A State Action Frequency Approach to Throughput Maximization over Uncertain Wireless Channels

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Abstract—We consider scheduling over a wireless system, where the channel state information is not available a priori to the scheduler, but can be inferred from the past. Specifically, the wireless system is modeled as a network of parallel queues. We assume that the channel state of each queue evolves stochastically as an ON/OFF Markov chain. The scheduler, which is aware of the queue lengths but is oblivious of the channel states, has to choose one queue at a time for transmission. The scheduler has no information regarding the current channel states, but can estimate them by using the acknowledgment history.

We first characterize the capacity region of the system using tools from Markov Decision Processes (MDP) theory. Specifically, we prove that the capacity region boundary is the uniform limit of a sequence of Linear Programming (LP) solutions. Next, we combine the LP solution with a queue length based scheduling mechanism that operates over long 'frames,' to obtain a throughput optimal policy for the system. By incorporating results from MDP theory within the Lyapunov-stability framework, we show that our frame-based policy stabilizes the system for all arrival rates that lie in the interior of the capacity region.

I. INTRODUCTION

In this paper, we consider the scheduling problem in a wireless uplink or downlink system, when there is no explicit instantaneous Channel State Information (CSI) available to the scheduler. The lack of CSI may arise in practice due to several reasons. For example, the control overheads, as well as the delay and energy costs associated with channel probing, might make instantaneous CSI too costly or impractical to obtain.

Our system consists of N wireless links, which are modeled as N parallel queues that are fed by stochastic traffic. We assume that only a single queue can be chosen at each time slot by the server for transmitting its data. The state of each wireless link is time-varying, evolving as an independent ON/OFF Markov chain. A given transmission is successful only if the underlying channel is currently ON.

Our basic assumption in this paper is that the scheduler cannot observe the current state of *any* of the wireless links. Nonetheless, when the scheduler serves one of the queues in a given time slot t, there is an ACK-feedback mechanism which acknowledges whether the transmission was successful or not, thereby revealing the channel state *a posteriori*. Since the channels are correlated across time by the Markovian assumption, this *a posteriori* CSI can be used for predicting the channel state of the chosen queue in future time slots.

The *capacity region* (or the rate region) of the system described above, is the set of all arrival-rate vectors that are stably-supportable by *some* scheduling policy. Our aim is to characterize the capacity region of the system, and to design a throughput optimal scheduling policy.

The general problem of scheduling parallel queues with time-varying connectivity has been widely studied for almost two decades. The seminal paper of Tassiulas and Ephremides [6] considered the case where both channel states and queue lengths are fully available to the scheduler. It was shown in [6] that the *max-weight algorithm*, which serves the longest connected queue, is throughput optimal.

Following this paper, several variants of imperfect and delayed CSI scenarios have been considered in the literature [2], [5], [7], [8]. However, our scheduling problem fundamentally differs from the models considered in these references. Specifically, no explicit CSI is ever made available to the scheduler, and acquiring channel state information is a *part of the scheduling decision* made at each time instant. This adds significant difficulties to the scheduling problem.

Two recent papers consider the scheduling problem where the CSI is obtained through an acknowledgment process, as in our model. In [1], the authors consider the objective of maximizing the *sum-rate* of the system, under the assumption that the queues are *fully-backlogged* (i.e., there is always data to send in each queue). It is shown that a simple *myopic policy* is sum-rate optimal. The suggested policy keeps scheduling the channel that is being served as long as it remains ON, and switches to the least recently served channel when the current channel goes OFF.

In [4], the authors propose a randomized round-robin scheduling policy for the system, which is inspired by the myopic sensing results in [1]. That policy is shown to stabilize arrivals that lie within an inner-bound to the rate region. However, the policy is *not* throughput optimal, and their method cannot be used to characterize the capacity region.

In this paper, we propose a throughput optimal scheduling policy for the system. In particular, the frame-based policy we propose can stabilize arrival rates that lie arbitrarily close to the capacity region boundary, with a corresponding tradeoff in the computational complexity. Our proof of throughput optimality combines tools from Markov decision theory within a Lyapunov stability framework. We also provide a characterization of the capacity region boundary, as the uniform limit of a sequence of LP solutions.

