

Scintillation efficiency of liquid argon in low energy neutron-argon scattering

W. Creus^{a*}, Y. Allkofer^{a†}, C. Amsler^{b‡}, A. D. Ferella^c, J. Rochet^b, L. Scotto-Lavina^d, and M. Walter^a

^aPhysik-Institut der Universität Zürich, CH-8057 Zürich, Switzerland

^bAlbert Einstein Center for Fundamental Physics, Laboratory for High Energy Physics, University of Bern, CH-3012 Bern, Switzerland

^cINFN Laboratori Nazionali del Gran Sasso, LNGS, Assergi, Italy

^dSUBATECH, Ecole des Mines de Nantes, CNRS/In2p3, Université de Nantes, Nantes, France

E-mail: claude.amsler@cern.ch

ABSTRACT: Experiments searching for weak interacting massive particles with noble gases such as liquid argon require very low detection thresholds for nuclear recoils. A determination of the scintillation efficiency is crucial to quantify the response of the detector at low energy. We report the results obtained with a small liquid argon cell using a monoenergetic neutron beam produced by a deuterium-deuterium fusion source. The light yield relative to electrons was measured for six argon recoil energies between 11 and 120 keV at zero electric drift field.

KEYWORDS: Dark matter; WIMP; liquid argon; quenching factor; monoenergetic neutrons.

*This work is based on the PhD Thesis of William Creus

†Now at Credit Suisse AG, Zurich

‡Corresponding author

Contents

1. Introduction	1
2. Liquid argon for direct searches	2
2.1 Experimental setup	3
3. Calibrations with γ-sources	7
3.1 Pulse height analysis	7
3.2 Trigger efficiency	9
4. Neutron data	10
5. Monte-Carlo simulation	13
6. Data analysis	15
6.1 χ^2 -fits	15
6.2 Systematic errors	17
6.3 Discussion	18
7. Conclusions	19

1. Introduction

It is known from astronomical observations that most of the gravitational mass in the universe is made of dark energy and non-baryonic dark matter which does not couple to electromagnetic radiation [1]. Dark matter has survived since the birth of the universe and hence must be stable and weakly interacting. The most prominent candidates for dark matter are the Weakly Interacting Massive Particles (WIMPs) [2], in particular the spin-1/2 neutralino with predicted mass in the GeV to TeV range. The neutralino would scatter on constituent quarks in nucleons, leading to nuclear recoils in the range of 1 – 100 keV. Non-accelerator laboratory (“direct”) searches are all based on the detection of nuclear recoils. The scattering cross section on nucleons is tiny, in the range 10^{-5} to 10^{-12} pb, comparable to that for neutrino interaction. For low masses the sensitivity decreases due to the low recoil energy and the detection threshold, while for high masses the loss of sensitivity is due to the exponentially diminishing WIMP flux.

The laboratory observation of dark matter is one of the most pressing issues in Particle Physics. The neutralino is being searched for at the LHC and direct searches for WIMPs are underway in non-accelerator underground experiments (for a review see [3]). The most stringent upper limits for WIMPs are obtained for the spin independent WIMP-nucleon cross section. Upper limits on the WIMP-nucleon cross section have been obtained by the XENON100 [4] and LUX [5] experiments

using liquid xenon, the latter quoting the most stringent upper limit of 7.6×10^{-10} pb for a WIMP mass of about 33 GeV.

At the LHC the neutralino would manifest itself by leaving a large missing energy when scattering off quarks. These “indirect” searches at the LHC are more competitive than direct searches for low WIMP masses, providing the best upper limits of about 10^{-3} pb below 3.5 GeV [6, 7].

Several direct searches were performed or initiated during the last ten years, employing different types of detectors such as solid state detectors or noble liquids (argon, neon or xenon) [3] which can be used in large volume time projection chambers. Experiments using liquid argon are underway: DEAP [8] and MiniCLEAN [9] at SNOLAB, DarkSide [10] at Gran Sasso, and ArDM [11] at Canfranc.

2. Liquid argon for direct searches

In liquid argon (LAr) scintillation light is emitted in a narrow VUV band around 128 nm with two components of different decay times, $\tau_1 \simeq 7$ ns and $\tau_2 \simeq 1.6$ μ s [12]. Heavily ionizing projectiles such as α particles or nuclear recoils contribute mostly to the fast decaying component, while the contribution from electrons and γ -rays to the slow component is larger. In this work we define the prompt fraction F_p as the fraction of prompt over total integrated pulse height, the prompt light being chosen as the integrated pulse height in the time interval between -20 and $+30$ ns of the time at which the light pulse reaches its maximum. Figure 1 shows the prompt fraction F_p measured during the early stage of the experiment, when a ^{210}Po α -source (5.3 MeV) was installed [13]. F_p is typically 0.25 and 0.75 for electron recoils and nuclear recoils, respectively. The prompt fraction is therefore useful as a discriminant to identify nuclear recoils and to reject background [14]. This property is the main advantage of argon over xenon (in addition to its lower price), but the disadvantage is the presence of the radioactive β -emitter ^{39}Ar .

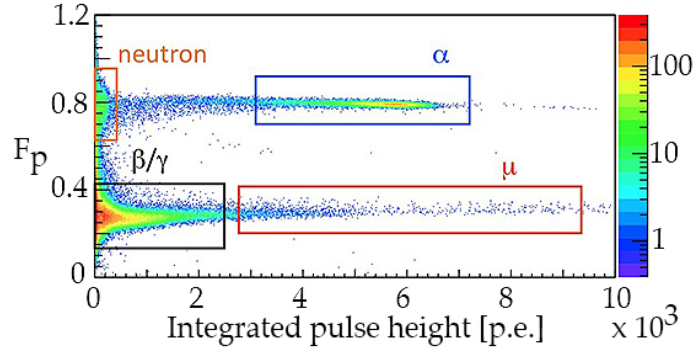


Figure 1. Fraction F_p of prompt to total light for various projectiles.

The scintillation light yield and its dependence on nuclear recoil energy is an essential input to the WIMP-nucleon cross section. The relative scintillation efficiency L_{eff} is defined as the ratio of the scintillation yield L_{nr} from nuclear recoils to that from electron recoils L_{er} ,

$$L_{eff} = \frac{L_{nr}(T_{nr})}{L_{er}(T_{er})}, \quad (2.1)$$

where T_{nr} and T_{er} stand for the nuclear recoil and electron recoil energy, respectively. L_{er} is determined from photopeaks or Compton edges, using γ -sources. The relative efficiency L_{eff} being an energy dependent quantity, a standard reference for calibration is required. For the sake of convenience we use in this work the 60 keV electronic photopeak from a ^{241}Am source. As discussed below, we have measured the light yield from various γ -sources (including a 32 keV $^{83\text{m}}\text{Kr}$ source) and have established its linearity for recoil electrons above 30 keV. The results obtained here can therefore be compared directly with those obtained from earlier experiments [15, 16, 17] using e.g. the $T_{er} = 122$ keV photopeak from a ^{57}Co source [16].

The relative scintillation efficiency is measured by mimicking the WIMP-nucleus interaction with neutron beams, e.g. by elastic scattering of monoenergetic neutrons under fixed scattering angles (see [16, 17] for argon and [18] for xenon data). The measured light yield is then compared with a simulation and L_{eff} is derived by applying iterative fits. This article reports the determination of L_{eff} in LAr at zero electric field using a monoenergetic neutron beam from deuterium-deuterium fusion. Details can be found in [13]. The measurements were motivated by the envisaged DARWIN dark matter project [20].

2.1 Experimental setup

A good way to calibrate the light output and to study the response of LAr to nuclear recoils is to scatter a beam of monoenergetic neutrons of energy T_n off argon nuclei, and to measure the light yield as a function of scattering angle Θ , from which the recoil energy T_{nr} can be calculated according to the formula

$$T_{nr} \simeq \frac{2T_n A}{(1+A)^2} (1 - \cos \Theta), \quad (2.2)$$

where Θ is the scattered neutron angle in the laboratory and $A \gg 1$ is the atomic mass number. The method is illustrated in figure 2 (left).

