ANALYSIS AND CLASSIFICATION OF MICROPROGRAMMED COMPUTERS

by

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ABSTRACT

A representation scheme is developed to represent microprogrammed computers for easy comparison. Design trade-off issues on ROM word dimensions, control store timing and bit encoding are analyzed. Also a summary of some microprogrammed computers is presented.

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1. Introduction

In the past the control section of a computer is implemented by an interconnection of logic elements. This interconnection of logic elements is hardwired, and little or no change can be incorporated easily into the design later on. Recently a new trend in control logic design, known as microprogramming, gradually replaces the conventional method of designing the control section. More and more computers nowadays are microprogramcontrolled.

With these thoughts in mind this thesis is written to analyze and classify or represent micro-programmed computers. The analysis focuses on some important tradeoff issues in the design of a microprogrammed control. The representation attempts to represent any general microprogrammed computer. The organization of the thesis is outlined as follow:

First the concept of microprogramming is introduced in chapter 2. Then a representation scheme for microprogrammed computer is proposed in chapter 3. In Chapter 4 three trade-off issues in the design of microprogrammed control are analyzed. Finally in chapter 5, summaries of some major micro-programmed computers are presented in terms of the representation scheme developed previously.

2. MICROPROGRAMMING

2.1 Why Microprogramming

In recent years microprogramming has replaced the conventional logic design for the control section of a digital computer. For one reason, microprogrammed implementation of a computer provides desirable flexibility in modifying or changing machine operations. Not only does it facilitate the design of the control section, but it also makes the maintenance and service of the machine a lot easier than the non-microprogrammed machine. All these have become a reality as a result of current technology even though microprogramming was known in the early fifties. But what is microprogramming?

2.2 What is Microprogramming?

Microprogramming is a systematic method to implement the control section of a modern digital computer system. Functionally a computer system may be divided into four units: the control unit, the arithmetic and logic unit, the main memory unit, and the input and output unit. This is shown in Figure 2.2.1.

Traditionally the control unit is realized by the interconnection of logic gates, flipflops, counters, rings, clocks, etc., all of which are hardwired together to





generate a sequence of control signals. Should the operation call for changes, a different sequence of control signals has to be generated, involving a considerable reconfiguration of the hardwares. This is inflexible and <u>ad hoc</u>. In order to provide a more flexible and more systematic design method than the traditional one, Wilkes (2) advocated the idea of microprogramming. Here we consider all the sub-machine level operations that are performed to carry out (interpret) the machine operations. For example a register-to-register addition instruction¹, a machine instruction, may be interpreted by the following sequence of sub-machine level operations:

- #1. ADDRESS OF REG 1 TO LOCAL MEMORY ADDRESS REGISTER
 (LMAR)
- #2. TRANSFER CONTENT OF REG 1 TO ADDER INPUT 1
- #3. ADDRESS OF REG 2 TO LMAR
- #4. TRANSFER CONTENT OF REG 2 TO ADDER INPUT 2
- #5. SET THE ADDER TO ADD
- #6. TRANSFER THE SUM FROM THE ADDER OUTPUT TO THE LOCAL MEMORY REGISTER (LMR)
- **#7.** ADDRESS OF REG 1 TO LMAR
- #8. WRITE THE CONTENT OF THE LMR INTO THE LOCAL MEMORY

Here all the registers are in a fast local memory, see Figure 2.2.2, which shows a section of a microprocessor (i.e. a processor that is microprogrammed). IFor example a 360 AR instruction



ADDER MODE : ADD, SUBTRACT, ETC.

Figure 2.2.2 A Section of Microprocessor

Each of the above basic sub-machine level operation is known as a micro-operation. Some other examples of micro-operation are other arithmetic or logical operations, shifting, counting, decrement, increment, register to register. register to bus transfer, and main memory request. Now the designer will gather all the necessary micro-operations for the machine he is designing. Analogous to a programmer's preparation of a program, he will formulate a microprogram to execute all the required machine opera-The microprogram is a sequence of microtions. instructions each of which may have one or more microoperations. Most of the micro-instructions are executed in one small time period. This is called the processor cycle time (pc). Some, like a main memory request, may require two pc's, or three pc's, or more, as present day main memory speed is still behind the central processor processing speed. This accounts for the main memory cycle time (mc) of usually two pc's or more. In order to avoid any waiting for the required data, a fast but costly main memory may be used. An alternative is to employ a relatively smaller but faster buffer memory in addition to the slow main memory storage.

Generally the microprogram is stored in some form of read-only memory (ROM) as a sequence of ROM words, see

Figure 2.2.3. A ROM word format is in Figure 2.2.4 The ROMAR contains the address of the ROM word to be read out The control levels from ROMDR go to the rest in ROMDR. of the CPU to initiate various micro-operations. While some portion of ROMDR goes to the branch and decision to set up the next ROM word address, with the help from the The ROM and its associated access me-CPU conditions. chanisms is also called the control store unit. Its cycle time is the control store cycle time (cc). Notice that there is a high level of parallelism existing in the microprocessor. If necessary, the adder, the shifter, the counter, the fast local memory and/or main memory requests can all be activated at the same time. An illustration is the example 4.1 given in section 4.1.

Also the micro-operations are of very basic primitive operations. Therefore microprogramming is on a much lower level than even machine instruction programming. As a result we can perform a variety of tasks with unusual speed and efficiency: semaphore manipulation, hardware special algorithm (like a square root algorithm), emulation, microdiagnastics, etc. These are some advantages of microprogramming, others are listed next.

