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**FLIGHT TRANSPORTATION LABORATORY  
REPORT R 91-4**

**PRESENTATIONS FROM THE  
MIT/INDUSTRY COOPERATIVE RESEARCH  
PROGRAM ANNUAL MEETING, 1991**

**Belobaba, Williamson, et al.**

**May 1991**

**MIT**

**DEPARTMENT  
OF  
AERONAUTICS  
&  
ASTRONAUTICS**

**FLIGHT TRANSPORTATION  
LABORATORY  
Cambridge, Mass. 02139**

## FTL REPORT R 91-4

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**O-D / SEGMENT SEAT INVENTORY CONTROL:**

**Modeling and Implementation Issues**

**Professor Peter P. Belobaba  
MIT Flight Transportation Laboratory**

**MIT/Industry Cooperative Research Program  
Annual Meeting  
May 23, 1991**

## PASSENGER ITINERARY CONTROL

- In contrast to the control of seat inventories by flight leg/booking class, passenger itinerary control requires methods that can distinguish among passenger itineraries vying for seats on the same flight leg, even within the same fare product "category".
- Passenger Itinerary Control concepts can be applied through:

**DUAL/OVERLAP FLIGHTS:** Two or more flight numbers representing different itinerary "paths" assigned to a single flight leg.

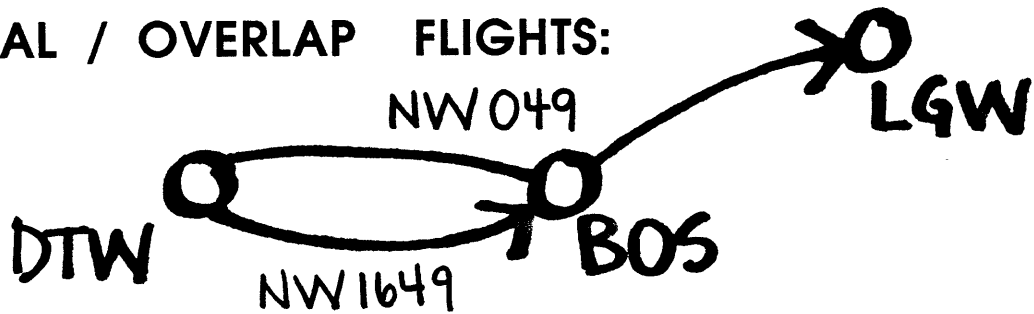
**POINT OF SALE CONTROL:** Seat availability is differentiated between points of sale due to currency or net revenue differences.

**SEGMENT CONTROL:** Seat availability is managed by booking class and passenger itinerary on a multiple-leg flight with the same flight number.

**O-D CONTROL:** Seat availability is managed by fare category and O-D itinerary, even across connecting flights.

# PASSENGER ITINERARY CONTROL

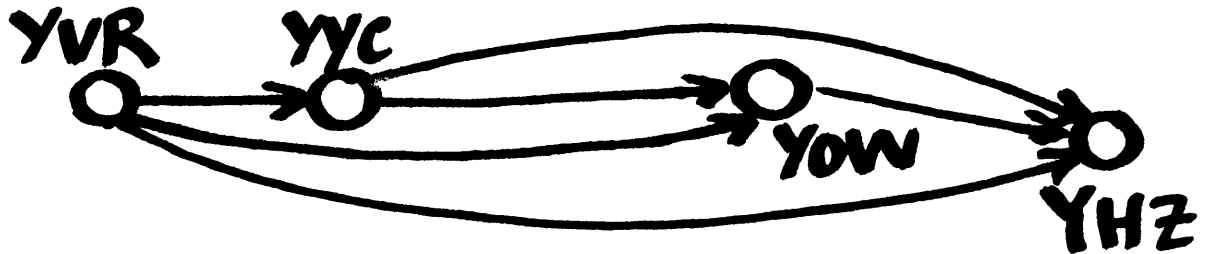
DUAL / OVERLAP FLIGHTS:



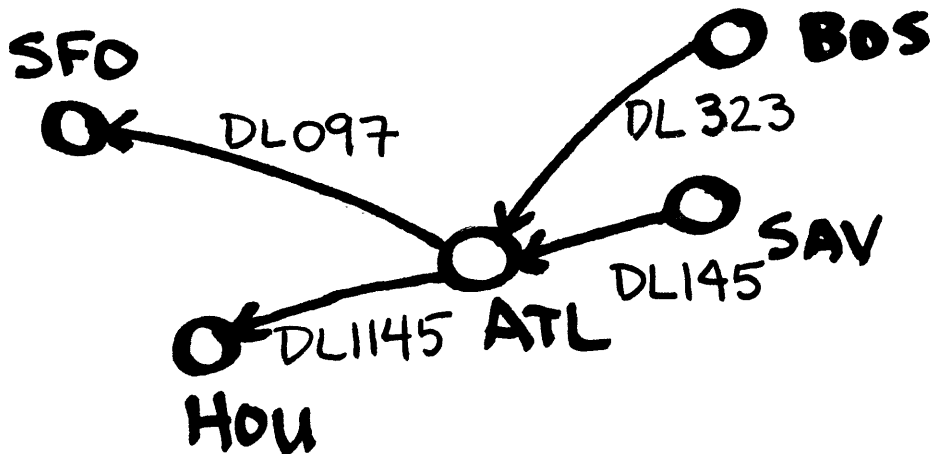
POINT OF SALE: KL 015



SEGMENT CONTROL: AC113



CONNECTING O-D CONTROL:



## NETWORK OPTIMIZATION APPROACHES

- Traditional O.R. approach to dealing with itinerary control is to perform a joint optimization over the entire network of flight legs defined by the problem.
  
- Network formulations and/or mathematical programming approaches are used to find the optimal allocation of seats to each origin-destination itinerary and fare type (ODF) on each flight leg:
  - requires demand forecasts and fare values for each ODF
  
  - problem representation can be deterministic or probabilistic
  
  - solution ensures balanced ODF allocations across flight legs
  
  - ODF allocations are "optimal" given assumed mathematical formulation of problem

- Implementation of these "optimal" network ODF seat allocations as ODF booking limits, however, can have substantial negative revenue impacts.
  - use of partitioned or discrete booking limits lowers expected revenue relative to nested limits
  - negative revenue impact becomes larger with more ODF allocations
  - dynamic simulations show that use of "optimal" partitioned segment/class limits on a 3-leg flight can result in revenue reductions of 1% to 2% relative to simple leg/booking class control
- The optimal solution to an assumed mathematical formulation does not maximize revenues when implemented this way.

# NESTING OF NETWORK OPTIMAL SOLUTIONS

## 1. Nesting of ODF Allocations Within Each O-D/Segment

- Network ODF allocations for each O-D/segment are nested into a shared inventory of seats, in order of normal nested booking classes
  - each ODF allocation is treated as a fare class "protection level" within the O-D/segment "nest"
  - each flight leg still has a discrete allocation of seats for each segment/O-D itinerary
  - simply summing discrete allocations gives sub-optimal nested booking limits within each O-D/segment nest



**EXAMPLE: 2 segments on Leg A-B  
(Capacity = 100)**

<b>ODF</b>	<b>Optimal Allocation</b>	<b>Segment Nesting</b>
<b>YAB</b>	<b>8</b>	<b>42</b>
<b>BAB</b>	<b>12</b>	<b>34</b>
<b>MAB</b>	<b>06</b>	<b>22</b>
<b>QAB</b>	<b>16</b>	<b>16</b>
<b>YAC</b>	<b>18</b>	<b>58</b>
<b>BAC</b>	<b>7</b>	<b>40</b>
<b>MAC</b>	<b>23</b>	<b>33</b>
<b>QAC</b>	<b>10</b>	<b>10</b>

## **2. Joint Allocation and Nesting Within O-D/Segment**

- **Published by Curry in Transportation Science (1990)**
  - approach jointly finds optimal allocation to each "O-D nest" and nested limits on each booking class within the nest
  - optimal solution to the formulated problem
  - still a discrete allocation of seats to each segment/O-D (i.e., "O-D nest")
- Both approaches above can have positive revenue impacts compared to leg/booking class control provided that number of discrete O-D nests does not become large
- Otherwise, negative revenue impacts can result when implemented as a control methodology

### **3. Nesting of ODF Allocations on Shadow Prices**

- **Described in Williamson's (1988) MIT Master's thesis**
  - **optimal ODF allocations are ranked and nested in order of shadow price values derived from the optimization algorithms**
  - **the shadow price of an ODF allocation is the amount by which total expected network revenue will increase (or decrease) if one additional seat is allocated to that ODF**
  - **on each flight leg, ODFs with highest shadow prices values receive greatest availability -- ODF allocations are treated as "protection levels" for nesting purposes**

**EXAMPLE: 2 segments on Leg A-B  
(Capacity = 100)**

<b>ODF</b>	<b>Optimal Allocation</b>	<b>Shadow Price</b>	<b>Nested Limits</b>
YAB	8	225	100
BAB	12	200	92
YAC	18	190	80
BAC	7	165	62
MAB	6	110	55
MAC	23	40	49
QAC	10	10	26
QAB	16	0	16

- Implementation into control structure possible through virtual inventory classes defined by shadow price ranges
- Nesting of optimal ODF allocations on current shadow prices results in theoretically sub-optimal booking limits for different ODFs
- Yet, a large number of dynamic booking simulations of this approach as a control methodology show consistent and substantial revenue improvement over leg/booking class control

#### **4. Network "Bid-Price" Approaches**

- **Developed at MIT: Simpson (1989) and Williamson (1990)**
  - **network optimization can also produce shadow prices on the capacity constraint associated with each flight leg, or "bid prices"**
  - **Bid Price Control of seat inventories simply requires a comparison of the fare of the requested ODF itinerary and the sum of the bid prices involved in the itinerary.**
  - **Implementation requires frequent (real-time?) updating of network bid prices to overcome absence of booking limit controls**
- **Bid Price Approach is a sub-optimal control application of optimal network solution, which overcomes negative impacts of discrete ODF allocations through "implicit nesting" of availability through bid price evaluation decision.**

## SUMMARY -- NETWORK OPTIMIZATION APPROACHES

- Network optimization approaches produce optimal ODF seat allocations over a network of flights:
  - require ODF demand forecasts and fares
  - generate partitioned ODF allocations that must be "nested" in sub-optimal ways to have positive revenue impacts
- Truly optimal solution for control of ODF itineraries over a network requires an approach that
  - accounts for nesting of ODFs explicitly
  - allows "desirability" of ODFs to change as demand materializes
  - recognizes dynamic nature of future booking process
  - overcomes "small number" problems of forecasting ODF demands

## CONCLUSIONS

- Network optimization methods produce an optimal solution to an assumed mathematical formulation of the O-D/segment control problem
- Implementation of optimal solutions in actual reservations control structures can lead to negative revenue impacts if done incorrectly
- Nesting of optimal network ODF allocations for control purposes is a sub-optimal solution, although some nesting approaches consistently produce better revenue impacts than others
- No one has formulated, let alone "solved" the dynamic, nested ODF network seat inventory control problem

APPLICATION OF NETWORK  
SOLUTIONS TO  
O-D SEAT INVENTORY CONTROL

Elizabeth L. Williamson  
Flight Transportation Laboratory  
Massachusetts Institute of Technology

Presented to

MIT/Industry Cooperative Research Program  
May 23, 1991  
Cambridge, MA

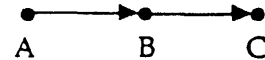


## Introduction

Reviewing network seat inventory control techniques and applying them to three different multi-leg examples, using real airline data:

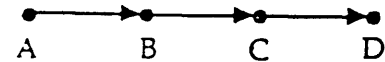
1) 2 Leg Flight

4 Fare Classes  
3 OD Pairs  
12 ODF Combinations



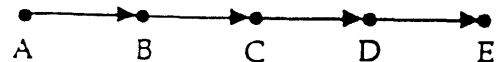
2) 3 Leg Flight

4 Fare Classes  
6 OD Pairs  
24 ODF Combinations



3) 4 Leg Flight

4 Fare Classes  
10 OD Pairs  
40 ODF Combinations



## Network Solutions Nested on Shadow Prices

- Network formulation used to find seat allocations for each ODF over an entire network of flights.
- Distinct allocations are nested according to the shadow price of each ODF.
- Shadow Price: The amount the optimal system revenue value would change if one more seat was made available to the given ODF.

## Nested Deterministic by Shadow Prices

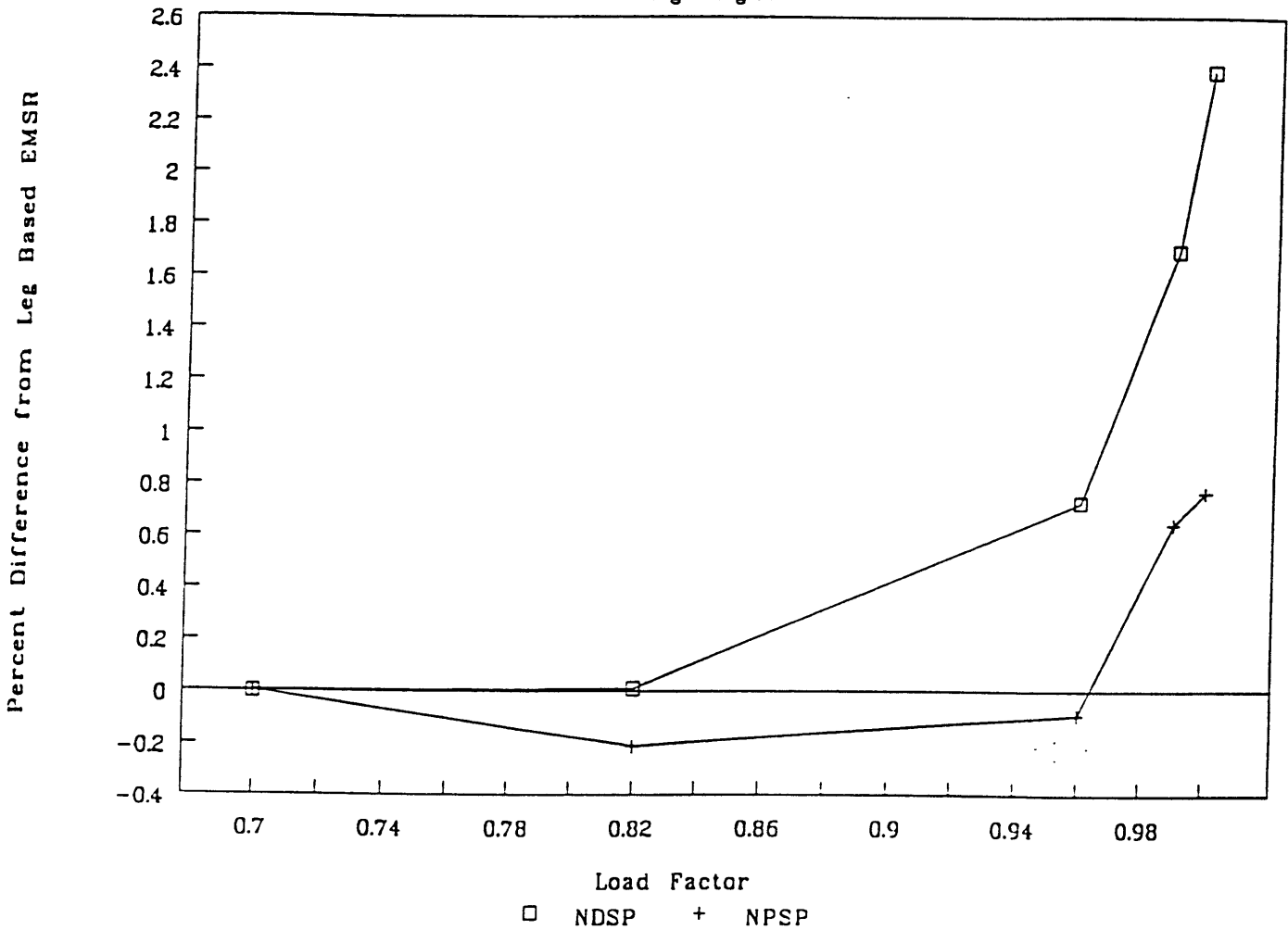
3 Leg Example

Leg BC - Capacity=90

ODF	Seats Allocated	Fare	Shadow Price	Booking Limit
ACY	2	519	322	90
BCY	10	440	243	88
ADY	3	582	216	78
ACM	1	344	147	75
BCM	22	315	118	74
BDY	6	440	74	52
ACB	4	262	65	46
ACQ	14	231	34	42
BCB	12	223	26	28
ADM	1	379	13	16
BCQ	15	197	0	15
BDM	0	307	-59	0
ADB	0	302	-64	0
ADQ	0	269	-97	0
BDB	0	221	-145	0
BDQ	0	199	-167	0

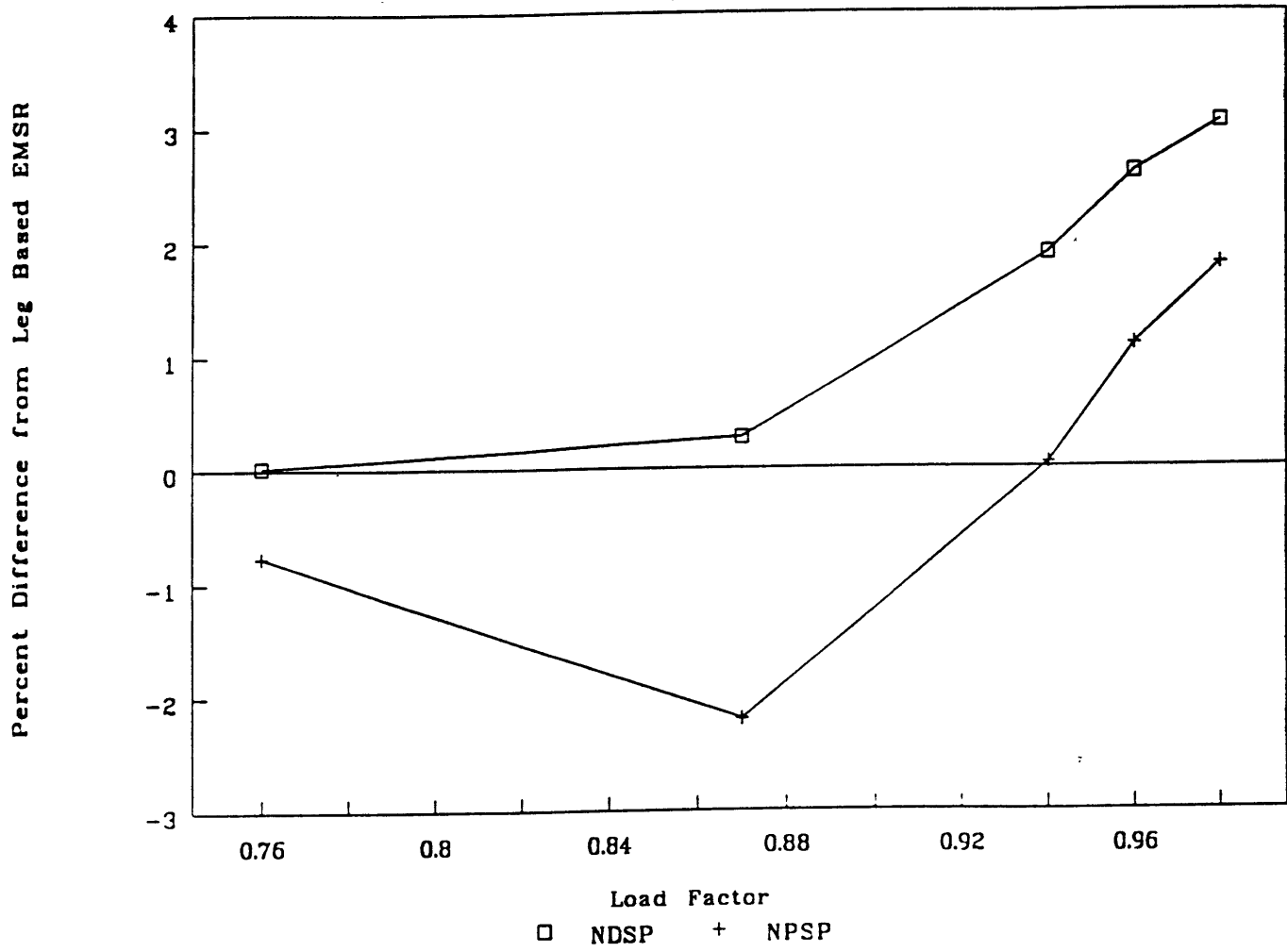
# NETWORK SOL'NS NESTED ON SHADOW PRICES

2 Leg Flight



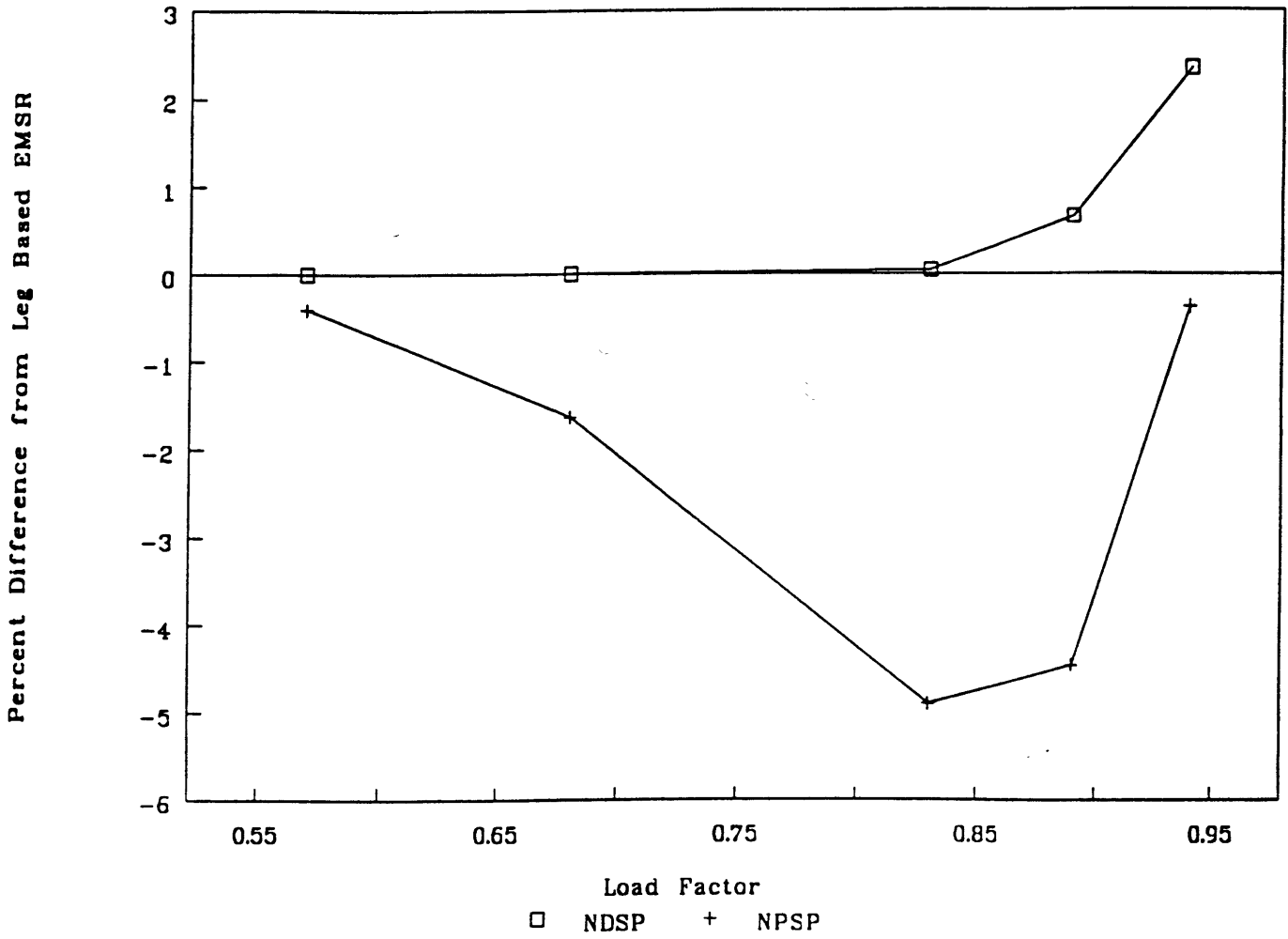
# NETWORK SOL'NS NESTED ON SHADOW PRICES

3 Leg Flight

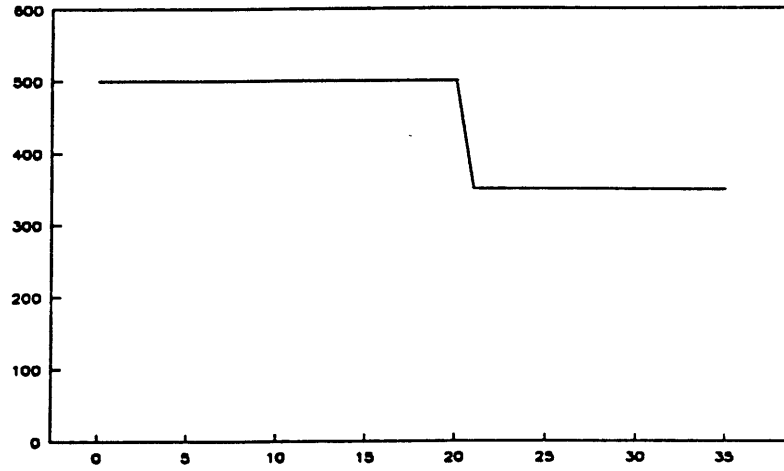


# NETWORK SOL'NS NESTED ON SHADOW PRICES

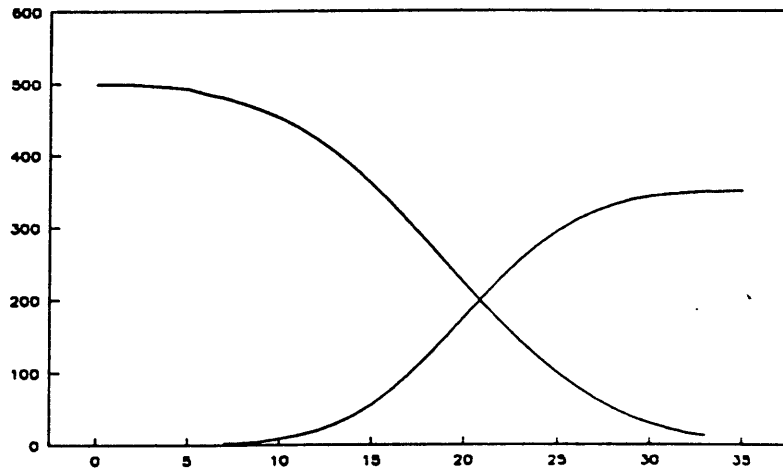
4 Leg Flight



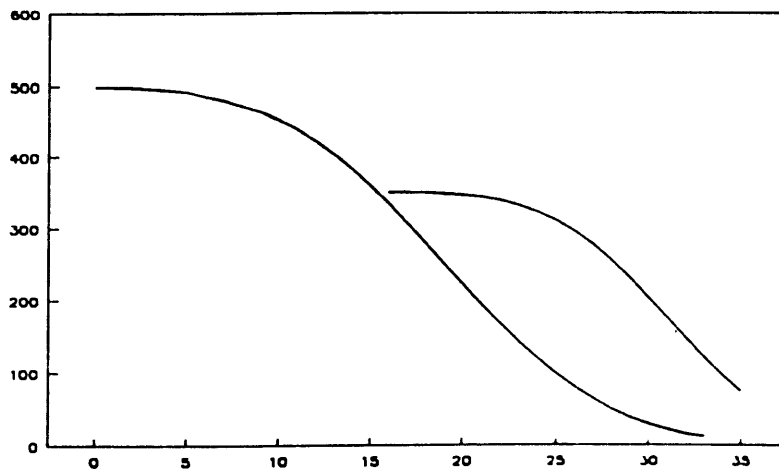
DISTINCT DETERMINISTIC APPROACH



DISTINCT PROBABILISTIC APPROACH



EMSR APPROACH



## EXAMPLE

### Single Leg, 4 Fare Classes

	MEAN	STD	FARE
Y	20	7	500
M	15	5	350
B	30	10	200
Q	25	8	150

### ALLOCATIONS

	DETER	PROB	EMSR
Y	20	27	17
M	15	19	20
B	30	31	27
Q	25	23	36

### BOOKING LIMITS

	NDSP	NPSP	EMSR	OPTIMAL
Y	100	100	100	100
M	80	73	83	83
B	65	54	63	62
Q	35	23	36	33



## Initial Allocations

3 Leg Example  
AB Leg - Capacity=75

	Distinct Deterministic					Distinct Probabilistic			
	Y	M	B	Q		Y	M	B	Q
AB	25	3	7	26	AB	28	5	10	26
AC	2	1	4	4	AC	3	0	1	0
AD	3	0	0	0	AD	2	0	0	0

## Difference in Allocations (Prob - Deter)

	Y	M	B	Q
AB	3	2	3	0
AC	1	-1	-3	-4
AD	-1	0	0	0

## Comparison of Allocations Over 15 Revisions

	Mean	Deter Alloc	Prob Alloc
AB Y	25.2	25	28
	25.1	25	28
	24.8	25	28
	24.0	24	28
	22.8	23	28
	22.0	22	26
	20.4	20	26
	19.3	19	26
	16.9	17	25
	15.6	16	23
	12.3	12	21
	9.2	9	19
	8.6	9	18
	5.9	6	15
	2.6	3	11

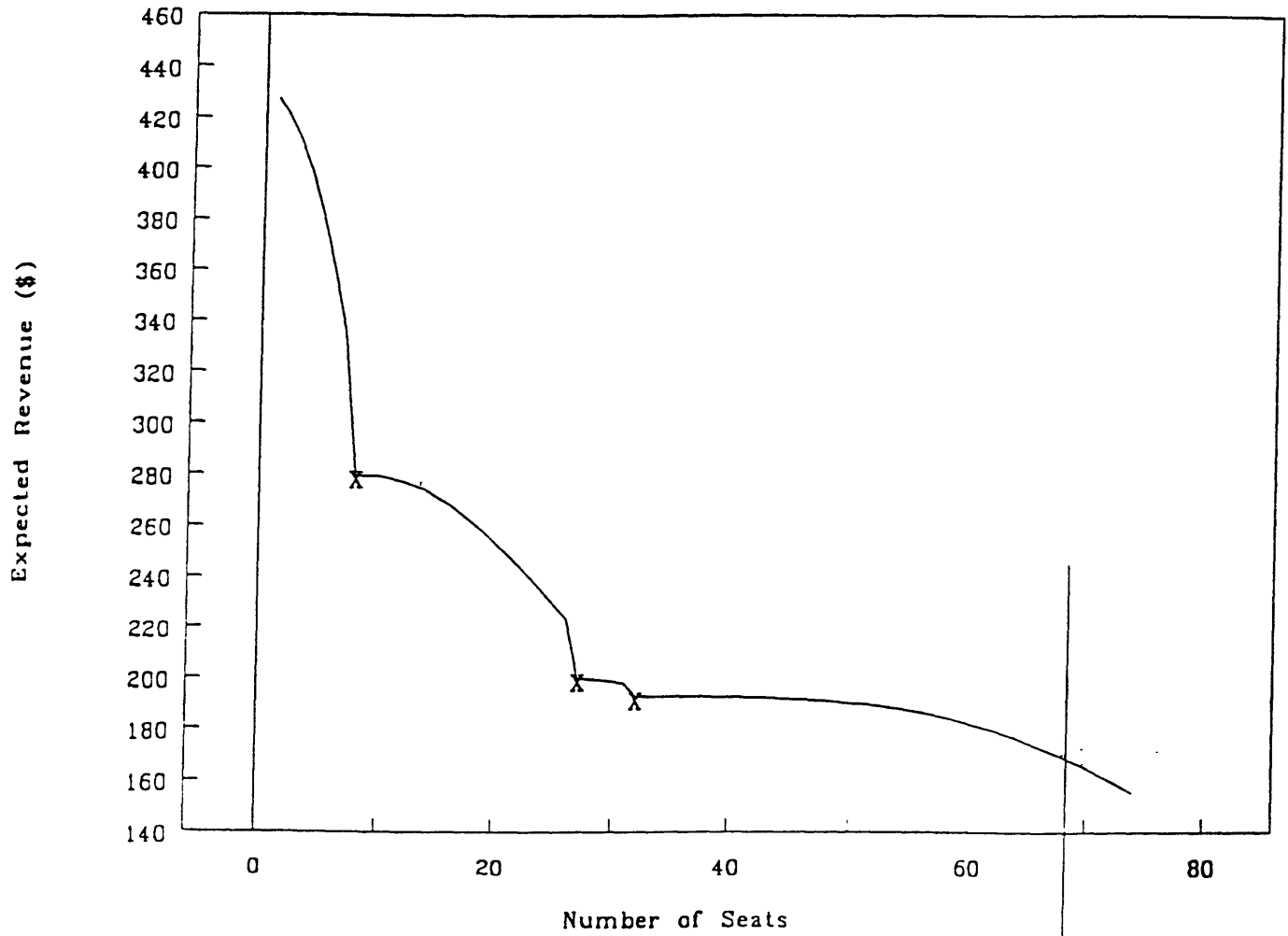
## Partially Nested versus Fully Nested

### Partially Nested (Curry):

- Determine discrete allocations for each OD, based on expected revenue from nested fare classes.
- Determine fare class booking limits within each OD allocation.

# Expected Revenue per Seat

O-D Pair BC



## Fully Nested versus Partially Nested

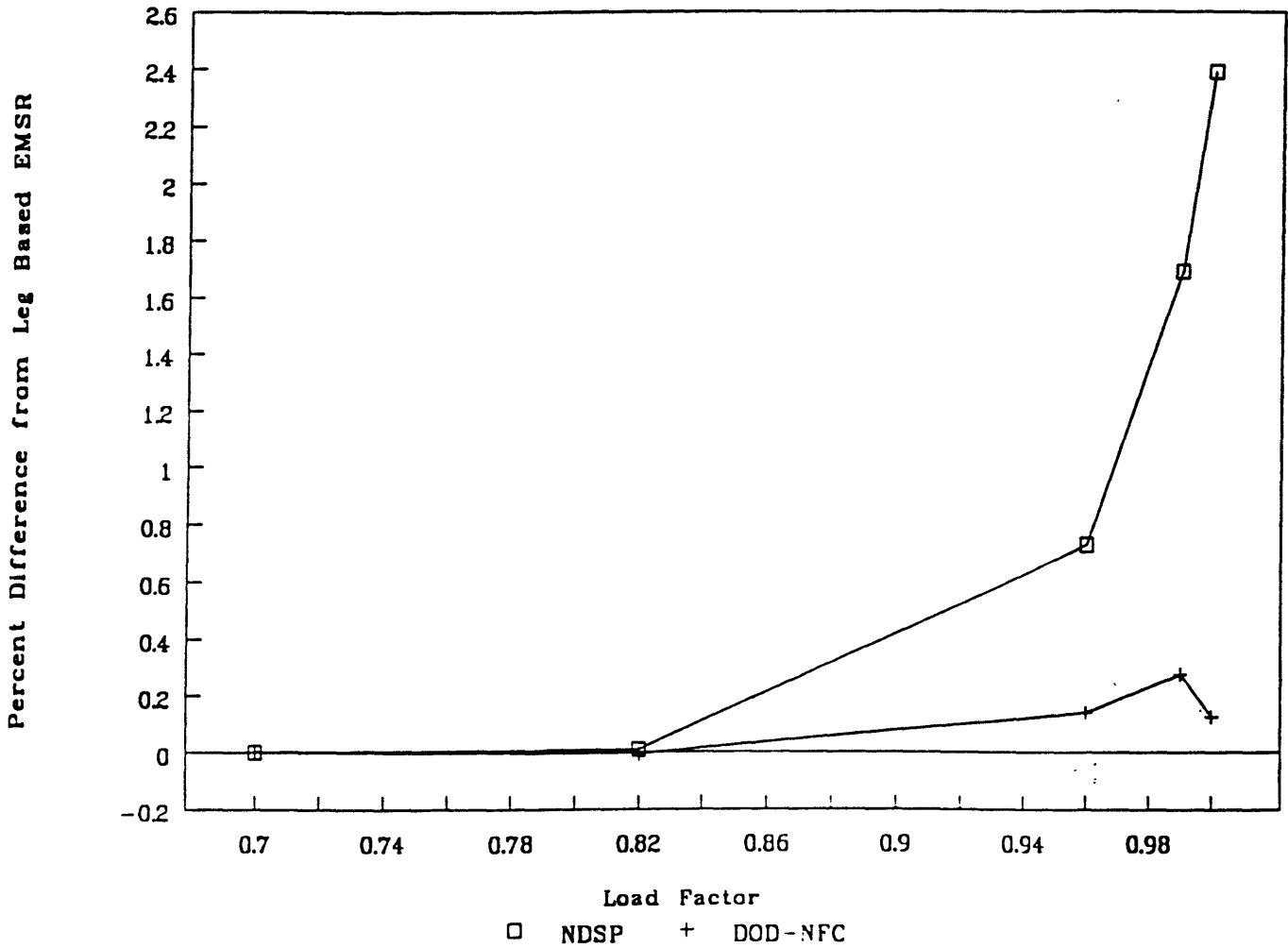
### 3 Leg Example

Leg BC - Capacity=75

ODF	NDSP Allocations	NDSP BL	DOD-NFC BL
ACY	2	75	4
ACM	1	38	3
ACB	4	31	0
ACQ	4	15	0
ADY	3	63	2
ADM	0	0	0
ADB	0	0	0
ADQ	0	0	0
BCY	10	73	64
BCM	22	60	57
BCB	12	27	38
BCQ	11	15	32
BDY	6	37	5
BDM	0	0	1
BDB	0	0	0
BDQ	0	0	0

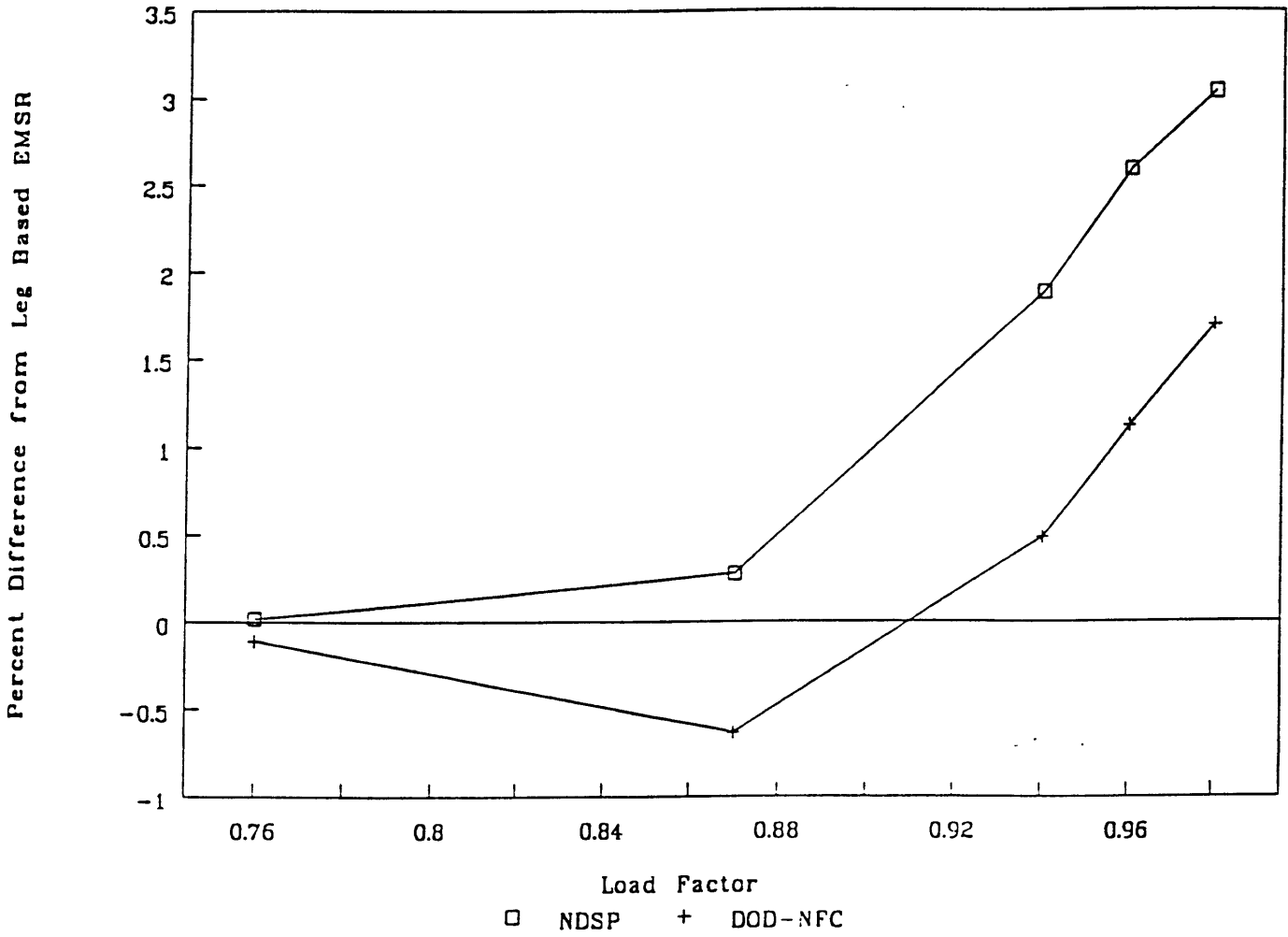
# FULLY NESTED VS. PARTIALLY NESTED

2 Leg Flight



# FULLY NESTED VS. PARTIALLY NESTED

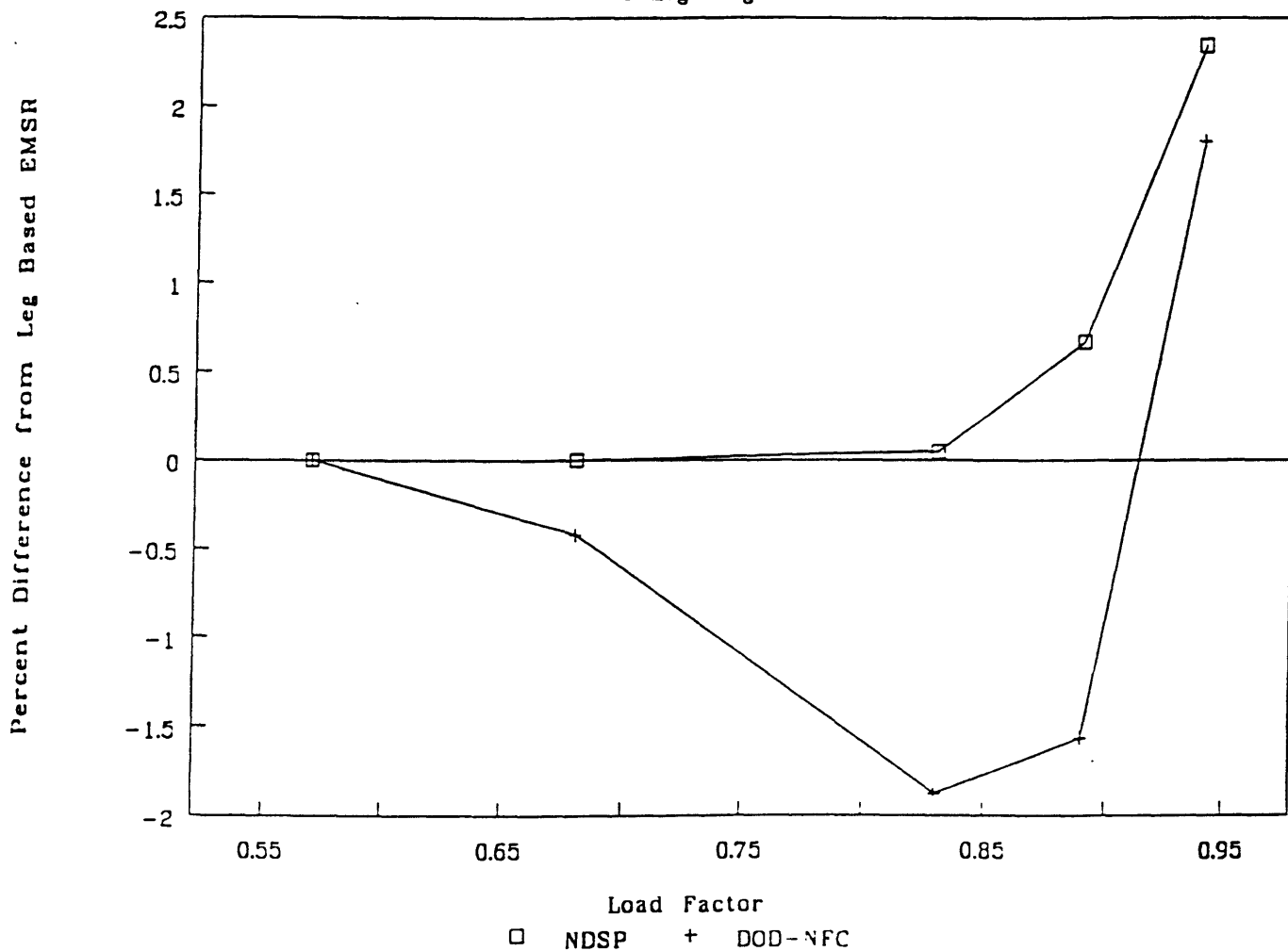
3 Leg Flight





# FULLY NESTED VS. PARTIALLY NESTED

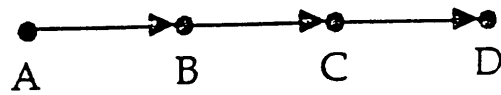
4 Leg Flight



## Bid Price

- Bid Price is a Shadow Price for the capacity constraints.
- Obtained from the same network formulations.
- The marginal value of the last seat of a given flight leg.
- Bid Prices establish a "cutoff" value for each flight leg, on which decisions can be made whether to accept or reject a given O-D/fare class request.
- For a single leg itinerary, a fare class is open for bookings if the corresponding fare is greater than the bid price, or shadow price, for the leg.
- For a multi-leg itinerary, fares must be greater than the sum of the bid prices from the respective flight legs.

