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## RESEARCH OBJECTIVES AND SUMMARY OF RESEARCH

The primary research interest of this group is in the real-time acquisition and processing of visual information for display to the visual and nonvisual senses, and in the psychology of human utilization of such information, for both communication and control. The motivation is an interest in human capabilities for information processing and in human information requirements. Applications include sensory-aids systems for the blind and the blind-deaf, picture-transmission systems, and special information-display systems for enhancement of human performance under conditions of stress.

Major projects now in progress include studies on reading machines, picture processing, pattern recognition, and automatic processing of visual data of significance in studies of biology and medicine.

1. Reading Machine Studies

Research during the past few years in the Cognitive Information Processing Group of the Research Laboratory of Electronics has led to the construction and operation of an experimental reading system for the blind. In its present configuration the system consists of a document-handling carriage, a flying-spot opaque scanner, a digital scanner control unit, and a general-purpose medium-sized computer (PDP-1). Focusing, black-and-white threshold setting and document loading are manually controlled by a sighted operator. The scanner control unit operating under control of the computer program reports coordinate letter contour and other statistical information of the view in the scanner field. This information is used for the generation of signatures that are searched in a signature table for the identification of the letters. The signature table is built up through training sessions. Identified letters are spelled out, one at a time, through the use of digitized speech samples. The present output rate of the spelled

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speech is 60-80 words per minute. Experience has indicated an identification error rate of approximately 0.3% with a type font which the machine has been trained on.

One long-term objective is to provide a real-time connected speech output for the reading machine. The steps required are the translation of English words in conventional spelling into phonetic spellings, the addition of intonation to utterances and the generation of synthetic speech. Other intermediate forms of outputs are also contemplated.

Another objective for future research is to develop a field version of a reading system and evaluate its characteristics under conditions of actual use by blind subjects. This will involve consideration of the problems encountered by a blind operator in the adjustments of focus and threshold, the alignment of the document, and in specifying which portion of the text is to be read next. Naturally, considerable research will be required both on the hardware and software of the present reading system before a field version is to be designed and constructed.

#### a. Character Recognition

The character recognition algorithm used in the reading machine system described above is being tested on several other type fonts, including news print. Variation of this and new algorithms will be investigated with a view toward further simplification and applicability to multiple type fonts. Consideration will also be given to the problems of broken and touching letters.

#### b. Opaque Scanners

The character recognition work thus far has been carried out with a scanner that has a small field of view and is fairly slow. Work will proceed on other types of scanners which will allow less sophisticated document handling and a faster throughput of characters.

#### c. Tactile Displays

Two tactile displays are under development, both of which are two-dimensional arrays of Braille-like tactile "dot" elements, in which each dot is either present or absent, according to external control. The first display, made up of solenoid-controlled poke probes, has a size of  $6 \times 8$  and is designed to present a Braille-like cell to each of 8 fingers. The second display is of the "moving-belt" variety, with size  $64 \times 128$ , and a frame rate of three or more per minute. These displays will be used as tactile outputs for the reading-machine system and also for general studies of tactile pattern perception, both dynamic and static.

#### d. Spelled-Speech Storage, Display, and Compression

Spelled-speech offers a slower, but simpler, auditory display than artifical speech. Under construction are magnetic and optical storage and read-out of the spoken-letter sounds, and the compression of spelled speech by sampling in sections, temporal truncation, and temporal-overlap superposition has been examined.

#### e. Phonetic Translation of English Text

The transliteration of spelled English words into phonetic spellings depends on the use of morphographemic rules, morphophonemic rules, as well as syntax and semantics. Although the dependence on semantics is relatively weak in an engineering sense, the dependence on syntax is heavy, in that intonation (a suprasegmental feature of speech such as English) cannot be determined without a certain amount of syntactic analysis. The problem of the selection of important morphographemic, morphophonemic, and syntactic rules, and the make-up of an accompanying morpheme lexicon are crucial to the generation of connected speech from text string input.

