Formal Verification of Secure Information Flow in Cloud Computing

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Abstract

Federated cloud systems increase the reliability and reduce the cost of computational support to an organization. However, the resulting combination of secure private clouds and less secure public clouds impacts on the overall security of the system as applications need to be located within different clouds. In this paper, the entities of a federated cloud system as well as the clouds are assigned security levels of a given security lattice. Then a dynamic flow sensitive security model for a federated cloud system is introduced within which the Bell-LaPadula rules and cloud security rule can be captured. The rest of the paper demonstrates how Petri nets and the associated verification techniques could be used to analyze the security of information flow in federated cloud systems.

Keywords: federated cloud system, information flow security, Bell-LaPadula rules, formal model, Petri net, diagnosability, model checking.

1. Introduction

The extent and importance of cloud computing is rapidly increasing due to the ever increasing demand for internet services and communications. Instead of building individual information technology infrastructure to host databases or software, a third party can host them in its large server clouds. However, large organizations may wish to keep sensitive information on their more restricted servers rather than in the public cloud. This has led to the introduction of federated cloud computing (FCC) in which both public and private cloud computing resources are used, see Watson (2012).

A federated cloud is the deployment and management of multiple cloud computing services with the aim of matching business needs. Data, services, and software are required to be allocated in different clouds for both security and business concerns. Although federated cloud systems (FCSs) can increase the reliability and reduce the cost of computational support to an organization, the large number of services and data on a cloud system creates security risks due to the dynamic movement of the entities between the clouds. As a result, it is necessary to develop tractable formal models faithfully capturing information flow security within FCSs.

In this paper, we introduce a formal model of dynamic information flow in an FCS, where services and data can migrate and change their security status dynamically. We then explain how Petri nets (more precisely, coloured Petri nets (CPNs)) could be used to analyse the correctness of such system. We also show how one could use the notion of diagnosability investigated in Germanos et al. (2014, 2015) in order to detect malicious events violating the proposed security policy in FCSs. We also evaluate experimentally the efficiency of the proposed setup using model checking of Clarke et al. (1999).

The paper is organized as follows. Section 3 provides the basic notions about security policies. In Section 4, a model for secure information flow analysis in FCSs is presented. The basic definitions relating to Petri nets are given in Section 5. Section 6 outlines how Petri nets could be used to support property verification in FCSs. Section 7 describes the diagnosis of behavioural properties, and Section 8 presents experimental results obtained for the proposed approach. Section 9 concludes the paper.

2. Related Work

There exist different methods for addressing workflow¹ security; for example, the flow-sensitive analysis of programs in Smith (2001) and Russo et al. (2009). Using Petri nets to model workflows, Knorr (2000, 2001) applied the Bell-LaPadula model to workflow security. In particular, Knorr (2000) considered the *read* and *write* security policies. In Knorr (2001), the deployment of blocks within a workflow across a set of computational resources was not considered. In addition, the paper considered the *clearance* level but not *location* level in its embodiment of Bell-LaPadula model.

Watson (2012) proposed to partition workflows over a set of available clouds in such a way that security requirements are met. The approach is based on a multi-level security model that extends Bell-LaPadula to encompass cloud computing. Watson (2012) also indicated that workflow transformations are needed when data are communicated between clouds. However, in this study, the concurrency of the events or the execution of tasks in the system, the dynamic movement of the services, and the changes of the clearance level were not considered. Zeng et al. (2014b,a) introduced a flow sensitive security model to capture information flow in FCSs systems, which can be captured by CPNs. However, the clouds and services were assumed to be fixed, and the dynamic movement of services was not considered. Zeng and Koutny (2014) proposed a formal model for data resources in a dynamic environment focused on the location of different classes of data resources and users. However, the Bell-LaPadula rules and server-side components were not considered.

As far as we aware, there is limited work related to formal verification of security in cloud computing systems. As an example, Gouglidis and Mavridis (2013) proposed a methodology for the development and verification of access control systems in cloud computing. The authors verify the access control systems against organizational security requirements using techniques that are based on simple transition systems. As another example, Benzadri et al. (2014) employed Bigraphical Reaction Systems to formally specify cloud services and customers as well as their interaction schemes. However, they did not consider security policies.

¹Information flow refers to paths followed by data from their original positions to the end users in computational processes. Workflows are used to specify the formation/implementation of such processes.

3. Security Policies in Cloud Computing Systems

In this section, we recall some basic concepts concerning security policies in cloud computing systems.

3.1. Information Lattices

Throughout the paper, we will assume that the basis of a federated cloud is a set P of single deployment clouds. Moreover, S will denote subjects (e.g., services, programs and processes), and O will denote objects (e.g., data resources and messages). Subjects and objects will jointly be referred to as entities, and their set will be denoted by E.

We will assign a *security level* to any entity, which will in practice be related to the degree of security of its contents, as well as to any cloud which will be related to the maximal security level of the entities it can contain.

A lattice for security concerns, $\mathcal{L}_{sec} = (L_{sec}, \leq_{sec})$ consists of a set L_{sec} and a partial order relation \leq_{sec} such that, for all $l, l' \in L_{sec}$, there exists a least upper bound $l \sqcup l' \in L_{sec}$, and a greatest lower bound $l \sqcap l' \in L_{sec}$. The lattice is complete if each subset L of L_{sec} has both a least upper bound $\coprod L$ and a greatest lower bound $\coprod L$, see Denning and Dorothy (1976), Denning and Dorothy (1982), and Landauer and Redmond (1993). Following Landauer and Redmond (1993), we will assume that the security lattice \mathcal{L}_{sec} is complete.

3.2. Security Requirements: Bell-LaPadula

We adopt the Bell-LaPadula multi-level control model of Bell and Lapadula (1973), with services modelled as the subjects S, and data as the objects O, Knorr (2001). Such a security model consists of the following components:

- A set of possible access rights R. The commonly used access rights are $read\ (=r)$ and $write\ (=w)$. In addition to reading and writing, there can be other access rights, e.g., data items that can be executed and/or updated. In order to simplify the presentation, the access rights used in this paper are read and write, $R = \{r, w\}$.
- A complete lattice for security concerns, $\mathcal{L}_{sec} = (L_{sec}, \leq_{sec})$.
- An access control matrix: $B: S \times O \to 2^R$. The access control matrix issues the subjects rights to access objects. For example, if a service s_1

reads a data item d_0 , then there will be the following entry in the access control matrix: $(s_1, d_0) \mapsto \{r, \dots\}$. Similarly, if a service s_3 writes a data item d_2 , then there will be the following entry in the matrix: $(s_3, d_2) \mapsto \{w, \dots\}$. Note that the empty set is a valid function value, e.g., $(s_9, d_7) \mapsto \emptyset$ means that the subject s_9 has no access rights to the data item d_7 .