2.3 Advantages of Microprogramming

The advantages of microprogramming are discussed with



Figure 2.2.3 A General Microprocessor Configuration

•



Figure: 2.2.4 ROM word format

respect to four view points. First, from a system architectural view point, the system architecture can be changed completely, for example by emulation, or extended, where variable instruction set is allowed. If the machine instructions were microprogrammed, a large set of instructions can be implemented for a small system at a low cost. Second, microprogrammed control makes logic designs systematic, uniform, and with ease. It is more tractable to check out the system than the conventional design, which is hardwired control.

Third, microprogrammed controls takes up very small space, and it is easy for maintenance. Microdiagnostics is superior to software diagnostics because of faster speed and closer resolution. Fourth, microprogramming is also economical viable after certain point in increasing logic complexity. An economic model for microprogrammed logic has set up by Bersner and Mills of IBM (15), and the conclusion is as follow,

In summary, a crude economic model has been used to compare the cost of conventional circuits with the cost of stored logic to perform the same data processing functions. The results indicate that there is a point at which, with increasing complexity, the cost of stored logic becomes less than the cost of conventional circuits. This cross-over point may occur at a relatively low degree of complexity. This model can be explored further but the validity of many of the assumptions and approximations does not warrant any further analysis of it.

An intuitive illustration of this model is shown in Figure 2.3.1.

Disadvantages of Microprogramming

From the architectural and economical views, microgrammed control is too expensive to justify for a small system in which basic repetitive tasks are performed. As far as performance is concerned, microprogrammed control may be slow if appropriate overlap between the control store cycle and the processor cycle is not established. This overlap issue will be discussed quantitatively in section 4.2. Finally there is a hardware cost increase due to ROM and access mechanisms.

2.4. Other meaning of Microprogramming

Microprogramming is also used to denote programming using machine instructions whose bits are used directly to control logic gates in the computer. In a sense the programmer and the logic designer are combined into one. This term has been used in the Lincoln Laboratory, and in the work done by Van der Poel (9). Also refer to (10) for comments on the two types of microprogramming. This secondary meaning of microprogramming is not oftenly used. In general the primary meaning of microprogramming is that of Wilkes, who introduced microprogramming in the 1950's.



Figure 2.3.1 Economic model

2.5 Present Status of Microprogramming

In deed technology played a big role in recognizing the importance of microprogramming, which was first noted back in the early 1950's (1), largely credited to Wilkes (2). For a period of time it remained an idea and received little attention in both the academic and industrial worlds. Recently in the 60's, a new interest has shown (3). This can be seen in the increased number of articles and technical reports on microprogramming and on issues closely related to it (3). Text books begin to mention microprogramming (4,6); some universities even offer courses on this subject area.

In 1964, IBM announced its System/360, a family of architecturally compatible computers, that is a programmer can write one program for all these computers, because they are functionally the same to him, even though the internal hardware configuration of each computer may be quite different (13). All of the then announced computers except the largest (model 70) are microprogrammed. This is followed by the appearance of a number of other systems that employs this same design philosophy. For example, the RCA Spectra/70, the Honeywell H 4200/H8200, and Burroughs 2500 and 3600. Some small microprogrammed computers are Standard Computer Corporation (SCC) IC-model 9,

Micro 800, and Meta 4 Series 16 (5). Some of the current machines with writable control stores are Interdata Model 3, SCC/C-model 9, and IC-9000, IBM 2025, and IBM 2085.

3. A REPRESENTATION SCHEME FOR MICROPROCESSOR

The present trend in computer logic design is that more and more computers are microprogrammed. Facing with any two microprocessors, how does one compare them? This question is not trival unless one is content with digesting the computer manuals for both microprocessors. Before going into the microprocessor system, it is profitable to examine the representation schemes used in other systems and to see how comparisons are made.

3.1 Review of representation schemes

In this section several system representation schemes are reviewed. First the system of electrical networks is examined. In elementary circuit analysis basic building blocks are resistors, capacitors, inductors, sources, and some nonlinear devices. A network is then synthesized by the interconnection of appropriate basic building blocks. The circuit may be described by differential equations containing the voltage and current as variables. Given any two circuits one may examine their topologies and their differential equation descriptions. Therefore comparison may be made between two circuits. In the same manner it is possible to describe a microprocessor in terms of circuits. The description, however, may be too

detailed for understanding and hence not useful to describe a microprocessor.

A second possible representation is that of logic design. Its components are AND, OR, NOT gates. The system is governed by the properties of the components and by the laws of boolean algebra. To compare two logic designs, one merely compares the circuits consisting of the logic components, or one may compare the boolean equations. A microprocessor can be represented by this network of logic components. But even at this level the description may be still too minute to allow easy comparison of two microprocessors.

A higher level description than logic design is that of register transfer language (RTL). Currently RTL is used as a primitive microprogramming language (12). In this respect RTL is closer to the description of a microprocessor than the previous two schemes of representation.

Another related scheme of representation is a computational model called the program graphs (16). It can represent precise description of parallel computations of arbitrary complexity on nonstructured data. The program graph is a directed graph consisted of nodes and links. While the modes represent computation steps, the links represent storage and transmission of data and/or control information. The focus here is on computation,

but the hardware structures are relegated to secondary position of importance. This is rather on contrary to microprogramming, in which knowledge of the hardware is essential. Improvement in this respect is included in another computational model called a computation schema (11).