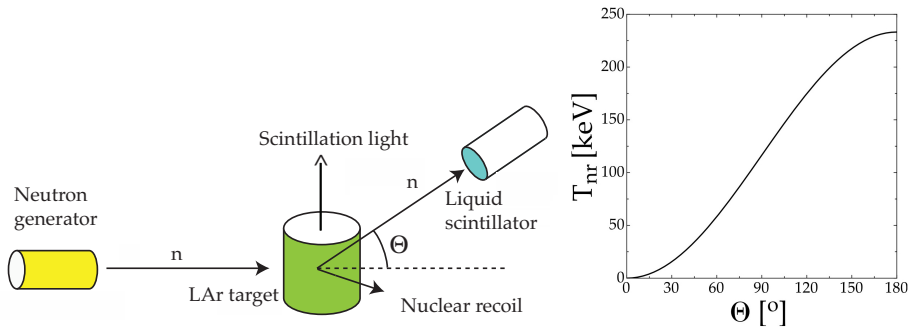


Figure 2. Left: principle of the scattering experiment with monoenergetic neutrons scattered under the angle Θ . Right: nuclear recoil energies in argon for incident neutron energies of 2.45 MeV.

We are using monoenergetic neutrons of $T_n = 2.45$ MeV from an electrostatic fusion source based on the reaction $dd \rightarrow {}^3\text{He} n$. The energy deposits are plotted in figure 2 (right) as a function of scattering angle. The commercially available neutron generator is of the deuterium-deuterium plasma fusion type from NSD-fusion [21]. The source is a cylinder at ground voltage containing

low pressure deuterium gas (10^{-2} mbar). An internal perforated cylindrical electrode at high voltage (typically 80 kV) induces a discharge. The ionized deuterons are accelerated towards the inner electrode and accumulate in the central regions with energies of about 15 keV. This is sufficient to overcome the Coulomb barrier and induce fusion. The plasma of ~ 25 mm length emits neutrons isotropically into 4π with a typical rate of 10^6 n/s. The certified operation time is 25 000 hours, after which the cell must be exchanged. The fusion generator is surrounded by a 90 cm diameter shield of borated polyester and the experiment is confined within a radiation controlled fence in our laboratory at CERN (figure 3, left). Residual radiation (mainly from scattered neutrons and X-rays) is well below the authorized limit of $2.5 \mu\text{Sv/h}$.

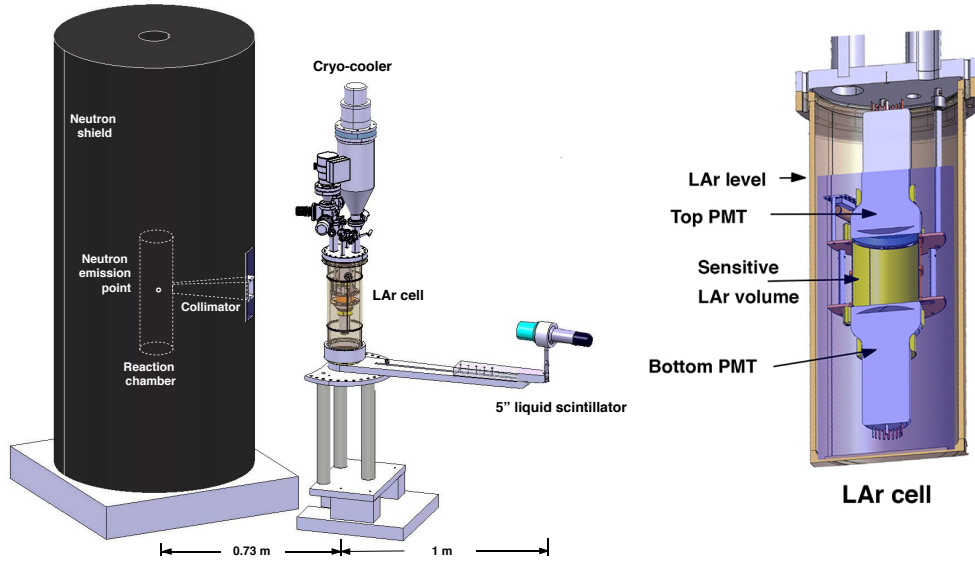


Figure 3. Left: neutron gun, argon cell and liquid scintillation counter used to measure L_{eff} in LAr. Right: sketch of the LAr cell with its vacuum chamber (see text).

The neutrons are collimated through a polyethylene orifice within roughly $0.2\% \times 4\pi$ sr to match the sensitive volume of the LAr cell. The collimator is defined by a lead box (wall thickness 2 mm) inserted into the polyester to protect against X-rays. The LAr cell (figure 3, right) is located at a distance of 73 cm from the neutron emission point. The sensitive volume of the cell consists of a 1.5 mm thin aluminium cylinder (75 mm in diameter and 47 mm high, hence a LAr volume of 0.2ℓ). The cell itself is contained in a larger cylindrical vessel (141 mm in diameter), also filled with LAr. The inner wall of the cell is covered by a Tetratex foil coated with a wavelength shifter made of tetraphenylbutadien (TPB) to shift the VUV scintillation light to a longer wavelength, following our developments described in [22]. The surface density of the TPB covering the reflector is $1.0 \pm 0.1 \text{ mg/cm}^2$. The light readout is performed with two Hamamatsu R6091-01 photomultipliers (PMT) on each side of the cell. The 3" bialkali PMTs have 12 dynodes and a Pt underlay to reduce the resistivity of the photocathode when operating at LAr temperature (~ 86 K). The surfaces of the PMTs are coated with a TPB/paraloid mixture (quantum efficiency estimated to be around 15%). To perform measurement at zero electric field the aluminium cylinder is polarized at the same voltage as the photocathode of the PMTs.

The detector is filled with condensed pure argon gas 6.0 containing less than 0.5 ppm of H₂O, 0.1 ppm of O₂, 0.1 ppm of H₂, 0.1 ppm of CO₂, and 0.1 ppm of CO. Platinum resistors are used to monitor the LAr level inside the cell. The vacuum and gas pressure are read out by pressure sensors. A blue LED ($\lambda = 390$ nm) connected to an optical fiber is inserted into the vessel for gain calibration. A slow control program written in Labview is used to monitor and record the temperature and pressure during operation.

For continuous operation a gas system is connected to the cell to provide condensation and recirculation of the argon. The gas is condensed on the top of the chamber by the cold head of a Sumitomo CH210 cryocooler with a nominal cooling power of about 80 W, driven by a Sumitomo F-70H helium compressor [23]. An outer vacuum chamber at a pressure of 10^{-5} mbar isolates the cryogenic refrigerator from ambient room temperature. The purification of the argon gas is achieved with two purification cartridges OXISORB-W mounted in parallel, which reduce the O₂ and H₂O levels to < 5 and < 30 ppb respectively [24]. The temperature is kept between the solidification and the boiling points of argon (85 K and 87 K respectively at 1 atm) by four resistive heaters located on the first stage cooling station of the cryocooler. Platinum sensors are connected along the coil pipe to monitor the cooling power. A PID controller driven by a LabView program reads out and regulates the temperature of the cold head at the desired value with a precision of about 10 mK. The current provided to the heaters is ensured by a TTI TSX 35 10 programmable PSU based on the GPID interface [25]. The typical power produced by the heaters to maintain the temperature for liquefaction is about 50 W.

The neutrons scattered off the LAr cell are detected by a 5" organic liquid scintillator counter (LSC) manufactured by SCIONIX [26]. The scattering angle Θ is varied by rotating the LSC around the LAr cell on a 1 m long arm. The LSC is shielded against direct neutrons from the source by a 10 cm thick polyethylene absorber. Events are recorded by a coincidence measurement of the LAr and LSC signals. To obtain the ratio L_{eff} , equation (2.1), the light output produced by the argon nucleus emitted under the corresponding recoil angle is compared to the reference electron recoil light yield.

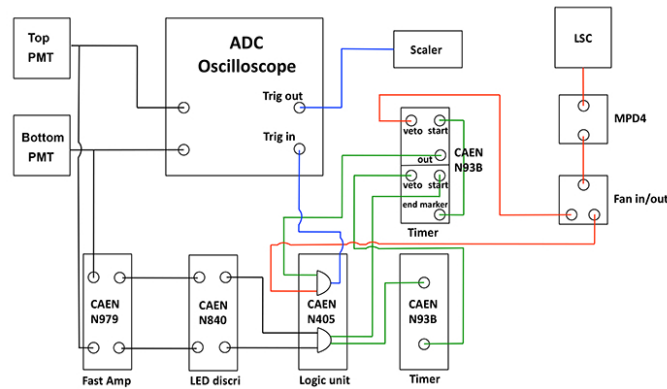


Figure 4. Diagram of the data acquisition system.

