## **Computational Approaches to Modeling the Conserved Structural Core Among Distantly Homologous Proteins**

by

Matthew Ewald Menke

Submitted to the Department of Electrical Engineering and Computer Science in partial fulfillment of the requirements for the degree of

Doctor of Philosophy in Computer Science

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### Abstract

Modern techniques in biology have produced sequence data for huge quantities of proteins, and 3-D structural information for a much smaller number of proteins. We introduce several algorithms that make use of the limited available structural information to classify and annotate proteins with structures that are unknown, but similar to solved structures. The first algorithm is actually a tool for better understanding solved structures themselves. Namely, we introduce the multiple alignment algorithm Matt (Multiple Alignment with Translations and Twists), an aligned fragment pair chaining algorithm that, in intermediate steps, allows local flexibility between fragments. Matt temporarily allows small translations and rotations to bring sets of fragments into closer alignment than physically possible under rigid body transformation. The second algorithm, BetaWrapPro, is designed to recognize sequences of unknown structure that belong to specific all-beta fold classes. BetaWrap-Pro employs a "wrapping" algorithm that uses long-distance pairwise residue preferences to recognize sequences belonging to the beta-helix and the beta-trefoil classes. It uses hand-curated beta-strand templates based on solved structures. Finally, SMURF (Structural Motifs Using Random Fields) combines ideas from both these algorithms into a general method to recognize beta-structural motifs using both sequence information and longdistance pairwise correlations involved in beta-sheet formation. For any beta-structural fold, SMURF uses Matt to automatically construct a template from an alignment of solved 3-D structures. From this template, SMURF constructs a Markov random field that combines a profile hidden Markov model together with pairwise residue preferences of the type introduced by BetaWrapPro. The efficacy of SMURF is demonstrated on three betapropeller fold classes.

Thesis Supervisor: Bonnie Berger Title: Professor of Applied Mathematics

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Much of the work in Chapter 2 of this thesis appeared as "Matt: Local Flexibility Aids Protein Multiple Structure Alignment" in *PLoS Computational Biology* in 2008. Most of Chapter 3 was published as "Prediction and comparative modeling of sequences directing beta-sheet proteins by profile wrapping" in *Proteins: Structure, Function, and Bioinformatics* in 2006, volume 63. Chapter 4 has yet to be published. I thank my coauthors for their permission to include our joint work in this thesis.

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# Chapter 1

# Introduction

A single protein chain consists of an ordered set of the twenty different amino acids, typically from 50 to 1000 residues in length. Proteins are termed homologous if they share a common evolutionary origin; since evolution was not observed over time, homology is generally inferred by similarity. Homology can be inferred by sequence similarity when proteins are evolutionarily close, but as their evolutionary relationship becomes more distance, direct inference of protein homology from sequence can become difficult. However, when 3-D structural information is also available, it can be easier to classify proteins. Proteins whose folded 3-D structure is known are termed *solved* protein structures.

The solved protein structures have been grouped together in hierarchical classification schemes such as the Structural Classification of Proteins (SCOP) [73] and CATH (Class, Architecture, Topology, Homologous superfamily) [76]. At the top level of the SCOP hierarchy, proteins are subdivided based on their predominant type of secondary structure: predominantly alpha, predominantly beta, or a combination of the two. Within these broad groups, there is a further subdivision into the fold, superfamily, and family levels of the SCOP hierarchy. Each successive level contains proteins that share progressively greater structural similarity.

In SCOP, at the 'family' level, this translates into a sufficient level of sequence similarity to clearly indicate an evolutionary relationship. The level of pairwise sequence identity at the family level is generally 30% or greater. At the 'superfamily' level, sequence identity is significantly lower, but structural and functional similarities indicate a probable common ancestor. Proteins in the same 'fold' have the same basic arrangement of secondary structure, but may have significant differences in intervening regions. Such proteins may not have an evolutionary relationship.

This thesis is largely concerned with the goals of recognizing, and aligning proteins that belong to the same SCOP superfamily or fold class. We consider two main subproblems: 1) aligning proteins in the same superfamily whose three-dimensional structures are known, so that the similar parts are matched, and 2) predicting when a protein whose sequence is known but whose structure is not should be placed in the same superfamily as a set of proteins whose 3-D structure is known. In some cases, we not only recognize that the protein folds into the appropriate family, but we also predict the sequence-structure alignment.

### **1.1 Protein Structural Alignment**

The problem of constructing accurate protein multiple structure alignments has been studied in computational biology almost as long as the better-known multiple sequence alignment problem [71]. The main goal for both problems is to provide an alignment of residueresidue correspondences in order to identify homologous residues. When applied to closely related proteins, sequence-based and structure-based alignments typically give consistent answers even though most sequence alignment methods are measuring statistical models of amino acid substitution rates, whereas most structure-based methods are seeking to superimpose alpha-carbon atoms from corresponding backbone 3-D coordinates while minimizing geometric distance. However, as has been known for some time [15], these answers can diverge when aligning distantly related proteins; most relevant, it is still possible to find good structural alignments when sequence similarity has evolutionarily diverged into "the twilight zone" [83]. In the twilight zone, distantly related proteins can still share a *common* core structure containing regions, including conserved secondary-structure elements and binding sites, in which the chains retain the folding topology (see [25] for a recent survey). Structural information can align the residues in this common core, even after the sequences have diverged too far for successful sequence-based alignment, because structural similarity is typically more evolutionarily conserved [1, 28, 106]. (While divergent sequence with conserved structure is the typical case and the one that structural alignment algorithms that respect backbone order such as Matt seek to handle, there are also well-known examples where structure has diverged more rapidly than sequence; see, for example, Kinch and Grishin [55] and Grishin [37].)

Applications of multiple structure alignment programs include understanding evolutionary conservation and divergence, functional prediction through the identification of structurally conserved *active sites* in homologous proteins [42], construction of benchmark datasets on which to test multiple sequence alignment programs [28], and automatic construction of profiles and threading templates for protein structure prediction [25, 78]. It has also recently been suggested that multiple structure alignment algorithms may soon become an important component in the best multiple sequence alignment programs. As more protein structures are solved, there is an ever-increasing chance that a given set of sequences to be aligned will contain a subset with structural information available. To date, however, only a handful of multiple sequence alignment programs are set up to take advantage of any available structural data [28, 77].

Pairwise structure alignment programs fall into three broad classes: the first class, to which Matt belongs, are aligned fragment pair (AFP) chaining methods [91, 110] which do an all-against-all best transformation of short protein fragments from one protein structure onto another, and then assemble these in a geometrically consistent fashion. The second class (which includes the popular Dali [40]), look at pairwise distances or contacts *within* each structure separately, then try to find a maximum set of corresponding residues that obey the same distance or contact relationships in pairs of structures– these are called *distance matrix* or *contact map* methods. The third class consists of everything else, from geometric hashing [74] borrowed from computer vision to an abstraction of the problem to secondary structural elements [23]. Some protein structure alignment programs are *non-sequential;* that is, they allow residue alignments that are inconsistent with the linear progression of the protein sequence [24, 57, 107, 115]. Most enforce an alignment consistent with the sequential ordering of the residues along the backbone– Matt belongs to the class of sequential protein aligners. There are strengths to both approaches: most useful protein

alignments are sequential; however, non-sequential protein aligners can handle cases where there is a reordering of domains, and circular permutations [37].

Multiple structure alignment programs are typically built on top of pairwise structural alignment programs. Even simplified variants of structure alignment are known to be NP-hard [35, 105]; important progress has been recently been made in theoretically rigorous approximation guarantees [59] for pairwise structural alignment using a class of single optimality criteria scores such as the Structal score [71], and also in provably fast parameterized algorithms for the pairwise structural alignment problem in the non-sequential case [107].

### **1.2** Protein Superfamily Recognition from Sequence

We consider the following set of problems. Given a set of proteins from a particular SCOP superfamily, can we predict if a new protein sequence, of unknown 3-D structure, also belongs to the same SCOP superfamily?

If sequence similarity to one of the solved structures is high, this is an easy problem. In fact, structural information need not be used at all. Protein sequence alignment algorithms, such as BLAST [2] and ClustalW [102], attempt to align protein sequences directly and return one or more of the highest scoring alignments using some metric. Generally, the scoring function penalizes unaligned gap positions and rewards aligning similar amino acids. Amino acid similarity can be calculated from a set of alignments assumed to be correct. Designed for searching through large databases, BLAST looks for similar subsequences and extends them to longer sequence alignments. Slower dynamic programming algorithms, such as ClustalW, tend to return better results. While these methods can be very accurate when two proteins are in the same SCOP family, they can fail at the superfamily level due to insufficient sequence similarity.

### **1.2.1** Protein Profile Hidden Markov Models

Profile hidden Markov model (HMM) methods, such as HMMER [27], are a more sophisticated approach that tends to perform better in cases of low sequence similarity than sequence alignment algorithms, and can also be deployed in the absence of structural infor-



Figure 1-1: HMMER hidden Markov model

HMM generated by HMMER, with states for matching multiple domains removed. Square states always output a residue, round states never do. The grayed out states are removed from the model, as no paths from Begin to End include them.

mation. Profile HMMs model a set of homologous proteins as a probabilistic walk through a directed graph which generates member protein sequences. Each edge has a learned probability of being taken. Some of the nodes, or states, output residues with a positiondependent probabilities.