A basic computation schema consists of two parts: the data flow graph, and the precedence graph. The former represents the data paths in terms of directed links joining deciders, operators, and cells. Being a directed graph, the latter prescribes the order of computation in the data flow graph in term of operator, instance nodes, conditional nodes, and iteration nodes. The schemata described emphasize the notions of concurrency and parallelism. It is powerful in that it can represent processors of arbitrary complexity. To represent a computation, one gives its corresponding data flow graph and precedence graph. In order to represent computations within a microprocessor, the precedence graph will be very elaborate and may challenge the ease of understanding.

On the other hand there exist macroscopic descriptions of computer systems. The processor-memory switch (PMS) and the instruction-set processor (ISP) are two new language developed by Bell and Newell to describe

computer systems (6). The PMS represents major hardware units in a processor. Its basic components are the processor, memory, switch, and control unit. At the ISP level a processor is described completely by giving the instruction set and the interpreter of the processor. The interpreter is in terms of its operations, data-types, and memories. As the name as well as the language indicates, both PMS and ISP are too macroscopic to describe the microprocessor. For example, the processor, and control units are basic components in the PMS description. However, the interest here is to know more about the processor and the control units themselves, not as unit components, but as systems themselves.

3.2 A representation scheme for microprocessor

The previous representation schemes are adequate in their own domain of description. As far as representing microprocessor is concerned they are inadequate. Either the representation scheme is too detailed and thus becomes too complicated; or too restricted, as in the program graphs and computation schemata; or too macroscopic, as in the PMS and ISP. In the case of microprocessor the focus is on its general characteristics which involves issues like the following: flexibility of data path, how many buses it has, how many working register it has, what

are the data transfer restrictions, what are the timing relationships, etc.

With the needs mentioned above, a representation scheme is proposed here to represent a microprocessor. The scheme has three components: the structure representation, the transfer constraint, and the cycle time. First the structure representation component is presented. It conveys the general hardware structure of the micro-The general hardware structure refers to the processor. conventional central processor hardwares, which includes the arithmetic and logic unit, with the working registers, the high speed local memory, and the control unit - ROM and associated hardware mechanisms. Also, buffer (or cache) memory unit, main memory unit, and input output unit are represented. Besides representing the general hardware structure. the structure representation also indicates the general data flows within the microprocessor. This realization is to be done with the minimum amount of complexity shown in the representation.

The general hardware structure of a microprocessor is abstractly represented by a set of passive and active elements. Active elements represent hardware units that performs transformations on data, and in general are denoted by (), or (f). While the former represents

any active element, the latter represents an active element whose data transformation is f. In other word. the output of this element is f(A) if the input is A, where A is usually a one-dimension or two-dimension vector input. Examples of active elements are shown in Figure 3.2.1. Passive elements, on the other hand, represent hardwares which perform no transformation on data but merely act as storage places for data. They are denoted by capital letters, or capital letters with subscripts which further denote the names or other properties of the hardware represented by this passive element. An example of passive elements is R, which represents a register. Another example is R_A , which represents register A. Other examples are given in Figure 3.2.2. Notice that the elements may represent a whole hardware unit or a portion of it. This provides flexibility in representing hardware components: from that of a simple increment operator to that of a whole arithmetic and logic unit, for example. Also notice in Figure 3.2.1 that a whole input output unit and interface together with some data transformation capability may be consider as an active element and is denoted by Other information concerning the elements may be given separately to supplement this part of the structure representation. This is shown in the example given in



Figure 3.2.1 Active elements

R	:	Register		M	:	Memory
RA	:	Register A		M _M	:	Main or primary memory storage
RCON	:	Console register		ML	:	Fast local memory
R _{CB}	:	Channel buffer regist	er	MU	:	Rom or control store
				MB	:	Buffer or cache memory
			MBCC	N	:	Console buffer
			ML		:	Input output local storage
			MB		:	Input output buffer

L : Latch

S : Staticizer

Figure 3.2.2 Passive elements

section 3.3.

To indicate the general data flows within the microprocessor, a set of links is used to connect graphically all the passive and active elements which represent the hardware structure of the microprocessor. This set includes the following three links:

The first link, a dotted link, is used to represent addressing an element by another element. For example a memory M addressed by an address register R, see Figure 3.2.3a. The second link is any data transmission path. The third link is common transmission path called a bus. Figure 3.2.3b and c illustrate the use of the second and the third links. Notice that the abstract links do not necessarily contain a width dimension, which may be given as in Figure 3.2.3c. This is consistent with the hardware representation elements which denote no width dimension. The interconnection of passive and active elements by the connecting links constitutes the structure representation, the first component of the microprocessor representation scheme proposed here.



Figure 3.2.3 Connecting links

The transfer constraint

The second component of the microprocessor represenration scheme is called the transfer constraint. This component can reveal all the detailed data flows and hardware structures within the microprocessor. It exhibits the nature of the micro-operations defined in conjunction with this microprocessor. If the micro-operations are simple and basic, microprogramming is easy and may have flexible implementation of machine instructions. If they are highly specialized, microprogramming may be difficult. Also what matters most in a microprocessor is the micro-operations that are allowed. All these information is contained in the ROM word format. Therefore the transfer constraint is denoted by the format of a ROM word together with explanation of all the fields of the ROM word. Consequently the transfer constraint conveys more information than that mentioned before.

