

1 Pollen Segmentation and Feature Evaluation for
2 Automatic Classification in Bright-field Microscopy

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27 **Abstract**

Besides the well-established healthy properties of pollen, Palynology and apiculture are of extreme importance to avoid hard and fast unbalances in our ecosystems. To support such disciplines computer vision comes to alleviate tedious recognition tasks. In this paper we present an applied study of the state of the art in pattern recognition techniques to describe, analyze, and classify pollen grains in an extensive dataset specifically collected (15 types, 120 samples/type). We also propose a novel contour-inner segmentation of grains, improving 50% of accuracy. In addition to published morphological, statistical, and textural descriptors, we introduce a new descriptor to measure the grain's contour profile and a logGabor implementation not tested before for this purpose. We found a significant improvement for certain combinations of descriptors, providing an overall accuracy above 99%. Finally,

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Preprint submitted to Computers and Electronics in Agriculture September 22, 2014

some palynological features that are still difficult to be integrated in computer systems are discussed.

28 *Keywords:* Apiculture, pollen, automatic classification, bright-field
29 microscopy, feature extraction, Fisher discriminant analysis, image
30 processing, morphology descriptors, statistical descriptors, texture
31 descriptors.

32 **1. Introduction**

33 A grain of pollen contains the male vegetative and generative cells re-
34 quired for fertilization of plants to ensure the development of seeds and con-
35 sequently the life of plants. The study of pollen, palynology, is therefore
36 of great interest in so diverse disciplines such as archeology, paleontology,
37 forensics, health (allergies) or agriculture (bee products, and crop forecast).
38 Specifically, bee pollen is collected by worker honey bees which is used as
39 food for the entire colony. For humans it is one of the richest and purest
40 natural foods, with an incredible nutritional and medicinal value [1, 2] and
41 one of the most interesting facts about bee pollen is that it cannot be syn-
42 thesized in a laboratory. The main nectar source and main pollen source
43 differ widely with latitude, region, season, and type of vegetation, where in
44 scarce nectar periods bees can harvest far away up to 3 km, i.e., in an area of
45 300-2800 hectares [3]. This reflects their large pollination capacity and the
46 maintenance of plant diversity which directly influences important human
47 activities like agricultural and forestry production. Furthermore, bees are
48 the most common pollinators with strong influence on ecological relation-
49 ships, ecosystem conservation, and stability, genetic variation in the plant
50 community, biodiversity, specialization, and evolution [4].

51 The pollen grains manifest a great variety of shapes, sizes, and ornamen-
52 tation and their description is genetically bound to their botanical family.
53 Externally, pollen grains are protected by a resistant wall called sporoderm,
54 conformed by an internal layer named intine and an outer layer named ex-
55 ine, where the latter exhibits in its surface distinct morphological structures
56 according to the pollen type. Generally, most of them are spheroidal in equa-
57 torial view, varying between oblate spheroidal and prolate spheroidal in the
58 range of 8-100 μm .

59 In the human activities previously mentioned a correct pollen identifica-
60 tion is vital in terms of production, bio-preservation, or simply knowledge
61 achievement. The recognition can be accomplished through different tech-
62 niques which in general are time consuming and require highly trained paly-
63 nologists who must analyze manually thousands of individual pollen grains:
64 Fourier transformed infra-red from attenuated total reflectance (FTIR-ATR)
65 spectroscopy represents a useful technique for identifying chemical struc-
66 tures [5]; and Polymerase Chain Reaction (PCR) is a recent method for
67 pollen authenticity based on molecular analysis. PCR technique stands out
68 for its specificity for botanical identification. Nevertheless both techniques
69 are expensive in terms of equipment and reagents, and requires several pro-
70 cessing days. Finally, the most common and affordable technique is bright-
71 field microscopy. This technique is time consuming too and therefore many
72 efforts have been put on automated classification systems. However it re-
73 mains a challenge to provide accurate pollen classifications in real scenarios.
74 For a recent study that provides a comparison of the microscopy techniques,
75 see [6].

76 The first attempt to automate pollen recognition was conducted in 1968
77 by Flenley by [7], who identified two difficulties attached to bright-field mi-
78 croscopy: images partially focused and multiple grain orientations (views).
79 Both are related with the reduction of 3D objects into 2D captures. The
80 depth of field of optical systems allows visualization of specimens partially in
81 focus. Here, the use of multifocus stacks and recent multifocus fusion tech-
82 niques [8] could eventually provide more details about pollen's surface, but
83 the way of collecting information is still an open issue. On the other hand,
84 morphology, surface ornamentation, and pori layout are strong indicators of
85 the pollen type, but such information strongly vary with the point of view.

86 Besides these inherent difficulties in capturing 3D features into 2D, two
87 main obstacles hamper the current progress in this field: a) the extraction of
88 knowledge from expert palynologists and b) the limited access to open pollen
89 databases with a large number of reference pollen per taxa. A previous work
90 in the area of aero-palynology (ASTHMA EU project) used multifocus stacks
91 and reported recognition rates around 97% for 5 pollen types [9]. Other
92 studies demonstrate accuracy ratios between 90-97% [10, 11, 12, 13, 14].
93 However, such ratios must be considered with care, they are not reliably
94 comparable because their training database usually differ largely in terms of
95 pollen genre and/or number of training samples, which is directly related to
96 obstacle b).

97 Most of these approaches, if not all, perform morphological and cer-
98 tain statistical description of gray-levels like mean, median, variance, en-
99 tropy,...etc. Some modern approaches incorporate more sophisticated de-
100 scriptors through spatial correlations like the Haralick's co-occurrence ma-

101 trices [15]. For instance, Zhang proposed Gabor transforms and invariant
102 moments [16], Rodriguez-Damian et al. [17] evaluated Fourier descriptors
103 and Run-Length Statistics, Chen et al. [11] incorporated a description of
104 the number of pores and recently Ronneberger et al. proposed 3D invariant
105 moments [18]. An interesting and profuse thesis can be consulted in [19].

106 In some applications, e.g. images from ambient air, a previous image
107 cleaning from dirt, fungal spores and other non-pollen particles [20] is re-
108 quired. This is also a time consuming process where a robust automatic
109 segmentation is a challenging problem.

110 In this paper we present a complete applied study of segmentation, de-
111 scription, and classification of bee pollen, reviewing the state of art and
112 proposing some novel techniques. For that, within the EU-funded project
113 APIFRESH, we recollected an important data base of 15 pollen types with
114 120 samples per type described in Sec. 2. Under the hypothesis that contour
115 and inner of grains typically manifest disparate statistical distributions, we
116 proposed in Sec. 3 a novel segmentation to apply descriptors separately across
117 these two regions. In Sec. 4 an important exercise of knowledge transfer is
118 done from palynology to computer vision together with a complete list of
119 descriptors. Sec. 5 and Sec. 6 describe classification strategies and classifiers.
120 Finally experimental results are presented in Sec. 7 and Sec. 8 concludes the
121 paper addressing unresolved challenging problems.

122 **2. Materials & Preparation: collecting database**

123 Bees collect pollen aggregated in balls and normally of the same pollen
124 type, which guarantees a certain corresponding hue. Therefore, balls were

125 separated in the laboratory and individualized by color tonality and then
126 labeled with a color code according to the Universal Code Guide PANTONE
127 747XR. Although pollen can share color, each color corresponds to a pollinic
128 type and a pollinic type can be matched to a larger group of plants (a family),
129 to a middle group of plants (some genera from the same family), to a reduced
130 group of plants (a genus) or more rarely to one species. Balls collected
131 from the same place of origin were classified in colors and for each color
132 we selected 25 pollen balls. Balls were dissolved with glycerogelatin drops
133 and prepared in slices sealed with a coverslip. Through the microscope each
134 botanical group has characteristic features that differentiate it from others
135 like morphology, surface structures or pori layout. For a summarized featured
136 list of the pollen types studied here consult the appendix in Sec. 9.

137 Although multiple studies have already evaluated a wide range of pollen
138 descriptors, most of them have been done with a reduced dataset and/or a
139 reduced number of pollen types. Without a doubt one of the major efforts in
140 this kind of studies has to do with the compilation, preparation and labeling
141 of datasets. Thus, some of those studies deal with 300-500 total samples
142 and/or 3-5 pollen types [10, 11, 9, 21, 22, 12]. The study from Chica [13]
143 is one the most complete in this respect with 5 pollen types and 1063 total
144 pollen grains. But one impressive case is Ronneberger et al. [14] with 180
145 000 airborne particles and 22 700 pollen grains. In this case study, we have
146 done an important effort to collect a considerable dataset in order to test
147 computer vision algorithms focused on a real automated pollen classifier.

148 The 15 pollen types studied were collected mostly from Spain (Guadala-
149 jara, Toledo, La Rioja, Madrid and Cantabria). Other types like *Aster* and

150 *Castanea* came from Italy (Grosseto, Cosenza and Asti), *Helianthus* from
 151 Bulgaria and *Teucrium* from Turkey. They are enumerated in Tab. 1 and
 152 some examples are depicted in Fig 1. Neither type is endemic, which means
 153 that their presence is common along the whole Mediterranean territory and
 154 some of them are present all over the planet. Besides, none of them comes
 155 from plants commonly cultivated.

Pollen types	<i>Aster, Brassica, Campanulaceae, Carduus, Castanea, Cistus, Cytisus, Echium, Ericaceae, Helianthus, Olea, Prunus, Quercus, Salix, Teucrium</i>
Magnification	×40
Original captures	2560×1920 RGB pixels
Cropped grains	from 200 to 600 gray pixels of width and height (variable aspect ratio)
Type grains	120 images/type
Total samples	1 800 images (grains)

Table 1: Pollen database description.

156 A NIKON E200 microscope (fluoride objective) and a camera NIKON DS-
 157 Fi1 were employed to capture the images. Auto-white background balance
 158 was previously carried out for every slice capture with the NIS-Elements
 159 Nikon software. In Fig. 2 a capture and a example of manual cropping is
 160 shown. See Tab. 1 for specifications of the captured and cropped images.

161 Every sample was manually cropped to ensure an effective surrounding
 162 region with no nearby samples or debris, so cropped image samples are not
 163 necessarily square. To ensure an optimum focus, every acquisition included a
 164 31-stack image where only the best focused slice was included in the dataset.
 165 This best focus was again manually selected. These stages and their automa-
 166 tion are beyond the scope of this study.