This paper is organized as follows. The model is presented in Section II. In Section III, we formulate a linear program
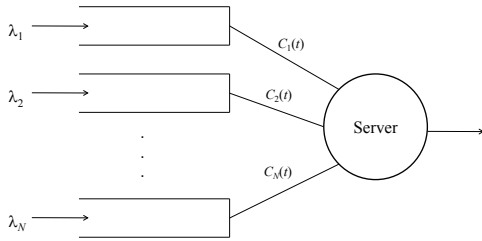
Fig. 1. A system of parallel queues served by a single server. The channels connecting the queues to the server are randomly time-varying.

Fig. 2. The Markov chain governing the time evolution of each of the channels state $C_i(t)$.

which leads to the characterization of the capacity region. In Section IV, we suggest the frame-based policy, which we prove to be throughput optimal. Proofs are omitted throughout due to space constraints, and can be found in [3].

II. System Description

The network model. We model the wireless system as consisting of N parallel queues (see Fig. 1). Time is slotted $(t = 1, 2, \ldots)$. Packets arrive to each queue $i \in \{1, 2, \ldots, N\}$ according to an independent stochastic process with rate λ_i. We assume that the arrival processes are independent of each other, and independent and identically distributed (i.i.d.) from slot-to-slot.

Due to the shared wireless medium, only a single transmission is allowed at a given time. In our queuing model, this is equivalent to having the queues connected to a single server, which is capable of serving only a single packet per slot. Each queue is connected to the server by an ON/OFF channel, which models the time-varying channel quality of the underlying wireless link. If a particular channel is OFF and the queue is chosen by the scheduler, the transmission fails, and the packet has to be retransmitted. If it is ON and chosen by the scheduler, a single packet is properly transmitted, and an ACK is received by the scheduler.

We denote the channel state of the i-th link at time t by $C_i(t) \in \{ON, OFF\}$, $i = 1, \ldots, N$. We assume that the states of different channels are statistically independent of each other. The time evolution of each of the channels is given by a two state ON/OFF Markov chain (see Fig. 2). Although our methodology allows for different Markov chains for different channels, we shall assume for ease of notation and exposition that the Markov chains are identically distributed across users. We further assume that $\epsilon < 0.5$, so that each channel is *positively correlated* in time.

Information structure. At each time t, we assume that the scheduler knows the current queue lengths $Q_i(t)$ prior to making the scheduling decision. Yet, *no* information about the current channel conditions is made available to the scheduler. Only *after* scheduling a particular queue, does the scheduler get to know whether the transmission succeeded or not, by virtue of the ACK-mechanism. The scheduler thus has access to the entire history of transmission successes and failures. However, due to the Markovian nature of the channels, it is
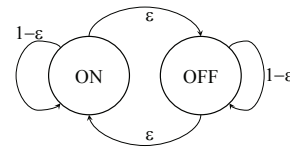
sufficient to record *how long ago* each channel was served, and the *state of the channel* (ON/OFF) when it was last served.

Scheduling objective. Given the above information structure, our objective is to design a scheduling policy that can support the largest possible set of input rates. More precisely, an arrival rate vector $\boldsymbol{\lambda} = (\lambda_1, \ldots, \lambda_N)$ is said to be *supportable*, if there exists some scheduling policy under which the queue lengths are finite (almost surely). The *capacity region* Γ of the system is the closure of all supportable rate vectors. A policy is said to be *throughput optimal* if it can support all arrival rates in the interior of Γ.

III. Optimal Policies for a Fully Backlogged System

In the interest of simplicity of notation and exposition, we restrict attention to the case of $N = 2$ queues in the rest of the paper, although our methodology extends naturally to more queues. In this section, we assume that the queues are fully backlogged, i.e., the queues never empty. As we shall see, our analysis of the fully backlogged system gives us insights about the optimal scheduling policy for the dynamic system with finite queues.