In addition, the transfer constraint tells the sequencing of ROM words. It shows the emit field, that is the constant field, and its size. As far as the micro-operations are concerned, the transfer constraint lists the mutually exclusive micro-operations defined by the hardwares and by the designers of the microprocessor. An example of the transfer constraint is shown in section 3.3. The transfer constraint, together with the structure,

is still not complete. It requires the third component as well to complete the representation scheme.

The cycle time

Even though the transfer constraint conveys a vast amount of information, it has no notion of any timing relationship whatsoever. For example, a certain combination of bits in a field of the ROM word is for making main memory read operation. This does not tell how long it will take to get the data from the main memory.

It is true in a microprocessor that most hardware operations are of time durations equal or less than the processor cycle time. In these cases, knowledge of the timings may not be necessary. In a main memory request, it is necessary to know how long it takes to get the data so that other operations may be performed on it. Usually the main memory is slower than the CPU processing speed. Similarly is the case for the local memory store. Its cycle time is critical for application of some microoperations. The main memory and local memory cycle times are not the determining factors for the system performance. Partly the performance depends on the processor cycle time. It is obvious that if two processors are identical except for the processor cycle time then their relative performance is determined by their relative processor cycle time.

Finally the control store cycle time also determine the performance.

Therefore we must know the cycle times for the processor, the control store, the main memory, and the local memory. This is the third component of the microprocessor representation scheme, the cycle time CT. CT is a set of cycle times including the above four times and any related cycle times. An example of the related cycle time is the cycle time of a buffer or cache memory.

CT = { pc,cc,mc,lmc, buffer memory cycle, others}

Finally a representation scheme for microprocessor has been proposed here. How adequate is this scheme with its three components, the structure representation, the transfer constraint, and the cycle time? This representation is adequate in the following manners: First, the interconnection of elements by links provides the basic hardware structure of the microprocessor. Also it indicates the general data flows within the micropro-Second, any detailed interconnection can be cessor. found in the transfer constraint component, which contains much information which any block diagrams lack. Third and last, the major timing relationships in the processor are given in terms of four or more cycle times. Other timings, on that of a circuit level, are not crucial to understand

the system structures and the general data flows.

To illustrate the representation scheme, an example is given next.

3.3. An example

This example is from a hypothetical microprocessor represented in Figure 2.2.3. It is represented here by the scheme just mentioned. The three components are as follow:

Structure representation,	see	Figure	3.3.1.
Transfer constraint,	see	Figure	3.3.2.
Cycle time,	see	Figure	3.3.3.

Notice in the example given in Figure 2.3.1., R_M is introduced as main memory data register. Similarly, R_F and R_{CTR} are introduced. It should be realized that new elements in the structure representation may be introduced as shown in the example. Another piece of information is given in the structure representation to supplement the elements. Specifically the memory storages, M_L, M_U, M_P , are given together with their storage size. ML:32x32 points to a 32 - word local memory where each word has 32 bits. In the cycle time, 180 ns is the cycle time of the processor; 200 ns, that of the control store; $1\mu_S$, that of the main memory; and 150 ns, that of the local memory storage. Structure representation:



 ${\rm R}_{\rm M}$: Main memory data register ${\rm R}_{\rm F}$: Local memory data register

 M_{L} : 32 x 32 M_{U} : 2k x 32 M_{M} : 256k x 8

R_{CTR} : Counter register

Figure 3.3.1

Transfer constraint:



Figure 3.3.2

Cycle time :

 $CT = \{180 \text{ n sec }; 200 \text{ n sec }; 1 \mu \text{ sec }; 150 \text{ n sec} \}$

Figure 3.3.3

4. SOME TRADE-OFF ISSUES

In the example given in section 2.2, which is portion of a microprogram, we have eight micro-operations. It is possible then to have eight micro-instructions, each one containing a single micro-operation, taking 8 pc's of time to execute the register-to-register add instruction. An alternative approach, using parallelism, can accomplish the same result in five micro-instructions, taking 5 pc's. In this case the first micro-instruction has one microoperation (#1); the second, two (#2,#3); the third, two (#4, #5); the fourth, two (#6, #7); the fifth, one (#8). If we implement each micro-instruction by a word, we may have eight words, or five words for our register-toregister add instruction. Clearly the widths of the words (bit dimension, or horizontal dimension) are different in both cases, since the latter approach requires the ability to specify two micro-operations in one microinstruction. Hence the bit dimension is also a consideration in the design other than the word dimension (or vertical dimension) which is the number of words used. There are more words in the first implementation than in the second one, but the second one uses more bits per word than the first, see figure 4.0.1. This issue has been mentioned qualitatively in (4). In the next section,





a quantitative analysis of this trade-off is given. Two other trade-off issues are covered in sections 4.2 and 4.3.

4.1 Horizontal and vertical dimensions of ROM words

As the above example has shown, one of the design issues is to determine the width of the ROM word and the number of ROM words. If the horizontal dimension is increased, the performance is improved because fewer words are needed to implement a particular instruction. However, increase in width invokes high cost as a result of memory increase, ROM data register bits increase, access mechanisms increase. On the other hand a decrease in width implies an increase in the number of ROM words used. Cost is reduced because more ROM words only calls for cost in memory; no access mechanisms are involved. Now the performance is degraded as more words are needed to implement the instruction. The trade-off problem here is to choose the optimum horizontal and vertical dimensions for lowest cost and at the same time meets the performance requirement.