167 The colors observed through the microscope, which are not necessarily
 168 consistent with the color of the ball which the pollen come from, did not

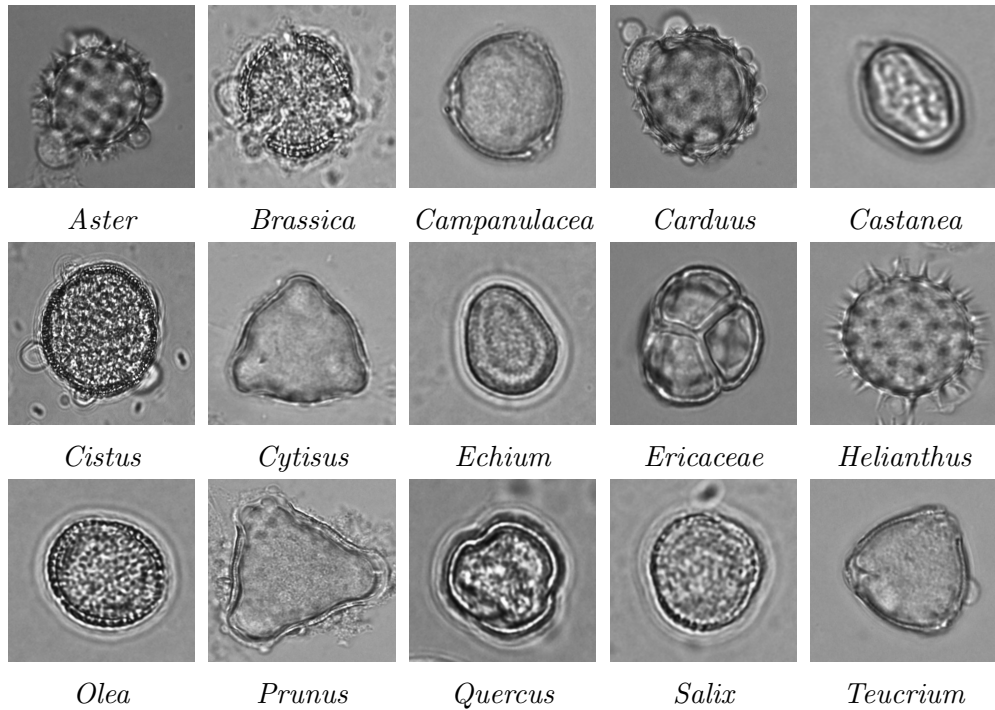


Figure 1: Examples of pollen database. Note these grains have been conveniently scaled here for aesthetic reasons.

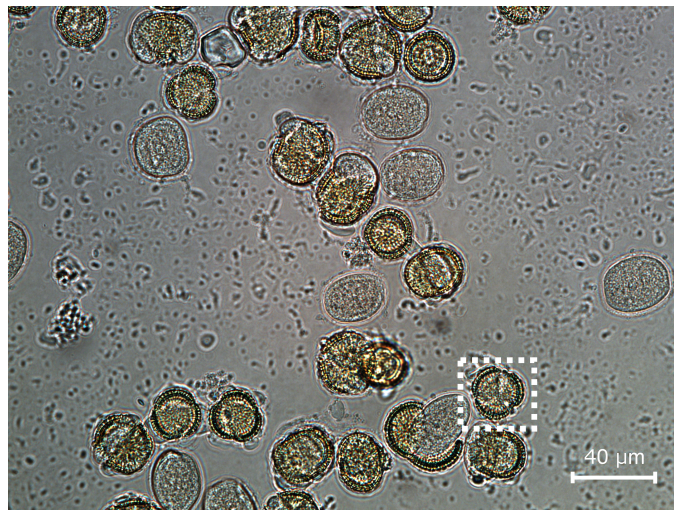


Figure 2: Microscope example of *Brassica* genre at magnification $\times 40$ of size 2560×1920 pixels. Framed sample of size 258×243 pixels.

169 presented evidences of discriminant significance. In addition the white bal-
170 ance performed by CCDs can significantly vary from one to other. Therefore
171 the images were finally converted to grayscale. By doing this we mitigated
172 at the same time the presence of yellowish lipids and other possible colored
173 debris present in the slices which could impair the pollen segmentation and
174 also feature extraction stages.

175 **3. Binary masks: contour-inner segmentation**

176 Binary masks are effective regions where descriptors must be computed,
177 while other regions out of the mask are ignored. The list of published works
178 about automatic pollen segmentation is short and there is still a need for a
179 definitive method without posterior supervision. In this work we present a
180 semi-automatic method which still requires manual outline corrections. Nev-
181 ertheless the main novelty that we propose is a dual segmentation for inner
182 areas and grain's contours. In these two areas there are visible structural
183 differences in terms of recognition and therefore our hypothesis is that some
184 descriptors should manifest different distributions too. This is not expected
185 to affect morphological descriptors but descriptors relating with statistical
186 properties of the pixels. One way to deal with such a dichotomy could be to
187 implement classifiers able to handle multi-modal distributions. However, in
188 this case we considered this dual segmentation more robust and controlled
189 approach. Doubling the number of effective regions will double dimension-
190 ality of the classification domain, but at the same time the classification
191 process gets simplified in terms of class separability according to the *a priori*
192 location knowledge of pollen's textures. The following items enumerate the

193 sequence of processes we used to give shape to such masks (see also in Fig. 3
194 a schematic block diagram).

- 195 1. Thresholding binarization: automatic thresholding segmentation with
196 the maximum histogram value. Similar techniques like Otsu's [22, 10,
197 13].
- 198 2. Maximum area: preservation of the biggest area, smaller regions re-
199 jected.
- 200 3. Hole filling: inside holes are filled if present.
- 201 4. Opening: erosion and dilation with a 15×15 kernel, holes revised again.
- 202 5. Inner-contour segmentation: erosion with a kernel proportional to the
203 equivalent binary mask diameter¹. Empirically adjusted to 15%.

204 These well-known algorithms are present in almost every image processing
205 software and therefore no further details are given in this respect. Due to
206 the presence of debris and some peculiar pollen types more complex to be
207 segmented, the binary masks were afterward manually checked for finishing
208 correction, see some examples in Fig. 4. Note that every pollen type present
209 different exine but the pollen type is not know a priori, therefore such a
210 15% is necessarily a compromised value that could better fit in some pollen
211 types than others, see Fig. 5. This value corresponds to exine sizes from 1-
212 $10\mu m$. At this moment we will leave possible improvements and alternative
213 segmentation strategies for an interesting further research.

¹diameter of a circle with the same area

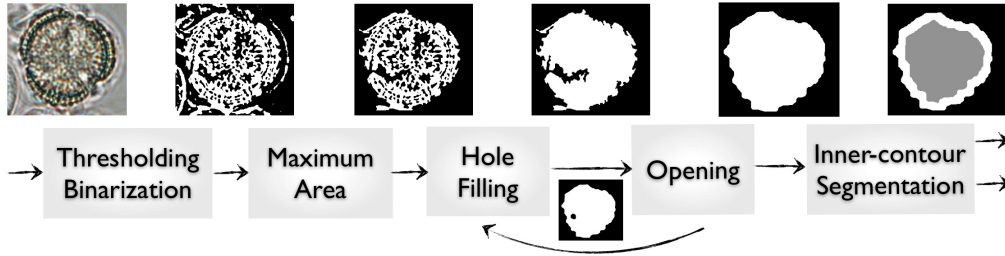


Figure 3: Segmentation example of a pollen grain borrowed from the previous Fig. 2 (258×243 pixels): image thresholding binarization with maximum histogram value; maximum area preservation and removal of smaller areas; inner holes filling-in; opening process with a 15×15 mask (it may need feedback); and inner and contour segmentation (15% grain diameter).

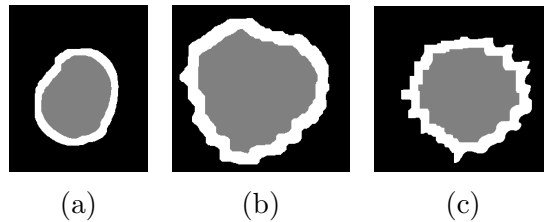


Figure 4: Examples of contour and interior pollen segmentation adjusted to 15% of their equivalent diameter. (a) *Echium* (237×285), (b) *Brassica* from Fig. 3 (258×243) and (c) *Helianthus* (354×330). Note these grains have been conveniently scaled here for aesthetic reasons.

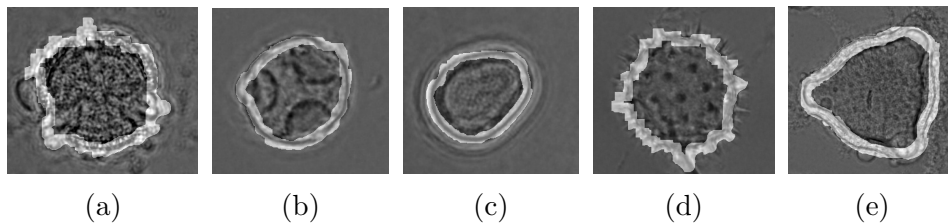


Figure 5: Examples of binary mask segmentation including a contour extraction with a kernel 15% of the grain diameter. (a) *Brassica* (368×320), (b) *Campanulaceae* (272×256), (c) *Echium* (288×272), (d) *Helianthus* (384×352) and (e) *Prunus* (512×512). Note again these grains have been conveniently scaled here for aesthetic reasons.

214 4. Pollen Feature Descriptors

215 As descriptions of pollen species can be found through numerous publica-
216 tions, a special effort must be done in translating such a knowledge in terms
217 of computer vision. To a significant extent the experts' capability to dis-
218 tinguish among similar pollen types comes from a knowledge not necessarily
219 extracted from such bright-field images, but also coming from text descrip-
220 tions, 3D spatial vision and simply reasoning that humans often do almost
221 effortlessly. Considering that some features are simply imperceptible without
222 such human capability recognizing, which is still not present in the state of
223 the art in computer vision, some other features do describe pollen grains as
224 for accomplishing a helpful automatic classification. In this way, according
225 to our palynologist team we described such pollen features in useful terms for
226 pattern classification in Tab. 2. Although not all the features will be faced
227 here, like for instance apertures which are for the moment under development
228 and some previous works can be found in [11, 23], other features like general
229 morphology or texture will be one of the basis of this study.

