribution in nematic phases through analysis of the dielectric properties of the material, and so reveal details of the structure in the twist-bend nematic phase. We have successfully employed such an approach to interpret the static and dynamic dielectric behavior of various nematic dimers, ranging from the symmetric dimers CB7CB or CB9CB [1,6] to the highly nonsymmetric CBO<sub>n</sub>O.Py dimeric family [28,29]. However, until now all dimers showing a stable  $N_{TB}$  phase and studied by dielectric spectroscopy have had identical terminal groups, and so the main motivation of this paper is to analyze the molecular orientational dynamics in the  $N_{TB}$  phase when the dimers are nonsymmetric. We have recently shown that 1''-(2',4-difluorobiphenyl-4'-yloxy)-9''-(4-cyanobiphenyl-4'-yloxy) nonane (FFO9OCB), an ether-linked nonsymmetric odd dimer, exhibits a monotropic  $N_{TB}$  phase [30], and that in binary mixtures with CB7CB there is also a monotropic  $N_{TB}$  phase, which can be vitrified [31].

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89 This phase, although monotropic, is stable enough to allow a  
 90 proper characterization. That is, the addition of a methylene-  
 91 linked dimer (CB7CB) to an ether-linked dimer (FFO9OCB)  
 92 enhances the stability of the twist-bend nematic phase, as  
 93 expected from earlier detailed miscibility studies [31–33].  
 94 Such behavior makes these mixtures the ideal candidates for  
 95 the focus of this study. The  $N_{TB}$ - $N$  transition is always first  
 96 order, regardless of the concentration of the two mesogenic  
 97 compounds in the mixed systems, with a decreasing first-order  
 98 transition entropy on increasing the FFO9OCB concentration  
 99 [31].

100 In this paper we present a complete dielectric study of a  
 101 mixture with a mole fraction of CB7CB equal to 0.48, having  
 102 a significant proportion of the nonsymmetric component  
 103 FFO9OCB, which conveniently shows a broad  $N_{TB}$  range that  
 104 on further cooling becomes a glassy state [ $N_{TB}$  glass ( $-6^\circ\text{C}$ )  
 105  $N_{TB}$  ( $77^\circ\text{C}$ )  $N$  ( $110^\circ\text{C}$ )  $I$ ]. Its static dielectric behavior  
 106 and the frequency-dependent dielectric permittivity will be  
 107 thoroughly examined and discussed in relation to the behavior  
 108 of pure components CB7CB and FFO9OCB. As will be shown,  
 109 the mixture presents a dielectric spectrum similar to that of  
 110 nonsymmetric dimers with three relaxation modes in both  
 111 nematic phases, which will be analyzed in the framework of  
 112 the molecular theory proposed by Stocchero *et al.* [34].

## 113 II. RESULTS AND DISCUSSION

114 Both pure liquid crystal dimers CB7CB and FFO9OCB  
 115 were synthesized according to the procedures reported earlier  
 116 [30,35]. Binary mixtures were prepared in sealed aluminum  
 117 pans, heated to the isotropic phase, and ultrasonicated. The  
 118 quality of the mixing was assessed by means of high-resolution  
 119 calorimetry. More information regarding this preparation  
 120 procedure, calorimetric studies, and also measurements of  
 121 splay and bend elastic constants can be found in [31].

122 Molecular calculations predict a distribution of molecular  
 123 shapes characterized by two broad peaks with maxima corre-  
 124 sponding to an extended conformer (*trans* conformer) with an  
 125 average angle between the mesogenic units of around  $120^\circ$  and  
 126 a hairpin-shaped conformer (*cis* conformer) with an internal  
 127 average angle around  $30^\circ$ . For high values of the nematic  
 128 order parameter the most extended conformers are stabilized  
 129 at the expense of the less extended conformers [1,21,34].  
 130 Figure 1 shows the chemical structures of the component  
 131 compounds together with a schematic representation of the  
 132 two main conformers for both dimers. The mean-square  
 133 dipole moment is given by the averaged vector sum of the  
 134 constituent dipole moments associated with the nitrile  
 135 groups for CB7CB ( $\sim 4$  D), and the two C-F bonds and  
 136 nitrile group for the case of FFO9OCB ( $\sim 2.25$  D). As can  
 137 be appreciated, extended orientationally averaged conformers  
 138 will contribute very differently to the permittivity component  
 139 along the director ( $\epsilon_{\parallel}$ ), with a zero mean-square dipole in  
 140 the case of CB7CB and a nonzero component in the case of  
 141 the nonsymmetric FFO9OCB. On the other hand, in both  
 142 cases the hairpin conformers make a large contribution to the  
 143 value of  $\epsilon_{\parallel}$ . Regardless of the configuration for both dimers  
 144 there will be a nonzero transverse dipolar contribution to the  
 145 perpendicular component of the permittivity ( $\epsilon_{\perp}$ ), which will  
 146 depend on the average angle between the terminal groups. For