Since the queues are assumed to be infinitely backlogged in this section, the state of the system is completely specified by the state of each channel the last time it was served, and how long ago each channel was served. In a system with two fully backlogged queues, the *information state* during slot t has the form $\mathbf{s}(t) = [k_1(t), b_1(t), k_2(t), b_2(t)]$, where $k_i(t)$ is the number of slots since the queue i was served, and $b_i(t) \in \{0, 1\}$ is the state of the channel the last time it was observed.[1] Since the channels are Markovian, $\mathbf{s}(t)$ is a sufficient statistic for the fully backlogged system. Note that $\min(k_1(t), k_2(t)) = 1$, $\forall\, t$, and $\max(k_1(t), k_2(t)) \geq 2\ \forall\, t$. Let $\mathcal{S}$ denote the (countably infinite) set of all possible states $\mathbf{s}(t)$.

Denote the l step transition probabilities of the channel Markov chain in Fig. 2 by $p_{11}^{(l)}$, $p_{01}^{(l)}$, $p_{10}^{(l)}$, and $p_{00}^{(l)}$. It can be shown by explicit computation that for $l \geq 1$,

$$p_{01}^{(l)} = p_{10}^{(l)} = \frac{1 - (1 - 2\epsilon)^l}{2}, \quad p_{11}^{(l)} = p_{00}^{(l)} = \frac{1 + (1 - 2\epsilon)^l}{2}.$$

Next, define the *belief* vector corresponding to state $\mathbf{s} \in \mathcal{S}$ as $[\omega_1(\mathbf{s}), \omega_2(\mathbf{s})]$, where $\omega_i(\mathbf{s})$, $i = 1, 2$ is the conditional probability that the channel i is ON. For example, if $\mathbf{s} = [1, ON, 3, OFF]$, the corresponding belief vector is

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[1] Throughout, 0 is used interchangeably to denote the channel state OFF, and 1 is used to denote ON.

$[1 - \epsilon, p_{01}^{(3)}]$. It can be shown that the belief vector has a one-to-one mapping to the information state, and is therefore also a sufficient statistic for the fully backlogged problem.

In each slot, there are two possible actions, $a \in \{1, 2\}$, corresponding to serving one of the two queues. Given a state and an action at a particular time, the belief for the next slot is updated according to the following equation.

$$\omega_i(t+1) = \begin{cases} (1-\epsilon)\omega_i(t) + \epsilon(1 - \omega_i(t)), & \text{if } a(t) \neq i, \\ 1 - \epsilon, & \text{if } a(t) = i, \ C_{a(t)}(t) = 1, \\ \epsilon, & \text{if } a(t) = i, \ C_{a(t)}(t) = 0, \end{cases}$$

where we have abused notation to write $\omega_i(t) = \omega_i(\mathbf{s}(t))$.

A *policy* for the fully backlogged system is a rule that associates an action $a(t) \in \{1, 2\}$, to the state $\mathbf{s}(t)$ for each t. A *deterministic stationary* policy is a map from $\mathcal{S}$ to $\{1, 2\}$, whereas a *randomized stationary* policy picks an action given the state according to a fixed distribution $\mathbb{P}\{a|\mathbf{s}(\cdot)\}$.

Suppose that a unit reward is accrued from each of the two channels, every time a packet is successfully transmitted on that channel, i.e., when the server is assigned to a particular channel and the channel is ON. Given a state $\mathbf{s}(t)$ at a particular time, and an action $a(t)$, the probability that a unit reward is accrued in that time slot is simply equal to the belief of the channel that was chosen. We are interested in the long term time average rate achieved on each of the channels under a given policy. From the viewpoint of the reward defined above, the average rate translates to the infinite horizon time average reward obtained on each channel under a given policy.