#### f. Artificial-Speech Generation

Rapid human adaptation to a sentence of synthesized speech under repeated exposure makes it very difficult for the experimenter himself to judge the quality and performance of his synthesizer and the procedure used. A facility that allows the experimenter to input phonetic strings to the synthesizer and to manipulate the procedure parameters easily should allow better artificial speech to be synthesized. The development of the equipment and the accompanying computer program is part of the reading-machine research effort.

#### g. Real-Time Data-Processing Facilities

Work continues on the development of real-time remote input-output subsystems that make it possible for two small general-purpose digital computers to be utilized simultaneously and cooperatively in the reading-machine system, one computer being mainly occupied with scanner control, character recognition, phonetic translation, and the other with the generation of speech from phonetic symbolic input.

F. F. Lee, D. E. Troxel, S. J. Mason

#### 2. Picture-Processing Studies

Picture-processing research is concerned principally with processing and encoding picture signals for efficient transmission, subject to a quality constraint in the received picture. Subsidiary matters concern picture processing for quality improvement or for feature recognition.

a. Picture Quality

Our long-range goal is to develop objective measures correlating with subjective rating of picture quality. As a preliminary goal, we need to establish subjective rating on a more satisfactory basis. At present, it is not possible to compare such evaluations made on different systems, using different subjects, different observers, at different times. To facilitate such comparison, we plan to produce a new set of standard subjects. For each subject we shall produce a set of standard photographs in which the quality and data rate are varied, and in which, for each data rate, the system parameters have been varied, for optimum quality. The system will be PCM, with additive random noise of uniform probability distribution. These sets of pictures should permit accurate evaluation of quality and coding efficiency of new systems by a matching process.

#### b. Picture Coding

During the past year, we have made good progress on picture compression by twodimensional contour coding. A technique has been developed for artifact-free reconstruction of pictures from the two-dimensional gradient or Laplacian. In the coming year, emphasis will be placed on more efficient coding and interpolation techniques for transmitting the contour data. Some effort may also be put into coding of textural information.

## c. Optical Image Processing

Our principal interest is in using optics as a tool for picture processing. In particular, we are interested in developing links between digital computers and coherent optics so that the two can be used to complement each other. Applications under consideration include matched-filter detection, and holographic television systems.

W. F. Schreiber, T. S. Huang

### 3. Pattern-Recognition Studies

"Pattern Recognition" is a common theme underlying the projects described above, whether the task is accomplished by human cognition, by computer data processing or, most commonly, by a combination of the two.

Complementary to the task-oriented projects, the following research studies in the general area of pattern recognition are being carried out.

## a. Psychophysics of Depth Perception

This project is designed to provide information on a subject's ability to make accurate distance and orientation judgments with respect to real and illusory threedimensional objects. The variation of such judgments will be studied without feedback, as well as with a continuous auditory or visual error signal.

## b. Effects of Spatial Transformation of Text upon Reading and Writing

## Performance

It has been shown that systematic transformations or printed text (such as inversions or rotations of letters and of words) produce regular changes in the learning rate, as well as in the asymptotic reading rate. These studies are being extended to a wider class of transformations and also to reading and writing performance, with cursive script used as the text.

#### c. Automatic Extraction of Information from Printed Sheet Music

With the aid of the scanner and ancillary equipment developed for the projects described above, it is possible to program a computer to determine note value, duration, phrasing, and certain other music indicators from ordinary printed sheet music. This study is being continued to see what additional parameters can be extracted by automatic recognition.

#### d. Cognitive Processes - Language Comprehension

Research will be directed toward clarifying the nature of the quick perception and comprehension of written information by studying how normal and speed readers interpret words and sentences presented tachistiscopically. The ability to detect various syntactic and semantic differences between a known sentence and a briefly presented one will be especially studied.