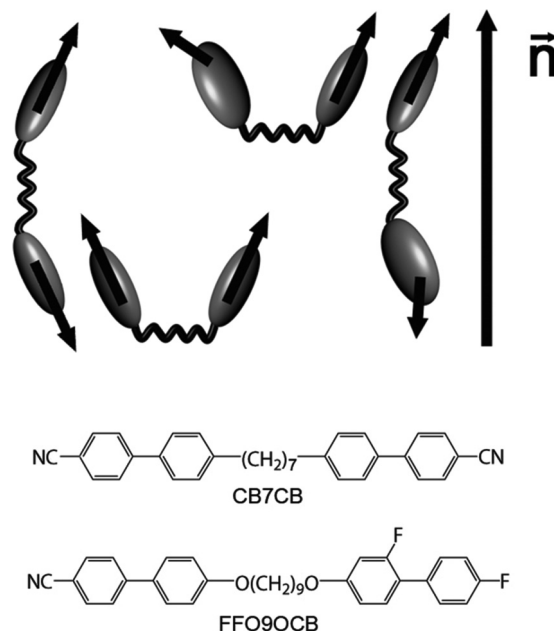


FIG. 1. Chemical structures of CB7CB and FFO9OCB. Schematic representation of the two main conformers for both dimers.

the  $N_{TB}$  phase “parallel” and “perpendicular” refer to the helix 147 axis. 148

In Fig. 2 we present both components of the static dielectric 149 permittivity for three mixtures (CB7CB mole fractions: 0.21, 150 0.48, and 0.82) together with the corresponding values for the 151 two pure compounds. The measurements were taken using 152 an Agilent Precision LRC meter E4890A and Instec cells of 153  $8\ \mu\text{m}$  thickness with antiparallel planar rubbing. Samples were 154 held on a hot stage (TMSG-600) and temperature controller 155 (TMS-93) from Linkam. The perpendicular component  $\epsilon_{\perp}$  156 was obtained directly using harmonic probe fields of low 157

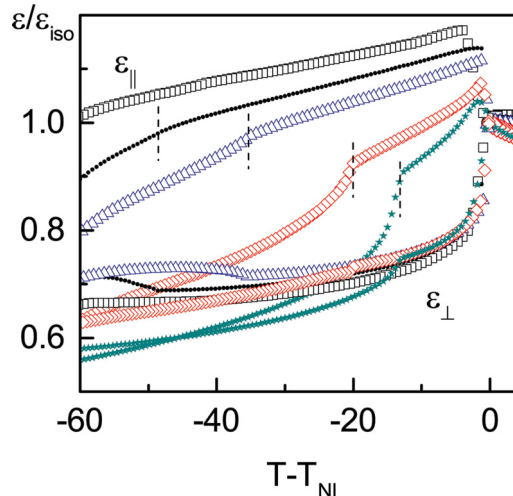


FIG. 2. Temperature dependence of the static permittivity of the two pure compounds and the three mixtures: ( $\square$ ) FFO9OCB; ( $\bullet$ )  $X_{CB7CB} = 0.21$ ; ( $\triangle$ )  $X_{CB7CB} = 0.48$ ; ( $\diamond$ )  $X_{CB7CB} = 0.82$ ; ( $\star$ ) CB7CB. Discontinuous lines correspond to the phase transition  $N_{TB}$ - $N$ .

158 amplitude,  $0.5 V_{\text{rms}}$ , well below the threshold voltage of the  
 159 Fréedericksz transition. On the other hand, the parallel com-  
 160 ponent  $\epsilon_{\parallel}$  was measured by applying voltages well above the  
 161 transition, which align the director parallel to the electric field.  
 162 We have chosen 5 kHz as most convenient for the aligning  
 163 field frequency [6]. As can be observed for all the samples, the  
 164 behavior at the  $I$ - $N$  transition is as expected for materials with  
 165 positive dielectric anisotropy:  $\epsilon_{\perp}$  decreases and  $\epsilon_{\parallel}$  increases.  
 166 On further lowering the temperature,  $\epsilon_{\perp}$  is gradually stabilized  
 167 in a very similar way, reflecting the increase of orientational  
 168 order and the subtle effect that changes in the conformational  
 169 distribution can exert on the averaged transverse component  
 170 of the molecular dipole moment. However, the behavior of  
 171 the parallel component strongly depends on the symmetric  
 172 or nonsymmetric structure of the dimers. The aforementioned  
 173 initial increase in the parallel permittivity on lowering the tem-  
 174 perature at the  $I$ - $N$  transition for CB7CB can only be explained  
 175 by the slight stabilization of hairpin conformers, which carry  
 176 a large longitudinal dipole moment, as opposed to the very  
 177 broad distribution of molecular conformers in the isotropic  
 178 phase [34]. After the initial increase, the parallel permittivity  
 179 rapidly decreases in the nematic phase on further reducing the  
 180 temperature. This behavior suggests a significant reduction of  
 181 the average mean-square molecular dipole moment as the ori-  
 182 entational order of the phase increases. Molecular calculations  
 183 for CB7CB using a continuous torsional potential [1] for the  
 184 connecting methylene chain showed that the increase of orien-  
 185 tational order produces a progressive increase of the population  
 186 of the more extended conformers with zero longitudinal dipole  
 187 moment at the expense of the hairpin-shaped ones, which is in  
 188 agreement with the observed temperature dependence of  $\epsilon_{\parallel}$ .  
 189 Such changes in the conformational distribution seem to be  
 190 common for liquid crystal dimers subject to a nematic potential  
 191 [34]. On entering the  $N_{\text{TB}}$  phase, the continuous decrease of  
 192 both components of the permittivity is accelerated, and at low  
 193 temperatures there is even a sign reversal in the dielectric  
 194 anisotropy from positive to negative.