HMMER constructs a profile HMM as follows (see Figure 1-1): Given a multiple alignment of homologous protein sequences, pick the most highly conserved positions to use in the HMM. For each of these positions, the model has three states: A match state, an insertion state, and a deletion state. Each match state corresponds to the conserved position itself, and has transitions to its own insertion state and the next position's match and deletion states. The deletion state corresponds to a particular protein not containing any residue in that particular position, and has transitions to the next match and deletion states. The insertion state corresponds to the residues between one conserved position and the next, and has transitions to itself and the next match state. Both the insertion and match states always output a single residue, and the deletion state outputs no residue. The HMM also has begin and end states. The begin state has a transition to each of the match states, and each of the match states has a transition to the end state. Both the transition probabilities and the probabilities of outputting each of the 20 residues at each insertion and match state are calculated based on the input alignment. In general, a profile HMM is any HMM with match, insertion, and deletion states arranged as described above with position-specific residue output probabilities. HMMer also uses five other states that allow it to recognize multiple instances of the motif in a single protein sequence.

After constructing a profile HMM, HMMER uses both the Viterbi and forward algorithms [104, 82] to calculate the probability of the HMM generating a given sequence. The Viterbi algorithm returns the path through the HMM most likely to generate a specific sequence, along with its probability. The path taken corresponds to an alignment of the input sequence to the original multiple sequence alignment. The slower Forward algorithm returns the probability that any path through the HMM returns the input sequence. HMMER 3.0 uses the score of the Viterbi algorithm as a filter to determine whether or not to run the Forward algorithm.

### 1.2.2 Threading

While the above methods only require sequence information, threading methods make use of protein structural information in order to identify even more distantly homologous proteins. Currently, the most successful methods for fold recognition at the superfamily level of similarity fall within the paradigm of *protein threading* [48, 14, 45, 93, 108]. In the most general sense, protein threading algorithms work by searching for the higest-scoring alignment of a sequence of unknown structure onto the previously solved structure of another protein. Ideally a threading algorithm is sensitive enough to not only give a yes/no answer for the fold recognition problem, but also to generate sequence-structure alignment and possibly a putative structure as well.

Some threaders use scoring functions that have no pairwise interaction component and find the best fit using dynamic programming. Algorithms that use scoring functions with pairwise components tend to perform better, but finding the best hit in the general case has been proven to be NP-complete [61]. As a result, these threading methods tend to be quite slow, particularly when threading onto tightly packed template structures.

Unfortunately, there is no general-purpose threading method that can reliably identify even a large subset of SCOP superfamily classes.

### **1.3 Our Contribution**

### 1.3.1 Matt

In Chapter 2 we introduce the program Matt ("Multiple Alignment with Translations and Twists"), an AFP fragment chaining method for pairwise and multiple sequence alignment, and test its performance on standard benchmark datasets. At the heart of our approach is a relaxation of the traditional rigid protein backbone transformations for protein superimposition, that allows protein structures *flexibility* to bend or rotate in order to come into alignment. While flexibility has been introduced into the study of protein folding in the context of docking [9, 26], and particularly for the modeling of ligand binding [62] and most recently in decoy construction for ab initio folding algorithms [86, 92], it has only recently been incorporated into general-purpose pairwise [87, 110] and multiple [111] structure alignment programs. There are two reasons it makes sense to introduce flexibility into protein structure alignment: the first is the main reason that's been addressed in previous work, namely, proteins that do not align well by means of rigid body transformations because their structures have been determined in different conformational states: a wellknown example is that the fold of a protein will change depending on whether it is bound to a ligand or not [62]. Matt is designed to also address the second reason to introduce flexibility into protein structure alignment, namely to handle structural distortions as we align proteins whose structural environment becomes increasingly divergent outside the conserved core.

#### 1.3.2 BetaWrapPro

In Chapter 3 we introduce the program BetaWrapPro that recognizes, and gives sequencestructure alignments for, proteins that are members of the single-stranded right-handed pectin lyase-like beta-helix superfamily, and several beta-trefoil superfamilies. BetaWrap-Pro uses sequence profiles, pairwise beta-strand hydrogen bonding preferences, and comparative modeling to recognize proteins that lie in these superfamilies. Given a sequence, BetaWrapPro uses BLAST to create a sequence profile containing information about which residues tend to align at each position of the input sequence. Dynamic programming is then used to locate the highest scoring matches to a template consisting only of gap length ranges and hydrogen-bonded beta-strands pairs. The score is the combination of pairwise hydrogen-bonding propensities of residues in beta-strands, gap penalties, and residue preferences learned from the proteins in the superfamily used to create the template. The highest scoring hits are then threaded onto the backbone of known structures using SCWRL [90], and those that are not good fits are removed. One important feature of the BetaWrapPro algorithm is that the hydrogen-bonding propensities, which are the primary component of the score, are learned from superfamilies other than the one being recognized. BetaWrapPro is a generalization of our previous work: BetaWrap [12] and Wrap-and-Pack [69] – programs that introduced the threading method we employ with scoring based on pairwise beta-strand hydrogen bonding preferences (Wrap-and-Pack is Menke's masters thesis and he worked on BetaWrap as an undergraduate). BetaWrapPro extends this to profiles, and by the incorporation of side-chain packing. It is shown that BetaWrapPro performs better than HMMs or the Raptor [108] threader on recognition and sequence-structure alignment of the beta-helices and beta-trefoils.

#### **1.3.3 SMURF**

Finally, in Chapter 4 we introduce SMURF ("Structural Motifs Using Random Fields"), a method that uses Markov random fields (MRFs) [72], an extension of Markov models, to train a model to identify a set of homologous proteins. SMURF uses the beta-strand propensities much like BetaWrapPro, but learns the model autonomously and learns individual residue probabilities from the input alignment. Given a multiple structure alignment generated by Matt, SMURF generates a Markov random field much like the HMMs generated by HMMER. The generated MRFs have match, insertion, and deletion states with the same connections HMMs created by HMMER have. In addition, the MRF has long-distance probability dependencies on match states corresponding to pairs of residues hydrogen-bonded to each other across a beta-sheet. Because of these additional dependencies, an HMM is no longer sufficient for the model. SMURF then trains the MRF just like HMMer, though it uses the BetaWrapPro tables for pairwise emission probabilities of the hydrogen-bonded beta residue pairs, because of sparse data. Sequences of unknown structure are then run against the MRF using dynamic programming, much like an HMM. The pairwise dependencies between hydrogen bonded beta-strands can result in significantly improved discrimination in predominantly beta structures. Because of the long range dependencies, significantly more memory and computation time is needed by SMURF than by HMM-based algorithms. We demonstrate that SMURF has significantly better performance than ordinary HMM methods on the six, seven, and eight-bladed beta-propeller folds.

### **1.3.4** Conclusions

We show in this thesis, that better structural alignments (Matt), capture of statistical dependencies of hydrogen-bonded beta residue pairs, profiles, and extensions of HMMs to a MRF framework can improve structural motif recognition for SCOP beta-structural superfamilies. We discuss future work, limitations of the methods, and open problems in Chapter 5.

# Chapter 2

# Matt: Local Flexibility Aids Protein Multiple Structure Alignment

### 2.1 Introduction

Proteins fold into complicated highly asymmetrical 3-D shapes. When a protein is found to fold in a shape that is sufficiently similar to other proteins whose functional roles are known, this can significantly aid in predicting function in the new protein. In addition, the areas where structure is highly conserved in a set of such similar proteins may indicate functional or structural importance of the conserved region. Given a set of protein structures, the protein structural alignment problem is to determine the superimposition of the backbones of these protein structures that places as much of the structures as possible into close spatial alignment.

We introduce an algorithm that allows local flexibility in the structures which allows it to bring them into closer alignment. The algorithm performs as well as its competitors when the structures to be aligned are highly similar, and outperforms them by a larger and larger margin as similarity decreases. In addition, for the related classification problem that asks if the degree of structural similarity between two proteins implies if they likely evolved from a common ancestor, a scoring function assesses, based on the best alignment generated for each pair of protein structures, whether they should be declared sufficiently structurally similar or not. This score can be used to predict when two proteins have sufficiently similar shapes to likely share functional characteristics.

### **2.1.1 Performance Metrics**

There are two related problems that protein structure alignment programs are designed to address. The first we will call the *alignment* problem, where the input is a set of k proteins that have a conserved structural common core, where the common core is defined as in Eidhammer et al. [29] as a set of residues that can be simultaneously superimposed with small structural variation. The desired output consists of a superimposition of the proteins in 3-D space, coupled with the list of which amino acid residues are declared to be in alignment and part of the core. The second problem, which we will call the *discrimination* problem, takes as input a pair of protein structures, and the output a yes/no answer, together with an associated score or confidence value, as to whether a good alignment can be found for these two protein structures or not. We discuss how to measure performance on the alignment problem first, and then on the discrimination problem below.

The classical geometric way to measure the quality of a protein structural alignment involves two parameters: the number of amino acid residue positions that are found to participate in the alignment (and are therefore found to be part of the conserved structural core), as well as the average pairwise root mean squared deviation (RMSD) (where RMSD is calculated from the best rigid body transformation using least squares minimization [52]) between backbone alpha-carbons placed in alignment in the conserved core. Clearly, this is a bi-criteria optimization problem: the goal is to *minimize* the RMSD of the conserved core while *maximizing* the number of residues placed in the conserved core.