We say that rate pair (λ_1, λ_2) is *achievable* in the fully backlogged system, if there exists *some* policy for which the infinite horizon time average reward vector equals (λ_1, λ_2). The closure of the set of all achievable rate pairs is called the *rate region* Λ of the fully backlogged system. It should be evident that a rate pair that is not achievable in the fully backlogged system, cannot be supportable in the dynamic system with random arrivals. Thus, the capacity region Γ of the queueing system is contained in the rate region Λ of the fully backlogged system. In fact, we show in Section IV that the two rate regions have the same interior, by deriving a queue length based policy for the original system that can stabilize any arrival rate in the interior of Λ. We now proceed to obtain an implicit characterization of the rate region boundary.

A. MDP formulation and state action frequencies

Let us consider a Markov decision process (MDP) formulation on the belief space for characterizing the rate region boundary.

It is easy to show that the rate region Λ is convex. Indeed, given two points in the rate region, each attainable by some policy, we can obtain any convex combination of the rate points by time-sharing the policies over sufficiently long intervals. Further, the rate region is also closed by definition. Therefore, any point on its boundary maximizes a weighted sum-rate expression. That is, if (r_1^*, r_2^*) is a rate pair on the boundary of Λ, then

$$(r_1^*, r_2^*) = \arg\max_{(\lambda_1, \lambda_2) \in \Lambda} w_1 \lambda_1 + w_2 \lambda_2 \quad (1)$$

for some weight vector $\mathbf{w} = [w_1, \ w_2]$, with $w_1 + w_2 = 1$. The following proposition shows that if the rate pair (λ_1, λ_2) is in Λ, then there must necessarily exist *state action frequencies* that satisfy a set of balance equations.

Proposition 1: Let $(\lambda_1, \lambda_2) \in \Lambda$. Then, for each state $\mathbf{s} \in \mathcal{S}$ and action $a \in \{1, 2\}$, there exists state action frequencies $x(\mathbf{s}; a)$, that satisfy

$$0 \leq x(\mathbf{s}; a) \leq 1, \quad (2)$$

the balance equations (3)-(6) (next page), the normalization condition

$$\sum_{s \in \mathcal{S}} x(\mathbf{s}; 1) + x(\mathbf{s}; 2) = 1, \quad (7)$$

and the rate constraints

$$\lambda_i \leq \sum_{\mathbf{s} \in \mathcal{S}} x(\mathbf{s}; i)\omega_i(\mathbf{s}), \ i = 1, 2. \quad (8)$$

Intuitively, a set of state action frequencies corresponds to a stationary randomized policy such that $x(\mathbf{s}; a)$ equals the steady-state probability that in a given time slot, the state is $\mathbf{s}$ and the action is a. Further, conditioned on being in state $\mathbf{s}$, the action a is chosen with probability $\frac{x(\mathbf{s}; a)}{\mathbb{P}\{\mathbf{s}\}}$, where $\mathbb{P}\{\mathbf{s}\} = x(\mathbf{s}; 1) + x(\mathbf{s}; 2)$. (If $\mathbb{P}\{\mathbf{s}\} = 0$, the policy prescribes actions arbitrarily).

Let us now provide an intuitive explanation of the balance equations. Equations (3)-(6) simply equate the steady-state probability of being in a particular state, to the total probability of entering that state from all possible states. For example, the left side of (3) equals the steady-state probability of being in the state $[1, b_1, k, b_2]$, $k > 2$, while the right side equals the total probability of getting to the above state from other states, and similarly for the other balance equations. Equation (7) equates the total steady-state probability to unity. Finally, in Equation (8), the term $x(\mathbf{s}; i)\omega_i(\mathbf{s})$ equals the probability that the state is $\mathbf{s}$, the action i is chosen, *and* the transmission succeeds. Thus, the right-side of (8) equals the total expected rate on channel i.

We now return to the characterization of the rate region boundary. In light of Proposition 1, Equation (1) can be rewritten as follows.

Problem INFINITE($\mathbf{w}$):

$$(r_1^*, r_2^*) = \arg\max_{(\lambda_1, \lambda_2)} w_1 \lambda_1 + w_2 \lambda_2 \quad (9)$$

subject to (2)-(8).

Since the state-space of this MDP is countably infinite, the optimization in (9) involves an infinite number of variables. In order to make this problem tractable, we now introduce an LP approximation.