195 For the nonsymmetric FFO9OCB dimer, the behavior is  
 196 slightly different. The parallel component also decreases as the  
 197 temperature is reduced but less drastically than for CB7CB;  
 198 this observation is related to the nonzero value of the average  
 199 dipole moment of the extended conformers [30]. This case is  
 200 intermediate between the two extremes: The CBnCB family  
 201 has two equal terminal groups, and no net longitudinal dipole  
 202 component for extended conformers, while in the CBO<sub>n</sub>O.Py  
 203 family [28,29] only one of the terminal groups has a significant  
 204 dipole moment. In the latter case, the static permittivity  
 205 is similar to the monomers of the nCB family, showing a  
 206 continuous increase as temperature decreases. Interestingly,  
 207 the static permittivity of the mixtures reveals the adequacy of  
 208 the model for the interpretation of the dielectric results.  $\epsilon_{\parallel}$   
 209 behaves in between the tendencies exhibited by both pure  
 210 compounds, smoothly approaching from one to the other  
 211 depending on the mole fraction. This is evidence that the  
 212 contribution of the net longitudinal dipole of the extended  
 213 nonsymmetric dimer hinders the drastic reduction of  $\epsilon_{\parallel}$  seen  
 214 for CB7CB and implies a higher value of the dielectric  
 215 anisotropy. Also noteworthy is the behavior of  $\epsilon_{\perp}$  at the  $N$ - $N_{\text{TB}}$   
 216 transition: While there is a decrease in the value for CB7CB,  
 217 that of the mixtures shows an appreciable increase which can

218 be explained in terms of the growth of the conical angle and  
 219 the contribution of a net longitudinal dipole moment.

220 The analysis of the frequency-dependent dielectric permit-  
 221 tivity for the mixtures in the  $N$  and  $N_{\text{TB}}$  phases will give  
 222 information on the molecular orientational dynamics. In order  
 223 to cover the whole frequency range  $10^{-2}$ – $1.8 \times 10^9$  Hz and  
 224 properly characterize the dielectric spectra of the materials,  
 225 three different analyzers are needed: These are AlphaA  
 226 from Novocontrol, HP4192A, and HP4291A. High-frequency  
 227 dielectric measurements require the utilization of cells with  
 228 untreated metal electrodes, which in our setup consists of a  
 229 parallel plate capacitor made of two circular gold-plated brass  
 230 electrodes with a 5-mm diameter separated by 50- $\mu\text{m}$ -thick  
 231 silica spacers.

232 For pure materials, the usual alignment achieved  
 233 spontaneously in these cells with gold electrodes is a random  
 234 planar alignment; i.e., the director is perpendicular to the  
 235 probe measuring electric field. For materials having a positive  
 236 dielectric anisotropy, it is possible to switch in the nematic  
 237 phase the alignment to homeotropic (director along the field  
 238 direction) with a suitable bias field. For the mixture studied,  
 239 although having a positive dielectric anisotropy, the director  
 240 alignment in the gold-electrode cells was not as described  
 241 above. Since it is not possible to view the sample in the dielec-  
 242 tric cell, assessment of the alignment was made by making the  
 243 appropriate capacitance measurements, and then fitting these  
 244 to the Havriliak-Negami function [see Eq. (3)]. From the fitting  
 245 it is possible to determine the extrapolated zero-frequency  
 246 permittivity, and compare this with values measured in  
 247 glass cells at low frequency, for which the alignment can  
 248 be checked visually. Thus, although the dielectric spectrum  
 249 obtained for the mixture in the gold-electrode cells exhibited  
 250 some distinctive features of the expected planar alignment,  
 251 it was not perfect. Similarly, on application of a bias field  
 252 the final aligned state was not a perfect homeotropic state.  
 253 We found that by gentle shearing, the degree of homeotropic  
 254 alignment could be increased, but even the best aligned  
 255 samples had an extrapolated value for the zero-frequency  
 256 parallel permittivity about 10% less than that expected from  
 257 separate low-frequency measurements. Thus we term the  
 258 state measured as “quasihomeotropic,” but for the purposes of  
 259 analyzing the dynamics probed along the parallel axis of the  
 260 permittivity, the degree of alignment was satisfactory.

261 The sample was placed at the end of a coaxial line and  
 262 a modified HP16091A coaxial test fixture was used as the  
 263 sample holder and then held in a Novocontrol cryostat, which  
 264 screens the system. Dielectric measurements were performed  
 265 on cooling with different temperature steps being stabilized  
 266 to  $\pm 20$  mK. However, it should be noted that due to the time  
 267 required to perform low-frequency scans down to  $10^{-2}$  Hz with  
 268 the AlphaA analyzer, only a few temperatures were measured  
 269 in this low-frequency range below  $40^\circ\text{C}$ , and will only be  
 270 used for a preliminary analysis of the glass transition dynamics  
 271 where they become relevant.

