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# EFFECTS OF INSERTION DEVICES ON BEAM EMITTANCES AT THE PHOTON FACTORY STORAGE RING

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<u>Abstract</u> The effects of the insertion devices on the beam emittances are estimated. The results are consistent with the observations.

# INTRODUCTION

The Photon Factory storage ring is a 2.5 GeV electron/positron storage ring dedicated to the synchrotron radiation experiments. In this ring, six insertion devices (wigglers) are installed to provide highly brilliant synchrotron lights. Three of them have relatively strong magnetic fields (greater than 1.5 T ) and affect the beam emittances through the mechanisms of radiation damping and radiation excitation. In this paper, we estimate the effects of the wigglers on the beam emittances. We also present some preliminary data.

#### INSERTION DEVICES

The parameters of the wigglers are summarized in Table 1. MPW#13<sup>4</sup> and MPW#16<sup>3</sup> are horizontal multipole wigglers. VW#14<sup>4</sup> is a superconducting vertical wiggler with three poles.

#### EFFECTS ON BEAM EMITTANCES

The changes in the beam emittances caused by wigglers can be written as follows;

$$\begin{aligned} & (\varepsilon_w / \varepsilon_o) = (I_{5w} / I_{5o}) / (I_{2w} / I_{2o}) , \\ & (\sigma_{Ew} / \sigma_{Eo})^2 = (I_{3w} / I_{3o}) / (I_{2w} / I_{2o}) , \\ & I_{2w} = I_{2o} + \int_w ds (1 / \rho_w^2) , \end{aligned}$$

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$$\begin{split} I_{3w} &= I_{30} + \int_{w} ds (1/\rho_{w}^{3}) , \\ I_{5w} &= I_{50} + \int_{w} ds (H/\rho_{w}^{3}) , \\ H &= \gamma \, \eta^{2} + 2\alpha \, \eta \, \eta' + \beta \, \eta'^{2} . \end{split}$$

Here, I 's are so-called synchrotron integrals and the subscripts "w" and "o" denote the integrals with and without the wigglers, respectively. The  $\rho$  is the bending radius of the wigglers. Assuming some analytic formulae for  $\rho$ , we can obtain analytic expressions for I 's<sup>5</sup>. In the calculation of the H, the contributions of both the dispersion ( $\eta$ ) proper to the ring itself and that produced by the wigglers are included. By using the above formulae, the changes in the beam emittances are estimated and shown in Figures 1, 2, 3. The calculations were done for the present operating energy (2.5 GeV) and also for the lower energy (1.5 GeV), where the effects of the wigglers are expected to be larger.

#### MPW#16

MPW#16 is installed at a dispersion-free section. The contribution of the horizontal dispersion ( $\eta$ ) produced by X MPW#16 to the radiation excitation in the horizontal betatron motion is negligibly small. Thus, the horizontal emittance ( $\varepsilon$ ) is reduced simply by the radiation damping. On the other hand, the energy spread ( $\sigma$ ) increases as the radiation excitation in the longitudinal motion dominates the radiation damping.

| NAME   | Bx(T)  | By(T)  | λ <sub>u</sub> (cm)  | N  | $\eta_{\rm XO}^{\rm (m)}$  | P <sub>w</sub> /P <sub>o</sub>                            |
|--|--|--|--|--|--|---|
| MPW#13<br>MPW#16<br>VW#14  | <br>5.0  | 1.5<br>1.5<br>   | 18.0<br>12.0<br>   | 13<br>26<br>   | 1.1<br>0.0<br>0.0  | 0.052<br>0.070<br>0.071                                   |
| NOTE Bx<br>horizontal<br>is the $\eta$<br>$\eta_{x0}$ is the<br>ratio of<br>maximum is<br>magnets. | and By a<br>l and vert<br>period ler<br>he dispers<br>the radia<br>field str | are the residual distribution fundation fundation fundation for the second distribution distribution for the second distribution for the second distribution for the second distribution distribution for the second distribution distribution for the second distribution distribut | maximum firections,<br>N is the r<br>ction at th<br>ss caused b<br>to that c | eld st<br>res pec<br>number c<br>he wiggl<br>by each<br>caused | rengths<br>tively.<br>of period<br>er, P_/P<br>wiggler<br>by the | in the<br>The λ<br>ds. The<br>is the<br>at its<br>bending |

TABLE 1Parameters of the insertion devices

#### MPW#13

MPW#13 is installed at a straight section where  $\eta \sim 1$  m. At 2.5 GeV, the effects of the radiation excitation and the radiation damping almost cancel each other. At 1.5 GeV, the radiation excitation dominates the radiation damping, and then the  $\varepsilon$  increases.