230 Along the subsequent subsections we organized descriptors in groups ac-
231 cording to their formulation, which at the same time will help to conduct the
232 later experiments. A brief notion is introduced here and we let the reader to
233 deepen along of plenty of well documented references. See descriptors cate-
234 gorized in Tab. 3. Note that with the exception of the morphological type,
235 the rest of descriptors are computed uniquely in those pixels tagged by the
236 segmented binary masks (contour and inner separately).

Table 2: Feature description of the 15 pollen types in terms of computer vision.

TYPE	INSIDE	CONTOUR	SIZE	POLAR VIEW			MERIDIAN VIEW			USUAL VIEW
				PERIMETER	APERTURES	APERTURES	PERIMETER	APERTURES	APERTURES	
<i>Quercus</i>	slightly granulated	thick	medium	circular or oval	3 depressions	circular or oval	circular or oval	enlarged towards poles	none	none
<i>Echium</i>	smooth	thin	small	oval (pear)	negligible	oval (pear)	oval (pear)	negligible	meridian	meridian
<i>Cistus</i>	reticular	medium	medium	circular	negligible	circular	circular	negligible	none	none
<i>Olea</i>	partially reticular	thick+reticular	medium	circular	3 subtle openings	circular	circular r	enlarged towards poles	none	none
<i>Salix</i>	wide reticular	thick+reticular	medium/small	circular	3 profound openings	circular	oval	enlarged towards poles	none	none
<i>Brassica</i>	reticular	medium	medium	tri-lobular	3 depressions	circular	circular	3 lineal fissures	none	none
<i>Retama</i>	reticular	medium	medium/small	triangular	3 depressions	circular	circular	3 lineal fissures	none	none
<i>Carduus</i>	dense prickles	thick+dense prickles	medium/large	circular	3 protuberances	circular	circular	protuberances	none	none
<i>Aster</i>	prickles	thick+prickles	medium/small	circular	3 tiny depressions	circular	circular	3 lineal fissures	none	none
<i>Helianthus</i>	prickles	thick+large prickles	medium	circular	3 tiny depressions	circular	circular	3 lineal fissures	none	none
<i>Teucrium</i>	smooth	thick poles	medium	oval	3 tampons	oval	triangular	two tampons	none	none
<i>Cytisus</i>	transparent	thin+non reticular	medium/small	triangular	3 thin openings	triangular	rhomboidal	rhombus opposite sides	none	none
<i>Ericaceae</i>	transparent	thick+non reticular	medium/large	tetrahedral	Tri-lobed	tetrahedral	tetrahedral	qua./bi-lobulated	none	none
<i>Castanea</i>	transparent	non reticular	small	circular	3 depressions	circular	Oval	several depressions	none	none
<i>Campulalacca</i>	trickles	thin+tiny prickles	small	circular	3 tiny depressions	circular	Oval	3 small depressions	polar	polar
<i>Prunus</i>	mainly striate	double+striate	medium/large	triangular	3 openings	triangular	Oval	central + large	polar	polar

small ~ 10 – 25 μ m . *medium* ~ 25 – 50 μ m . *large* ~ 50 – 100 μ m

CATEGORY	DESCRIPTOR	ANNOTATION	TOTAL DESCRIPTORS
Morphological	Area, Perimeter, Shape,	6 features	6
	Eccentricity, Fullness, Contour Profile	(3 eccentricities)	
Statistical	1 st Order	13 features	13
	2 nd Order Haralick	<i>distance</i> = 1, 3, 5 <i>direction</i> = 0°, 45°, 90°, 135°	19x3x4 = 241
Transformed space	LBP	mean, variance, asymmetry and kurtosis	4
Moments	Hu	7 moments	7
Space-frequency	Fourier	4 scales	241x4 = 964
	Wavelets	4 scales (3 orientations)	241x4 = 964
	Gabor	4 scales (6 orientations)	241x4 = 964

Table 3: List of descriptors grouped in testing categories.

237 *4.1. Morphological Descriptors*

238 The binary masks described in the previous section establish an appropri-
239 ate framework to compute morphological features related to pollen’s contour
240 and area.

241 *4.1.1. Area*

242 This descriptor can be calculated as the sum of pixels in the binary mask
243 of size $M \times N$ given $B \in (0, 1)$:

$$Area = \sum_{n=1}^N \sum_{m=1}^M B(m, n) \tag{1}$$

244 *4.1.2. Perimeter*

245 This descriptor is the number of pixels that belong to the object and
246 which have at least one neighbor belonging to the background.

$$Perimeter = \sum_{n=1}^N \sum_{m=1}^M P(n, m)$$

$$P(m, n) = \begin{cases} 1 & \text{if } \exists B(m \pm 1, n \pm 1) = 1 \\ 0 & \text{otherwise} \end{cases} \quad (2)$$

248 4.1.3. Shape

249 This descriptor measures the elongation of an object. For a circle its value
250 is equal to 1. It is calculated in the following way:

$$Shape = \frac{4 \cdot \pi \cdot Area}{Perimeter^2} \quad (3)$$

251 4.1.4. Eccentricity

252 these descriptors also reflect elongation but in relation with the object's
253 center of mass, also called centroid and defined as:

$$(m_c, n_c) = \left(\frac{1}{Area} \sum_{(m,n) \in Area} m \cdot B(m, n), \frac{1}{Area} \sum_{(m,n) \in Area} n \cdot B(m, n) \right) \quad (4)$$

254 The first *Eccentricity*₁ is defined as a quotient of the maximum and min-
255 imum distance between the centroid and object's border, also called outer
256 and inner circumference radius.

$$Eccentricity_1 = \frac{Outerradius}{Innerradius} \quad (5)$$

257 Similarly *Eccentricity*₂, is calculated as quotient of the semi-axes of the

<i>Mean</i>	$\mu = \sum_{i=0}^{H-1} i \cdot h(i)$
<i>Mode</i>	$i = \operatorname{argmax}(h(i))$
<i>Variance</i>	$\sigma = \sum_{n=0}^{H-1} (i - \mu)^2 \cdot h(i)$
<i>1st Quartile</i>	$\mu_{q1} = \sum_{i=3\lceil H/4 \rceil}^H i \cdot h(i)$
<i>2nd Quartile</i>	$\mu_{q2} = \sum_{i=2\lceil H/4 \rceil}^{3\lceil H/4 \rceil} i \cdot h(i)$
<i>3rd Quartile</i>	$\mu_{q3} = \sum_{i=\lceil H/4 \rceil}^{2\lceil H/4 \rceil} i \cdot h(i)$
<i>Interquartile Range</i>	$\mu_{q3} - \mu_{q1}$
<i>Minimum</i>	$\min(h(i))$
<i>Maximum</i>	$\max(h(i))$
<i>Range</i>	$\max(h(i)) - \min(h(i))$
<i>Entropy</i>	$\sum_{i=0}^{H-1} h(i) \cdot \log(h(i))$
<i>Asymmetry</i>	$\frac{1}{\sigma^3} \sum_{n=0}^{H-1} (i - \mu)^3 \cdot h(i)$
<i>Kurtosis</i>	$\frac{1}{\sigma^4} \sum_{n=0}^{H-1} (i - \mu)^4 \cdot h(i)$

Histogram $h(i)$, bins number H , floor operator $\lceil \]$.

Table 4: First order statistical descriptors.

258 best fitting ellipse for the object and *Eccentricity*₃ is a ratio of the inertia
259 moments of the two semi-axes of the best fitting ellipse (see forwards for a
260 description of moments).

261 4.1.5. Fullness

262 is the ratio of the object area to bounding rectangle area.

263 4.2. Statistical Descriptors

264 4.2.1. 1st-order Statistical: histogram

265 These descriptors, listed in Tab. 4, measure typical statistics in image
266 histogram $h(i)$. These group of descriptors are sensible to global variation of
267 gray pixel levels, but they ignore their local correlation.

268 *4.2.2. 2st-order Statistical (Haralick): co-occurrence matrix*

269 These descriptors, listed in Tab. 5, measure statistics in co-occurrence ma-
270 trix $c(m, n)$ defined as the distribution of co-occurring neighbor gray values.
271 For a complete guide to statistical description consult [15].

272 *4.3. Contour Profile Descriptor*

273 In this section we introduce a novel descriptor to describe micro structures
274 present along the perimeter of grains. As described in Tab. 2, some pollen
275 types have reticular exines, which is translated into corrugated contours at
276 the zenithal microscope view. In computer vision terms this means that the
277 variance of gray levels along the pollen contour is higher than in pollen with
278 no reticular surface. Although this measure could not classify by itself one
279 specific pollen type, it can work as an efficient support tool for discriminating
280 among pollen groups of highly, medium and low reticular exines.

281 The first step uses the center of mass of binary masks described in Sec. 3
282 to accomplish square cropping. One simple way of making this calculation
283 is by means of moment equations described in Sec. 4.5. After that Cartesian
284 coordinates (x, y) are transformed into polar logarithmic coordinates $\rho =$
285 $\log(\sqrt{(m - m_c)^2 + (n - n_c)^2})$, $0 \leq \rho \leq \rho_{max}$ and $\omega = \arctan((m - m_c)/(n -$
286 $n_c))$, $0 \leq \omega \leq 2\pi$ [23]. See in Fig. 6-(b) and (e) a couple of examples of polar
287 logarithmic transformations.