- A clearance map: $c: S \to L_{sec}$. This represents the maximum security level at which each subject (i.e., service) can operate.
- A security level map: $\ell: E \to L_{sec}$. This represents the security level of each subject and object.

The Bell-LaPadula model states that a system is secure with respect to the above model if the following conditions are satisfied for all subjects $s \in S$ and objects $o \in O$:

clearance:
$$\ell(s) \leq_{sec} c(s)$$
 (1)

no-read-up:
$$r \in B(s, o) \Rightarrow c(s) \ge_{sec} \ell(o)$$
 (2)

no-write-down:
$$w \in B(s, o) \Rightarrow \ell(o) \ge_{sec} \ell(s)$$
 (3)

For workflows, the implications of these conditions are that a subject: (i) can only operate at a security level that is less than or equal to its clearance; (ii) cannot read data that is at a higher security level than its own clearance; and (iii) cannot write data residing at a lower security level.

In the standard Bell-LaPadula model recalled above, it is implicitly assumed that the security levels of entities are fixed. However, in a typical FCS security scenario, the system moves through a set of states where these can change. We will deal with such a dynamic scenario in the rest of this paper.

As a first step, we extend the Bell-LaPadula model by assigning security levels also to clouds:

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$$\ell: E \cup P \to L_{sec}$$

Moreover, a new mapping loc is used to return the location of each entity:

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$$loc: E \rightarrow P$$

Then add an additional rule that an entity can only be deployed in a cloud with a security level that is greater than or equal to that of the entity. That is, for each entity e: an entity e is located in cloud p, then we must have

$$\ell(loc(e)) \ge_{sec} \ell(e) \tag{4}$$

4. System Model

We now introduce a formal model for capturing the dynamic behaviour of federated cloud computing systems. Such a model can then be analyzed to verify that the system satisfies the requirements of a given set of Bell-LaPadula rules, as well as the cloud security rule for confidentiality considerations and any user-specified policies.

The proposed model uses tuples to represent entities located in the clouds. Each such tuple comprises information about the nature of the entity (service or data), the security information (the security and clearance levels), and the location information (the hosting cloud). Since there can be duplicates of both services and data within a given cloud, the state of the system is a multiset of entities, allowing for an arbitrary multiplicity of any service or object. The transformations of the system are then defined through the simultaneous execution of individual actions, each action being executed instantaneously and possibly many times.

It is assumed that the system is based on a fixed set of clouds with fixed security levels (issues involved in the modelling of dynamic changes of the set of clouds as well as their security levels are discussed in Remark 4.1). It is, however, possible to model the dynamic changes of the security levels of subjects and objects as well as their creation and destruction.

To aid the understanding of the system model, it is introduced in three stages. First, we specify the overall structure in Definition 1. Then, in Definition 2, we introduce rules which explain the dynamic transformation between the system states. Finally, in Sections 4.1, 4.2, and 4.3, we specify the exact format of the three kinds of actions supported by the model.

Definition 1 (DFSSM structure). A dynamic flow-sensitive security model for federated clouds is a septuple:

$$DFSSM = (P, S, O, \mathcal{L}_{sec}, \ell, \mathcal{A}, st_{init}), \qquad (5)$$

where: P is a finite nonempty set of clouds; S is a finite nonempty set of subjects/services; O is a finite nonempty set of objects/data; \mathcal{L}_{sec} is a complete security lattice; $\ell: P \to \mathcal{L}_{sec}$ is a mapping assigning security levels to the clouds; $\mathcal{A} = \mathcal{A}_{ac} \uplus \mathcal{A}_{df} \uplus \mathcal{A}_{cf}$ is a finite set of actions, each action being a pair $\phi = (\phi^{in}, \phi^{out})$ consisting of two finite multisets over the set of tuples

$$\mathcal{M} = (S \times L_{sec} \times L_{sec} \times P) \cup (O \times L_{sec} \times P) ;$$

and st_{init} is an initial state defined as a finite multiset over \mathcal{M} . In general, a state of DFSSM is a finite multiset over \mathcal{M} , and $x \in \mathcal{M}$ is present in a state st if st(x) > 0.

A tuple $(s, l, c, p) \in \mathcal{M}$, denoted by (s, l, c)@p, represents a service s with the security level l and the clearance level c ($c \geq_{sec} l$) residing on cloud p. Similarly, a tuple $(o, l, p) \in \mathcal{M}$, denoted by (o, l)@p, represents a data item o with the security level l residing on cloud p.

An entity can have several different copies, and each of these copies can have a different security level and may reside in a different cloud. As already mentioned, we allow multiple copies of a single entity to be present in a cloud. Hence a state is a multiset st over \mathcal{M} rather than a subset of \mathcal{M} . For example, $st_8(s_6, 1, 2, p_4) = 4$ means that in the state st_8 there are four copies of service s_6 with security level 1 and clearance level 2 residing on cloud p_4 .

Now we define how the system can proceed from one state to another state by executing a multiset of actions. It is assumed that the executed (instances of) actions cannot share input entities. For example, if there is one copy of an entity present, then at most one action which has this entity in its input can be executed. This results in conflicts between actions which could potentially be executed, and contributes to nondeterminism in system execution. The formal semantics, and then property verification, take into account all possible ways in which such conflicts could be resolved.

Below (-) and (+) are respectively the multiset subtraction and addition operations.

Definition 2 (DFSSM semantics). A multiset $\Phi = \{\phi_1, \dots, \phi_n\}$ of actions over \mathcal{A} , where $\phi_i = (\phi_i^{in}, \phi_i^{out})$ for $i = 1, \dots, n$, is enabled at state st if

$$\Phi^{in} = \phi_1^{in} + \ldots + \phi_n^{in} \le st .$$

Then Φ can then be executed leading to a state st' given by:

$$st' = st - \Phi^{in} + \Phi^{out} = st - \Phi^{in} + \phi_1^{out} + \dots + \phi_n^{out}$$
.

We denote this by $st \xrightarrow{\Phi} st'$.

With such a definition we can state precisely what are the states which can be reached from the initial one.