### 3 Leg Example Capacity=75



A-B	34
B-C	197
C-D	169

BC:      197

AC:      231

AD:      400

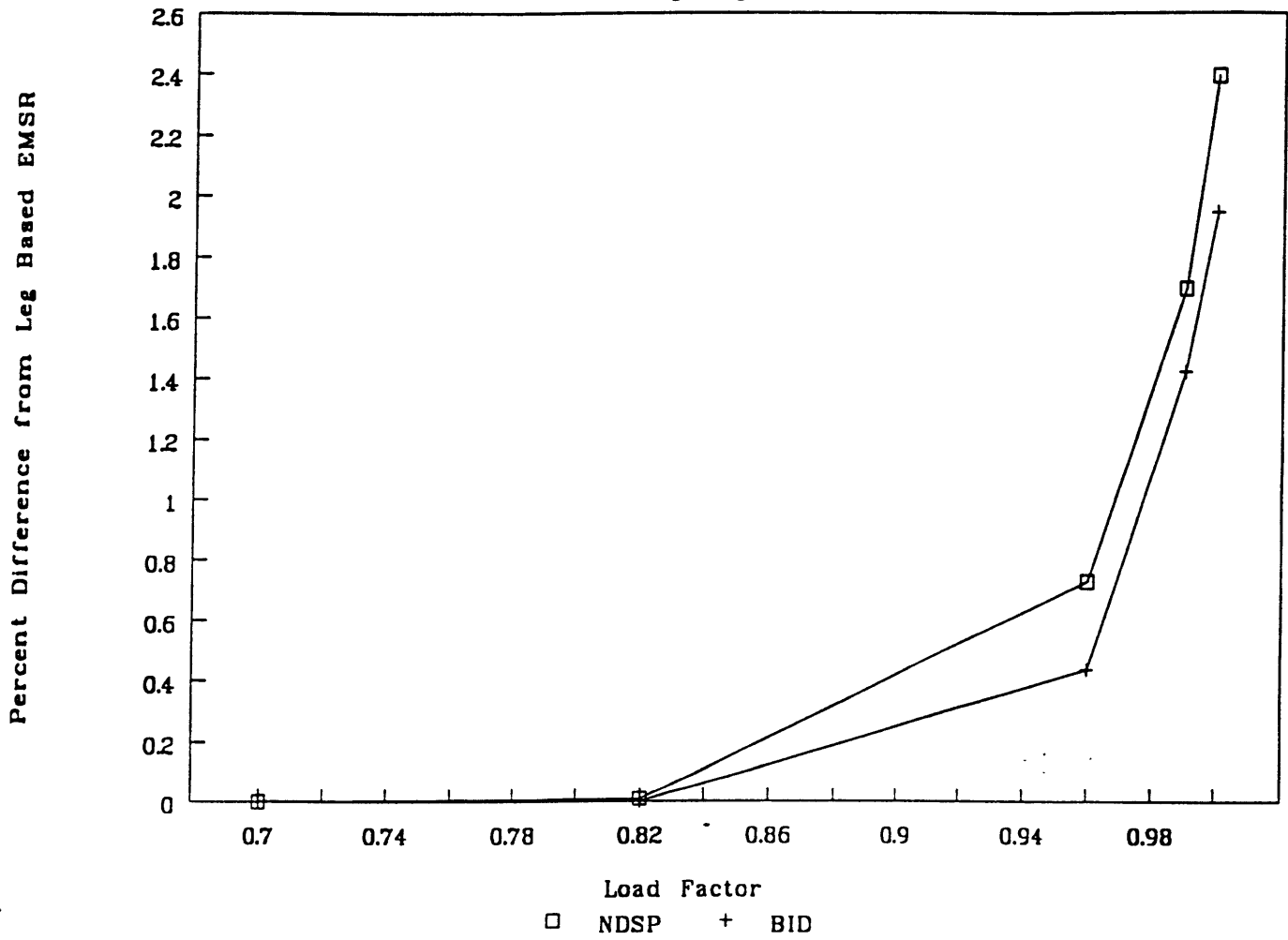
Y	440
M	315
B	223
Q	197

Y	519
M	344
B	262
Q	231

Y	582
M	379
B	302
Q	269

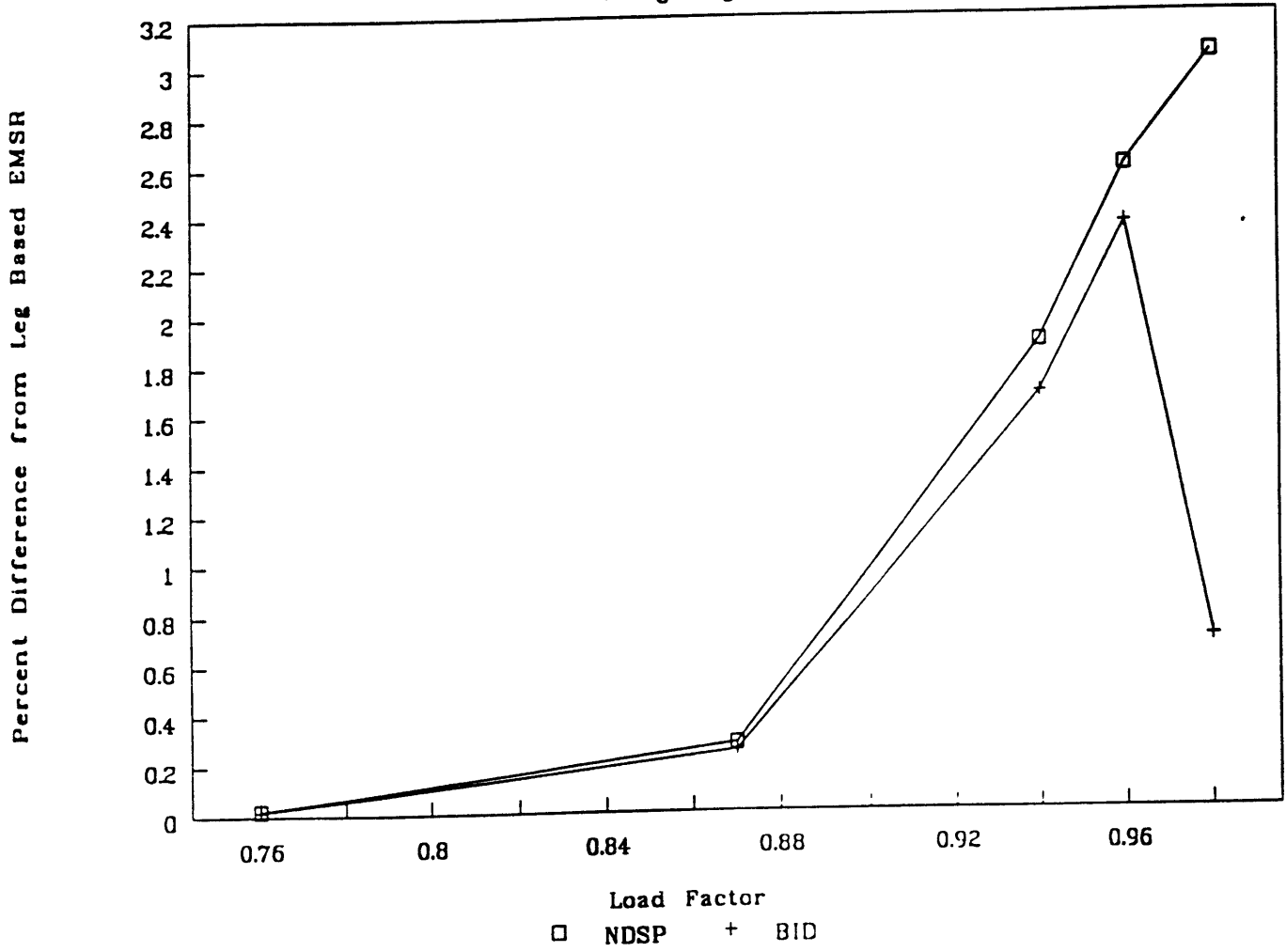
# DETERMINISTIC NETWORK METHODS

2 Leg Flight



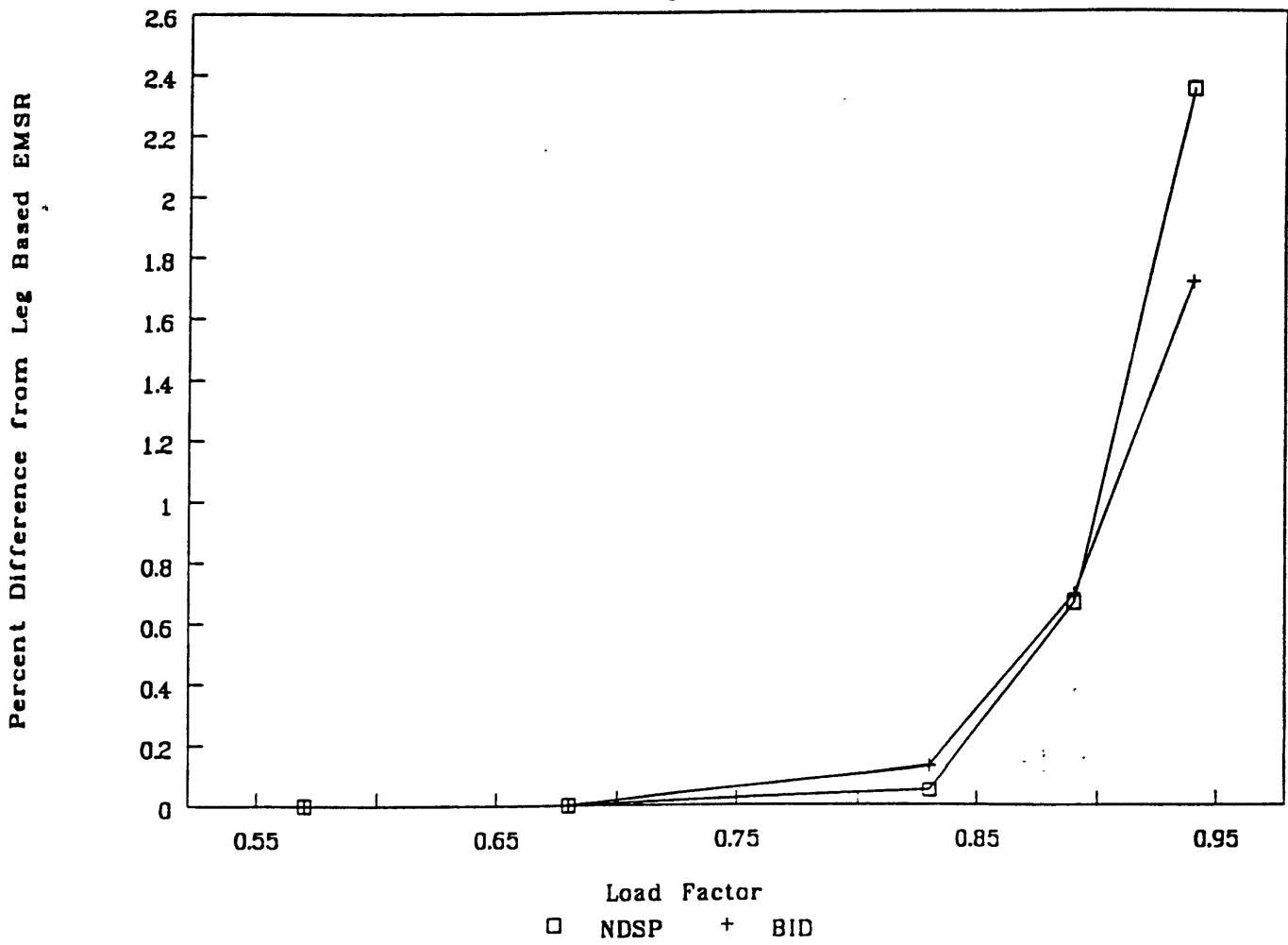
# DETERMINISTIC NETWORK SOLUTIONS

3 Leg Flight



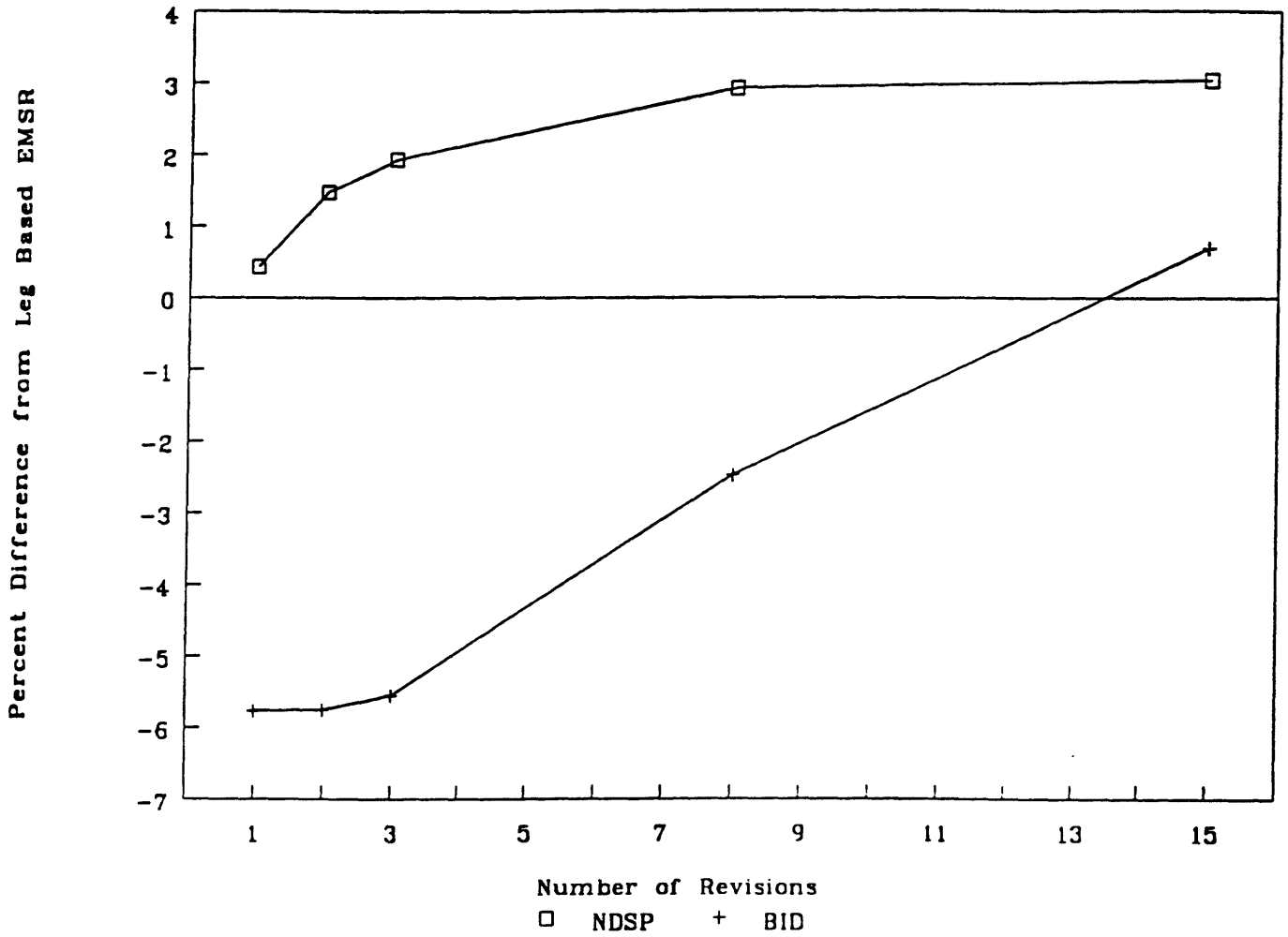
# DETERMINISTIC NETWORK METHODS

## 4 Leg Flight



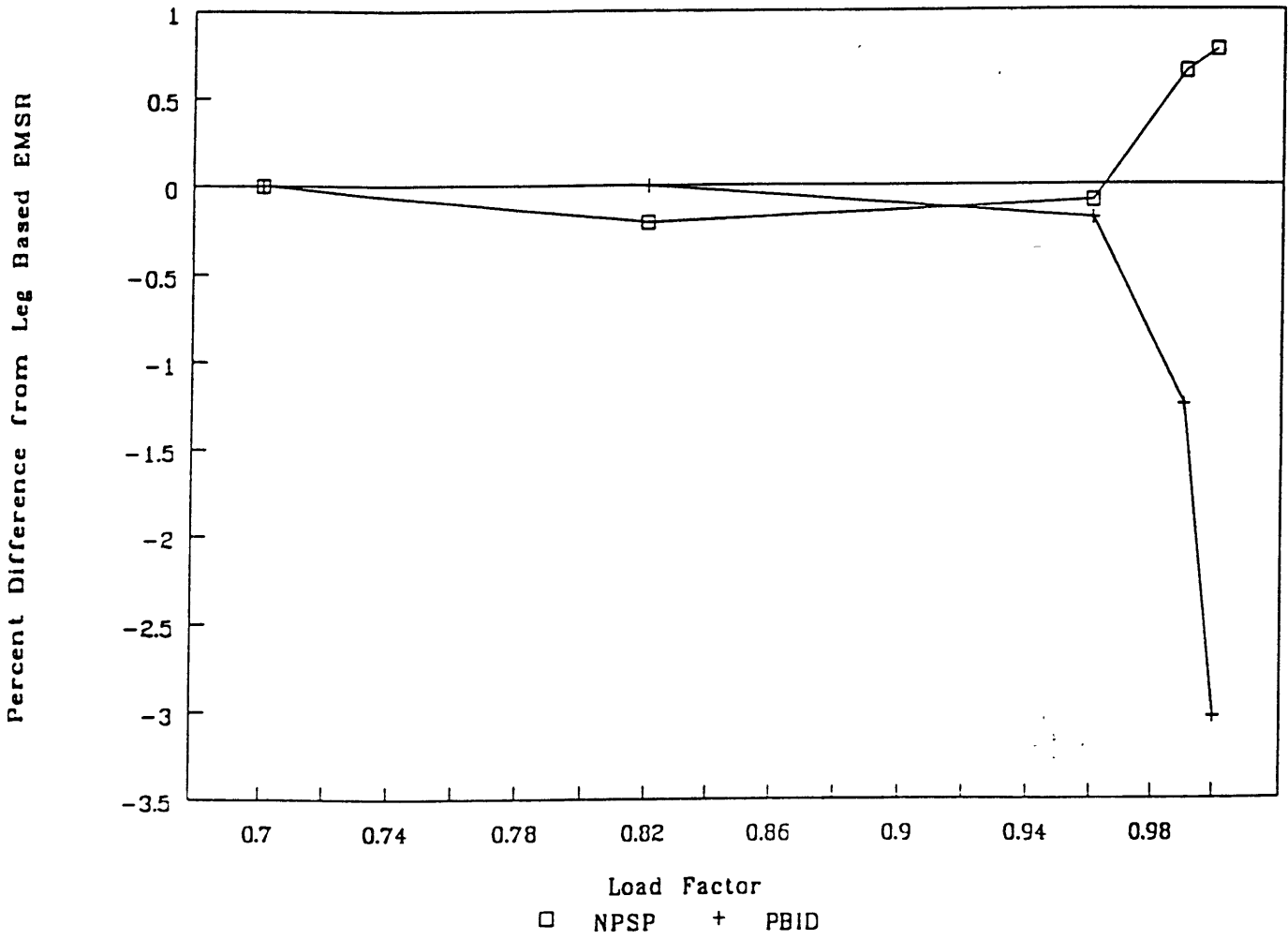
# Revenue Impacts vs. Revisions

3 Leg Example - 98% Load Factor



# PROBABILISTIC NETWORK METHODS

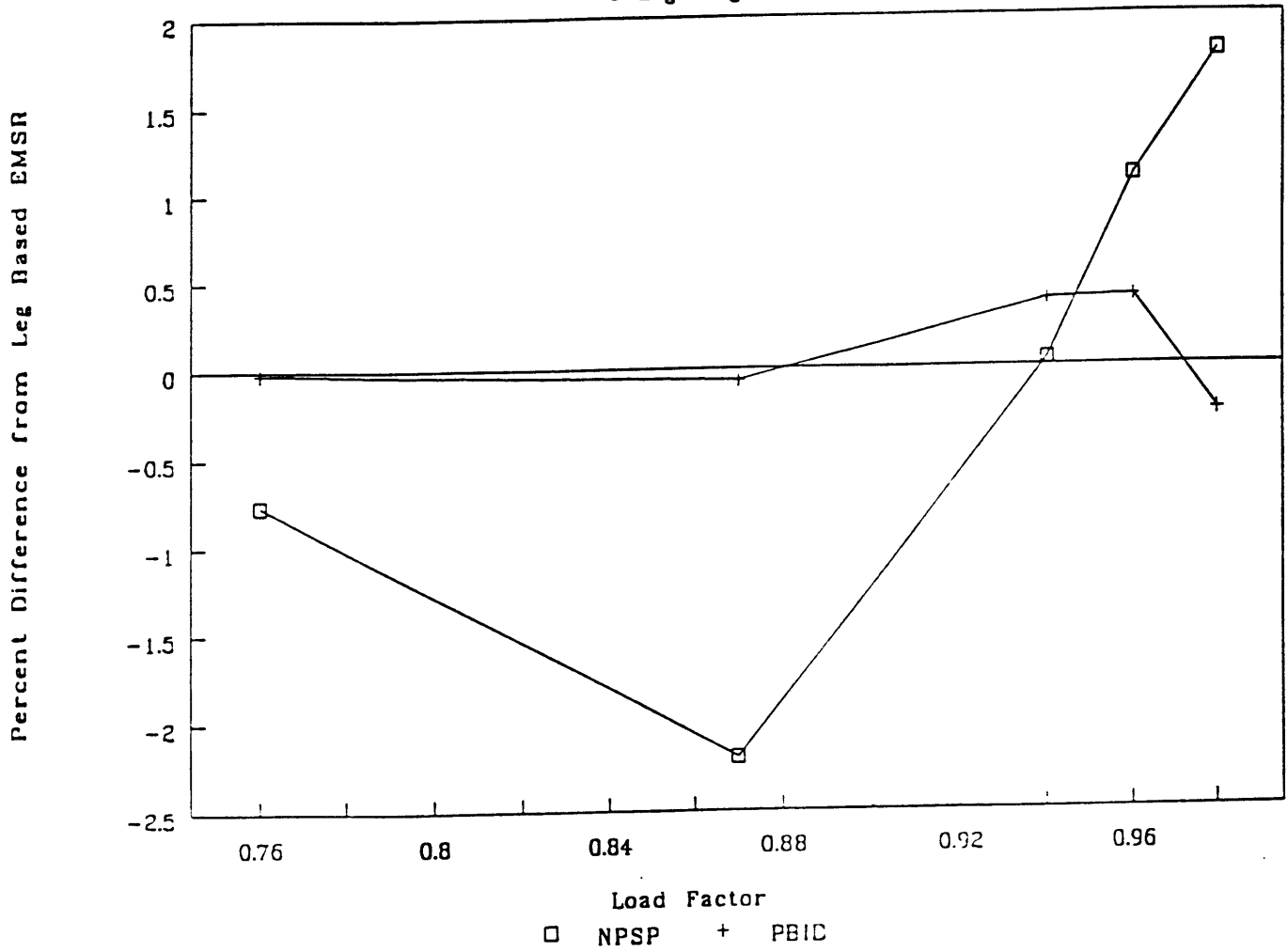
2 Leg Flight





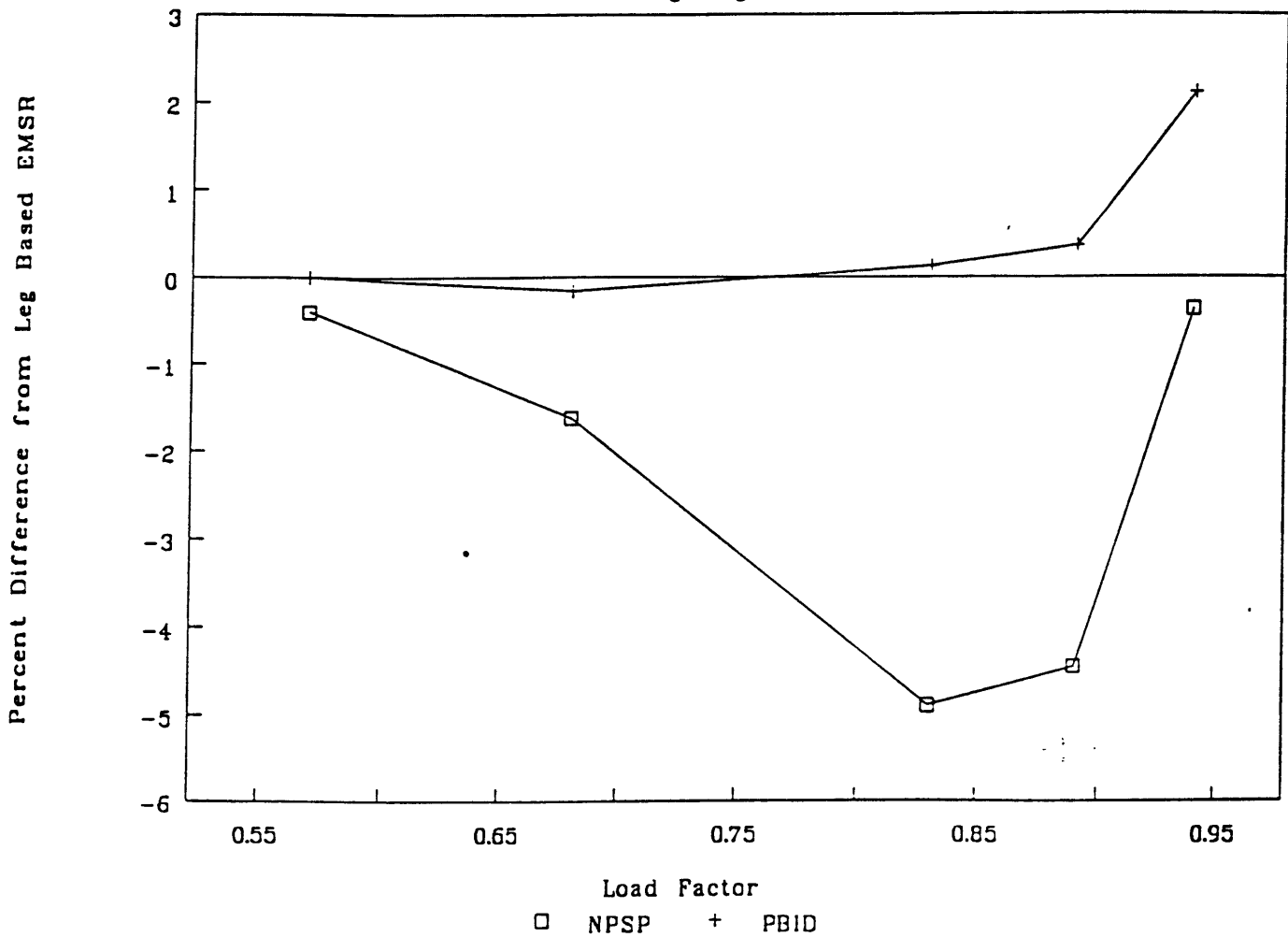
# PROBABILISTIC NETWORK SOLUTIONS

3 Leg Flight



# PROBABILISTIC NETWORK METHODS

## 4 Leg Flight



## UPPER BOUND

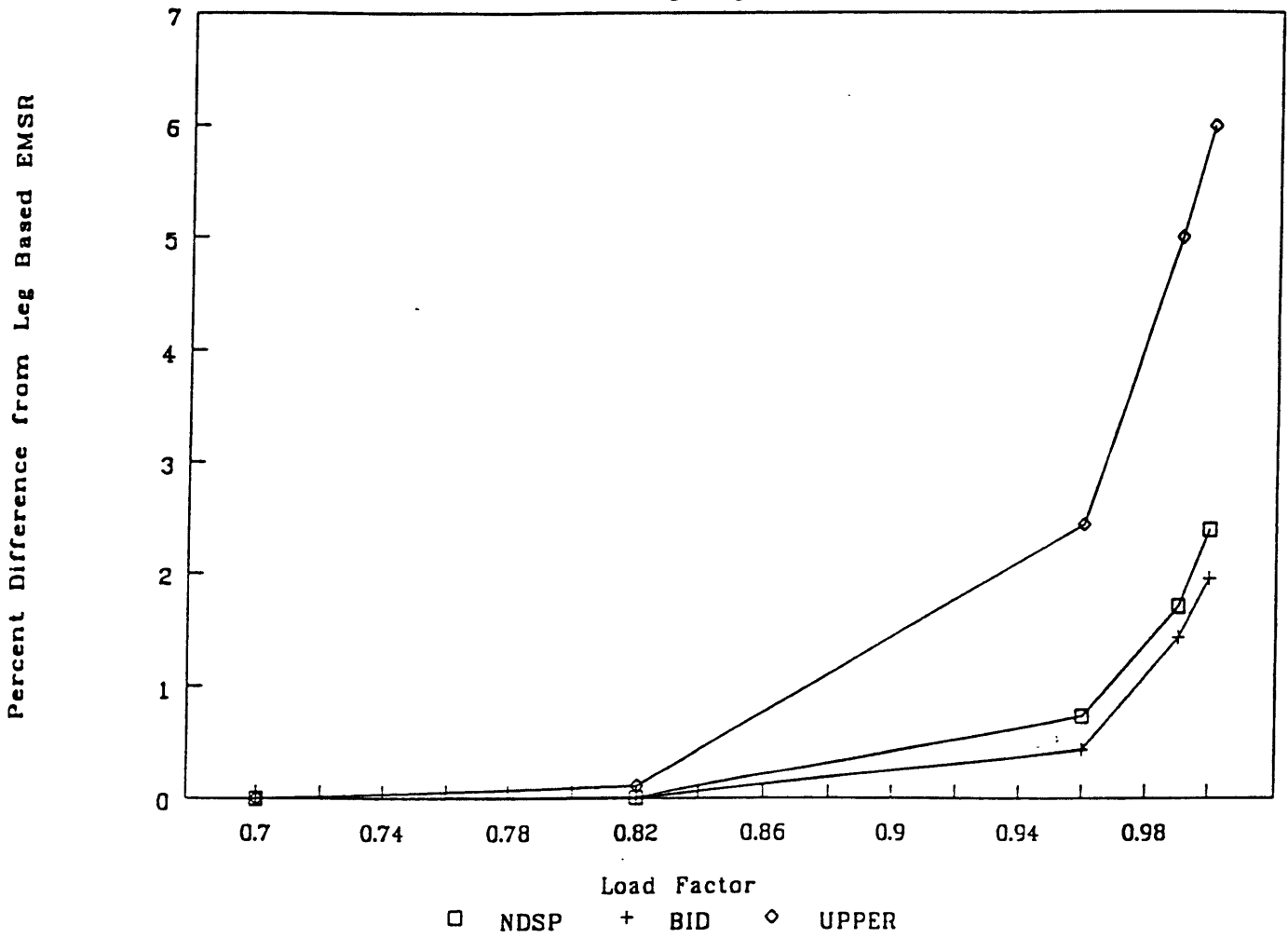
	MEAN	STD DEVI
ABY	36.12	14.91
ABB	9.94	13.92
ABM	18.61	16.01
ABQ	34.06	25.96

## ACTUAL DEMAND

ABY	35	28	48
ABB	14	12	8
ABM	18	18	16
ABQ	39	32	34

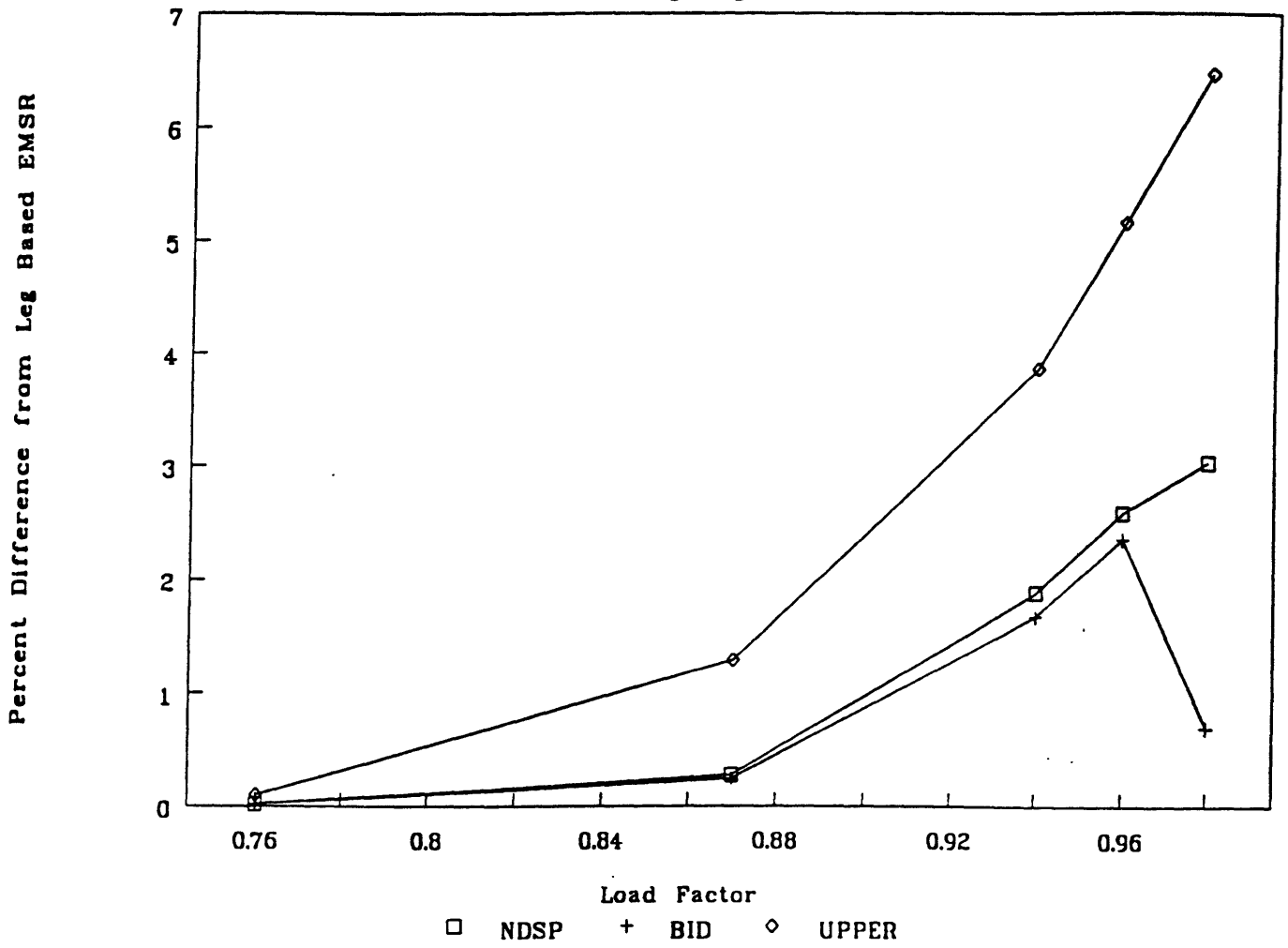
# UPPER BOUND COMPARISON

2 Leg Flight



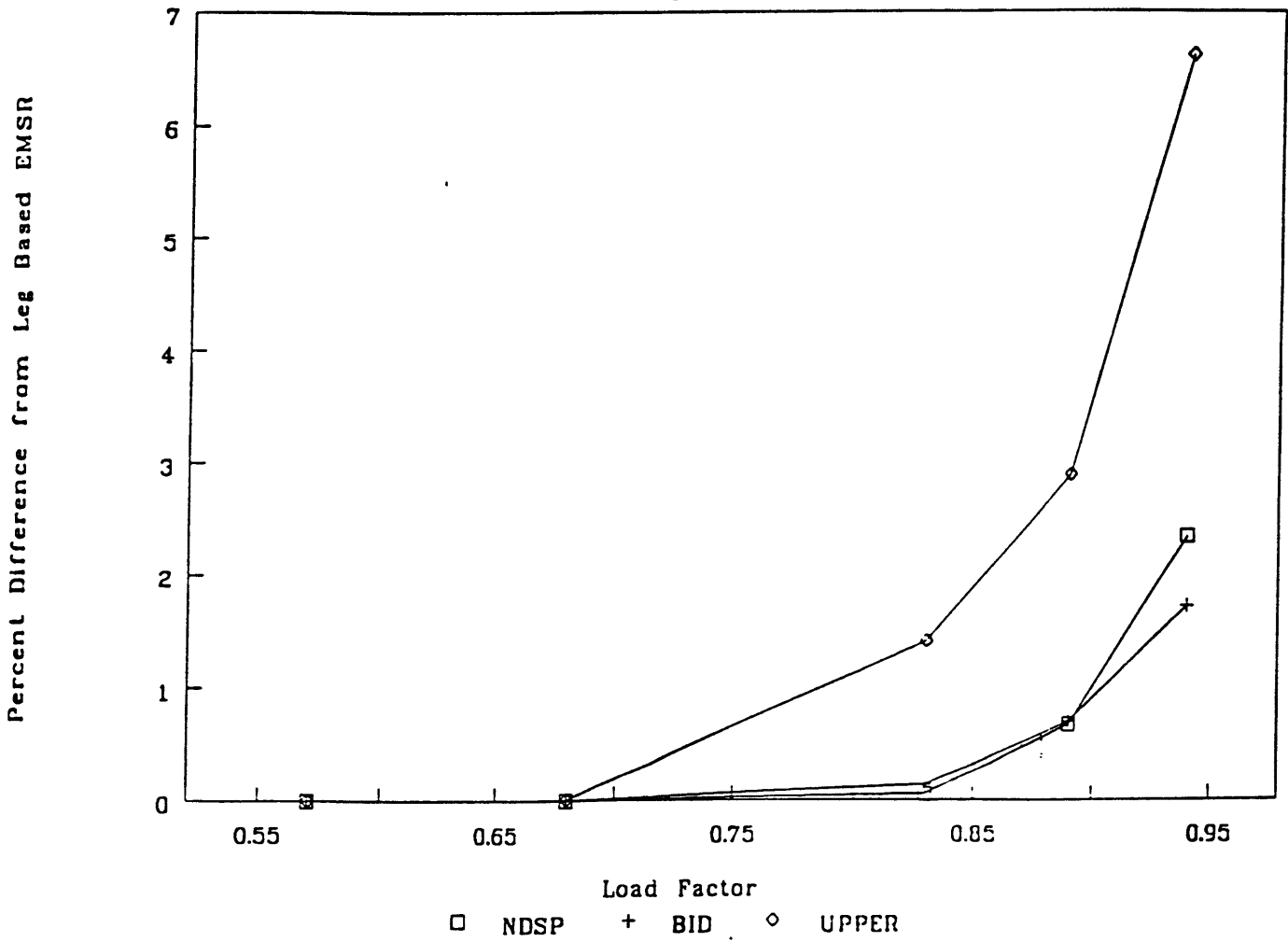
# UPPER BOUND COMPARISON

3 Leg Flight



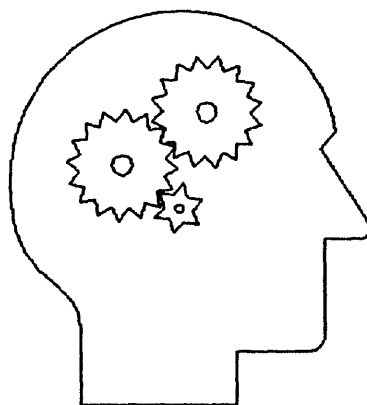
# UPPER BOUND COMPARISON

4 Leg Flight



## Summary

- Nested Deterministic on Shadow Prices outperforms Nested Probabilistic on Shadow Prices.
- Given full ODF forecasts, better to use a fully nested method, such as NDSP, rather than a partially nested method.
- Deterministic Bid Price approach performs well and uses a very simple control methodology, however it is important to be able to make frequent revisions using such an approach.
- Using Upper Bound, the true potential from better control of seat inventories over current leg based approaches can be determined.



## Planning and Scheduling of Tasks in a Dynamic Environment

Lyman R. Hazelton

23 May 1991





The Strategic Control of systems requiring *planning* and *scheduling* of activities is called

## *Operations Management*

- Reasoning about the future in a dynamic environment.
- Determination of the time that a state or process should be maintained.
- Situation dependent objectives.
- No final system state.
- Often involve non-quantifiable parameters.



A decision was made to attempt to solve the problem with an "Expert Systems" approach. However, existing AI planning methods

- Were based on a back-chained, goal seeking technology.
- Have been shown to be NP-hard or even Non-terminating for conjunctive goals.
- Assumed a single actor, non-stochastic universe.
- Had no logic or even representation for time dependent activities.

In summary, the automatic reasoning technology necessary to attack the problem did not exist.