To formulate this trade-off problem in precise terms, the following assumptions and definitions are taken:

A set of micro-operations, $\{\dots, m_{j}, \dots\}$ is established as the most primitive hardware operations in the microprocessor. Each machine instruction i is to be implemented

by choosing micro-operations from the set. A particular machine instruction may consist of following sequence:

m1, m2, m3; m6, m9, m10, m13^{*}; m7, m8, m14, m15, m16, m4, m5, m19, m20; m30, m31, m32, m37, m50.

The above sequence may be executed in at least four consecutive instances of times (steps). Each step performs different number of micro-operations; three in the first step, four in second step, nine in the third, and five in the fourth. This sequence of steps is abbreviated as

{3, 4*, 9, 5}
or in general,

{n_{i1}, n_{i2}, n_{i3}, ..., n_{ij},... }

for a particular machine instruction i which can perform as many as n_{i1} micro-operations simultaneously in the first step, as many as n_{i2} in the second step, and so on. The execution order of the steps as given must be kept, as results in a previous step may be needed by micro-operations in the current step. $n_i j$ indicates branching is to be performed.

The total cost of the ROM and its associated access mechanisms is no more than C, the cost constraint.

There is a speed requirement, S_i , for each machine instruction. Machine instructions include basic machine

instructions like binary, decimal, floating point, logical instructions, and system instructions like V operation, or P operation. Also there is no sharing of ROM words among machine instructions.

Let T be the processor cycle time. As the width of the ROM increases, T has a slight increase because word drive pulse has to propagate a longer path. For this analysis T is assumed to be constant over the range of x that is of interest.

Let a be the cost per bit for ROM word access mechanism and its associated hardware and design cost. Hardwares here include ROM data register, ROM field decoders and drivers, and sense amplifiers.

Let g(k) be the cost per word for a word of k bits. Here g(k) involves just memory cost and therefore is much smaller than a k. Then g(k) = k b, where b is the cost of memory per bit.

Finally let

x be the number of bits per word

y₁ be the number of words for machine instruction i. y be the total number of words for all machine instructions.

Then the first trade-off issue can be formulated as

Minimize f = xa + y x b

Subject to the following constraints:

 $f \leq C$ $y_{i}T \leq S_{i}$ $x \leq \max \max n_{ij}$ $x \geq \min \min n_{ij}$ $y_{i} \equiv \sum_{j} \left[\frac{n_{ij}}{x}\right]$

where $\begin{bmatrix} \underline{u} \\ \overline{v} \end{bmatrix}$ is an integer such that $\begin{bmatrix} \underline{u} \\ \overline{v} \end{bmatrix}$ $\mathbf{v} \ge \mathbf{u} \ge \begin{bmatrix} \underline{u} \\ \overline{v} \end{bmatrix} \mathbf{v} - \mathbf{v}$ Notice also $\mathbf{y} = \sum_{\mathbf{i}} \mathbf{y}_{\mathbf{i}}$.

There are at least three methods to solve this minimization problem. It may be solved as a non-linear programming problem. Or it can be first linearized and then solved as a linear programming problem. Lastly it may be solved by a tabulation method. Since x is bounded from both ends as shown in the constraints, f may be found by computing all y_i 's for every x within the bounds. Example 4.1 below will illustrate this tabulation method.

Example 4.1. Given four machine instructions 1,2,3,4, and their $n_{i,j}$ sequences,

{3, 4^{*}, 9, 5 } , { 3, 5^{*}, 8^{*}, 6, 2 } , {3, 11^{*}, 2^{*}, 1 } , { 3, 4, 13^{*}, 4 }

Also, a=50 units of cost

g(k) = 2k units of cost $S_1 = S_2 = S_3 = S_4 = 5$ C = 80

Solution by tabulation method:

f = 50x + 2xy

x = 8, see Figure 4.1.1.

It can be seen from the example above that not all x's between the maximum x and the minimum x need to be tested. Only those that are included in the Nij's need to be tested.

The assumption that there is no sharing of ROM words among machine instruction may be reconsidered now. If indeed there is sharing e.g. a common subroutine, the analysis may be carried out in two parts. The first part optimizes the common subroutine; the second part, the nonsharing portions of the instructions.

This then constitutes a formal treatment on the ROM word dimensions trade-off. The next issue concerns the timings for a microprocessor.

4.2. Timings for a microprocessor

In a microprocessor, there are at least three timing cycles: the main memory cycle time (mc), the processor cycle time (pc) and the control store cycle time (cc).

							the second se	
x	y ₁	y ₂	y ₃	У ₄	y= y _i	2 xy	50 x	f
13	4	5	4	4	17	442	650	1092
11	4	5	4	5	18	396	550	946
9	4	5	5	5	19	342	450	792
			e	E	20	320	400	720
6	5	6	5	5	21	2.52	300	552
5	5	7	6	6	34	240	250	490
4	7	8	6	7	28	224	200	424
3	8	9	7	10	34	204	150	354

x=8

Figure 4.1.1. Example 4.1

Here the issue is how are the three cycle times chosen and what relationships are there between them, if any.

Ideally the pc is given below,

where $t(m_i)$ is the time required by micro-operation $m_i \in \{\dots m_i \dots\}$ as defined in 4.1, excluding main memory request. This means that any micro-operation can be executed in one pc'.