## e. Visual Perception and Eye-Movement Relations

We shall explore the ability of the system controlling eye movements to learn to follow points or scan lines whose positions are modified in determinate ways by movement of the eyes. Of especial interest will be the effect of eye-movement adaptation on the perception of motion and form.

M. Eden, P. A. Kolers, P. H. Liss

## 4. Biological Image Processing

Biological image processing deals with the acquisition and analysis of visual patterns that are important to medicine and biology. The picture-processing facilities described above are being used to explore the feasibility of using fully automatic techniques or machine aids to human classification of such objects as white cells, chromosome counting, particle counting in micro-autoradiographs, and three-dimensional visualization of micro-anatomic structures.

## a. Chromosome Project

As an exploratory venture into Biological Image Processing, we have started assembling a procedure for karyotyping human chromosomes. In particular, we are addressing ourselves to the problems presented by touching and overlapping chromosomes. We hope to achieve our aim of distinguishing overlapping chromosomes by obtaining photographs in which the density in the overlap regions is different from that in the nonoverlapping regions, then to outline the chromosomes through appropriate programming.

## b. Blood Cell Inventorying

The objective is to see if the distinctions between the various blood cells are sufficiently well understood to allow us to devise an automatic inventorying procedure. Standard blood smears stained with Wright's solution are photo-micrographed, and then scanned through three color filters on a flying-spot scanner. The digital data are then entered into the computer, where various algorithms will be employed to attempt separation. Ultimately, we hope to construct a computer-controlled microscope scanner.

## c. Branching Structures

Algorithms have been devised for generating two-dimensional venation patterns such as are typified by tree leaves. The parameters of the algorithm serve as data for a possible classification of leaf type according to species. The work will be extended to measure the analogous parameters of actual leaves by picture-processing techniques.

M. Eden, W. L. Black, O. J. Tretiak

## A. REPRODUCTION OF GRAPHICAL DATA BY FACSIMILE<sup>\*</sup>

There is a broad category of documentary and graphical data which is commonly transmitted by facsimile and in which only two brightnesses, black and white, exist in the input. Although substantial savings in channel capacity could be made by restricting the transmitted information to these two levels, it is found in practice that a continuous

<sup>\*</sup>This work was done by the author while he was at the Indian Institute of Technology, Kanpur, U.P., India, under the Kanpin Indo-American Program, a project financed by USAID.

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(a)

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(d)

Fig. XXX-1. (a) 70 samples/inch, continuous tone scale.

(b) 70 samples/inch, binary tone scale.

- (c) 200 samples/inch, continuous tone scale.
- (d) 200 samples/inch, binary tone scale.

These pictures should be viewed at approximately twice normal viewing distance. The resolution refers to the original copy.

(analog) tone scale gives superior results. It is the purpose here to report some experiments along these lines and to present some preliminary conclusions.

Eight examples of original documents, including typing, book, newspaper, and magazine print, and several non-Roman scripts, were converted into transparencies, with careful attention paid to photographic quality, including sharpness, graininess, and the preservation of the original tone scale. These transparencies were then scanned at approximately 70, 100, 140, and 200 samples per inch (of the original) in each direction. The sampled data were displayed on a cathode-ray tube and photographed with the original continuous tone scale, and also quantized into various numbers of steps. Attention was given to comparison of the analog and two-level reproductions. The scanning aperture was small (sharply focussed) in all cases, but the reproduction aperture was made just large enough to reduce the visibility of the dot structure to a low level.

The results show that at the lower sampling densities analog transmission does give superior quality, but the difference between analog and binary reproduction becomes less as the sampling density increases. The two reproductions seem nearly comparable at 200 samples/inch or less, the difference depending on the copy. On the basis of these tests, we have reached the following preliminary conclusion:

> Very high-quality transmission of graphical data is possible, by using discrete sampling in both directions with only two transmitted levels of brightness.