B. LP approximation using a finite MDP

In this section, we introduce an MDP with a finite state space, which as we show, approximates the original MDP arbitrarily closely. The state action frequencies corresponding to the finite MDP approximation can then be solved as an LP.

$$x([1, b_1, k, b_2]; 1) + x([1, b_1, k, b_2]; 2) = x([1, b_1, k-1, b_2]; 1)(1-\epsilon) + x([1, 1-b_1, k-1, b_2]; 1)\epsilon, k > 2, \qquad (3)$$

$$x([1, b_1, 2, b_2]; 1) + x([1, b_1, 2, b_2]; 2) = \sum_{l \geq 2} x([l, b_1, 1, b_2]; 1)p_{11}^{(l)} + x([l, 1-b_1, 1, b_2]; 1)p_{01}^{(l)}, \qquad (4)$$

$$x([k, b_1, 1, b_2]; 1) + x([k, b_1, 1, b_2]; 2) = x([k-1, b_1, 1, b_2]; 2)(1-\epsilon) + x([k-1, b_1, 1, 1-b_2]; 2)\epsilon, k > 2, \qquad (5)$$

$$x([2, b_1, 1, b_2]; 1) + x([2, b_1, 1, b_2]; 2) = \sum_{l \geq 2} x([1, b_1, l, b_2]; 2)p_{11}^{(l)} + x([1, b_1, l, 1-b_2]; 2)p_{01}^{(l)}, \qquad (6)$$

First note that the belief of a channel that has not been observed for a long time increases monotonically toward the steady state value of 0.5 if it was OFF the last time it was scheduled. Similarly, the belief decreases monotonically to 0.5 if the channel was ON the last time it was scheduled. The key idea now is to construct a finite MDP whose states are the same as the original MDP, with the exception that the belief of a channel that remains unobserved for a long time is clamped to the steady state ON probability, 0.5. Specifically, when a channel has not been scheduled for τ or more time slots, its observation history is entirely forgotten, and the belief on it is assumed to be 0.5. The action space and the reward structure are exactly as before. We show that this truncated finite MDP closely approximates the original MDP when τ gets large.

Let us now specify the states and state action frequencies for this finite MDP. There are $4(\tau - 2)$ states of the form $[1, b_1, k_2, b_2]$, $2 \leq k_2 \leq \tau - 1$, $b_1, b_2 \in \{ON, OFF\}$ that correspond to the first channel being scheduled in the previous slot, and the second channel being scheduled less that τ time slots ago. In a symmetric fashion, there are $4(\tau - 2)$ states of the form $[k_1, b_1, 1, b_2]$, $2 \leq k_1 \leq \tau - 1$, $b_1, b_2 \in \{ON, OFF\}$ that correspond to the second channel being scheduled in the previous slot. Finally, there are 4 states $[1, b_1, \phi, \phi]$, $b_1 \in \{ON, OFF\}$ and $[\phi, \phi, 1, b_2]$, $b_2 \in \{ON, OFF\}$ in which one of the channels has not been seen for at least τ slots, and its belief reset to 0.5. Let us denote by $\hat{\mathcal{S}}$ the above set of states for the finite MDP, and let $\hat{x}(\mathbf{s}; a)$, $\mathbf{s} \in \hat{\mathcal{S}}$, $a \in \{1, 2\}$ denote the state action frequencies for the finite MDP. These state action frequencies satisfy normalization, balance equations, and rate constraints, analogous to (2)-(8).

For a fixed $\mathbf{w}$ and τ, let us now consider the following LP.

Problem FINITE(τ,$\mathbf{w}$):

$$(\hat{r}_1, \hat{r}_2) = \arg\max_{(\hat{\lambda}_1, \hat{\lambda}_2)} w_1 \hat{\lambda}_1 + w_2 \hat{\lambda}_2 \qquad (10)$$

subject to normalization, balance equations and rate constraints, analogous to (2)-(8).