FIGURE 1 Changes in the emittance and the energy spread produced by MPW#16 are shown as the functions of the field strength. "L" denotes  $(\sigma_{\rm EW}/\sigma_{\rm EQ})$  and "H" denotes  $(\varepsilon_{\rm Z}/\varepsilon_{\rm XO})$ . The numbers in brackets denote the beam energy (2.5 GeV or 1.5 GeV).



FIGURE 2 Changes in the emittance and the energy spread for MPW#13.

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VW#14

VW#14 is installed at a dispersion-free section and the  $\varepsilon_{x}$  is reduced by the radiation damping. On the other hand, the vertical emittance ( $\varepsilon_{y}$ ) is increased. Here, we have assumed  $\varepsilon_{y0} = 0.02\varepsilon_{x0}$ . The vertical dispersion ( $\eta_{y}$ ) produced by VW#14 causes the radiation excitation and increases  $\varepsilon_{y}$ .



FIGURE 3a Changes in the emittances and the energy spread for VW#14 at 2.5 GeV. "L", "H" and "V" denote  $(\sigma_{\rm EW}/\sigma_{\rm Eo})$ ,  $(\varepsilon_{\rm XW}/\varepsilon_{\rm XO})$  and  $(\varepsilon_{\rm YW}/\varepsilon_{\rm YO})$ , respectively.



FIGURE 3b Changes in the emittances and the energy spread for VW#14 at 1.5 GeV.

# MEASUREMENTS ON BEAM EMITTANCES

In this section, we will present some preliminary data on the changes in the beam emittances caused by the wigglers. We measured the beam sizes at a beam line called BL21 for several field strengths of VW#14 and MPW#16. Because  $\eta \neq 0$  at the source point of BL21, the horizontal beam size ( $\sigma_{x}$ ) is affected by both changes in  $\varepsilon$  and  $\sigma_{x}$ . Furthermore, when the wigglers are excited, the linear optics of the ring is also distorted<sup>7</sup>. Therefore, we need the values of  $\sigma_{x}$ ,  $\beta$  and  $\eta$  at the source point of BL21 to determine the emittances. Here, we use the calculated value for  $\sigma_{x}$ , while for  $\beta$  and  $\eta$  we use the values extrapolated from their measurements near the source point of BL21. The measured data were converted to the transverse emittances using the relations;

$$\varepsilon_{x} = \{\sigma_{x}^{2} - \eta_{x}^{2}(\sigma_{E}/E)^{2}\}/\beta_{x},$$
  
$$\varepsilon_{y} = \sigma_{y}^{2}/\beta_{y},$$

where;



FIGURE 4 Measured data on the transverse emittances are shown as the functions of P/(P+P). White squares are  $(\varepsilon_{X}/\varepsilon_{X})$ . Black squares are  $(\varepsilon_{Y}/\varepsilon_{Y})$ . The alphabets on the horizontal axis indicates the following cases; A: VW#14 0 T and MPW#16 0 T, B: VW#14 0 T and MPW#16 1.2 T C: VW#14 0 T and MPW#16 1.5 T, D: VW#14 5 T and MPW#16 0 T E: VW#14 5 T and MPW#16 1.2 T, F: VW#14 5 T and MPW#16 1.5 T.

$$\sigma_{x,y} = \sigma_{x,y}^{\text{dsgn}} (\sigma_{x,yw} / \sigma_{x,yo})^{\text{meas}} ,$$
  

$$\beta_{x,y} = \beta_{x,y}^{\text{dsgn}} (\beta_{x,yw} / \beta_{x,yo})^{\text{meas}} ,$$
  

$$\eta_{x} = \eta_{x}^{\text{dsgn}} (\eta_{xw} / \eta_{xo})^{\text{meas}} .$$

Here the superscript "dsgn" denotes the design value without wigglers and "meas" denotes the measured value. In Figure 4, the relative changes of the transverse emittances ( $\varepsilon_{X,YW}$ ) are plotted as the functions of P/(P+P), where P is the radiation loss caused by the bending magnets and P is that caused by the wigglers. In the case of MPW#16 and VW#14, it can be considered that  $\varepsilon_{X}$  is reduced simply by the radiation damping because of zero dispersion at their locations, and so the changes in  $\varepsilon_{X}$  are consistent with this expression. On the other hand,  $\varepsilon_{X}$  seems to increase with the excitation of the wiggler, VW#14, on  $\varepsilon_{X}$  (see Figure 3a). The other is that the increase of  $\sigma_{X}$ may contribute to the increase of  $\sigma_{X}$ , since the measurement indicates that  $\eta$  is not strictly zero at the source point of BL21.

### SUMMARY

The changes in beam emittances produced by the wigglers are estimated. The measured data on the beam emittances are consistent with the calculations. It is also demonstrated that the effects of wigglers will be more significant for low energy rings, when the wigglers have high fields.

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