We first take a traditional geometric approach: reporting for all programs and all benchmark datasets, the average number of residues placed into the common core structure, alongside the average RMS of the pairwise RMSDs among all pairs of residues that participate in a multiple alignment of a set of structures. In addition, results are compared against Homstrad reference alignments. This approach follows Godzik and Ye's evaluation of their *multiple* structure alignment program, POSA [111].

More sophisticated geometric scoring measures have also been suggested, some to col-

lapse the bi-criteria optimization problem into a single score to be optimized [58], such as the Structal score [71], others to incorporate more environmental information into the similarity measure, such as secondary structure, or solvent accessibility [51, 99]. The *p*-value score that we develop to handle the discrimination problem, described below, is a collapse of the bi-criteria optimization problem into one score that provides a single lens on pairwise alignment quality.

An alternative approach to measuring the performance of a structure alignment algorithm comes from the discrimination problem directly. Here, the measure is typically receiver operating characteristic (ROC) curves; looking for the ratio of true and false positives and negatives from a "gold-standard" classification for what is alignable or not, based either on decoy structures or a classification scheme such as SCOP or CATH. Indeed, a possible concern with adding flexibility to protein structure would be that the added flexibility in our alignment might lead to an inability to distinguish structures that should have good alignments from those that do not. We therefore test our ability to distinguish true alignable structures from decoys on the SABmark dataset (which comes with a ready-made set of decoy structures) as compared to competitor programs.

### 2.1.2 Our Contribution

We introduce the program Matt (Multiple Alignment with Translations and Twists), an AFP fragment chaining method for pairwise and multiple sequence alignment that outperforms existing popular multiple structure alignment methods when tested on standard benchmark datasets. At the heart of Matt is a relaxation of the traditional rigid protein backbone transformations for protein superimposition, which allows protein structures *flex-ibility* to bend or rotate in order to come into alignment. While flexibility has been introduced into the study of protein folding in the context of docking [9, 26], particularly for the modeling of ligand binding [62], and more recently in decoy construction for ab initio folding algorithms [86, 92], it has only recently been incorporated into general-purpose pairwise [87, 110] and multiple [111] structure alignment programs. There are two reasons it makes sense to introduce flexibility into protein structure alignment. The first is the main reason that has been addressed in previous work, namely, aligning proteins that do not align well by means of rigid body transformations because their structures have been determined in different conformational states: a well-known example is that the fold of a protein will change depending on whether it is bound to a ligand or not [62]. Matt is designed to also address the second reason to introduce flexibility into protein structure alignment, namely to handle structural distortions as we align proteins whose shape becomes increasingly divergent outside the conserved core.

We find that at each fixed value for number of aligned residues, Matt is competitive with other recent multiple structure alignment programs in average RMSD on the popular Homstrad [70] and outperforms them on the SABmark [103] benchmark datasets (see Tables 2.1, 2.2 and 2.3). We emphasize again that this is an *apples-to-apples* comparison of the best (i.e., the standard least squares RMSD minimization) rigid body transformation for Matt's alignments, just as it is for the other programs– while Matt allows impossible bends and breaks in intermediate stages of the algorithm, it is stressed that the final Matt alignments and RMSD scores come from legal, allowable "unbent" rigid body transformations. We also present RMSD/alignment length tradeoffs for Matt performance on the same datasets. In the case of Homstrad, where a manually curated "correct" structural alignment is made available as part of the benchmark, Matt alignments are also measured against the reference alignments, where we are again competitive with or outperforming previous structure alignment programs (see Table 2.1).

In addition, Matt's ability to distinguish truly alignable folds from decoy folds is tested with the standard benchmark SABmark set of alignments and decoys [103]. The SABmark decoy set was constructed to contain, for each alignable subset, decoy structures that belong to a different SCOP superfamily, but whose sequences align reasonably well according to BLAST [103]. Thus, they may be more similar at the local level to the true positive examples, and thus fool a structure alignment program better than a random structure. Here, we tested both the "unbent" Matt alignments described above, but also the "bent" Matt alignments, where the residues are aligned allowing the impossible bends and breaks. We test Matt's performance both against the decoy set and also against random structures taken from the Protein Data Bank (PDB; http://www.rcsb.org/pdb). We use Matt's performance

on the truly random structures to generate a *p*-value score for pairwise Matt alignments. Rather than choose from among the large number of competitor pairwise structural alignment programs, Matt was instead tested against other multiple structure aligners, in fact the same programs we used for measuring how well they aligned protein families known to have good alignments. The exception was that we also tested the FlexProt program [87], a purely pairwise structure alignment program that was of special interest because it also claims to handle flexibility in protein structures.

We have made Matt's source code along with its structural alignments available at http://groups.csail.mit.edu/cb/matt and http://matt.cs.tufts.edu so anyone can additionally compute any alternate alignment quality scores they favor.

### 2.1.3 Related Work

The only general protein structure alignment programs that previously tried to model flexibility are FlexProt [87] and Ye and Godzik's FATCAT [110] (both for pairwise alignment), and FATCAT's generalization to multiple structure alignment, POSA [111]. FATCAT is also an AFP chaining algorithm, except it allows a globally minimized number of translations or bends in the structure if it improves the overall alignment. In this way, it is able to capture homologous proteins with hinges, or other discrete points of flexibility, due to conformational change. Our program Matt is fundamentally different: it instead allows flexibilities everywhere between short fragments- that is, it does not seek to globally minimize the number of bends, but rather allows continuous small local perturbations in order to better match the "bent" RMSD between structures. Because Matt allows these flexibilities, it can put strict tolerance limits on "bent" RMSD, so it only keeps fragments that locally have very tight alignments. Up until the last step, Matt allows the dynamic program to assemble fragments in ways that are structurally impossible- one chain may have to break or rotate beyond the physical constraints imposed by the backbone molecules in order to simultaneously fit the best transformation. This is repaired in a final step, when the residue to residue alignment produced by this unrealistic "bent" transformation is retained; the best rigid-body transformation that preserves that alignment is found, and then



Figure 2-1: Overview of the Matt algorithm

either output along with the residue-residue correspondences produced by the "bent" Matt alignment *or* extended to include as yet unaligned residues that fall within a user-settable maximum RMSD cutoff under the new rigid-body transformation to form the final Matt "unbent" alignment.

#### 2.1.4 Matt Implementation

Matt accepts standard PDB files as input, and outputs alignment coordinates in PDB format as well. In addition, when only two structures are input, Matt outputs a *p*-value for whether or not Matt believes the structures are alignable (see below). There is an option to output the "bent" structures in PDB format. Matt also outputs the sequence alignment derived from the structural alignment in FASTA format and a RasMol script to highlight aligned residues. Windows and Linux binaries and source code are available at http://groups.csail.mit.edu/cb/matt and http://matt.cs.tufts.edu.

### 2.2 Algorithm Overview

The input to Matt is a set of g groups of already multiply aligned protein structures (at the beginning of the algorithm, each structure is placed by itself into its own group). The

iterative portion of the Matt algorithm runs g - 1 times, each time reducing the number of separate groups by 1 as it merges two sets of aligned structures in a progressive alignment. As we discuss in detail below, the Matt alignments produced in the iterative portion are not geometrically realized by rigid body transformations: they allow local "bends" in the form of transpositions and rotations. Once there is only one group left, Matt enters a final pass, where it corrects the global alignment into an alignment that obeys a user-settable RMSD cutoff by means of geometrically realizably rigid-body transformations. A flowchart describing the stages of the Matt algorithm appears in Figure 2-1.

#### The iterative portion: fragment pairs

There are three main phases to the iterative portion of the Matt algorithm. The first phase is similar to what is done by many existing AFP chaining residues: for simplicity, it is first described here for pairwise alignment (that is, when each group consists of a single structure). Matt considers fragments of five to nine adjacent amino acid residues. A fragment pair is a pair of fragments of equal length, one from each structure. For every fragment pair, between any pair of structures, an alignment score is calculated based on an estimated *p*-value of the minimum RMSD achievable by a rigid-body transformation of the C-alpha atoms of one fragment onto the other. *p*-values are estimated by generating a table of random RMSD alignments of the National Center for Biotechnology Information (NCBI) non-redundant PDB.

The generalization from aligning fragments from two structures to aligning fragments from two groups of multiple structure alignments is straightforward. The alignment score of a pair of fragments, one from each group alignment, is calculated based on a single rigid-body transformation acting on all of a group's structures together.

#### Dynamic programming assembly with translations and twists

Matt's main novel contribution involves how we assemble these short fragments into a global alignment. Note that Matt is an alignment program that respects the sequential order of residues along the backbone, so it only assembles aligned fragments that are consistently ordered.

Matt iteratively builds up longer and longer sets of aligned fragments using dynamic programming. When deciding whether to chain two sets of aligned fragments together, Matt uses a score based on the sum of the alignment scores of the individual aligned fragments together with a penalty based on the geometric consistency of the transformations associated with deforming the backbone of one set onto the other. Transformation consistency cutoffs were determined empirically using a fifth of the Homstrad benchmark dataset. The consistency score (specified exactly in Methods below) is a function of both relative translation and relative rotation angles; the angles are calculated using quaternions for speed.

Matt finds the highest scoring assembly for all pairs of groups of aligned structures that were input. It then chooses the pair of groups with the highest scoring assembly, and uses that assembly to create a new multiple alignment that merges those two groups. If only one group remains, the algorithm proceeds to the final pass; otherwise, it enters the realign and extend phase before looping back to calculate all fragment pairs again.