Definition 3 (DFSSM reachable states). The reachable states of DFSSM in Definition 1 is the minimal set of states RS containing st_{init} such that if $st \in RS$ and $st \xrightarrow{\Phi} st'$, for some multiset of actions Φ , then $st' \in RS$.

DFSSM is intended to model a federated cloud system that is divided into three sub-models: the access control sub-system, the data flow sub-system, and the control flow sub-system. To reflect this division, we will now describe the format of action sets employed by these three sub-models: \mathcal{A}_{ac} (for access control), \mathcal{A}_{df} (for data flow), and \mathcal{A}_{cf} (for control flow).

4.1. Access Control Sub-system

To simplify the presentation, we will assume that a subject can only access a single object at a time. Then, in the access control sub-system, each $\phi = (\phi^{in}, \phi^{out}) \in \mathcal{A}_{ac}$ is such that:

$$\phi^{in} = \{(s, l, c)@p, (o, l')@p\} \text{ or } \phi^{in} = \{(s, l, c)@p\}$$

$$\phi^{out} = \{(s', l, c)@p, (o', l'')@p\} \text{ or } \phi^{out} = \{(s', l, c)@p\}$$

where $p \in P$, $s, s' \in S$, $o, o' \in O$, and $l, l', l'', c \in L_{sec}$. Moreover, as we need to formally capture the security policy of the cloud system, the set of actions \mathcal{A}_{ac} is composed of two subsets: the *read* actions $\mathcal{A}_{ac}^{(r)}$, and *write* actions $\mathcal{A}_{ac}^{(w)}$.

The basic form of a read action is:

$$\phi^{in} = \{(s, l, c)@p, (o, l')@p\} \text{ and } \phi^{out} = \{(s', l, c)@p, (o, l')@p\}$$

where

$$c \ge_{sec} l' \quad \& \quad \ell(p) \ge_{sec} c \sqcap l'$$
 (6)

according to the Bell-LaPadula rules (1,2) and the cloud security rule (4). Moreover, to represent destruction of objects, we allow destructive read actions of the form:

$$\phi^{in} \ = \ \{(s,l,c)@p,(o,l')@p\} \ \ \text{and} \ \ \phi^{out} \ = \ \{(s',l,c)@p\}$$

where, as before, $c \geq_{sec} l'$ and $\ell(p) \geq_{sec} c \sqcap l'$.

The basic form of a write action is:

$$\phi^{in} = \{(s,l,c)@p,(o,l')@p\} \text{ and } \phi^{out} = \{(s',l,c)@p,(o',l'')@p\}$$

where

$$l'' \ge_{sec} l \quad \& \quad \ell(p) \ge_{sec} c \sqcap l' \sqcap l'' \tag{7}$$

according to the Bell-LaPadula rules (1,3) and the cloud security rule (4). Moreover, to represent the creation of objects, we allow creation actions of the form:

$$\phi^{in} \ = \ \{(s,l,c)@p\} \quad \text{and} \quad \phi^{out} \ = \ \{(s',l,c)@p,(o',l')@p\}$$

where, as before, $l' \geq_{sec} l$ and $\ell(p) \geq_{sec} c \sqcap l'$.

4.2. Data Flow Sub-system

Objects can migrate between different clouds. Each action $\phi = (\phi^{in}, \phi^{out}) \in \mathcal{A}_{df}$ is such that:

$$\phi^{in} = \{(o, l)@p\} \text{ and } \phi^{out} = \{(o', l')@p'\},$$
 (8)

where $p, p' \in P$, $o, o' \in O$, and $l, l' \in L_{sec}$.

4.3. Control Flow Sub-system

Similarly, services can also migrate between different clouds. The last type of actions concerns the migration of the subjects in different locations. Each action $\phi = (\phi^{in}, \phi^{out}) \in \mathcal{A}_{cf}$ is such that:

$$\phi^{in} = \{(s, l, c)@p\} \text{ and } \phi^{out} = \{(s', l', c')@p'\},$$
 (9)

where $p, p' \in P$, $s, s' \in S$, and $l, l', c, c' \in L_{sec}$.

Note also that in practice the actions in \mathcal{A} can be specified in a more convenient way; for example, by using guards and parameters. This is illustrated in the Petri net representation discussed later in this paper, where net transitions use guards and arcs use parameters (variables).

Remark 4.1. The system model introduced above has been kept deliberately simple, or low-level. This should allow one to define on top of it a variety of user-friendly, and thus more practical, notations for system specification and property verification. We will demonstrate in the rest of this paper how this can be achieved.

Despite its relative simplicity, the model is very expressive and yet tractable. Basically, it is equivalent to the model of Place/Transition nets (PTNs) introduced in Section 5 which is a class of Petri nets where state reachability is decidable (it is generally accepted that PTNs are a fundamental class of concurrent system models where reachability is decidable).

One could then ask what would happen if we increased the modelling power of the basic system model. A possible extension could allow, for example, to check for the absence of certain kinds of services and/or data. This would lead, in terms of Petri nets, to the introduction of inhibitor arcs and a loss of the decidability of state reachability as PTNs extended by inhibitor arcs are Turing powerful. The same would be the case if the execution model assumed that at each step a maximal multiset of action was executed. Finally, we

conjecture that allowing dynamic creation and deletion of clouds as well as changing of their security levels would also lead to a Turing powerful model.

Therefore, as one of our aims is to keep the system model tractable, we believe that the formalisation presented above strikes a right balance between being useful for practical applications and amenable to automated verification.

4.4. System Security

We now can capture a key property of information flow across different clouds.

Definition 4. Let DFSSM be as in (5). A state st of DFSSM is secure if $\ell(p) \geq_{sec} l$ and $\ell(p) \geq_{sec} c$, for all entities (o, l)@p and (s, l, c)@p present in st. Moreover, DFSSM is secure if all its reachable states are secure.

That is, a state is secure if all copies of entities present reside in clouds without causing security violation. One can then state a general security policy guaranteeing the security of the system model. Such a policy is formulated by placing a suitable condition on the actions of the model.

Theorem 4.1. Let DFSSM be as in (5) and the following hold:

- $l' \leq_{sec} \ell(p')$, for every action $\phi \in \mathcal{A}_{df}$ as in (8), and
- $l' \leq_{sec} c' \leq_{sec} \ell(p')$, for every action $\phi \in \mathcal{A}_{cf}$ as in (9).

Then DFSSM is secure provided that st_{init} is secure.