288 The second step computes a snake algorithm from the bottom of the
289 polar transformed images (outskirts in Cartesian coordinates), i.e. from the
290 maximum radius. Starting from a horizontal line, each location (pixel) of that
291 line is moved upwards if the gray level at the current location is higher than a
292 given threshold (we used 30% of the maximum graylevel). When a dark gray

<i>Energy</i>	$\sum_{i=0}^{H-1} \sum_{j=0}^{H-1} c(i, j)^2$
<i>Variance</i>	$\sum_{i=0}^{H-1} \sum_{j=0}^{H-1} (i - \mu)^2 \cdot c(i, j)$
<i>Contrast</i>	$\sum_{n=0}^{H-1} n^2 \left(\sum_{i=0}^{H-1} \sum_{j=0}^{H-1} c(i, j) \right), \quad i - j = n$
<i>Dissimilarity</i>	$\sum_{i=0}^{H-1} \sum_{j=0}^{H-1} i - j \cdot c(i, j)$
<i>Correlation</i>	$\frac{1}{\sigma_x \sigma_y} \sum_{i=0}^{H-1} \sum_{j=0}^{H-1} i \cdot j \cdot c(i, j) - \mu_x \mu_y$
<i>Autocorrelation</i>	$\sum_{i=0}^{H-1} \sum_{j=0}^{H-1} i \cdot j \cdot c(i, j)$
<i>Measure of Correlation 1</i>	$\frac{T - HXY1}{\max(HX, HY)}$
<i>Measure of Correlation 2</i>	$(1 - \exp[2 \cdot (HXY2 - T)])^{0.5}$
<i>Cluster Shade</i>	$\sum_{i=0}^{H-1} \sum_{j=0}^{H-1} (i + j - \mu_x - \mu_y)^3 \cdot c(i, j)$
<i>Cluster Prominence</i>	$\sum_{i=0}^{H-1} \sum_{j=0}^{H-1} (i + j - \mu_x - \mu_y)^4 \cdot c(i, j)$
<i>Maximum Probability</i>	$\max(c(i, j)), \quad i = [0 \dots H - 1], j = [0 \dots H - 1]$
<i>Entropy</i>	$T = - \sum_{i=0}^{H-1} \sum_{j=0}^{H-1} c(i, j) \cdot \log(c(i, j))$
<i>Sum Average</i>	$\sum_{i=0}^{2(H-1)} i \cdot c_{x+y}(i)$
<i>Sum Entropy</i>	$\sum_{i=0}^{2(H-1)} c_{x+y}(i) \cdot \log(c_{x+y}(i, j))$
<i>Sum Variance</i>	$- \sum_{i=0}^{2(H-1)} (i - \text{SumEntropy})^2 \cdot c_{x+y}(i)$
<i>Difference Entropy</i>	$- \sum_{i=0}^{H-1} c_{x-y}(i) \cdot \log(c_{x-y}(i, j))$
<i>Difference Variance</i>	$\sum_{i=0}^{H-1} i^2 \cdot c_{x-y}(i)$
<i>Homogeneity 1</i>	$\sum_{i=0}^{H-1} \sum_{j=0}^{H-1} \frac{c(i, j)}{1 + i - j }$
<i>Homogeneity 2</i>	$\sum_{i=0}^{H-1} \sum_{j=0}^{H-1} \frac{c(i, j)}{1 + (i - j)^2}$

H bins number, HX and HY entropy of p_x and p_y .

$$\mu_x = \sum_{i=0}^{H-1} \sum_{j=0}^{H-1} i \cdot c(i, j); \quad \mu_y = \sum_{i=0}^{H-1} \sum_{j=0}^{H-1} j \cdot c(i, j)$$

$$c_x(i) = \sum_{j=0}^{H-1} c(i, j); \quad c_y(j) = \sum_{i=0}^{H-1} c(i, j)$$

$$\sigma_x = \sqrt{\sum_{i=0}^{H-1} c_x(i)(i - \mu_x)^2}; \quad \sigma_y = \sqrt{\sum_{j=0}^{H-1} c_y(j)(j - \mu_y)^2}$$

$$c_{x+y}(k) = \sum_{i=0}^{H-1} \sum_{j=0}^{H-1} c(i, j); \quad i + j = k, k = [0 \dots 2(H - 1)]$$

$$c_{x-y}(k) = \sum_{i=0}^{H-1} \sum_{j=0}^{H-1} p(i, j); \quad |i - j| = k, k = [0 \dots H - 1]$$

$$HXY1 = - \sum_{i=0}^{H-1} \sum_{j=0}^{H-1} c(i, j) \log(c_x(i) \cdot c_y(j))$$

$$HXY2 = - \sum_{i=0}^{H-1} \sum_{j=0}^{H-1} c_x(i) \cdot c_y(j) \cdot \log(c_x(i) \cdot c_y(j))$$

Table 5: Second order statistical descriptors (Haralick).

Algorithm 1: Contour Profile Descriptor

```
Transform image into polar coordinates  $PIMAGE(radius, angle)$ ;  
 $SNAKE(angle) = radius_{max}$ ;  
 $radius = radius_{max}$ ;  
while angles exist and are not anchored do  
  if [ $(SNAKE(angle \pm 1) < aCurvature)$  and  
    ( $PIMAGE(SNAKE(angle) + 1, angle) > aThreshold$ )] then  
    |  $SNAKE(angle) = radius - 1$ ;  
  else  
    | anchor  $SNAKE(angle) = radius$ ;
```

293 pixel is found it may belong highly probably to the pollen contour and the
294 snake at that point is fixed. Some elastic properties are given to the snake,
295 so that it can fit to the curved contour. We used 1 pixel maximum curvature.
296 Previously the polar image is smoothed by a 5×5 uniform filter to remove
297 spurious values and outskirts debris. Such contours found by snakes do not
298 necessarily match with those binary contours found in Sec. 3 for the binary
299 masks. Other descriptors that operate globally in a given region could not
300 require a segmented region extremely precise. However this contour profile
301 descriptor in concrete requires a path as much precise as possible. In any case
302 such snaked-contours could be also applied for all descriptors as some studies
303 revealed some improvements [10]. Considering the snake as a uni-dimensional
304 function, the whole algorithm is described in Algorithm 1.

305 The third and final step draws a profile of gray levels along the snake
306 and measures its variance in relation to the mean local value obtained by
307 smoothing in our case the gray profile with a 21-bin uniform filter. See
308 Fig. 6-(c) and (f). A high contour profile variance will indicate that the
309 grain contour, the exine, is probably reticulated and a low variance means

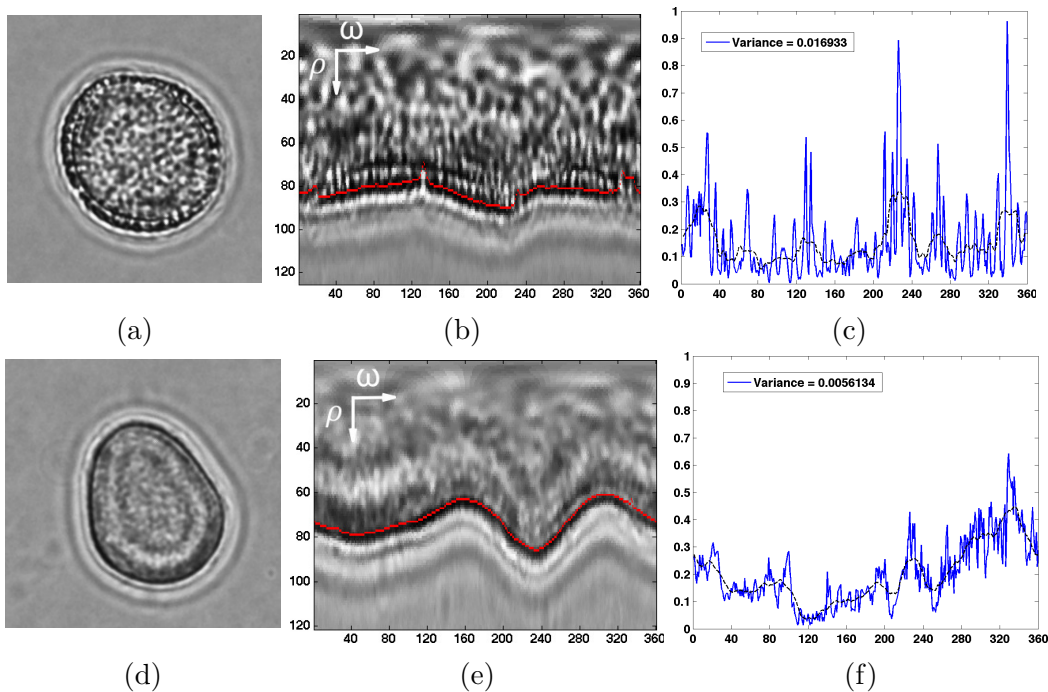


Figure 6: Reticular descriptor of contour profile (exine). (a) *olea* and (d) *echium* samples, (b) and (e) polar transformation, (c) and (f) gray level profile and variance measurement (blue line) and local mean obtained with a 21-bin uniform filter (black dotted line).

310 no reticulation.

311 4.4. Local Binary Patterns

312 The Local Binary Pattern (LBP) operator [24] is based on the idea that
 313 textural properties within homogeneous regions can be mapped into patterns,
 314 which represent micro-features. It uses a 3×3 square mask called “tex-
 315 ture spectrum,” to compare masked values with their central pixel, those
 316 ones lesser are labeled with “0” otherwise with “1”. The labeled pixels
 317 are multiplied by a fixed weighting function and summed to obtain a label:
 318 $LBP(g_c) = \sum_{p=0}^7 s(g_p - g_c)2^p$, where $\{g_p | p = 0, \dots, 7\}$ are the neighbors of

319 g_c and the comparison function is defined as: $s(x) = \begin{cases} 1 & \text{if } x \geq 0 \\ 0 & \text{otherwise} \end{cases}$

320 Ojala et al. [25] improved their proposal by including a circular mask
 321 denoted by the subscript (P, R) where P is the number of sampling points
 322 and R is the radius of the neighborhood. If sampling coordinates, $(x_p, y_p) =$
 323 $(x_c + R \cos(\frac{2\pi p}{P}), y_c - R \sin(\frac{2\pi p}{P}))$, do not fall at integer positions, then the
 324 values are bilinearly interpolated. Furthermore, they observed that over
 325 90% of patterns can be described with few LBP patterns, so, they intro-
 326 duced a uniformity measure $U(LBP_{P,R}(g_c)) = |s(g_{P-1} - g_c) - s(g_0 - g_c)| +$
 327 $\sum_{p=1}^{P-1} |s(g_p - g_c) - s(g_{p-1} - g_c)|$, which corresponds to the number of tran-
 328 sitions (0/1) in the labeled LBP.

329 In this way, the uniform-LBP ($LBP_{P,R}^{uni}$) can be obtained as:

$$LBP_{P,R}^{uni}(g_c) = \begin{cases} \sum_{p=0}^{P-1} s(g_p - g_c) & \text{if } U(LBP_{P,R}(g_c)) \leq 2 \\ P + 1 & \text{otherwise} \end{cases} \quad (6)$$

330 After this process is completed a labeled image is generated and the pixel-
 331 wise information is encoded as a histogram, so that it can be interpreted as a
 332 fingerprint or a signature of the analyzed object. $LBP_{P,R}^{uni}$ produces $(P + 2)$ -
 333 bin histograms [26]. Then from all statistical descriptors only mean, variance,
 334 asymmetry and kurtosis are computed assuming a studied trade-off between
 335 overloaded dimensionality vs. accuracy impairment [27].