272 The frequency dependence of the real,  $\epsilon'(\omega)$ , and imaginary,  
 273  $\epsilon''(\omega)$ , parts of the quasihomeotropic dielectric permittivity  
 274 components are given in Fig. 3 for temperatures in (b)  
 275 the nematic, and (c) the twist-bend nematic phases together  
 276 with (a) a three-dimensional plot of the dielectric losses vs  
 277 temperature and frequency. Although in the isotropic phase

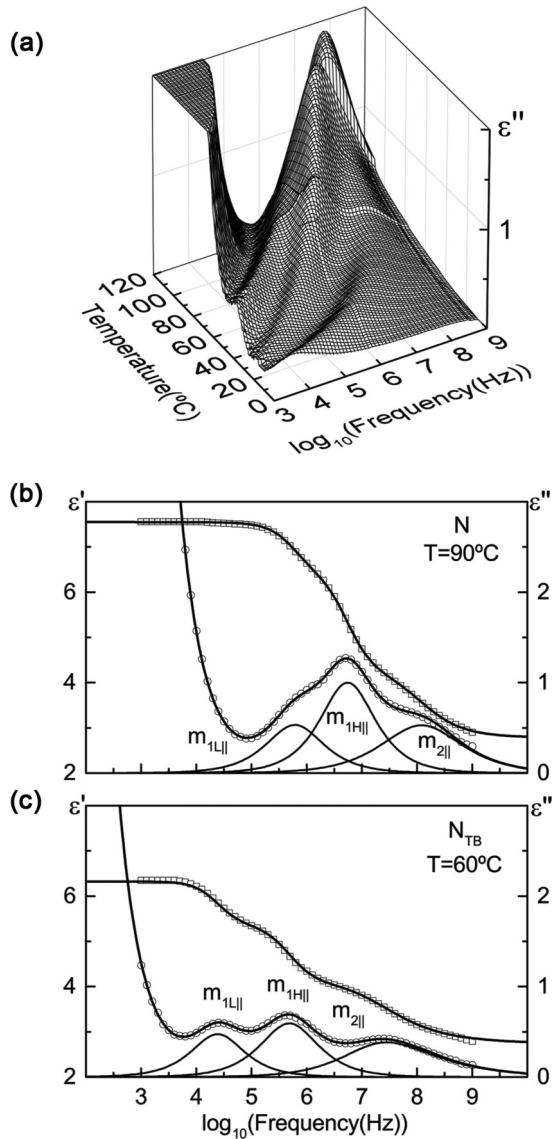


FIG. 3. Mixture with 0.48 mole fraction of CB7CB. (a) Three-dimensional plot of the dielectric losses vs temperature and logarithm of the frequency. Frequency dependence of  $\epsilon'$  ( $\square$ ) and  $\epsilon''$  ( $\circ$ ) (b) in the  $N$  phase, and (c) in the  $N_{TB}$  phase. In (b,c) solid lines are fits to Eq. (3).

dimers which considers that molecular reorientation occurs via a two-step process involving the individual orientational relaxation of the mesogenic units with different rates:  $k_i^{T \rightarrow C}$  (rate coefficient for the reorientation of the rigid unit  $i$  from the *trans* to the *cis* configuration) and  $k_i^{C \rightarrow T}$  (inverse process). Note that reorientations (end-over-end processes) of the connected dipolar groups are considered to be individual, but not independent, because of the correlation imposed by the flexible spacer and accounted for by the conformational distribution through the detailed balance equation  $P_T^{eq} k_i^{T \rightarrow C} = P_C^{eq} k_i^{C \rightarrow T}$  [34], where  $P_T^{eq}$  and  $P_C^{eq}$  are the equilibrium populations of the *trans* and *cis* configurations, respectively. Whole molecular reorientation is excluded, since the energy barrier for the simultaneous rotation of both units is too high and results in a nonsignificant transition rate [34]. As order increases, calculation showed that the four wells become deeper but the barriers are still much smaller for the individual flip-flops than for the whole molecular reorientation. While the dynamics are determined by the energy barriers between the states, the dielectric strength of the relaxations are determined by the relative equilibrium populations of the orientational states.

For symmetric dimers the flipping rates of both units are equal and the resulting dipole moment correlation function

$$C_{||}(t) = 4\langle\mu_{||}\rangle^2 P_C^{eq} \exp(-2k^{C \rightarrow T}t), \quad (1)$$

has a monoexponential decay, and so only a single low-frequency absorption, which, as has been shown for CB7CB and CB9CB [6,11], can be detected at frequencies corresponding to those of the intermediate frequency relaxation observed here and whose strength depends on the conformational distribution. On the other hand, for nonsymmetric dimers, relaxation rates would be different, and, depending on the shape and dipole moments of each unit, a variety of frequency relaxation profiles is predicted. In the case of FFO9OCB and assuming a relationship between dipole moments of both units given by  $\langle\mu_{||}\rangle_{FF} \approx 1/2\langle\mu_{||}\rangle_{CN}$ , the model leads to the correlation function

$$C_{||}(t) = \frac{1}{4}\langle\mu_{||}\rangle_{CN}^2 (P_T^{eq} - 3P_C^{eq})^2 \exp(-2k_B t) + 4\langle\mu_{||}\rangle_{CN}^2 P_C^{eq} P_T^{eq} \exp(-2k_A t), \quad (2)$$