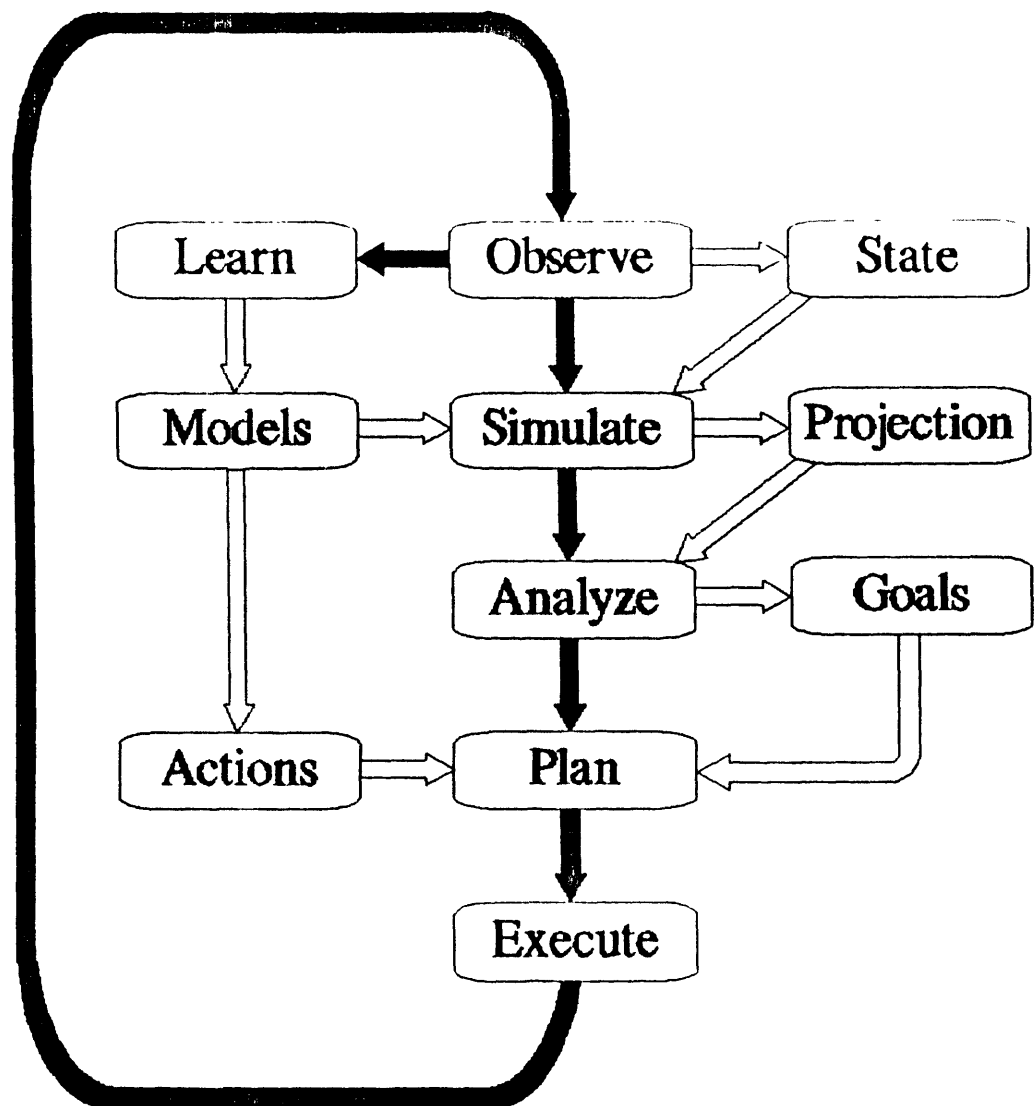


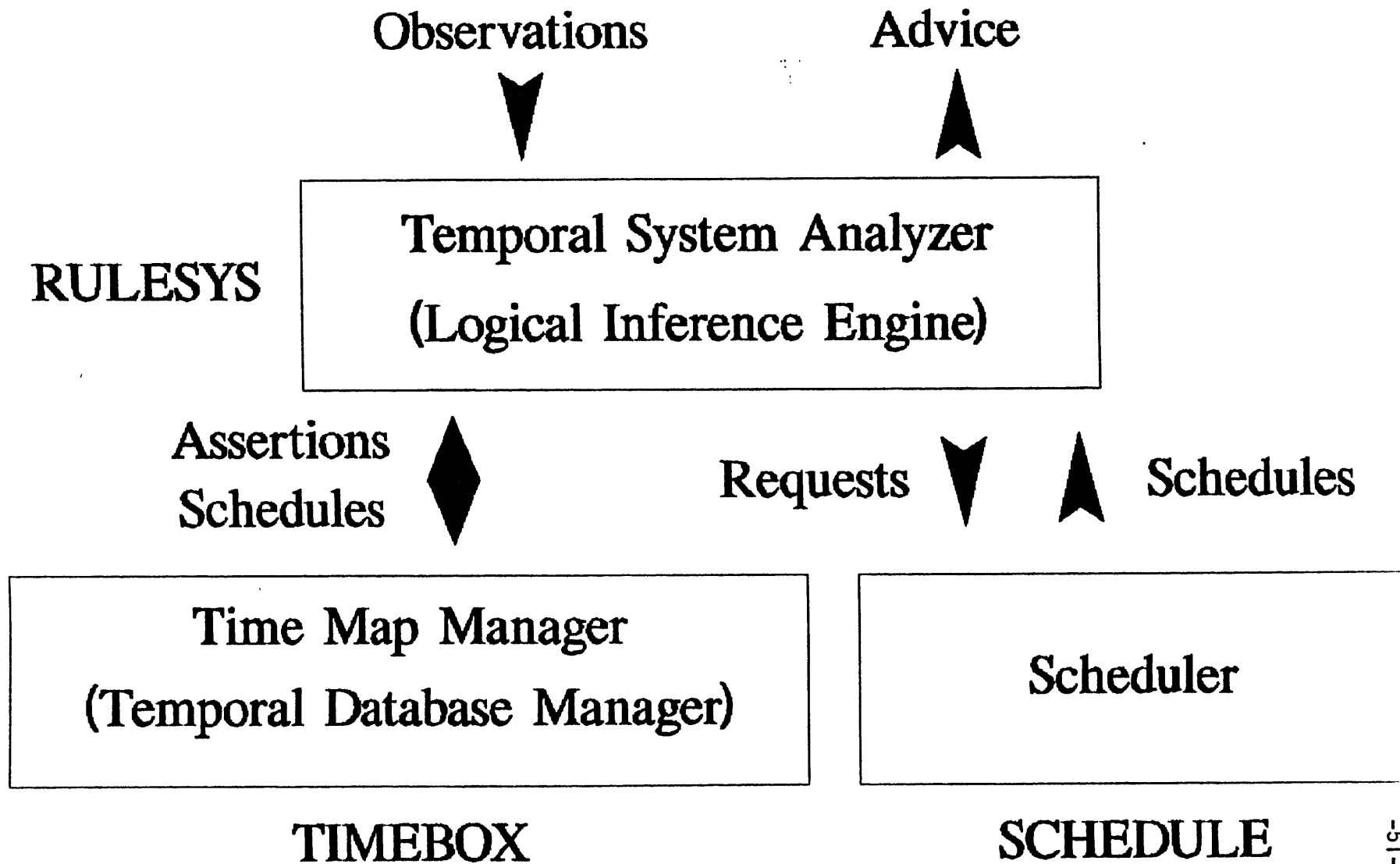
At the time the research was initiated:

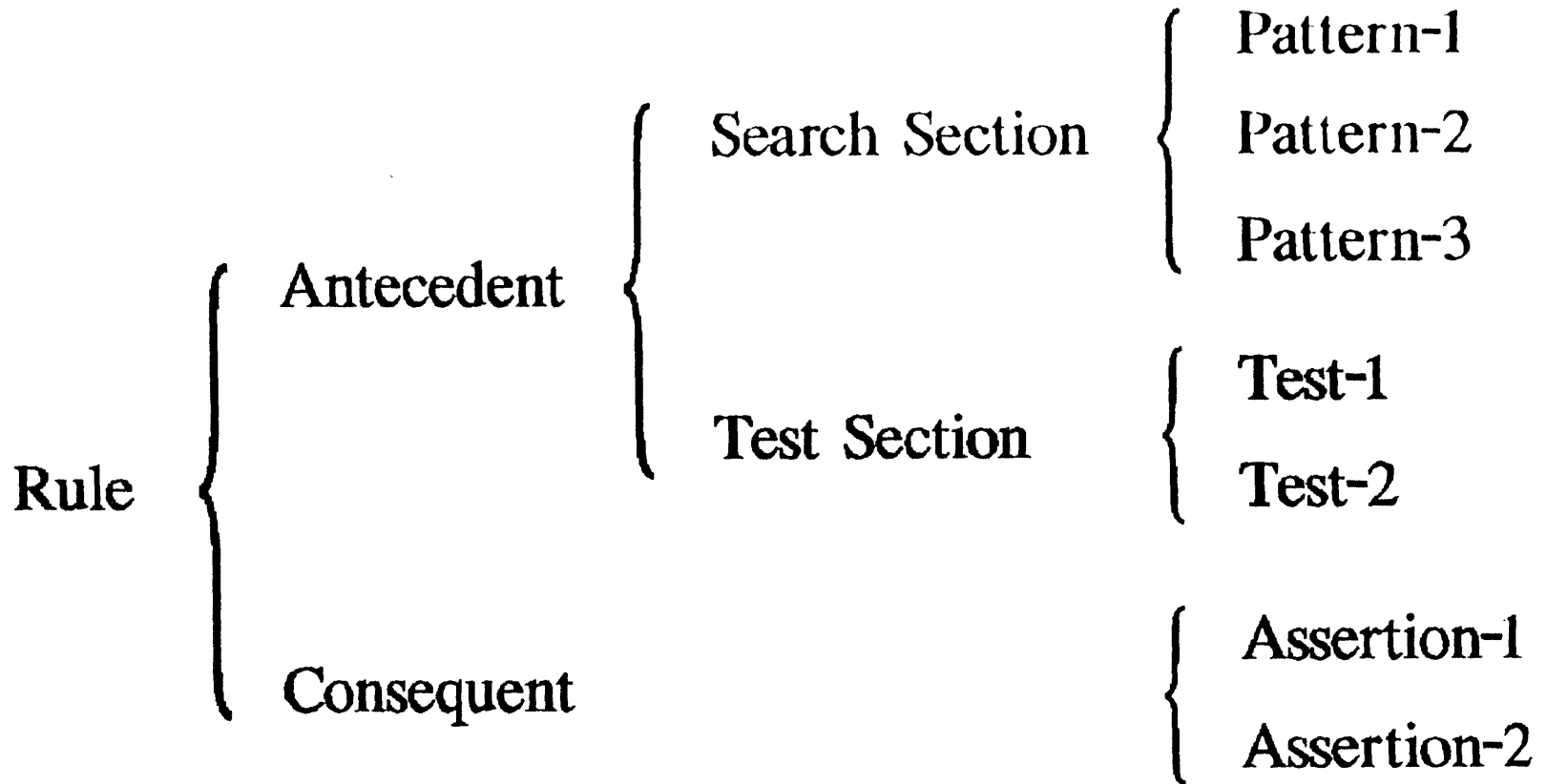
- There were NO programs or even algorithms for temporal database management
- There were NO data representations for concurrent temporarily bounded information
- Automatic plan generation was restricted to
  - Single Actor Domains
  - Determinate Domains
  - Instantaneous Actions



## Operations Management Model









**Goal:**  
**PAINTED CEILING**  
**and**  
**PAINTED LADDER**

**Plan: PAINT LADDER**

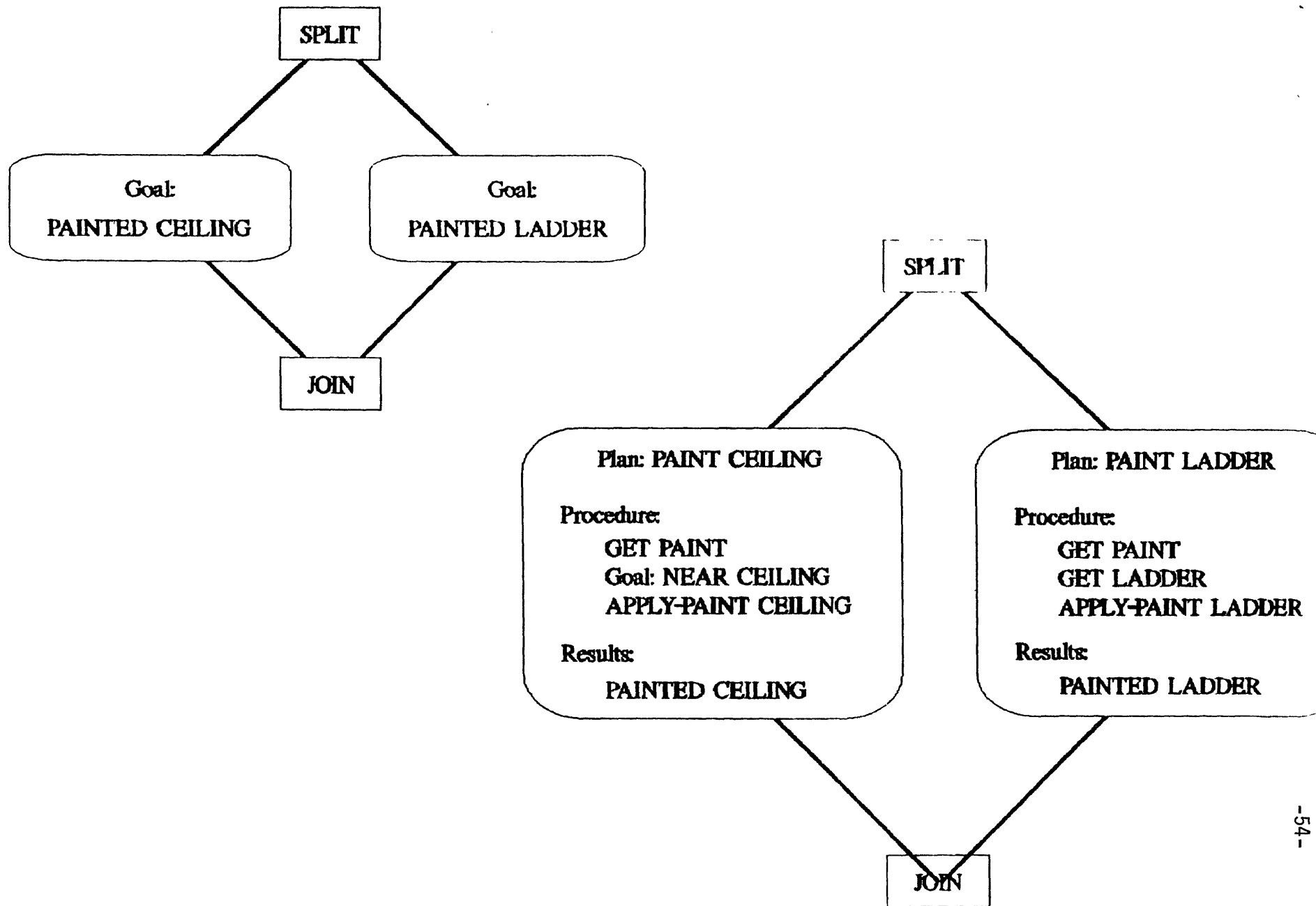
**Procedure:**  
**GET PAINT**  
**GET LADDER**  
**APPLY-PAINT LADDER**

**Results:**  
**PAINTED LADDER**

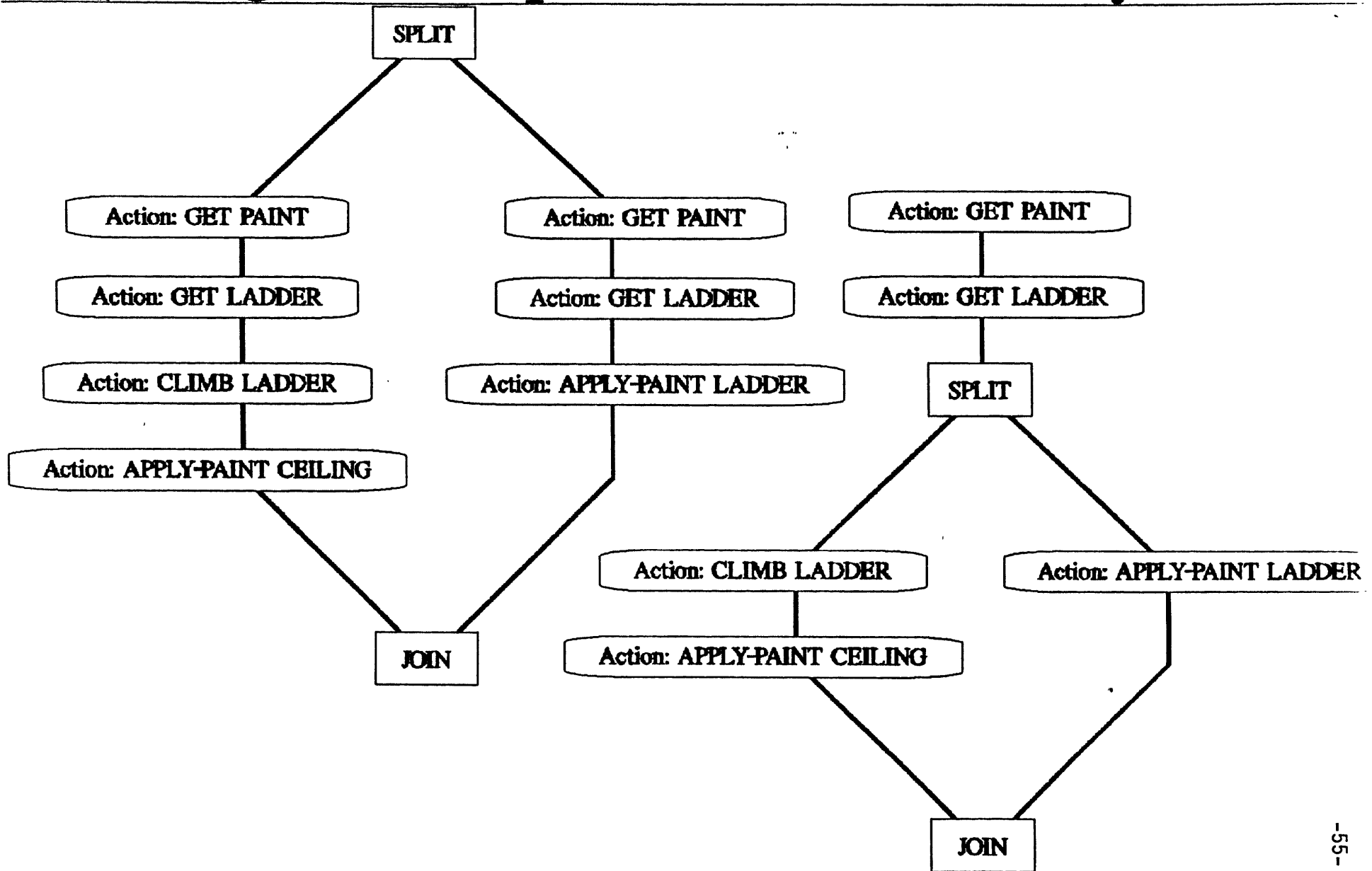
**Plan: PAINT CEILING**

**Procedure:**  
**GET PAINT**  
**Goal: NEAR CEILING**  
**APPLY-PAINT CEILING**

**Results:**  
**PAINTED CEILING**





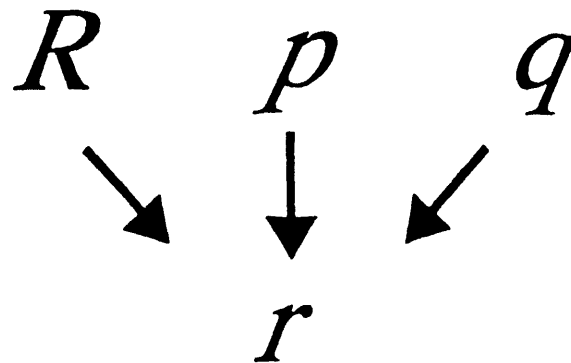


- Truth Maintenance

A first attempt to extend logic into a dynamic environment.

$$R: p \cdot q \rightarrow r \cdot \{R \ p \ q\} \top r$$

$$\sim p \mid \sim q \top \neg r$$



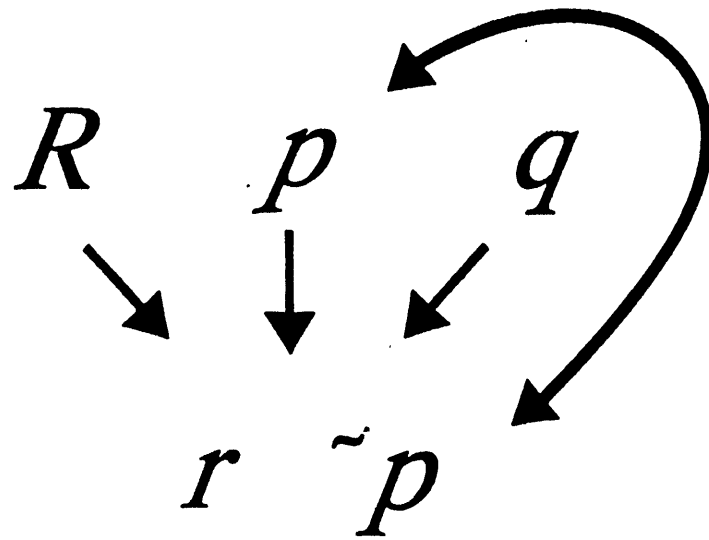


- Inferred evolution

$$R: p \cdot q \rightarrow r \cdot \tilde{p} \cdot$$

$$\{R \ p \ q\} \top r$$

$$\tilde{p} \mid \tilde{q} \top r \quad (\text{TM})$$





- Introduce **EXPLICITLY** the **TIME INTERVAL** during which a proposition (was, is, will be) true:

$$p(\tau)$$

where  $\tau$  is a time interval having a starting time and an ending time.



- Persistence:

$$R: p \rightarrow q$$

$$\sim p \not\rightarrow q \quad (\text{NO TM})$$

If it is raining ( $p$ ), the roads will be wet ( $q$ ).

But if it stops raining ( $\sim p$ ), the roads do not instantly become dry. Wet roads persist.



- Temporal Logic (continued)
  - Rules of Inference

Modus Ponens:

$$p \rightarrow q$$

$$p(\tau)$$

$\therefore q(\tau)$  Non-persistent

$\therefore q(\text{start}(\tau), \infty)$  Persistent



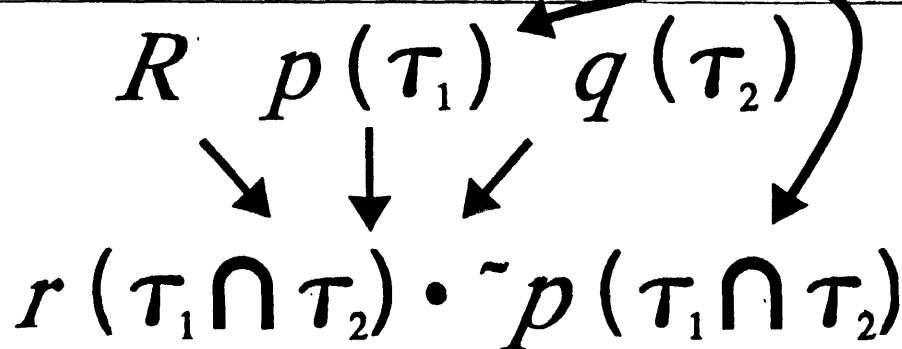
- Inferred evolution revisited

$$R: p(\tau_1) \cdot q(\tau_2) \rightarrow r(\tau_1 \cap \tau_2) \cdot \sim p(\tau_1 \cap \tau_2)$$

$$\{R \ p(\tau_1) \ q(\tau_2)\} \top r(\tau_1 \cap \tau_2)$$

$$\{R \ p(\tau_1) \ q(\tau_2)\} \top \sim p(\tau_1 \cap \tau_2)$$

$$\sim p(\tau) \mid \sim q(\tau) \top r(\tau)$$





- The problem stems from the fact that the reasoner's BELIEF (i.e., knowledge) changes during the reasoning process.

There are TWO time intervals involved in temporal reasoning.



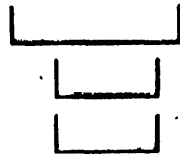


- The **ACTIVITY** interval, during which the proposition (was, is, will be) true
- The **BELIEF** interval, during which the reasoner believes a proposition about some activity interval to be true

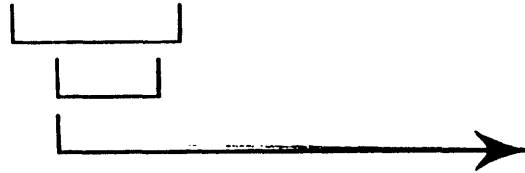


## Types of consequents

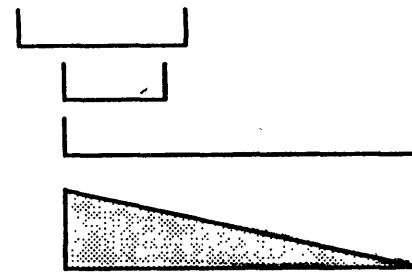
Bounded



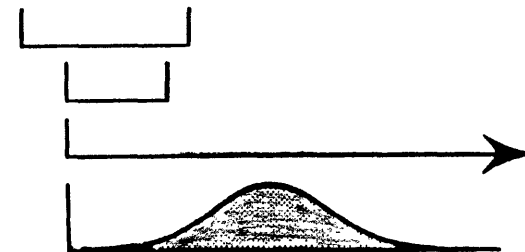
Persistent



Decayed



Probabilistic



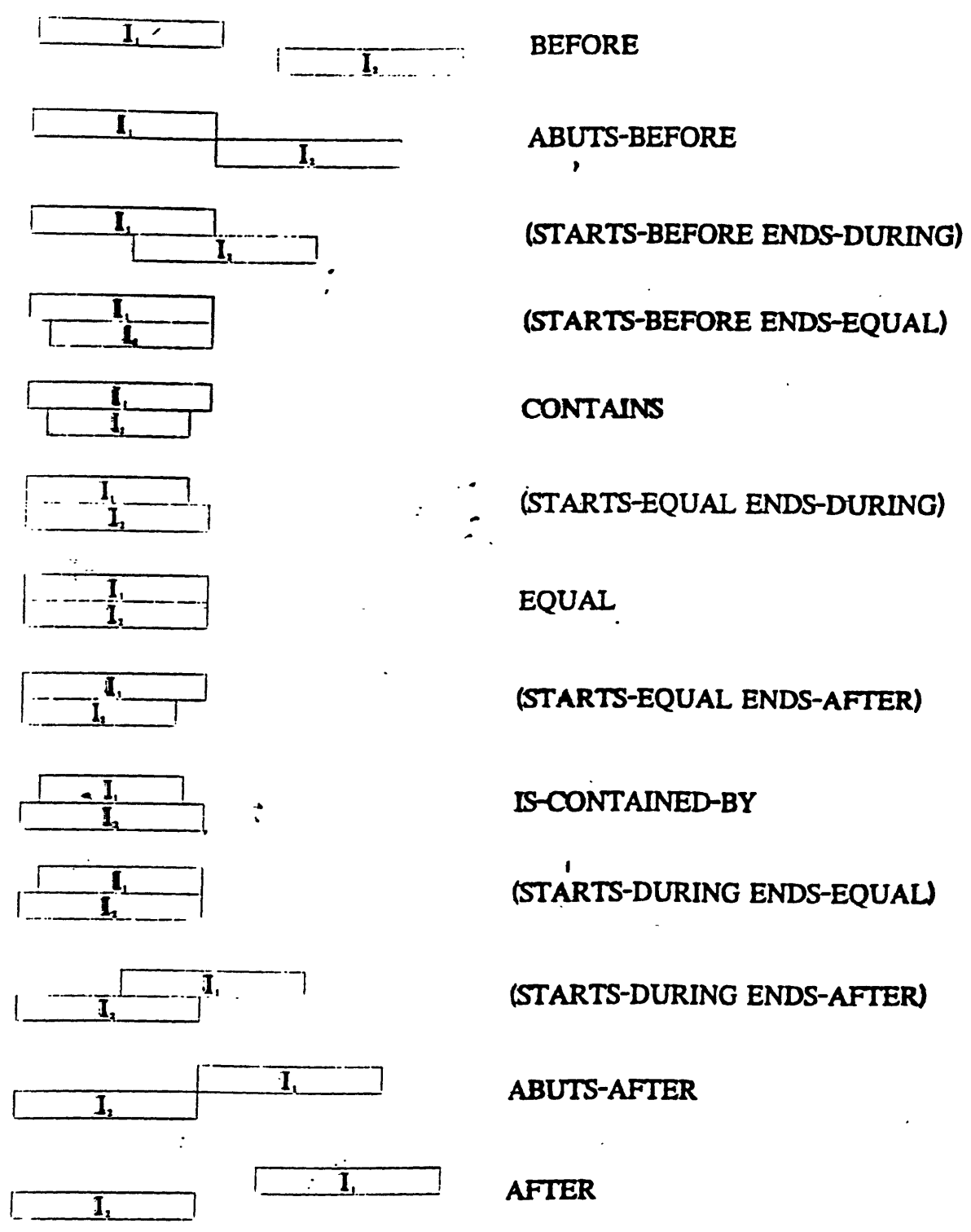
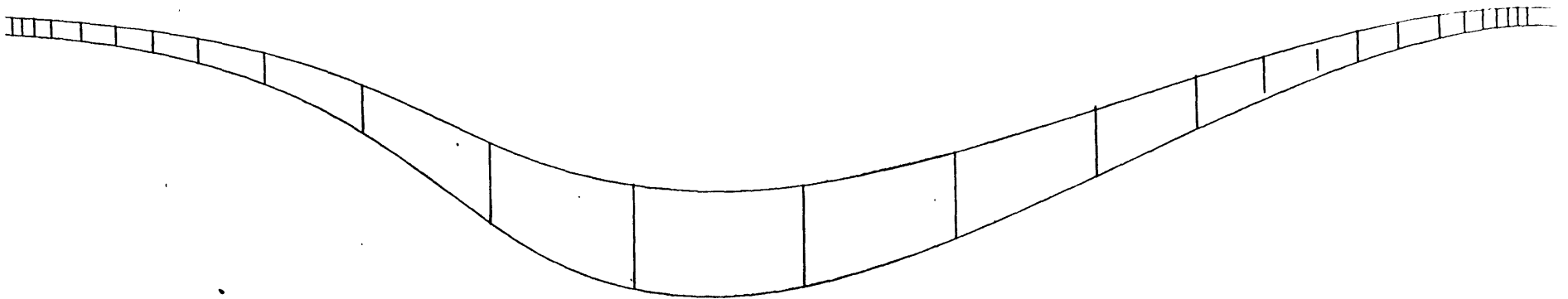


Figure 3.2: Temporal Relations

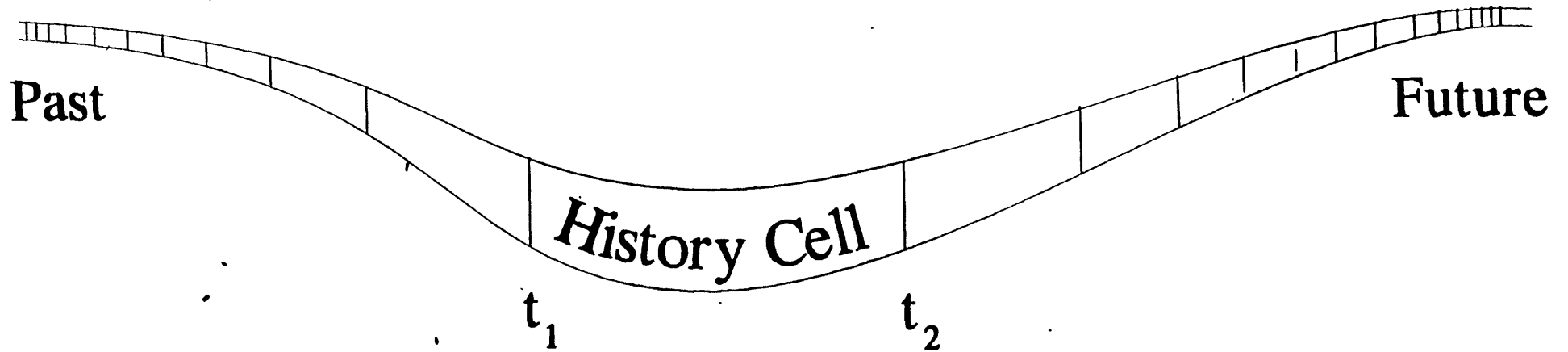


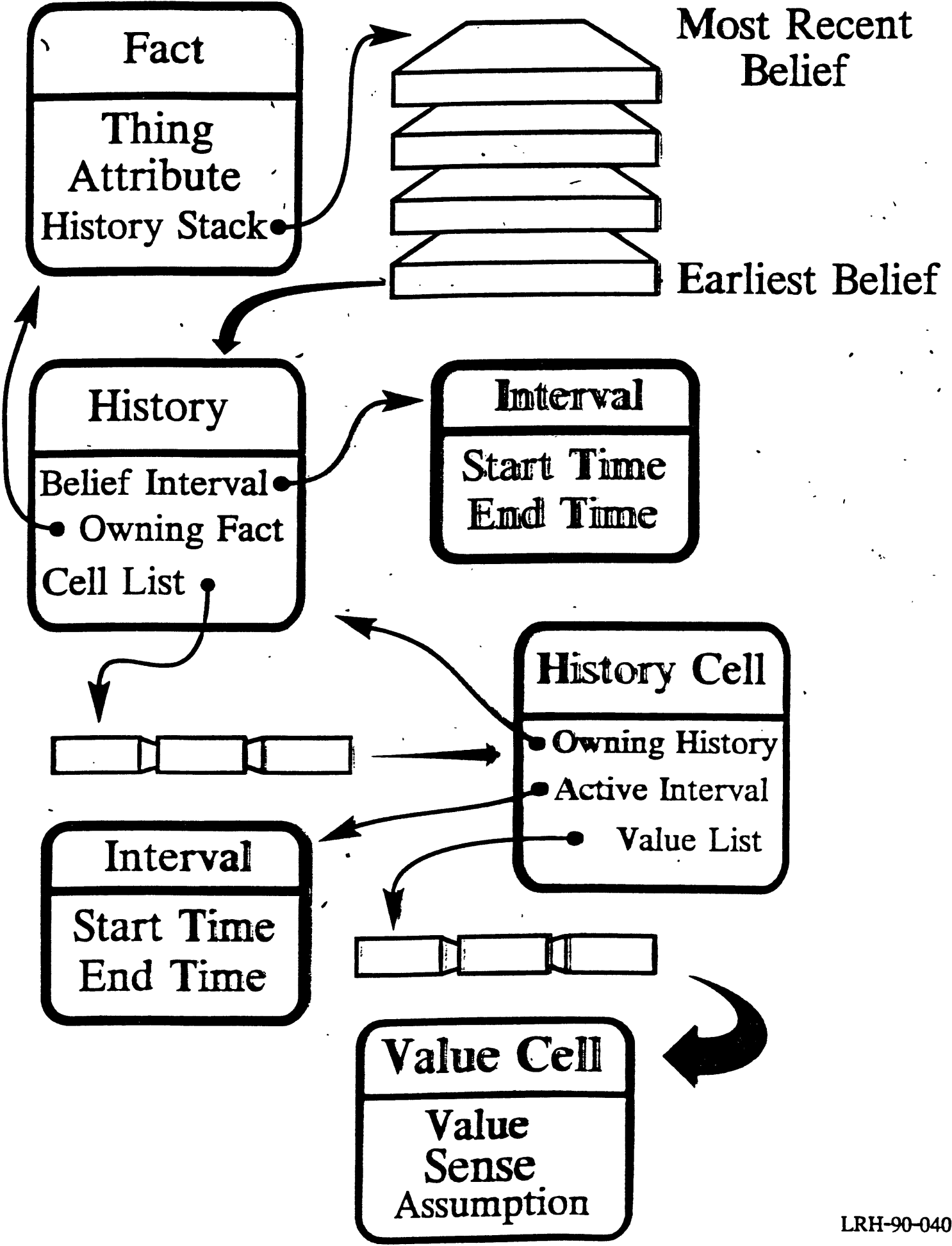


**FACT:**

**thing**

**attribute**





## CONTRIBUTIONS

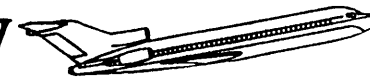
- Extension to Non-monotonic Temporal Logic  
by introducing Belief Intervals
- Introduced Persistence as rule specific knowledge
- Designed structures to represent time dependent  
knowledge
- Implemented an efficient temporal database  
management program



## CONTRIBUTIONS (continued)

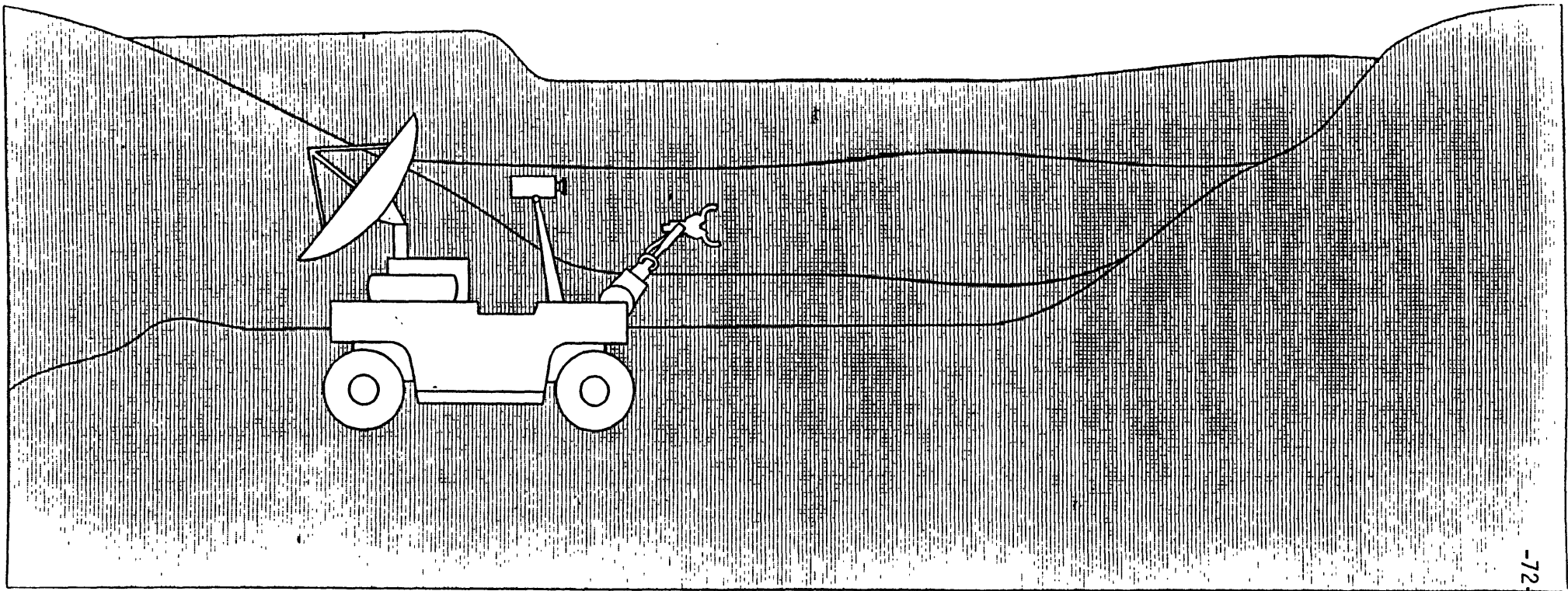
- Implemented a Temporal System Analyzer employing Extended Temporal Logic and Persistence
- Created a Scheduler Program, thereby extending Domain Independent Planning to include Parallel, Time Bounded, Non-Instantaneous Actions





Novel ideas and methods developed for this system include

- A highly compact representation for the description of discrete time dependent processes.
- An efficient time based logical inference system.
- Deeper understanding of human cognitive and communication processes involved in Command and Control Systems.
- A replacement of "Truth Maintenance" by "History Maintenance", and a better understanding of default versus dynamic logic.



# **Concentration in U.S. Air Transportation: An Analysis of Origin-Destination Markets since Deregulation**

**Jan Van Acker**

**Flight Transportation Laboratory  
May 23, 1991**

# Agenda

- I. Thesis Objective and Methodology
- II. Analysis of Top 100 Markets
- III. Analysis of Dominated City Markets
- IV. Conclusions

# I. Thesis Objective

- Study effects of deregulation on concentration
- Focus on Origin-Destination City-Pair Markets

# Focus on Concentration in O-D City-Pairs

- Other studies found:
  - Fares are positively related to concentration
  - Concentration levels have decreased on average
- Our study looked at:
  - Top 100 domestic O-D markets
  - Markets out of dominated cities

# Measurement of Concentration

- Concentration indices used:
  - Hirschman-Herfindahl Index (HHI)
  - 2-Firm Concentration Ratio (C2)
  - Number of Competitors with >5% Market Share  
(Number of Effective Competitors)
- Market share is measured in terms of local passengers transported in market

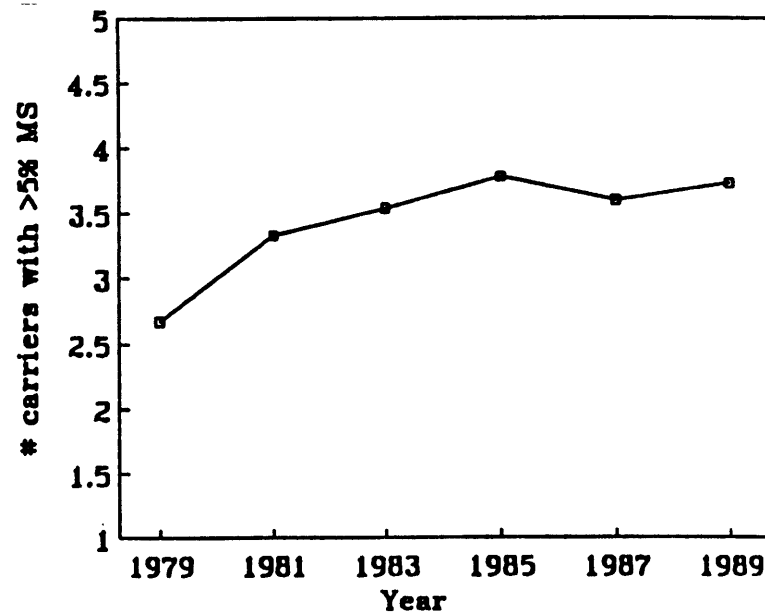
## II. Changes in Concentration in Top 100 Markets

- Markets ranked 1-100 in terms of local passengers transported in 1989
- Cumulative number of passengers was 31% of U.S. domestic total in 1989
- Years studied: 1979, 1981, 1983, 1985, 1987, 1989
- With focus on 1979, 1985, 1989



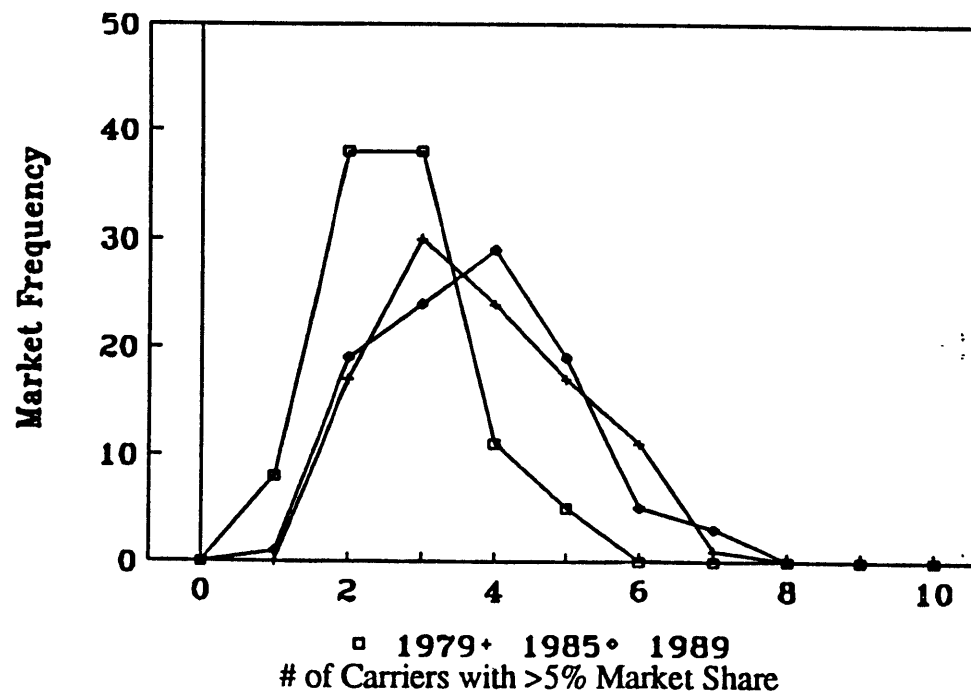
# Average Number of Effective Competitors was One more in 1989 than in 1979

Year	Average Number of Effective Competitors
1979	2.7
1981	3.3
1983	3.5
1985	3.8
1987	3.6
1989	3.7



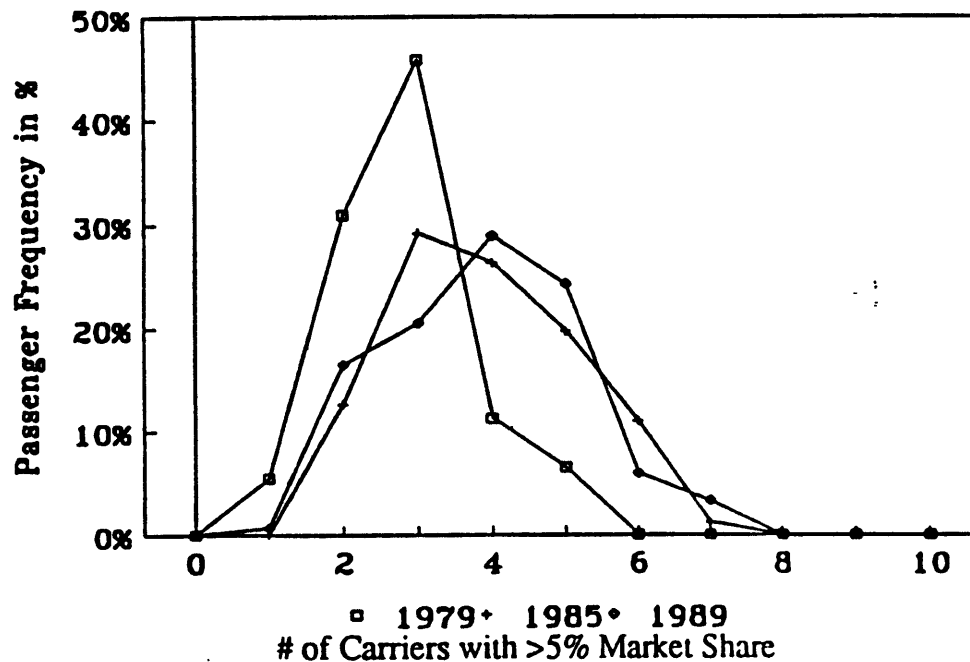
# 56 Markets Were Served by Four or More Effective Competitors in '89, as Compared to only 16 in '79

# Carriers With >5% MS	1979	1985	1989
1	8	0	1
2	38	17	19
3	38	30	24
4	11	24	29
5 to 6	5	28	24
7 to 8	0	1	3



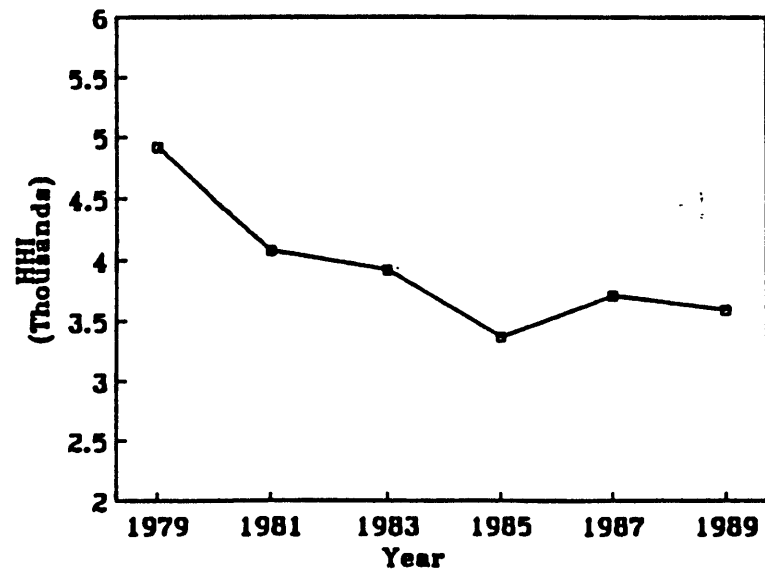
# 62% of the Passengers Flew in Markets Served by 4 or More Effective Competitors in '89 - - only 18% in '79

# Carriers With >5% MS	1979	1985	1989
1	5.5%	0.0%	0.7%
2	30.9%	12.6%	16.5%
3	45.8%	29.1%	20.5%
4	11.3%	26.3%	28.9%
5 to 6	6.5%	30.7%	30.2%
7 to 8	0.0%	1.2%	3.3%



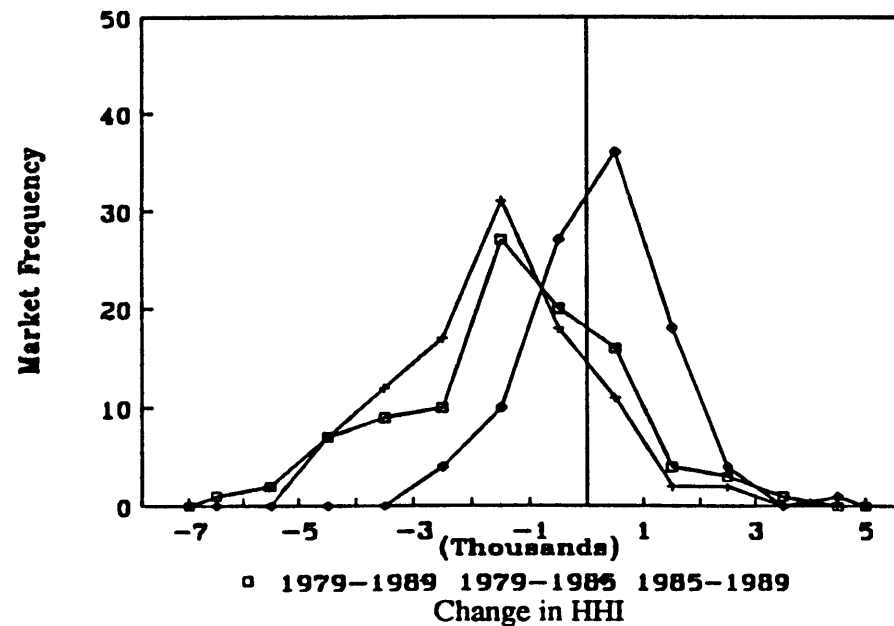
# Average HHI Was Lower in 1989 than in 1979