336 *4.5. Hu Moments*

337 Image moments, originally proposed by [28], describe not only invariant
 338 morphological features of shapes but also high order statistical features. They
 339 are formulated as follows:

$$\mu_{pq} = \sum_m \sum_n (m - m_c)^p \cdot (n - n_c)^q \cdot g(m, n) \quad (7)$$

340 Where $m_c = \frac{r_{10}}{r_{00}}$ and $n_c = \frac{r_{01}}{r_{00}}$.

341 *4.6. Space-frequency Descriptors*

342 These do not really constitute descriptors themselves but transformations
 343 where features, somehow hidden, arise with higher visibility. It is in this
 344 transformed domains where features are measured by applying the mathe-
 345 matical previously introduced descriptors, in our case the statistical descrip-
 346 tors. For every sub-band there are 241 statistical descriptors (13 1st-order
 347 statistical plus 19 2nd-order statistical with 3 distances and 4 orientations)
 348 and for the whole transformed domain with 4 scales the total number of
 349 descriptors is 964, see Sec. 4.2.

350 *4.6.1. Fourier Transform*

351 It is the first formal proposal to analyze spectral contain of a signal where
 352 2D frequencies arise in this context from graylevel variations along features
 353 like contour, edges, stripes and other periodic structures like textures. The
 354 Fourier spectrum is split in octave bands apart and averaged as follows:

$$Fourier_l = \sum_{r=\frac{1}{2^l}}^{\frac{1}{2^{l-1}}} \sum_{\theta=0}^{360} |I(r, \theta)| drd\theta, , l \in \{1, \dots, L\} \quad (8)$$

355 Where I is the Fourier transform of the image in polar coordinates and
 356 L the number of levels. For the experiments we selected 4 decomposition
 357 levels, which is a common value in most computer vision algorithms. Note
 358 the continuous DC-component (luminance) is disregarded and binary mask
 359 cannot be used here since the spatial dimension is lost.

360 4.6.2. Wavelet Transform

361 Although some pollen types present stationary structures (textures) through
 362 their inner regions, they mostly present a different spectral content not only
 363 along the interior but also along their contour. The Fourier transform loses
 364 the space localization where this happens and frequencies from different areas
 365 are mixed. In the late 80's wavelets were firstly proposed with Daubechies
 366 and Mallat as main precursors [29]. We used the overcomplete version and 5
 367 stem long of Daubechies basis to build our descriptors as the energy on every
 368 scaled level as follows:

$$Wavelet_l = \sum_{o=1}^3 \sum_{u=1, v=1}^{U, V} |W_{l,o}(u, v) \cdot B(u, v)|, \quad l \in \{1, \dots, L\} \quad (9)$$

369 Where W is the wavelet transform of the image for the scale l and ori-
 370 entation o whose vertical and horizontal coordinates extend to $U = M$ and
 371 $V = N$. Based on preliminary observations, the number of scales was set
 372 to $L = 4$. Note that to achieve orientation invariance all bands in the same
 373 scale must be summed, i.e the vertical, horizontal and diagonal bands. The
 374 residual DC-component was discarded. As previously stated, prior to this
 375 wavelet average the coefficients are masked by the corresponding contour
 376 and inner binary masks $B(u, v)$.

377 *4.6.3. LogGabor Transform*

378 Firstly proposed by Dennis Gabor in 1946 [30], the Gabor filters are dif-
 379 ferent versions of a Gaussian-shaped window modulated by a sinusoid. The
 380 result is the partition of the Fourier plane into bands modulated in orien-
 381 tation and octave bands apart in frequency. Gaussian shape ensures an
 382 optimum spreading in both dimensions, i.e. space location vs. frequency
 383 discrimination, while one weakness of wavelets is the pronounced frequency
 384 overlapping. In addition, the Gaussian envelop is modulated by a complex
 385 exponential with odd and even phases, which is effective for analyzing fea-
 386 tures with odd phase like ridges and even phase like edges. In this study
 387 we used the overcomplete implementation of logGabor filters proposed by
 388 Fischer et al. [31] never tested before for this task. Similarly to wavelets, the
 389 logGabor descriptor is formed by calculating the energy at every scaled level:

$$\begin{aligned}
 Gabor_l &= \sum_{o=1}^O \sum_{u=1, v=1}^{U, V} |F^{-1}(G_{lo} \cdot I) \cdot B(u, v)|, \quad l \in \{1, \dots, L\} \\
 G_{lo} &= \exp\left(-\frac{1}{2} \left(\frac{\rho - \rho_l}{\sigma_\rho}\right)^2\right) \exp\left(-\frac{1}{2} \left(\frac{\theta - \theta_{pl}}{\sigma_\theta}\right)^2\right)
 \end{aligned} \tag{10}$$

390 Where F^{-1} is the inverse Fourier transform, G_{lo} is the logGabor filter with
 391 L scales and O orientations in log-polar coordinates (ρ, θ) and $(\sigma_\rho, \sigma_\theta)$ are
 392 the angular and radial bandwidths, see [31] for more implementation details.
 393 Again $L = 4$, $O = 6$ and the residual DC-component is discarded.

394 5. Discriminant Analysis

395 In case of task-specific methods like this study, descriptors are either
396 chosen after a comprehensive literature review study but also after empirical
397 experiment feedback. With a generalized descriptor extraction, the large
398 set of image descriptors provides an extensive numeric description of the
399 image content [32]. However, descriptors that are discriminant for one specific
400 dataset may not be discriminant for others, probably because they describe
401 features that are widely spread along all classification groups or because they
402 are redundant (correlated) with respect to other descriptors. In that case
403 such descriptors provide useless information that moreover will likely degrade
404 the classification performance not only in terms of accuracy but also in terms
405 of speed due to the higher dimensionality [33, 34]. To reduce the number of
406 irrelevant descriptors, discriminant analysis minimizes the classification error
407 for the smallest possible subset of descriptors. Thousands of descriptors are
408 extracted from the methods here described and it is a fact widely studied
409 that beyond a certain limit an increasing number of descriptors not only
410 provokes an increasing computational time but also impairs classification [35].
411 Therefore a feature selection process is then required to remove redundant
412 information.

413 5.1. Floating Selection

414 A preliminary study was carried out to elucidate which are individually
415 the most discriminant descriptors. For that we employed the Sequential
416 Forward Feature Selection (SFFS) [36]. It constructs an incremental priority
417 subset of descriptors by adding the descriptor in the excluded subset that

1	L	asimmetry.LBP.Org	26	S	Dissi_1.135.Org	51	S	Dissi_3.0.KEx	76	S	Contr_5.0.Org
2	L	curtosis.LBP.Org	27	S	Dissi_1.90.Org	52	S	Dvarh_5.135.KEx	77	S	Entro_3.0.Org
3	M	Perimeter.Org	28	S	Dissi_1.45.Org	53	S	Denth_5.45.Org	78	S	Denth_3.0.KEx
4	M	Area.KEx	29	S	Denth_1.135.Org	54	S	Dissi_3.45.Org	79	S	Denth_1.135.KEx
5	M	Area.Org	30	S	Dvarh_3.0.KEx	55	S	Denth_5.90.Org	80	S	Dissi_3.135.KEx
6	M	EquivDiameter.Org	31	S	Denth_3.0.Org	56	S	Denth_5.135.Org	81	S	Dissi_3.45.KEx
7	M	EquivDiameter.KEx	32	S	Dissi_1.0.KEx	57	S	Entro_1.0.Org	82	G	OrgS_Gbf6
8	M	Perimeter.KEx	33	S	Denth_1.90.Org	58	S	Dissi_1.90.KEx	83	S	Denth_1.0.KEx
9	S	Entropy.Org	34	S	Dissi_3.90.Org	59	S	Dissi_1.45.KEx	84	S	Denth_1.90.KEx
10	S	Entropy.KEx	35	S	Dvarh_5.0.KEx	60	S	Dissi_1.135.KEx	85	S	Entro_3.90.Org
11	S	Dvarh_3.0.Org	36	S	Dvarh_3.45.KEx	61	S	Dissi_5.90.Org	86	S	Denth_3.45.KEx
12	S	Dvarh_1.135.Org	37	S	Denth_1.0.Org	62	G	OrgS_Gbf26	87	S	Denth_1.45.KEx
13	S	Dvarh_3.135.Org	38	S	Dvarh_3.135.KEx	63	S	Entro_1.135.Org	88	S	Denth_5.0.KEx
14	S	Dvarh_3.90.Org	39	S	Dvarh_3.90.KEx	64	S	Contr_3.135.Org	89	S	Denth_3.135.KEx
15	S	Dvarh_3.45.Org	40	S	Denth_1.45.Org	65	S	Dvarh_1.90.KEx	90	S	Denth_3.90.KEx
16	S	Dvarh_5.0.Org	41	S	Denth_3.45.Org	66	S	Contr_3.90.Org	91	S	Contr_3.45.Org
17	G	OrgS_Gbf2	42	S	Dvarh_1.135.KEx	67	S	Dissi_5.0.KEx	92	S	Contr_1.0.Org
18	G	OrgS_Gbf14	43	S	Denth_3.90.Org	68	S	Entro_1.90.Org	93	S	Contr_5.90.Org
19	S	Dissi_1.0.Org	44	S	Dissi_3.135.Org	69	S	Entro_1.45.Org	94	G	OrgS_Gbf8
20	S	Dvarh_5.45.Org	45	S	Denth_3.135.Org	70	G	OrgS_Gbf12	95	S	Denth_5.45.KEx
21	S	Dvarh_5.90.Org	46	S	Dvarh_5.45.KEx	71	G	OrgS_Gbf4	96	S	Contr_1.45.Org
22	S	Dvarh_1.90.Org	47	S	Denth_5.0.Org	72	S	Dvarh_1.45.Org	97	S	Dissi_5.90.KEx
23	G	OrgS_Gbf1	48	S	Dvarh_5.90.KEx	73	S	Contr_1.135.Org	98	S	Denth_5.90.KEx
24	S	Dvarh_5.135.Org	49	S	Dissi_5.0.Org	74	S	Dissi_3.90.KEx	99	S	Denth_5.135.KEx
25	S	Dissi_3.0.Org	50	S	Contr_3.0.Org	75	G	OrgS_Gbf10	100	S	Entro_3.135.Org

Table 6: The 100 most discriminant descriptors listed in order of importance. *L* stands for LBP, *M* for morphological, *S* for statistical and *G* for logGabor. Extension *Org* means that the descriptor was calculated in the pollen kernel and *KEx* in the outer exine.