The above result can only be applied in specific cases, e.g., when the system applies very strict security policies to the migration of data and services. In general, we need to verify that a given system specification yields a secure system, e.g., by applying a suitable model checking technique.

4.5. Well-formedness

In addition to verifying the security property of Definition 4, there are other desirable functional properties which one would normally need to verify using, e.g., model checking tools. The following are examples of such properties formulated for DFSSM in (5):

- DFSSM is live, if for every reachable state st' and every action ϕ , there is a state st'' reachable from st' at which ϕ can be executed.

- DFSSM is bounded, if there is $n \ge 1$ such that the size of each reachable state is less than n.
- DFSSM is well-formed, if there is a state st such that DFSSM is both live and bounded after replacing st_{init} by st.

5. Petri Nets

Petri nets are a graphical modelling tool for a formal description of systems whose dynamics are characterized by concurrency, synchronization, mutual exclusion and conflict. In this section, we briefly recall three classes of Petri nets used in our discussion (see Reisig (1985) and Jensen (2009) for more details).

5.1. Place/Transition Nets

A Place/Transition net (PTN) N consists of two disjoint finite sets of nodes, Pl and Tr, respectively called *places* and *transitions*, a mapping W: $(Pl \times Tr) \cup (Tr \times Pl) \rightarrow \mathbb{N}$ specifying the weights of *arcs* that connect the nodes, and the *initial marking* (state) $M_0: Pl \rightarrow N$. In general, any finite multiset of places is a marking (or state) of N.

Intuitively, places carry (black) *tokens* which represent the current distribution of resources in a system modelled by the net. In other words, the current state of the modelled system is given by the number of tokens in each place.

Transitions are the active components of the net. An input arc of a transition tr starts at a place pl and ends at tr provided that n = W(pl, tr) > 0. In such a case, n is the arc's weight signifying that an execution of tr requires n tokens in pl which are consumed as a result. Similarly, an output arc from tr to pl exists provided that m = W(tr, pl) > 0, and an execution of tr inserts m tokens into pl.

A transition tr is allowed to be executed (or fired) at a marking M if $M(pl) \geq W(pl, tr)$, for all places pl. Its firing produces a new marking M' such that M'(pl) = M(pl) - W(pl, tr) + W(tr, pl), for all places pl. In general, one can fire a finite multiset of transitions $U = \{tr_1, \ldots, tr_k\}$ provided that $M(pl) \geq W(pl, tr_1) + \cdots + W(pl, tr_k)$, for all places pl (that is, input tokens cannot be shared), and its firing results in a marking M' such that $M'(pl) = M(pl) - W(pl, tr_1) - \cdots - W(pl, tr_k) + W(tr_1, pl) + \cdots + W(tr_k, pl)$, for all places pl. One can then consider finite and infinite execution sequences

starting from the initial marking, and introduce the notion of a reachable marking.

Petri nets, in particular PTNs, have been widely used for structural modelling of workflows and have been applied in a wide range of qualitative and quantitative analyzes (see, for example, van der Aalst (1996, 1997, 1998)). A Petri net representing a workflow has, in particular, the following characteristics:

- Workflow activities are represented by net transitions, and executing an activity corresponds to the firing of a transition.
- Net markings represent the states of the corresponding workflow. Each token represents a control flow point of one of the concurrent processes described by the workflow, or an existing data resource.

5.2. Coloured Petri Nets

PTNs are a low-level model, and in practical applications, it is convenient to use more compact (but behaviourally equivalent) high-level Petri net models. An example of such a compact model are *coloured Petri nets* (CPNs), where the tokens are tuples of values, the arcs are used as selectors allowing one to specify the format of input and output tokens, and transitions have associated *guards* which allow one to easily express, e.g., various security policies.

Let Tok be a finite set of elements (or colours) and VAR be a disjoint finite set of variable names. In a CPN:

- Each place has a *type*, which is a subset of *Tok* indicating the colour of tokens this place can contain. A marking is obtained by placing in each place a multiset of tokens belonging to the type of the place.
- Each arc is labelled with a multiset of variables from VAR.
- Each transition has a *guard*, which is a Boolean expression over $Tok \cup VAR$. For a transition t, VAR(t) denotes the set of variables appearing in its guard and labelling its input and output arcs.

The enabling and firing rules of coloured Petri Nets are as follows: when tokens flow along the incoming arcs of a transition t, they become bound to variables labelling those arcs, forming a binding mapping $\sigma: VAR(t) \to Tok$.

If this mapping can be extended to a total mapping σ' in such a way that the guard of t evaluates to true and the values of the variables on the outgoing arcs are consistent with the types of the places these arcs point to, then t is enabled and σ' is an enabling binding of t. An enabled transition can fire, consuming the tokens from its pre-set and producing tokens in places in its post-set, in accordance with the values of the variables on the appropriate arcs given by σ' . One can then define an enabling condition and firing rule for a multiset of transitions with enabling bindings similarly as it was done for PTNs, and introduce notions like marking reachability by generalizing those defined for PTNs.

5.3. Labelled Petri Nets

The class we need allows one to describe properties related to *observability* of executed transitions.

A labelled Petri net (LPN) is a triple $\mathcal{N} = (N, X, lab)$ such that N is an unlabelled net; X is a finite set of labels; and $lab : Tr \to X \cup \{\epsilon\}$ is a labelling function, and ϵ is the empty word. The labelling function associates to each transition tr a label lab(tr) indicating how tr is observed by an external environment. In particular, $lab(tr) = \epsilon$ means that tr is invisible, or internal to the computing system represented by \mathcal{N} .

6. Dynamic Flow-sensitive Security Model in CPNs

We will now outline how CPNs could be used to represent (and then used to verify) a given DFSSM. To facilitate the discussion, following the definitions in Section 4, the net modelling DFSSM is decomposed into three parts: the access control sub-net, data flow sub-net, and control flow sub-net.