where  $k_A = \frac{1}{2}(k_A^{T \rightarrow C} + k_A^{C \rightarrow T})$  ( $A$  stands for the unit containing the CN group) and  $k_B = 2(P_C^{eq} k_B^{C \rightarrow T}) = 2(P_T^{eq} k_B^{T \rightarrow C})$  ( $B$  stands for the unit containing the FF group). Equation (2) entails the emergence of an additional lower-frequency relaxation mode. Both low-frequency processes are related to the individual flip-flop motions of the units, and dielectric strengths are determined by equilibrium population their of the conformers [30,34]. Experimental results for FFO9OCB clearly confirm [30] such model's prediction. Accordingly, we associate the three dielectric relaxations observed for the mixture to (i) a superposition of the precessional motion of the dipolar groups around the director and the rotation around the long axis at the high-frequency branch of the spectrum ( $m_2$ ) and (ii) the end-over-end reorientation of the dipolar groups parallel to the director at low frequencies ( $m_{1L}$  and  $m_{1H}$ ) [34]. It is evident that the mixture shows a behavior resembling that of nonsymmetric dimers, with the appearance of a third dielectric mode at low frequencies, that in this case results from the fluorinated group reorientations.

there is only one mode, in both nematic phases the dielectric permittivity shows three relaxations, as in other nonsymmetric dimers [11,28,29] and in particular as in FFO9OCB [30]. The interpretation of such previous results required the development of a suitable theoretical model that is worth recalling here. Stocchero *et al.* [34] proposed a dynamic model based on the time-scale separation between the motion of the mesogenic units and the fast relaxation of the flexible chain. The original model of Maier-Saupe [36] for the dielectric relaxation of a dipolar molecule in a nematic potential was a two-state model representing the two orientations of a dipole along the director axis. In the case of the model of Stocchero *et al.* the resulting potential presents four deep wells corresponding to the four stable states of the dimer with the terminal groups parallel or antiparallel to the director. Such a potential provides the basis of the kinetic model for nematic

348 The dielectric strengths of  $m_{1L}$  and  $m_{1H}$  for nonsymmetric  
 349 dimers are predicted to depend on the conformational pop-  
 350 ulation distribution and on the relative value of the dipole  
 351 moments of both terminal groups. Although the precise  
 352 temperature dependence is intricate, the usual trend [11,28,29]  
 353 is that the strength of the lower-frequency mode ( $m_{1L}$ )  
 354 increases while that of  $m_{1H}$  decreases when the temperature  
 355 is reduced as found for FFO9OCB [30]. Despite the similarity of  
 356 the dielectric spectra of the mixture with that of FFO9OCB, the  
 357 contribution of the symmetric CB7CB is clear when comparing  
 358 the much higher strength of the  $m_{1H}$  mode with respect to that  
 359 of pure FFO9OCB, as this mode can be associated with the  
 360 reorientation of the nitrile groups of both dimers. In order to  
 361 describe accurately the behavior of the mixture, the spectra for  
 362 each temperature have been analyzed by fitting each relaxation  
 363 mode according to the Havriliak-Negami function through the  
 364 empirical relationship

$$\begin{aligned} \varepsilon(\omega) &= \varepsilon'(\omega) - i\varepsilon''(\omega) \\ &= \sum_k \frac{\Delta\varepsilon_k}{[1 + (i\omega\tau_k)^\alpha]^\beta} - \frac{i\sigma_{dc}}{\omega\varepsilon_0} + \varepsilon_\infty, \end{aligned} \quad (3)$$

365 where  $\varepsilon_\infty$  is the extrapolated high-frequency permittivity,  $\Delta\varepsilon_k$   
 366 is the strength of the corresponding relaxation mode, and  
 367  $\sigma_{dc}$  is the dc conductivity. The relaxation time  $\tau_k$  is related  
 368 to the frequency of maximum loss through the parameters  
 369  $\alpha_k$  and  $\beta_k$ , which describe the width and the asymmetry of  
 370 the relaxation spectra, respectively ( $\alpha = \beta = 1$  corresponds  
 371 to a simple Debye-like process). The two low-frequency  
 372 modes have a near-Debye shape in both mesophases and  
 373 the high-frequency one is broader and asymmetric (having  
 374 a Cole-Davidson shape with  $\alpha$  about 0.8 and  $\beta$  ranging from  
 375 0.7 to 0.6). Dielectric strengths for each relaxation are given  
 376 as a function of temperature in Fig. 4. The strength of the  
 377 high-frequency mode  $m_2$  in the  $N$  phase shows a decrease as  
 378 the temperature decreases. On the other hand, the strengths of  
 379 the two low-frequency modes,  $m_{1L}$  and  $m_{1H}$ , are correlated:  
 380 while that of  $m_{1H}$  decreases, the strength of  $m_{1L}$  increases as  
 381 temperature decreases in the  $N$  phase. This is the same trend  
 382 observed for the corresponding modes for FFO9OCB [30].  
 383 The strengths of the three modes exhibit small jumps at the  
 384  $N$ - $N_{TB}$  phase transition, but a proper quantitative analysis is