418 increments the highest the classification rate. For every step the priority
419 subset is re-arranged and re-examined in case of one of the descriptors impairs
420 classification with the new formed group. As a result this algorithm often
421 converges to a ordered list by discrimination capacity. In Tab. 6 there is
422 such a list for the first 100 features. The percentage of LBPs descriptors
423 is only 2% although they are on the top. The percentage in that list of
424 morphological descriptors is 6%, logGabor 9% and the statistical descriptors
425 83%. Although this is an interesting list for elucidating some discriminant
426 descriptors, one should bear in mind that later on their contribution will be
427 altered by the LDA transformation (see Sec. 5.3).

428 5.2. Correlation

429 Some overloaded features like Fourier, wavelets and Gabor are treated
430 like new domains themselves where the whole bank of statistical descriptors
431 can be calculated and extracted from each decomposition band. This means
432 that the total number of descriptors becomes 4 times larger given a 4-level
433 decomposition transform. This approach increases the workload to a cuttered
434 extend to be easily computable. Therefore, for these feature groups of space-
435 frequency transform we decided to remove those statistical variables that are
436 highly correlated.

437 To remove redundant information we firstly used the correlation coef-
438 ficient as the similarity measure between two or more features. Hence, a
439 threshold value must be defined for determining the correlation value from
440 which features are considered redundant. This measure has been commonly
441 adopted for unsupervised feature selection [37]. In our study, an empirical
442 threshold of 98% was adopted. Such a decision reduced the number of de-
443 scriptors in such a way that for instance a 4-level Fourier bands with 964
444 initial descriptors gets shortened to 224, 4-level wavelet decomposition from
445 964 to 143 or the actual statistical descriptors from 964 to 147. In summary
446 with this technique it is achieved an overall 75-80% dimensionality reduction
447 and the corresponding computing time. In return classification accuracy,
448 according to calculations shown afterwards, is insignificantly affected.

449 5.3. Linear Discriminant Analysis

450 Since the previous methods generate high dimensional feature vectors and
451 a limited dataset is available in our context, Linear Discriminant Analysis
452 (LDA) [38] constitutes an efficient tool for dimensionality transformation.

453 Since oversized spaces crowd together classes which impairs classification,
454 LDA transforms the original space into an orthogonal and linear space where
455 feature vectors are prioritized in order of importance while others are rejected.
456 This implies that classes must be linearly separated which is not always
457 fulfilled. LDA also requires unimodal Gaussian likelihoods which was so
458 validated.

459 **6. Training & Classification Techniques**

460 Dimensionality reduction is a fundamental step in any classification prob-
461 lem. In most cases we cannot assume parameter independence, which pre-
462 vents from separately assessing each parameter from the rest. This issue is
463 the so called Model Selection Problem (MSP). In this case we validated nor-
464 mal distributions by means of normality test of K.S. normality test, Levene's
465 homocedasticity and the analysis of variance (ANOVA) [39, 40].

466 10-*fold* cross-validation is a simple and yet widely employed method for
467 model evaluation that randomly splits up data into 10 disjoint subsets of
468 approximately equal size. Each fold is then classified separately by using the
469 remaining 9 subsets to train the model. In the end the average of all folds
470 provides an estimation of the classification accuracy of the model. A similar
471 procedure was exercised with groups of 1 element, also called *leave-one-out*.
472 Both training methods threw similar results and for the sake of simplicity
473 only leave-one-out will be presented in the experiments.

474 Although many classifiers can be found and some of them could signifi-
475 cantly improve accuracy rates, it is not the main purpose here to carry out
476 a thorough analysis of classifiers' performance, but again to discover which

477 descriptor or combination of descriptors better discriminate between pollen
478 types. Hence, although we do compare an extensive bank of classifiers like
479 nearest-neighbor, k -means, Parzen classifier, decision tree, neural networks,
480 quadratic Bayes normal classifier, Fisher classifier, linear discriminant or sup-
481 port vector machine, we selected here three representative ones, which in turn
482 were three of the best classifiers tested.

483 *6.1. Fisher classifier*

484 Fisher's linear classifier finds a linear discriminant function by minimizing
485 the errors in the least square sense [35]. This linear discriminant is based on
486 finding a direction in the feature space such that the projection of the data
487 minimizes Fisher's criterion, i.e., the ratio of the squared distance between
488 the class means and averaged class variances. The linear classifier is then
489 perpendicular to this projection.

490 *6.2. Support Vector Machine*

491 Support Vector Machines (SVM) finds a discriminant function by max-
492 imizing the geometrical margin between positive and negative samples [41].
493 Thus, the space is mapped so that examples from different classes are sepa-
494 rated by a gap as wide as possible. Besides linear classification, SVMs act as
495 a non-linear classifier by using the so-called kernel trick. This trick can be
496 considered a mapping of the inputs onto a high-dimensional feature space in
497 which classes become linearly separable. SVMs minimize both training error
498 and geometrical margin. The latter accounts for the generalization abilities
499 of the resulting classifier. SVMs are one of the best classifiers available and
500 have been applied to many real-world problems.

501 *6.3. Random Forest*

502 A Decision Tree (DT) is a conceptually simple, yet robust, and widely
503 used tool for decision support in which classification is performed through
504 a tree graph [42]. The classification starts from an initialization node (*root*
505 *node*) from which a given test sample is tested at each stage (*internal node*)
506 of the classification, all the way down to the end of a tree branch (*leaf* or
507 *terminal node*) [43]. The path followed by the sample depends on threshold-
508 based conditions associated to each internal node.

509 To select the optimal threshold-based conditions, DT algorithms make
510 use of a brute force method, which consists of testing all potential variables
511 and selecting the variable that maximizes a given criterion. When building
512 the DT, this criterion characterizes the quality of the split created by the
513 transition from an internal node to its associated leaves [43].

514 To improve classification accuracy and robustness, the Random Forest
515 (RF) classifier, built upon an ensemble of DTs, learn from different subsets of
516 the training dataset and no pruning is performed after their construction [42].
517 Each DT is built using the values of random feature vectors in a way that
518 all DTs from the RF possesses the same distribution. The random feature
519 vectors may be generated using several techniques, such as bagging [42],
520 random split selection [44] and the so-called random subspace technique [45].
521 When classifying an unknown sample, its feature vector is tested using all
522 DTs of the RF. Their outputs constitute votes for the most popular class,
523 which in turn is the RF prediction. Nowadays, the RF classifier is considered
524 as one of the most accurate learning algorithms and its performance has been
525 proven on many datasets [46].

526 7. Results

527 Given the total number of descriptors is 6 320, considering that space-
528 frequency, moments, LBPs and statistical descriptors are duplicated due to
529 the contour-interior pollen segmentation. Given also the feature reducing
530 and transformation algorithms (correlation and LDA) and the three selected
531 classifiers (Fischer, SVM and Random Forest), the number of possible ex-
532 periments is considerable. We organized the results in several experiments
533 to show concrete aspects of descriptors and classifiers.

534 Although the experiments are driven according to the best accuracy/error
535 rates, one should bear in mind that the obtained absolute values could be
536 hardly compared quantitatively to other studies due to discrepancies in fea-
537 ture vector, dimensionality reduction and/or classifiers. One example case
538 could be [14] with an astonishing number of particles/grains and classifi-
539 cation rate around 98.5%, but not comparable because 1) 3D information
540 is additionally incorporated 2) pollen grains were only 12% of the training
541 date set and 3) allergenic pollen is not necessarily the same pollen than for
542 beekeeping.

543 7.1. Experiment 1: whole and contour+inner segmentation.

544 Descriptors were tested here according to their mathematical definition
545 type. At the same time descriptors were compared when applied for both
546 segmentation cases: whole-segmented grain and contour+inner segmenta-
547 tion. In order to simplify the case study, the same classifier was used for
548 all of them, in this case Fisher but with no particular reason, except for its
549 accurate performance behavior. Albeit similar results can be observed with

550 the remaining classifiers.

551 From the plot in Fig. 7 most descriptors lead to similar classification er-
552 ror around $\varepsilon \sim 0.3$ when they operate individually. Two of them are above
553 0.7 though, i.e. LBP and moments. This corroborates that macro-features
554 derived from morphology descriptors already provide competitive accuracy
555 on a par with local micro-feature analysis performed by (spatio)-frequency
556 descriptors. We have no plausible explanation for the lower rates delivered
557 by LBP and moments. Note that although some LBPs had an important dis-
558 criminant capacity in Fig. 6, all together combined do not perform as high
559 as other texture descriptors. This could be to the reason that the number
560 of LBP descriptors 4 is not actually enough for the current database. The
561 McNemar's significance test [47] provides a confidence value to accept that
562 methods are statistically significant provided a minimum threshold typically
563 chosen 95% of confidence. That value is found by projecting the classifi-
564 cation discrepancies of both methods through a chi-quadratic function as a
565 expectation model for binomial distributions. McNemar's threshold delivered
566 here a more than amply averaged value $T = 230.98 > \chi_{1,0.95}^2 = 3,84$ except
567 for 5 pairs which can not be considered significative: Wavelets vs. Fourier,
568 morphological and statistical; Fourier vs. statistical and morphological vs.
569 statistical on averaged $T = 1.95$.

570 Another favorable observation reveals a significant improvement when
571 computing doubly but separately for contour and inner pollen regions, as we
572 hypothesized. Overall, one can observe a drastic decline of errors achieving
573 an overall accuracy improvement of 50% ($T = 344.62$). Note that morpho-
574 logical descriptors have no counterpart for contour+inner segmentation. All

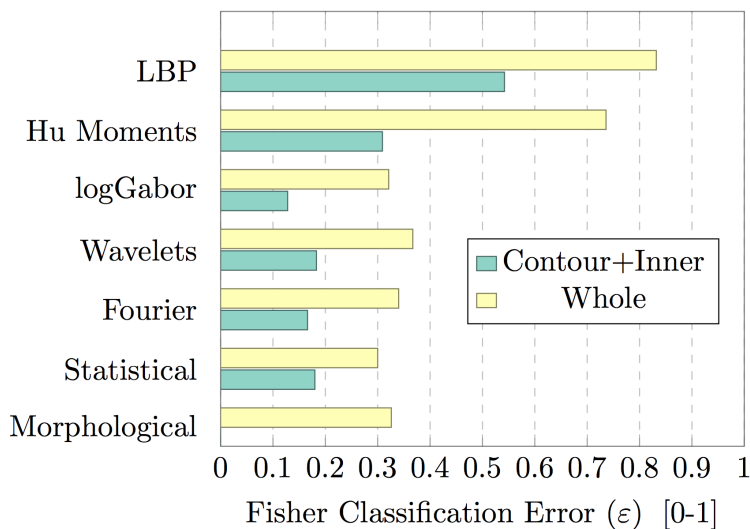


Figure 7: Comparing descriptors types under the Fisher classification error.