Figure 4 shows the schematic of the data acquisition system. The analog signals from the two LAr PMTs are split (not shown in the figure) and fed into the low and high gain inputs of a

10-bit digitizer (LeCroy Oscilloscope WavePro 735Zi DSO). The low and the high gain signals are matched later offline. This method increases the dynamic range so that signals from single photoelectrons and from α -emitters are collected with high sensitivity without ADC saturation [27]. A cross check is performed by comparing the pulse height obtained by this method with the pulse height from several γ -sources. The accuracy of the signal matching between the high and low gain is $\sim 2\%$. The data are collected with 5 000 points at 1GS/s with 500 ns pre-sample for pedestal subtraction. Data are stored on a hard disk and then analyzed offline. The signals from each PMT are fed into a CAEN N979 $\times 10$ amplifier before being fed into leading edge CAEN N840 discriminators where the thresholds have been set to 0.5 photoelectrons. The logic signals are then connected to a CAEN N405 unit for the coincidence between the two PMTs.

Neutron signals from the LSC are processed by an analog pulse shape discriminator module Mesytec MPD4 [28]. This module determines the fraction of fast (< 20 ns) component of the scintillation light. For electrons the prompt fraction F_p (prompt over total integrated pulse height) is about 0.95, while for proton recoils $F_p < 0.8$ (figure 5).

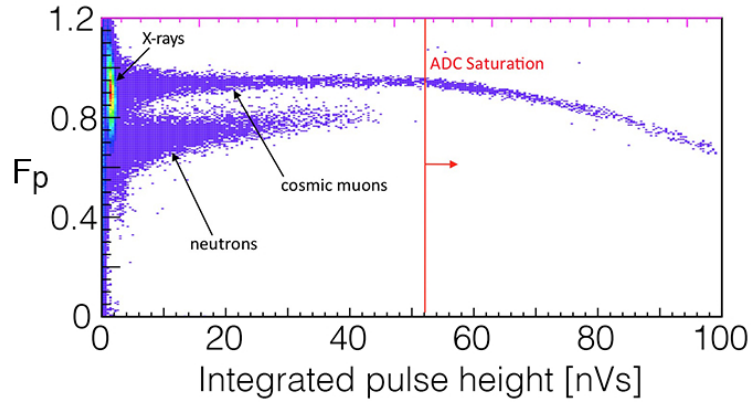


Figure 5. Prompt fraction F_p of scintillation light in the LSC versus integrated pulse height. The upper band is produced by electronic recoils from bremsstrahlung (generated by the neutron generator) and cosmic muons, the lower band by proton recoils from neutron scattering.

The energy calibration of the LSC is performed with radioactive γ -sources. The energy resolution is determined from the signals induced by backscattered photons from ^{137}Cs or ^{22}Na sources, which are detected by a small BaF crystal [29]. The time-of-flight between the LAr cell and the LSC is measured to select elastic events. The LSC signal is fed into a linear fan in/out module which feeds the timer and logic units. The time-of-flight between the LAr cell and the LSC is calculated from the time difference of the TAC output of the MPD4 module and the signal from the LAr cell. The time-of-flight is calibrated by the coincidence of the 511 keV back-to-back γ -rays from a ^{22}Na source located at mid-distance between the LAr cell and the LSC. Events are accepted within a time delay of 200 ns between the LAr and LSC signals. This trigger setting was used during part of the data taking (TR₂ data sample, see table 1 below). For the TR₁ data sample taken earlier a programmable trigger logic in the oscilloscope was used for the coincidence between the LAr and LSC signals.

3. Calibrations with γ -sources

3.1 Pulse height analysis

The light yield from the LAr cell is the ratio of collected to produced light intensities, which strongly depends on factors such as geometry, photomultiplier efficiency, wavelength shifter, etc. The energy calibration in LAr is performed by using the 60 keV photo-absorption peak from an external ^{241}Am source. The source is placed at a distance of 10 cm from the vessel to reduce pile-up events. The light yield has to be corrected for the finite integration time. As mentioned earlier, nuclear recoils contribute mostly to the fast component (τ_1), while the contribution from electrons to the slow component (τ_2) is larger. Therefore the light yield has to be corrected first for losses due to impurities in LAr which are reducing the lifetime of the slow component [30].

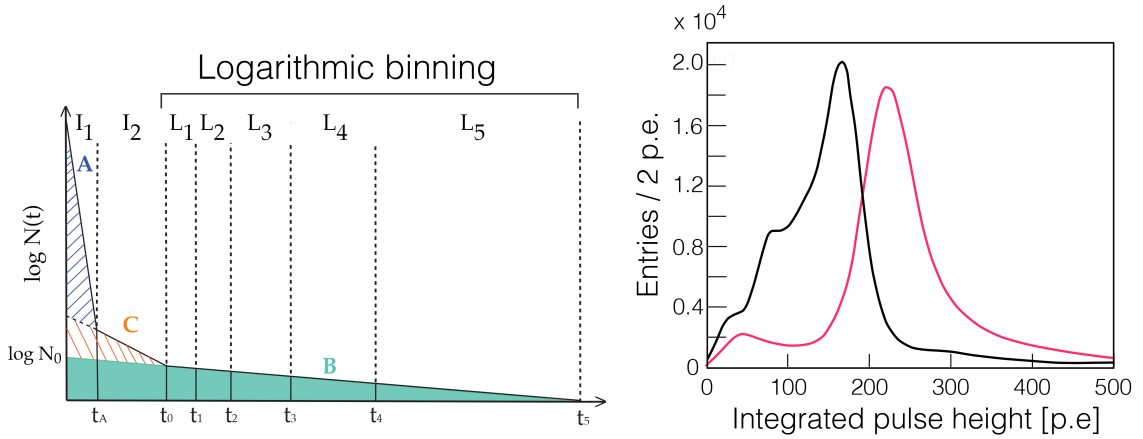


Figure 6. Left: logarithmic binning method showing the contributions of the populations A, B and C. Right: pulse height distribution from the 60 keV γ -source (in photoelectrons, p.e.) for the raw data (black curve) and after correction with the log binning method (red curve).

We have developed a new technique to correct for the reduced light yield caused by argon impurities. This event-by-event method consists in dividing the pulse shape in three time regions I_1 , I_2 , and L , as sketched in figure 6 (left). Time $t = 0$ corresponds to -20 ns below the maximum pulse height. The first interval (I_1) corresponds to $4\tau_1$. The integral over I_1 contains the contributions A from the fast component and B from the slow component. A third contribution C is present in the interval I_2 , between 40 ns and 100 ns. This component has been observed earlier in argon and is reported to stem from the wavelength shifter [31]. The rest of the pulse shape is divided logarithmically into $n = 5$ time bins L_i from t_0 to t_5 defined as

$$t_i = t_0 + \tau_2 \cdot \ln \left(\frac{n+1}{n+1-i} \right) \quad (3.1)$$

with $i = 1 \dots 5$ and where τ_2 is the measured decay time of the slow component. Thus the expected number of events in each bin L_i is constant. Impurities affect the late regions of the light pulse, hence affect only the slope of the slow component B but not its amplitude N_0 at $t = 0$. The measured number of entries in L_i can be obtained by building the arithmetic mean of the five bins. The contribution B_{corr} from the slow component, corrected for impurities, is then obtained by integrating

$N(t)$ with the time constant $\tau_2 = 1.6 \mu\text{s}$ which corresponds to pure LAr. Once B_{corr} is obtained, C is found from the I_2 integral and, finally, A from the I_1 integral after subtracting the contribution from B_{corr} and C . Details can be found in [13]. Let us define the fraction of prompt light determined with the logarithmic binning by the ratio

$$r_{LB} = \frac{A}{A + B_{corr} + C}. \quad (3.2)$$

Figure 6 (right) shows the raw energy distribution from the ^{241}Am source for runs taken under various purity levels. Mixing data with different purities leads to a spread of the deposited energy distribution (black curve). However, applying the logarithmic binning method to correct the spectrum leads to a decrease of the width of the distribution and shifts the distribution towards higher photoelectron numbers.

Light yield calibrations were performed periodically during data taking. The corrected average light yields are $3.75 \pm 0.08 \text{ p.e./keV}_{er}$ and $3.39 \pm 0.07 \text{ p.e./keV}_{er}$ for the TR₁ and TR₂ data respectively [13]. The slightly different light yields are due to the different thicknesses of wavelength shifter covering the surfaces of the PMTs. The long term stability of the light yield is shown in figure 7 for the TR₁ data. Further external radioactive sources were employed to cover a wide energy range: 122 keV photoelectron from ^{57}Co , 341 keV, 478 keV and 1060 keV Compton edges from ^{22}Na , ^{137}Cs and ^{22}Na respectively. Figure 8 illustrates the perfect linearity of the system.