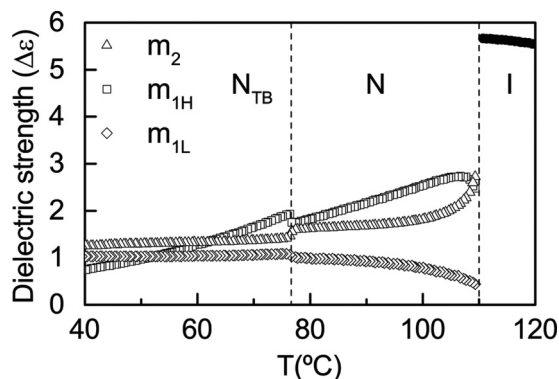


FIG. 4. Mixture with 0.48 mole fraction of CB7CB. Dielectric strength of the relaxation modes vs temperature: (●) isotropic phase; (Δ)  $m_2$ ; (□)  $m_{1H}$ ; (◇)  $m_{1L}$ .

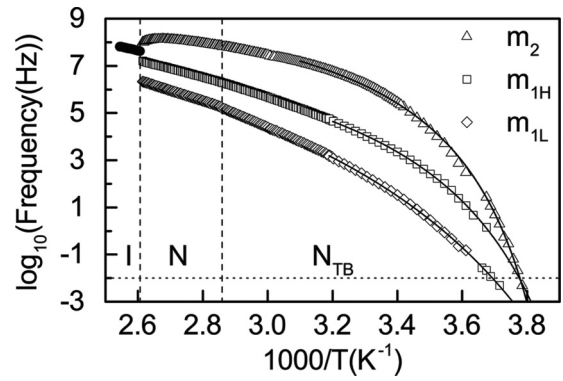


FIG. 5. Mixture with 0.48 mole fraction of CB7CB. Arrhenius plot of the frequency of the relaxation modes: (●) isotropic phase; (Δ)  $m_2$ ; (□)  $m_{1H}$ ; (◇)  $m_{1L}$ . Solid lines are fits to the VFT law, Eq. (4).

not possible because the achieved alignment is not perfect. In  
 fact we think that in a perfect parallel alignment  $\Delta\varepsilon_2$  should  
 be slightly smaller, taking into account the value obtained  
 for FFO9OCB [30], and the strengths of the low-frequency  
 modes slightly higher; the jumps at the transition downwards  
 are provoked by the appearance of the tilt. What is interesting  
 is the general trend:  $\Delta\varepsilon_{1H}$  decreases while  $\Delta\varepsilon_{1L}$  tends to  
 saturate. It is important to recall that, even if the alignment  
 were perfect, the precise analysis of the temperature dependence  
 would be complicated since it involves both the temperature  
 evolution of the population of the different conformers and  
 the relative value of the dipoles in the terminal mesogenic  
 units [28–30,34]. The frequency dependence of the modes can  
 be determined over a broad temperature range, and as can be  
 observed in Fig. 5 its temperature dependence in the  $N$  phase  
 is similar to that found for FFO9OCB. Remarkably, at the  $N$ - $N_{TB}$   
 phase transition the frequencies remain almost unaltered,  
 compatible with a weakly first order phase transition. The  
 two low-frequency modes follow the Arrhenius law in the  
 $N$  phase with activation energies of  $85 \text{ kJ mol}^{-1}$  ( $m_{1L}$ ) and  
 $70 \text{ kJ mol}^{-1}$  ( $m_{1H}$ ). At the higher temperatures in the  $N_{TB}$   
 phase, the low-frequency modes also follow the Arrhenius  
 law with activation energies slightly larger, namely, 115 and  
 $91 \text{ kJ mol}^{-1}$ , respectively. However, in line with the glass  
 transition detected by calorimetry at  $-6^\circ\text{C}$  [31], on reducing  
 the temperature further there is a slowing down of the dynamics  
 as the glassy state is approached, strongly deviating from the  
 Arrhenius behavior. For this temperature range, Fig. 5 shows,  
 superimposed, the corresponding fitting to the VFT (Vogel-  
 Fulcher-Tammann) temperature-dependent relationship,

$$f_k = \frac{\omega_k}{2\pi} = f_{k0} \exp\left[\frac{B}{T - T_0}\right], \quad (4)$$

where  $f_{k0}$ ,  $B$ , and  $T_0$  are fitting parameters. The first important  
 observation is that the  $m_{1H}$  mode seems to merge with  $m_2$ ,  
 in the same way as happens with the analogous  $m_1$  and  
 $m_2$  for CB7CB on approaching the glassy  $N_{TB}$  phase [2].  
 However, at least in our frequency-temperature window,  $m_{1L}$   
 evolves separately. For dielectric relaxation, a glass transition  
 (known as a dynamic glass transition) is obtained when the  
 characteristic relaxation frequency reaches  $10^{-2} \text{ Hz}$ . In Fig. 5

we can see how this value corresponds to the same temperature for  $m_2$  and  $m_{1H}$  (around  $-10^\circ\text{C}$ ) while it is reached at a slightly higher temperature for  $m_{1L}$  (around  $-6^\circ\text{C}$ ). This implies that, from a dielectric point of view, two glass transition temperatures involving different molecular motions are present; the lower-temperature glass transition due to the dynamic disorder of the cyanobiphenyl group and that at higher temperatures attributed to the fluorinated group reorientations. In the latter case, the nematic environment at these low temperatures makes the steric interactions of each group much stronger, hindering the reorientations and increasing the required thermal energy. Accordingly, the associated glass transition temperature is higher than for the cyanobiphenyl group [37]. However, the analysis of the dynamics at this double glass transition is beyond the scope of this paper and needs to be confirmed by other experimental techniques and thoroughly examined with more detailed models [2].