The cc on the other hand is

 $cc = t_a + t_c + t_1 + pc' + t_1 + t_b$

Where t_a is the access time to the control store (CS).

t is the CS decode time.

 t_1 is the transmission time from the decoder to the rest of the cpu.

t_b is the branch and address decision delay, as shown in Figure 4.2.1. The branch and address decision reflects the current cpu conditions and cny test results before accessing the next ROM word.

Since $cc - pc' = t_a + t_c + 2t_1 + t_b \ge 0$, the processor is idle during this portion of the control store. The objective is to reduce the difference between cc and pc'. One way to do it is to use fast circuits and fast transmission cables so that t_a , t_c , t_1 , and t_b are made as small as possible. This is a rather brute force method. Another methods are given below.

Overlap method

This method is to overlap the cc with the pc'. The analysis following will show how much overlap should be taken so that the performance requirement Si for each machine instruction is still met.

Assume the overlap is S, as shown in Figure 4.2.2. For no branching in the microprogram, the effective cc is

 $cc' \equiv cc-S = t_a + t_c + 2t_1 + pc' + t_b - S$ For branching in microprogramming the effective cc is

$$cc" \equiv \left[\frac{cc}{cc - S} \right] \quad cc' \equiv kcc'$$

where $\begin{bmatrix} \underline{a} \\ \overline{b} \end{bmatrix}$ means $\begin{bmatrix} \underline{a} \\ \overline{b} \end{bmatrix}$ $b \ge a \ge b \left(\begin{bmatrix} \underline{a} \\ \overline{b} \end{bmatrix} - 1 \right)$, since the status

of the cpu is only known in the latter microprogrammed word after approximately a cc. As far as branching is concerned, S should be as small as possible. Also an increase in S implies the system has to keep track of conditions for more and more processor cycles simultaneously. This will increase the complexity of the system.

Therefore we want to minimize S

subject to the following constraints:

 $y_1^2 cc' + y_1^1 cc'' \le Si$ for every machine instruction i $S \ge 0$

where $y_{i}^{1} = Ui + Vi$



A Control storage configuration

Figure 4.2.1 A control storage configuration



Figure 4.2.2 Overlap of S for cc.

Ui = number of
$$n_{ij}^*$$
 in y_i
Vi = {1, if last n_{ij} is n_{ij}^* , or if last n_{ij} is not
the k th item in the last k grouping of n_{ij} 's.
(See Multiple access for groupings of n_{ij} 's.)
0, otherwise

 y_1^2 = number of n_{ij} 's not included in y_1^1 and there must be no overlap between same t_i 's from different ROM cycles, $t_i \in \{ t_a, t_c, t_l, pc', t_b \}$ This can be solved as a linear programming problem to get the optimum value of S. Or it may be solved by taking value of k from 1 to n, for some n, and list the constraints for each k to get the optimum S.

Now the effective pc = cc' = cc - S, while the control store cycle time still is cc.

Example 4.2 Use example 4.1 with x = 8, performance requirement: $S_1 = 3.8$; $S_2 = 4$, $S_3 = 3.7$, $S_4 = 3$. Since x = 8, possible micro-instruction sequence for the four machine instructions are:

{3, 4*, 5, 4, 5, }, {3, 5*, 4, 4*, 2 },
{3, 7, 4*, 2*, 1 }, {3, 4, 8, 5*, 4 }
See Figure 4.2.3.

Multiple access

Another approach to design the pc and cc is to assume that multiple TOM access mechanisms can be implemented to access more than one ROM words. The trade-off here is the minimum number of ROM words accessed versus the cost in

			48		
		y ₁	у ₂	^у 3	y 4
k=1		5cc	50 c	5cc	500
k=2	u	1	2	2	1
	v	1	1	1	1
	y _i '	2	3	3	2
	y _i ²	3	2	2	3
y ² cc'+yi	cc'	7cc' =3.5cc	8ec ' =4cc	8cc* =4cc	7cc ' =3.5cc
k=3	u	1	2	2	1
	v	0	1	1	1
	y,'	1	3	3	2
	y _i 2	2 4	2	2	3
y ² cc'+y	'cc ' '	7cc' =2 1/3cc	11cc' =3 2/3cc	11cc* =3 2/3cc	9cc • =3cc
k=4	u	1	2	2	1
	v	1	1	1	1
	y _i '	2	3	3	2
	y _i 2	2 1	2	2	3
y ² cc'+y	'cc•'	9cc ' =2 1/4cc	3 1/2cc	3 1/2cc	2 3/4 cc

Figure 4.2.3 Example 4.2

			49		
		y 1	y ₂	^y 3	y 4
k=5	ú	1	2	2	1
	v	1	1	1	1
	y'	2	3	3	2
	y _i 2	1	2	2	3
y ² cc'+y	' ^{'cc} ''	2 1/5cc	3 2/5cc	3 2/5cc	2 3/5cc

. k=3 is optimum

pc	=	cc'	=	cc	-	S	=	<u></u>	=	<u> </u>
								k		3

Figure 4.2.3 Example 4.2 (cont.)

the number of access mechanisms used.

let w be the number of ROM words accessed at one time. It is desired to

Minimize w

Subject to the following constraints:

 $g_{i}^{W} cc_{1}(w) \leq S_{i} \forall$ machine instruction i w Ca \leq CA

where $cc_1(w) = cc + (w - 1) pc'$

Ca is the approximate cost of the access mechanisms for a single ROM word.