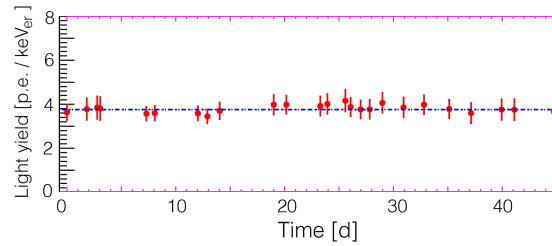


Figure 7. Light yield as a function of time for the TR₁ data sample.

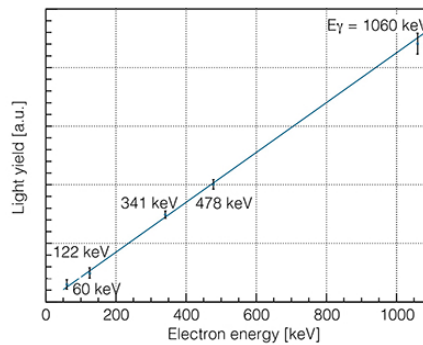


Figure 8. Light yield from LAr measured with various γ -sources (in arbitrary units). In the present work the calibration is obtained from the light yield of the 60 keV ^{241}Am photopeak.

The response to very low energy electrons was also measured with a ^{83}Rb source (half-life of 86 days) of about 180 kBq which was introduced into the system. A ^{83}Rb trap was directly connected to the gas system. The daughter metastable $^{83\text{m}}\text{Kr}$ nuclide (half-life of 1.8 h) illuminates the central part of the LAr cell and diffuses photons uniformly. The measured light yield at 32.1 keV is obtained as 3.68 ± 0.15 p.e./keV_{er} in good agreement with results from the other sources.

3.2 Trigger efficiency

Understanding the low energy roll-off of the trigger efficiency is essential to determine L_{eff} , especially for low energy recoils. We have studied the trigger efficiency with the 511 keV annihilation γ -rays from a ^{22}Na positron source. The energy distribution of the Compton scattered electron is linear at low energy, as illustrated by the red dashed box in figure 9 (left). As a comparison figure 9 (right) shows the measured electron recoil spectrum in LAr.

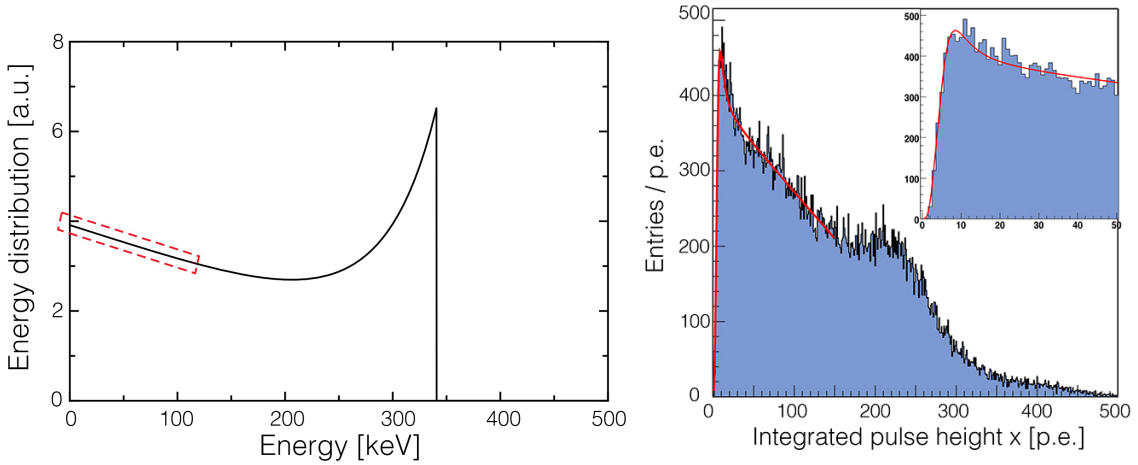


Figure 9. Left: theoretical electron recoil spectrum from the 511 keV annihilation γ of a ^{22}Na positron source (computed with the Klein–Nishina formula). The red dashed box shows the linear part of the spectrum at low energy. Right: measured integrated pulse height x of the prompt light in photoelectrons (p.e.) fitted with the function (3.3) (red curve). The inset shows the low energy region.

The low energy part is fitted with the following model function:

$$\mathcal{F}(x) = S \cdot [(D + E \cdot x) + L(a, \mu, \sigma)]. \quad (3.3)$$

The function

$$S = (1 - e^{-\frac{x}{b}})^c \quad (3.4)$$

describes the trigger efficiency, where x is the pulse height in photoelectrons. The term $(D + E \cdot x)$ describes the linear shape of the spectrum at low recoil energies. The parameters D and E are determined by the fit. The Landau distribution $L(a, \mu, \sigma)$ takes the Čerenkov light from the γ -ray interaction in the PMT glass into account, where a is a normalization parameter, μ the most probable value and σ a scale parameter (adapted from the CERNLIB routine G110 *denlan*). Most of the Čerenkov events contribute to the prompt light.

The fit is performed in two steps. First, the linear part of the spectrum is fitted. Second, the parameters of the linear function and the Landau function are fixed and the parameters b and c are

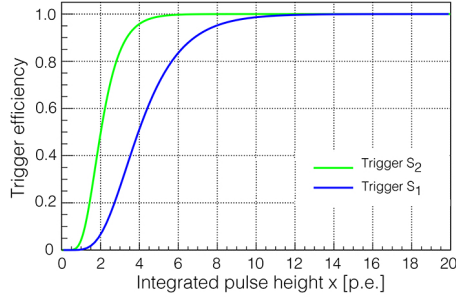


Figure 10. Trigger efficiency S for the ^{22}Na source measurement as a function of integrated pulse height x for the two trigger settings.

determined. The measured trigger efficiency S is displayed in figure 10 by the green curve for the S_2 data. The efficiency is $\sim 100\%$ at 8 photoelectrons (p.e.) , $\sim 96\%$ at 4 p.e., $\sim 50\%$ at 2 p.e. and $\sim 5\%$ at 1 p.e. The roll-off of the trigger efficiency for the TR_1 data that used the programmable trigger logic in the oscilloscope is shown by the blue curve. The efficiency is lower, reaching $\sim 95\%$ at 8 p.e., $\sim 55\%$ at 4 p.e. and $\sim 6\%$ at 2 p.e.

4. Neutron data

The neutron generator was operated most of the time at 80 kV to keep the accidental background from bremsstrahlung generated by the neutron generator at an acceptable level. The corresponding neutron flux is 6×10^5 neutrons/s into 4π . The scattered rate from the sensitive LAr volume, recorded by the LSC, is 1 neutron/min. The background rate is estimated to be 5/min, caused mainly by diffusely scattered neutrons and X-rays from bremsstrahlung ($\sim 3\text{--}4/\text{min}$), and to a lesser extent by cosmic muons saturating the MPD4 analog pulse shape discriminator.

Θ [$^\circ$]	T_{nr} [keV] [keV]	Trigger	Running time [10^3s]	Trigger	Running time [10^3s]
25	11.5	TR_1	269	TR_2	382
30	16.4	TR_1	284	TR_2	234
40	28.5	TR_1	379	TR_2	219
50	43.4	TR_1	291	–	–
60	60.5	TR_1	288	–	–
90	119.5	TR_1	196	–	–

Table 1. Angular settings and corresponding argon recoil energies. The trigger type (see text) and running time are also given.

Neutron scattering data are measured at six angles corresponding to argon recoil energies between 11 and 120 keV (table 1). The data are taken with the two different triggers TR_1 and TR_2 . The raw data are first corrected for impurities and for the trigger efficiency roll-off described in section 3.2.

The discriminator r_{LB} (3.2), which is based on the logarithmic binning method (and thus differs from the prompt fraction F_p), suppresses background from accidental coincidences with X-rays, γ -rays and cosmic muons. As an example, figure 11 shows a scatterplot of r_{LB} in LAr as a function of integrated pulse height for the $\Theta = 25^\circ$ data sample. Events above the green line are mostly neutron induced, those below the line stem mostly from background.