The main result of this section shows that the *solution to this LP approximates the boundary point* specified by the problem INFINITE($\mathbf{w}$) for every $\mathbf{w}$, when τ is large.

Proposition 2: For a given $\mathbf{w}$ with $w_1 + w_2 = 1$, and τ, let $\hat{\boldsymbol{\eta}}(\tau, \mathbf{w})$ denote the solution to the problem FINITE(τ,$\mathbf{w}$), and let $\mathbf{r}^*(\mathbf{w})$ denote the solution to INFINITE($\mathbf{w}$). Then, $\hat{\boldsymbol{\eta}}(\tau, \mathbf{w})$ converges *uniformly* to $\mathbf{r}^*(\mathbf{w})$, as $\tau \to \infty$.

We next show a result that asserts that using the state action frequencies obtained from the finite MDP in the backlogged system entails only a negligible sub-optimality, when τ is large. The finite MDP solution is applied to the backlogged system as follows. If the state in the backlogged system is such that both channels were served no more than τ time slots ago, then we schedule according to the state action frequencies of that particular state in the finite MDP. On the other hand, if one of the channels was served more than τ time slots ago, the finite MDP would not *have* a corresponding state and state action frequencies. In such a case, we schedule according to the state action frequencies of one of the four states in the finite MDP in which the belief is clamped to the steady-state value. For example, if the system state is $[1, b_1, k_2, b_2]$, with $k_2 > \tau$, we schedule according to the state action frequencies of the state $[1, b_1, \phi, \phi]$ in the finite MDP, and so on.

Proposition 3: Suppose that the optimal state action frequencies obtained by solving the problem FINITE(τ, $\mathbf{w}$) are used to perform scheduling in a fully backlogged system, as detailed above. Let $\hat{\mathbf{r}}(\tau, \mathbf{w})$ denote the average reward vector so obtained. Then for every $\mathbf{w}$ with $w_1 + w_2 = 1$, we have that $\hat{\mathbf{r}}(\tau, \mathbf{w})$ converges *uniformly* to the optimal reward $\mathbf{r}^*(\mathbf{w})$, as $\tau \to \infty$.

We pause briefly to emphasize the subtle difference between Propositions 2 and 3. Proposition 2 asserts that optimal reward obtained from the finite MDP is close to the optimal reward of the infinite MDP. In this case, the optimal solution to the finite MDP is applied to the finite state-space. On the other hand, in Proposition 3, the optimal policy obtained from the finite MDP is used on the original *infinite* state-space, and the ensuing reward is shown to be close to the optimal reward. From a practical perspective, Propositions 2 yields a characterization of the rate region, while Proposition 3 plays a key role in the throughput optimality proof of the frame-based policy in Section IV.

C. An Outer Bound

We now derive an outer bound to the rate region Λ, using 'genie-aided' channel information. Although the bound is *not* used in deriving our optimal policy, it is of interest to compare the outer bound we obtain to existing bounds in the literature.

Consider a fictitious, fully backlogged system in which the channel processes follow the same sample paths as in the original system. However, after a channel is served in a particular time slot, a genie reveals the states of all the channels in the system. Therefore, at the beginning of a time slot in the fictitious system, the scheduler has access to *all* the
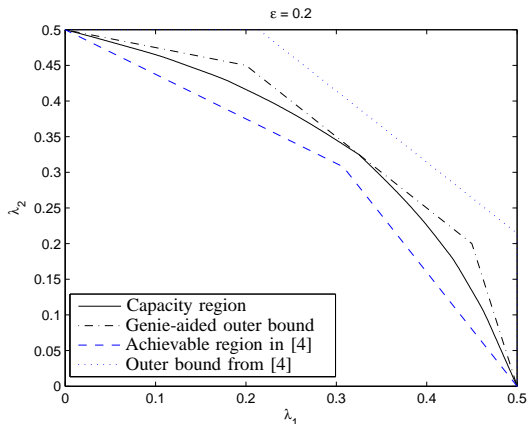
Fig. 3. The capacity region, our outer bound, and the inner and outer bounds derived in [4], for $\epsilon = 0.2$.