6.1. Access Control Sub-net

Fig. 1 shows the structure of the access control sub-net, representing the interactions of the subjects and objects residing on the same cloud. Data destruction and creation can be represented by simplified versions of the read and write transitions (one only needs to delete the arrows from read to the lower place, and from the lower place to write). In this diagram, tokens represent entities; places represent different clouds; and transitions capture the activities and security rules (see Section 4.1). s, 1, etc., are parameters (variables), and f, f', g, h are application specific partial functions used to capture ongoing computations and the resulting changes to data values and

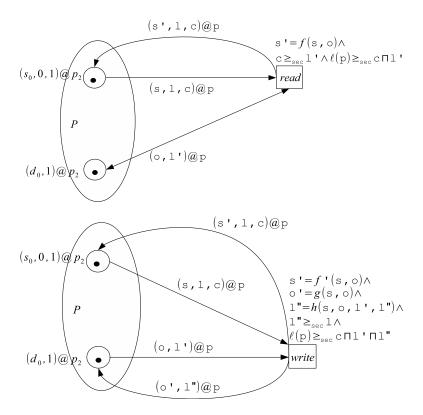


Figure 1: Basic structure of the access control sub-net. It shows one subject and one object, both residing on the same cloud, p_2 . Note that $\mathfrak{s}, \mathfrak{l}$, etc., are parameters (variables), and f, f', g, h are partial functions. Note that places are represented by circles, transitions by boxes, and a double-headed arc represents two arcs with the same label pointing in opposite directions.

services. Since f, f' are partial functions, they can be used to filter out pairs (s, o) for which there is no read and/or write access. Moreover, s' = f(s, o) checks whether a service can read data or not, and 1'' = h(s, o, 1', 1'') specifies that after a service writes data, the security level of the data will be changed from l' to l'', and o' = g(s, o) specifies how the new data value is calculated.

6.2. Data Flow and Control Flow Sub-nets

We will now use an example to illustrate the definition of a dynamic flowsensitive security model, and the way it can be represented using coloured Petri nets.

We consider two public clouds, p_0 and p_1 , and one private cloud, p_2 . The security levels of clouds, services, and data are listed in Table 1. As services and data can be deployed on different clouds, Table 2 shows all the valid mappings of entities to clouds. We can observe, e.g., that both s_0 and s_1 can be deployed on p_0 , p_1 , and p_2 . However, the data item d_0 can only be deployed on cloud p_2 .

Table 1: Security level of clouds, services and data in the DFSSM.

Services	Security level	Clearance level
s_0	0	1
s_1	0	0
Data	Security level	
d_0	1	
d_1	0	
d_2	0	
Clouds	Security level	
p_0	0	
p_1	0	
p_2	1	

We assume that in the initial state of the system there is one data item, d_0 , and two services, s_0 and s_1 , all residing on cloud p_2 . Moreover, in this example we assume that the functions f, f', g, h do not change the values associated with the entities except that $g(s_0, d_0) = d_1$, $h(s_0, d_0, 0, 1) = 0$ and $g(s_1, d_1) = d_2$. That is, service s_0 can re-write the data item d_0 into d_1 and reduce its security level to 0, whereas service s_1 can re-write d_1 into d_2 .

The structure and dynamics of the system are represented by the coloured Petri net in Fig. 2. Note that here and later, the access control sub-net (on

Table 2: Valid mappings of entities to clouds

Entities	$\frac{\text{Cloud } p_0}{\text{Cloud } p_0}$	Cloud p_1	Cloud p_2
s_0	•	•	•
s_1	•	•	•
d_0			•
d_1	•	•	•
d_2	•	•	•

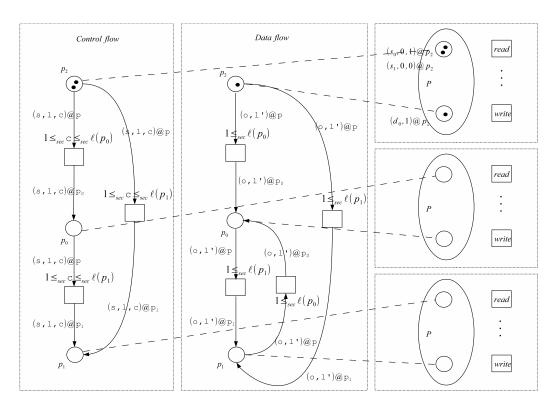


Figure 2: A Petri net model of a system consisting of clouds p_0 , p_1 and p_2 , as well as two services, s_0 and s_1 , and one data item, d_0 , all residing on cloud p_2 .

the right) is represented schematically (see Fig. 1 for its internal details). Note that places are labelled with the names of the corresponding clouds, and a dashed line joins two duplicate depictions of the same place.

The two services s_0 and s_1 are represented by two tokens in place labelled as p_2 in control flow, one token being $(s_0, 0, 1)@p_2$ and the other $(s_1, 0, 0)@p_2$. The leftmost sub-net (control flow sub-net) shows how the services can migrate between different clouds. Note that the security policy for service migration is represented by the guards of the form $1 \leq_{sec} c \leq_{sec} \ell(p_1)$ associated with the transitions in the control flow sub-net (see Section 4.4).

The data resources are represented by a single token, $(d_0, 1)@p_2$, inside another place labelled p_2 (belonging to the data flow sub-net). It follows from the security levels of the data resources and clouds that such a resource can never enter p_0 or p_1 . Note also that the security policy for data migration is represented by the guards of the form $1 \leq_{sec} \ell(p_0)$ associated with the transitions in the data flow sub-net (see Section 4.4).

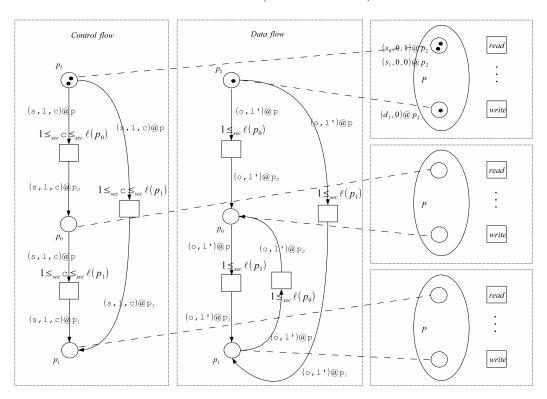


Figure 3: A reachable state of the system with s_0 , s_1 , and d_1 residing on cloud p_2 .

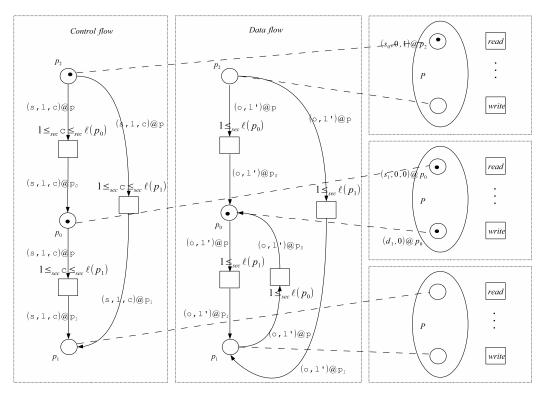


Figure 4: A reachable state of the system with s_1 and d_1 residing on cloud p_0 ; and s_0 residing on cloud p_2 .