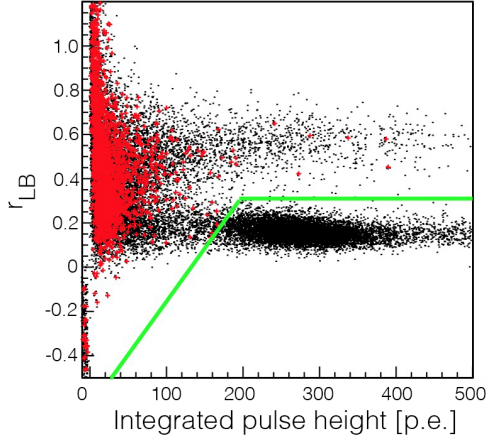


Figure 11. Scatterplot of the r_{LB} discriminator versus integrated pulse height for $\Theta = 25^\circ$. The green line shows the cut applied to select elastic neutron scattering (red region) and reduce background.

Figure 12 (left) shows a scatterplot of the prompt light fraction F_p (defined in section 2) versus time-of-flight for $\Theta = 25^\circ$. The event distributions for the data taken at the larger scattering angles are similar. The time-of-flight projection is shown in figure 12 (right). Events in red are nuclear recoils, while events in blue are mostly due to background (lying below the green line in figure 11). Since the LAr and the LSC triggers are not correlated the accidental background is uniform and appears as a flat component in the time-of-flight spectrum.

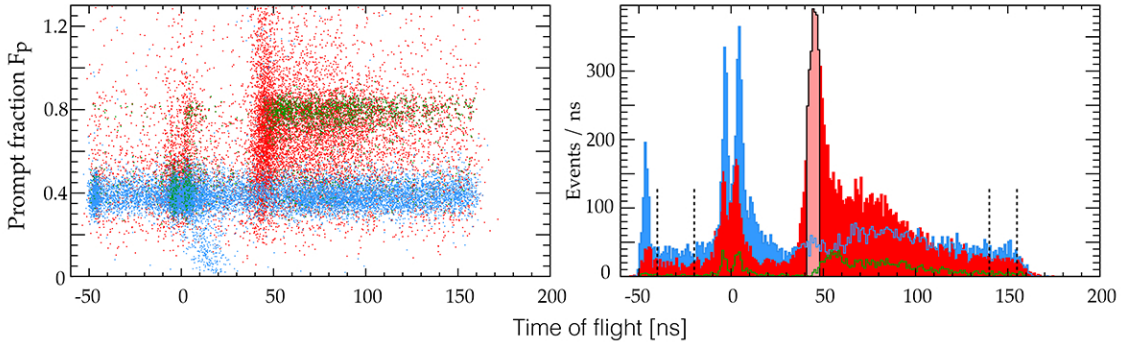


Figure 12. Prompt fraction versus time-of-flight (left) and corresponding projection on the time-of-flight axis (right) for $\Theta = 25^\circ$. The events in red correspond to nuclear recoils selected by the r_{LB} cut, while the anticut selects the electron-recoils (events in blue). The events in green correspond to nuclear recoils at energies above 120 photoelectrons. The elastic neutron scattering events selected to calculate L_{eff} lie in the pink window. The vertical dashed lines delimit the intervals used to evaluate the contribution from accidental events.

The most prominent red peak is due to elastically scattered neutrons at the expected time-of-flight of about 43 ns. These events are also associated with large values of F_p and therefore contribute mostly to the prompt light. An accumulation of events is observed around 80 ns, corresponding to inelastically scattered neutrons in LAr. The broad tail of this distribution is mainly due to neutron scattering outside the active volume and inelastically scattered neutrons. The two peaks around zero time-of-flight are due to cosmic muons flying between the LAr cell and the LSC, the peak at -3.1 ns corresponding to muon from the LSC to the LAr cell and the one at $+3.1$ ns to those flying in the opposite direction. In the electronic (blue) recoil band an accumulation of events is observed above the elastic peak. They are correlated in time with neutrons scattered inelastically in the target but outside the sensitive volume, while the ensuing emitted photons are converted in the active volume. The events shown in dark green are nuclear recoil events with energy deposits above 120 photoelectrons, mostly due to multiple neutron scattering. The accumulation of events at -50 ns is due to an electronics artifact at the edge of the trigger time window.

Two cuts are applied to select elastic neutron scattering. A time-of-flight cut window is applied between -2 ns and $+6$ ns of the most probable value for the elastic peak (pink area in figure 12 corresponding to $41 - 48$ ns at $\Theta = 25^\circ$). The cut by the r_{LB} discriminator (green line in figure 11) removes efficiently accidental coincidences with X-rays, γ -rays, inelastic scatters and cosmic muons. Figure 13 shows the contribution to the fast light for the selected data. The recoil energy distribution shown in this figure will be fitted to the Monte Carlo data, as described in section 5.

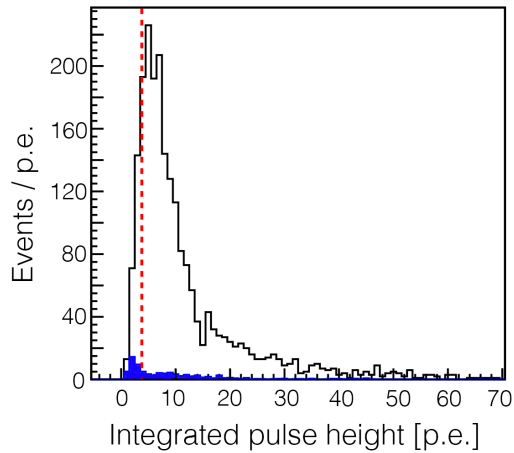


Figure 13. Nuclear recoil energy distributions at $\Theta = 25^\circ$ (in photoelectrons). The plot shows the contribution to the fast light. The accidental spectrum is shown in blue. The vertical red dashed line indicates the pulse height corresponding to 90% trigger efficiency.

To estimate the contribution from residual accidentals we choose events lying far from the elastic peak in the two intervals delimited by the vertical dashed lines in figure 12. The background spectra below and above the elastic peak are found to be compatible. The contribution from accidentals is negligible, as shown by the blue histogram in figure 13. However, neutrons that scatter off various materials outside the LAr cell before or after interacting in the LAr sensitive volume also contribute background. This external background cannot be removed from the data and is

therefore taken into account by Monte-Carlo simulation.

5. Monte-Carlo simulation

The detector response was simulated extensively with GEANT4. The Monte-Carlo simulation takes into account the neutron generator assembly with its shielding and collimator, the cryostat and the various components of the LAr cell such as the vacuum vessel, the TPB reflector foil, the photomultipliers, the support mechanics, and the LSC. A photograph of the LAr cell and a drawing of the simulated one are compared in figure 14.

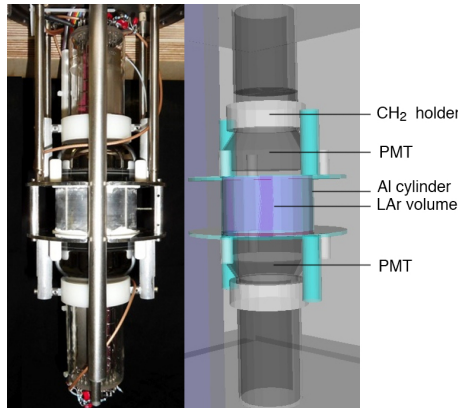


Figure 14. Photograph of the LAr cell and PMT (left) and drawing of its simulated counterpart (right).

In the simulation monoenergetic neutrons of 2.45 MeV are emitted isotropically into 4π . A sample of 100 million interactions in the active LAr volume was generated at each measured angle. Figure 15 (left) shows for $\Theta = 25^\circ$ the various simulated contributions to the nuclear recoil energy spectrum (left) and to the time-of-flight distribution (right) prior to smearing by the experimental resolution. A clear elastic peak is observed at the expected recoil energy, as well as the exponentially decreasing material background tail (black histogram). Neutrons that scatter elastically only once in the active LAr volume are shown by the blue histogram. The dashed red histogram corresponds to single scattering in the active LAr volume, preceded or followed by scattering elsewhere in the apparatus (external background). The multiple scattering events in LAr are shown in green. Inelastically scattered neutrons in LAr are represented by the dashed orange histogram. The energy deposits are shifted to higher values by the conversion of the γ -rays emitted during the de-excitation of the argon atoms.

Figure 15 (right) shows the corresponding time-of-flight distributions at $\Theta = 25^\circ$. The position in time of the elastic peak is consistent with data. A comparison with the data of figure 12 shows that nearly all inelastic scatters are removed by the time-of-flight cut of 41–48 ns. Their time-of-flight distribution (enhancement around 70 ns) is also in good agreement with data.