There is a subsidiary matter of importance in binary transmission, however. When only two brightness levels are used, the decision level of the quantizer is of great importance. Factors such as different reflectivity of background, color and darkness of ink, quality of print, focus, and so forth, make it highly desirable to use some local averaging to adjust the decision level to an optimum value. Preliminary qualitative work shows this approach to have merit. We hope to do further studies at a later date.

Some examples are shown in Fig. XXX-1 above.

W. F. Schreiber

## B. IMAGE TRANSMISSION BY TWO-DIMENSIONAL CONTOUR CODING

This research is an extension of the work done by J. W. Pan,<sup>1</sup> as suggested by Professor W. F. Schreiber.<sup>2</sup> A block diagram of the proposed system is shown in Fig. XXX-2.



Fig. XXX-2. Block diagram of the proposed system.

In this system an image is treated as a two-dimensional signal of the spatial coordinates x and y. The large changes in brightness in a picture occur at the edges of objects and are accentuated by the visual system. The edge points can be isolated by the gradient or Laplacian operator. The fact that these edge points lie along connected contours in two dimensions is used to code the location and characteristics of each point efficiently. Two-dimensional reconstruction filters are derived to synthesize the highfrequency picture from the decoded-edge information. A two-dimensional lowpass or out-of-focus picture is also formed which can be transmitted with a relatively small number of bits. After a possible accentuation to make the picture appear "sharper," the "synthetic highs" signal is added to the lowpass picture to yield the final output. A reduction in the total number of bits required to describe a picture by a factor of 4 to 23 is possible as compared with 6-bit PCM.

The pictures used in this investigation were flying-spot-scanned, quantized to 256 levels, which permits an 8-bit representation, and recorded on digital magnetic tape by the picture-processing equipment constructed in our laboratory. The IBM 7094 II and other facilities of the Computation Center, M. I. T., were used to process these pictures, and the equipment in our laboratory was used to display and photograph the output from the simulation. Limitations of core storage and processing speed led to the choice of pictures that were sampled with a  $256 \times 256$  array.

The lowpass filter,  $\ell(x, y)$ , used in this study was a circularly symmetric Gaussian function with  $\sigma = 4$  samples. This spreads over approximately 10 per cent of the picture height. The original and the lowpass pictures are shown in Fig. XXX-3. In an earlier report<sup>3</sup> it was shown that the gradient operator could be used as an edge



(a)







detector and that it is possible to reconstruct the high-frequency part of the picture by operating on the gradient signal with a two-dimensional linear filter. It is also possible to use the Laplacian operator and to derive a reconstruction filter for this signal.<sup>4</sup>

The principal edges in a picture lie along contours in two dimensions which are continuous. A large "contour start threshold" is set to isolate the important edges in the picture. After finding a point for which the magnitude of the gradient exceeds the contour start threshold, the neighboring points are examined and the contour extended in the direction of the maximum magnitude. This process continues until no neighbor point exceeds the "edge-point threshold" when an "end-of-contour" signal is sent. The starting point is examined again to see if the contour extends in the opposite direction to that first taken.

In transmitting the location of the contour points a great deal of advantage can be taken of their connectivity. The beginning point of a contour requires 16 bits to specify its location, although some sort of two-dimensional run-length coding could reduce this. The first sample on the contour can be in any direction, so that 3 bits are necessary to specify this. Because contours tend to be long, straight or curved lines, it is expected that the next point will lie in the same direction as the last, or perhaps 45° to either side. A variable-length code can be generated to describe these vector direction changes (vdc) efficiently. At any point that is on a contour, the gradient is quantized into 4 possible magnitudes and 8 directions. Since we expect the gradient direction change (gdc) can be coded in the same way as the vdc. In fact, changes in these two quantities are probably highly correlated. Since we search for the maximum value of the magnitude along a contour, we can also expect that to change slowly. An efficient code for the gradient magnitude change (gmc) can be derived from the conditional probabilities

