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## MODELS AND PROCEDURES FOR ELECTRIC ENERGY DISTRIBUTION PLANNING. A REVIEW

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**Abstract:** Distribution system planning is a key component to accomplish the service in a fast growing demand market, both from a technical point of view and from the economic costs management. In the near future, electric companies will need faster and cheaper planning tools to evaluate different scenarios and their consequences for the rest of the system and provide their clients with safe reliable and economic energy. The objective of this paper is to review different articles about this subject trying to continue the previous work from Gonen and Ramírez-Rosado in 1986 (Gönen,1986). *Copyright © 2002 IFAC*

**Keywords:** planning, distribution, optimisation.

### 1. INTRODUCTION

The distribution system planning goal is to assure that a demand growth can be satisfied in an optimal way from the secondary feeders to the substations from where energy must be delivered to the final client economically while complying with several technical specifications. These considerations and several others - like the difficulties to obtain urban soil, aesthetic and ecological considerations - can harden the problem of optimal planning calculus. The people in charge of distribution planning should consider the energy consumption, their geographical location, laws regarding the use of soil plus other aspects to come up with the substations dimensioning and location, the maximum efficiency routes, while minimising the energy loss in the feeders and deployment costs, plus satisfying the reliability of service constraints.

The planners usually divide the planning in several subproblems, which can be efficiently solved by algorithms and procedures already available. The

objective is minimising the installation costs of substations and feeders, plus the implied costs associated to maintenance and operation, while satisfying several constraints related to the allowable voltage values, reliability, service maintenance, etc.

As the distribution system related costs constitute an important part of the electric power systems total costs, the need of more rigorous mathematical models and the development of more efficient algorithms is obvious. The final objective should be minimising incurred costs and achieving the desired goals.

The design of electric energy distribution system planning is executed around the existing system using a procedure containing the following steps: demand forecasting and assignment to existing or new areas, location and dimensioning of substations, dimensioning and routing of feeders and distribution networks. Today, and thanks to the computers development, improvements to the proposed plans can be obtained analysing several different

alternatives by using mathematical models and different optimisation procedures.

## 2. MODELS REVIEW

In this section we will review the published works about growth planning of the distribution systems, as well as different approaches given to this topic in order to know the models, resolution methods and constraints.

Of the works existing about this topic, we have revised the ones which have appeared in specialised journals, as IEEE and IEE.

The models have been classified in accordance to several characteristics such as system treatment, planning horizon and time lapse, methods to handle the problems related with substations and/or feeders consider: costs, location and dimensioning problems, voltage drops and radiality consideration, and finally the proposed mathematical methods to solve them, as suggested by Gönen T. and Ramírez-Rosado in 1986.

### 2.1. Handling of the Distribution System.

From the point of view of how the system is handled, the problem of distribution system planning is usually subdivided in two subproblems, due to their large size. The two subproblems are:

The subproblem of optimal dimensioning and/or location of electric distribution substations [Adams et al. 1984, Adams, Laughton, 1973, Adams, Laughton, 1974, Afuso et al. 1982, Bouchard et al. 1994, Crawford, Holt Jr 1975, Holt Jr, Crawford 1976, Hongwei et al. 1993, Masud 1974, Masud 1978].

The subproblem of dimensioning and/or location of feeders [Adams, Laughton, 1974, Mikic 1986, Wall et al. 1979].

Some researchers try to solve the problem as a sequence of both subproblems, after analysing the location and dimensioning of substations in a first step, the optimal dimensioning and routing from the feeders is calculated. But from a mathematical point of view, this approach does not guarantee us that an optimal solution to the global problem is found, because each subsystem is solved independently and the optimisation of the whole system is not separable in two unrelated subproblems [Skrlec 1996]. The solutions may end up in a local minimum of the separated problems, not reaching the global minimum.

Due to the errors incurred in the separated treatment of both subproblems, and thanks to the development of fast computer systems, nowadays the solution of the whole problem in a single step is devised. This methodology tries to solve together the analysis of location of substations, dimensioning of substations and feeders and finally distribution networks routing [Aoki et al. 1990, Blanchard et al. 1996, Boardman, Meckiff 1985, Brauner, Zobel 1994, El-Kadi 1984,

Fawzi et al. 1983, Gönen, Foote 1981, Gönen, Foote 1982, Gönen 1986, Hindi, Brameller 1977, Hsu, Chen 1990, Lin et al. 1998, Miranda et al. 1994, Nara et al. 1991, Nara et al. 1992, Ponnaivaikko, Prakasa 1981, Quintana et al. 1993, Ramírez-Rosado, Bernal-Agustin 1998, Ramírez-Rosado et al. 1999, Ramírez-Rosado., Gönen 1991, Sun et al. 1982, Tang 1996, Thompson, Wall 1981, 70].

### 2.2. Planning horizon.

In the revised models, the plan duration can be defined as simple (one step) or as multiple (several steps).