### III. SUMMARY

In our opinion the most interesting aspect of our results is that we have been able to study the dielectric spectra for a nonsymmetric dimer exhibiting the  $N_{\text{TB}}$  phase. We demonstrate that in a mixture containing a nonsymmetric element with an adequate molecular dipole the spectra resemble those of the nonsymmetric component by exhibiting three relaxation processes. The spectra can be satisfactorily explained in terms of the theoretical model for dielectric relaxation in liquid crystal dimers proposed by Stocchero *et al.* [34]. Recently, a study of the dielectric spectra of a six-component mixture, denoted KA(0.2) (three symmetric and three nonsymmetric dimers) in the  $N$  and  $N_{\text{TB}}$  phases was reported, attributing  $m_{1L}$

to whole molecule end-over-end rotation of cybotactic groups [38]. Interestingly, although x-ray studies in symmetric dimers such as CB9CB [33] also suggest the presence of domains, our dielectric results of this material [6] show a single relaxation process at frequencies similar to those of  $m_{1H}$  as predicted by Stocchero's model. In light of our previous studies and those presented here, we believe that the low-frequency mode described for the KA(0.2) mixture could be attributed to the contribution of the individual reorientation of the mesogenic units of the nonsymmetric compounds constituting the sample. Remarkably, in our mixture we could follow the dielectric modes over a very broad frequency-temperature range both in the  $N$  and  $N_{\text{TB}}$  phases. From a dielectric point of view, both nematic phases exhibit the same molecular active modes, with a similar behavior (only small changes in the strength, related to the director tilt, and in the activation energies) and the molecular environment, nematic or twist-bend nematic, scarcely affects the dielectric properties. However, as the mixture shows a glass transition, when reducing the temperature the molecular modes seem to become increasingly collective as already described for CB7CB [2].

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- [1] M. Cestari, S. Diez-Berart, D. A. Dunmur, A. Ferrarini, M. R. de la Fuente, D. J. B. Jackson, D. O. López, G. R. Luckhurst, M. A. Pérez-Jubindo, R. M. Richardson, J. Salud, B. A. Timimi, and H. Zimmermann, *Phys. Rev. E* **84**, 031704 (2011).
- [2] D. O. López, N. Sebastian, M. R. de la Fuente, J. C. Martínez-García, J. Salud, M. A. Pérez-Jubindo, S. Diez-Berart, D. A. Dunmur, and G. R. Luckhurst, *J. Chem. Phys.* **137**, 034502 (2012).
- [3] D. Cheng, J. H. Porada, J. B. Hooper, A. Klitnick, Y. Shen, M. R. Tuchband, E. Korblova, D. Bedrov, D. M. Walba, M. A. Glaser, J. E. MacClennan, and N. A. Clark, *Proc. Natl. Acad. Sci. USA* **110**, 15931 (2013).
- [4] V. Borsch, Y. K. Kim, J. Xiang, M. Gao, A. Jáklí, V. P. Panov, J. K. Vij, C. T. Imrie, M. G. Tamba, G. H. Mehl, and O. D. Lavrentovich, *Nat. Commun.* **4**, 2635 (2013).
- [5] V. P. Panov, R. Balachandran, J. K. Vij, M. G. Tamba, A. Kohlmeier, and G. H. Mehl, *Appl. Phys. Lett.* **101**, 234106 (2012).
- [6] B. Robles-Hernández, N. Sebastián, M. R. de la Fuente, D. O. López, S. Diez-Berart, J. Salud, M. B. Ros, D. A. Dunmur, G. R. Luckhurst, and B. A. Timimi, *Phys. Rev. E* **92**, 062505 (2015).
- [7] V. P. Panov, M. Nagaraj, J. K. Vij, Y. P. Panarin, A. Kohlmeier, M. G. Tamba, R. A. Lewis, and G. H. Mehl, *Phys. Rev. Lett.* **105**, 167801 (2010).
- [8] P. A. Henderson and C. T. Imrie, *Liq. Cryst.* **38**, 1407 (2011).
- [9] C. S. P. Tripathi, P. Losada-Pérez, C. Glorieux, A. Kohlmeier, M. G. Tamba, G. H. Mehl, and J. Leys, *Phys. Rev. E* **84**, 041707 (2011).
- [10] M. Sepelj, A. Lesac, S. Baumeister, S. Diele, H. L. Nguyen, and D. W. Bruce, *J. Mater. Chem.* **17**, 1154 (2007).
- [11] D. A. Dunmur, G. R. Luckhurst, M. R. de la Fuente, S. Diez, and M. A. Pérez-Jubindo, *J. Chem. Phys.* **115**, 8681 (2001).
- [12] C. Meyer, G. R. Luckhurst, and I. Dozov, *Phys. Rev. Lett.* **111**, 067801 (2013).
- [13] C. Meyer, G. R. Luckhurst, and I. Dozov, *J. Mater. Chem. C* **3**, 318 (2015).
- [14] D. A. Dunmur, M. R. de la Fuente, M. A. Perez-Jubindo, and S. Diez, *Liq. Cryst.* **37**, 723 (2010).
- [15] D. A. Dunmur, M. Cestari, S. Diez-Berart, A. Ferrarini, M. R. de la Fuente, D. J. B. Jackson, D. O. López, G. R. Luckhurst, M. A. Pérez-Jubindo, R. M. Richardson, J. Salud, B. A. Timimi, and H. Zimmermann, *Presented at the 23rd International Liquid Crystal Conference, Kraków, Poland, July 11–16, 2010*, Oral 60 (unpublished).
- [16] R. J. Mandle, E. J. Davis, C. C. A. Voll, C. T. Archbold, J. W. Goodby, and S. J. Cowling, *Liq. Cryst.* **42**, 688 (2015).
- [17] R. J. Mandle, E. J. Davis, C. T. Archbold, C. C. A. Voll, J. L. Andrews, S. J. Cowling, and J. W. Goodby, *Chemistry* **21**, 8158 (2015).
- [18] Z. Ahmed, C. Welch, and G. H. Mehl, *RSC Adv.* **5**, 93513 (2015).