Figure	XXX-5	XXX-6	XXX-7	XXX-8
Number of edge points	3994	8900	13980	2301
Number of contours	125	263	485	55
Number of bits for				
vdc	9850	20300	38400	5900
gdc	8420	17400	30600	4260
gmc	4840	11200	18900	2880
start point	2625	5513	10185	1155
lows	3000	3000	3000	3000
Total number of bits	28735	57413	101085	17195
Reduction factor	13.7	6.85	3.9	22.9

Table XXX-1.	Contour	coding	data	for	the	figures.
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Contour Start Threshold = 38 Edge-Point Threshold = 12



Fig. XXX-5. Two-dimensional bandlimiting. Reduction Factor = 16



(b)





(d)



Contour Start Threshold = 25 Edge Point Threshold = 6

(e)

Fig. XXX-6. Simulation result. (a) Original. (b) Lowpass. (c) Gradient. (d) Synthetic highs. (e) Output.







(d)



Contour Start Threshold = 25

Edge Point Threshold = 6

(e)

Fig. XXX-7. Simulation result. (a) Original. (b) Lowpass. (c) Gradient. (d) Synthetic highs. (e) Output.



(b)





(c)





Contour Start Thresnold = 25 Edge Point Threshold = 6

(e)

Fig. XXX-8. Simulation result. (a) Original. (b) Lowpass. (c) Gradient. (d) Synthetic highs. (e) Output. of change from each level.

The output picture with a reduction factor of 13.7 as compared with 6-bit PCM is shown in Fig. XXX-4. A similar bit reduction by two-dimensional bandlimiting is illustrated in Fig. XXX-5.

Figures XXX-6, XXX-7, and XXX-8 show other input pictures and the results of processing. The synthetic highs were accentuated by 1.2 before being added to the lows to give the output pictures. The coding data and bit reduction for each is given in Table XXX-1.

The reduction factor in bit rate over 6-bit PCM as calculated in Table XXX-1 should increase with a higher resolution system. For an  $n \times n$  picture the total number of points goes as  $n^2$ , while the number of points on the edges is proportional to n. Thus if not many new contours were found in a 512 × 512 picture the reduction factor would approximately double over that found with a 256 × 256 picture.

D. N. Graham

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# C. FOURIER-TRANSFORM REPRESENTATION OF PICTURES

With the appearance of the Cooley-Tukey algorithm,<sup>1</sup> which reduces the number of operations in the machine calculation of Fourier series, possibilities for new investigations in picture processing have presented themselves. The use of PCM picture transmission has been well investigated.<sup>2</sup> Now, given an array of numbers, constituting a sampling of image brightness levels, the Fourier series may be determined for a periodic, two-dimensional, discrete function generated from the array. This Fourier series



Fig. XXX-9.

- (a) Original picture used in the study.
- (b) Result of 5-bit quantization on conventional PAM samples.
- (c) Result of 5-bit quantization on Fourier series samples.









will be periodic in two dimensions also. If the image was properly bandlimited before sampling, then the two-dimensional period of the Fourier series, centered around the DC term, is a sampled version of the Fourier transform of the original unsampled image. The coefficients in a period of the Fourier series, which are, in general, complex, are equal in number to the samples taken of the image. The transform of a real function obeys a symmetry condition,  $F(u, v) = F^*(-u, -v)$ , where F(u, v) is the two-dimensional transform with frequency variables u and v, and \* denotes conjugation. This allows representation of the periodic two-dimensional Fourier series by only one-half of the coefficients in any period of the series. Instead of using N real numbers to represent a picture, N/2 complex numbers may be used by Fourier analysis.