CA is the total cost allowed for access mechanisms Given a sequence of micro-instructions n_{ij} for a machine instruction i, grouping of n_{ij} is by k starting with lowest j. Each grouping either has k or less n_{ij} 's. For the latter case the last n_{ij} must be a n_{ij}^* or it is not the k th item in the last k grouping of n_{ij} 's. Let g_{k}^{k} be the number of such groupings $g_{k}^{W} = g_{k}^{kj}$

 g_{i}^{k} be the number of such groupings. $g_{i}^{w} = g_{i}^{k}|_{k=w}$ Therefore the optimum w will give the optimum $cc_{1}(w)$ = cc + (w-1) pc'.

Now the speed gain is clear because w pc"s are sharing one (cc - pc') instead of 1 pc' sharing one (cc - pc') in a single BOM access strategy.

Example 4.3 Given 4 machine instructions with n_{ij} 's as follow:

{3,4*,9,5} ,{3,5*,8*,2} ,{3,11*,2*,1} , {3,4,13*,4} x = 8, performance requirement: S1 = 3.8, S2 = 4, S3 = 5, S4 = 6; CA = 3Ca. Finally, pc' = 1/3(cc - pc'), or pc' = ¼ cc. Solution by tabulation method : See Figure 4.2.4.

The underlines indicate the grouping of multiple access. In the above example the optimum solution is w=2.

It is important to realize that the performance Si may be relaxed so that only certain desired machine instructions have the performance constraints Si's, as long as the total performance is under certain limit, that is $y_i T \leq Si$ for $i \in \{ \begin{array}{c} \text{desired machine ins-}\\ \text{truction } i \\ \} \end{array}$

 $\sum_{i} y_{i} T \leq i$ Si

are used instead of the stricter constraints of

 $y \stackrel{T}{=} Si$ machine instruction i.

So far the discussion involves only pc and cc. Now mc will be considered. There is really no basic dependence between mc and pc, or between mc and cc. However, it is desirable to have mc = pc so that there is no waiting when data is required. If mc = 2pc's or more, there is a performance loss of 1 pc or more everywhere there is a main memory request and that this can not be moved earlier by 1 pc or more (or equivalently by 1 ROM word or more). Since x=8, possible N_{ij} sequences are as follow:

$$3,4^{*},5,4,5 \quad 3,5^{*},4,4^{*},2 \quad 3,7,4^{*},2^{*},1 \quad 3,4,8,5^{*},4$$

$$w=1 \quad 5cc_{1}(1) \quad 5cc_{1}(1) \quad 5cc_{1}(1) \quad 5cc_{1}(1) \\ w=2 \quad 3,4^{*},5,4,5 \quad 3,5^{*},4,4^{*},2 \quad 3,7,4^{*},2^{*},1 \quad 3,4,8,5^{*},4 \\ \quad 3cc_{1}(2) \quad 3cc_{1}(2) \quad 4cc_{1}(2) \quad 3cc_{1}(2) \\ =3 \quad 3/4 \quad cc_{c}(1) \quad =3 \quad 3/4 \quad cc_{1}(1) \quad =5cc_{1}(1) \quad 3/4cc_{1}(1)$$

$$w=3 \quad 3.4^{*}, 5.4.5 \quad 3.5^{*}, 4.4^{*}, 2... \quad 3.7.4^{*}, 2^{*}.1.1 \quad 3.4.8, 5^{*}.1 \quad 4... \\ 2cc_{1}(3) \quad 3cc_{1}(3) \quad 3cc_{1}(3) \quad 3cc_{1}(3) \\ =3cc_{1}(1) \quad =4 \ 1/4cc_{1}(1) \quad =4 \ 1/4cc_{1}(1) \quad =4 \ 1/4cc_{1}(1) \\ =4 \ 1/4cc_{1}(1) \quad =4 \ 1/4cc_{1}(1) \\ =4 \ 1/4cc_{1}(1) \quad =4 \ 1/4cc_{1}(1) \\ =4$$

Figure 4.2.4 Example 4.3

Hence there is strong dependence between pc and cc but little or no dependence of either one with mc. The next issue on trade-offs is on how much encoding.

4.3 Encoding of ROM bits

Finally we will deal with the encoding problem for the ROM fields. Encoding saves bits and hence cost, but it increases control line delay time because it requires time to decode.

The assumptions are the following:

- . A group of mutually exclusive lines are to be encoded (n).
- . If a line is not encoded, its cost is Cw.
- If a line is one of j encoded lines, its cost is
 (log₂j) Cw.
 The cost of decoding is offset by the saving resulting
 from the reduction of ROM bits.
- . A cost limit Co is imposed, and $(\log_{2^n}) C_w/_n \leq C_0 \leq nC_w$
- . Decoding delay is approximately linear with the number of lines encoded, i.e.

 $\Delta tj = jT_0$

where tj is the j - out put decoder delay; T_0 is a very small number.

Associated with each line is ti and Ti, where ti is the delay time of line i without encoding. Ti is the maximum delay for line i whether it is encoded or not.

The problem of encoding M lines out of $_{\rm N}$ lines is to maximize M

subject to the following constraints:

ti + $\Delta t_M \leq Ti$ \forall line i that is encoded

 $(n - M) Cw + (\log_2 M) Cw/M \leq Co$

 $M = 2^k$, where k is an nonnegative integer.