- [19] E. Gorecka, N. Vaupotič, A. Zep, D. Pocięcha, J. Yoshioka, J. Yamamoto, and H. Takezoe, *Angew. Chem., Int. Ed.* **54**, 10155 (2015).
- [20] A. Zep, S. Aya, K. Aihara, K. Ema, D. Pocięcha, K. Madrak, P. Bernatowicz, and H. Takezoe, *J. Mater. Chem. C* **1**, 46 (2013).
- [21] M. Cestari, E. Frezza, A. Ferrarini, and G. R. Luckhurst, *J. Mater. Chem.* **21**, 12303 (2011).
- [22] I. Dozov, *Europhys. Lett.* **56**, 247 (2001).
- [23] R. B. Meyer, in *Molecular Fluids*, edited by R. Balian and G. Weill (Gordon and Breach, New York, 1976).
- [24] S. M. Shamid, S. Dhakal, and J. V. Selinger, *Phys. Rev. E* **87**, 052503 (2013).
- [25] R. Memmer, *Liq. Cryst.* **29**, 483 (2002).
- [26] C. Greco and A. Ferrarini, *Phys. Rev. Lett.* **115**, 147801 (2015).
- [27] N. Vaupotič, S. Curk, M. A. Osipov, M. Čepič, H. Takezoe, and E. Gorecka, *Phys. Rev. E* **93**, 022704 (2016).
- [28] N. Sebastián, M. R. de la Fuente, D. O. López, M. A. Pérez-Jubindo, J. Salud, S. Diez-Berart, and M. B. Ros, *J. Phys. Chem. B* **115**, 9766 (2011).
- [29] N. Sebastián, M. R. de la Fuente, D. O. López, M. A. Pérez-Jubindo, J. Salud, and M. B. Ros, *J. Phys. Chem. B* **117**, 14486 (2013).
- [30] N. Sebastián, D. O. López, B. Robles-Hernández, M. R. de la Fuente, J. Salud, M. A. Pérez-Jubindo, D. A. Dunmur, G. R. Luckhurst, and D. J. B. Jackson, *Phys. Chem. Chem. Phys.* **16**, 21391 (2014).
- [31] D. O. López, B. Robles-Hernández, J. Salud, M. R. de la Fuente, N. Sebastián, S. Diez-Berart, X. Jaen, D. A. Dunmur, and G. R. Luckhurst, *Phys. Chem. Chem. Phys.* **18**, 4394 (2016).
- [32] K. Adlem, M. Čopič, G. R. Luckhurst, A. Martelj, O. Parri, R. M. Richardson, B. D. Snow, B. A. Timimi, R. P. Tuffin, and D. Wilkies, *Phys. Rev. E* **88**, 022503 (2013).
- [33] E. Ramou, Z. Ahmed, C. Welch, P. K. Karahaliou, and G. H. Mehl, *Soft Matter* **12**, 888 (2016).
- [34] M. Stocchero, A. Ferrarini, G. J. Moro, D. A. Dunmur, and G. R. Luckhurst, *J. Chem. Phys.* **121**, 8079 (2004).
- [35] P. J. Barnes, A. G. Douglass, S. K. Heeks, and G. R. Luckhurst, *Liq. Cryst.* **13**, 603 (1993).
- [36] G. Meier and A. Saupe, *Mol. Cryst.* **1**, 515 (1966).
- [37] S. Diez-Berart, D. O. López, J. Salud, J. A. Diego, J. Sellarés, B. Robles-Hernández, M. R. de la Fuente, and M. B. Ros, *Materials* **8**, 3334 (2015).
- [38] R. R. Ribeiro de Almeida, C. Zhang, O. Parri, S. N. Sprunt, and A. Jáklı, *Liq. Cryst.* **41**, 1661 (2014).