Of interest is the result of quantization on picture quality when Fourier series samples are used for picture representation. Partial results in this investigation have been obtained. Figure XXX-9a is the original picture used in this study. This picture was sampled to form a 64 × 64 array and then quantized to 5 bits per sample. A linear interpolation scheme was then used to obtain the picture in Fig. XXX-9b. Figure XXX-9c was obtained by first calculating a Fourier series using the 64 × 64 sample array, quantizing the series samples to 5 bits, inverting the series to get a picture array, and then finally interpolating. Figure XXX-9b and 9c are seen to be comparable, thereby indicating that the Fourier series samples are no more susceptible to quantization noise than are conventional PAM samples. The degradation of Fig. XXX-9b and 9c with respect to Fig. XXX-9a is due not only to quantization but also to the heavy aliasing in the sampling process.<sup>3</sup> It is expected that at least a slight improvement is possible for Fig. XXX-9c by using a readjustment of quantization scale, since some of the Fourier series samples were well out of range.

The sampling array was limited to  $64 \times 64$ , because of memory limitations of the IBM 7094 computer.

G. B. Anderson

#### References

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## D. EFFECT OF MULTIPATH ON HOLOGRAM TELEVISION SYSTEMS

## 1. Introduction

There are three reasons why one might want to transmit a hologram of a scene instead of a conventional picture of the scene.

(i) Although the hologram itself is two-dimensional, the reconstruction of the original scene can be made three-dimensional.

(ii) The effect of channel disturbances on the quality of the reconstructed picture of a hologram television system will be different from its effect on the received picture of a conventional television system. In certain cases, the degradation in picture quality in a hologram TV system may be more acceptable than that in a conventional TV system.

(iii) A hologram may be more amenable to certain bandwidth compression schemes than a conventional picture.

In order to exploit the second point mentioned above, it is necessary to find out how various channel disturbances will affect the reconstructed picture in a hologram TV system. In this report, we present some preliminary results on the effect of multipath or echo on the reconstructed picture of an analog hologram TV system.

#### 2. Theoretical Analysis for Fourier-Transform Holograms

Let f(x,y) be the light (amplitude) distribution, as a function of the spatial coordinates x and y, which we wish to reconstruct at the receiver. Then, except for some scale factors, the Fourier-transform hologram of f(x,y) is

$$H(u,v) = |F(u,v)+Ae^{-jau}|^2,$$
 (1)

where F(u, v) is the Fourier transform of f(x, y), u and v are the spatial frequencies, and A and a are real constants. The term in the right-hand side of Eq. 1, which is responsible for the reconstruction, is<sup>1</sup>

$$H_{1}(u, v) = A F(u, v) e^{Jau}$$
 (2)

If the hologram is scanned (in the v-direction, say), and transmitted in analog fashion, and if there are two different transmission paths, then the received hologram will be

$$H_{r}(u, v) = H(u, v) + bH(u, v-d),$$
 (3)

where b and d are real constants. The term on the right-hand side of Eq. 3, which is responsible for the reconstruction, is

$$H_{r1}(u,v) = [AF(u,v) + AbF(u,v-d)] e^{Jau}$$
(4)

and the reconstructed light (amplitude) distribution will be proportional to











Fig. XXX-10. (a) Original scene. (b) Its Fourier-transform hologram. (c) Reconstruction from the hologram.

$$g(x,y) = f(x,y)(1+b\cos dy) + jbf(x,y) \sin dy.$$
 (5)

The observed intensity distribution then is

$$|g(x, y)|^{2} = (1 + b^{2} + 2b \cos dy)|f(x, y)|^{2}.$$
 (6)

Therefore, the reconstructed scene is the original scene multiplied by a biased sine wave. It will contain fringelike structures, the spacing of the fringes being dependent on d, the delay of one of the transmission paths. The case of more than two transmission paths can be analyzed in a similar way.

#### 3. Experimental Results

The case just discussed was simulated on an optical bench. An apparatus was arranged to make Fourier-transform holograms of a transparency. The multipath was simulated by shifting and double-exposing the film in the hologram plane.