Year	Average HHI
1979	4917
1981	4077
1983	3913
1985	3361
1987	3705
1989	3586



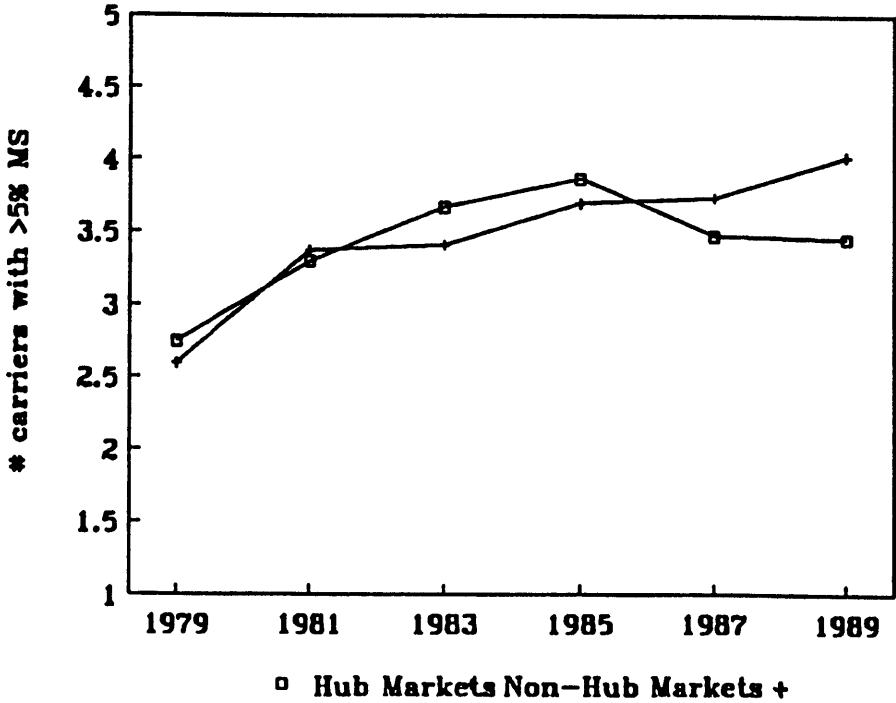
# The Majority of the Markets Experienced a Decrease in HHI from 1979 to 1989

Change in HHI	1979-1989	1979-1985	1985-1989
-8000 to -6000	1	0	0
-6000 to -4000	9	7	0
-4000 to -2000	19	29	4
-2000 to 0	47	49	37
0 to 2000	20	13	54
2000 to 4000	4	2	4
4000 to 6000	0	0	1
Total Decreased	76	85	41
Total Increased	24	15	59
Average Change	-1330	-1555	225



# The Non-Hub Markets Were Served on Average by a Greater Number of Effective Competitors in '89 than the Hub Markets

Year	Hub Markets	Non-Hub Markets
1979	2.7	2.6
1981	3.3	3.4
1983	3.7	3.4
1985	3.9	3.7
1987	3.5	3.7
1989	3.5	4.0



## Concentration Decreased from '79 to '89 in All but One of the Non-Hub Markets

Change in # Carriers With >5% MS	'79-'89	'79-'85	'85-'89
-4 to -3	0	0	0
-2 to -1	1	5	11
0	8	11	19
1 to 2	33	24	17
3 to 4	7	9	2
5 to 6	0	0	0
<b>Total Decreased</b>	1	5	11
<b>Total Increased</b>	40	33	19
<b>Average Change</b>	1.10	0.33	1.43

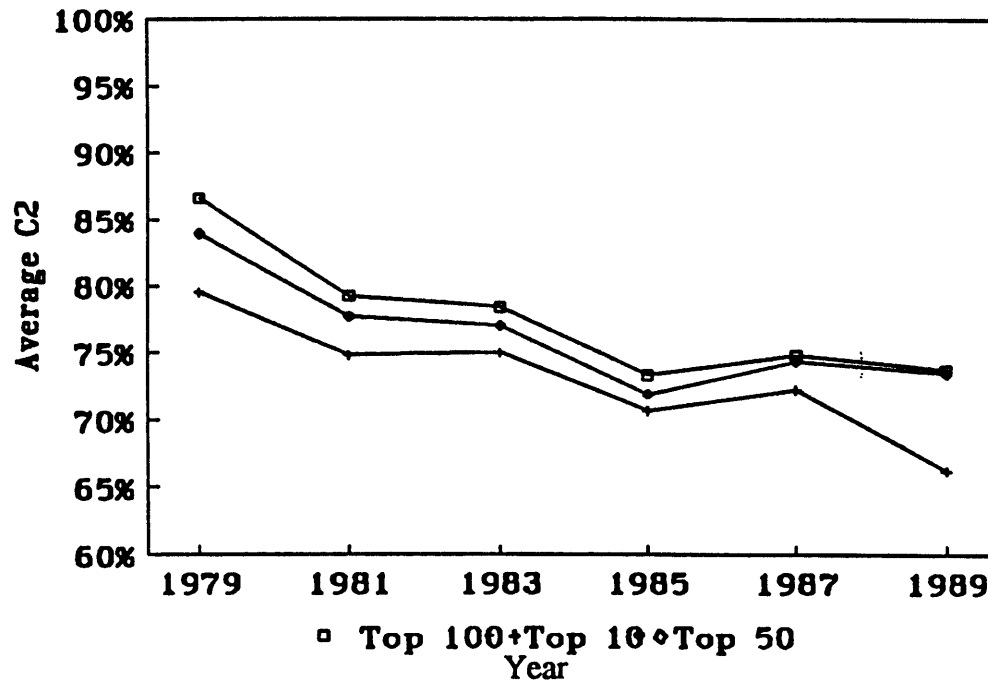
## But Was Higher in '89 than in '79 in 30% of the Hub Markets

Change in # Carriers With >5% MS	'79-'89	'79-'85	'85-'89
-4 to -3	1	0	1
-2 to -1	11	7	26
0	9	8	16
1 to 2	25	28	8
3 to 4	4	8	0
5 to 6	1	0	0
Total Decreased	12	7	27
Total Increased	30	36	8
Average Change	1.12	-0.41	0.71



# The Top 10 Markets Were on Average Less Concentrated than the Top 50 and Top 100 Markets

Year	Top 100 Markets	Top 10 Markets	Top 50 Markets
1979	86.6%	79.5%	83.9%
1981	79.2%	74.8%	77.7%
1983	78.4%	75.0%	77.0%
1985	73.3%	70.6%	71.8%
1987	74.7%	72.2%	74.3%
1989	73.6%	66.2%	73.3%



# Conclusions of Top 100 Markets Analysis

- Average concentration was lower in '89 than in '79
- Concentration was lower in 70% of the markets
- Non-hub markets were better off on average in 1989 than hub markets
- Top ten markets were less concentrated on average than top 100 markets

### III. Changes in Concentration in Top Ten Markets out of Dominated Cities

- Cities at which 60% of total passenger enplanements in 1985 were carried by one airline, or 85% by two:

Atlanta	Detroit	Pittsburgh
Charlotte	Greensboro	Raleigh/Durham
Cincinnati	Memphis	St. Louis
Dayton	Minneapolis	Salt Lake City
Denver	Nashville	Syracuse

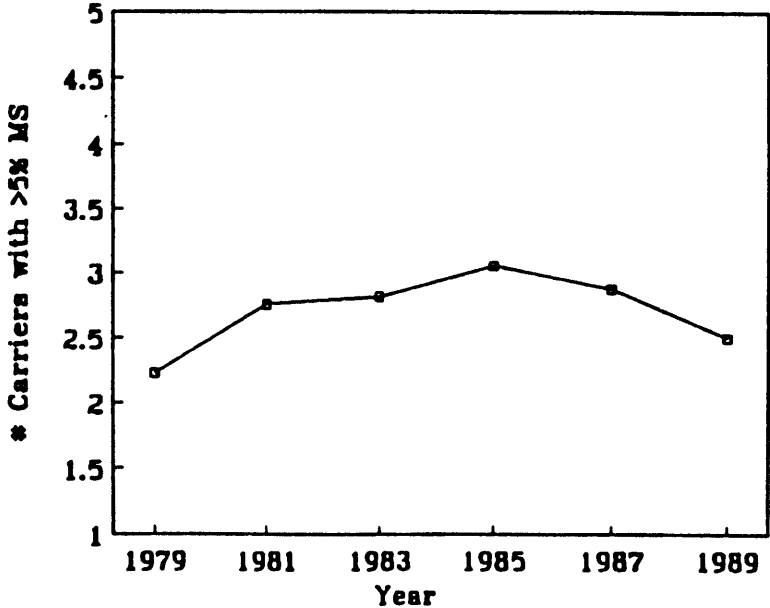
- Markets ranked 1-10 in terms of local passengers transported in 1989 out of each of the cities

# Changes in Concentration in Top Ten Markets out of Dominated Cities

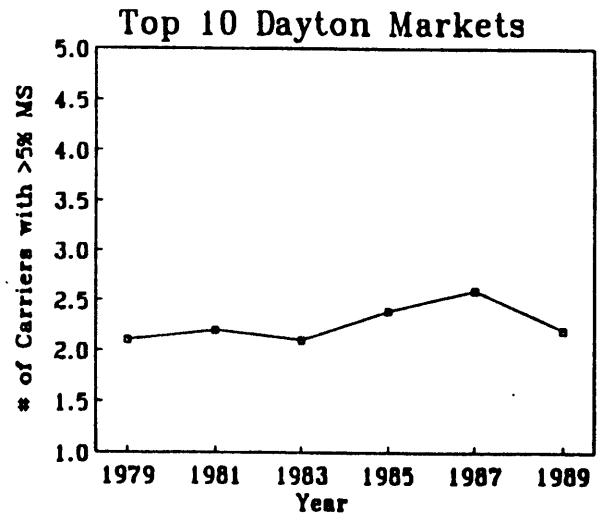
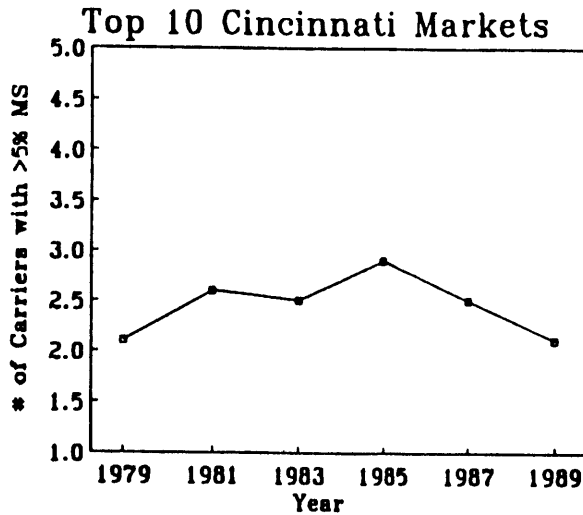
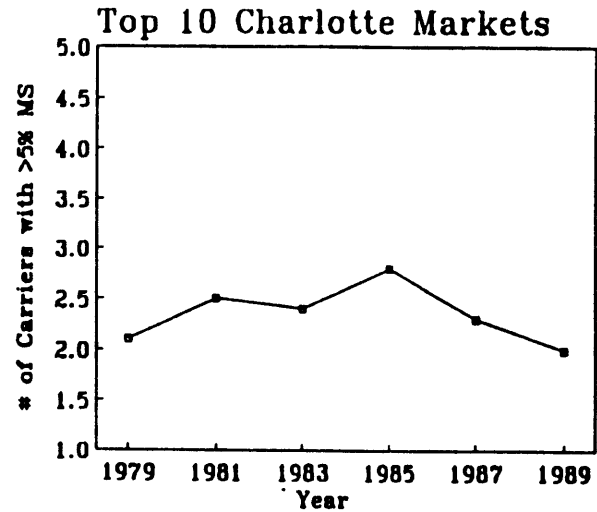
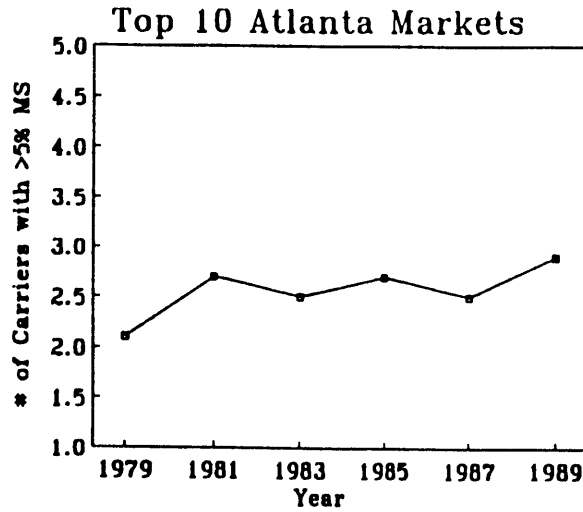
- Years studied: 1979, 1981, 1983, 1985, 1987, 1989
- With focus on 1979, 1985, 1989

# Average Number of Effective Competitors in 150 Markets Peaked in '85, but Was Still Higher in '89 than in '79

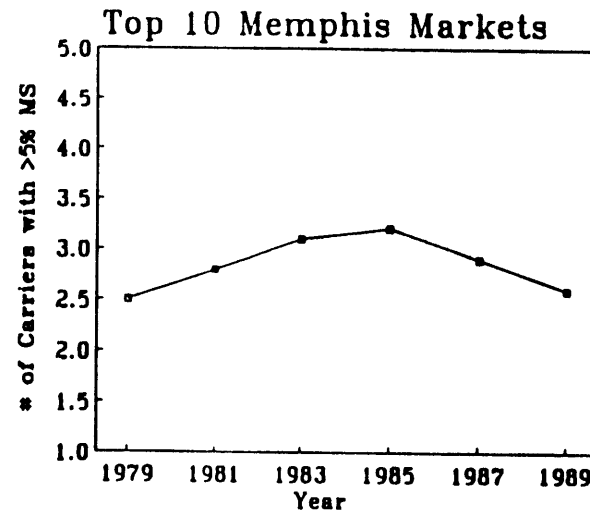
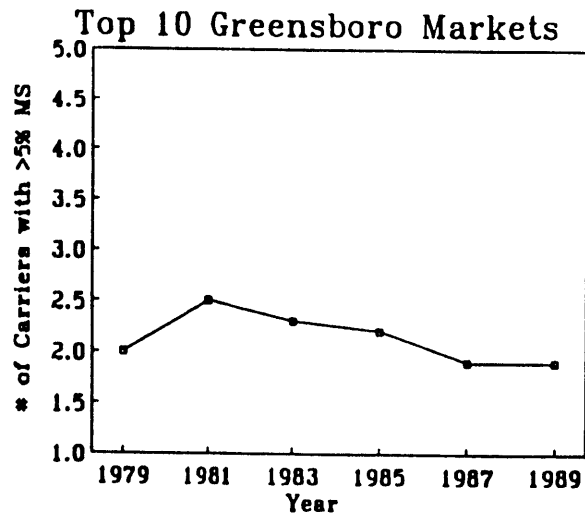
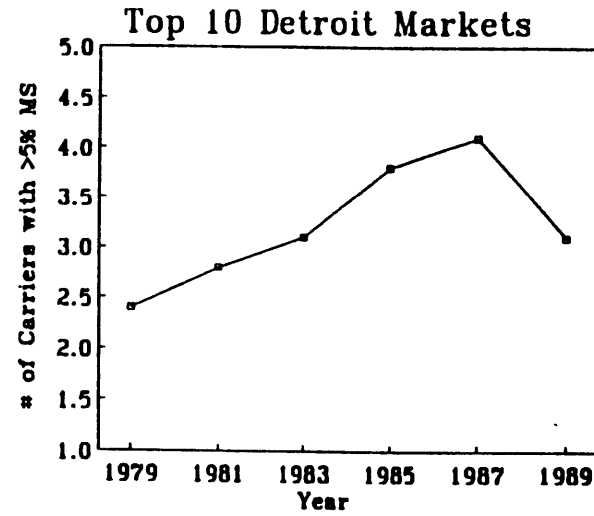
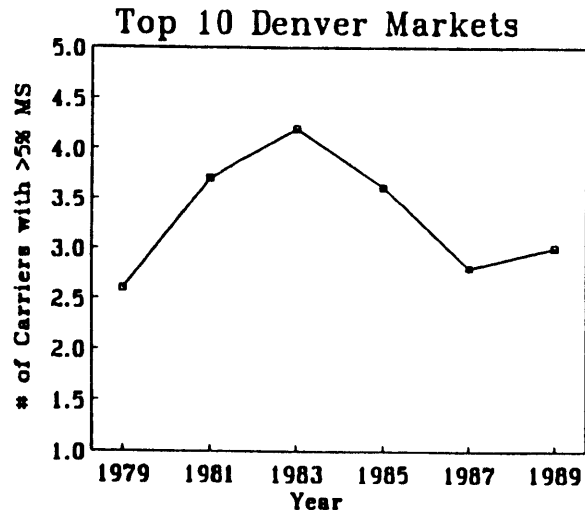
Year	Dominated Airport Markets
1979	2.2
1981	2.8
1983	2.8
1985	3.1
1987	2.9
1989	2.5



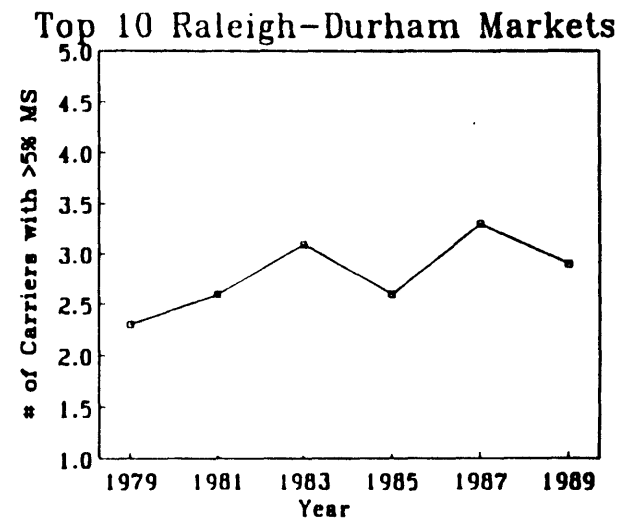
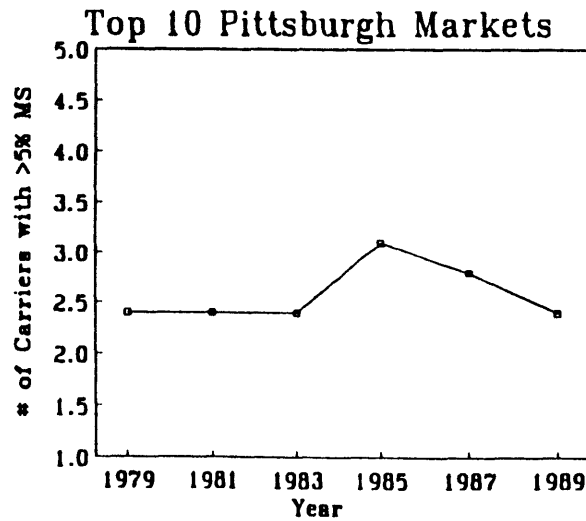
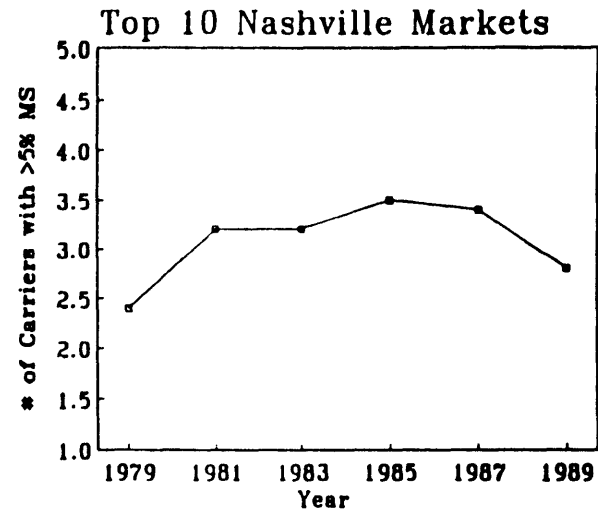
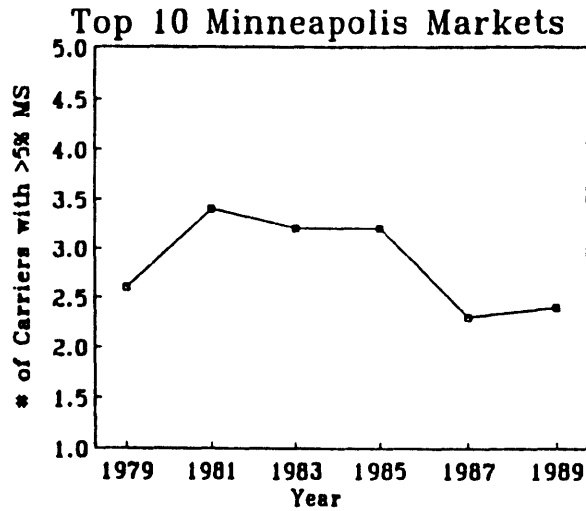
# Average Number of Effective Competitors for each of the Dominated Cities



# Average Number of Effective Competitors for each of the Dominated Cities

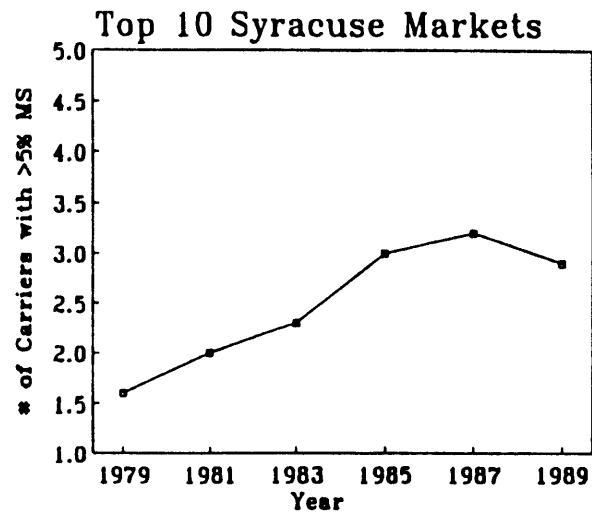
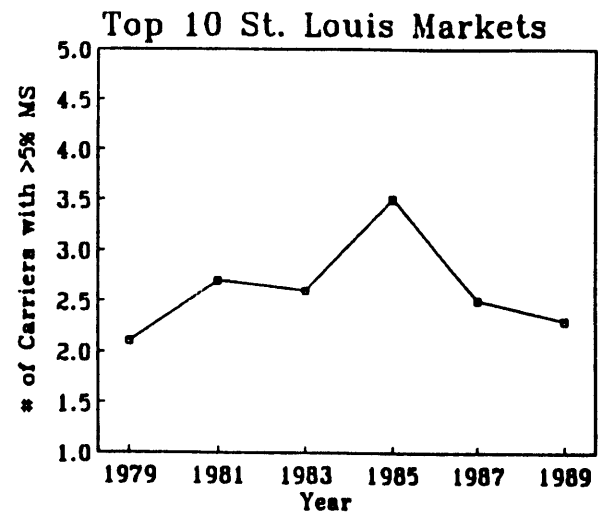
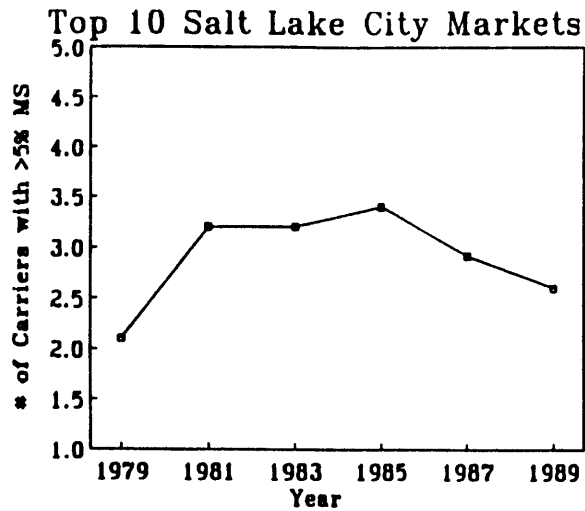


# Average Number of Effective Competitors for each of the Dominated Cities





# Average Number of Effective Competitors for each of the Dominated Cities



# Changes in Concentration in the Top Ten Atlanta Markets

O-D City-Pair Markets		HHI	Change in HHI		
		1989	'79-'89	'79-'85	'85-'89
Atlanta	Boston	5446	455	-547	1002
Atlanta	Chicago	2949	-2538	-2031	-508
Atlanta	Dallas/Fort Worth	5932	-350	-1968	1618
Atlanta	Los Angeles	5089	-219	-656	437
Atlanta	Miami	3737	-1004	-885	-119
Atlanta	New York	3913	-935	-1294	359
Atlanta	Orlando	5608	482	-880	1362
Atlanta	Philadelphia	4097	-995	-410	-585
Atlanta	Tampa	6002	955	-637	1593
Atlanta	Washington	4701	-193	-721	528
Total Decreased			7	10	3
Total Increased			3	0	7
Average		4747	-434	-1003	569

## Concentration Levels Decreased Substantially in Most of the Top Ten Syracuse Markets

O-D City-Pair Markets		HHI	Change in HHI		
		1989	'79-'89	'79-'85	'85-'89
Syracuse	Atlanta	4418	-5552	-4065	-1487
Syracuse	Boston	9045	175	-4091	4266
Syracuse	Chicago	4119	-5473	-5889	417
Syracuse	Detroit	8942	3967	-740	4707
Syracuse	Los Angeles	1585	-5234	-4924	-310
Syracuse	New York	5820	653	-1756	2409
Syracuse	Orlando	3047	-6014	-5507	-507
Syracuse	Philadelphia	9741	790	493	296
Syracuse	Tampa	2695	-5875	-5178	-697
Syracuse	Washington	8289	-1406	-4879	3473
Total Decreased			6	9	4
Total Increased			4	1	6
Average		5770	-2397	-3653	1257

## Concentration Increased in all Top Ten St. Louis Markets after the TWA-Ozark Merger

O-D City-Pair Markets		HHI	Change in HHI		
		1989	'79-'89	'79-'85	'85-'89
St. Louis	Chicago	3347	-2161	-3019	858
St. Louis	Dallas/Fort Worth	4528	-506	-2037	1530
St. Louis	Denver	4671	-238	-2333	2095
St. Louis	Detroit	3306	-2180	-2200	20
St. Louis	Houston	3561	-916	-1626	710
St. Louis	Los Angeles	5486	-48	-654	606
St. Louis	New York	8860	2650	-1356	4006
St. Louis	Phoenix	4780	-320	-1360	1040
St. Louis	San Francisco	6567	155	-547	701
St. Louis	Washington	8252	302	-3798	4100
Total Decreased			7	10	0
Total Increased			3		10
Average		5336	-326	-1893	1567

# Conclusions of Dominated City Markets Analysis

- Single trend of hub development led to decreased concentration through '85 at most of the cities, but to increases from '85 on
- Two-hub markets were less concentrated than one-hub markets in 1989
- Average concentration across the 150 markets was slightly lower in '89 than in '79

## IV. Conclusions

- Concentration was lower in top 100 markets, both on average and in most of the markets
- Concentration in non-hub markets decreased throughout period '79-'89 because of development of hub-and-spoke networks
- These networks led to increases in concentration in most hub markets after 1985

# Conclusions

- Single trend of hub development led to decreases in concentration through '85 at most of the dominated cities, but to increases from '85 on
- Concentration was on average slightly lower in the 150 markets out of dominated cities in 1979 than in 1989, and was lower in half of the markets

**Pricing in the Airline Industry  
Current Practice and  
Future Research**

**Theodore C. Botimer  
MIT Flight Transportation Laboratory  
Presentation to Cooperative Research Program  
May 23, 1991**



# Presentation Outline

## Overview

- Nature of Airline Competition
- Fare Product Differentiation
- Seat Inventory Management
- Pricing Strategies
- Role of the Pricing Analyst
- “The Ultimate Pricing Model”
- Theoretical Issues for Investigation

## Case Study Analysis

- Case Study Overview
- Case Study Objectives
- O/D Market Choice
- ATL - BOS Market
- ATL - STL Market
- Conclusions

## Nature of Airline Competition

- Hub and spoke route structures prevail in the industry allowing almost every major carrier to serve any O/D market
- Most competition on non-price level
- Dollar value of nonstop service is unclear
- Must consider strength of competitive position in each O/D market separately
- Characterize competition in all markets:
  - major players
  - level of service offered
  - number of flights per day offered
  - nonstop vs. nonstop competition
- Anticipate response to price changes:
  - who are the competitors?
  - do the competitors offer comparable service in the market?
  - how have competitors reacted to fare changes in the past?
  - what response will be given to hostile reactions by competitors?

## Fare Product Differentiation

- Airlines seek to segment demand by offering differentiated fare products in different fare classes
  
- Delta offers tickets in 10 fare classes:
  - 1) F - full fare first class
  - 2) Y - full fare coach class
  - 3) B - reserved for military/  
convention/negotiated fares
  - 4) M - highest discount coach fare
  - 5) H - discount coach class fare
  - 6) Q - discount coach class fare
  - 7) K - reserved for competitive filings
  - 8) L - reserved for competitive filings
  - 9) A - first class free tickets
  - 10) W - coach class free tickets
  
- Differentiation occurs within fare classes
  - peak vs. off-peak fares
  - weekday vs. weekend fares

## Fare Product Differentiation (con't)

- Fare restrictions or “fences” used to control which type of consumer is able to purchase which type of ticket
  
- Common fare restrictions include:
  - advanced purchase requirements
  - Saturday night stayover
  - blackout periods
  - flight validity restrictions  
(good for travel between...)
  - ticket purchase restrictions  
(purchase tickets by...)
  - availability limits for discount fares
  - military discount fares
  - senior citizen discount fares

## **Seat Inventory Management (IM)**

- Pricing sets O/D prices and restrictions
- IM decisions made with fixed prices and restrictions
- IM seeks to maximize revenue given fixed prices and restrictions
- IM controls price/seat quantity decisions
  - protect full fare seats
  - limit discount fares
  - strictly limit deep discount fare seat availability
- Matching stances require booking limits
  - strictly limited availability on competitive fare filings

## Pricing Strategies and Their Effects

- Matching a fare
  - retain market share
  - possible drop in yield
  - remain listed on Page 1 of CRS
  - often done to remain competitive
  - viewed as price taker in the market
  
- Not matching a fare
  - possible loss of market share
  - maintain yield
  - may lose competitiveness
  - loss of goodwill
  
- Partially matching a fare
  - attempt to retain market share
  - reduce non-matching yield loss
  - market factors influence strategy
  - will be non-competitive at peak
  - accept that competitor offers low fare on all flights

## **Role of the Pricing Analyst**

- Analysts do not look at operating costs
- Consider strength of competitive position in each O/D market
- Add routing restrictions to discount fares
- Pricing analysts should be familiar with own market and relevant hub:
  - traffic flows
  - flight load factors
- Be aware of fare differential effects
  - high differentials not seen on CRS
  - business travelers susceptible to higher differentials
  - not all fares registered in ATP listings are available in reality
- Must monitor the number of bookings to determine the effect on yield of changes

# Ultimate Pricing Model

- Inputs:
  - published daily fare changes
  - system-wide flight schedule
  - price level (by O/D market & flight)
  
- Outputs:
  - Suggested strategy
    - matching
    - partial matching
    - not matching
  - Projected impact on market share
  - Projected impact on revenue
  - Management reports telling:
    - suggested matching decision
    - implemented matching decision
    - reasons for matching decision
  - Ability to run simulations
  - Ability to do what-if scenarios



## Theoretical Issues for Investigation

- Joint seat/price optimization problem
- Optimal differential pricing strategies
- Model development for pricing strategies
  - matching
  - not matching
  - other pricing strategies
- Impacts of price changes
- Measurements of price elasticity
- Explore impacts of pricing strategies on:
  - profitability
  - load factor
  - yield
  - customer satisfaction

## Case Study Overview

- Close look at 10 O/D markets
- Representative cross section of markets flown by Delta Airlines
- Quarterly analysis
- Examine quarterly data 1986:1 - 1990:2
- Give consideration to:
  - published fares
  - competitive responses
  - major price level changes
- Use information from several data bases:
  - PIPPS (Historical ATP data)
  - DOT O/D traffic stats (10% sample)
  - Official Airline Guide
- Preliminary analysis on two markets:
  - ATL - BOS
  - ATL - STL

## Case Study Objectives

- Initial look at revenue management from pricing perspective
- Develop market by market case studies
  - Present a market overview
  - Characterize pricing practices
  - Analyze competitive environment
  - Uncover competitive characteristics
  - Highlight major market events
- Analyze the quality and level of detail of the available data sources
- Relate market strength to fare level
  - between carriers
  - over time
- Develop a measure of the sensitivity of travelers to changes in fare level
- Determine selling fares during the period
- Use available data to determine the effects of pricing decisions
- Discuss future directions for research

## O/D Market Choice

### Length of Haul

- Short Haul (<1000 miles)
- Medium Haul (1000-2000 miles)
- Long Haul (>2000 miles)

### Nature of Competition

- Delta offers non-stop service
- Only competitors offer non-stop service
- No one offers non-stop service

### Markets Chosen

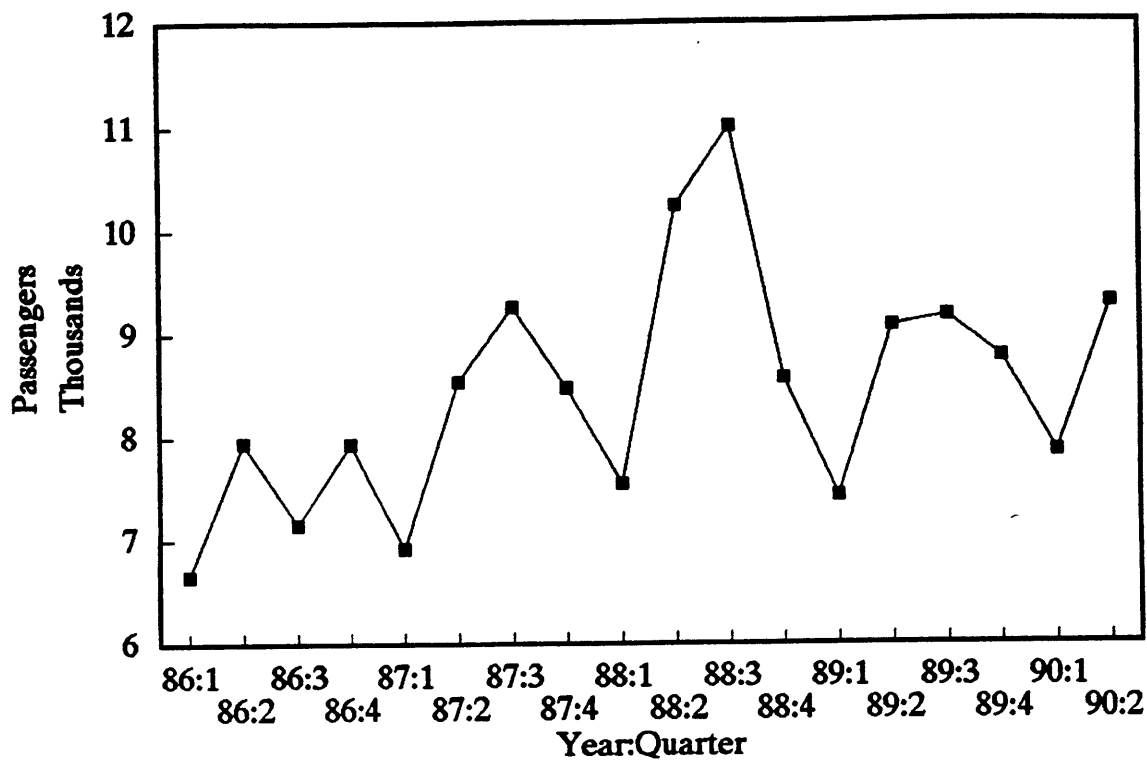
- 1) ATL-BOS
- 2) ATL-SEA
- 3) ATL-STL
- 4) BOS-PHX
- 5) CLT-MSP
- 6) DFW-PHL
- 7) JAN-SDF
- 8) MSP-SAN
- 9) MSY-PWM
- 10) SAV-SAN

## ATL - BOS Market Characteristics 1986:1 - 1990:2

- Two non-stop carriers during the period
  - Delta
  - Eastern
  
- Non-stop carriers flew 93% of all pax
  
- Frequency of approximately 12 daily non-stops each way
  
- Total traffic level of 925 passengers per day in both directions
  
- Carriers with ATL hub
  - Delta
  - Eastern
  
- Eastern Airlines strike in 1989:2

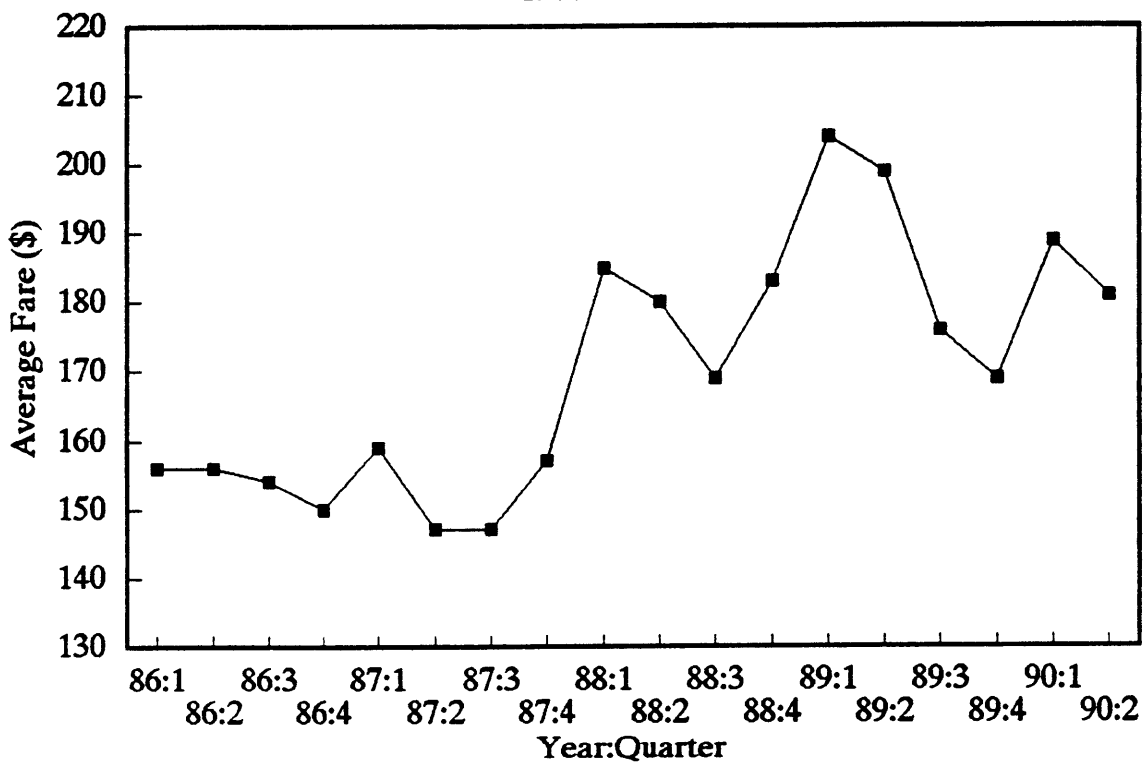
# ATL-BOS Passengers

1986:1 - 1990:2



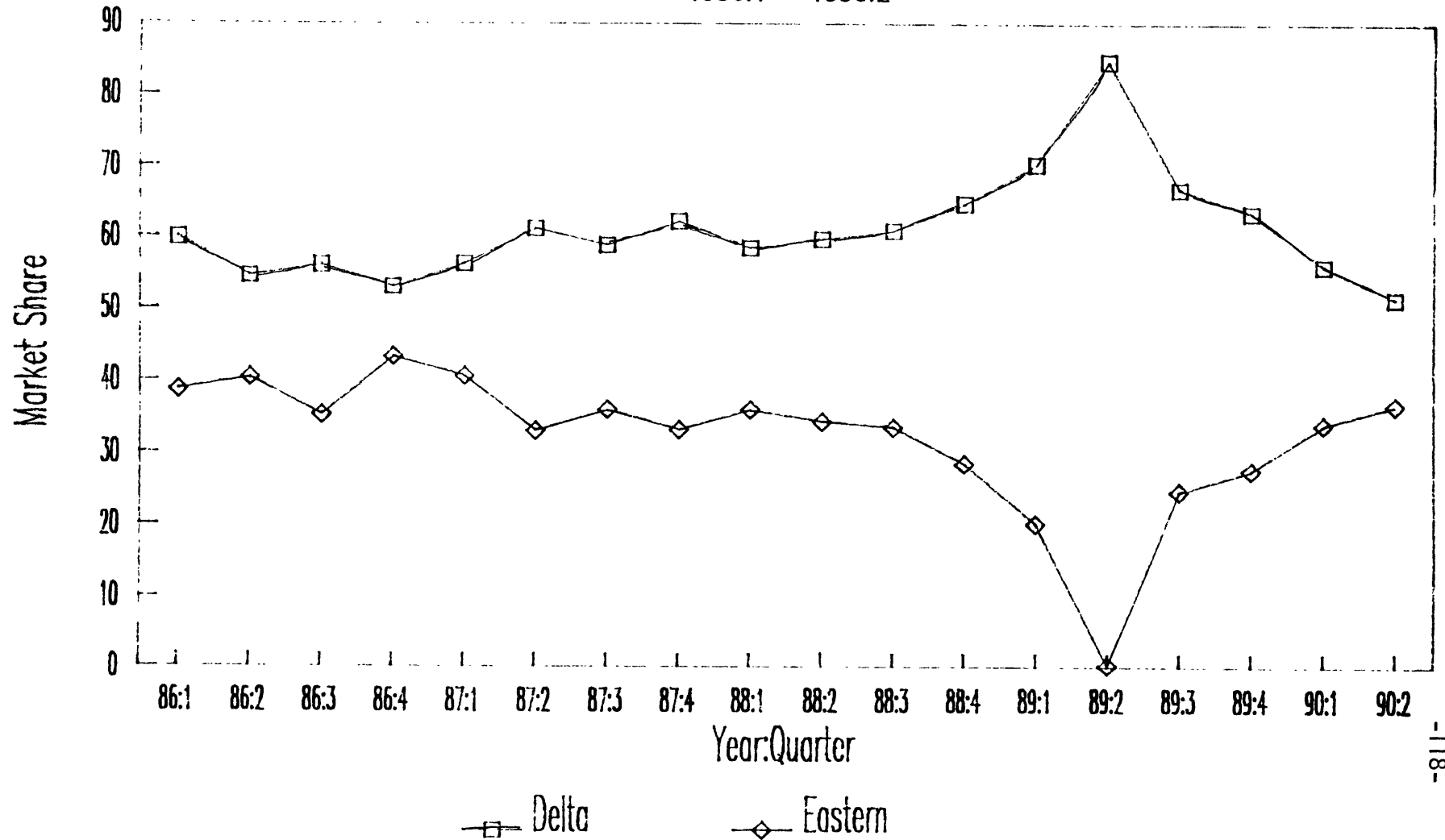
# ATL-BOS Average Fare

1986:1 - 1990:2



# ATL-BOS Market Share

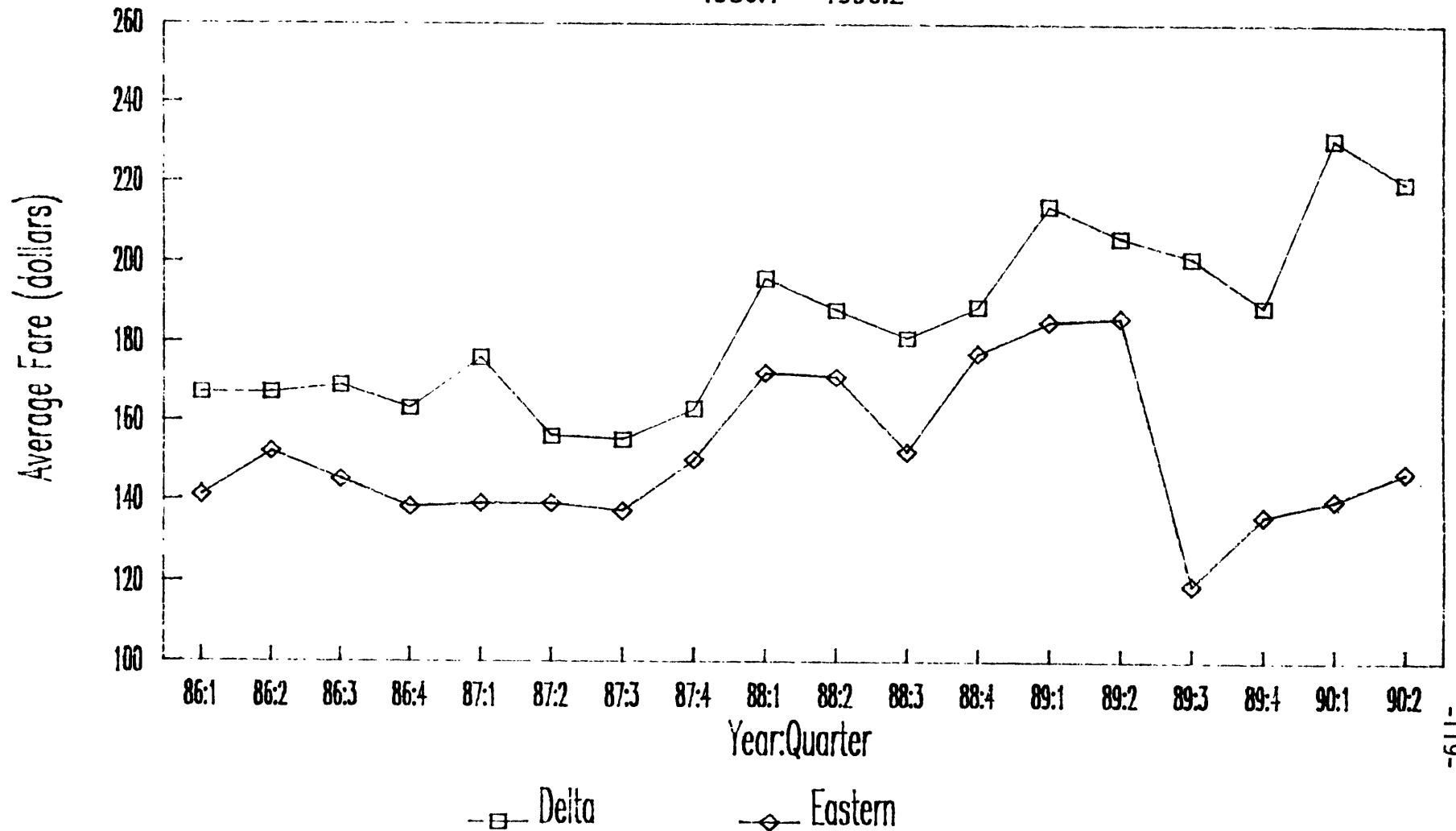
1986:1 - 1990:2





# ATL-BOS Average Fare

1986:1 - 1990:2



**ATL - BOS  
Summary Table**

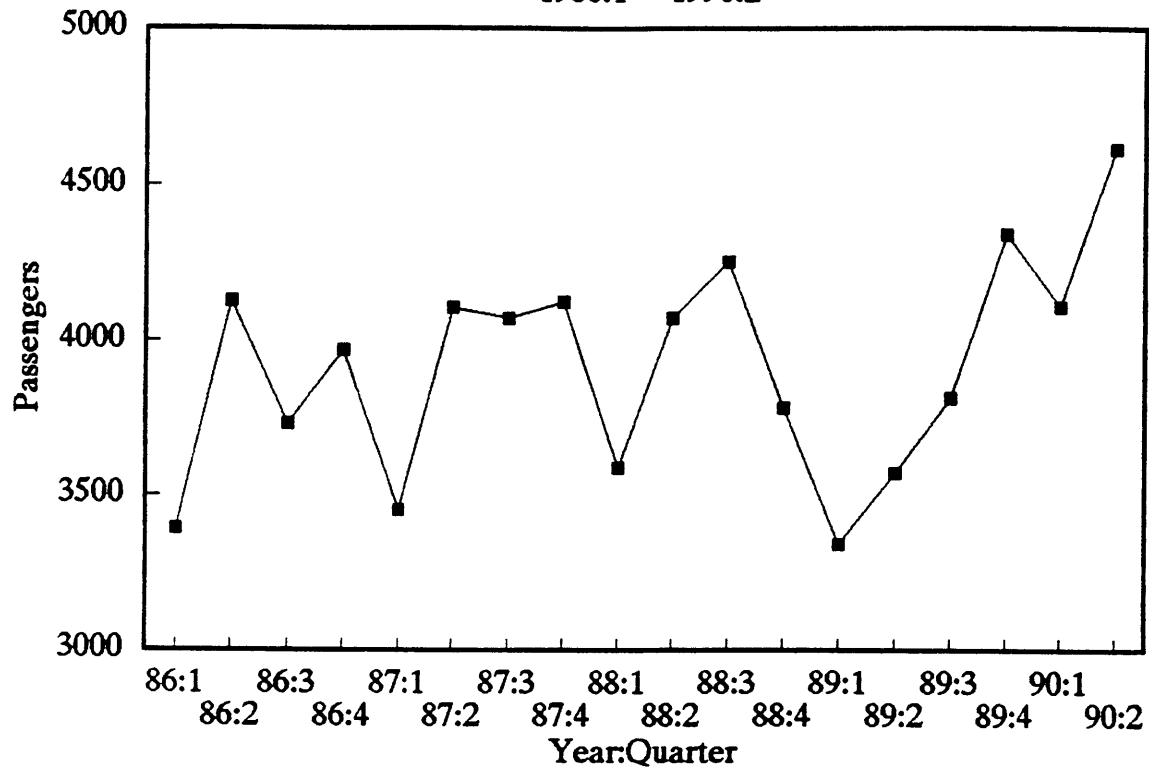
	Passengers	Revenues	Average Fare	Coupon Mileage	Passengers Per Day	Market Share	Revenue Share	Yield Per CPM
Delta 88:2	6118	1152456	188	5872057	67.2	59.74	62.63	19.63
Delta 89:2	7676	1584791	206	7372559	84.4	74.95	88.01	21.50
% Change	25.47	37.51	9.60	25.55	25.47	25.47	40.51	9.53
Eastern 88:2	3508	599469	171	3348572	38.5	34.25	32.58	17.90
Eastern 89:2	9	1674	186	8514	0.1	0.09	0.09	19.66
% Change	-99.74	-99.72	8.84	-99.75	-99.74	-99.74	-99.71	9.83
OA 88:2	615	88075	143	653125	6.8	6.01	4.79	13.49
OA 89:2	1387	214329	155	1429440	15.2	13.54	11.90	14.99
% Change	125.53	143.35	7.90	118.86	125.53	125.53	148.65	11.19
Market 88:2	10241	1840000	180	9873754	112.5	100.00	100.00	18.64
Market 89:2	9072	1800794	199	8810513	99.7	100.00	100.00	20.44
% Change	-11.41	-2.13	10.48	-10.77	-11.41	0.00	0.00	9.68