The simple step models - usually called static models - consider that the energy demand will be static during the horizon of planning. There is no analysis of the demand growth, and there is no need to study the possible changes in substation and feeders installations through the planning period. Usually the horizon considered is one year [Adams, Laughton, 1974, Aoki et al. 1990, Crawford, Holt Jr 1975, El-Kadi 1984, Fawzi et al. 1983, Gönen, Foote 1981, Hindi, Brameller 1977, Holt Jr, Crawford 1976, Masud 1974, Sun et al. 1982, Thompson, Wall 1981, Wall et al. 1979].

In the multiperiod case researchers have opted for two methodologies:

a) A pseudodynamic one based on solving a group of problems with a single period, where each period output is the next period input plus a demand growth forecasting. As in the previous case, the optimal solution to these subproblems might be suboptimal for the whole problem, as the decisions taken in a step of the resolution cannot be modified afterwards.

b) A dynamic methodology, known as dynamic models, which try to solve the multi-period distribution system planning in a single procedure, and the building decisions for. In the dynamic methodology the decision building for several years or steps are optimised in a single procedure.

Several efforts have been made to develop more sophisticated methods to solve the multi-period distribution system planning known as dynamic models [Adams et al. 1984, Adams, Laughton, 1973, Adams, Laughton, 1974, Afuso et al. 1982, El-Kadi 1984, Gönen, Foote 1982, Gönen 1986, Masud 1978, Sun et al. 1982].

### 2.3. Voltage losses and radiality considerations

Both considerations have a great deal of importance in planning. When planning the interested is centered in obtaining a radial network of feeders, because radial networks are usually cheaper and easier to administrate, while the voltage losses are restricted by technical considerations, usually represented as a minimum allowable voltage.

The radially has not been included in some of the studied mathematical methods [Adams, Laughton, 1974, Gönen, Foote 1981, Gönen, Foote 1982, Sun et al. 1982].

Some revised models [Adams, Laughton, 1974, El-Kadi 1984, Gönen, Foote 1981, Gönen, Foote 1982, Hindi, Brameller 1977, Sun et al. 1982, Thompson, Wall 1981, Wall et al. 1979] do not include any constraint related to the minimum allowable voltage, thus creating solutions which may not be valid for real situations, as they may not deliver energy in the needed conditions.

#### 2.4. Mathematical models used.

The problem could be naturally seen as a non-linear combinatorial optimisation problem, but many researchers use linear approximations to reduce the problem. Then, the problem can be seen as a mixed integer linear programming problem [Adams et al. 1984, Adams, Laughton, 1974, Afuso et al. 1982, Aoki et al. 1990, El-Kadi 1984, Fawzi et al. 1983, Gönen, Foote 1981, Gönen, Foote 1982, Gönen 1986, Hindi, Brameller 1977, Masud 1974, Masud 1978, Nara et al. 1991, Ramírez-Rosado., Gönen 1991, Sun et al. 1982, Thompson, Wall 1981, Wall et al. 1979], and solved using the available procedures based on the simplex method. The references [Adams et al. 1984, Adams, Laughton, 1973, Afuso et al. 1982] use a dynamic programming model and [Crawford, Holt Jr 1975, Holt Jr, Crawford 1976] use graph theory related models, and solve the problem combining shortest path algorithms and transportation algorithms. It's interesting to remark that many of the revised models used for practical problems use employ Branch and Bound algorithm as their solution technique [Adams et al. 1984, Afuso et al. 1982, Fawzi et al. 1983, Gönen, Foote 1982, Hindi, Brameller 1977, Sun et al. 1982, Thompson, Wall 1981, Wall et al. 1979]. The models developed in [Adams, Laughton, 1974, Gönen, Foote 1981, Gönen, Foote 1982, Gönen 1986, Ramírez-Rosado., Gönen 1991] use straight mathematical programming formulations.

In the reviewed papers from the last years, there is a tendency to use evolutionary algorithms [Bouchard et al. 1994, Lin et al. 1998, Miranda et al. 1994, Ramírez-Rosado, Bernal-Agustin 1998, Neimane, Andersson 1999, Skrlac 1996] and expert systems [Chen, Hsu 1989, Hsu, Chen 1990, Wong, Cheung 1987, Dueire, Carvalho 1996, Tumazos 1997] as solution procedures, obtain which have achieved good results with these techniques.

Table I is presented as an annex, there the characteristics of each reviewed work is shown.