Example 4.4 Encoding problem for group of 8 mutually exclusive control lines. The following information is given:

Cw = 10; Co = 60; t1 = 7, t2 = 6, t3 = 8, t4 = 9, t5 = 4,t6 = 6, t7 = 7, t8 = 6; T1= 10, T2 = 9, T3 = 10, T4 = 15, T5 = 10, T6 = 9, T7 = 14, T8 = 13

Maximize M subject to ti + tM = ti + M \leq Ti (8 - M) 10 + (log₂M) 10/M \leq 60 M = 2^k

Solution by tabulation: See figure 4.3.1. For M = 2, $60 + \frac{1}{2}10 = 65 \nleq 60$ 4, $40 + \frac{2}{4}10 = 45 \le 60$ 8, $80 \qquad \pounds 60$ M = 4 on lines 4, 5, 7, 8 X marks indicates that a line may be encoded for a particular M.

i	t _i	Τ _i	M=2	M=4	M=8
1	7	10	x		
2	6	8	x		
3	8	9	x		
4	9	15	x	×	
5	4	10	x	x	
6	6	9	x		
7	7	11	x	x	
8	6	12	x	x	

Figure 4.3.1 Example 4.4

5. SUMMARIES OF MICBOPROCESSORS

The summaries of microprocessors are given here in term of the representation scheme developed in chapter 3. Each microprocessor is summarized in three components: 1) the structure representation, 2) the transfer constraint, and 3) the cycle time. This serves to illustrate the representation scheme as used on some major microprogrammed computers. Another purpose is for ready comparison of microprocessors. The machines given below include the ones from Honeywell, IBM, RCA, and Univac:

- H4200 : Medium-to-large business data processing. Figure 5.0.1.
- IBM 360/40 : Medium-to-small general purpose processing. Figure 5.0.2.
- IBM 370/155 : Medium high performance general purpose processing. Figure 5.0.3.
- RCA SPECTRA/70: Medium general purpose processing. Figure 5.0.4.
- UNIVAC C/SP: Medium communication processing. Figure 5.0.5.









3)

CT: { 125 n sec, 125 n sec, 750 n sec, 125 n sec }



M_L: 144 × 22 M_M: 16K × 262 K BYTE M_M: 4K TO 8K × 56

RDCP: Direct control present register









BREAK-IN : CHANGING CPU MODE TO I/O MODE CONTROL OR VICE VERSA

IOPR.....I/O PRIVITY_REQUEST _ I/O MODE ONLY IOSSB.....I/O STAT SETTING B _ I/O MODE ONLY LSWK.....LOCAL STORE WRITE _ IMO LSRD.....LOCAL STORE READ _ IMO IMISC.....I/O MISCELLANEOUS _IMO IOSS.....I/O STAT SETTING _ IMO IODF.....I/O DATA FLOW CONTROL _ IMO

3) CT: $\{115n \text{ sec; } 115 \text{ n sec; } 2.07 \text{ ,u sec FOR } M_p (16BYTE); 230 \text{ n sec FOR } M_B$ 58 n sec; 230 n sec(4 BYTES) $\}$





fields

- #of bits 2) AEU F 3 BASIC AEU FUNCTION
 - V 4 VARIATION OR FARTHER SPECIFICATION OF F
 - C 8 COUNTER CONTROL FIELD
 - M_L & M 2 M_L CONTROL TO VARIOUS R'S HARDWARE S 6 M_L ADDRESS OR SOURCE REGISTER REGISTER D 6 SOURCE OR DESTINATION REGISTER
 - BRANCH T 6 ANY ONE OF 63 SPECIFIC TEST CONDITION CONTROL N 6 NEXT EO ADDRESS IN ROM IF TEST FALSE
 - A 6 NEXT EO ADDRESS IN ROM IF TEST TRUE
 - E 5 FOR EXCEPTION CODE
 - I 1 FOR I/O SERVICE INTERVENTION

3) CT: $\{480 \text{ n sec}, 480 \text{ n sec}, 1.44 \mu \text{ sec}, 480 \text{ n sec} \}$ or 960 n sec



3) CT:
$$\{630, 270/570, 630, \approx 150\}$$

6. Conclusion

A background in microprogramming has been presented to introduce a representation scheme and the trade-off issues. An understanding of a microprocessor is persued in two aspects: internal and external. First the internal aspects of a microprocessor are taken up in the three trade off issues analyzed. The three issues are the ROM word dimensions, the timing relationships within the microprocessor, and the encoding of ROM bits. Second the external aspects of a microprocessor are taken up in the representation scheme, which is consisted of three components: the structure representation, the transfer constraint, and the cycle time. The representation scheme attempts to represent a microprocessor in concise terms for easy comparison with other microprocessors.

The analysis done in chapter 4 may be reconsidered now. Many assumptions are idealized to bring out the prominent deciding factors in the trade-offs. No attempts have been made to cover all the factors. It can be seen from the formulation of the trade-off problems that other factors contributing to the design may be easily incorporated. This only lengthens the process of analysis. As for the representation scheme, it is only a scheme to represent the microprocessor. This may serve as an

introduction to a more superior scheme.

It is hoped that the analysis of the trade-off issues may provide concrete guidelines and directions in some practical design problems in microprogramming. Though other trade-off issues have not been covered, the approach presented here may be applied to them as well. Finally it is hoped that the thesis can stimulate interest in microprogramming and its related areas.

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