## **ATL - STL Market Characteristics 1986:1 - 1990:2**

- **Four non-stop carriers during the period**
  - **Delta**
  - **Eastern**
  - **Ozark**
  - **TWA**
  
- **Non-stop carriers flew over 90% of all pax**
  
- **Frequency of approximately 15 daily non-stops each way**
  
- **Total traffic level of under 450 passengers per day in both directions**
  
- **Carriers with ATL hub**
  - **Delta**
  - **Eastern**
  
- **Carriers with STL hub**
  - **Ozark**
  - **TWA**
  
- **Eastern Airlines strike in 1989:2**
  
- **Ozark - TWA merger in 1987**

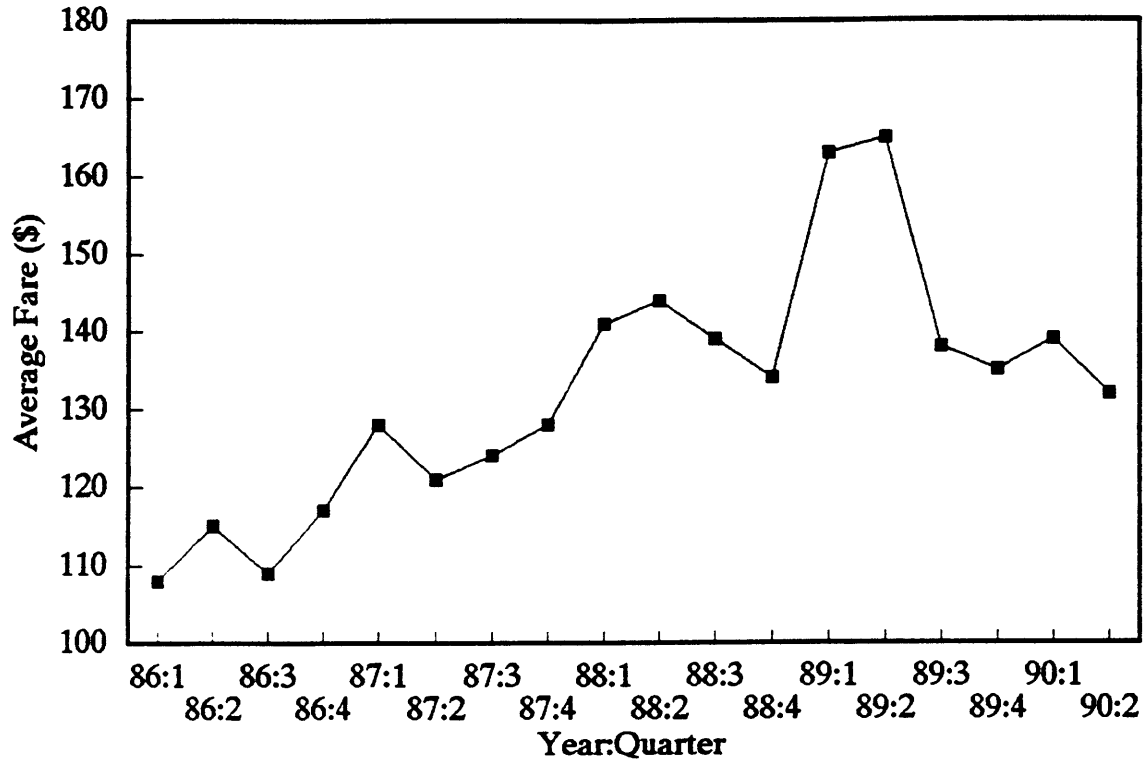
# ATL – STL Passengers

1986:1 – 1990:2



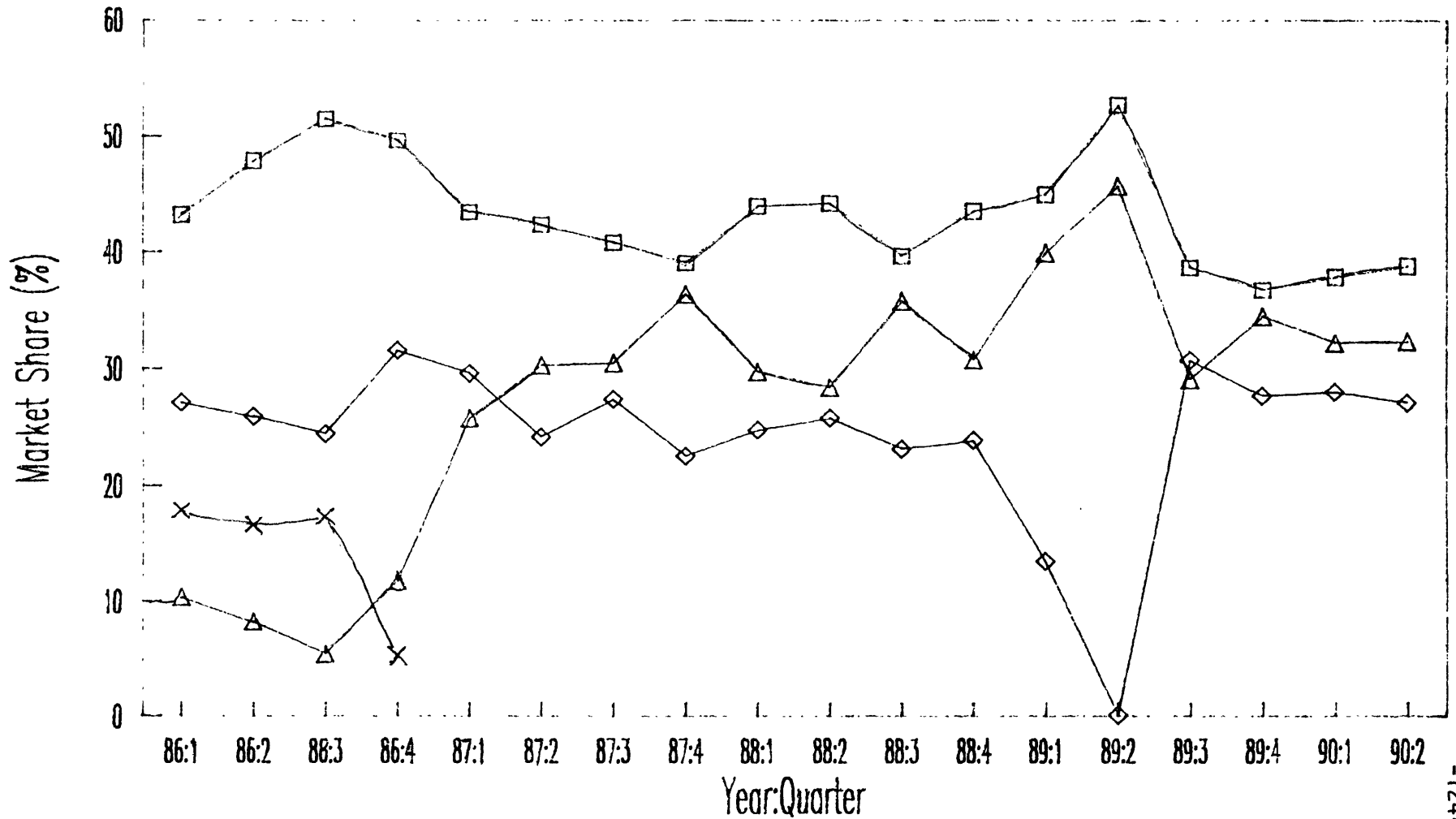
# ATL – STL Average Fare

1986:1 – 1990:2



# ATL - STL Market Share

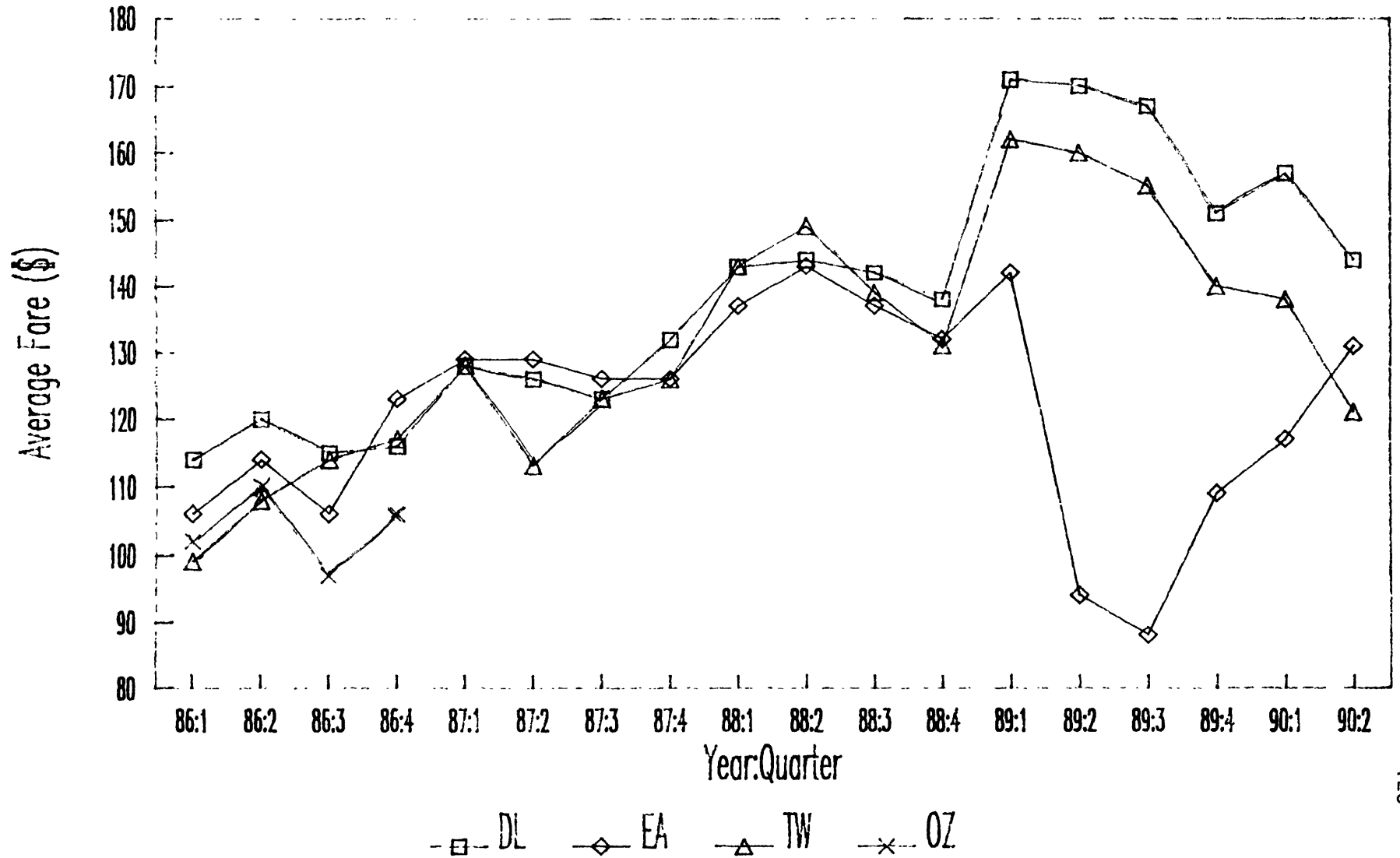
1986:1 - 1990:2



DL FA TW OZ

# ATL - STL Average Fare

1986:1 - 1990:2



**ATL - STL  
Summary Table**

	Passengers	Revenues	Average Fare	Coupon Mileage	Passengers Per Day	Market Share	Revenue Share	Yield Per CPM
Delta 88:2	1799	259057	144	881790	19.8	44.20	44.15	29.38
Delta 89:2	1882	320589	170	919694	20.7	46.24	54.47	34.86
% Change	4.61	23.75	18.29	4.30	4.61	4.61	23.39	18.65
Eastern 88:2	1049	149500	143	510126	11.5	25.77	25.48	29.31
Eastern 89:2	1	94	94	484	0.0	0.02	0.02	19.42
% Change	-99.90	-99.94	-34.04	-99.91	-99.90	-99.90	-99.94	-33.73
TWA 88:2	1155.00	172264.00	149	560872.00	12.7	28.38	29.36	30.71
TWA 89:2	1631.00	261282.00	160	793400.00	17.9	40.07	44.52	32.93
% Change	41.21	51.68	7.41	41.46	41.21	41.21	51.68	7.22
OA 88:2	67	6003	90	48980	0.7	1.65	1.02	12.26
OA 89:2	57	6560	115	38358	0.6	1.40	1.11	17.10
% Change	-14.93	9.28	28.45	-21.69	-14.93	-14.93	8.96	39.54
Market 88:2	4070	586824	144	2001768	44.7	100.00	100.00	29.32
Market 89:2	3571	588525	165	1751936	39.2	100.00	100.00	33.59
% Change	-12.26	0.29	14.30	-12.48	-12.26	0.00	0.00	14.59



## **Conclusions**

- **Carrier strength varies by O/D market**
- **Delta holds a stronger position in ATL - BOS than in ATL - STL**
- **Delta fare levels may have been too high in ATL - STL during the strike given its competitive position**

## **Future Directions**

- Quantify consumer price sensitivity and market share changes**
- Determine relationships between market strength and fare levels**
- Develop a model to characterize competitive structure of markets**

# CHANGES IN O-D PASSENGER TRAFFIC FLOWS

## NEWARK AIRPORT

Chung Y. Mak

and

Professor Peter P. Belobaba

MIT Flight Transportation Laboratory

MIT / Industry Cooperative Research Program

Annual Meeting

May 24, 1991

## **BACKGROUND : PREVIOUS ANALYSIS**

- **Removal of PeoplExpress from the New York (EWR) market has had the most significant impact on traffic flows.**
- **Domestic connecting passengers have dropped in both absolute and percentage terms at all three airports, suggesting a shift by carriers away from New York airports as domestic hubs.**

### **Newark Airport (EWR)**

- **Stable departure levels since PE withdrawal, but fewer seats and reduced aircraft sizes.**
- **Major drop in on-board passengers after 1986-3; downward trend continues through 1989-3 for virtually all carriers.**
- **Local originating passengers cut by half when PE failed; levels have barely returned to pre-1984 levels.**
- **Domestic connecting passengers were similarly affected by PE withdrawal from EWR.**

# Total Seats Departed for Majors

All New York City Area Airports

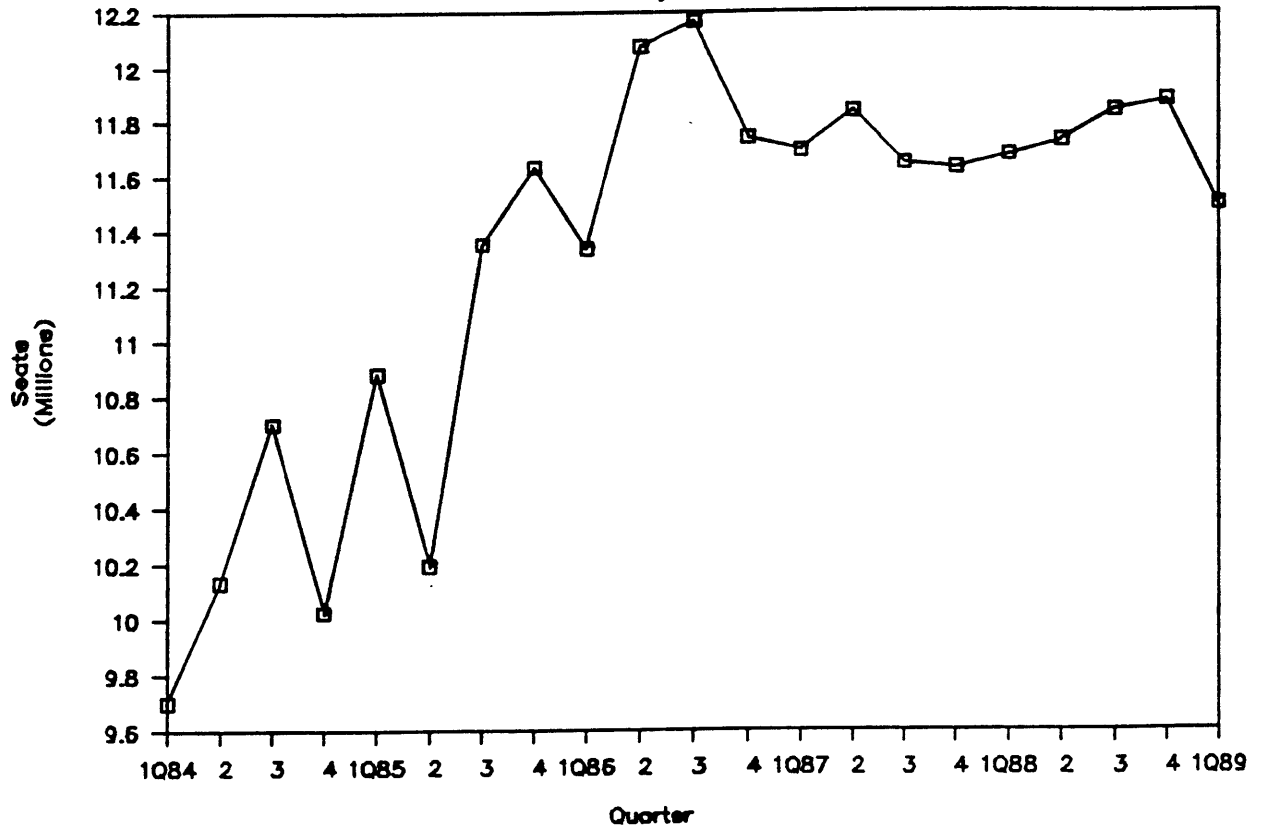


Figure 1.2

# Total Seats Departed for Majors (T9)

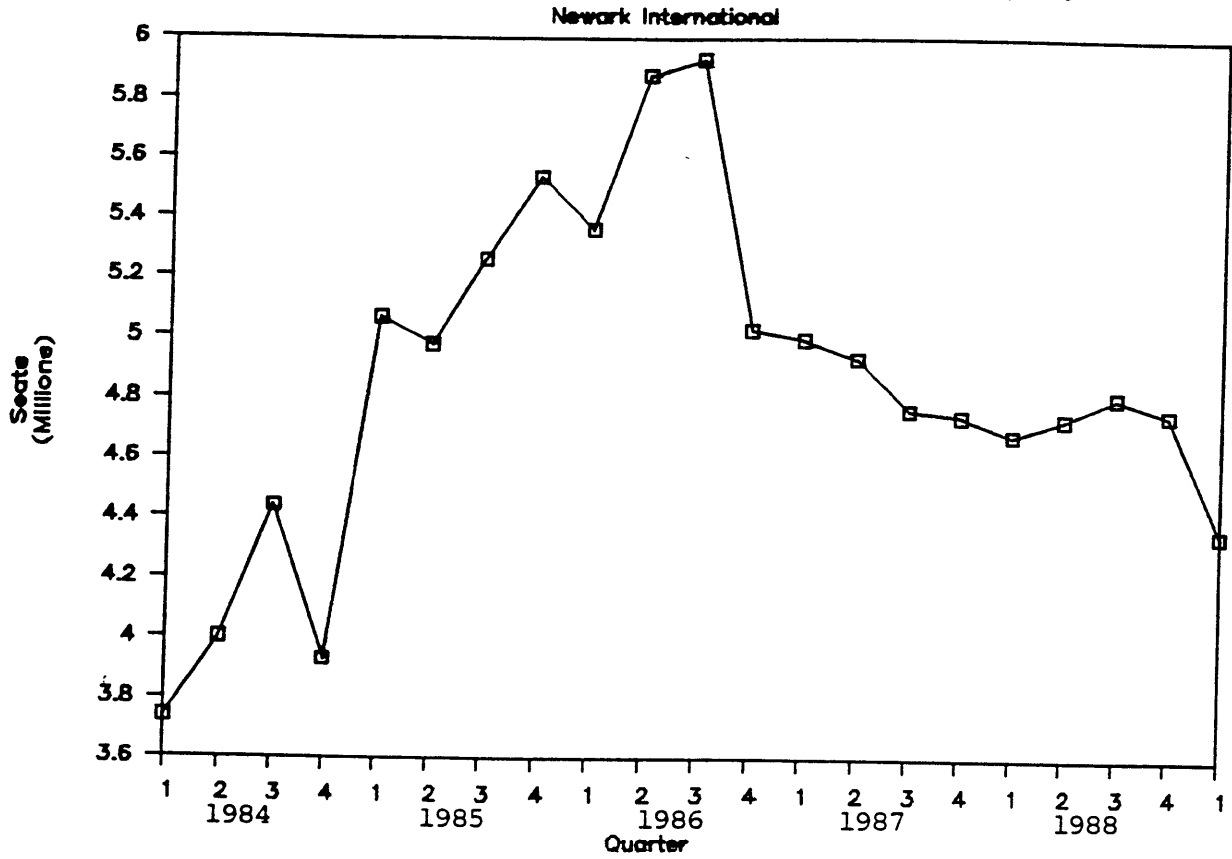


Figure 1.8

# Total Seats Departing

Newark International

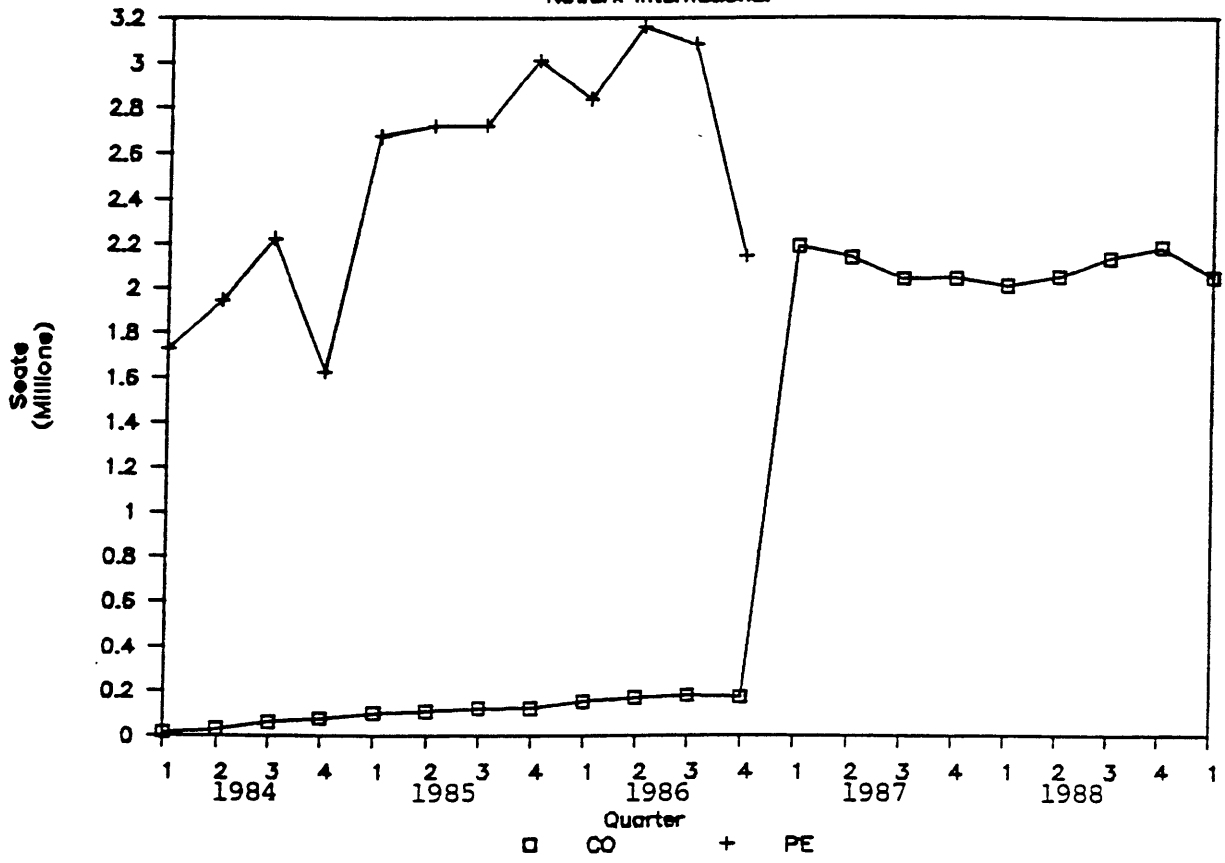


Figure 1.9

# Total Onboard Pax for Majors

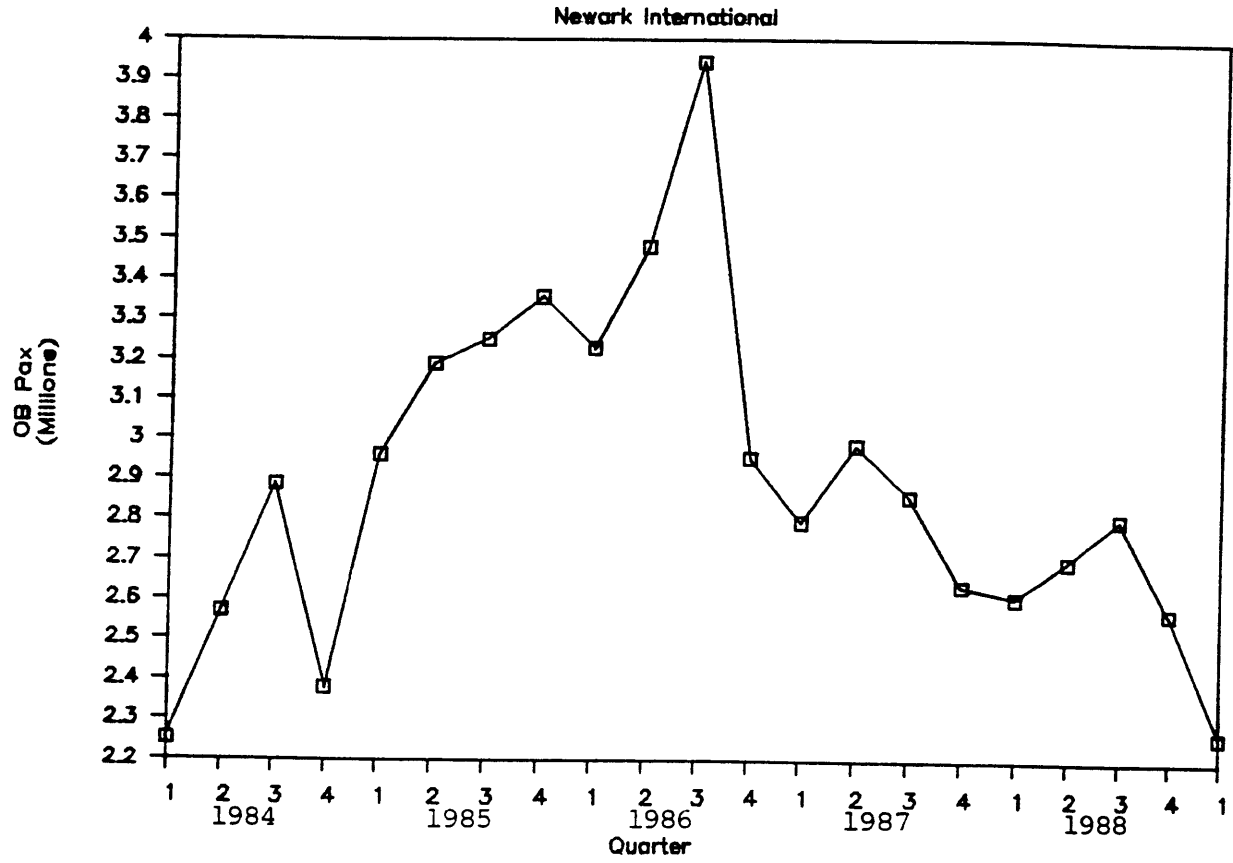


Figure 2.3



# Total Onboard Pax

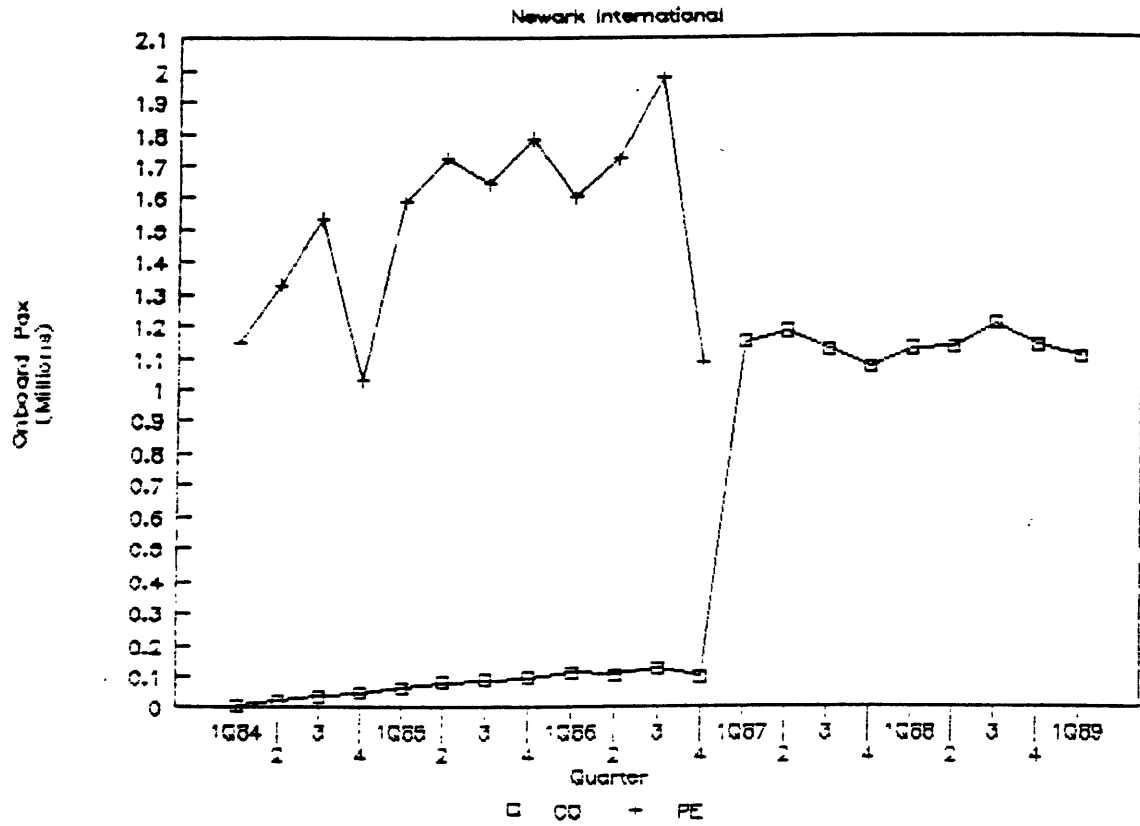


Figure 2.6

# Total Connecting Pax (EWR)

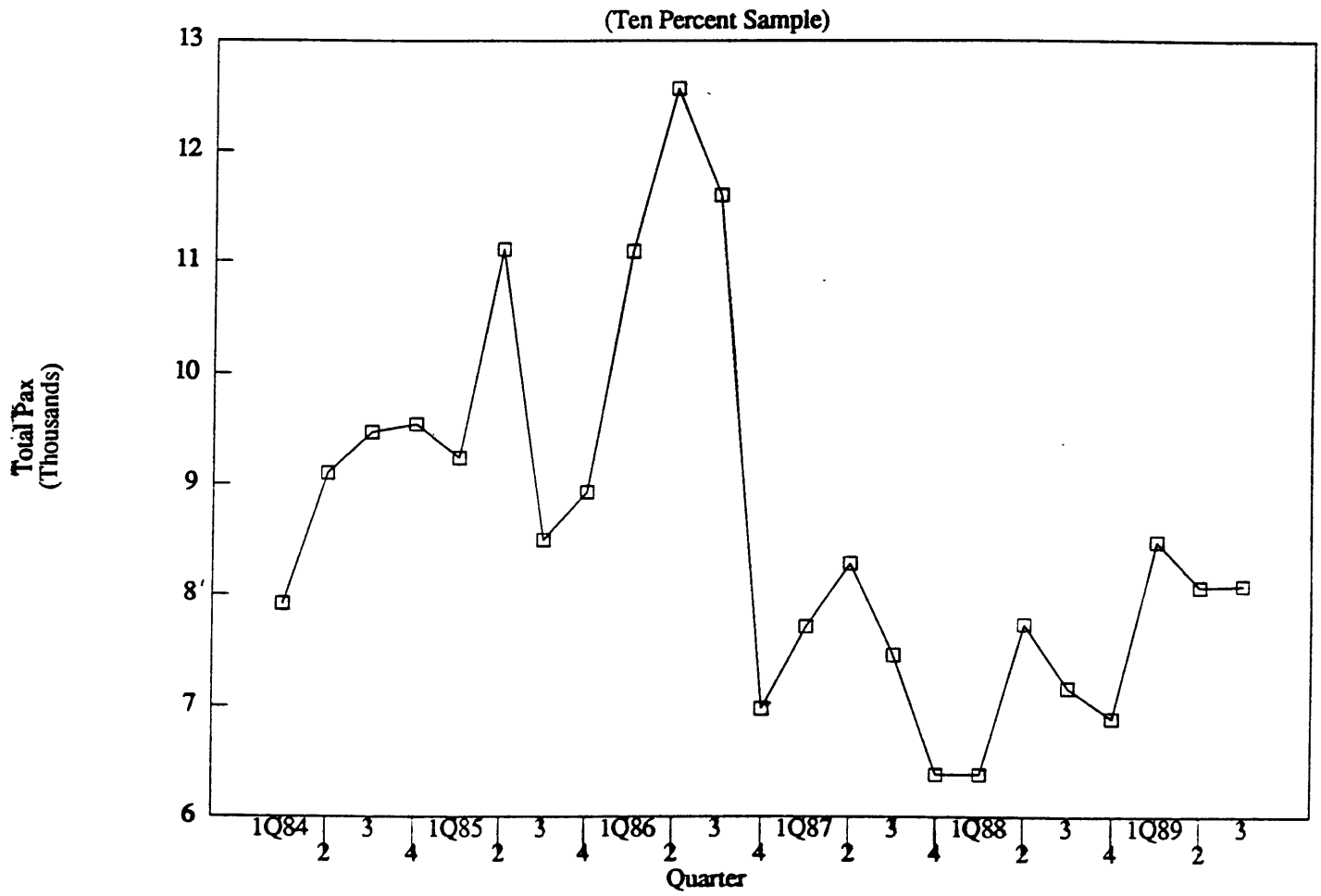


Figure 3.5

# Total Connecting Pax (EWR)

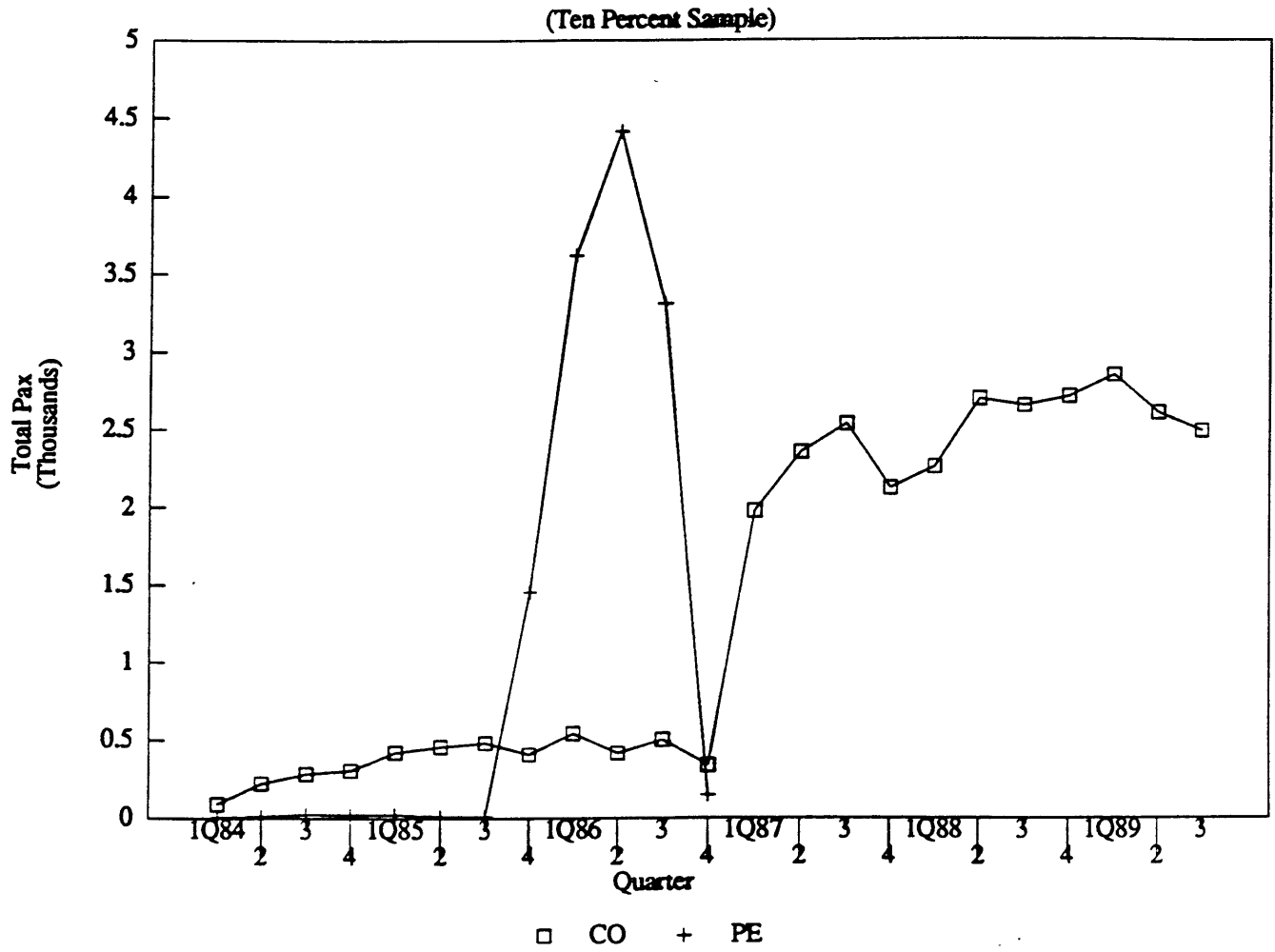


Figure 3.8

## NEWARK AIRPORT

### TRAFFIC FLOW ANALYSIS (Phase 2)

#### OBJECTIVE

- Identify and evaluate changes in O-D passenger traffic flow patterns through Newark (EWR) and alternative hub routings.
- Determine shifts in connecting traffic away from EWR in O-D markets previously served by PeoplExpress.

#### HISTORICAL DATA

- Ten percent ticket coupon sample provides passenger itinerary information by quarter from 1985 to 1989.
- Database Products Inc. "OD Plus" database used to extract data.
- Official Airline Guide (OAG), schedule data for each of the periods.

## **PASSENGER TRAFFIC FLOW ANALYSIS**

### **DEMAND AND SUPPLY MEASURES**

- Ten percent O-D passengers travelled between each selected city pair by carrier.
- Scheduled service in each city pair by carrier.

### **AIR CARRIERS**

- “Major” U.S. carriers offering service to domestic destinations, defined to include smaller airlines with large market presences (e.g. Midway).