The position of the single elastic peak and its resolution depend on the sizes of the neutron source and on the solid angle acceptances of the LSC and LAr cell. Uncertainties on recoil energies are determined by fitting a Gaussian to the single elastic peak. Before applying the time-of-flight cut to the simulated data the finite time resolution is taken into account by convoluting a Gaussian

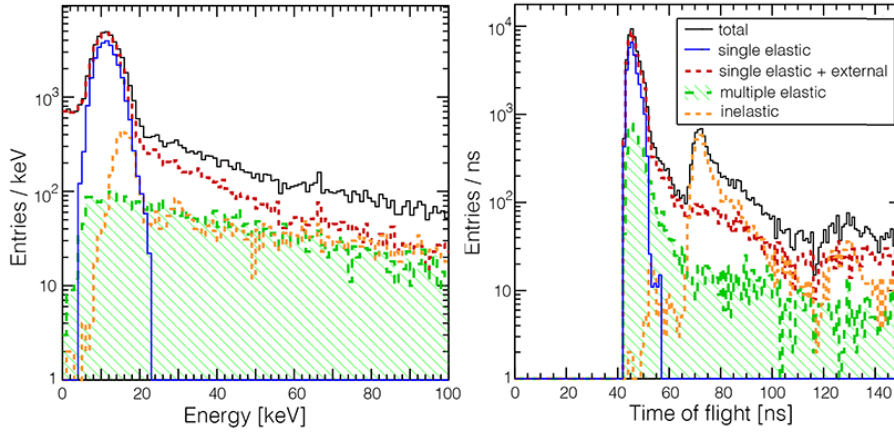


Figure 15. Simulated recoil energy distribution at $\Theta = 25^\circ$ (left) and corresponding time-of-flight spectrum (right) from the contributions listed in the inset: single elastic scattering (with and without external scattering), multiple scattering and inelastic scattering in the LAr sensitive volume.

with the experimental rms resolution of 2.88 ns. The recoil energy distribution at $\Theta = 25^\circ$ is shown in figure 16 after the time-of-flight cut. The black histogram will be used to fit to the data of figure 13.

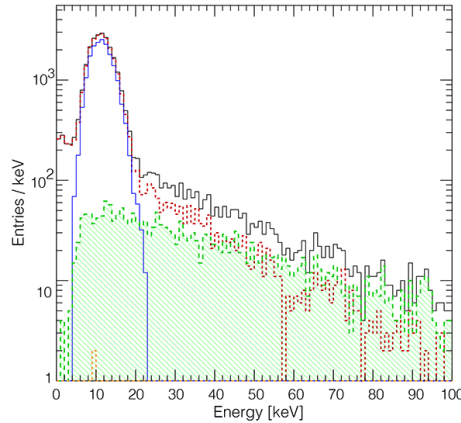


Figure 16. Simulated recoil energy distribution at $\Theta = 25^\circ$ after the time-of-flight cut. The color codes are the same as in figure 15.

The various contributions to the nuclear recoil spectrum after the time-of-flight cut are listed in table 2 for the six scattering angles. Below 40° single elastic scattering off argon is the dominant contribution to the recoil energy spectra. The contribution from multiple scattering in LAr is small ($\sim 10\%$) thanks to the small dimension of the LAr cell compared to the elastic neutron mean free path. The decreasing contribution of elastic events with increasing scattering angle is due to the angular dependence of the differential elastic cross section for neutron-argon interaction at 2.45 MeV which reaches a minimum around 90° [32].

Θ	Single elastic	Single elastic + external	Multiple elastic	Inelastic
[$^\circ$]	[%]	[%]	[%]	[%]
25	67.7	23.5	8.8	0.02
30	65.3	25.1	9.6	0.02
40	54.8	31.4	13.7	0.06
50	49.7	34.3	16.0	0.04
60	40.9	31.8	20.5	0.04
90	29.1	45.1	25.6	0.18

Table 2. Rms contributions to the recoil spectrum after time-of-flight cut.

6. Data analysis

6.1 χ^2 -fits

The method developed in this work to extract L_{eff} follows the one described in [18, 19] for liquid xenon. We have performed a χ^2 -minimization to determine the relative light efficiency L_{eff} (2.1) as a function of recoil energy T_{nr} at six scattering angles.

To obtain the simulated spectrum in photoelectrons the energies in keV are first multiplied by the free parameter L_{eff} under χ^2 test and then by the light yield Ly measured with the ^{241}Am source. The number of photoelectrons $N_{p.e.}$ is allowed to fluctuate according to a Poisson distribution and the energy resolution is described by the rms deviation of a Gauss distribution defined as $R\sqrt{N_{p.e.}}$, where R is the second free parameter under χ^2 test. The gain fluctuation of the PMTs is taken into account by convoluting the nuclear recoil energy spectrum in photoelectrons with a Gaussian distribution with rms deviation $R_{p.e.}\sqrt{N_{p.e.}}$. The parameter $R_{p.e.}$ is determined from the resolution of the measured PMT single photoelectron distribution and found to be $R_{p.e.} = 0.4$ [13]. The trigger efficiency (figure 10) is then taken into account to obtain the simulated recoil energy spectrum. For each scattering angle the χ^2 is computed as follows:

$$\chi^2(L_{eff}, R) = \sum_{i=1}^N \frac{[h_i - h_{MC,i}(L_{eff}, R)]^2}{\sigma_i^2 + \sigma_{MC,i}^2}, \quad (6.1)$$

where $L_{eff} \equiv L_{eff}(T_{nr})$ and the resolution $R \equiv R(T_{nr})$ are the free parameters. The events are divided into N bins expressed in photoelectrons. The number of events in the measured and the simulated bins i are labelled h_i and $h_{MC,i}$ respectively. The corresponding statistical uncertainties are denoted by σ_i and $\sigma_{MC,i}$. The fit range is chosen separately for each angle in such a way as to avoid the bias induced at low energy by the trigger inefficiency (which underestimates L_{eff}) and by the high energy tail (which overestimates L_{eff}). Fits are performed for different photoelectron ranges and the suitable fit range is selected as the one associated with stable values of L_{eff} . For example, at 25° the range fitted was from 2 to 38 photoelectrons (see figure 13). The χ^2 surfaces are illustrated in figure 17 (left) as a function of R and L_{eff} for $\Theta = 25^\circ$ (S_2 data), 40° (S_2 data) and 90° (TR_1 data).

Following the method described in [19] a rotated paraboloid is fitted to the χ^2 map generated around the minimum value for each of the six scattering angles Θ_j . This procedure to extract the