575 subsequent experiments will consider exclusively contour-inner segmentation.

576 To justify the rejection of the space-frequency descriptors above a 98%
 577 correlation threshold (see Sec. 5.2), the classification error obtained for in-
 578 stance with logGabor is $\varepsilon = 0.124$, while with the 100% of descriptors a
 579 similar error is obtained $\varepsilon = 0.128$ and the significance test is low $T = 0.78$.

580 *7.2. Experiment 2: descriptor types combinations.*

581 The combination of different types of descriptors can strengthen the dis-
 582 crimination capacity. In Fig. 8 morphological and statistical descriptors con-
 583 stitute a baseline for comparison since they provided high accuracy rates
 584 and bring together the two main discriminant features: shape and texture.
 585 From this chart, when statistical descriptors are combined with morpho-
 586 logical descriptors provided together an improvement of 51.1%. Adding to
 587 these two groups the space-frequency descriptors separately provided an over-

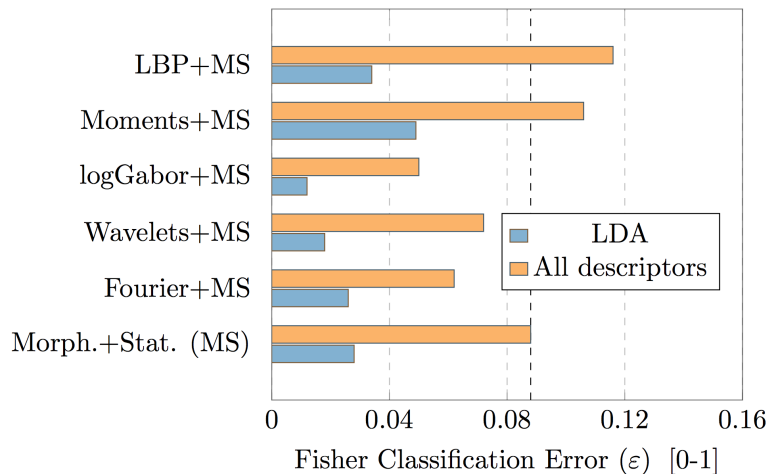


Figure 8: Accuracy performance of Morphological+Statistical (MS) and remaining descriptors with contour+inner segmentation.

588 all accuracy improvement of 34% (averaged $T = 81.31$), while the logGabor+
 589 morphological+statistics are the most accurate with $\varepsilon = 0.05$. Note
 590 that moments and LPB produces slight impairments. Significance test be-
 591 tween pairs delivered an averaged value ($T = 23.63$), except for Fourier vs.
 592 Wavelets ($T = 1.35$) and Moments vs. LBP ($T = 1.04$). This tendency is
 593 confirmed in Fig. 9 where morphological+statistical combined with space-
 594 frequency descriptors achieve the lowest error rates. Particularly the combi-
 595 nation of morphological+statistical+all space-frequency descriptors provided
 596 the lowest error rate $\varepsilon = 0.032$ ($T = 31.05$ averaged with comparative cases).
 597 Note also that neither LBP nor moments barely affect performance.

598 7.3. Experiment 3: LDA dimensionality reduction.

599 In previous Figs. 8 and 9 already compared the improvement achieved by
 600 LDA. All combinations of descriptors augmented their accuracy significantly
 601 and reduced the overall classification error around 70% (averaged $T = 89.54$).

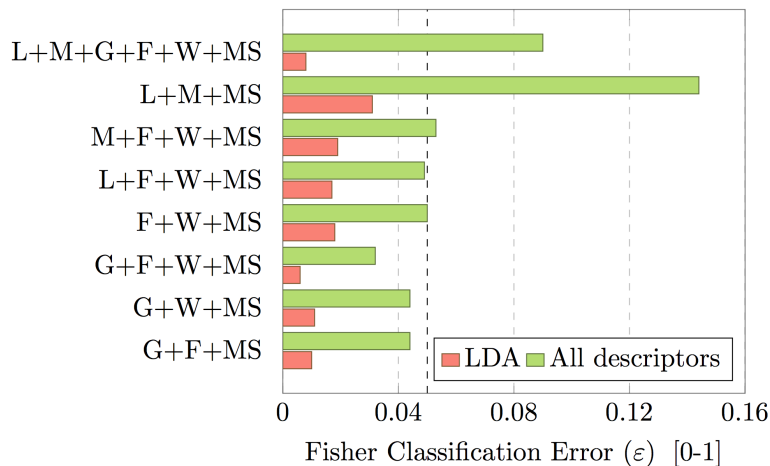


Figure 9: Accuracy performance (contour+inner segmentation) of Morphological+Statistical (MS) and combinations of remaining descriptors: Wavelets (W), Fourier (F), logGabor (G), Moments (M), LBP (L). Note that the vertical dashed line corresponds to previous logGabor+MS error rate 0.05.

602 This suggests that, besides unimodal Gaussian likelihoods tested in advance,
 603 most descriptors can be linearly separated. Now most combinations classify
 604 with less than 2% error and an outstanding case is the combination of mor-
 605 phological, statistical descriptors with the three space-frequency descriptors
 606 achieving 99.4% accuracy rate ($\varepsilon = 0.006$), see its confusion matrix in Tab. 7.
 607 Note also that LDA successfully deals with the addition of LBP and moments
 608 achieving a similar error $\varepsilon = 0.008$ and low significant difference $T = 0.35$
 609 for these two cases.

610 7.4. Experiment 4: Classifiers

611 In Fig. 10 Fisher classifier was compared with SVM and Random Forest
 612 by using four reference groups of descriptors. Although there is a slight
 613 improvement tendency in favor of Random Forest, outcomes did not show
 614 preference in all groups, nor even for other groups not shown here. Thus no

ACTUAL \ PREDICTED	<i>Aster</i>	<i>Brassica</i>	<i>Campanula.</i>	<i>Carduus</i>	<i>Castanea</i>	<i>Cistus</i>	<i>Cytisus</i>	<i>Echium</i>	<i>Ericaceae</i>	<i>Helianthus</i>	<i>Olea</i>	<i>Prunus</i>	<i>Quercus</i>	<i>Salix</i>	<i>Teucrium</i>
<i>Aster</i>	120	0	0	0	0	0	0	0	0	0	0	0	0	0	0
<i>Brassica</i>	0	119	0	0	0	0	0	0	0	0	1	0	0	0	0
<i>Campanula.</i>	0	0	118	0	0	0	2	0	0	0	0	0	0	0	0
<i>Carduus</i>	0	0	0	119	0	0	0	0	0	0	0	1	0	0	0
<i>Castanea</i>	0	0	0	0	120	0	0	0	0	0	0	0	0	0	0
<i>Cistus</i>	0	0	0	0	0	120	0	0	0	0	0	0	0	0	0
<i>Cytisus</i>	0	0	0	0	0	0	120	0	0	0	0	0	0	0	0
<i>Echium</i>	0	0	0	0	0	0	0	120	0	0	0	0	0	0	0
<i>Ericaceae</i>	0	0	0	0	0	0	0	0	120	0	0	0	0	0	0
<i>Helianthus</i>	6	0	0	0	0	0	0	0	0	114	0	0	0	0	0
<i>Olea</i>	0	1	0	0	0	0	0	0	0	0	119	0	0	0	0
<i>Prunus</i>	0	0	0	0	0	0	0	0	0	0	0	120	0	0	0
<i>Quercus</i>	0	0	0	0	0	0	0	0	0	0	0	0	120	0	0
<i>Salix</i>	0	0	0	0	0	0	0	0	0	0	0	0	0	120	0
<i>Teucrium</i>	0	0	0	0	0	0	0	0	0	0	0	0	0	0	120

Table 7: Confusion matrix for the best case combining Morphological+Statistical+Fourier+Wavelets+logGabor descriptors and LDA.

615 pair of group and classifier revealed evident superiority here. This leads to
616 the point that descriptors and classifiers must be selected as two parts that
617 work together accordingly.

618 8. DISCUSSION: Grain features, limits and possibilities

619 Several important contributions have been made in this work. A consid-
620 erable data base of pollen grains has been elaborated. It was compound of 15
621 pollen types and 120 samples per type manually cropped. Grains have been
622 automatically segmented (manually revised) to make binary masks. A bench
623 of the state of the art in morphological, statistical and texture descriptors to-
624 gether with a new contour profile descriptor has been exhaustively tested for
625 classifying the 15 pollen types. Some of them like texture descriptors have
626 not been evaluated before in this field. Furthermore we proposed a novel
627 contour+inner segmentation which provided an overall 50% improvement up

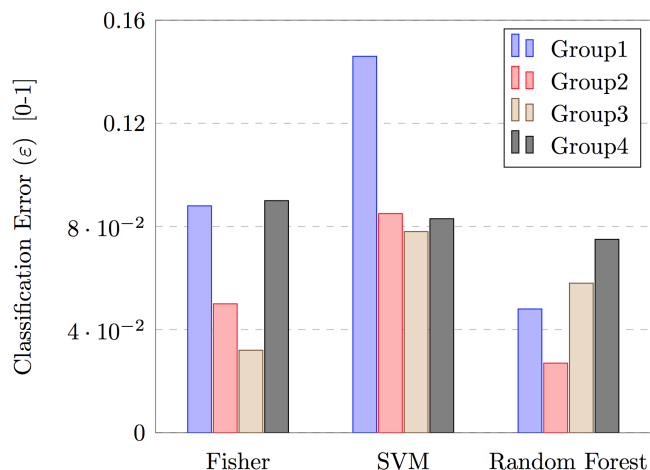


Figure 10: Performance comparison of classifiers Fisher, SVM and Decision Tree with Group1 (MS), Group2 (MS+F+W) and Group3 (MS+G+W+F) and Group4 (MS+W+F+G+M+L).