### 3. CONCLUSIONS

From the review we can obtain these conclusions:

- Due to the problem complexity, the model will always be approximated to their real counterparts.
- Most reviewed models do not include the fixed costs from the feeders.
- Many models have poor representations of the feeders, usually linearizing the losses in a single step.
- The linearization of voltage losses does not reflect the real problem.
- Most models do not consider or badly treat the voltage loss as a constraint giving non applicable results in some cases.
- Many models do not consider the demand growth on the studied period.
- Some models consider a uniform growth of the demand on the whole geographical area of study.
- Reliability is badly considered.
- A topic still not treated is the sensibility analysis on the planned system expansion to the changes in the demand forecasting. The forecasting of the demand depends on several factors and is not usually verified. More efficient procedures, including sensibility analysis would provide a method allowing a better consideration of alternatives.
- In the recent works, the greatest effort has been the development of better model approximations for solving via Artificial Intelligence procedures. Researchers involved in these developments consider that those methods are the fittest for the problem characteristics and hardness.
- Many works have only academic interest, and few have been applied to real life problems.
- Some researchers consider fuzzy formulations as a way to stop resource wastes. The definition of good levels of truth and falseness, as well as tolerable constraint violations must be defined.
- There are no works regarding the distribution system planning of urban areas.

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TABLE I

		YEAR	AUTHOR
Substations	Fixed costs	1973	Adams y Laughton
	Variable costs	1974	Adams y Laughton
	Optimal location problem	1974	Masud
	Optimal sizing problem	1975	Crawfort y Holt
	Area load transfer	1976	Crawfort y Holt
	Load x distance	1977	Hindi y Brameller
	Fixed costs	1978	Masud
	Variable costs	1979	Wall y Thompson
	Optimal routing problem	1980	Ross D.W., Carson M., Cohen A.I.
	Optimal sizing problem	1981	Gönen y Foote
Feeders	Fixed costs	1981	Ponnaivaiko y Rao
	Variable costs	1981	Wall y Thompson
	Optimal routing problem	1982	Afuso, Geréz, Rodriguez
	Optimal sizing problem	1982	Gönen y Foote
	Fixed costs	1982	Sun, Farris, Cote, Shoults
	Variable costs	1983	Fawzi, Ali, El-Sobki
	Optimal routing problem	1984	Adams, Afuso, Geréz, Rodriguez
	Optimal sizing problem	1984	El-Kady
	Fixed costs	1985	Boardman J.T., Meckiff C.C.
	Variable costs	1986	Gönen y Ramirez-Rosado
Substations and feeders	Fixed costs	1986	Mikic
	Variable costs	1987	Wong, Cheung
	Optimal routing problem	1988	Youssef H.K., Hackan R
	Optimal sizing problem	1989	Chen J., Hsu Y.
	Fixed costs	1990	Aoki, Nara, Satoh, Kitagawa
	Variable costs	1990	Hsu, Chen
	Optimal routing problem	1991	Nara, Satoh, Aoki, Kitagawa
	Optimal sizing problem	1991	Ramirez-Rosado y Gönen
	Fixed costs	1992	Kagan N., Adams R.N.
	Variable costs	1992	Nara, Satoh, Kuwabara, Aoki, Kitagawa, Ishihara
One stage (static)	Fixed costs	1993	H. Dai, Y. Yu, C. Huang, C. Wang, S. Ge
	Variable costs	1993	Quintana, Temraz, Hipel
	Optimal routing problem	1993	Carneiro M., França P.M., Silveira P.D.
	Optimal sizing problem	1995	Bouchard D.E., Salama M.M.A., Chikhani A.Y.
	Fixed costs	1994	Brauner, Zobel
	Variable costs	1994	Miranda V., Ranito J.V., Proença L.M.
	Optimal routing problem	1996	
	Optimal sizing problem	1996	Tang Y.
	Fixed costs	1996	Yahab Kobi, Oron Gideon
	Variable costs	1996	Zanoni Dueire Lins, M. Alfonso de Carvalho Jr.
Several stages	Fixed costs	1996	Skrlec D., Krajar S., Privicevic B., Blagajac S.
	Variable costs	1997	Tumazos S.
	Optimal routing problem	1997	Peponis G.J., Papadopoulos
	Optimal sizing problem	1998	Lin W.M., Su Y.S., Tsay M.T.
	Fixed costs	1998	Ramirez-Rosado I., Bernal-Agustin J.L.
	Variable costs	1999	Cannas B., Celli G.
	Optimal routing problem	1999	Ferreira L., Carvalho P., Barruncho L.
	Optimal sizing problem	1999	Ramirez I., Dominguez J., Yusta J.
	Fixed costs	1999	Neimane V., Andersson G.
	Variable costs	1999	
Mathematical Programming system			
Special Algorithm			

CCT= Shortest path and transportation  
 BB= Branch and Bound  
 PD= Dynamic programming  
 NF= Network Flow Algorithm  
 FF= Ford and Fulkerson  
 DA= Dijkstra Algorithm  
 TCA= Transshipment capacitated Algorithm  
 BE= branch exchange Algorithm  
 MSBE= Multi-stage branch exchange Algorithm  
 CFyP= Clustering and Forecasting, Planning Algorithm  
 KB= Knowledge-Based  
 ES= Expert System  
 AI= Artificial Intelligence  
 GA= Genetic Algorithm  
 MCV/FP= Multiple Capacitated Vehicle Routing Problem  
 NCA= Network Configuration Algorithm  
 TS= Tabu search