#### **Realign and extend phase**

The realignment phase does not change the residue correspondences in the multiple alignment, but tries to find local transformations that tighten RMSD in the aligned fragments in the newly merged group. It is described in more detail in Section 2.4, Methods.

The extension phase is then called. The multiple alignment is extended greedily off both ends of all its fragments as long as average RMSD is below a cutoff (4 Å). Extended fragments are allowed to overlap for up to five residues in this phase (if this produces any inconsistencies in the alignment, note that they are fixed in the next dynamic programming iteration). When only one group of structures remains, the result is the bent Matt alignment. The algorithm enters the final pass to produce the *rigid bent* and *unbent* Matt alignments.

#### **Final pass**

The input to the final pass is simply *which* residues have been aligned with which in the final bent alignment; that is, the multiple sequence alignment derived by the bent multiple structure alignment Matt has generated. Once the mapping of which residues are to be

aligned has been fixed, finding the associate transformation that optimizes RMSD of the aligned residues of one structure against a set of structures aligned to a reference structure is straightforward. We build up a single multiple structure alignment from such transformations using a similar method to that introduced by Barton and Sternberg [5]. In particular, additional protein structures are added progressively to the overall alignment. Each time a new structure is added, all existing structures are "popped out" in turn, and re-aligned back to the new reference alignment. This brings the atoms into tighter and tighter alignment.

The resulting rigid RMSD Matt alignment leaves the sequence alignment from the bent step *unchanged*, and thus only includes sets with five or more contiguous residues. This alignment is what we call the *rigid bent* Matt alignment, below. We then do a final pass to add back shorter segments. In particular, now that we have a final global multiple structure alignment, we greedily add back in fragments of four or fewer residues that fall between already aligned fragments but whose RMSD is below a user-settable cutoff. That user-settable cutoff is entirely responsible for the different tradeoffs between average RMSD and number of aligned residues that we obtain (see Figures 2-2 and 2-3)– in the comparisons with other programs, the cutoff was uniformly set at 5 Å.

### 2.3 Results

### **2.3.1** The Benchmark Datasets

Perhaps the most popular dataset for testing protein structural alignment programs is Homstrad [70], which is a manually curated set of 1,028 alignments, each of which contains between two and 41 structures. Homstrad contains highly homologous proteins, with similarity comparable to the *family* level of the hierarchical SCOP [73] structural classification database. In this paper, in order to be comparable to the results for POSA presented in [111], we test only on the 399 Homstrad alignments with more than two structures in the alignment (that is, Homstrad sets with between three and 41 structures that necessitate a multiple rather than a pairwise structure alignment program).

We also test Matt on the superfamily and twilight zone SABmark [103] benchmark

datasets. The superfamily set contains 3,645 domains sorted into 426 subsets representing structures at the superfamily level of the SCOP hierarchy, a set designed to be welldistributed in known protein space, and presumably containing more remote homologs than Homstrad. The twilight zone set contains 1,740 domains sorted into 209 subsets whose homology is even more remote than the superfamily set. Both the superfamily and twilight zone sets have subsets containing between three and 25 structures.

Since the "correct" alignments provided by SABmark are generated automatically from existing structure alignment programs, we do not report the percentage of "correctly" aligned residue pairs as we did for the manually curated Homstrad, but rather report only the objective geometric measures of alignment quality (number of residues placed in the conserved core, and average pairwise RMSD among residues placed in the combined core).

SABmark additionally provides a set of decoy structures for nearly all its 462 sets of alignable superfamily (and 209 alignable twilight zone) sets of structures. We constructed a *decoy* discrimination test suite as follows. Each SABmark superfamily (or twilight zone) test set comes with an equal number of decoy structures with high sequence similarity (see [103]). For each test set, a random pair of structures in the positive set (that belong to the same SCOP superfamily and are supposed to align) and a random decoy was selected. Then a *random* discrimination test suite was similarly constructed, the only difference being that the decoy was chosen to be a random structure in a different SABmark set, not a decoy structure that was specifically chosen to have high sequence similarity to the positive set.

### **2.3.2** The Programs to Which Matt Is Compared

On Homstrad, we compare Matt to three recent multiple structure alignment programs: listed in alphabetical order, they are MultiProt [88], Mustang [60], and POSA [111]. Note that MultiProt has sequential and non-sequential alignment options; we compare against the option that, like Matt, respects sequence order. MultiProt is an AFP program that uses rigid body superimposition. Mustang uses a combination of short fragment alignment, contact maps, and consensus-based methods. We were particularly eager to test Matt against

POSA, because it is the only other multiple structure alignment program that allows flexibility, though as discussed in the Introduction, POSA's flexibility is more limited. POSA outputs two different structural alignments: one comes from the version of POSA that disallows bends, and the other from the version with limited bends allowed. We test both versions, and results appear in Table 2.1.

We were not able to obtain POSA code. (Our statistics on Homstrad come from POSA alignments provided by the authors as supplementary data). Because we were not able to obtain POSA code, we were not able to test POSA on all of SABmark, but we do compare Mustang and MultiProt to Matt on the entire SABmark benchmark. On the other hand, we were able to submit individual sets of SABmark structures to the POSA online server; POSA sometimes did nearly as well as Matt on the examples we tested, but other times, it missed finding alignable structures entirely. We show both cases in two in-depth examples: Figure 2-4 shows alignments of Matt, MultiProt, Mustang, and POSA on a seven-bladed beta-propeller, and Figure 2-5 shows alignments of the four programs on a set of lefthanded beta-helix structures. POSA and Matt are the only algorithms that successfully align all seven blades of the beta-propeller. POSA, however, entirely misses the alignable regions in the beta-helix fold.

For the discrimination problem, Matt is compared against MultiProt and Mustang again, but also against FlexProt [87]. FlexProt has an option to allow from zero to four bends in the aligned structure, which is specified at runtime. FlexProt scores each of these structures by length of the alignment found. On each structure, the alignment with the number of bends that produces the highest-scoring alignment is output. In the case of both POSA and FlexProt, the "bent" alignment outputs the (best rigid-body transformation) RMSD of the aligned structures with bends allowed, and the "unbent," or regular, version outputs the RMSD of the best rigid-body transformation that places the same set of residues in alignment as the bent version.

Program Name	Average Core Size	Average Normalized Correct Pairs	Average RMSD
MultiProt	142.331	132.350	1.347
Mustang	171.363	155.932	2.669
POSA (unbent)	165.160	152.475	2.004
POSA (bent)	167.847	154.482	2.224
Matt	172.276	155.352	2.044

Table 2.1: Homstrad performance comparison

### 2.3.3 Performance

Table 2.1 shows the following quantities for each program on the 399 Homstrad reference alignments that contain at least three structures each (this is the identical set of reference alignments on which POSA was tested). The first field is the average number of residues placed in the common core. The second is "average normalized correct pairs" computed according to the Homstrad reference alignments. This quantity is computed as follows: for each set of structures, we look at every pair of aligned residues that also participate in a Homstrad correct alignment. Then, we normalize based on the number of structures in the set (so the alignments in the set of 41 structures do not weight more heavily than the alignments in the set of three structures), dividing by the number of pairs of distinct structures in the reference set. (Note that, as discussed in [60], having additional pairs placed into alignment that Homstrad does not consider part of the "gold-standard" alignment is a positive, not a negative, if RMSD remains low. This is because declaring a pair of nearly aligned residues "aligned" or not is a judgment call that Homstrad makes partially based on older multiple structure alignment programs whose performance is weaker than the most recent programs.) The second column is the same "average RMSD" measure that POSA reports: the average RMS of the pairwise RMSDs among all pairs of residues that participate in a multiple alignment in a set of structures.

We downloaded and ran MultiProt and Mustang and computed RMSD statistics ourselves. POSA is only accessible as a web server; however, Homstrad alignments are available online at http://fatcat.burnham.org/POSA/POSAvsHOM.html. POSA's website provides two sets of multiple alignments: one derived from running their algorithm allowing geometrically impossible bends, and one running an unbent version of their algorithm. Note that for POSA's bent alignments, we had to recalculate RMSD from the multiple se-


Figure 2-2: Matt SABmark performance tradeoff

Average pairwise RMSD versus average number of residue positions placed in the common core.

quence alignment provided from their bent alignments, because unbent RMSD based on bent alignments was not provided on their website. It is of independent interest that, as expected, POSA's unbent version has better RMSD, while POSA's bent version finds more residues participating in the alignments overall.

Matt scores slightly better than POSA on Homstrad. Matt's average core size is comparable with that of Mustang, but Matt has a lower RMSD. The size of the alignments that MultiProt finds are much smaller than for the other programs (though its average RMSD is therefore much lower): this becomes even more pronounced on the more distant structures in SABmark (see Figure 2-2). Note that the core-size/RMSD tradeoff of Matt is very sensitive to cutoffs set in the last pass of the Matt algorithm, when it is decided what segments of less than five consecutive residues are added back into the alignment. Throughout this paper, the results reported in our tables come from setting the cutoff at 5 Å. By comparison, if the cutoff is set at 3.5 Å, Matt achieves 168.038 average core size, 153.362 average normalized pairs correct, and 1.862 average RMSD on Homstrad. Full tradeoff results on RMSD versus number of residues based on changing the last pass cutoff appear in Figure 2-3. Note that Matt's cutoffs for allowable bends were trained on a random 20% of the Homstrad dataset.