628 to 99.4% accuracy. We concluded that the traditional morphological and sta-
 629 tistical descriptors together with space-frequency representations, specifically
 630 logGabor, provided the best classification accuracy rates. Moreover the di-
 631 mensionality reduction with LDA improved classification by 70%. Along this
 632 research we also come across with other several challenging issues addressed
 633 in the following.

634 After long conversations with palynologists, they argue that the geomet-
 635 ric shape and number of apertures are the first aspects they look for in a
 636 preliminary screening. Although size is an effective feature to discriminate
 637 between broad groups of pollen types, this should be taken carefully since
 638 size could vary more than 10 microns in some circumstances like the sub-
 639 strate conditions or how much water received the plant. Thus it could be
 640 recommended to simplify the size in two classes: small and medium-large.
 641 Other morphological refinement would consider triangularity, rhomboicity or

642 even more complex shapes adapted to the wide range of shapes exhibited by
643 the pollen. After that, depending on the possible pollen types according to
644 their morphology, the search would resume for some other details like retic-
645 ular texture, spikes, apertures, exine width,... etc. This leads again to the
646 idea of a hierarchical-tree classification.

647 Unfortunately some pollen types are almost equal even for experts which
648 shows up the difficulty of this task. For instance *Cruciferae* and *Olea* are
649 similar except for the polar area and apertures. *Retama* and *Cytisus* belong
650 to the same family *Fabaceae* and are consequently similar except for the
651 almost negligible aperture and triangular view of the former.

652 In addition to the obvious place of origin, the first and effective way of
653 classifying pollen is the color ball. Bees rarely harvest pollen of different
654 types in the same ball, therefore the knowledge of a given color drastically
655 reduces the number of possible candidates. Such a description can be easily
656 incorporated in an automatic recognition software by displaying a color chart
657 where the user could select the most similar ball tonality. This pre-processing
658 stage could help computer vision tasks not only by reducing computation
659 time but also reducing error classification rates (decision tree). As previously
660 indicated, the color ball is not consistent with the color later observed through
661 the microscope and furthermore we found no evidence that color could have
662 any discriminant capacity beyond this point, therefore images were converted
663 to grayscale.

664 A pollen type may present different appearances according to their view
665 with respect to the z-view and consequently their morphological and also
666 statistical descriptors can drastically vary. Although it is still unclear how

667 to handle such a difficulty, three alternatives are discussed. Multimodal clas-
668 sifiers deal with complex probability distributions functions made of several
669 monomodal pdf's. This could be the case of some morphological descriptors
670 like 'circularity' (and related) that clearly present two or more probability
671 means depending on the view. This approach is more database consistent,
672 although increases the complexity. Another approach could split those multi-
673 appearance types in two or more different subclasses (polar, meridian,...)
674 which refines database description and simplifies classification, however this
675 doubles the effort for labeling each pollen type and collecting more training
676 samples. Hybrid tree-monomodal classification or decision rule could also be
677 employed for classifying in two steps. Firstly the monomodal classifiers could
678 be used for those descriptors not affected by the z-laying and secondly for
679 those sensible to view, without making separated classes for each z-laying.
680 This alternative demands a smaller training dataset than the previous option,
681 however it needs for a decision rule adjustment and still needs for tedious
682 polar/meridian/others labeling.

683 Precise segmentation is a critical point for the whole classification pro-
684 cess. Some studies using snakes and other computer vision techniques showed
685 remarkable results [48]. Effectively segmentation should be done accurately,
686 although our purpose in the current study focuses on comparing descriptor's
687 discriminant capacity while optimum classification rates remain a secondary
688 goal. Therefore we do not pursue perfect binary masks, but suitable enough
689 to be equally shared by all descriptors. However since one of the main con-
690 tributions here is the strategy of splitting grains in contour and inner parts,
691 therefore segmentation techniques will require a further study.

692 In a real scenario there is a need for an 'unknown' class, also known as
693 outlier detection. This class contains samples that do not belong to any of the
694 trained classes. Furthermore rejection class is also required to embrace those
695 ambiguous samples due to malformations or a bad cropping. Considering a
696 commercial software the goal is to discover the origin of the harvested balls
697 and a pollen ball contains hundreds of grains whose majority belongs to the
698 same pollen type due to a smart habit of bees. In this scenario it is not
699 therefore so critical the ratio of false-negative (attributed to a outlier-class),
700 since there are hundreds of attempts to find out the principal pollen type.
701 Instead false-positive ratio should be minimized as much as possible. In other
702 words, once a pollen grain is considered to belong to a certain class, one must
703 be highly confident on that assertion. Such a confident threshold has to be
704 modeled according to not only the classification error but also according to
705 population ratio present in every pollen ball or slice preparation.

706 **9. Appendix:**

707 Description of the main features of the 15 pollen types studied in this
708 paper.

709 *Aster* - isopolar, radially symmetric, medium size ($P = 22 - 31\mu m$, $E =$
710 $20 - 29\mu m$), spheroidal to prolate (elliptic), in equatorial view ($P/E = 0.96 -$
711 1.20), circular or trilobulate in polar view, 3-zonocolporate, ornamentation
712 echinate-perforate.

713 *Brassica* - isopolar, radially symmetric, medium size ($P = 21 - 30\mu m$, $E =$
714 $27 - 27\mu m$), oblate spheroidal to prolate (elliptic) in equatorial view ($P/E =$
715 $0.90 - 1.28$), circular or trilobulate in polar view, 3-zonocolpate, ornamenta-

716 tion reticulate.

717 *Campanulaceae* - isopolar, radially symmetric, small or medium size ($P =$
718 $18 - 29\mu m$, $E = 20 - 34\mu m$), oblate spheroidal to spheroidal in equatorial
719 view ($P/E = 0.80 - 0.96$), subtriangular in polar view, 3-zonoporate, orna-
720 mentation echinate.

721 *Carduus* - isopolar, radially symmetric, medium to big size ($P = 31 -$
722 $50\mu m$, $E = 31 - 51\mu m$), oblate spheroidal to prolate (elliptic) in equato-
723 rial view ($P/E = 0.85 - 1.20$), trilobulate in polar view, 3-zonocolporate,
724 ornamentation echinate-perforate-finely reticulate.

725 *Castanea* - isopolar, radially symmetric, small size ($P = 14 - 15\mu m$, $E =$
726 $9 - 11\mu m$), prolate (elliptic) in equatorial view ($P/E = 1.27 - 1.55$), triangular
727 in polar view, 3-zonocolporate, ornamentation rugulate.

728 *Cistus ladanifer* - isopolar, radially symmetric, small to medium size
729 ($P = 41 - 55\mu m$, $E = 50 - 53\mu m$), spheroidal to prolate spheroidal in
730 equatorial view ($P/E = 0.91 - 1.19$), circular in polar view, 3-zonocolporate, or-
731 namentation reticulate.

732 *Cytisus* - isopolar, radially symmetric, medium to small size ($P = 20 -$
733 $33\mu m$, $E = 15 - 29\mu m$), spheroidal to prolate spheroidal (elliptic or sub-
734 rhomboid) in equatorial view ($P/E = 0.86 - 1.55$), circular to trilobulate in
735 polar view, 3-zonocolporate, ornamentation finely reticulate.

736 *Echium* - heteropolar, radially symmetric, small size ($P = 13 - 25\mu m$, $E =$
737 $8 - 15\mu m$), prolate (pyriform) in equatorial view ($P/E = 1.30 - 1.87$), trilob-
738 ulate in polar view 3-zonocolporate, perforate-finely reticulate.

739 *Ericaceae* - tetragonal tetrads, medium to big size ($P = 27 - 67\mu m$),
740 pollen 3-zonocolporate, ornamentation psilate to verrucate.

741 *Helianthus* - isopolar, radially symmetric, medium size ($P = 27-31\mu m$, $E =$
742 $27 - 33\mu m$), oblate spheroidal to spheroidal in equatorial view ($P/E =$
743 $0.90 - 1.00$), circular in polar view, 3-zonocolporate, ornamentation echinate-
744 perforate.

745 *Olea* - isopolar, radially symmetric, small to medium size ($P = 20 -$
746 $27\mu m$, $E = 19 - 31\mu m$), spheroidal to prolate (elliptic) in equatorial view
747 ($P/E = 1.05 - 1.31$), circular or trilobulate in polar view, 3-zonocolporate,
748 ornamentation reticulate-verrucate.

749 *Quercus* - isopolar, radially symmetric, medium size ($P = 19-33\mu m$, $E =$
750 $15-34\mu m$), oblate to prolate (elliptic) in equatorial view ($P/E = 0.86-1.35$),
751 circular or triangular in polar view, 3-zonocolporate, ornamentation granulate-
752 verrucate.

753 *Rubus* - isopolar, radially symmetric, small to medium size ($P = 16 -$
754 $28\mu m$, $E = 14 - 24\mu m$), spheroidal to prolate (elliptic) in equatorial view
755 ($P/E = 1.00 - 1.57$), circular or trilobulate in polar view, 3-zonocolporate
756 or 3-zonocolporoidate, ornamentation reticulate.

757 *Salix* - isopolar, radially symmetric, small to medium size ($P = 16 -$
758 $27\mu m$, $E = 16 - 23\mu m$), prolate (elliptic) in equatorial view ($P/E = 1.10 -$
759 1.20), subtriangular in polar view, 3-zonocolporate, ornamentation reticulate.

760 *Teucrium* - isopolar, radially symmetric, medium to big size ($P = 35 -$
761 $66\mu m$, $E = 26 - 45\mu m$), spheroidal to prolate (elliptic) in equatorial view
762 ($P/E = 1.05 - 1.65$), circular or triangular in polar view, 3-zonocolporate,
763 ornamentation echinate-perforate.

764 **Acknowledgements**

765 This work has been supported by the European project APIFRESH FP7-
766 SME-2008-2 "Developing European standards for bee pollen and royal jelly:
767 quality, safety and authenticity" and we would like to thank to Mr. Wal-
768 ter Haefeker, President of the European Professional Beekeepers Association
769 (EPBA). J. Victor Marcos is a "Juan de la Cierva" research fellow funded
770 by the Spanish Ministry of Economy and Competitiveness. Rodrigo Nava
771 thanks Consejo Nacional de Ciencia y Tecnología (CONACYT) and PAPIIT
772 grant IG100814.

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