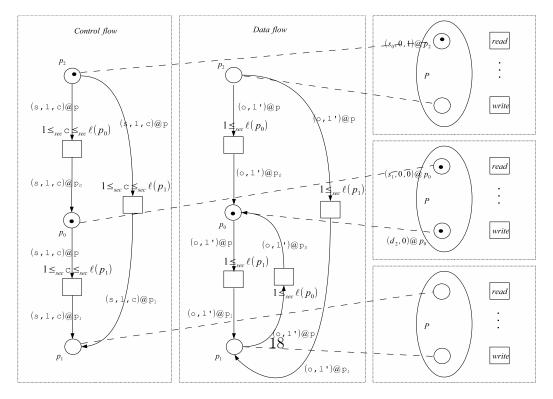


Figure 5: A reachable state of the system with s_1 and d_2 residing on cloud p_0 ; and s_0 residing on cloud p_2 .

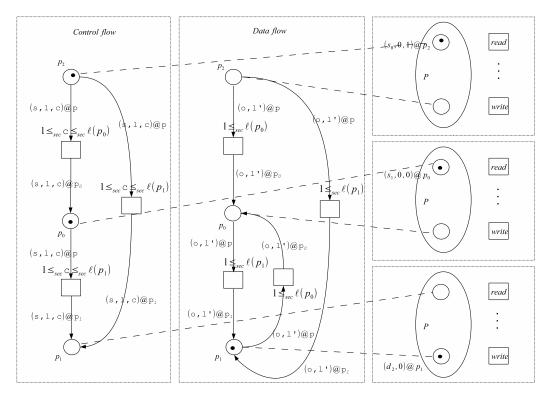


Figure 6: A reachable state of the system with s_1 residing on cloud p_0 ; d_2 residing on cloud p_1 ; and s_0 residing on cloud p_2 .

We can then illustrate the dynamic behaviour of the system modelled by CPN using a series of diagrams depicting four reachable states: (i) Fig. 3: after service s_0 re-wrote d_0 to d_1 on cloud p_2 ; (ii) Fig. 4: after service s_1 and data d_1 migrated from cloud p_2 to cloud p_0 ; (iii) Fig. 5: after service s_1 re-wrote d_1 to d_2 on cloud p_0 ; and (iv) Fig. 6: after data d_2 migrated to cloud p_1 .

In general, a CPN model like that outlined above can be translated into a behaviourally equivalent model as in (5) (essentially, each transition tr is replaced by a set of actions obtained from the enabling bindings of tr). Similarly, each system model as in (5) can be translated into behaviourally equivalent CPN. It is then possible to apply model chacking tools developed for CPNs to reason about security aspects in FCSs. In this paper, we do not follow this fairly standard path of development, and in the last part we introduce concepts and analytical techniques which can be applied to diagnose the presence of faults in FCSs which impact of the security properties. To

the best of our knowledge, this is the first study of this kind.

7. Diagnosis and WF-diagnosability

In this section, we outline the diagnosis and weakly fair diagnosability property. This formal verification technique will be used in Section 8.

Diagnosis is the procedure of discovering abnormal behaviours of a system, and diagnosability is an associated property of, e.g., a Petri net stating that in any possible execution sequence (called below executions) an occurrence of a fault can eventually be diagnosed. Sampath et al. (1995) proposed a method for diagnosability based on the construction of a diagnoser automaton that allows one to estimate states of the system by observing executions. Subsequent improvements were introduced in Jiang et al. (2001) and Schumann and Pencolé (2007), where the basic idea was to build a verifier by constructing the product of the system with itself through synchronisation on observable transitions. If the system is given as an LPN, then the verifier can be constructed directly (see Madalinski and Khomenko (2010)), and the problem reduces to model checking of a fixed property expressed in LTL-X (see Pnueli (1977) and Lamport (1983)). Subsequently, Haar et al. (2003) proposed the weak diagnosis which is in fact more powerful than the standard diagnosis as in Benveniste et al. (2003). Based on the weak diagnosis, the weakly fair diagnosability verification property was proposed in Agarwal et al. (2012) and then improved in Germanos et al. (2014).

7.1. Petri Nets and Diagnosability

The system under consideration is modelled by an LPN \mathcal{N} . Transitions are partitioned into observable and invisible, i.e., the labelling function lab maps transitions to $Obs \cup \{\varepsilon\}$, where Obs is an alphabet of observable actions and $\varepsilon \notin Obs$ is the empty word representing invisible action. This labelling function lab can be applied to finite and infinite executions, projecting them onto words in Obs^* or Obs^{ω} . We assume that the \mathcal{N} is free from deadlocks and divergencies, i.e., every execution can be extended to an infinite one, and every infinite execution has infinitely many observable transitions. Some of the invisible transitions are designated as faults. An example in Fig. 7 has observable transitions t_3 , t_4 , and t_5 with $lab(t_3) = a$, $lab(t_4) = b$ and $lab(t_5) = tick$ (the other transitions are unobservable, i.e., invisible). Note that we represent faults by black boxes, and the observable transitions are shaded.

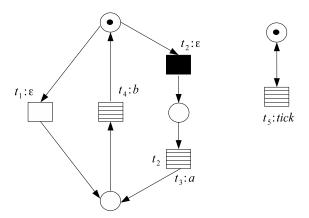


Figure 7: An undiagnosable LPN which would be diagnosable without t_5 . Making t_3 WF makes the LPN diagnosable.

7.1.1. Standard diagnosability

Given a finite execution ψ of \mathcal{N} , the observer sees $lab(\psi) \in Obs^*$, and only on this basis needs to conclude whether some fault transition tr has occurred in ψ . In a diagnosable system, once a fault has occurred, the observer is able to eventually detect this fact. That is, provided that the suffix of ψ after the first occurrence of a fault is sufficiently long, the observer should be able to conclude that each execution ρ with $lab(\rho) = lab(\psi)$ involves a fault which has either already occurred or will definitely occur in future.

Definition 5 (Diagnosability). \mathcal{N} is diagnosable if for all infinite executions ψ and ρ such that $lab(\psi) = lab(\rho)$, ψ contains a fault iff ρ contains a fault.