Figure 2-3: Matt Homstrad performance tradeoff

Average pairwise RMSD versus average number of residue positions placed in the common core

Program Name	Average Core Size	Average RMSD
MultiProt	68.701	1.498
Mustang	104.162	4.146
Matt	104.692	2.639

Table 2.2: SABmark superfamily performance comparison

Program Name	Average Core Size	Average RMSD
MultiProt	36.354	1.536
Mustang	66.833	5.035
Matt	66.967	2.916

Table 2.3: SABmark twilight zone performance comparison

While Matt competes favorably with the other programs on Homstrad, Matt was designed for sets of more distantly related proteins than appear in the Homstrad benchmark. Thus, the best demonstration of the advantage of the Matt approach appears on the more distantly related proteins in the SABmark benchmark sets. Here, Matt is seen to do exactly what was hoped: by detouring through bent structures, it finds rigid RMSD alignments that place as many residues in the conserved alignment as Mustang does (and more than 50% more than MultiProt does) while reducing the average RMSD from that of Mustang by more than 1.4 Å (see Tables 2.2 and 2.3). It should again be emphasized that none of Matt's parameters were trained on SABmark.

Looking by hand through the alignments, MultiProt consistently aligns small subsets of residues correctly, but leaves large regions unaligned that both Mustang and Matt believe to be alignable. Mustang, on the other hand, frequently misaligns regions, particularly in the case when there are many alpha-helices tightly packed in the structure. On two of the twilight zone sets, Mustang fails to find anything in the common core. Altogether on the twilight zone set, there are four sets of structures for which Mustang fails to find at least three residues in the common core (and there is one set of structures in the superfamily set where Mustang also fails to find anything in the common core). Though the effect is negligible, these four sets are removed from Mustang's average RMSD calculation.

Although these tables show overall performance, it is also helpful to look at actual examples. We pulled two example reference sets out of the SABmark superfamily benchmark. Figure 2-4 shows the Matt alignment versus MultiProt, POSA, and Mustang alignments of the SABmark structures in the set labeled Group 137 (beta-propellers; PDB IDs d1nr0a1, d1nr0a2, d1p22a2, and d1tbga). POSA does second best to Matt here, and in fact, the overall alignment of the structures in POSA is most similar to Matt– the same propeller blades are overlaid in both alignments. Although it is hard to see in the picture, Mustang is superimposing the wrong blades, which accounts for the terrible RMSD. MultiProt makes a similar error, but then gets a low RMSD by aligning less of the structure. Figure 2-5 shows a Matt alignment of the SABmark structures in the set labeled Group 144 (beta-helices; PDB IDs d1hm9a1, d1kk6a, d1krra, d11xa, d1ocxa, d1qrea, d1xat, and d3tdt). Here, POSA



Figure 2-4: Comparative beta-propeller alignment

The four SABmark domains in the set Group 137, consisting of seven-bladed beta-propellers as aligned by POSA, Mustang, MultiProt, and Matt. Backbone atoms that participate in the common core of the alignment show up colored as red (PDB ID d1nr0a1), green (PDB ID d1nr0a2), blue (PDB ID d1p22a2), and magenta (PDB ID d1tbga); residues in all four chains that are not placed into the alignment by the tested algorithm are shown in gray. These pictures were generated by the Swiss PDB Viewer (DeepView) [38].

the portion that it declares in the common core very tightly (this is a theme throughout the SABmark dataset), but it only places five rungs in the common core. Both these figures were generated using the Swiss PDB Viewer (DeepView) [38]. Core size and RMSD comparisons on both these reference sets appear in Table 2.4.

We then turn to the discrimination problem. Matt, FlexProt, Mustang, and MultiProt were tested on the SABmark superfamily and SABmark twilight zone decoy test suites described in the previous section. Using a method similar to what Gerstein and Levitt [34] did to systematically assess structure alignment programs against a gold standard, length of alignment versus RMSD for the true positives and true negatives were plotted in the plane



Figure 2-5: Comparative beta-helix alignment

Aligned portions of the eight SABmark domains in the set Group 144, consisting of the left-handed beta-helix fold as aligned by POSA, Mustang, MultiProt, and Matt. Backbone atoms that participate in the common core of the alignment show up colored as red (PDB ID d1hm9a1), green (PDB ID d1kk6a), blue (PDB ID d1kra), magenta (PDB ID d1lxa), yellow (PDB ID d1ocxa), orange (PDB ID d1qrea), cyan (PDB ID d1xat), and pink (PDB ID d3tdt); residues in all three chains that are not placed into the alignment by the tested algorithm are shown in gray. These pictures were generated by the Swiss PDB Viewer (DeepView) [38].

Program Name	Propeller Core Size	Propeller RMSD	Beta-Helix Core Size	Beta-helix RMSD
MultiProt	180	1.73	79	1.01
Mustang	218	6.13	83	7.05
POSA	252	2.62	23	3.13
Matt	261	2.35	98	2.42

Table 2.4: Sample multiple structure alignments from SABmark benchmark



Figure 2-6: Distinguishing alignable structures from decoys

Positive (blue) and SABmark decoy (red) pairwise alignments plotted by RMSD versus number of residues for Matt, FlexProt, MultiProt, and Mustang on the SABmark superfamily set.

for all programs. Figure 2-6 displays the results on the SABmark superfamily set versus SABmark decoys. The separating line marks where the true positive and true negative percentages are roughly equal.

When comparing ROC curves over the four different programs, we find that Matt consistently dominates both FlexProt and MultiProt at almost every fixed true positive rate. Mustang does as well. Interestingly, Matt and Mustang are incomparable– on the Superfamily sets, Matt does better than Mustang when the true positive rate is fixed over 93% (90% for the random decoy set), and Mustang does better thereafter. For the twilight zone set, the situation is reversed: SABmark does better than Matt when the true positive rate is between 93% and 98%, but Matt does better between 70% and 92% true positives; then, performance reverses, and Mustang does better below 70% true positive rates. Sample percentages for the four programs near the line where the true positive and true negative percentages are roughly equal appear in Tables 5 and 6 on the superfamily and twilight zone family sets, respectively.

Unsurprisingly, for all four programs, the SABmark decoy set was more difficult to

True	Matt N	Negative	MultiPro	MultiProt Negative Mustan		g Negative	FlexProt Negative	
Positive	Random	SABmark	Random	SABmark	Random	SABmark	Random	SABmark
95.04	81.80	71.16	49.88	47.28	74.94	71.63	64.30	46.81
94.09	84.63	75.65	60.99	56.03	76.36	73.29	72.10	54.14
93.14	85.82	77.30	70.45	65.72	82.51	78.96	78.01	62.65
92.20	87.00	79.20	76.83	72.58	85.82	82.03	81.80	68.79
91.02	90.54	82.74	81.56	79.20	89.60	84.16	87.71	75.89
90.07	92.43	86.52	84.16	82.74	94.33	89.36	90.78	78.82

Table 2.5: Discrimination performance on the SABmark superfamily set

True negative percentage correct on the multiple structure alignment programs at a fixed true positive percentage rate in the range close to where the true positive and true negative rates are equal. Results in **bold** are the best at that fixed true positive rate.

True	Matt Negative		MultiProt Negative		Mustang Negative		FlexProt Negative	
Positive	Random	SABmark	Random	SABmark	Random	SABmark	Random	SABmark
85.17	85.65	83.73	71.29	70.81	77.99	77.03	78.47	67.94
84.21	88.52	84.21	74.16	73.68	78.95	77.51	80.38	69.86
83.25	89.95	85.17	74.64	74.16	80.86	78.47	80.86	70.33
82.30	90.43	86.12	76.08	75.12	81.34	78.95	81.82	72.73
81.34	90.91	86.12	77.03	75.60	82.30	80.38	82.30	73.68
80.38	92.34	87.56	77.03	76.56	84.69	81.82	82.30	73.68

Table 2.6: Discrimination performance on the SABmark twilight zone set

True negative percent correct on the multiple structure alignment programs on the more difficult SABmark twilight zone set at a fixed true positive percentage rate, in the range close to where the two rates are equal. Results in bold are the best at that fixed true positive rate. Matt is always the best in this range.

classify than the random decoy set. What was more surprising is how competitive Mustang is with Matt on the discrimination tasks— it is surprising because Mustang was uniformly worse at the alignment problem. In essence, Mustang produces alignments with very high RMSD, but consistently even higher RMSD on the decoy sets. We hypothesize that this may be due to Mustang's use of contact maps, a global measure of fold-fit that may be harder for decoys to match, whereas the decoys may have long regions of local similarity. Matt and Mustang both do qualitatively better at all discrimination tasks than either MultiProt or FlexProt.

Note that in Figure 2-6 and in both Tables 2.5 and 2.6 we have used the RMSD of the best rigid-body transformation that matches the *bent* Matt or FlexProt alignment. At first, we hypothesized that the bent RMSD values might give better discrimination; after all, the bent structures are the local pieces that align really well. However, giving credit for the lower bent RMSD values also greatly improved the RMSD values for the decoy structures, leading in every case to worse performance on the discrimination tasks. Thus, reporting

an RMSD value for the rigid superimposition that minimized the RMSD of the residues placed into a bent alignment produced the best separation of true alignments from decoys.