## ANALYSIS METHODOLOGY

- **Obtained top 500 US Domestic O-D markets in terms of passenger traffic for 1989.**
- **Selected markets served by PeoplExpress in 1986.**
- **Discarded all city pairs with New York as an Origin/Destination, leaving 50 sample markets.**
- **Used O-D Plus to obtain passenger traffic data for 3rd quarter 1986 for all major carriers serving these city pairs.**
- **Selected O-D pairs based on market share and passenger information for detailed analysis :**
  - **markets with greater than 5% market share by PeoplExpress in 1986 or;**
  - **markets with more than 20 passengers carried by PeoplExpress per day.**
- **A total of 20 markets were chosen based on these criteria.**
- **Used O-D Plus again to obtain detailed passenger traffic information by individual market and carrier from 1985-3 to 1989-3.**

## 20 SELECTED O-D MARKETS

	<u>1986-3</u> <u>PE Share</u>	<u>1986-3</u> <u>Pax/Quarter</u>
CHI-BDL	3.30%	5440
ORL-CMH	2.25%	280
PIT-HOU	4.95%	3240
PIT-LAX	4.91%	1810
WAS-MIA	5.74%	7950
WAS-BUF	9.36%	3500
WAS-DEN	8.73%	7500
WAS-PVD	4.99%	1670
BOS-CHI	6.02%	11960
BOS-DFW	4.18%	2960
BOS-DET	2.36%	2120
BOS-FMY	5.16%	570
BOS-HOU	5.41%	2600
BOS-LAX	1.14%	1920
BOS-ORL	1.80%	2110
BOS-PIT	16.45%	9490
BOS-SFO	1.86%	2530
BOS-WAS	3.44%	9220
BOS-DEN	12.10%	9320
BWI-DEN	6.45%	1930

## **FINDINGS**

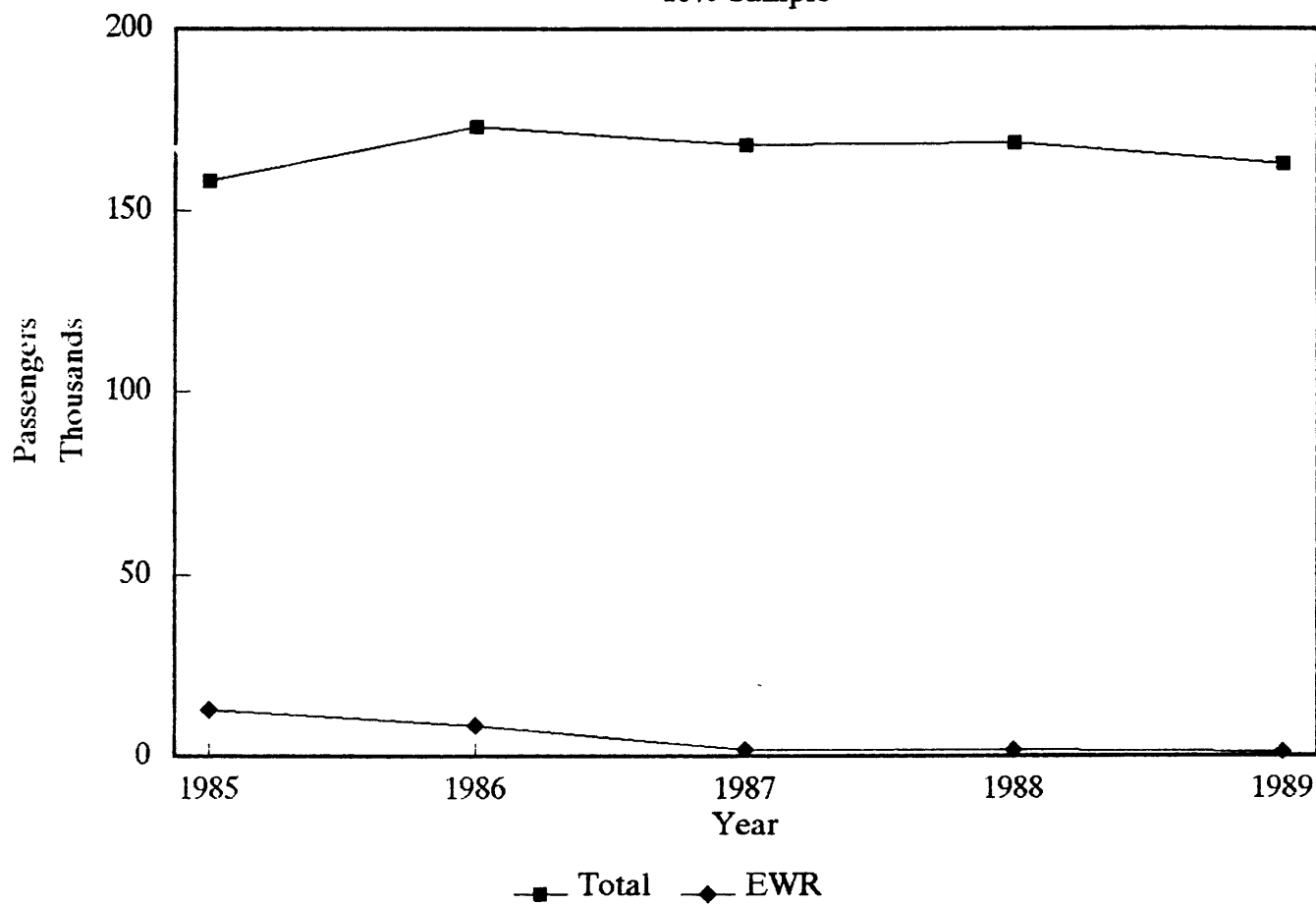
### **Aggregate : 20 O-D Markets**

- **Total traffic in selected O-D pairs decreased slightly since withdrawal of PeoplExpress in 1986-3.**
  - **aggregate traffic decreased by 5.94% from 1986-3 to 1989-3.**
- **However, proportion of this traffic connecting through EWR dropped from 4.84% to 0.71% during the same period.**
- **In 1985, PeoplExpress carried 8% of total traffic in these markets.**
- **By 1989, Continental carried a total of 10% of traffic in these markets.**
- **However, only 1% was carried by CO via EWR.**



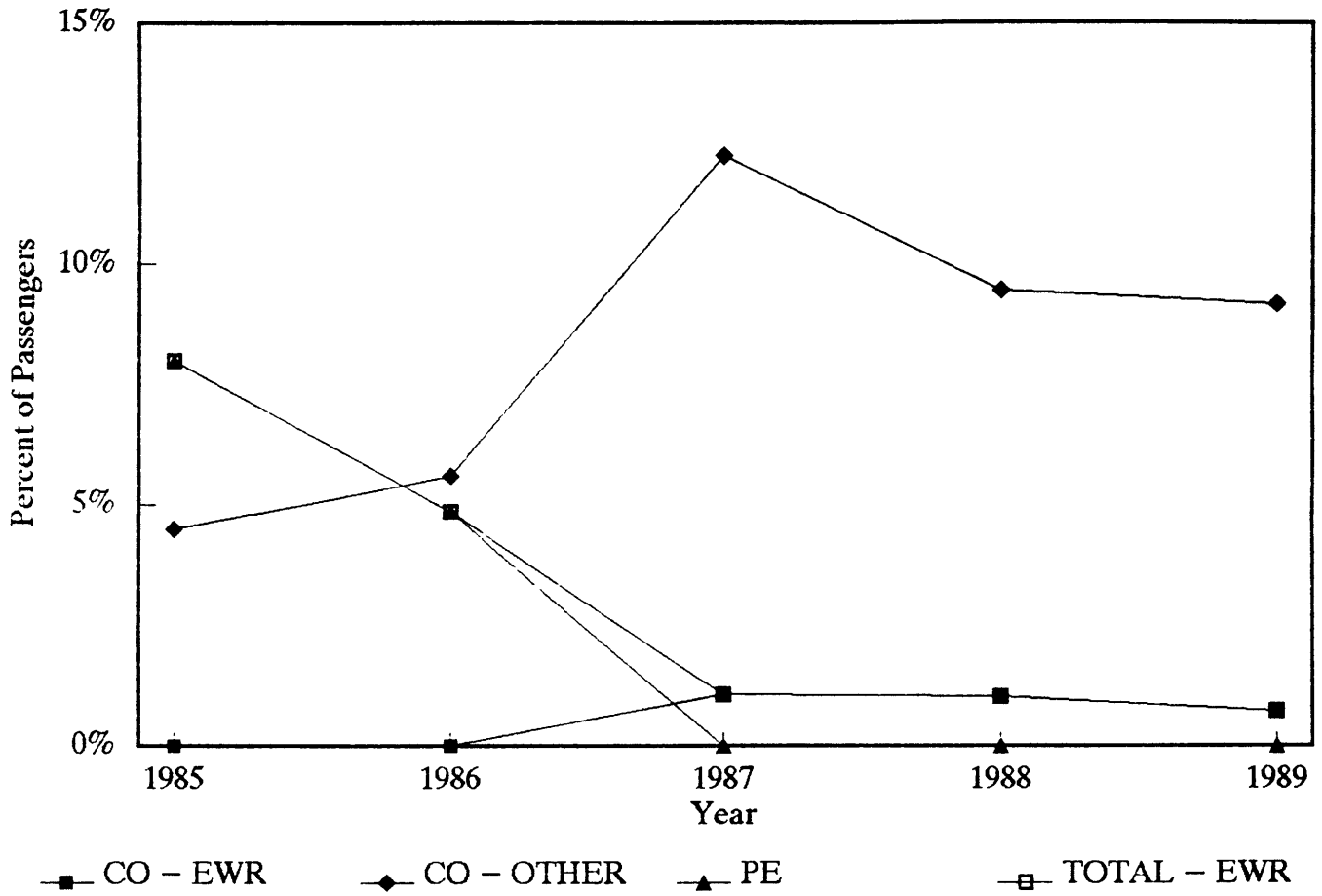
# Total Passengers for 20 Selected Market

10% Sample



# Total Market Share

20 Selected Markets



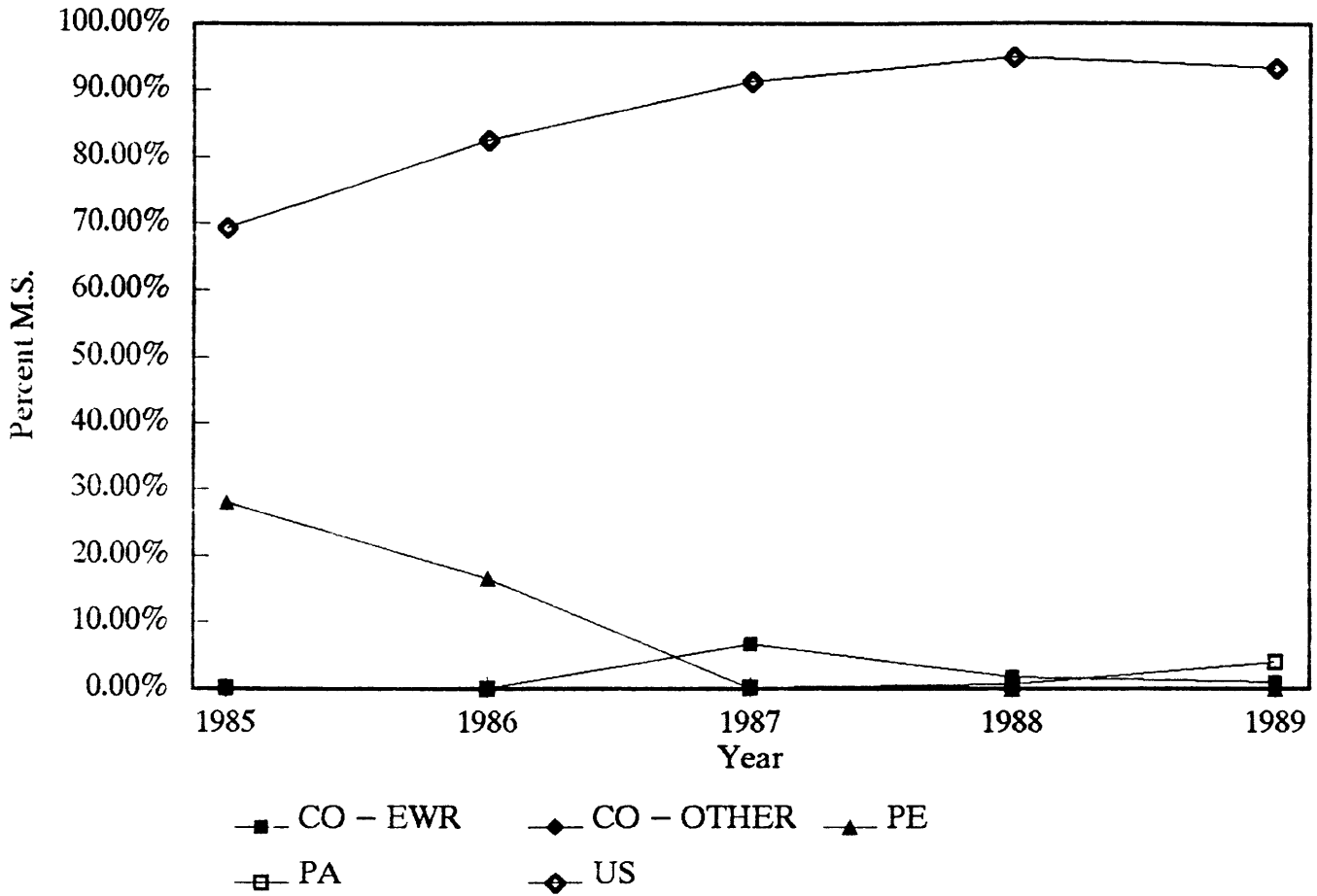
## Disaggregate Market Analysis

Examples of market share changes 1985 to 1989 follow, showing PE, CO and the two competing carriers with the greatest increase in market share :

- "CO - Other" refers to Continental traffic routed primarily through other CO hubs.

# Market Share Comparison

BOS - PIT

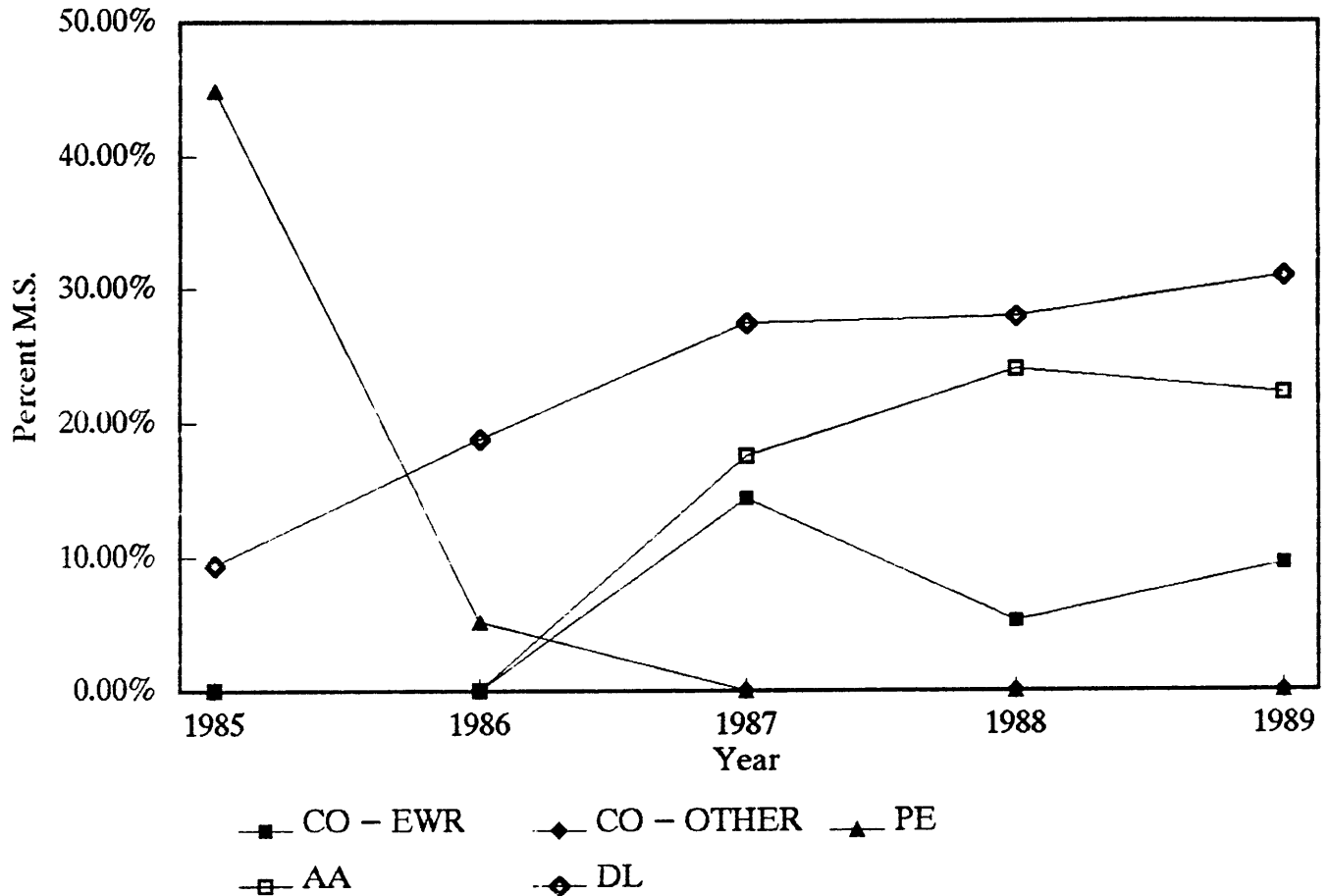


## BOS-PIT :

- PE had 28% market share in 1985, virtually all of which was taken over by USAir (non-stop service).
- CO never recaptured significant market share.

# Market Share Comparison

BOS - FMY

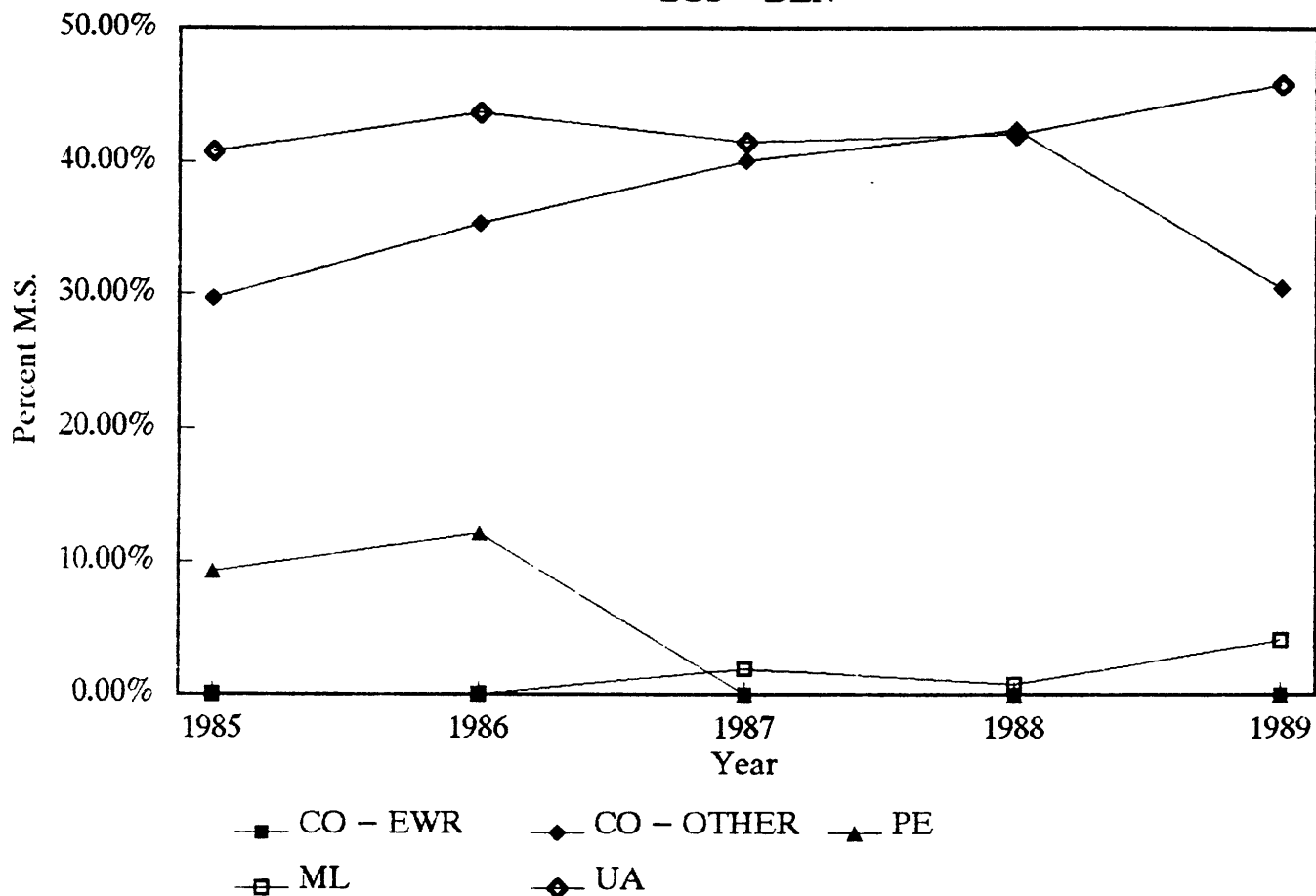


## BOS-FMY :

- PE had peak market share of 45% in 1985, of which CO now carries only 9% via EWR.
- AA market share grew from 0 to 24% (CNX via RDU).
- DL also took over market share (via ATL and CVG).

# Market Share Comparison

BOS - DEN

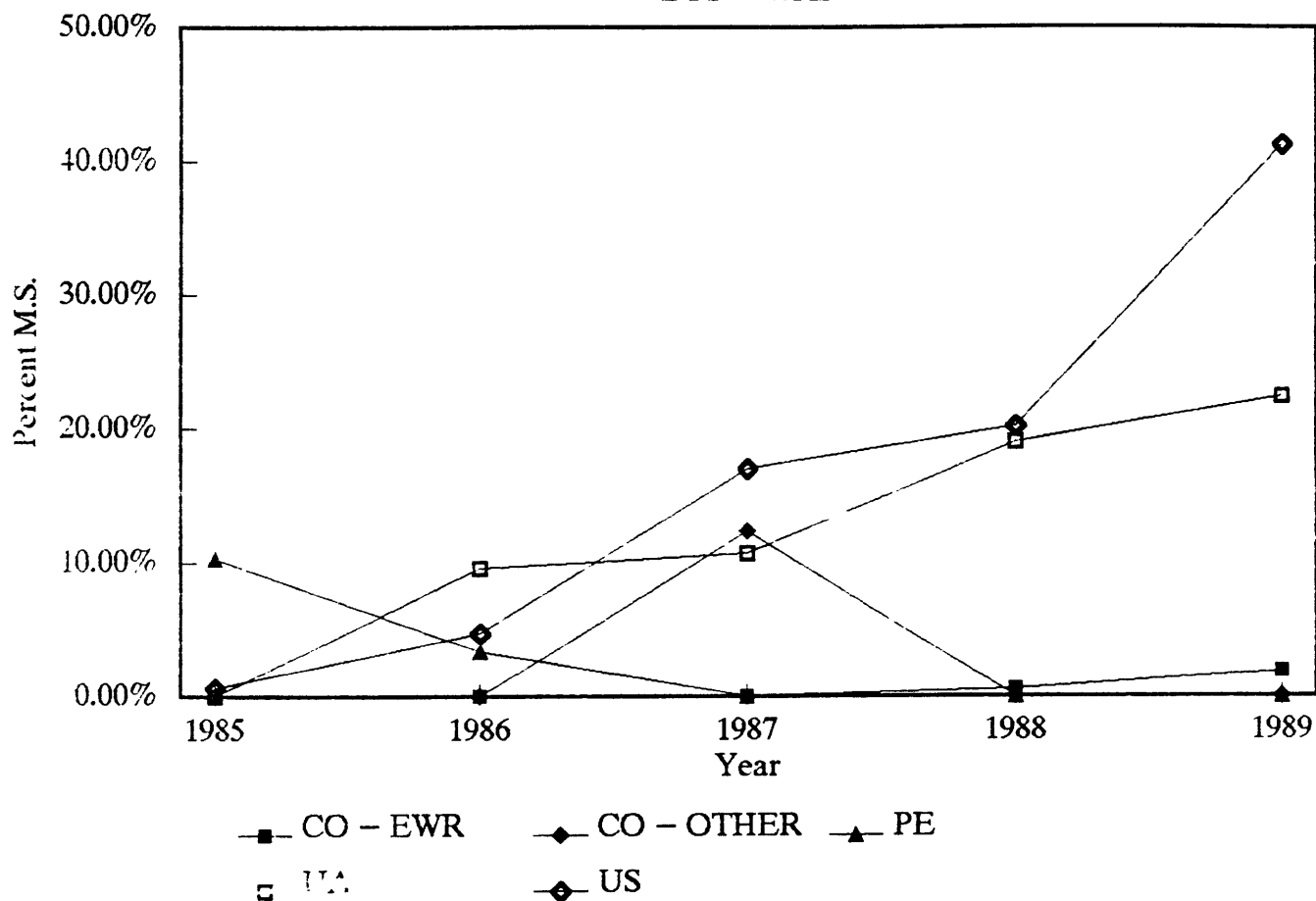


## BOS-DEN :

- CO has captured most of PE's 12% market share, but on non-stop service. UA also shows market share growth (non-stop service).

# Market Share Comparison

BOS - WAS

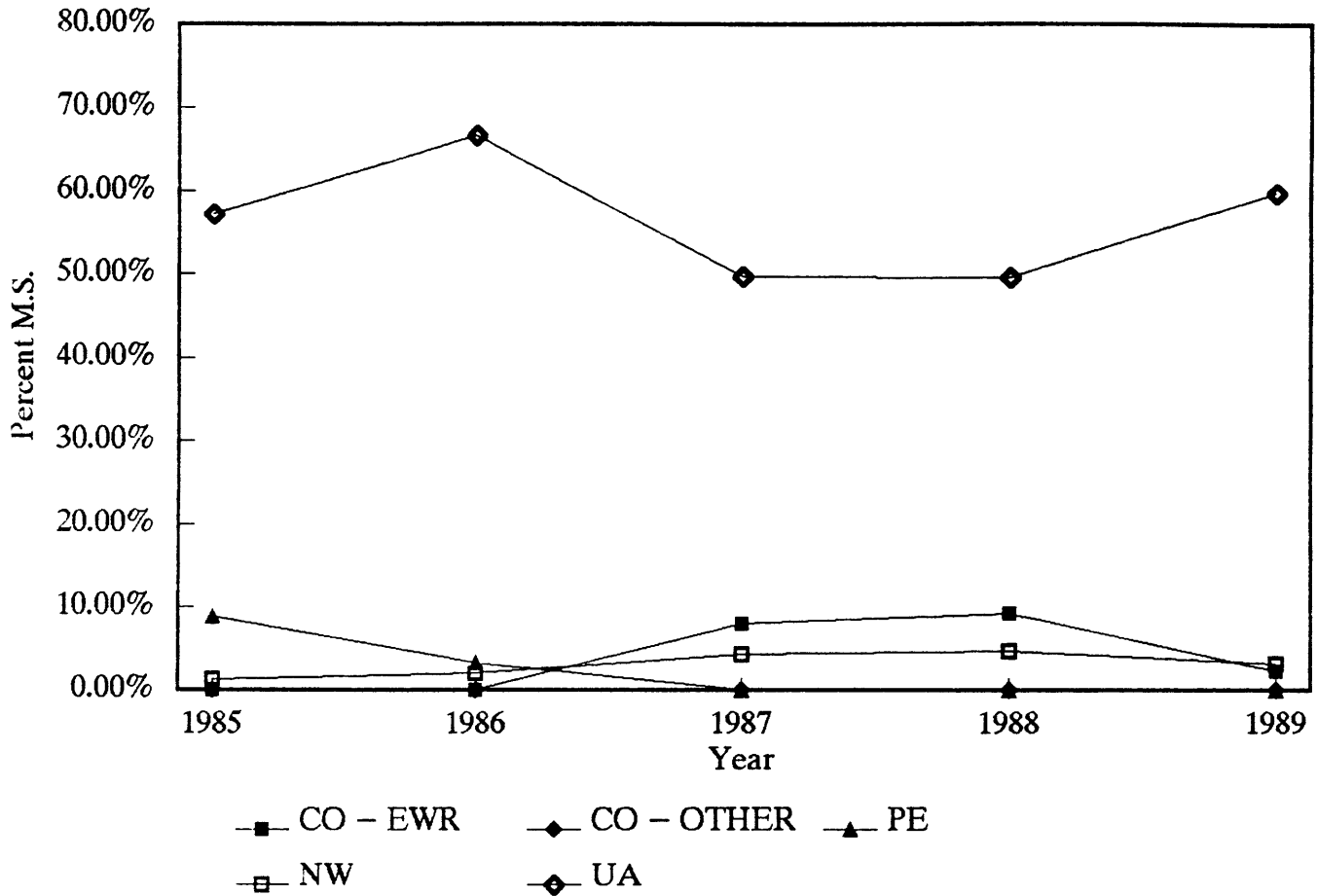


## BOS-WAS :

- PE had 10% market share in 1985. CO did not capture any of this traffic (via EWR), except in 1987 when CO offered non-stop service to IAD.
- Greatest MS growth by US and UA (both non-stop services).

# Market Share Comparison

CHI - BDL



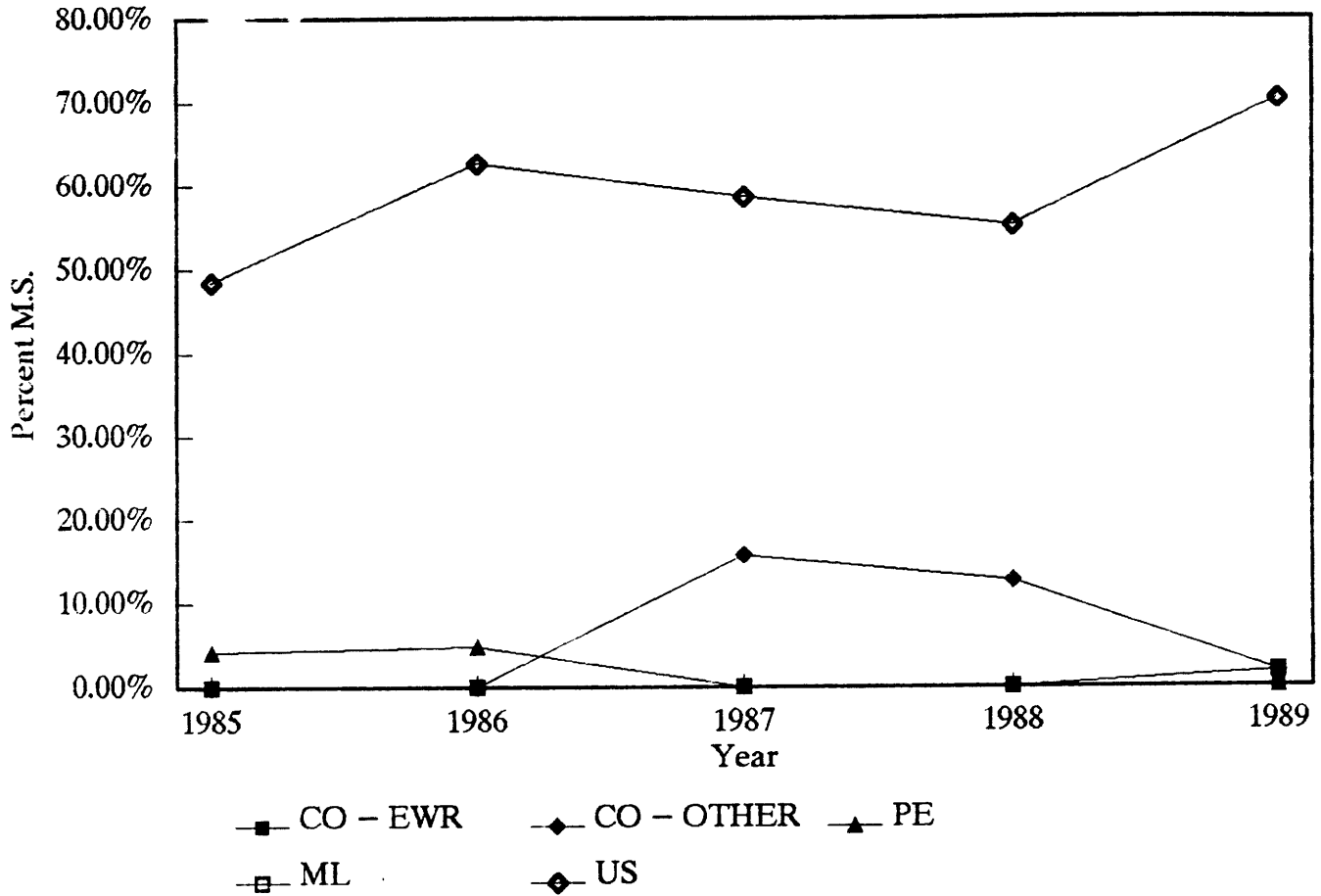
## CHI-BDL :

- PE's 9% market share in 1985 was captured by CO via EWR until 1988, when UA increased non-stop service.



# Market Share Comparison

PIT - LAX

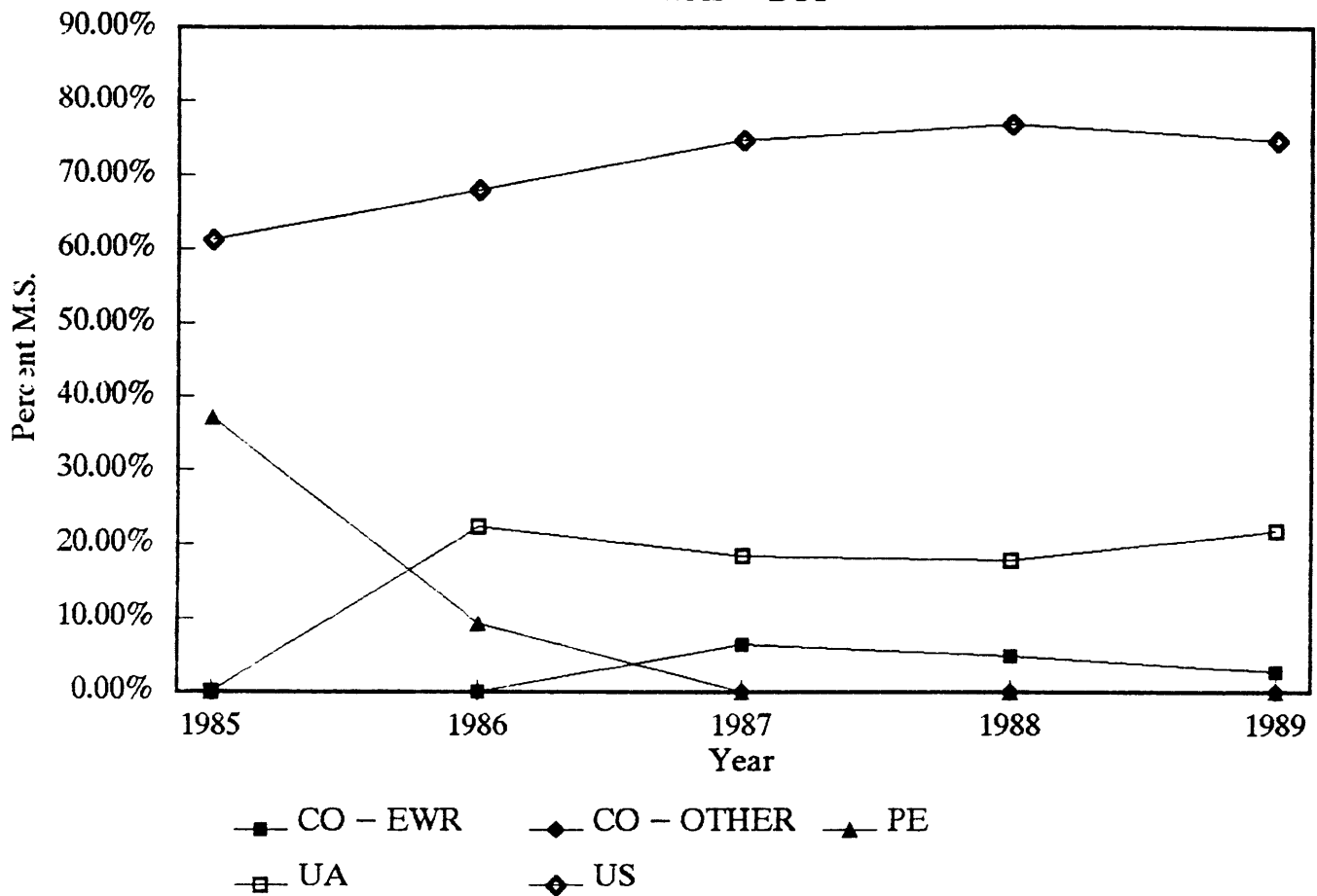


## PIT-LAX:

- PE carried up to 5% of market share in 1986 via EWR.
- CO increased its MS from 0 to 16% in 1987, but not via EWR (i.e. via IAH, DEN, CLE).

# Market Share Comparison

WAS - BUF

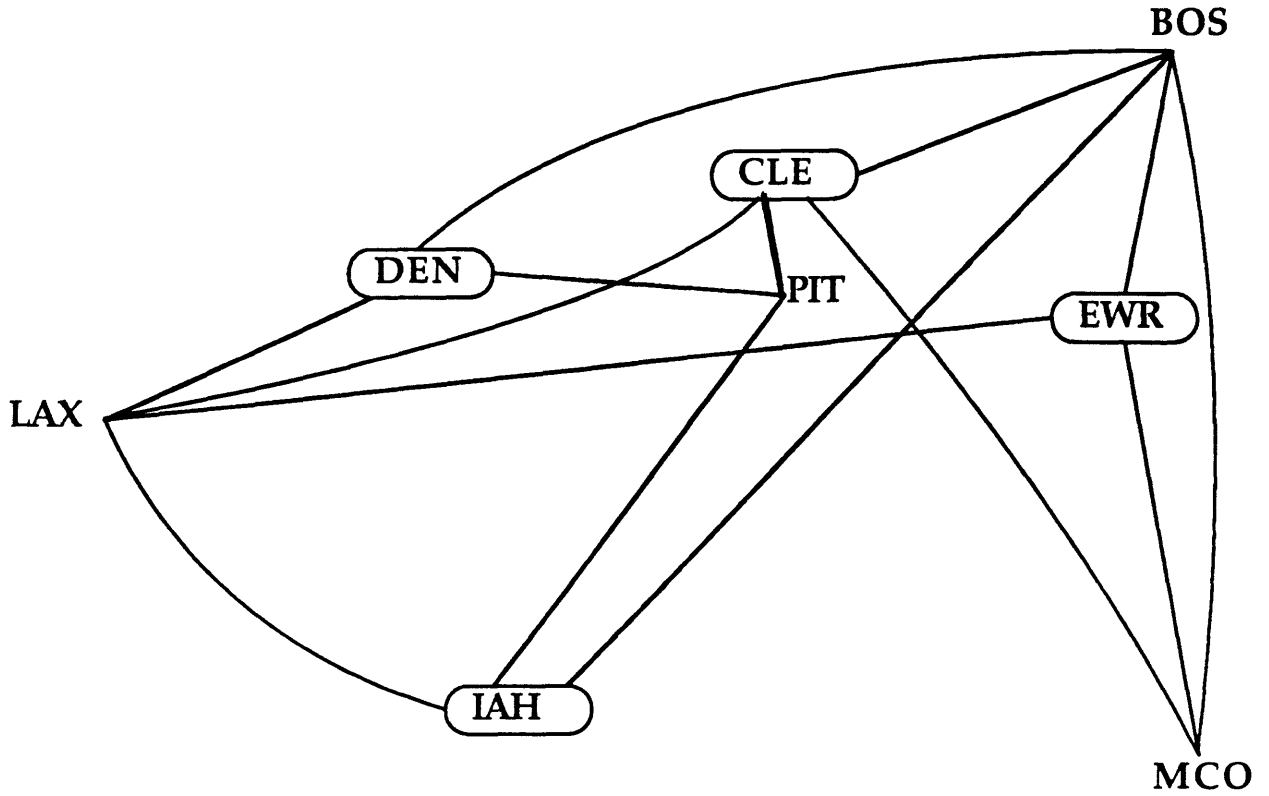


## WAS-BUF:

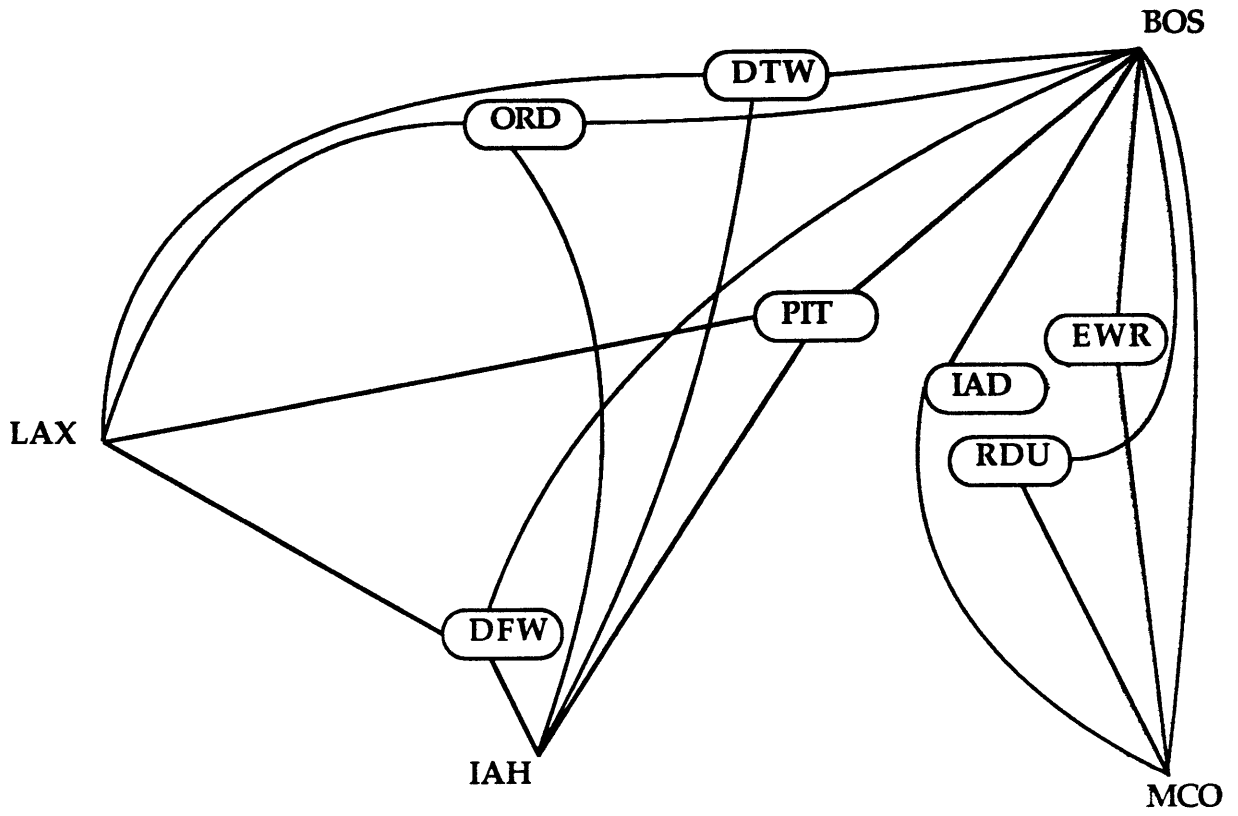
- PE carried 37% of market share in 1985, only 7% of which was captured by CO via EWR in 1987.
- Biggest market share gains went to UA (non-stop to IAD) and US (non-stop to BWI/DCA).

## **SUMMARY OF FINDINGS**

- **O-D routings with PeoplExpress in 1986 were almost exclusively through EWR, and PE had an average of 8% MS in 20 selected markets.**
- **After withdrawal of PeoplExpress from EWR :**
  - **CO became an effective competitor in many of these markets, but traffic was split between EWR, CLE, DEN, and IAH hubs.**
  - **Growth of alternative and new hubs operated by other carriers further reduced attractiveness of EWR connections.**



O-D Routings  
After PeoplExpress 1989  
(via Continental Airlines)



O-D Routings  
After PeoplExpress 1989  
(Other Carriers)

## **CONCLUSIONS**

- **Withdrawal of PeoplExpress has had significant negative impact on connecting traffic levels at Newark.**
- **Continental took over from PeoplExpress, and Newark (EWR) became one of the 4 hubs operated by Continental with CLE, DEN, IAH.**
- **CO now serves many O-D pairs through its alternative hubs, providing a bigger choice of departures and more direct routings.**
- **CO did not replace PE as a competitor, it replaced PE as the hub operator of EWR.**
- **Development of existing and new hubs by other carriers captured additional EWR market share.**

# Airline Seat Inventory Control For Group Passenger Demand

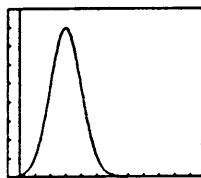
Presented by

Peter Belobaba  
Tom Svrcek

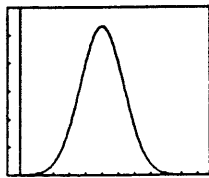
May 1991

## Individual Passenger Seat Inventory Control

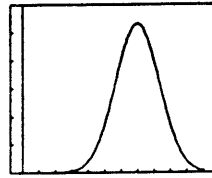
Assumes Demand For Each Individual Fare Class Is Independent And Normally Distributed.



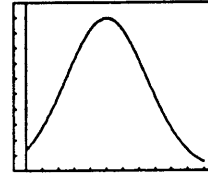
Y Class



B Class



M Class

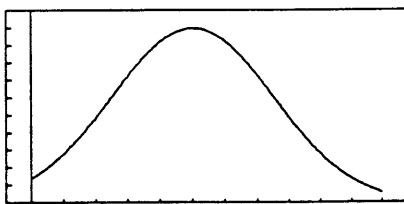


Q Class

### Definition

Expected Marginal Revenue (EMR) Of An Additional Seat Allocated To A Particular Fare Class Is

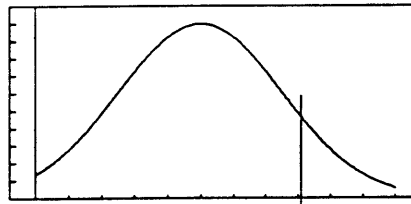
$$EMR(i) = \text{Fare Class Revenue} * \text{Probability of Selling Seat } i.$$



15

$$P(X > 0) = .999$$

$$EMR(1) = \$500$$



15

$$P(X > 25) = .05$$

$$EMR(26) = \$25$$



## Individual Passenger Seat Inventory Control

### Example : Setup

Total Fare Classes :	4
Aircraft Capacity :	100

<u>Fare Class</u>	<u>Demand Mean</u>	<u>Demand Stdev</u>	<u>Average Revenue</u>
Y	14	5	380
B	12	6	320
M	35	10	270
Q	42	12	220

# Individual Passenger Seat Inventory Control

## Results

Seat No.	Y	B	M	Q	Highest EMR
1	378.94	312.78	269.90	219.92	378.94
2	378.16	309.39	269.87	219.90	378.16
3	376.86	304.77	269.82	219.87	376.86
4	374.74	298.65	269.76	219.83	374.74
5	371.43	290.79	269.68	219.78	371.43
6	366.43	280.99	269.57	219.73	366.43
7	359.24	269.16	269.43	219.65	359.24
8	349.31	255.22	269.25	219.56	349.31
9	336.20	239.24	269.00	219.44	336.20
10	319.63	221.34	268.69	219.30	319.63
11	299.47	201.81	268.29	219.19	312.78
12	275.85	181.12	267.77	218.89	309.39
13	249.13	160.00	267.10	218.61	304.77
14	220.07	138.88	266.26	218.26	299.47
15	190.00	118.19	265.21	217.83	298.65
16	159.93	98.66	263.91	217.32	290.79

...

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...

...

Fare Class Allocations	
Y	16
B	13
M	34
Q	37

.
.
.
158.48
156.37
152.17

## Group Passenger Demand

### Why Is Group Demand Different From Individual Passenger Demand ?

- Group Demand Is Realized Many Months In Advance  
Examples : Rose Bowl, Mardi Gras ...
  
- Groups Negotiate For A Lower Fare  
(Bulk Pricing)
  
- Unused Bookings Are Absent From Seat Inventory For Months,  
Potentially Displacing Individual Passengers
  
- Cancellation Penalties Often Difficult To Enforce  
Due To Competitive Environment

## Problem Statement

Given We Receive A Request For A Group Request Of Size S For A Specific Origin/Destination And Date.

What Is The Minimum Group Fare An Airline Should Charge Given That We May Potentially Displace S Individual Passengers ?