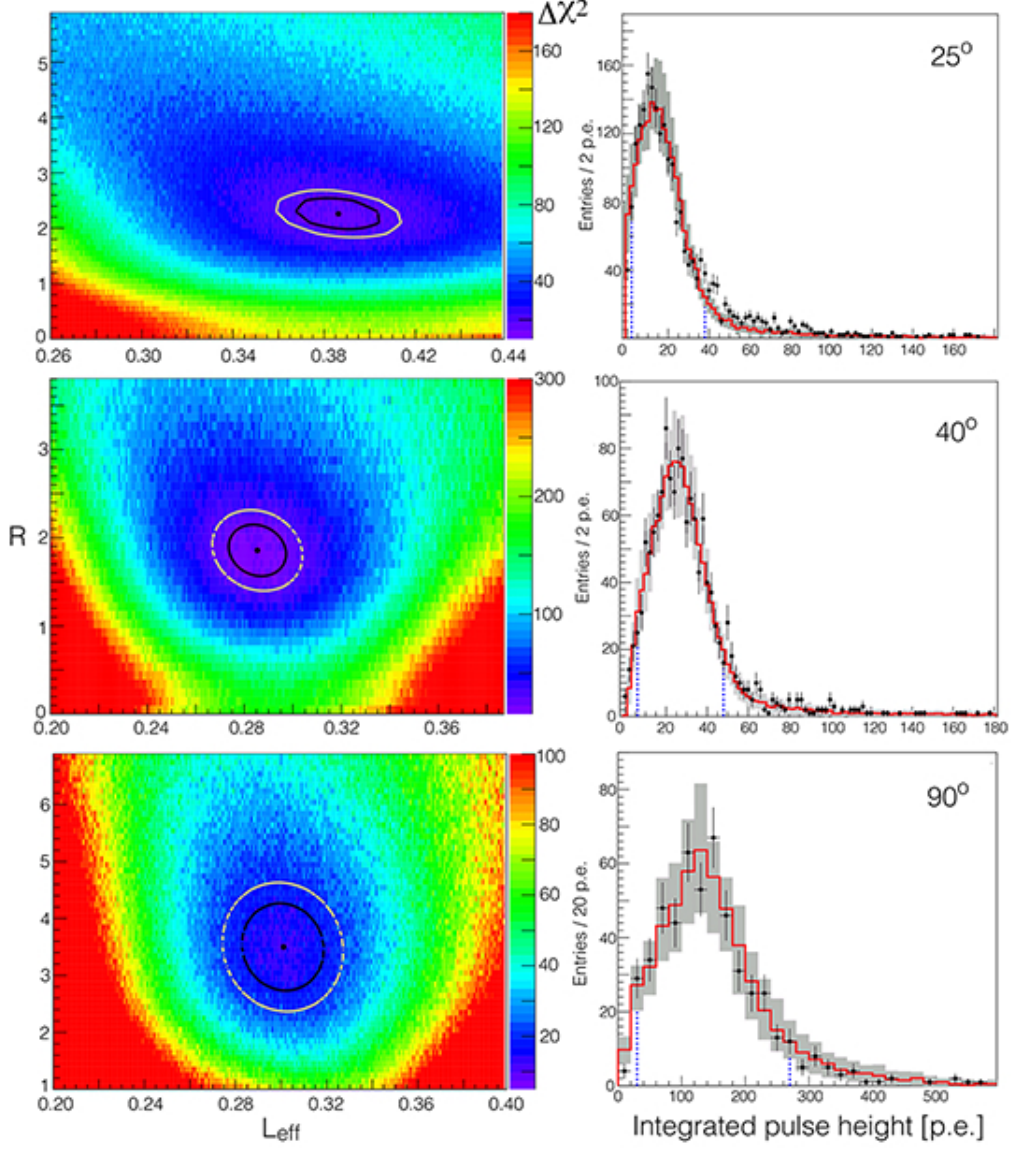


Figure 17. Left: χ^2 maps as a function of L_{eff} and R for three scattering angles. The location of the minimum χ^2 is shown by a dot. The curves are the 1σ and 2σ contour lines. Right: corresponding Monte-Carlo fits (red histograms) to the energy recoil spectra (black data points) with rms errors (grey zones). The dotted blue lines delimit the fitted ranges.

final values for $L_{eff,j}$ and R_j ($j = 1..6$) averages out small variations on the χ^2 surface. The rotated χ^2 is defined as

$$\chi^2(L_{eff}, R) = \chi_{min,j}^2 + \left[\frac{(L_{eff} - L_{eff,j}) \cos \omega_j - (R - R_j) \sin \omega_j}{A_j} \right]^2 + \left[\frac{(L_{eff} - L_{eff,j}) \sin \omega_j - (R - R_j) \cos \omega_j}{B_j} \right]^2. \quad (6.2)$$

where the paraboloid rotation angle ω_j and the parameters A_j and B_j are determined by the fit, together with the minimum $\chi_{min,j}^2$. The location of $\chi_{min,j}^2$ is indicated by the black dots in figure 17 (left). The 1σ and 2σ contours, determined by the values $\chi_{min}^2 + 2.3$ and $\chi_{min}^2 + 6.2$, respectively, are also shown in figure 17 (left).

Figure 17 (right) shows the measured nuclear recoil distributions (black dots) and the Monte-Carlo fits (red histograms). The grey zones show the statistical uncertainties on the fit, determined by the 1σ contours in figure 17 (left). The blue dashed lines correspond to the fit ranges used to compute the χ^2 . The results of the fits are given in table 3 with statistical errors only.

Θ [$^\circ$]	L_{eff}	ΔL_{eff} (stat)	R	ΔR	χ^2	d.o.f
25	0.386	0.0185	2.26	0.29	18.0	16
30	0.305	0.0142	1.84	0.28	19.8	18
40	0.285	0.0127	1.86	0.30	20.9	19
50	0.294	0.0159	2.79	0.42	36.8	24
60	0.283	0.0167	3.43	0.72	33.6	20
90	0.301	0.0177	3.49	0.74	15.4	10

Table 3. Results of the fits. Listed are the optimum values of the scintillation efficiency L_{eff} and resolution R as a function of scattering angle Θ . The rms errors are statistical only. The χ^2 values and numbers of degrees of freedom (d.o.f) refer to the least square fit (6.1).

6.2 Systematic errors

The reliability of the procedure to extract L_{eff} by including the additional fit parameter R has been studied in [19] for liquid xenon. The analysis was cross-checked by describing the energy dependence of the resolution with model functions without free parameters. No significant deviation was observed between the values of L_{eff} obtained with this method and those determined with the resolution left as a free parameter. A similar test is performed in our work: the measured nuclear recoil spectra with the elastic peak above trigger efficiency roll-off are fitted with Gaussian functions to obtain the experimental resolution. The simulated contribution of the energy spread due to the finite size of the detector is then subtracted quadratically from the measured resolutions. No significant deviation is observed on L_{eff} between the two methods (figure 18).

The following sources of systematic uncertainties are taken into account. The uncertainty in the light yield ΔLy measured with the ^{241}Am source is determined by the error on the calibration constant, estimated to $\pm 2.1\%$ for the TR_1 and $\pm 1.6\%$ for the TR_2 data. The uncertainty $\Delta Trig$ on the trigger efficiency is determined by changing the values of the parameters b and c in (3.4). The error $\Delta\Theta$ on the angular setting of the LSC is estimated to be $\pm 0.5^\circ$. The systematic uncertainties are listed in table 4 together with our final results. The main contributions to the systematic error on L_{eff} stem from the calibration of the americium source and from the trigger efficiency roll-off. The latter large value at 50° is due to the trigger settings for the TR_1 data, for which the effect of the roll-off is more pronounced (see figure 10). To estimate the systematic error introduced by the uncertainty on the lifetime of the slow component we have varied τ_2 between 1.5 and 1.6 μs . This

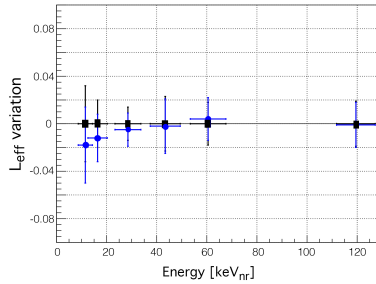


Figure 18. Plot showing how L_{eff} varies when using fixed resolutions R (blue circles) instead of free fit parameters (black rectangles).

leads to an additional (negligible) systematic error of typically 0.003 on L_{eff} . The uncertainties in nuclear recoil energies are determined by the angular acceptance of the LSC and are estimated by Monte-Carlo simulation. The total uncertainties on L_{eff} are obtained by summing the statistical errors (table 3) and systematic errors quadratically.

Θ [$^\circ$]	T_{nr} [keV]	L_{eff}	ΔL_{eff}	ΔL_y	$\Delta Trig$	$\Delta \Theta$
25	11.5 ± 2.8	0.386	0.032	0.0068	0.0252	0.0028
30	16.4 ± 3.9	0.305	0.020	0.0054	0.0126	0.0010
40	28.5 ± 5.2	0.285	0.014	0.0051	0.0013	0.0007
50	43.4 ± 6.0	0.294	0.023	0.0064	0.0154	0.0006
60	60.5 ± 7.1	0.283	0.018	0.0062	0.0022	0.0004
90	119.5 ± 7.7	0.301	0.019	0.0064	0.0000	0.0000

Table 4. Scintillation efficiency L_{eff} and rms error ΔL_{eff} as a function of scattering angle. The last three columns list the rms systematic errors to ΔL_{eff} .

6.3 Discussion

The final results for the relative scintillation efficiency from table 4 are plotted in figure 19, together with previous measurements. Above $\simeq 25$ keV recoil energy L_{eff} is constant with a mean value $\langle L_{eff} \rangle = 0.30 \pm 0.02$. This result is in fair agreement, although somewhat higher, than that from MicroCLEAN which reports an average value of 0.25 ± 0.02 above 20 keV [16]. Our simulations are in excellent agreement with data and we stress here the importance of modelling accurately interactions outside the active volume, in particular for large active volumes (3.14 ℓ in [16] compared to 0.2 ℓ in the present work).