### **2.3.4** *p*-Value Calculation

*p*-values for pairwise Matt alignments are calculated based on our 2-D alignment versus RMSD graphs. To calculate *p*-values, we find the slope m of a line in the alignment length versus RMSD graph that maximizes the number of elements from the random negative set on one side and has at least 90% of the SABmark positives on the other. This value was chosen because it allows roughly the same percentage of the negative set to be on the other side. These were then used to calculate *z*-scores of the distribution of RMSD –  $m \times length$  of the random negative set. These are fit to a standard Gaussian distribution to calculate *p*-values for pairwise alignments.

### 2.4 Methods

### 2.4.1 Pairwise alignment

First, it is useful consider Matt's behavior on pairwise alignments. In what follows, we assume structures are sequentially ordered from their N terminal to their C terminal.

#### Notation and Definitions

**Definition 2.4.1** A block denotes the C-alpha atoms of a set of five to nine adjacent amino acid residues in a protein structure. For block B, let  $b_h$  denote the first residue and  $b_t$  denote the last residue of the block. A block pair is a pair of blocks of equal length, one from each of a pair of structures.

For block pair BC, define  $T_{CB}$  to be the minimum RMSD transformation that is applied to C to align its C-alpha carbons against those of B, and let  $\text{RMSD}_{BC}$  denote the RMSD of the two blocks under  $T_{CB}$ . Minimum transformations are calculated using the standard classical singular value decomposition method of Kabsch [52].



Figure 2-7: Assembling sequential block pairs

Two Sequential Block Pairs that could form part of an assembly. Block pair BC precedes block pair DE because B precedes D and C precedes E in their respective protein sequences.

**Definition 2.4.2** For block pair BC,

$$Score(BC) = -\log Pr[RMSD_{BC}]$$

Here, *p*-values are estimated by generating a table of random five-residue RMSD alignments of the NCBI non-redundant PDB [39] (update dated 7 May 2007) with a BLAST *E*-value cutoff of  $10^{-7}$ . For longer block pairs, negative log *p*-values for a given RMSD are assumed to increase linearly with respect to alignment length. (This assumption was verified empirically to be approximately true in the relevant range.)

**Definition 2.4.3** Let S be a set of block pairs. Two block pairs BC and DE are sequential if  $b_t$  precedes  $d_h$  (and  $c_r$  precedes  $e_h$ ) and there is no block pair with any residue that lies between them in S.

**Definition 2.4.4** A set of block pairs is called an assembly if it consists of block pairs  $P_1$ ,  $P_2, \ldots, P_n$  such that  $P_i$  and  $P_{i+1}$  are sequential.

Note that the definition of sequential means that the  $P_i$  will be non-overlapping and seen in both structures in precisely this order; see Figure 2-7.

### Matt Assembly

A Matt pass uses dynamic programming to create an assembly of block pairs. A pass takes an assembly and three cutoff values as input and outputs a new assembly. The new assembly contains all the block pairs of the original assembly. The three cutoffs are a maximum block-pair RMSD cutoff and maximum values for the displacement and relative angles for each sequential pair of blocks (the "translations" and "twists," respectively, of Matt's acronym). Using multiple passes and relaxing cutoffs in each successive pass results in favoring strongly conserved regions while still detecting more weakly conserved regions.

All Matt results in this paper use a three-pass algorithm. All three passes use a cutoff of 45 on the angle between the transformations of two sequential block pairs. The first pass is restricted to block pairs with a minimum negative log p-value of 2.0, and sequential block pairs must have a displacement no greater than 4. The second pass uses a minimum negative log p-value of 1.6 and a maximum displacement of sequential pairs of 5. The last pass uses cutoffs of 0.6 and 10, respectively. The values of these cutoffs were determined by training on a random 20% of the Homstrad benchmark dataset.

More formally, the score of a set of block pairs S is the sum of the alignment scores of the individual block pairs and a bonus based on how consistent the transformations associated with the two block pairs are. This score is used internally throughout the construction of the alignment, but is not used to determine the p-value, which is instead computed directly based on length and RMSD of the resulting alignments; see the section on calculating p-values at the end of Section 2.1.

$$\begin{aligned} \text{Score}(S) &= \sum_{BC \in S} -\log(\text{Pvalue}(\text{RMSD}_{BC})) + \\ &\sum_{BC,DE} \text{ sequential in } S - \log(\text{SolidAngle}(\text{Angle}(T_{CB}, T_{ED}))/2) + \\ &\sum_{BC,DE} \text{ sequential in } S - \text{Displacement}(BC, DE) \end{aligned}$$

where

$$Displacement(BC, DE) = (Length(T_{CB}(c_t) - T_{ED}(c_t)) + Length(T_{CB}(e_h) - T_{ED}(e_h)))/2$$

and Length is defined to be ordinary Euclidean distance, Angle is the angle of  $T_{CB}T_{ED}^{-1}$ in axis-angle form, and SolidAngle is the solid angle associated with an angle, measured as a fraction of the sphere. SolidAngle(q) ranges from 0 to 1 and is the probability of a given ray and a random point in 3-D space forming an angle less than q. To prevent overflow, if Angle has a value below 0.1 radians, it is set to 0.1 radians.

We note that a naive implementation of dynamic programming would use  $O(n^4)$  time (where n is the length of the longer string), as there are  $O(n^2)$  block pairs. We reduce this to an  $O(n^3 \log n)$  algorithm by incorporating geometric knowledge of the structural transformations to reduce the search space. In particular, for each of structure two's C-alpha atoms, an oct-tree [43] that partitions Euclidean space based on the transformed positions of that C-alpha atom is created. Each transformation comes from a previously considered block pair that ends with the C-alpha atom in question. When the dynamic program is assembling a block pair starting with the kth C-alpha atom in structure two, it searches the oct-trees for all of structure two's C-alpha atoms before k for compatible transformations (meaning the associated transformations of the atom are within the distance cutoff).

### **Final Output**

The final output is an assembly A, a bent assembly A' (only output with a command-line option), BentRMSD(A'), UnbentRMSD(A), and a p-value for the assembly.

The result of the dynamic programming algorithm described above gives the bent alignment A', together with a set of local transformations (allowing translations and rotations) that produced the alignment. Its associated RMSD is BentRMSD(A').

To produce the unbent alignment, the set of which residues are to be placed into alignment is retained from A', and all geometric information is discarded. Then, the best global rigid-body transformation that minimizes the RMSD of this alignment is found using the classical SVD method of Kabsch [52]. The result is the rigid-bent RMSD, which is not output explicitly, but implicitly forms the basis for the *p*-value calculation (as described in the *p*-value section at the end of Section 2.1, the Introduction). Note that so far the sequence alignment from the bent step is unchanged, and thus only includes sets of contiguous residues that are at least 5 Å in length. A final pass then greedily adds back shorter segments of four or fewer residues that fall between already aligned fragments but whose RMSD under the global transformation falls below a user-settable cutoff. The resulting alignment is A, with its associated unbent RMSD(A).

### 2.4.2 Multiple Alignment

In this subsection, we extend the definitions of assemblies to sets of more than two structures in the natural way. The input to each iteration of the Matt multiple alignment algorithm is the set of structures to be aligned that have been partitioned into sets, where the structures in each set are multiply aligned in an assembly. The output of the iteration leaves all but two sets unchanged; the structures in those two sets are merged into a single set with a new multiple alignment assembly. (The initial iteration of Matt places each structure into its own set and is equivalent to the pairwise alignment algorithm described above.)

Analogous to blocks, we define *block-tuples*.

**Definition 2.4.5** A block-tuple is an aligned set of equal-length blocks. A block-tuple pair is a set of two block-tuples, one from each of two sets of aligned structures.

At each iteration, for every pair of sets in the partition, Matt uses the merge procedure detailed below to combine the two assemblies into a single assembly and computes its score. It then chooses the highest-scoring pair of sets to merge in that iteration. Matt terminates when all structures have been aligned into a single assembly, outputting the assembly, bent RMSD, and unbent RMSD.

### Merging

Here is a high-level description of the steps of the merge procedure. The merge procedure take as input two assemblies, each possibly containing multiple structures. Each step is explained in more detail:

1. Find the pair of structures,  $a_0$  from assembly A and  $b_0$  from assembly B, that have the highest-scoring pairwise structural alignment, according to the pairwise structural alignment algorithm of the previous section.

- For each block b of a<sub>0</sub>, let T<sub>b</sub> denote the transformation of b back to its original atomic coordinates. Transform every block in the block-tuple associated with b in A by T<sub>b</sub>. Do the same for each block of b<sub>0</sub> and its associated block-tuple.
- 3. Within each of A and B separately, realign all blocks within each block-tuple to reduce RMSD using the LocalOpt procedure (described below).
- 4. Still within each of A and B separately, an extension step is performed than can lengthen block-tuples into unaligned regions or other block-tuples. Note that this step may temporarily produce overlapping blocks, but that this is corrected later, and only non-overlapping block-tuples are returned at the end of the merge procedure.
- 5. Taking the set of all aligned block-tuples of A, we consider all sets of five to nine adjacent residues entirely contained within one of these block-tuples by sliding a window of appropriate length. We do the same for the block-tuples of B. These become the building blocks of new block-tuple pairs in the merged assembly. Just as in the pairwise case, all equal-length building blocks, one each from A and B, are pairwise aligned and scored. Note that the RMSD algorithm easily generalizes to align sets of aligned residues by treating each aligned k-length set of m structures against n structures as a single RMSD alignment of kmn residues. Let  $T_{BA}(r, s)$ be the transformation that produces the lowest RMSD on the block-tuple pair  $r \in$  $A, s \in B$ .
- 6. Dynamic programming is used to find the optimal assembly of pairs of new blocktuples. The dynamic programming algorithm in the multiple structural case has the same form as in the pairwise case. The angle penalty is calculated as before from  $T_{BA}(r, s)$ . The displacement penalty is calculated slightly differently. In each residue position, an average C-alpha atom position is calculated for both A and B. The displacement is calculated using the averages as if they were positions of atoms of single structures in a pairwise alignment. Note that as in the pairwise case, this algorithm does not allow block-tuples to overlap, so the final set of block-tuples that are aligned by the merge procedure will be a legal assembly.