Figure XXX-10 shows the original scene on the transparency, its Fourier-transform







(a)



Fig. XXX-11. (a) A two-path hologram. (b) Its reconstruction.

Fig. XXX-12. (a) Another two-path hologram (with smaller delay). (b) Its reconstruction.

hologram, and the reconstruction from the hologram. Figures XXX-11 and XXX-12 show The delay, d, in two simulated two-path holograms and their reconstructions. Fig. XXX-12 is approximately 1/4 that in Fig. XXX-11. These reconstructed pictures

clearly exhibit the fringelike structures predicted by Eq. 6.

4. Fresnel Holograms

A similar analysis of a Fresnel hologram indicated that the effect of multipath in that case is twofold: The reconstructed picture will contain ghost images just as in a conventional TV system, and the overlapping areas of the images will contain fringe-like structures.

T. S. Huang, P. L. Stamm

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# E. OPTICAL SPATIAL FILTERING FOR SIMULTANEOUS DELAY AND DOPPLER ESTIMATES OF RADARLIKE SIGNALS

Optical processors have been recognized in recent years as efficient tools for performing spectral analysis and linear filtering, particularly when the data to be processed are two-dimensional.<sup>1</sup> Both coherent and incoherent systems are possible, although the coherent systems are generally more useful. These systems have found application in various kinds of pattern recognition,<sup>2</sup> analysis of nuclear particle tracks in bubble chamber photographs,<sup>3</sup> analysis of seismic data,<sup>4</sup> processing of video signals in synthetic aperture radar,<sup>5</sup> and pulse compression (matched filtering).<sup>6</sup>



Fig. XXX-13. Space-domain filter function from which the frequency-domain filter was constructed; actual size, 3/8 inch square.

The investigation reported here concerns the use of a coherent spatial matched filter to extract range and Doppler information from a radar or radarlike signal recorded on photographic film, and to present the estimates in a two-dimensional display. An experimental system has been constructed and successfully demonstrated. In the system

the Fourier-transfrom properties of a lens were used to generate the spatial frequency spectrum of an input signal, and the filtering was done in the frequency plane. Computergenerated space-domain filter function transparencies (see Fig. XXX-13) were made with our laboratory's picture-processing equipment, and the frequency plane filter was made photographically with the same optical equipment used for the filtering. Both the signals and frequency plane filter were recorded by modulation on carriers. The signal used was a 49-bit pseudo-random binary shift register code, chosen for its sharply peaked autocorrelation function. The filter was constructed with 7 discrete Doppler channels separated by 1/2 cycle/bit (nothing precludes a continuous filter in the Doppler direction; it was made discrete for simplicity of display). One-half of the spatial frequency plane was blocked to make the system independent of carrier phase.<sup>1</sup>

The system functioned approximately as predicted by theory, although the spurious responses ("self-noise") of the filter were larger than expected (Fig. XXX-14). This



Fig. XXX-14. Response of system to noisefree input; 5 bits/cm horizontal, arbitrary intensity (each trace) vertical; the traces correspond to equidistant channels in the output plane.

we attribute to severe nonlinearity in the photographic process used to construct the frequency-plane filter. The system successfully extracted signals from Gaussian noise with a 0-db S/N energy ratio; a distortionless system should be able to improve this by approximately 10 db (see Fig. XXX-15).

Substantial improvements in performance can probably be obtained by using filters constructed directly in the frequency domain on a computer<sup>7</sup>; this was not attempted because of the low quality of the optical equipment available to us (many of the distortions introduced by an aberrated lens are cancelled if the lens that is to be used for the



Fig. XXX-15. Response to signal plus Gaussian noise, 0-db S/N energy ratio; same scale as in Fig. XXX-14.

processing is also used for transforming the filter function). High-quality optical equipment and care in the construction of filters should result in improving attainable compression ratios by one or two orders of magnitude.

A.H. M. Ross

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