For example, the LPN in Fig. 7 is not diagnosable. Indeed, one can only conclude that fault has occurred after observing a. However, the infinite execution $t_2t_5^{\omega}$ contains a fault but never fires t_3 . If t_5 is removed, the LPN becomes diagnosable.

7.2. Weak Fairness

The example of Fig. 7 exhibits a pathological property of the standard notion of diagnosability: a diagnosable system ceases to be such simply because of some unrelated concurrent activity. In practice, it is often reasonable to assume that the system cannot perpetually ignore an enabled transition. Then LPN Fig. 7 becomes diagnosable, by disallowing the infinite execution $t_2t_5^{\omega}$.

One can capture this idea using weak fairness (see Vogler (1995)). First, the designer specifies transitions which cannot be postponed indefinitely, designating them as weakly fair (WF). An infinite execution ψ is then weakly fair (WF) if, for each WF transition tr, if tr is enabled after some prefix of ψ then the rest of ψ contains at least one transition in confl(tr), where confl(tr) is the set of all transitions $tr' \neq tr$ sharing an input place with tr, see Fig. 8. Moreover, all finite executions are regarded as WF. One than takes the WF executions as a refined semantics of the net, i.e., other executions are considered impossible. Coming back to the example in Fig. 7, if t_3 is WF then the execution $t_2t_5^{\omega}$ is not WF and thus disallowed, and so the LPN becomes diagnosable.

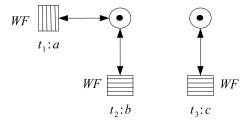


Figure 8: (i) The execution $(t_1t_2t_3)^{\omega}$ is WF as no enabled transition is continually ignored by it. (ii) The execution $(t_1t_2)^{\omega}$ is not WF as t_3 is enabled but all the transitions in $confl(t_3) = \{t_3\}$ are continually ignored. (iii) The execution $(t_1t_3)^{\omega}$ is WF: even though t_2 is continually ignored, $t_1 \in confl(t_2) = \{t_1, t_2\}$ is fired.

Definition 6 (WF-diagnosability). \mathcal{N} is WF-diagnosable if each infinite WF execution ψ containing a fault has a finite prefix $\hat{\psi}$ such that every infinite WF execution ρ with $lab(\hat{\psi}) < lab(\rho)$ contains a fault.

The way of constructing a verifier corresponding to WF-diagnosability was described in Germanos et al. (2014). Using it, we can check the satisfaction of an LTL-X formula that captures the WF-diagnosability property.

8. Experimental Results

We now present experimental results relating to the diagnosis of potential actions of malicious insider in a cloud computing systems.

We use three scalable benchmarks based on the model shown in Fig. 2. To keep the model simple, we do not consider how the interaction between entities (tokens in the PN model) inside clouds are related to the security

rules (1), (2), and (3). Instead, we evaluate the cloud security rule (4) which states that an entity must be deployed on a cloud with a security level that is greater than or equal to that of the entity. In other words, an entity can move to another cloud according to its security permission. We then assume that a malicious insider can move some entities to unauthorised clouds. This should, clearly, be detected and addressed by the cloud management system.

For the verification task, we used the Maria toolset (see Mäkelä (2005)). Its on-the-fly model checker verifies properties expressed in temporal logic by computing the product of a property automaton and the reachability graph of an LPN interpreted as automaton. Benchmark representations in Maria input language are available from the authors upon request.

DFSSMCLOUD (n#S, n#D). Fig. 9 shows an LPN modelling the system comprising three clouds, p_0 , p_1 and p_2 . Cloud p_2 contains n services (indicated by (n#S)) and n data items (indicated by (n#D)). These entities can be distributed to clouds p_0 and p_1 , according to some predefined security policy respecting DFSSM, via transitions t_1 and t_3 , respectively. Also, services and data can flow from cloud p_2 to cloud p_1 directly via transition t_2 . It should be noted that both services and data can flow from cloud p_2 to clouds p_0 and p_1 , and, similarly, from cloud p_0 to cloud p_1 . However, from cloud p_1 to cloud p_0 only data can flow. Thus, eventually, cloud p_2 will become empty, as only data can move from cloud p_1 to cloud p_0 and vice versa, and services will stay in cloud p_1 unable to be transferred to other clouds (p_2 and/or p_0).

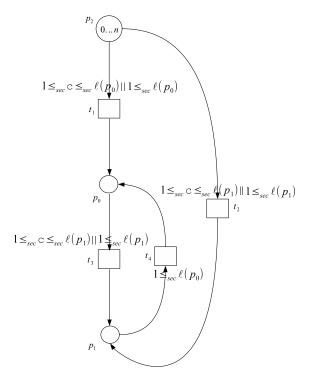


Figure 9: The DFSSMCLOUD benchmark, which corresponds to the net in Fig. 2. The nets of *Control Flow* and *Data flow* are merged into a single net.

DFSSMCLOUDINS (n#S, n#D). Fig. 10 shows the previous system with a malicious insider represented by a black transition t_5 . The actions of the insider are invisible and they can move services and data from cloud p_2 to p_3 . If this happens, then no entities will be moved from cloud p_2 to cloud p_1 via cloud p_0 , or directly to cloud p_1 via transition t_2 . Although cloud p_3 can send entities to cloud p_1 , the type of entities it can send is restricted to services. Thus, if an attack occurs, no data can be sent to cloud p_0 as it was expected, and it will finally remain empty. Moreover, even if the services can be transferred to cloud p_1 from cloud p_3 , it is not guaranteed that they have not been modified by the malicious insider, making the entities untrustworthy.

NoDfssmCloudIns (n#S, n#D). Fig. 11 is similar to Fig. 10 except that it does not model a Dfssm cloud system because we removed the security policy. In the right-hand side of this figure we can see the corresponding verifier. Its purpose is to check whether the WF-diagnosability property holds, i.e., that a malicious event can be eventually detected.

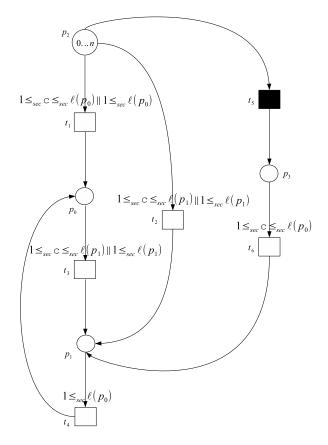


Figure 10: The DfssmCloudIns benchmark. The black transition indicates malicious behaviour in the system.