Below 20 keV our data show the upturn in L_{eff} already reported by MicroCLEAN [16] but not observed by SCENE [17]. L_{eff} is usually predicted to decrease at low energy due to the combination of energy loss (described by Lindhard’s theory) and scintillation quenching (described by Birk’s law) [33]. This prediction is shown by the dotted curve in figure 19. However, based on the work described in [35] the NEST group has recently applied on argon their model for liquid xenon [36]. The authors developed a parametrization to compare with liquid xenon data that reproduce

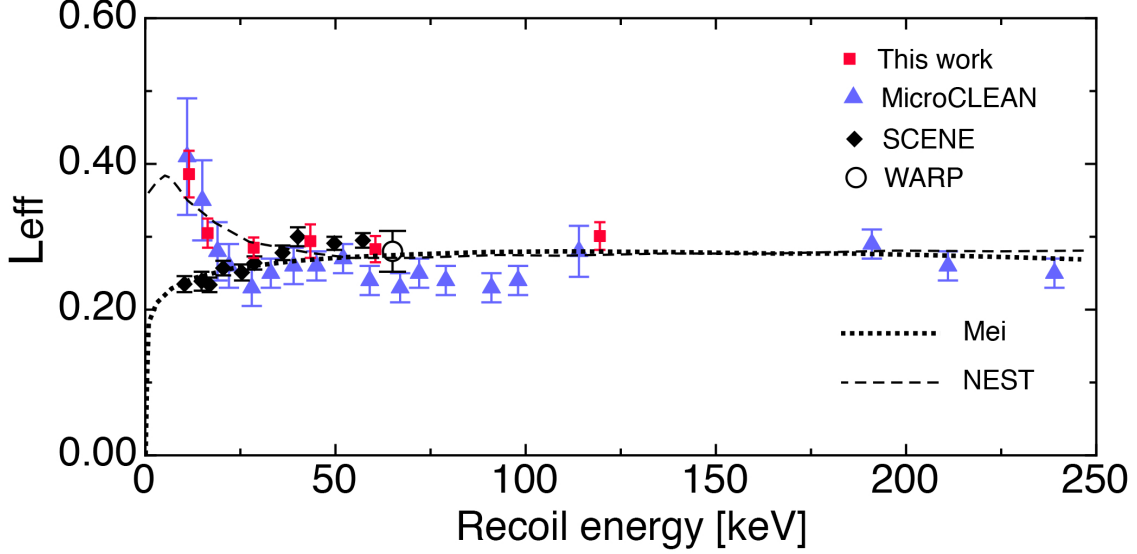


Figure 19. Relative scintillation L_{eff} in liquid argon as a function of nuclear recoil energy from the present experiment (red squares), compared to the previous measurements by MicroCLEAN (blue triangles) [16], SCENE (black diamonds) at zero electric field [17] and WARP (open circle) [15]. The dotted and dashed curves show the predictions from the theoretical models by Mei [33] and NEST [34].

the upturn observed here and by MicroCLEAN. The upturn could for instance be due to an increasing exciton-ion ratio at low energies, which would lead to an increasing light yield since it takes less energy to excite than to ionize [37]. The NEST prediction extrapolated to LAr [34] is shown by the dashed curve in figure 19.

7. Conclusions

Summarizing, the knowledge of the scintillation efficiency L_{eff} at low nuclear recoil energies is important for direct dark matter searches using noble liquids. We have measured L_{eff} for nuclear recoils, relative to electrons, between 11 keV and 120 keV in liquid argon. Single elastic neutron-argon scattering dominates thanks to the small active volume of our argon cell and the well collimated neutron beam, while the contamination from neutron inelastic scattering is negligible. A χ^2 minimization is performed leaving L_{eff} and the energy resolution as free parameters. The extraction of L_{eff} is challenging at very low energy where systematic uncertainties on L_{eff} are determined by the inefficiency of the trigger. At higher energy the uncertainties on L_{eff} are dominated by statistical errors. The scintillation efficiency is constant with mean value $\langle L_{eff} \rangle = 0.30 \pm 0.020$ between 16 keV and 120 keV. The results below 20 keV confirm the energy upturn reported earlier. The increasing value of L_{eff} will enhance the detection efficiency for low mass WIMPs and be beneficial to dark matter searches using LAr.

Acknowledgments

The contribution of P. Otyugova to the design and installation of the neutron generator facility is

gratefully acknowledged. This work was supported by a grant from the Swiss National Science Foundation.

References

- [1] T A. Porter, R. P. Johnson, and P. W. Graham, *Annu. Rev. Astron. Astrophys.* **49** (2011) 155
- [2] G. Jungman, M. Kamionkowski, K. Griest, *Physics Reports* **267** (1996) 195
- [3] M. Drees and G. Gerbier in *Review of Particle Physics, Chin. Phys.* **C 38** (2014) 090001, p 353
- [4] E. Aprile *et al.* (XENON100 Collaboration), *Phys. Rev. Lett.* **107** (2011) 131302
- [5] D.S. Akerib *et al.* (LUX Collaboration), *Phys. Rev. Lett.* **112** (2014) 091303
- [6] V. Khachatryan *et al.* (CMS Collaboration), *JHEP* **09** (2012) 094
- [7] V. Khachatryan *et al.* (CMS Collaboration), *arXiv:1408.3583* (2014)
- [8] P.-A. Amaudruz *et al.* (DEAP Collaboration), Int. Conf. on High Energy Phys. (ICHEP 2014), Valencia, *arXiv:1410.7673*
- [9] A. Hime *et al.* (MiniCLEAN Collaboration), Proc. of DPF-2011 Conf., Providence, RI, *arXiv:1110.1005*
- [10] T. Alexander *et al.* (DarkSide Collaboration), *Journal of Instrumentation* **8** (2013) C11021
- [11] C. Amsler *et al.* (ArDM Collaboration), *Journal of Instrumentation* **5** (2010) P11003
- [12] A. Hitachi *et al.*, *Phys. Rev.* **B 27**(1983) 5279
- [13] W. Creus, *Light Yield in Liquid Argon for Dark Matter Detection*, PhD Thesis, University of Zurich (2013)
- [14] W. H. Lippincott *et al.*, *Phys. Rev.* **C 78** (2008) 035801
- [15] R. Brunetti *et al.*, *New Astronomy Reviews* **49** (2005) 265
- [16] D. Gastler *et al.*, *Phys. Rev.* **C 85** (2012) 065811
- [17] H. Cao *et al.* (SCENE Collaboration), *Phys. Rev.* **D 91** (2015) 092007
- [18] G. Plante *et al.*, *Phys.Rev.* **C 84** (2011) 045805
- [19] G. Plante, *The XENON100 Dark Matter Experiment: Design, Construction, Calibration and 2010 Search Results with Improved Measurement of the Scintillation Response of Liquid Xenon to Low-Energy Nuclear Recoils*, PhD Thesis, Columbia University (2012)
- [20] L. Baudis, *Journal of Physics: Conference Series* **375** (2012) 012028
- [21] NSD-Fusion GmbH, <http://www.nsd-fusion.com/>
- [22] V. Boccone *et al.* (ArDM Collaboration), *Journal of Instrumentation* **4** (2009) P06001
- [23] Sumitomo Cryogenics of America, INC. F-70H and F-70L Helium Compressors
- [24] https://www-off-axis.fnal.gov/flare/technical_papers/Brochre_Gas_Purification.pdf
- [25] <http://www.tequipment.net/TTi/TSX-3510P/DC-Power-Supplies/Lab-Power-Supplies/>
- [26] <http://www.scionix.nl>, see also P. Schotanus, Neutron Workshop at CIEMAT (2006)
- [27] C. Regenfus *et al.*, *J. Phys. Conf. Ser.* **375** (2012) 012019

- [28] <http://www.mesytec.com/datasheets/MPD-4.pdf>
- [29] G. Dietze, *IEEE Transactions on Nuclear Science* **26** (1979) 398
- [30] C. Amsler *et al.*, *Journal of Instrumentation* **3** (2008) P02001
- [31] E. Segreto, *Phys. Rev. C* **91** (2015) 035503
- [32] National Nuclear Data Center, <http://www.nndc.bnl.gov>
- [33] D.-M. Mei, Z.-B. Yin, L. C. Stonehill, A. Hime, *Astropart. Phys.* **30** (2008) 12, *arXiv:0712.2470*
- [34] M. Szydakis *et al.* (NEST Team), http://nest.physics.ucdavis.edu/data/LBL_NEST_2012.pdf
- [35] F. Bezrukov, F. Kahlhoefer, M. Lindner, *Astropart. Phys.* **35** (2011) 119, *arXiv:1011.3990*
- [36] M. Szydakis *et al.*, *arXiv:1106.1613*
- [37] M. Szydakis, private communication