"Answer:"

$$\text{Min. Group Fare} = \frac{\text{Total Expected Revenue Of Displaced Individual Pax}}{\text{Size Of Group Request}}$$

$$\text{Example: } \frac{\$ 2,200}{20} = \$ 110 \text{ Per Group Pax}$$

## Group Passenger Seat Inventory Control

### Two Solution Methodologies

#### Case 1:

Assume Group Is Indivisible. Find The Itinerary With The Smallest Displacement Cost Of Individual Passengers.

#### Case 2:

Relax Indivisibility Constraint. Find Optimal Split Over N Possible Alternatives For Each Group Request.

## Group Passenger Seat Inventory Control

Large Hub and Spoke Networks Operated by Today's Major Carriers Allow for Several Different Routings (with Similar Departure and Arrival Times) For Many Origin – Destination Pairs.

For Example, Delta Air Lines Service Between:

New York (EWR/LGA/JFK) and Seattle (SEA)

Dept	Arr	Flts	Stps/Via
5:20aE	11:35a	377 / 835	ATL
7:05aJ	12:30p	1429 / 1655	SLC
8:15aL	1:45p	467 / 233	DFW
8:20aE	1:45p	281 / 233	DFW
9:30aL	2:45p	937 / 623	CVG
9:50aE	2:45p	583 / 623	CVG
11:00aJ	8:23p	1601 / 301	MCO
11:29aL	5:10p	983 / 833	DFW
11:55aE	5:10p	887 / 833	DFW
3:29pL	8:25p	1187 / 367	CVG
3:29pL	10:40p	1187	2
4:15pE	8:25p	1038 / 367	CVG
5:10pE	12:25a	237 / 300	LAX
5:20pJ	10:40p	1425 / 1187	SLC
6:45pL	1:33a	729 / 625	ATL
6:50pE	1:33a	1421 / 625	SLC

## Group Passenger Seat Inventory Control

### Numerical Example : Setup

Dept Date : 12 JUL 91
Group Size : 15

### Possible Outbound Itineraries

1) 

DL	583	EWR	950A	CVG	1142A	72S
DL	623		108P	SEA	245P	72S

2) 

DL	99	EWR	340P	ATL	640P	757
DL	197		652P	SEA	910P	757

3) 

DL	887	EWR	1155A	DFW	226P	72S
DL	833		312P	SEA	510P	72S

4) 

DL	281	EWR	820A	DFW	1055A	72S
DL	233		1152A	SEA	145P	72S

Published Fares for EWR/SEA on 12 JUL 91		
---	--	--

Y	\$642.00	O/W
---	----------	-----

B	\$425.00	O/W
---	----------	-----

M	\$325.50	O/W
---	----------	-----

Q	\$277.00	O/W
---	----------	-----

## Group Passenger Seat Inventory Control

### Numerical Example: Results

#### Itinerary #1

<u>Seat</u>	<u>Flt 583</u>	<u>Flt 623</u>	<u>Itin #1</u>
134	24.40	97.20	121.60
135	24.24	93.80	118.04
136	24.21	93.10	117.31
137	21.59	92.99	114.58
138	20.83	88.88	109.71
139	19.53	83.76	103.29
140	19.41	83.51	102.92
141	19.25	81.42	100.67
142	17.72	78.50	96.22
143	16.21	77.91	94.12
144	14.99	77.55	92.54
145	14.92	74.68	89.60
146	12.58	74.19	86.77
147	12.42	73.15	85.57
148	11.79	67.81	79.60
149	11.51	66.82	78.33
150	10.23	65.29	75.52
	Leg 1	Leg 2	Total

Min. Group Fare Calculation =>  $1426.75 / 15 = \$95.12$



## Group Passenger Seat Inventory Control

### Group Booking Model Output

Rank	Itin <u>Out</u>	Displacement Cost Estimate Per Passenger		Total	Min. Group Fare	Request for <u>15 Pax</u>
		<u>Leg 1</u>	<u>Leg 2</u>			
1	4)	0.00	87.80	87.80		\$87.80
2	1)	16.48	78.64	95.12		\$95.12
3	3)	0.00	137.93	137.93		\$137.93
4	2)	79.38	157.13	236.51		\$236.51

Lowest Published Fare for EWR/SEA on 12JUL91 :	\$277.00
Minimum Group Fare :	\$87.80

Negotiation Does The Rest !

## Group Passenger Seat Inventory Control

### What Is The Optimal Reduced Fare ?

For The Carrier:

\$277.00

For The Group:

\$87.80

### Competitive Advantage

Carrier Implementing Displacement Cost Strategy Has

$$\$277.00 - \$87.80 = \$189.20$$

Of "Competitive Leverage".

## Group Passenger Seat Inventory Control

### Case 2: Relaxation Of Indivisible Group Constraint

Group Seat	<u>Itin 1</u>	<u>Itin 2</u>	<u>Itin 3</u>	<u>Itin 4</u>
15	117.31	259.11	139.99	104.97
14	114.58	255.68	139.97	102.82
13	109.71	247.17	139.95	99.52
12	103.29	246.32	139.92	96.09
11	102.92	245.43	139.85	92.52
10	100.67	244.42	139.73	88.85
9	96.22	234.76	139.52	86.32
8	94.12	232.73	139.16	85.08
7	92.54	230.30	138.55	84.85
6	89.60	228.77	138.44	84.46
5	86.77	226.53	137.59	82.47
4	85.57	226.22	136.08	81.23
3	79.60	224.97	135.31	77.34
2	78.33	224.46	133.84	77.05
1	75.52	220.83	131.09	73.42

### Model Output

<u>Optimal Split Over All Itineraries</u>	
Itinerary 1	5 Pax
Itinerary 4	10 Pax
Minimum Group Fare (Divided)	<u>\$81.79</u>
Minimum Group Fare (Undivided)	<u>\$87.80</u>

## Group Passenger Seat Inventory Control

### Question:

Why Are Groups Different From Traditional Bulk Pricing ?

### Answer:

In Bulk Pricing, Marginal Cost Of Each Additional Item Is Non-Increasing.

### Example:

6 Bagels at \$ 0.40 / item 24 Bagels at \$ 0.30 / item
---

### But:

6 group pax at \$ 175.00 / pax 24 group pax at \$ 189.00 / pax
---

Each Additional Passenger We Displace Has A Higher Expected Marginal Revenue Than The Previous One.

The Larger The Group, The Higher The Average Fare

## Group Passenger Seat Inventory Control

### User Optimal Strategy

- Be Flexible In Times / Dates
- Be Willing To Split Up
- Book Only As Many Seats As You Need

### Carrier Optimal Strategy

- Find "Minimum Displacement" Seats For Each Requested Itinerary
- Try To "Split" Groups When Possible
- Book Only "Genuine" Seats

## Conclusions

- Minimum Group Fare Based On Displacement Of Individual Passengers
- No Distribution Assumptions Necessary For Group Passenger Demand
- Given N Outbound Itineraries And R Return Itineraries, We Can Find The Best Of  $N * R$  Possible Combinations
- Optimal Mix Of Divisible Group is No More "Difficult". All Necessary Information Exists !
- Better Utilization Of Excess Capacity Means Greater Revenue Potential For Airlines

# Airline Crew Scheduling Re-visited

Presentation at the  
MIT/FTL -Industry Cooperative Research Program Review  
May 23 /24, 1991

Professor Robert W. Simpson

## Problem Statement

### GIVEN:

1. A fixed schedule of flights  $F$  for one type of aircraft
  - a flight is one or more flight legs
  - arrival / departure times are fixed
  - schedule is cyclic over a day or week,  $C$
  - schedule remains in effect over planning horizon,  $H$
  
2. A set of crew bases  $B$  where a number of crews  $N_B$  are domiciled to fly this type of aircraft

### FIND:

the cheapest set of work schedules, or "bidlines"  $b$  for these crews during  $H$  which does not violate work rules imposed by regulations or airline/union agreements;

- a crew trip  $t$  consists of a series of flights to be flown starting from base and returning within one or more days
  
- a work schedule  $b$  is a set of trips away from base on various days of the planning horizon,  $H$



## Typical Crew Work Rules - 1

### 1. Regulatory Rules

(imposed by civil aviation authorities for safety)

- Maximum Daily Flight Hours
- Maximum Weekly (or 7 day period) Flight Hours
- Maximum Monthly Flight Hours
- Maximum Duty Hours ( duty time is time without rest)
- Minimum Off-Duty Interval

Note- Crew trips and bidlines which conform to these rules will be called legal or feasible.

These rules limit crew utilization to be substantially less than that expected by airlines from their aircraft, and mean that crews and aircraft cannot remain together during trips away from base. It is desirable to estimate the minimum number of crews required to cover one cycle of a given schedule as it would give a lower bound on the number of crew trips which must be generated. It is easy to compute the maximum number of airborne crews, but due to these constraints it is less than the minimum required crews.

Due to the aircraft flying perhaps 18 hours per day, and a daily duty limit of 12 or 14 hours, some crews must start their duty in the middle of the day to cover late night flights. Due to the minimum off-duty interval of 8-10 hours, crews on late night flights cannot start flying on the earliest flights the next morning

## Basis for Crew Costs

There are two kinds of crews: cockpit and cabin.

The cockpit crew flies together for one month, paired differently each month. Each aircraft requires a fixed crew.

The cabin crew complement has a minimum, but higher loads causes more members on certain legs. Changing reservation information can change work schedules dynamically.

There are three components which determine the monthly pay of crew members at a US Airline:

1. Monthly Base Pay - independent of hours flown  
- depends on grade and longevity
2. Hourly Flight Pay - \$ per flight hour  
- depends on aircraft type
3. Trip Credit Pay - \$ per trip away from base  
- depends on details of trip itinerary  
- may be zero
4. Overnight Costs - costs of meals, food, and transport  
to overnight crew away from base

## Typical Crew Work Rules - 2

### 2. Airline/Union Trip Agreements

- Daily Flight Guarantee (eg. min. hours if called to duty)
- Flight/Duty Ratio Guarantee (eg. flight/duty time  $> 0.5$ )
- Flight/ Trip Ratio Guarantee (eg. flight/trip time  $> 0.25$ )
- Maximum No. of Daily Landings
- Deadhead Time is Flight Time

Note- These rules may cause a "penalty" to the airline in the form of extra pay and hourly credit to be assigned to a particular crew trip if it violates them. The total flight hours paid in a crew schedule may exceed the number of hours flown in the aircraft schedule.

Deadheading is flying the crew as passengers to/from base to other stations where their flying begins or ends.

## Typical Crew Work Rules - 3

### 3. Airline/Union Bidline Agreements

- Max. Monthly Flight Hours
- Min. Monthly Flight Hours
- Min. Days Off per month
- Min. Weekends Off per Month
- Max. Duty Hours per Week
- Min. Off Duty Time at Base
- Max. Percentage for Reserve Crew Bidlines

These rules affect the monthly pattern of work for crews but generally do not cause extra costs. Whereas an aircraft may fly 300 hours per month, crews are limited to less than 100, so there are 3-5 times as many crews as aircraft.

Note- Due to schedule deviations caused by weather, crew sickness, or aircraft equipment failures, reserve crews are given bidlines which mainly consist of periods when they are "On-Call" and must be able to report for duty within 1 or 2 hours. There may be a few flights actually scheduled into a reserve bidline, caused perhaps by holidays or schedule changes.

## **The Current Airline Crew Scheduling Process**

**Stage 1. - Generation of Feasible Crew Trips from Bases**

**Stage 2. - Selection of "Optimal" Trips from Bases**

**Stage 3. - Construction of Crew Bidlines for Bases**

**Stage 4. - Construction of Reserve Crew Bidlines for Bases**

**Stage 5. - Execution of Crew Bidding Process**

- Note: 1. It is a sequential, heuristic Process and is not optimal, even if some of the stages are done optimally.
2. There should be some feedback of crew scheduling problems into the aircraft scheduling and airline market service planning. At present, this feedback does not exist since crew scheduling is done by airline flight operations personnel late in the airline schedule planning process. There is a need for some early assessment of crew scheduling problems in airline schedule development.
  3. The availability and continual use of reserve crews affects the desirability of detailed optimal planning of fixed monthly bidlines.
  4. A related process is crew re-scheduling by flight operations personnel when deviations from schedule plan are occurring. There is a need for good methods of solving real time, operational crew scheduling problems to minimize additional costs from disruptions.

## Stage 1 - Generate Feasible Crew Trips

### STEP 1 - Establish "Flights", F

For various reasons, it may be desirable to have an unbroken sequence of flights or flight legs; ie., there may be some arbitrary specification of where crew connections can be made. Even though their flight number may change for marketing reasons, here these sequences will be called flights,  $f$ , belonging to a set  $F$ . Every crew trip  $t$  will now consist of a sequence of these flights.

### STEP 2 - Generate feasible (or legal) Crew "Trips", T

Since there are a number of necessary and desirable attributes for a crew trip, it is necessary to generate each trip individually. It is not possible to create a crew "circulation flow". The number of feasible crew trips may be of the order of a million for a typical US domestic fleet of 100 aircraft, and in the next step, (the selection of the best trips to "cover" the schedule), the solution may only involve a set of trips of the order of twice the number of aircraft in the fleet, ie., we are looking for the best 200 crew trips. Furthermore, there may not be much difference between the top 1000 solutions. It is desirable to find some "efficient" way to generate only the "best trips" as top candidates for a "cover" or solution.

Thus, it is vital to find some new way to generate trips which:

- 1) have zero trip penalty costs and good crew utilization
- 2) start from a given crew base after a specified start time
- 3) involve a specified flight or combination of flights
- 4) overnight at a specified location

## Stage 2 - Select a Set of Crew Trips for each Base

1. All flights in the aircraft schedule must be covered by the selected set of crew trips.
2. Since each trip starts at a given crew base, the flying assigned to that crew base by selecting a set of trips must be proportional to the number of crews domiciled at that base.
3. The Selection Problem takes two mathematical forms:

a) The Set Covering Version;

$$\text{Minimize } [C.T] \text{ given constraints } \begin{bmatrix} E.T \geq 1 \\ H.T \geq B \end{bmatrix}$$

where E is a zero-one matrix where columns j correspond to possible trips, and have a one in rows if the trip uses the flight corresponding to that row

where H is a matrix of flight hours per trip, and B is the total number of flight hours desired to be assigned to a crew base corresponding to that row

where T is a zero-one row variable to select trip j such as to minimize costs

Since the constraints allow the row sum to be greater than unity, deadheading is allowed and the costs include all components.

b) The Set Partitioning Version;

In this form, no deadheading is allowed and the constraints are equalities. The costs may be reduced to only the penalty costs associated with the guarantees.

### Example of Trip Selection

Trips, $t_j$		0 1 1 0 1 1 0 0 0									
		$c_1$	$c_2$	$c_3$	$c_4$	$c_5$	$c_6$	$c_7$	$c_8$	$c_9$	..... = Cost = $c_2 + c_3 + c_5 + c_6$
Flights, $f_i$	$f_1$	0	0	0	0	0	1	0	1	0	..... = 1
	$f_2$	0	1								..... = 1
	$f_3$	1	0	1				1			..... = 1
	$f_4$	0	0	0	1	0	1	0	1	0	..... = 1
	$f_5$	0	0	0	1	0	1	0	0	0	..... = 1
	$f_6$	1	0			1					..... = 1
	$f_7$	0	1	0	1					1	..... = 1
	$f_8$	0	1	0				1	0		..... = 1
Bases, $B$	a		5		8		6		7	8	..... > 10
	b			7		4				6	..... < 15
	c	6						6			..... < 5

Cheapest solution to this Set Partitioning Problem is the set of trips (2,3,5,6)

With a large number of rows and columns, this problem is very difficult to solve exactly. With a few hundred rows and columns, there are a number of interesting ways to get solutions. If the lowest cost columns can be produced easily, and the lowest cost column which provides needed cover could be generated, good solutions may be found quite quickly.

The trip characteristics which are desirable depend on the bidline constraints and the number of crew available. It might seem important to generate trips which do as much flying as legally possible in a duty period, but this would just mean more days off per month for each crew. It is always important to avoid incurring penalties from the guarantees.



## The Crew Tree - A New Method for Constructing Crew Trips

It is possible to create methods which generate any crew trip from a given base and evaluate it for feasibility and cost. Such methods may be controllable by the analyst in creating new trips with particular characteristics which can be added to the cover matrix as desired to obtain better solutions.

An efficient method of finding "best" crew trips from a base is to create a labelling method which constructs a "crew tree" on the Schedule Map for the aircraft. This tree is rooted in the departures from that base, and finds the best crew routing for any flight in the schedule if it were to be flown by a crew from that base. The definition of "best" can be varied but maximizing the flight time achieved is a good basis.

The tree stops whenever the daily limits of flight and duty time are reached, so that it describes the "scope" of feasible crew routings from that base in one duty period. The labels indicate the routing used to reach any flight and the starting departure from base.

Whenever a crew routing returns to its base on some arrival flight a "best" crew trip has been found. The crew can go off-duty at that time. The analyst knows that for that pair of departure-arrival flights at this crew base a crew trip has been found which maximizes the amount of flying achieved. It is possible to extend the tree construction to find the second best and third best trips at the same time.

Crew Trees can be constructed for each base. Best trips can be extracted and the next tree constructed to generate more trips. It seems possible to generate a Crew circulation for one base at a time if needed.

## Handling Overnight Trips

For discussion purposes, assume that there is a daily cycle in the aircraft schedule. Since there is usually a small number of crew bases and the aircraft schedule requires flights into secondary cities later in the evening with an early departure the next morning, there are identifiable "overnight" visits for aircraft and crew. Since these overnight visits cause out of pocket cost, they require special handling. There may be more than one crew overnighing at certain cities.

The crew tree will show the "best" way to route a crew from any base into the overnight arrival flights (if it is possible). Since there will be crew duties starting the next day at these bases, A crew tree is constructed from these overnight bases showing the best way to route crews back to base. By examination, it is easy to find the best two day trip for overnight crews. The search can be extended to three day trips if it is allowable or desirable.

The selection of low cost, efficient overnight trips can be made first. Once they are fixed, then all other trips must start and end at their crew bases within one day. The departure and arrival flights used for overnighing are then removed from the Schedule Map before constructing the one day trips.

The crew tree method is a new way to generate candidate trips for the second step of selection using some search methods of solving the set covering or partitioning problem. It is designed to only put forward the best candidates and keep the selection matrix very small. The process is not optimal, and it is intended that the analyst should be able to participate interactively in these searches, and return to this stage after the monthly bidlines have been initially constructed .

## Stage 2 - Constructing the Bidlines

Given the trips that are to be used for constructing the bidlines, there are a variety of techniques to generate potential bidlines which obey all or most of the bidline rules. These rules may be soft in the sense that crew schedulers may know where and how often they can be bent.

There are research problems in beginning and ending the monthly bidlines, or "transitioning" between months. For domestic schedules, there are also problems arising from weekend deviations in the daily schedule. These problems may be handled by Reserve Crews, but if good methods of constructing bidlines can be automated, there are likely to be efficiencies in the number of reserve bidlines used (and therefore the crews required to support the fleet).

One method used to generate bidlines is to create an efficient "pattern" of trips over 7 days, and to involve 7 crews in flying exactly the same bidline for the month. This reduces the size of the selection matrix. A much smaller matrix of trips versus patterns is used to select the "best" set of patterns to be used. The focus then changes to finding good candidate patterns for the bidlines. The patterns can be "mixed" to provide some variety in the crews' monthly work if desired.

The solution of the bidline selection process once again requires a good heuristic search methods of quickly "solving" set covering and set partitioning problems.

## Conclusions

1. There are some new approaches to creating interactive methods to support the crew scheduler in finding good low cost schedules for the crews.
2. There is a need to create methods for re-scheduling crews when deviations occur in executing the schedule. This should affect the current use of reserve crews
3. There seems to be a need to create similar methods for the cabin crews which are responsive to their differences in scheduling rules.
4. There is a need to provide some "early warning" methods for market and aircraft schedulers to cause a feedback of expensive crew scheduling problems before the aircraft schedule is finalized.

## COMPUTER AIDS FOR EXECUTION RESCHEDULING

1. Execution Rescheduling
2. The Influence of Rapid Advances in Computer Technology
3. The "Airline Scheduling Workstation" (ASW)
4. A 2-Stage Development Approach for An ASW
5. STAGE 1: A Manual, Interactive Graphics Scheduling System
6. STAGE 2: Automated Decision Support
7. Conclusions

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## I. EXECUTION RESCHEDULING

### GOAL:

- execute the operational schedule at least extra "cost" due to schedule aberrations

### INPUTS:

- Operational schedule
- Operational deviations
  - Weather, breakdowns
  - Late arrivals
- Expected traffic loads and revenues
- Short term operating costs

### OUTPUTS:

- Modified execution schedule
- Cancellations
- Delays

## II. The Influence of Rapid Advances in Computer Technology

### Old Approach

- "Techniques in search of an Application"
- use mainframe: large, fast supercomputer
- construct fixed code for technique
- user submits data, receives solution
- user reviews solution to comprehend it
- causality: user cannot ask for explanation of solution
- user may interface with OR analyst

### New Approach

- "Customize techniques to the Application"
- smaller, interactive graphic workstations on common network
- create various fast heuristics to solve subproblems
- create links to solve large scale problems on mainframe
- user is master, computer is servant, direct interface
- processes are custom built to meet application needs
- systems to match existing procedures and organization

### III. THE AIRLINE SCHEDULING WORKSTATION (ASW)

#### A COMPUTER TOOL FOR AIRLINE SCHEDULERS BASED ON THREE NEW TECHNOLOGIES:

1. Table top Engineering Workstations with a speed of 1-4 mips and disk storage of 100 -1000 MB working together on a local area network, interfaced with existing airline mainframe systems.
2. Large (19 inch), high-quality color displays with interactive, instantaneous, manipulation of schedule graphics information using a "mouse".
3. Object-oriented programming to provide modular code, easily extendable to handle time-varying scheduling constraints, policies, etc., and to reduce programming support.

We shall call this tool the ASW (Airline Scheduling Workstation)



## IV. DEVELOPMENT APPROACH FOR AN ASW

### GENERAL DEVELOPMENT STRATEGIES

- Involve schedulers at all development stages-- (there will be cultural and organizational shock)
  
- provide familiar systems and reports first to ensure that the new system will not preclude doing certain schedule sub-processes by old methods.
  
- Expect changes in organization and procedures as workstation capabilities are perceived.
  
- Establish a local area network of workstations in scheduling area, capable of interfacing with the airline's existing mainframe system. (e.g., 3 workstations at \$15,000 each). (Establish a "Schedule Generation" workroom).
  
- Develop modern, transportable, modular, object-oriented software, for automation of sub-processes in scheduling
  - easily extendable
  - easily supported
  - C, PASCAL, LISP language
  - good data structures
  
- A Two-Stage development process
  - STAGE 1: introduction of manual, interactive graphics scheduling system
  
  - STAGE 2: introduction of automated decision support

## V. STAGE 1 - A MANUAL, INTERACTIVE GRAPHICS SCHEDULING SYSTEM

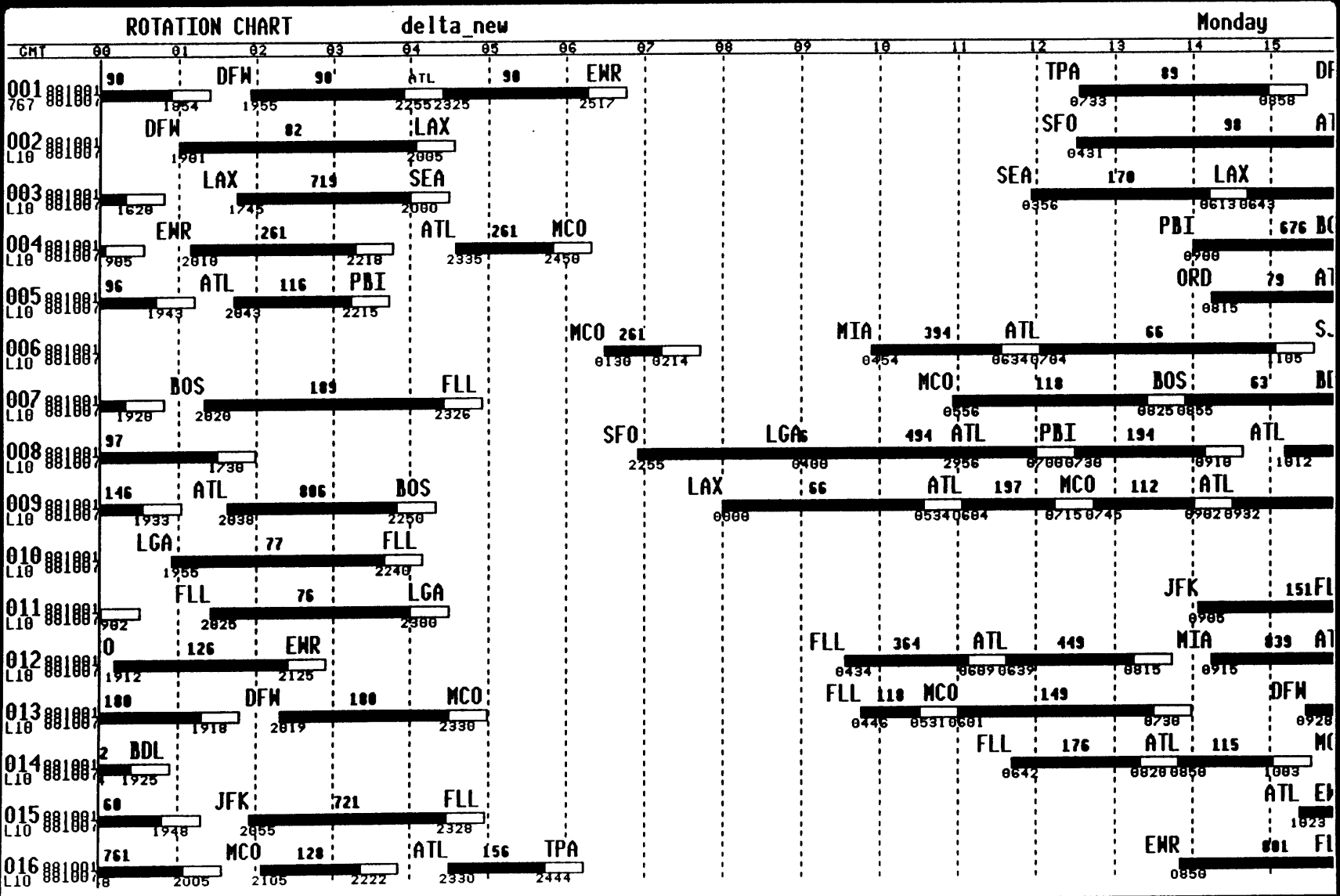
- A) Provide computer graphic displays of schedule information
  - instantaneously modifiable by mouse
  - global data base modification
  - selectable screen data -- by fleet, station
  - save alternate solutions
  - audit trail
  - memo pad for scheduler
  - keyed to input data, and assumptions used
  - automated search routines, etc. to minimize keyboard and mouse work
  
- B) Provide instantaneous error flagging (even if error occurs off-screen)
  - e.g., insufficient gates, flow imbalance, double crew layover, violation of turnaround or transit times, insufficient aircraft.
  
- C) Integrate crew, gate, maintenance schedule with aircraft schedule
  
- D) Provide familiar printed reports and graphics for distribution around airline
  
- E) Provide interface to mainframe data system to maintain current scheduling processes.

HOME DOWN LEFT RIGHT OTHERS REPORTS EDIT SEARCH WINDOW WEEKDAY QUIT ALGORITHM

FILES  
CURRENT  
INTERMEDIATE  
FUTURE

HOME DOWN LEFT RIGHT OTHERS REPORTS EDIT SEARCH FILE WEEKDAY QUIT ALGORITHM

WINDOW  
ROTATION\_CHART  
SCHEDULE\_LISTING  
STATION CHART  
STATION PROFILE  
SUB PROFILES





OTHERS

REPORT

EDIT

ADD

COPY

DELETE

DELETEALL

INTERCHANGE

MOVE 1

MOVE ALL

MODIFY

SWAP

UNDELETE

ZOOM

ARCH

FILES

WINDOW

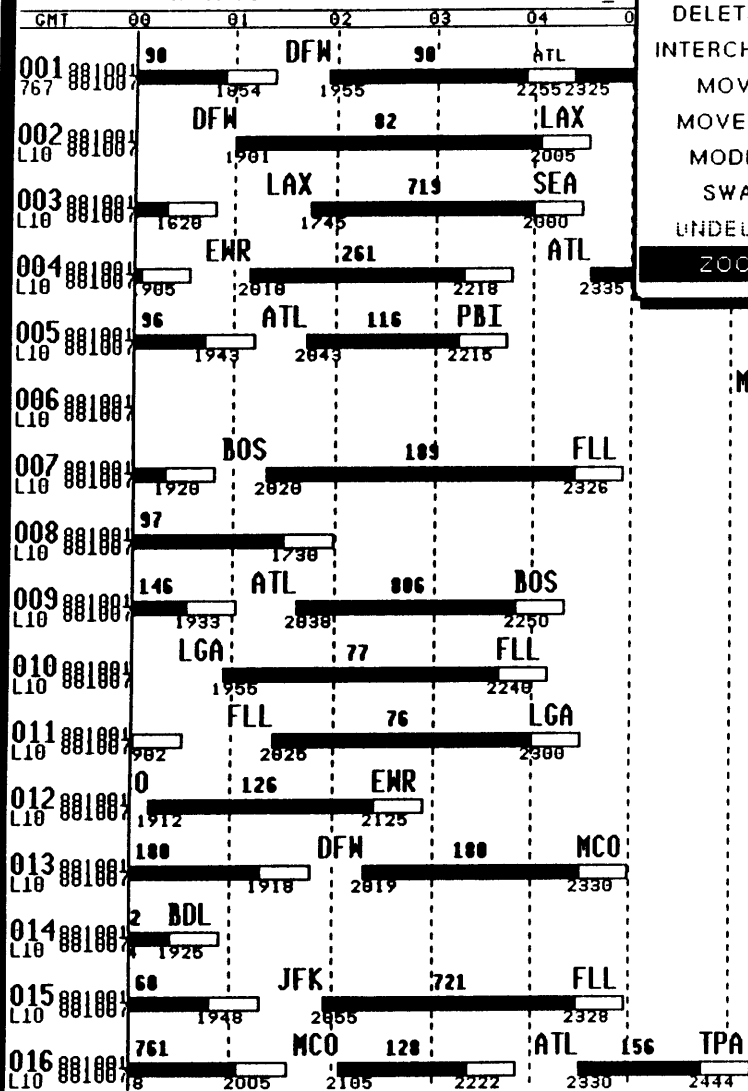
WEEKDAY

QUIT

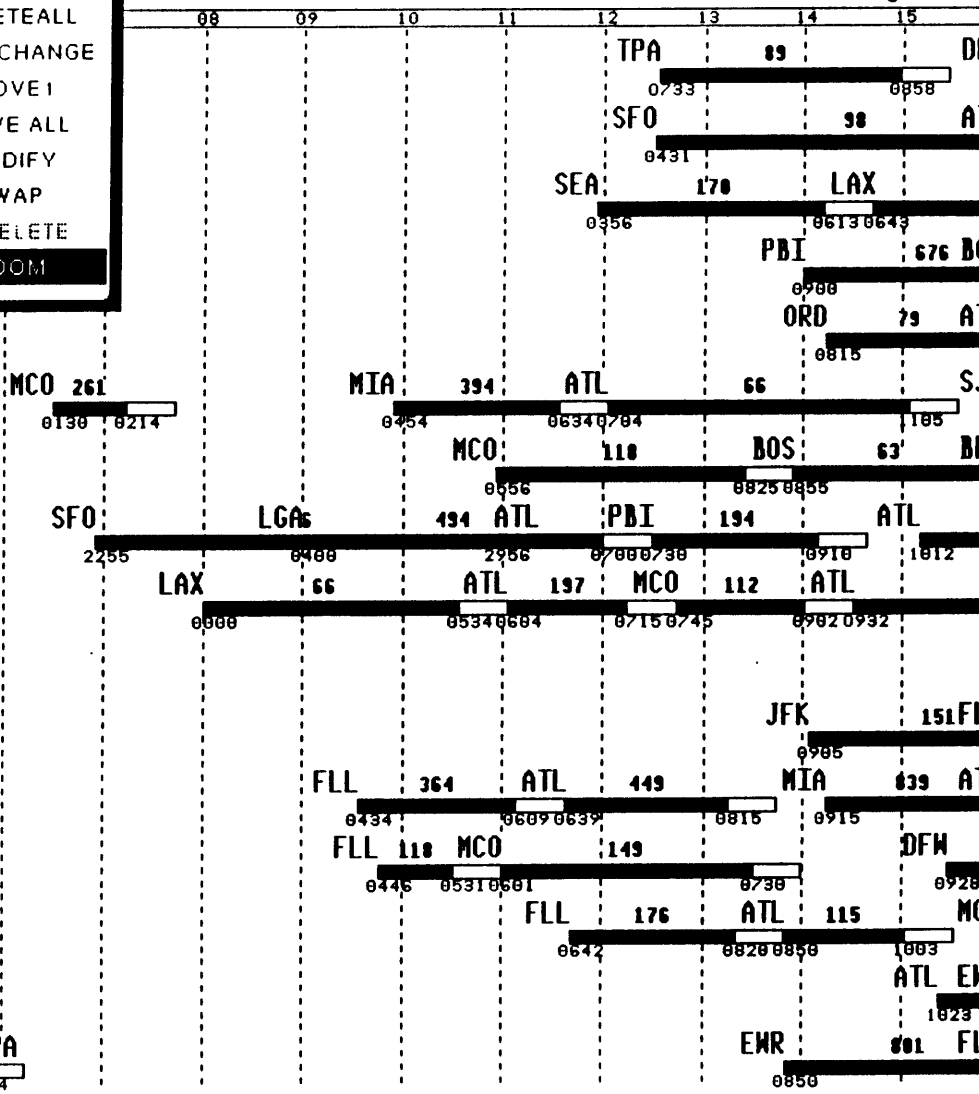
ALGORITHM

### ROTATION CHART

delta\_n



### Monday





OTHERS

REPORTS

EDIT

SEARCH

FILES

WINDOW

WEEKDAY

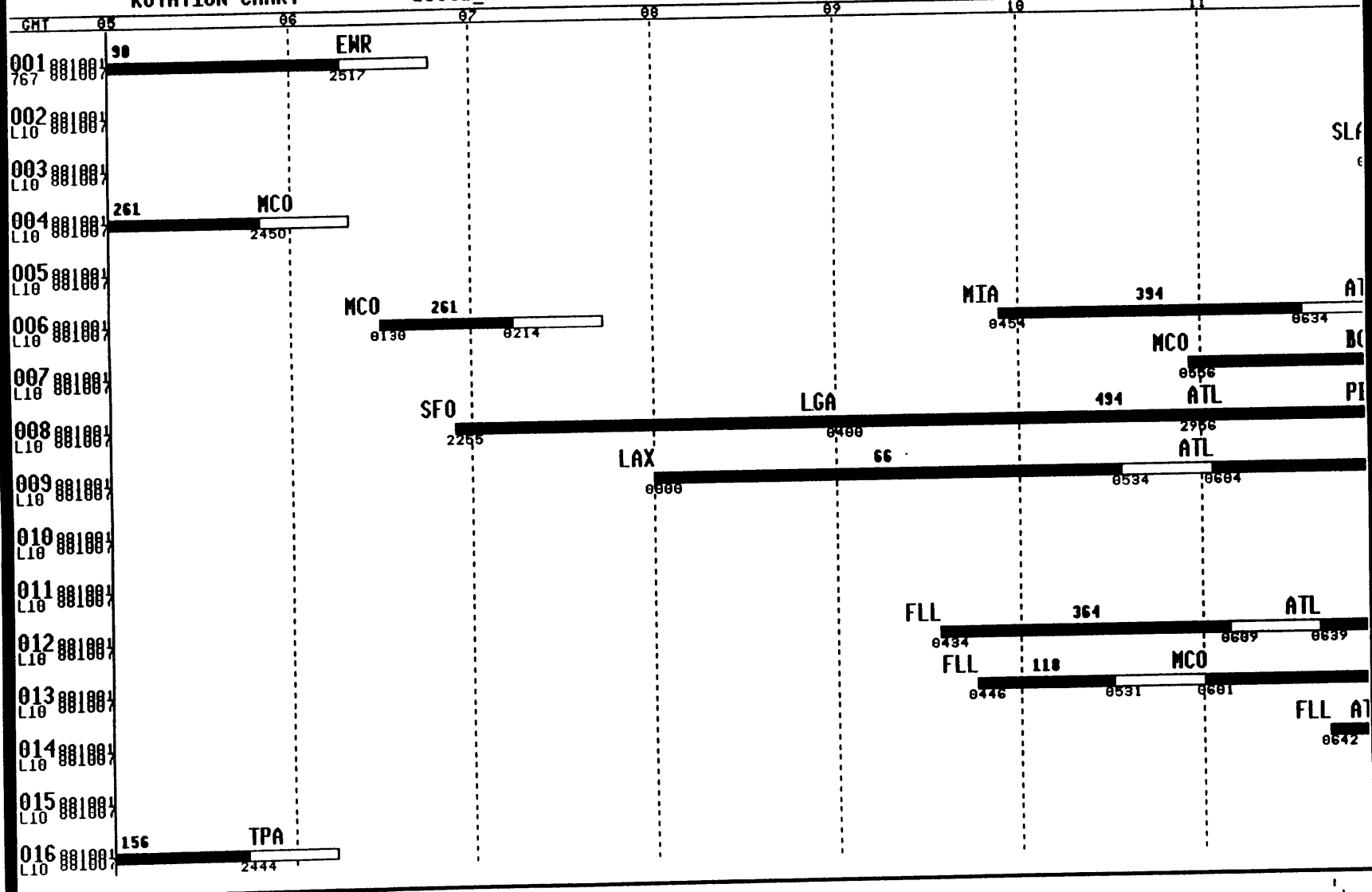
QUIT

ALGORITHM

### ROTATION CHART

delta\_new

Monday





OTHERS

REPORTS

EDIT

SEARCH

FILES

WINDOW

WEEKDAY

QUIT

ALGORITHM

ROTATION CHART

delta\_new

Monday

GMT	00	01	02	03	04	05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	
001	881007	DFW	90	ATL	90	EWR							TPA	89				DFW	89			LAX	90	DF		
002	881007	DFW	82	LAX									SFO	98	ATL	155	MCO	158	ATL	82			DF			
003	881007	LAX	715	SEA									SEA	170	LAX	140						DFW	179	LA		
004	881007	EWR	261	ATL	261	MCO							PBI	576	BOS	111	MCO	111	ATL	141			EM			
005	881007	ATL	116	PBI									ORD	79	ATL	83					SJU	96	AT			
006	881007						MCO 261			MIA	394	ATL	66								SJU	82	ATL	70	ORD	
007	881007	BOS	109	FLL									MCO	110	BOS	63					BDA	85	ATL	74	BO	
008	881007	97											SFO	LGAc	494	ATL	PBI	194	ATL	65	MIA	97	ATL			
009	881007	ATL	806	BOS									LAX	66	ATL	197	MCO	112	ATL	117		LAX	146	AT		
010	881007	LGA	77	FLL																		LAX	134	ATL	150	LO
011	881007	FLL	76	LGA									JFK	151							FLL	144	JFK	153	FL	
012	881007	126	EWR										FLL	364	ATL	449	MIA	839	ATL	799	PBI	74	ATL	182	MCO	
013	881007	180	DFW	100	MCO								FLL	11	MCO	149					DFW	149		SFO		
014	881007	2	BDL										FLL	176	ATL	115	MCO	80	ATL	80	BDA	62	BOS	62	B	
015	881007	JFK	721	FLL									ATL	194	EWR	87					FLL	60	JF			
016	881007	761	MCO	120	ATL	156	TPA						EWR	801	FLL	800					EWR	829	ATL			





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ARCH FILES WINDOW WEEKDAY QUIT ALGORITHM

**ROTATION CHART** delta\_ne

CHT	00	01	02	03	04	05	06	07
001	90	DFW	90	ATL	90	ENR		
002		DFW	82	LAX				
003		LAX	719	SEA				
004		ENR	261	ATL	261	MCO		
005		ATL	116	PBI				
006							MCO 261	
007		BOS	189	FLL				
008							SFO	
009		ATL	806	BOS				
010		LGA	77	FLL				
011		FLL	76	LGA				
012			126	ENR				
013		180	DFW	180	MCO			
014		BDL						
015		JFK	721	FLL				
016		761	MCO	120	ATL	156	TPA	

**Monday**

	12	13	14	15	16	17	18	19	20	21	22	23	24
TPA	89						DFW	89		LAX	90	DF	
SFO	90						ATL	155	MCO	150	ATL	82	DF
SEA	170	LAX	140							DFW	179	LA	
PBI	876						BOS	111	MCO	111	ATL	141	ED
ORD	79						ATL	83		SJU	96	AT	
SJU	82									ATL	70	ORD	
MCO	118						BOS	63		ATL	74	BC	
LGA	494	ATL	PBI	194	ATL	65	MIA	97	ATL				
LAX	66	ATL	197	MCO	112	ATL	117			LAX	146	AT	
FLL	11	MCO	149	DFW	149					SFO			
FLL	176	ATL	115	MCO	80	ATL	80	BDA	62	BOS	62	B	
ATL	194	ENR	87							FLL	60	JF	
ENR	881	FLL	800	ENR	829	ATL							



OTHERS

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WINDOW

WEEKDAY

QUIT

ALGORITHM

00

ROTATION CHART

delta\_new

Monday

GMT	00	01	02	03	04	05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	
001	881007	DFW	DFW	ATL	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW
002	881007	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW
003	881007	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW
004	881007	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW
005	881007	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW
006	881007	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW
007	881007	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW
008	881007	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW
009	881007	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW
010	881007	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW
011	881007	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW
012	881007	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW
013	881007	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW
014	881007	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW
015	881007	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW
016	881007	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW	DFW



OTHERS    REPORTS    EDIT    SEARCH    FILES    WINDOW    WEEKDAY    QUIT    ALGORITHM

ROTATION CHART		delta_new																									
CHY		00	01	02	03	04	05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	
001	88100%	90	DFW	90	ATL	90	EWR							TPA	89				DFW	89					LAX	90	DF
767	88100%	1954	1955		2205	2205	2517							0733	0858				1152		1308	1415					
002	88100%		DFW	82		LAX								SFO	90				ATL	155	MCO	150		ATL	82	DF	
L10	88100%	1901			2005									0431					1131	207	1320	1425	1542	1655	1800		
003	88100%		LAX	719		SEA								SEA	170	LAX	140							DFW	179	LA	
L10	88100%	1628	1745		2000									0956	0610	0643			1122				1524		16		
004	88100%		EWR	261		ATL	261	MCO							PBI	576	BOS						MCO	111	ATL	141	EV
L10	88100%	1908	2018		2218	2335	2450							0900					1131	205		1451	1524	1641	1713	1900	
005	88100%		ATL	116		PBI								ORD	79								ATL	83	SJU	96	AT
L10	88100%	1943	2043		2215									0456	0741				1157		1500	1705					
006	88100%							MCO	261						MIA	394	ATL	66					SJU	82	ATL	70	ORD
L10	88100%							0130	0214					0454	0637	084			1105		1300	1530	1644	1735			
007	88100%		BOS	109		FLL									MCO	110	BOS	63				BDA	85	ATL	74	BC	
L10	88100%	1920	2020		2320									0556	0823	0955			1155		1355		1500	1705	19		
008	88100%		97												SFO	LGA	494	ATL	PBI	194	ATL	65	MIA	97	ATL		
L10	88100%		1730											2455	0400	2956	0700	0730	0910	1012	1150	1250	1430	1530			
009	88100%		ATL	806		BOS									LAX	66	ATL	197	MCO	112	ATL				LAX	146	AT
L10	88100%	1933	2030		2250									0000	0530	064	0710	0745	0900	0932		1101	1240				
010	88100%		LGA	77		FLL																					
L10	88100%	1955			2240																						
011	88100%		FLL	76		LGA																					
L10	88100%	1902	2025		2300																						
012	88100%		126		EWR																						
L10	88100%	1912			2125																						
013	88100%		100		DFW	100		MCO																			
L10	88100%	1910	2019		2300																						
014	88100%		BDL																								
L10	88100%	1925																									
015	88100%		JFK	721		FLL																					
L10	88100%	1940	2055		2320																						
016	88100%		761		MCO	120		ATL	156	TPA																	
L10	88100%	1940	2005	2105	2222	2330	2444																				