channel states in the previous slot, and not just the channel that was served. Clearly, the rate region for the genie-aided system, denoted by $\overline{\Lambda}$, is an outer bound to the rate region of the original system. The boundary of the region $\overline{\Lambda}$ can be explicitly characterized (see [3]) in terms of ϵ:

$$\overline{\Lambda} = \left\{ (\lambda_1, \lambda_2) \middle| \begin{array}{c} \epsilon\lambda_1 + (1-\epsilon)\lambda_2 \leq (1-\epsilon)/2; \\ (1-\epsilon)\lambda_1 + \epsilon\lambda_2 \leq (1-\epsilon)/2; \\ \lambda_1 + \lambda_2 \leq 3/4 - \epsilon/2 \end{array} \right\}. \quad (11)$$

D. Numerical Example

In this section, we use the finite LP approximation obtained in Section III-B to numerically compute and plot the capacity region for a two queue system. Specifically, we use the solution to the problem FINITE(τ,**w**) with large enough τ, which, according to Proposition 2, uniformly approximates the rate region boundary for all **w**. We also plot the genie-aided outer bound obtained above, and compare the rate region and our outer bound to the inner and outer bounds derived in [4].

Fig. 3 shows the numerically obtained rate region, the genie-aided outer bound, and the inner and outer bounds derived in [4] for our symmetric two queue system with $\epsilon = 0.2$. The capacity region, shown with a dark solid line, was obtained by solving the LP approximation FINITE(τ, **w**) for all weight vectors, and large enough τ. The dash-dot curve in the figure is our genie-aided outer bound. The achievable region of the randomized round-robin policy proposed in [4], is shown by a dashed line. Finally, the outer most region in the figure is the outer bound derived in [4].

Interestingly, we observe that the genie-aided outer bound is tight at the symmetric rate point; see [3] for details.

IV. A THROUGHPUT OPTIMAL FRAME-BASED POLICY

In this section, we return to the original problem, with finite queues and stochastic arrivals. We propose a throughput optimal queue length based policy that operates over long 'frames.'

In our frame-based policy, the time axis is divided into frames consisting of T slots each, and the queue lengths are

updated at the beginning of each frame. Given the queue length vector $\mathbf{Q}(kT)$ at the beginning of each frame, the idea is to maximize a weighted sum rate quantity over the frame, where the *weight vector is the queue length vector* for that frame. The weighted rate maximization is, in turn, performed approximately by solving the finite MDP. Intuitively, the above procedure has the net effect of performing max-weight scheduling over each time-frame, where MDP techniques are employed to compute each of the 'optimal schedules.' More precisely, our policy operates as follows.

FRAME-BASED POLICY:
  (i) At the beginning of time frame k, update the queue length vector $\mathbf{Q}(kT)$.
 (ii) Compute the normalized queue length vector $\tilde{\mathbf{Q}}(kT)$, whose entries sum to 1.
(iii) Solve the problem FINITE($\tau, \tilde{\mathbf{Q}}(kT)$) and obtain the state action frequencies $\hat{x}(\mathbf{s}, a)$, $\mathbf{s} \in \hat{\mathcal{S}}, a \in \{1, 2\}$.
(iv) Schedule according to the state action frequencies obtained in the previous step during each slot in the frame.

The main result of this paper is the throughput optimality of the frame-based policy, for large enough values of T and τ. Specifically, our frame-based policy can stabilize all arrival rates within a δ-stripped region of Λ, for any $\delta > 0$. As we shall see, a small δ could require large values of T and τ, which increases the dimensionality of the LP (depends on τ) as well as the average delay (depends on T). Thus our policy offers a tradeoff between computational complexity and delay on the one hand, and better throughput on the other. Our main theorem is stated below. Note also that our policy requires queue length information only at the beginning of each frame.

Theorem 1: Given any $\delta > 0$, there exist large enough τ and T such that the frame-based policy stabilizes all arrival rates in the δ-stripped rate region $\Lambda - \delta\mathbf{1}$.

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