The merge procedure has now been specified except for LocalOpt and the extension procedure. We now explain both these steps in detail.

### LocalOpt

LocalOpt acts independently on A and B; therefore, it is described here only on A. The intuition for the LocalOpt step comes from merges in the previous iterations. The block-tuple alignment that an assembly inherits is the result of a global RMSD alignment of the block-tuple of potentially many protein structures. Therefore, while keeping the residue alignments fixed, it is often still possible to transform the coordinates of the C-alpha atoms to improve bent RMSD. LocalOpt acts separately on each block-tuple in the assembly. In particular, if  $a_0, a_1, \ldots, a_r$  are the structures within a block-tuple (where  $a_0$  is the reference structure as defined by merge), each  $a_i$  is removed in turn and then realigned to minimize RMSD to the other r structures for each block-tuple.

#### **Extension phase**

In the extension phase, both ends of block-tuples of five to nine residues are explored in order to determine if additional adjacent residues have a good multiple alignment. The LocalOpt transformations associated with each block-tuple in each structure are applied to the residues immediately before and after the block-tuple. If the average distance between all pairs of residues in all structures before or after a block-tuple is less than 5 Å, the residues are added to the block-tuple. This is done in a greedy fashion. Note that this allows block-tuples to be longer than nine residues or even to overlap (though in practice, we do not allow them to overlap by any more than five residues to bound computational time).

#### **Final output**

When only one assembly remains, as in the pairwise case, this produces the bent alignment. As before, a final realignment and extension phase is done in which additional *i*-residue segments are greedily added to the common core, for i = 4 down to 1, provided their average RMSD lies below a (user-settable) cutoff. This cutoff is solely responsible for the size of common core/RMSD tradeoff found in Figures 2-2 and 2-3. All residues that were aligned in the iterative phase are kept in the final alignments. Block-tuples are not allowed to overlap in the final extension phase. A new RMSD alignment of the original unbent structures is done, aligning residues according to the extended block-tuples. This assembly, its RMSD, and the sets of aligned residues are the algorithm's unbent output. A p-value is not output when a group of more than two structures is to be aligned.

### 2.5 Discussion

We introduced the program Matt, which showed that detouring through local flexibility in an AFP alignment algorithm could aid in protein multiple structure alignment. We suggest that looking at local bends in protein structure captures similarity well for fundamental biological as well as mathematical reasons. In particular, Matt may be both capturing flexibility inherent naturally in some protein structures themselves and modeling structural distortions in the common core that arise as proteins become more evolutionarily distant.

Matt runs in  $O(k^2n^3 \log n)$  time, where k is the number of sequences participating in the alignment and n is the length of the longest sequence in the alignment. Compared with Mustang and MultiProt, Matt takes about the same amount of time to complete running on the benchmark datasets. We find that Matt is typically several times slower on most sets of structures; however, there are a small percentage of sets of substructures in both benchmark datasets where both Mustang and MultiProt take orders of magnitude more time to complete their alignments than they do on the typical set of structures. Matt is saved in these difficult cases with lots of self-similar substructures by its implementation of the oct-trees, which allows for better pruning of the search space. Matt also supports a multithreaded implementation, which is faster still. Matt is sufficiently fast that it should be feasible to construct a set of reference alignments for similar fold classes based on Matt, covering the space of all known folds, which we intend to do.

Examining some of the Matt alignments by hand, the program seems to typically do a better job of aligning the ends of alpha-helices and beta-strands than its competitors; we

therefore suggest that Matt may be a useful tool for construction of better sequence profiles for protein structure prediction, and for the construction of better templates for protein threading libraries. For these applications, both Matt's rigid unbent alignments and the geometrically impossible bent alignments may be of interest.

Finally, looking at how Matt (or the other structure aligners) performs on the two SABmark benchmarks raises again the philosophical question of how far into the twilight zone it makes sense to align protein structures. Clearly at the superfamily level, there is typically substantial structural similarity. At the twilight zone level, there is much increased divergence. Examining these alignments in more details may help develop our intuition about the limits of comparative modeling for protein structure prediction as we go further into the twilight zone.

# Chapter 3

# **BetaWrapPro**

# 3.1 Introduction

Successful computational prediction of protein structural motifs from sequence remains a very challenging problem. It is most difficult in the case of proteins whose secondary structure is "mainly beta," meaning that many of the amino acid residue participate in beta-sheet formation. While there is evidence that residues involved in beta-sheet formation that are close in space exhibit strong statistical biases [75, 98], these residues may be difficult to discover due to being a variable and potentially long distance apart in the protein sequence. In fact, simply predicting the correct annotation of secondary structure of these folds can be problematic: even the best secondary structure predictors such as PHD [84] and PSIPRED [47] predict alpha-helices more accurately than beta-strands [64]. It has been our experience that general secondary structure predictors do not suffice even to correctly determine the number of beta-strands in a sequence that folds into one of these motifs, never mind finding the ends of the strands. Tertiary structure predictors such as Rosetta [11] and LINUS [95] while performing well on all-alpha and alpha/beta proteins, are also challenged by topologically complex all-beta proteins [11, 95]. Many threading programs also have particular problems recognizing and then threading beta-sheet topologies correctly once sequences fall into the so-called "twilight zone" [83] of less than fifteen percent sequence homology to known structures.

The stabilizing interactions from a beta-sheet's side-chains, generally pointing orthog-



Figure 3-1: The beta-helix and beta-trefoil folds

The beta-helix fold is characterized by a repeating pattern of parallel beta-strands in a triangular prism shape [112]. The cross-section, or rung, of a beta-helix consists of three beta-strands connected by variable-length turn regions (A); the backbone folds in a helical fashion with beta-strands from adjacent rungs stacking on top of each other (B) from 1plu [113]. The beta-trefoil fold consists of three leaves (C) around an axis of three-fold symmetry. Two beta-strands from each leaf form a 6-stranded anti-parallel barrel and two more from each leaf form a cap at one end of the barrel (D) from 1bff [54]. In all figures, the darkened regions correspond to the positions the templates.

onal to the strand axis, involve contacts with residues that are often very distant in the linear amino acid sequence. For beta-sandwich structures the packings between sheets show very little structural organization and considerable packing diversity [16, 17]. Higher order features such as the "ridges-into-grooves" that characterize alpha-helix-to-alpha-helix packings within proteins are absent. Beta-sheet proteins do preserve the general packing pattern of a buried core dominated by hydrophobic side-chains, and a mosaic surface that mixes polar with hydrophobic side-chains.

Our computational approach to this problem has been focused initially on two classes of beta-sheet proteins that have some topological regularity: beta-helices and beta-trefoils. The pectin lyase-like single-stranded right-handed beta-helix superfamily<sup>1</sup> is a coiled fold wherein each rung is composed primarily of beta-strands (Figure 3-1A and B). Beta-helices are elongated molecules in which the N-terminal and C-terminal are far apart, and form characteristic hydrophobic stacks between rungs [112]. The largest group of these folds with solved structures are involved with complex polysaccharide metabolism, either recog-

<sup>&</sup>lt;sup>1</sup>SCOP classification; henceforth referred to as the beta-helix fold.

nizing and binding to such molecules or involved in their synthesis or remodeling. Rather than having a crevice or pocket as an active site, the elongated lateral surface of the betahelix provides the recognition and catalytic elements [44]. A number of these proteins are virulence factors for bacterial and fungal pathogens, including pertactin from *Bordetella pertussis* and pectate lyase from *Erwinia chrysanthemi*. Because of the extended nature of the active sites, they cannot currently be recognized from examination of amino acid sequence alone. The ability to predict the fold from sequence alone would be of considerable value in medical microbiology. The beta-trefoil SCOP [73] fold<sup>2</sup> consists of three mainly-beta leaves folded around an axis of three-fold symmetry (Figure 3-1C and D). Their functions are diverse, including neurotoxins, inhibitors, and cytokines.

Both motifs have repeating structural segments: the rungs in the beta-helix and the leaves in the beta-trefoil. However, unlike coiled-coils, collagen, or leucine-rich repeats, they do not have a characteristic signature at the sequence level. Their intracellular folding process may have a progressive or sequential aspect, through which the sequence directs the native fold. We have been involved in developing algorithms that have a "wrapping" component, which may capture the processes that have an initiation stage followed by progressive interaction of the sequence with the already-formed motifs.