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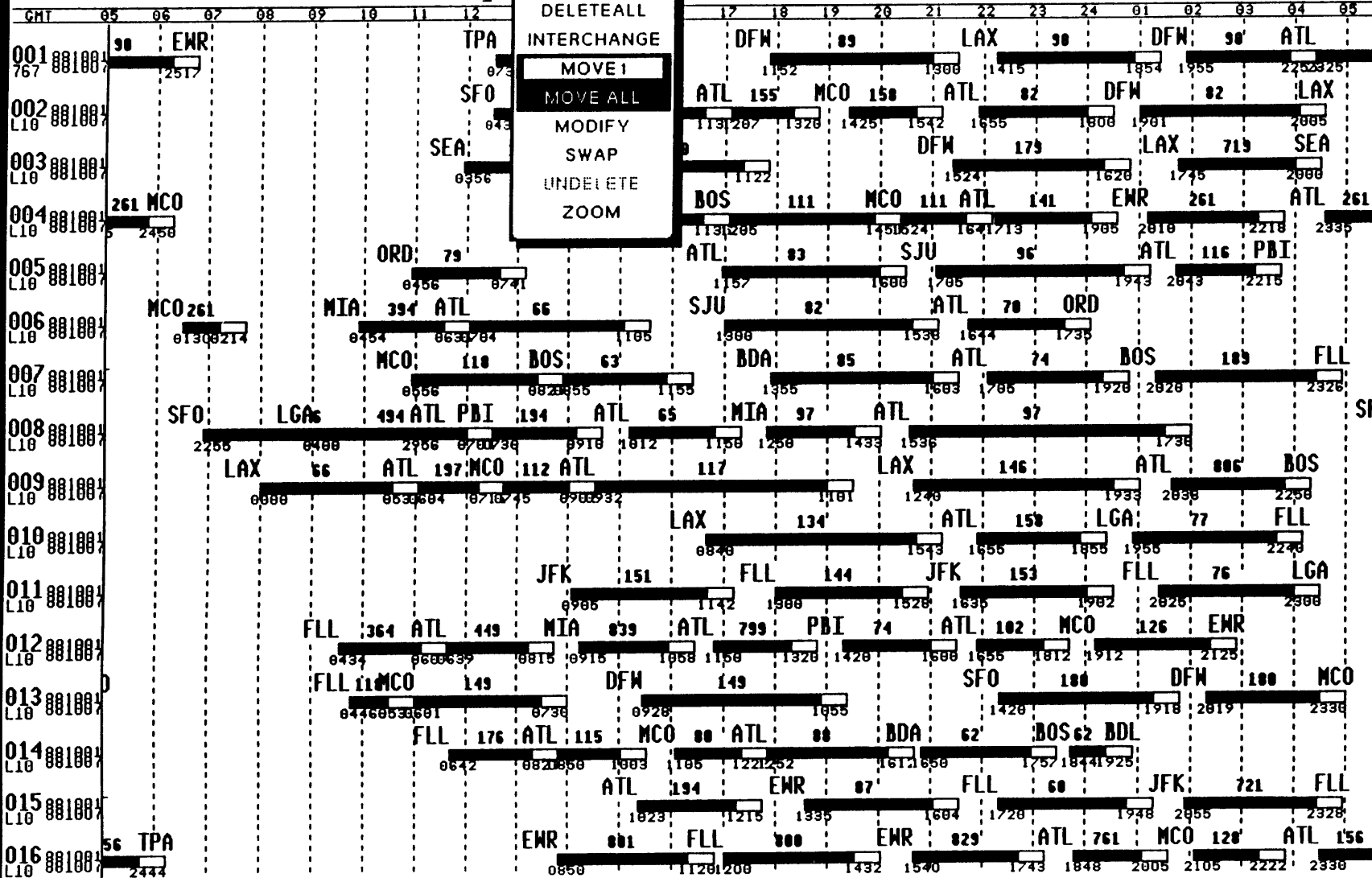
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### ROTATION CHART

delta\_ne

Monday





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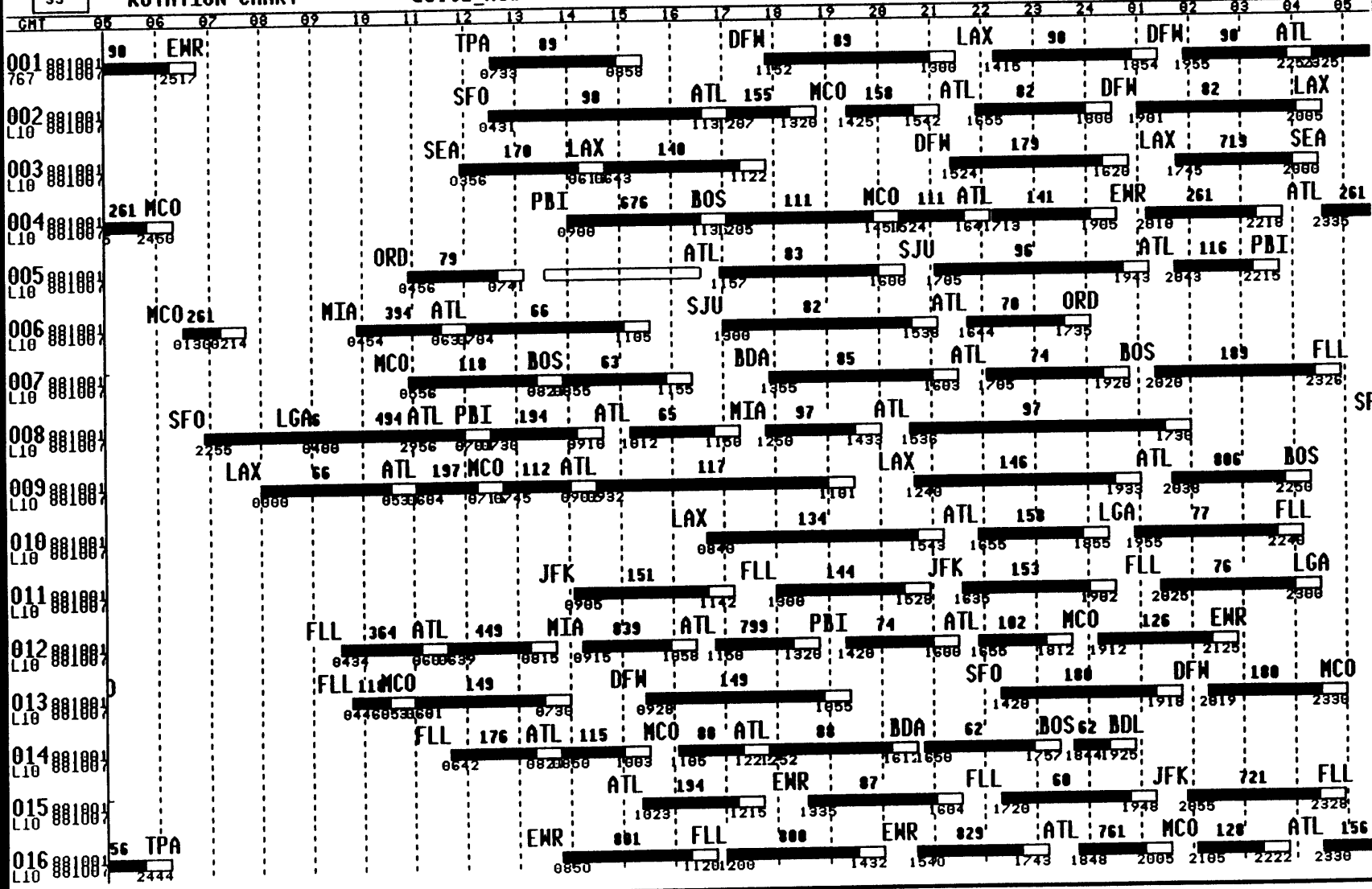
ALGORITHM

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ROTATION CHART

delta\_new

Monday



ROTATION CHART

delta\_new

Monday

GMT	05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	01	02	03	04	05
001	88100%	90 EWR						TPA 89						DFW 89				LAX 90			DFW 90			ATL	
002	88100%							SFO 98					ATL 155		MCO 158			ATL 82			DFW 82			LAX	
003	88100%							SEA 170		LAX 140								DFW 179			LAX 719			SEA	
004	88100%	261 MCO								PBI 676		BOS		111		MCO 111		ATL 141			EWR 261			ATL 261	
005	88100%							ORD 79		ATL 83			SJU 96					ATL 116			PBI				
006	88100%	MCO 261						MIA 394		ATL 66			SJU 82					ATL 78			ORD				
007	88100%							MCO 118		BOS 63			BDA 85					ATL 74			BOS 189			FLL	
008	88100%	SFO						LGAs 494		ATL PBI 194			ATL 65		MIA 97			ATL 97							SF
009	88100%							LAX 66		ATL 197		MCO 112		ATL 117				LAX 146			ATL 885			BOS	
010	88100%												LAX 134					ATL 158			LGA 77			FLL	
011	88100%									JFK 151			FLL 144					JFK 153			FLL 76			LGA	
012	88100%							FLL 364		ATL 449		MIA 839		ATL 799		PBI 74		ATL 102			MCO 126			EWR	
013	88100%							FLL 11		MCO 149			DFW 149					SFO 100			DFW 100			MCO	
014	88100%							FLL 176		ATL 115		MCO 88		ATL 88		BDA 62					BOS 62			BDL	
015	88100%									ATL 194			EWR 87					FLL 60			JFK 721			FLL	
016	88100%	56 TPA								EWR 881			FLL 800					EWR 829			ATL 761			MCO 128	ATL 156



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ROTATION CHART

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CHT	05	06	07	08	09	10	11	12
001	EMR						TPA	
002							SFO	
003							SEA	
004	MCO							
005							ORD	
006	MCO						MIA	
007							MCO	
008	SFO						LGA	
009							LAX	
010								
011							JFK	
012							FLL	
013							FLL	
014							FLL	
015							ATL	
016	TPA						EWR	

DELETEALL  
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Monday

05	06	07	08	09	10	11	12	01	02	03	04	05
DFW							LAX		DFW		ATL	
ATL							MCO		ATL		DFW	
BOS							MCO		ATL		LAX	
SJU							ATL		ORD			
MIA							BDA		ATL		BOS	
FLL							MIA		ATL			
JFK							FLL		JFK		FLL	
MCO							FLL		MCO		DFW	
ATL							ATL		EWR		MCO	
EWR							FLL		EWR		ATL	



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ROTATION CHART

delta\_new

Monday

GMT	05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	01	02	03	04	05
001	881007	90 EWR						TPA 89						DFW 89				LAX 90			DFW 90		ATL		
002	881007							SFO 98					ATL 155	MCO 150				ATL 82			DFW 82		LAX		
003	881007							SEA 170	LAX 140									DFW 179			LAX 719		SEA		
004	881007	261 MCO						PBI 576	BOS					111	MCO 111	ATL 141				ENR 261		ATL 261			
005	881007							ORD 79	ATL 83				SJU 96					ATL 116			PBI				
006	881007	MCO 261						MIA 394	ATL 66				SJU 82					ATL 70			ORD				
007	881007							MCO 110	BOS 63				BDA 85					ATL 74			BOS 109		FLL		
008	881007	SFO	LGA 6					494	ATL PBI 194	ATL 65			MIA 97					ATL 97							SF
009	881007							LAX 66	ATL 197	MCO 112	ATL 117							LAX 146			ATL 806		BOS		
010	881007												LAX 134					ATL 150			LGA 77		FLL		
011	881007							JFK 151					FLL 144					JFK 153			FLL 76		LGA		
012	881007							FLL 364	ATL 449	MIA 839	ATL 799	PBI 74	ATL 102	MCO 126	EWR										
013	881007							FLL 11	MCO 149		DFW 149				SFO 100			DFW 100			MCO				
014	881007							FLL 176	ATL 115	MCO 80	ATL 88	BDA 62	BOS 62	BDL											
015	881007								ATL 194		EWR 87		FLL 60		JFK 721										
016	881007	56 TPA											EWR 801	FLL 800		EWR 829		ATL 761			MCO 120		ATL 156		





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ROTATION CHART

delta\_new

Monday

CHT	05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	01	02	03	04	05
001	88100%	90 EWR						TPA 83					DFW 89				LAX 90			DFW 90			ATL		
002	88100%							SFO 90					ATL 155		MCO 150		ATL 82			DFW 82			LAX		
003	88100%							SEA 170		LAX 140							DFW 179			LAX 719			SEA		
004	88100%	261 MCO						PBI 176		BOS 111			MCO 111		ATL 141		EWR 261			ATL 261					
005	88100%							ORD 79		ATL 83			SJU 96				ATL 116			PBI					
006	88100%	MCO 261						MIA 394		ATL 66			SJU 82				ATL 70			ORD					
007	88100%							MCO 118		BOS 63			BDA 85				ATL 150			LGA 77			FLL		
008	88100%	SFO						LGA 494		ATL PBI 194			ATL 65		MIA 97		ATL 97								
009	88100%							LAX 66		ATL 197		MCO 112		ATL 117			LAX 146			ATL 806			BOS		
010	88100%												LAX 134				ATL 74			BOS 109			FLL		
011	88100%							JFK 151					FLL 144				JFK 153			FLL 76			LGA		
012	88100%							FLL 364		ATL 449		MIA 839		ATL 799		PBI 74		ATL 102		MCO 126			EWR		
013	88100%							FLL 11		MCO 149			DFW 149				SFO 100			DFW 100			MCO		
014	88100%							FLL 176		ATL 115		MCO 80		ATL 88		BDA 62		BOS 62		BDL					
015	88100%									ATL 194			EWR 97				FLL 60			JFK 721			FLL		
016	88100%	56 TPA						EWR 801		FLL 800			EWR 829				ATL 761			MCO 120			ATL 156		



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ALGORITHM

EDIT

ADD

COPY

DELETE

DELETEALL

INTERCHANGE

MOVE 1

MOVE ALL

MODIFY

SWAP

UNDELETE

ZOOM

ROTATION CHART

delta\_n

Monday

GMT	05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	01	02	03	04	05
001	88100%	90 EWR						TPA					DFW	09		LAX	90			DFW	90		ATL		
002	88100%							SFO					ATL	155	MCO	150	ATL	82		DFW	82		LAX		
003	88100%							SEA								DFW	179			LAX	719		SEA		
004	88100%	261 MCO											BOS	111	MCO	111	ATL	141		EWR	261		ATL	261	
005	88100%							ORD	79	ATL	83		SJU	96		ATL	116			PBI					
006	88100%	MCO 261						MIA	394	ATL	66		SJU	82		ATL	70			ORD					
007	88100%							MCO	110	BOS	63		BDA	85		ATL	150			LGA	77		FLL		
008	88100%	SFO	LGA	494	ATL	PBI	194	ATL	65	MIA	97	ATL	97												SF
009	88100%	LAX	66	ATL	197	MCO	112	ATL	117				LAX	146		ATL	806			BOS					
010	88100%												LAX	134		ATL	74			BOS	109		FLL		
011	88100%							JFK	151	FLL	144	JFK	153	FLL	76	LGA									
012	88100%							FLL	364	ATL	449	MIA	839	ATL	793	PBI	74	ATL	102	MCO	126	EWR			
013	88100%							FLL	11	MCO	149	DFW	149	SFO	100	DFW	100	MCO							
014	88100%							FLL	176	ATL	115	MCO	80	ATL	80	BDA	62	BOS	62	BDL					
015	88100%							ATL	194	EWR	87	FLL	60	JFK	721	FLL									
016	88100%	56 TPA						EWR	801	FLL	800	EWR	829	ATL	761	MCO	120	ATL	156						



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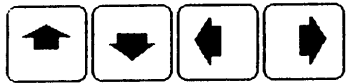
ALGORITHM

ROTATION CHART

delta\_new

Monday

GMT	05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	01	02	03	04	05	
001	88100%	90 EWR																								
002	88100%																									
003	88100%																									
004	88100%	261 MCO																								
005	88100%																									
006	88100%	MCO 261																								
007	88100%																									
008	88100%	SFO																								
009	88100%																									
010	88100%																									
011	88100%																									
012	88100%																									
013	88100%																									
014	88100%																									
015	88100%																									
016	88100%	56 TPA																								



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 TUESDAY  
 WEDNESDAY  
 THURSDAY  
 FRIDAY  
 SATURDAY  
 SUNDAY  
 WEEKLY

QUIT    ALGORITHM

ROTATION CHART		delta_new																						
GMT		05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20	21	Monday					
																			01	02	03	04	05	
001	88100%	90 EWR						ORD: 79	ATL	83				SJU		96								
767	88100%							0456		0741	0833			1236	1341									
002	88100%								SFO		98			ATL	155	MCO	150							
L10	88100%								0431					1131	1207	1320	1425	1542						
003	88100%								SEA:	170	LAX		140					DFW						
L10	88100%								0356		0610	0743			1122		1624	1628						
004	88100%	261 MCO								PBI	576	BOS		111	MCO	111	ATL	141	EWR	261	ATL	261		
L10	88100%									0908				1131	1205	1451	1624	1641	1713	1905	2018	2218	2335	
005	88100%									TPA	89				DFW	89	LAX	90	DFW	90	ATL			
L10	88100%									0733		0858			1152		1308	1415	1854	1955		2252	2325	
006	88100%	MCO 261							MIA:	394	ATL	66		SJU	82	ATL	70	ORD						
L10	88100%								0454		0631	0704			1308		1538	1644	1735					
007	88100%									MCO:	110	BOS:	63		BDA:	85	ATL	74	BOS	103	FLL			
L10	88100%								0656		0823	0855			1355		1603	1705	1920	2020		2328		
008	88100%	SFO:	LGA:						494	ATL	PBI	194	ATL	65	MIA	97	ATL	97					SF	
L10	88100%								2256	0408	2956	0703	0838	0918	1012	1158	1250	1433	1536		1738			
009	88100%	LAX	66	ATL	197	MCO	112	ATL						117			LAX	146	ATL	806	BOS			
L10	88100%	0900		0530	0604	0710	0745	0900	0932					1101		1240		1933	2038		2258			
010	88100%									LAX	134	ATL	150	LGA:	77	FLL								
L10	88100%									0848				1543	1655	1855	1955				2248			
011	88100%									JFK	151	FLL	144	JFK	153	FLL	76	LGA						
L10	88100%									0905		1142		1308	1528	1635	1902	2025		2308				
012	88100%									FLL	364	ATL	449	MIA	839	ATL	799	PBI	74	ATL	102	MCO	126	EWR
L10	88100%									0434	0600	0639	0816	0915	1058	1150	1320	1420	1600	1655	1812	1912	2125	
013	88100%	FLL	11	MCO	149	DFW	149	SFO	100	DFW	100	MCO												
L10	88100%	0446	0533	0601		0730		0928		1055				1420		1918	2019					2338		
014	88100%	FLL	176	ATL	115	MCO	80	ATL	80	BDA	62	BOS	62	BDL										
L10	88100%	0642		0821	0858	1003	1105	1221	1252			1611	1650	1757	1844	1925								
015	88100%									ATL	194	EWR	87	FLL	60	JFK	721	FLL						
L10	88100%									1023		1215	1335		1604	1728	1948	2055		2328				
016	88100%	56 TPA								EWR	801	FLL	800	EWR	829	ATL	761	MCO	128	ATL	156			
L10	88100%									0850		1120	1208		1432	1540	1743	1848	2005	2105	2222	2330		



OTHERS    REPORTS    EDIT    SEARCH    FILES    WINDOW    WEEKDAY    QUIT    ALGORITHM

ROTATION CHART

delta\_new

Weekly

CHT	05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	01	02	03	04	05	
001	88100%	90	EWR:			ORD:	79	ATL	03		SJU	96		ATL	116	PBI										
767	88100%		2517			0456		0741	0833			1236	1341		1619	1719	1851									
Tu	88100%	90	EWR:			ORD:	79	ATL	03		SJU	96		ATL	116	PBI										
Me	88100%	90	EWR:			ORD:	79	ATL	03		SJU	96		ATL	116	PBI										
Th	88100%	90	EWR:			ORD:	79	ATL	03		SJU	96		ATL	116	PBI										
Fr	88100%	90	EWR:			ORD:	79	ATL	03		SJU	96		ATL	116	PBI										
Sa	88100%	90	EWR:					ATL	03		SJU	96		ATL	116	PBI										
Su	88100%	90	EWR:			ORD:	79	ATL	03		SJU	96		ATL	116	PBI										
			2517			0456		0741	0833			1236	1341		1619	1719	1851									
002	88100%					SFO		90		ATL	155	MCO	150	ATL:	02	DFW					02				LAX	
L10	88100%					0431				1131	207	1328	1428	1542	1655		1808	1901							2008	
Tu	88100%					SFO		90		ATL	155	MCO	150	ATL:	02	DFW					02				LAX	
Me	88100%					0431				1131	207	1328	1428	1542	1655		1808	1901							2008	
Th	88100%					SFO		90		ATL	155	MCO	150	ATL:	02	DFW					02				LAX	
Fr	88100%					0431				1131	207	1328	1428	1542	1655		1808	1901							2008	
Sa	88100%					SFO		90		ATL	155	MCO	150	ATL:	02	DFW					02				LAX	
Su	88100%					0431				1131	207	1328	1428	1542	1655		1808	1901							2008	
003	88100%					SEA:	170	LAX	140					DFW	179	LAX	719	SEA								
L10	88100%					0956		0610	0543			1122		1524		1628	1745	2008								
Tu	88100%					SEA:	170	LAX	140					DFW	179	LAX	719	SEA								
						0956		0610	0543			1122		1524		1628	1745	2008								

				OTHERS	REPORTS	EDIT	SEARCH	FILE	WINDOW	WEEKDAY	QUIT	ALGORITHM
									ROTATION_CHART			
									SCHEDULE_LISTING			
									STATION_CHART			
									STATION_PROFILE			
									SUB_PROFILES			

ELI	A/C	FREQ	FROM	TO	DEPT	ARRV	CLASS	MEAL	EFFE	ROTN#
60	L10	X6	FLL	JFK	1720	1948			851110-999999	015-015-015-015-000-015
62	L10	X6	BDA	BOS	1650	1757			851110-999999	014-014-014-014-014-000-014
62	L10	X6	BOS	BDL	1844	1925			851110-999999	014-014-014-014-014-000-014
63	L10	X6	BDL	BOS	0700	0744			851110-999999	021-021-021-021-021-000-021
63	L10	X6	BOS	BDA	0855	1155			851110-999999	007-007-007-007-007-000-007
65	L10	X6	ATL	MIA	1012	1150			851110-999999	008-008-008-008-008-000-008
66	L10	X6	LAX	ATL	0900	0534			851110-999999	009-009-009-009-009-000-009
66	L10	X6	ATL	SJU	0704	1105			851110-999999	006-006-006-006-006-000-006
67	L10	X6	ATL	FLL	1326	1505			851110-999999	023-023-023-023-023-000-023
70	L10	X6	ATL	ORD	1644	1735			851110-999999	006-006-006-006-006-000-006
74	L10	X6	PBI	ATL	1420	1600			851110-999999	012-012-012-012-012-000-012
74	L10	X6	ATL	BOS	1705	1920			851110-999999	007-007-007-007-007-000-007
76	L10	X6	FLL	LGA	2025	2300			851110-999999	011-011-011-011-011-000-011
77	L10	X6	LGA	FLL	1955	2240			851110-999999	010-010-010-010-010-000-010
79	767	X6	ORD	ATL	0815	1100			851110-999999	001-001-001-001-001-000-001
80	L10	X6	MCO	ATL	1105	1222			851110-999999	014-014-014-014-014-000-014







				OTHERS	REPORTS	EDIT	SEARCH	FILES	WINDOW	WEEKDAY	QUIT	ALGORITHM
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ATL TIME\_ZONE : - 05 39

DATE : 881001 Saturday

LOCAL

00	01	02	03	04	05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24		
						364 FLL	394 MIA		176 FLL	112 NCO	194 PBI	799 EUR	83 DFW	98 SFO		97 MIA	82 SFO	111 NCO	167 LGA	829 EUR	116 SFO	146 LAX	177 ORD	120 NCO	261 EUR	98 DFW


05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	01	02	03	04	05				

GMT

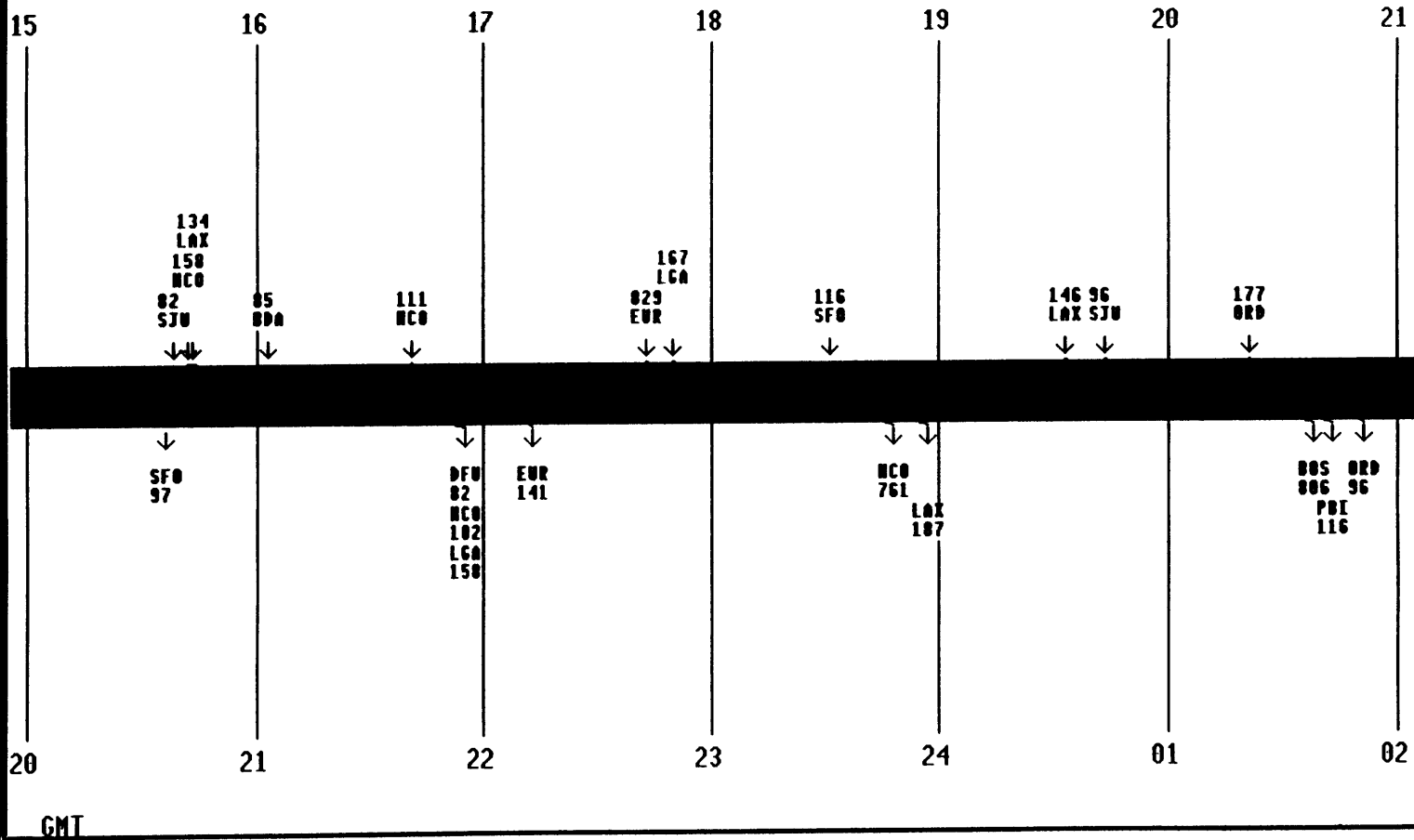


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OTHERS REPORTS EDIT SEARCH FILES WINDOW WEEKDAY QUIT ALGORITHM

ATL TIME ZONE : - 05

DATE : 881001 Saturday

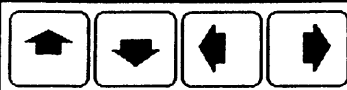
LOCAL



T	Saturday				881001				ATL				TIME ZONE : -05			
									0326	SFO	0520	0605	ATL	137	D	L10
									0604	MCO	0715	0030	ATL	197	D	L10
	364	D	L10		0434	FLL	0609	0030								
	394	D	L10	MCO 0240	0454	MIA	0634	0526								
								0030	0639	MIA	0815	0100	ATL	449	D	L10
	176	D	L10		0642	FLL	0820	0030								
								0030	0850	MCO	1003			115	D	L10
	112	D	L10	ATL 0030	0745	MCO	0902	0030								
	194	D	L10	LGA 0030	0730	PBI	0910	0340								
								0030	0932	LAX	1101	0139	ATL	117	D	L10
	799	D	L10		0753	EWR	0957	0030								
								0030	1023	EWR	1215	0120	FLL	194	D	L10
								0030	1027	MCO	1140	0110	DFW	195	D	L10
	83	D	L10		0749	DFW	1045	0115								
	839	D	L10	ATL 0100	0915	MIA	1058	0052								
	98	D	L10		0431	SFO	1137	0030								
								0052	1150	PBI	1320			799	D	L10
									1157	SJU	1600	0105	ATL	83	D	L10
								0115	1200	ORD	1309	0427	ATL	83	D	L10
								0030	1207	MCO	1320	0105	ATL	155	D	L10

K T E S	Saturday				881001				LGA				TIME ZONE : -05			
									0400	PBI	0700	0030	ATL	494	D	L10
	702	D	L10	BOS 0035	1155	PBI	1422	0108								
								0108	1530	ATL	1750	0107	LAX	167	D	L10
	158	D	L10	LAX 0112	1655	ATL	1855									





OTHERS    REPORTS    EDIT    **SEARCH**    LES    WINDOW    WEEKDAY    QUIT    ALGORITHM

**FLIGHT NUMBER**

**ROTATION**

**ROTATION CHART**

delta\_new

Monday

GMT	05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	01	02	03	04	05	
001	88100%	90 EWR								ORD 79		ATL		83		SJU		96		ATL	116		PBI			
767	88100%	2517								0815		1108	1157		1508	1705				1943	2043		2215			
002	88100%								SFO	90		ATL 155		MCO 150		ATL		82		DFW		82		LAX		
L10	88100%								0431		113207	1320	1425	1542	1655		1808	1901		2000			2000			
003	88100%								SEA	170	LAX	140				DFW		175		LAX		715		SEA		
L10	88100%								0356		0610543		1122		1524		1628		1745		2000					
004	88100%	261 MCO							PBI	576		BOS		111		MCO 111	ATL	141		EMR	261		ATL	261		
L10	88100%	2458							0908		113205		1450524	1641713		1905	2010		2215		2335					
005	88100%								TPA	89					DFW		89		LAX	90		DFW	90		ATL	
L10	88100%								0733		0858		1152		1308	1415		1854	1955		2205	2325				
006	88100%	MCO 261							MIA	394	ATL	66			SJU		82		ATL	70		ORD				
L10	88100%	01309214							0454		0633704		1105		1508		1538	1644		1735						
007	88100%								MCO	110		BOS	63			BDA		85		ATL	74		BOS	105	FLL	
L10	88100%								0555		082055		1155		1355		1503	1705		1920	2020			2320		
008	88100%	SFO	LGA						494	ATL	PBI	194		ATL	65	MIA	97			ATL		97			SF	
L10	88100%	2255	0408						2956	0700730	0910	1012	1157	1330		1530		1730		1920	2020					
009	88100%	LAX	66						ATL 197	MCO 112	ATL									LAX		146		ATL	806	BOS
L10	88100%	0908							0530804	0710745	0900932			1101		1240		1933	2030		2250					
010	88100%														LAX		134			ATL	150		LGA	77	FLL	
L10	88100%													0840		1043	1055		1055		1055			2240		
011	88100%								JFK	151					FLL		144		JFK	153		FLL	76	LGA		
L10	88100%								0905		1142	1508		1520	1635		1902	2025		2300						
012	88100%								FLL	364	ATL	449		MIA	839	ATL	799		PBI	74		ATL	102	MCO	126	EMR
L10	88100%								0434		0500539	0815	0915	1058	1150	1320	1420		1508	1655	1812	1912		2120		
013	88100%								FLL 11	MCO	149				DFW		149			SFO		100		DFW	100	MCO
L10	88100%								0446053001		0730		0920		1055		1420		1918	2019		2330				
014	88100%								FLL	176	ATL	115		MCO	80	ATL	80		BDA	62		BOS	62	BDL		
L10	88100%								0642		0820550	1003	1105	122152		1612150		1757	18441920							
015	88100%														ATL	194		EMR	87		FLL	60		JFK	721	FLL
L10	88100%													1023		1210	1335		1604	1720		1930	2055		2320	
016	88100%	56 TPA							EMR	801		FLL		800		EMR	825		ATL	761		MCO	120	ATL	156	
L10	88100%	2444							0850		11201200		1432	1540		1743	1848		2005	2105		2222		2330		

## VI. STAGE 2 - AUTOMATED DECISION SUPPORT

### INTRODUCTION OF AUTOMATED ALGORITHMS, EXPERT SYSTEMS

- to assist human schedulers with certain sub-problems
- to eliminate manual effort at certain steps of process
- to broaden search for optimal or good solutions to scheduling sub-problems
- may introduce mainframe, large scale optimization algorithms

### EXAMPLES OF EXISTING AUTOMATED DECISION SUPPORT ALGORITHMS

- a) Best cancellation of flights given breakdowns and spares
- b) Least revenue loss when reducing available fleet
- c) Optimal switching of flights between types of aircraft
- d) Automatic switching for transition to new schedule plan
- e) Automatic weekend schedule cancellations
- f) Automatic holiday period rescheduling
- g) Minimum fleet size for given services with time windows
- h) Automatic gate assignment at all stations
- i) Automatic aircraft rotation generation (with maintenance constraints)

## VI. AUTOMATED DECISION SUPPORT

- a) Best cancellation of flights given breakdowns and spares
- b) Least revenue loss when reducing available fleet

### Fleet Routing Models

- use network flow algorithms

#### OBJECTIVE:

Maximize Operating Income

#### GIVEN:

- Set of potential services to be flown with fixed operating times and known net operating income
- Daily ownership costs of aircraft
- Desired overnights
- Fixed number of available aircraft

#### OUTPUT:

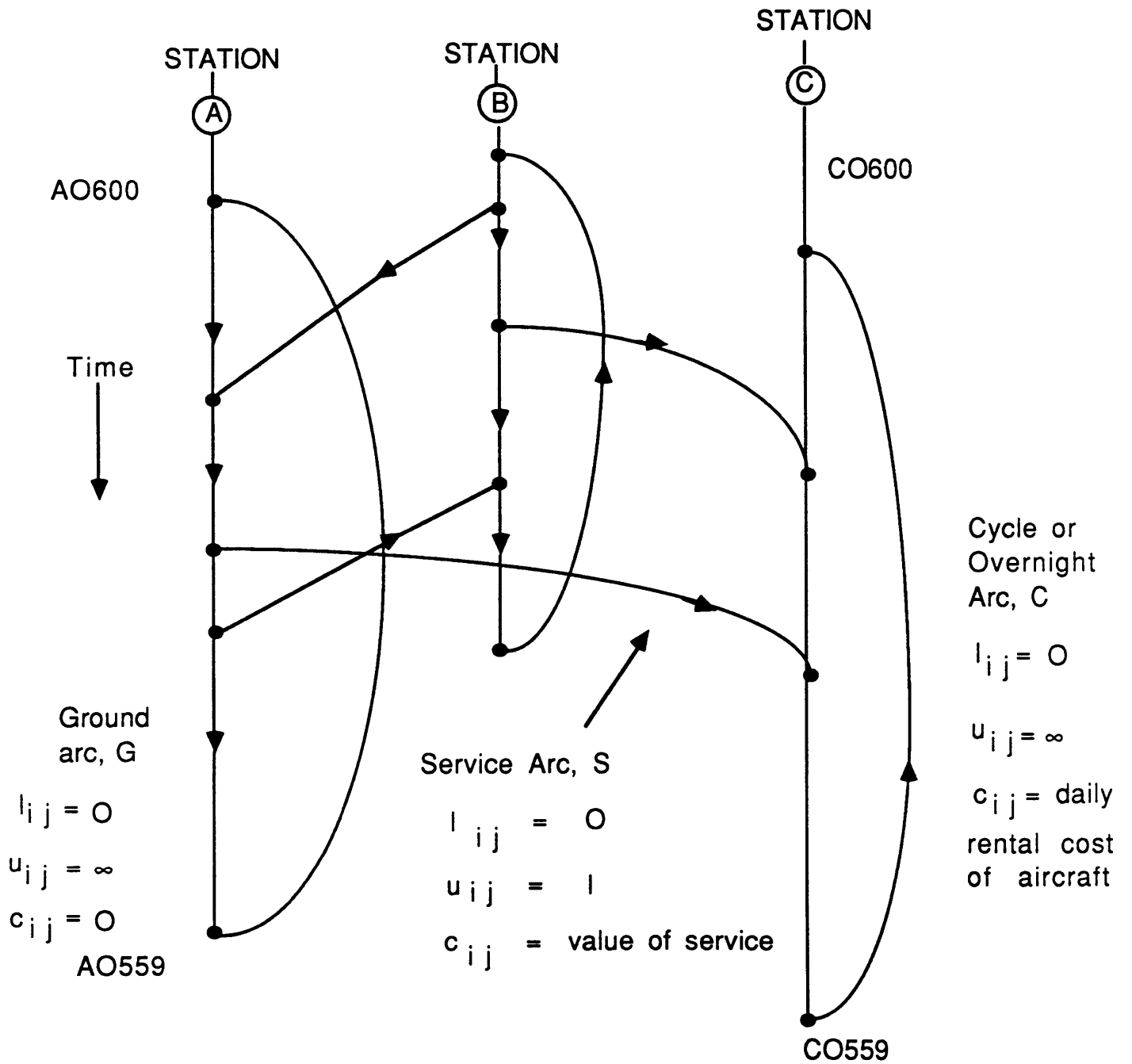
- "Best" services to be flown
- Marginal value for services not flown
- Marginal value of adding an aircraft to fleet

#### WEAKNESS:

- Fixed service times
- Fixed net income for services i.e. no spill if not flown
- Single type of aircraft-solved sequentially



# SCHEDULE MAP





OTHERS

REPORTS

EDIT

SEARCH

FILES

WINDOW

WEEKDAY

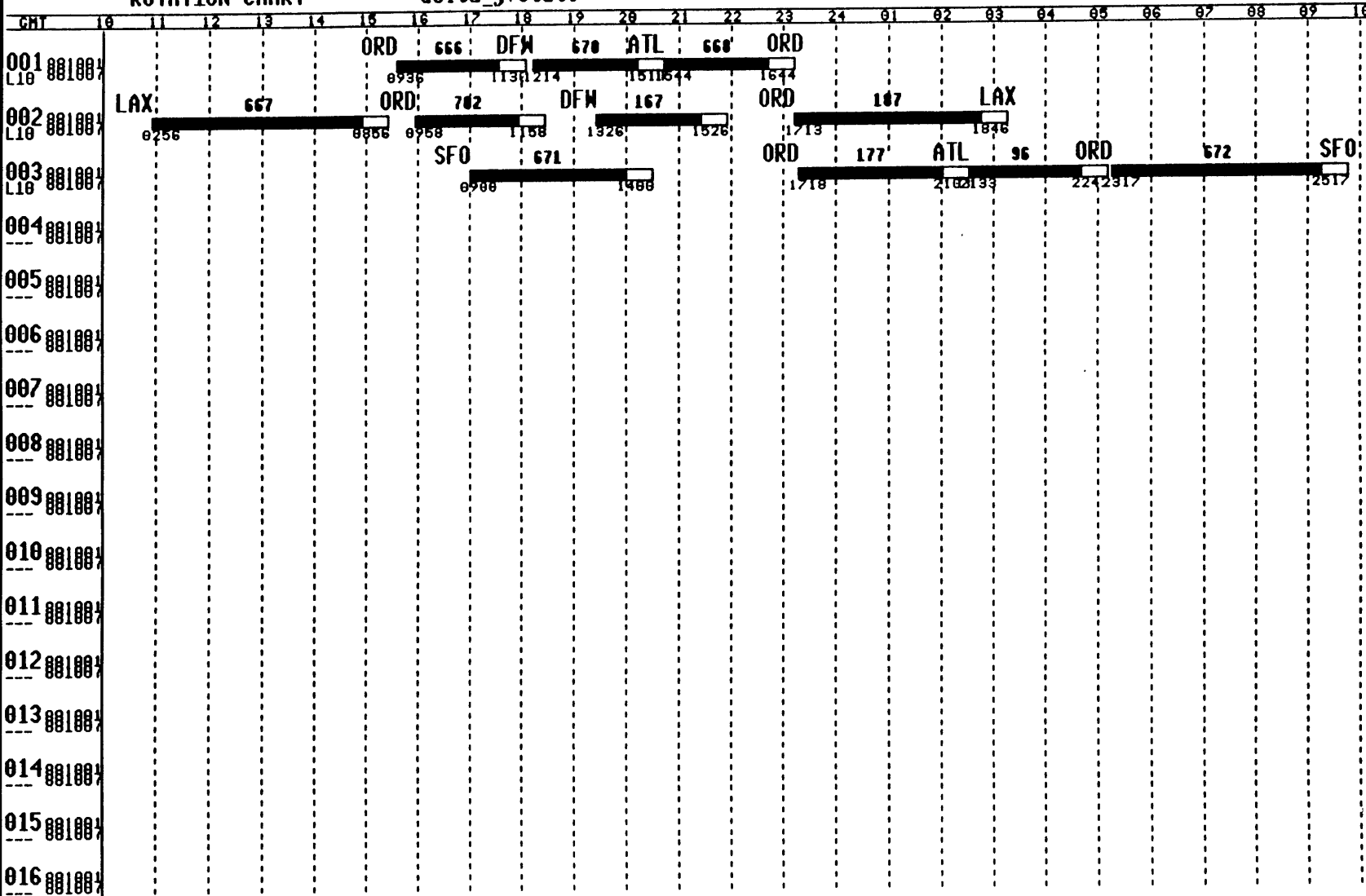
QUIT

ALGORITHM

ROTATION CHART

delta\_jvctst6

Monday





OTHERS

REPORTS

EDIT

SEARCH

FILES

WINDOW

WEEKDAY

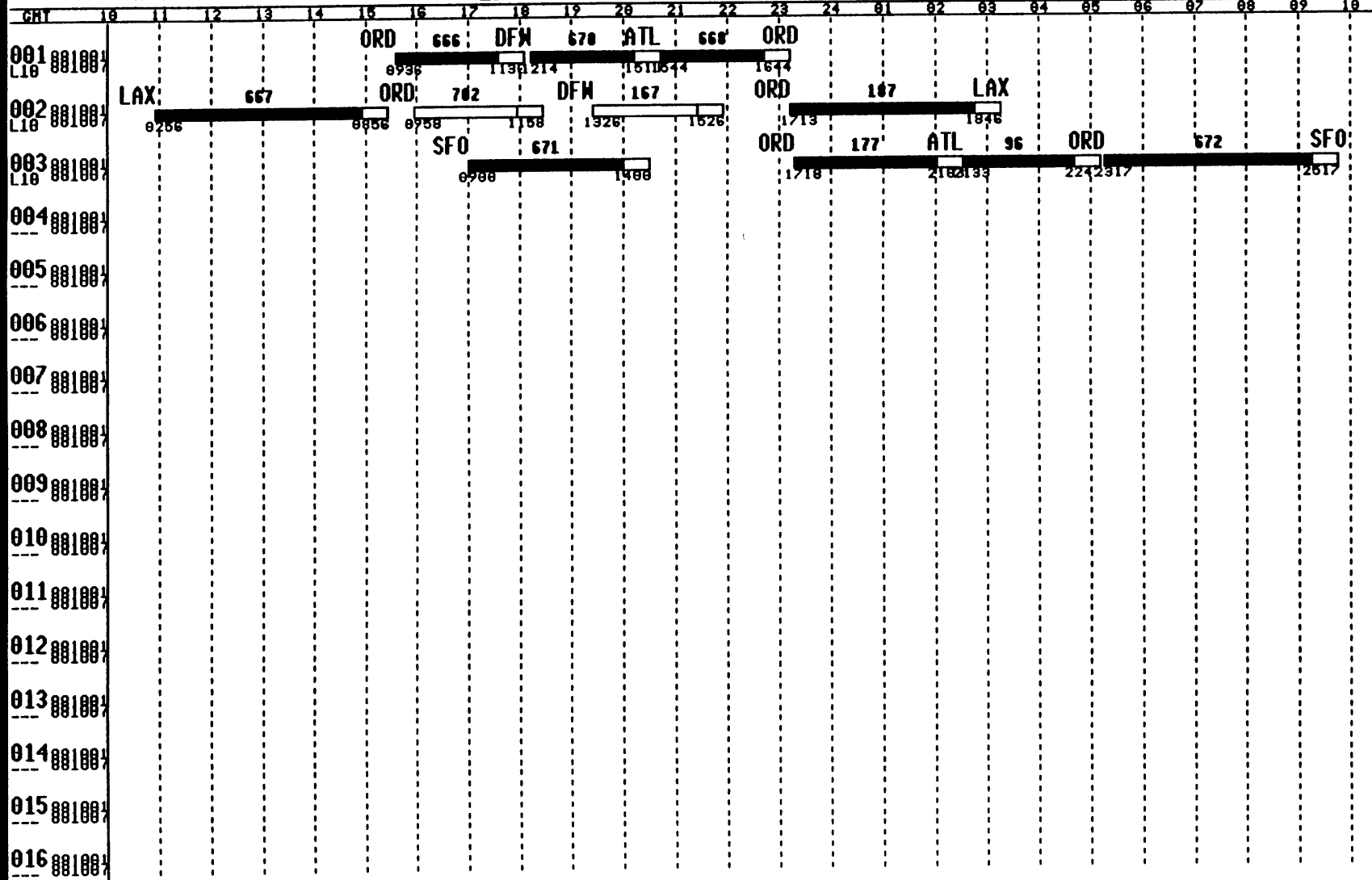
QUIT

ALGORITHM

ROTATION CHART

delta\_jvctst6

Monday



## VII. SUMMARY - STATE OF THE ART IN COMPUTERIZED SCHEDULING

### Conclusions

1. We cannot create analytical models which are adequate to describe mathematically the complete airline scheduling problem.
2. For existing models which promise utility, we generally do not have the correct data inputs, and it is difficult to conceive of creating the necessary models for passenger behavior in today's competitive markets. The existence of large scale solution techniques is not sufficient to justify their use at present.
3. We can provide quick, accurate answers to many sub-problems which occur in the complete scheduling process, but we need an environment which allows these techniques to be available to human schedulers. This environment is now available in the form of a network of computer workstations.
4. It is attractive to consider a single, integrated system to be used by various airline personnel as the scheduling process moves from initial planning to final execution.
5. People will remain an important part of the airline scheduling process. They are responsible for generating good schedules, and need "decision support" in their activities. There never will be a "push - button" scheduling system.
6. The desired approach is an incremental introduction of computerized assistance via graphic workstations. The strategy should be to create evolutionary stages:  
  
Stage 1 - Introduce the Scheduling Workstations  
Stage 2 - Introduce Automated Decision Support  
Stage 3 - Extend to real time Execution Rescheduling

VI. SUMMARY - STATE OF THE ART IN COMPUTERIZED SCHEDULING  
(con't)

7. The scheduling process is not permanent
  - as time goes by, the problems change (perhaps temporarily), and the markets evolve, and there will be emphasis on different aspects. It will not be possible to create a completely automated decision maker which keeps up with changes.
  
8. As these tools are developed, they have their impact on the Scheduling Process
  - it will change in its flow of information, the sequence of processing will change, and eventually the airline's organizational structures will change. The introduction of computer automation must be adaptive to allow these changes to occur.
  
9. Every airline will have to develop its own automated scheduling system and manage the evolutionary impact on its operations. There is no single, turnkey solution to be provided by outsiders. A conceptual, long term plan is needed to direct the evolutionary effort and prevent building an incoherent set of sub-systems.