Initially, we verify that the security rule (4) holds in Fig. 9. The specific property for this case is captured by the LTL-X formula $\phi_1 = \Box \Diamond p_0$, i.e., data will always be sent to cloud p_0 . This is achieved by assigning security guards in the transitions which allow specific entities to move to each cloud.

The next case is to verify that the action of the malicious insider (see Fig. 10) can be detected due to the introduced dynamic flow-sensitive security policy. Here, we check again whether p_0 will eventually contain some data using the same LTL-X formula as previously. In this case, the formula is violated as it is possible for cloud p_1 to contain only services and cloud p_3 to contain only data.

In the last case, we remove the security policy turning the system into a standard cloud system with a malicious insider. In such a case, we are able

to detect the malicious action by applying diagnosis. To this end, we build a corresponding verifier (Fig. 11), as explained in Germanos et al. (2014), and check whether the WF-diagnosability property holds. It should be noted that in this model the transitions do not have guards to ensure that the security policy holds. Checking the WF-diagnosability property, the detection of a malicious insider becomes more 'expensive' in verification time. That is, each time the size of the model is increased, the state space of the verifier is increased significantly. We are therefore assured that a malicious action can be detected. In our case, we verify the following WF-diagnosability property

$$\phi_{diag} = \Box \, \overline{p}_2 \lor \Diamond \neg \, stub_monitor$$

This property states that our cloud computing system is diagnosable, meaning that a malicious action can be detected, if \bar{p}_2 is always marked or eventually the place $stub_monitor$ is empty. This is necessary because if the faulty transition t_5' fires, the WF stub transition will be enabled, and after firing the place $stub_monitor$ will become empty indicating the occurrence of a malicious action. Similarly, if transition t_5 fires then the place \bar{p}_2 becomes empty indicating the malicious action. Thus, a counterexample is an infinite WF execution containing a malicious action but no stubs.

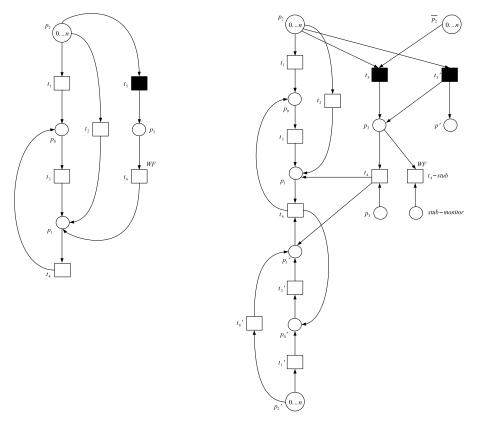


Figure 11: The NoDfssmCloudInsbenchmark (left) and the corresponding verifier (right). The black transition indicates malicious behaviour.

The experimental results are summarised in Tables 3, 4, and 5, where the meaning of the columns is as follows (from left to right): the name of a benchmark, the verification time, and the number of states. The time is measured in seconds. All experiments were conducted on a PC with 64-bit Windows 7 operating system, an Intel Core i7 2.8 GHz Processor with 8 cores and 4GB RAM (no parallelisation was used for the results in this table). The MARIA tool has confirmed that the verification property of each benchmark holds.

Benchmarks	Vrf Time	Number of states
Design Design (1#S, 1#D)	0.047	9
Designation Designation Designation Designation $(2\#S, 2\#D)$	0.046	31
Desimed Design (3#S, 3#D)	0.062	65
Desimed Design (4#S, 4#D)	0.062	111
Design De	0.077	169

Table 3: Experimental results for DfssmCloud benchmark.

Benchmarks	Vrf Time	Number of states
Design Design (1#S, 1#D)	0.12	15
Design Clouding $(2\#S, 2\#D)$	0.20	78
Design D	0.31	263
Design De	0.46	681
DfssmCloudIns (5#S, 5#D)	0.71	1479

Table 4: Experimental results for DfssmCloudIns benchmark.

Benchmarks	Vrf Time	Number of states
NoDessmCloudIns (1#S, 1#D)	0.11	315
NoDessmCloudIns (2#S, 2#D)	1	2772
NoDessmCloudIns (3#S, 3#D)	6	13500
NoDfssmCloudIns (4#S, 4#D)	39	47025
NoDessmCloudIns (5#S, 5#D)	79	131859

Table 5: Experimental results for NoDfssmCloudIns benchmark.

COMPARISON OF VERIFICATION TIME

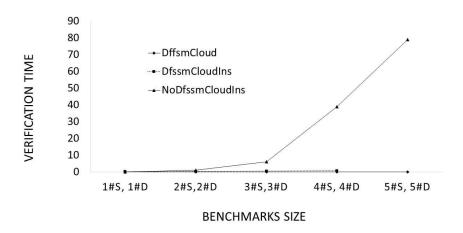


Figure 12: Verification time increases dramatically when the number of services and data in NoDfssmCloudIns becomes larger. The verification times of DfssmCloud and DfssmCloudIns are almost the same.

COMPARISON OF NUMBER OF STATES

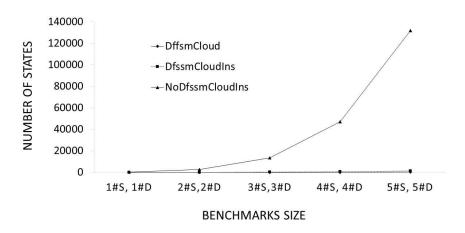


Figure 13: The state space increases dramatically when the number of services and data in NoDfssmCloudins becomes larger. The state space of DfssmCloud and DfssmCloudins are almost the same.

Fig. 12 and Fig. 13 compare verification times and state space for the

benchmarks. We can observe that in a standard cloud system the verification of diagnosability increases significantly with the size of the system.

9. Conclusions

In this paper, we presented a dynamic flow-sensitive security model which can be used to analyze the information flow in FCSs. The entities present in the cloud system can be assigned different security levels belonging to a given security lattice. Moreover, each cloud is assigned a security level which captures the confidentiality level of the cloud. It is also possible to specify in a formal way different security policies for the movement of entities between different clouds. The resulting formal model can then be represented by a suitable CPN, and its dynamic behaviour analyzed using the existing verification methods and tools developed for Petri nets. We also discussed how diagnosability under weak fairness could be used to detect malicious intruders within an FCS.

10. Acknowledgments

We would like to thank the referees for their comments and useful suggestions. This research was supported by the 973 Program Grant 2010CB328102, NSFC Grant 61133001, and EPSRC UNCOVER project.

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