Fold recognition and sequence-structure alignment are difficult problems for both these protein folds, just as they are for many protein folds that lie in the "mainly-beta" top level of the SCOP hierarchy. The difficulty comes from the fact that there is insufficient sequence similarity to apply standard homology-based approaches. Both the beta-helix and the beta-trefoil folds lie in the so-called "twilight zone" of sequence homology [83], with sequence identity between members of the fold class lower than 15%. While there is evidence that residues involved in beta-sheet formation that are close in space exhibit strong statistical biases [75, 98], these residues may be difficult to discover due to being a variable and potentially long distance apart in the protein sequence. In fact, simply predicting the correct annotation of secondary structure of these folds can be problematic: even the best secondary structure predictors such as PHD [84] and PSIPRED [47] predict alpha-helices

<sup>&</sup>lt;sup>2</sup>Here, we consider the STI-like and cytokine SCOP superfamilies, for reasons explained in Section 3.4, and refer specifically to them with the term beta-trefoil.

more accurately than beta-strands [63]. Tertiary structure predictors such as Rosetta [11] and LINUS [95], while performing well on all-alpha and alpha/beta proteins, are also challenged by topologically complex all-beta proteins [11, 95].

Various researchers have found that considering interactions between pairs of residues can lead to improvements in beta-strand prediction. An information theoretic approach to the problem of determining the correct alignment between interacting beta-strands in parallel and anti-parallel beta-sheets [98] suggests that when it is possible to limit the search to a window of sequence around suspected interacting strands, consideration of inter-strand residue-residue pairings can be of significant value in determining the correct alignment between beta-strands. Similarly, Olmea et al. [84] note that exploiting information contained in the correlation between residue pairs seems to be a promising method for modeling the constraints that govern the folding process. Recognition tools for various folds have been built using pairwise interaction probabilities, including the coiled-coils [7, 31]. Previous studies [13, 21, 69] took a somewhat different approach, namely to search for secondary and supersecondary structure at the same time. These produced the BetaWrap program for recognizing the motif characteristic of the pectin lyase-like superfamily of the singlestranded right-handed beta-helix SCOP fold class, and Wrap-and-Pack, for recognizing the beta-trefoil motif. Other recent work [66] studied recognition of the beta-helix fold using Markov random fields. However, these programs are strictly fold recognizers. For example, BetaWrap predicts a structure to be in the template class if the average score of the top five alignments produced for overlapping sub-regions is good; it does not output a single global alignment of the putative structure to the motif.

Sequence profiles have previously been used for structure prediction in various ways. The profile encodes information about residue conservation (which locations are conserved, which are variable) and what types of substitutions are found at each location [36]. This additional information allows more distant homologies to be found by aligning profiles rather than sequences [114]. Strongly conserved residues are often of structural importance, as demonstrated by programs such as PSIPRED, which uses profiles for secondary structure prediction, and GenThreader [46], which uses this prediction as an input to its neural-network based threader. Sequence profiles have also been used to detect disulfide bonds

based in part on Cys-Cys conservation [19]. Panchenko et al. [78] present a method for threading a sequence onto a profile of a structural template and its homologs. In some sense our approach is the opposite, in that we wrap a sequence profile onto a structural template.

We introduce the program BetaWrapPro, which performs both fold recognition and sequence-structure alignment for the beta-helix and beta-trefoil motifs. The algorithm is based on the fold recognition algorithms of BetaWrap and Wrap-and-Pack, which use statistical correlations between pairs of residues in adjacent beta-strands to decide if a query sequence aligns well to the abstract structural template for a motif. We generalize this method to take advantage of the additional data provided by sequence profiles and by pairwise correlations of non-adjacent residues, and extend it to predict structure alignments for the conserved region of the motif.

To further support the utility of this method, we note that a list of the highest-scoring two hundred sequences with no known structure was provided with the first BetaWrap paper [13]. Since then, six have had their structure determined, and all were found to form the beta-helix fold (see Table 3.5).

# 3.2 The Algorithm

BetaWrapPro "wraps" a profile of a target sequence onto the abstract supersecondary structural template for a beta-helix (Figure 3-1A) or beta-trefoil (Figure 3-1C) derived from structural alignments with the dynamic programming algorithms of BetaWrap [13] and Wrap-and-Pack [69]. They were extended in this work to operate on sequence profiles, and the BetaWrap algorithm was also changed to include data on cater-corner residues. The concept behind the algorithm is that there is a statistically significant difference in residue pairing probabilities between aligned beta-strands and other structure [98]. This statistical signature can be used in conjunction with an abstract structural template to recognize supersecondary structure. The templates introduce constraints reflecting fold characteristics derived from structural alignments of known structures. The algorithms were extended to deal with sequence profiles rather than individual sequences, and BetaWrap was also modified to take into account diagonally adjacent residues, as described below.

A profile for a sequence n residues in length can be represented as a 20-by-n matrix that encodes some statistic of the amino acid composition for each position in the target sequence. This is based on the substitutions that occur in each position in a sequence alignment of the target to a number of other sequences<sup>3</sup>. Each row of the matrix corresponds to one of the 20 amino acids, and each column corresponds to a position in the target sequence. An entry in the matrix thus presents information concerning the chance of observing a specific amino acid in that position, based on a number of similar sequences. Logically, each residue pairing can be scored based on the distribution, rather than a particular amino acid. To create this matrix, PSI-BLAST is run on the non-redundant NCBI BLAST sequence database from July 18, 2005 for two iterations.

Wrapping mimics the progressive manner in which these folds may form: the structure is built around an initial structural segment, or seed. For beta-helices, the seed is a B2-T2-B3 rung section which matches a hydrophobic-residue sequence pattern common to the fold. The beta-trefoil search requires two phases, the first starting from two aligned beta-strands to build an individual leaf, and then to combine the leaves into a complete trefoil. In either case, the profile is searched forward and backward from the initial segment for neighboring segments based on a beta-strand alignment score. The score is primarily based on observed correlations between pairs of residues in adjacent beta-strands, and also incorporates information on turn lengths and observed residue stacking preferences. The correlations are derived from similar beta-sheets taken from the PDB, excluding the template fold class. The probability that a residue of type X will align with a residue of type Y is determined by the pairwise frequency of X and Y aligning over the frequency of X appearing, conditional on whether X is exposed or buried. Conditional probabilities are defined for stacking residues in adjacent beta-strands and for cater-corner residue pairs, i.e. those residues one off from a vertical alignment in either direction. Probabilities used for beta-trefoil scoring are given in Tables A.1 and A.2, and for the beta-trefoils in Tables A.4, A.3, and A.5.

The exact formula for computing the interaction probability between positions i and j

<sup>&</sup>lt;sup>3</sup>Columns involving a gap in the target are ignored.

in a sequence is given in Equation 3.1, where d varies over each of the twenty amino acids,  $Pr[r_i, d]$  is the log probability of the residue in position i interacting with d, and f(d, j) is the frequency with which residue d appears in position j of the profile. The weight w assigned to the interaction is based on the relative locations of i and j: for beta-helix scoring, inward-pointing adjacent residues have a weight of 1, outward of 0.5, and one-off of 0.25, which reflects that there are twice as many one-off residues as adjacent residues. All beta-trefoil adjacent residues are weighted 1, and one-off residues 0.5. There are several score adjustments reflecting fold-specific knowledge. The beta-helices receive a penalty of -1 for each standard deviation away from the mean number of residues between rungs, -1 for each large hydrophobic residue at positions that bound the beta-strands, and a +1 bonus for each pair of stacked aliphatic, aromatic, and polar residues. The trefoils are also penalized according to gap length, and given a +1 bonus for each residue predicted to be a beta-strand by PSIPRED.

$$Pr[i,j] = w \sum_{d=1}^{20} Pr[r_i,d]f(d,j)$$
(3.1)

The final beta-trefoil wrap is the one with the best score. The five-rung beta-helix wrap is taken as a consensus by combining pairs of adjacent rungs from each of the ten highest-scoring wraps and finding the four overlapping rung pairs which appear most frequently. This alignment of the target to a structural template can then be passed to standard packing [50] methods to determine putative atomic coordinates for the structurally conserved regions. In fact, BetaWrapPro uses SCWRL [90] to place side-chains onto several representative backbones, and the structure with the lowest SCWRL energy score is presented in PDB format. The energy score is a measure of how well the sequence fits the backbone template: a high energy score implies that many atoms are too close to one another, and thus the sequence is unlikely to form the target fold, either because it forms another fold or because it is poorly aligned to the structural template. Note that only a partial structure is output, for those regions that correspond to the template not including loops. This is similar to the outputs of other fold recognition programs such as PROSPECT [109].

# 3.3 Results

# 3.3.1 Recognition and Alignment of Sequences with Known Structures

On the positive and negative test databases described in Section 3.4, Materials and Methods, BetaWrapPro recognizes the beta-helix fold with 100% sensitivity at 99.7% specificity in cross-validation and with 100% sensitivity at 92.5% specificity in cross-validation for the beta-trefoils. This is an improvement over the results for BetaWrap (100.0% sensitivity, 95.0% specificity) and Wrap-and-Pack (88.9%, 96.3% resp. on the same databases). Given the improvement in specificity achieved by BetaWrapPro, over 300 false positives reported by BetaWrap as hits in the PDB-minus have been eliminated.

BetaWrapPro also produces accurate alignments of the target sequence onto the structural template. In sequence-heterogeneous motifs such as those BetaWrapPro predicts, this is difficult to accomplish by the common sequence similarity methods. However, the profile wrapping technique proves to be successful at predicting alignment to a supersecondary structure template across diverse sequence families. All results stated in this section are from the leave-family-out cross-validation described in Section 3.4. In particular, we are always packing onto a backbone from a different SCOP family.

On the twelve beta-helices in our database, the sequence-structure alignment is accurate for 88% of predicted residues. The beta-trefoil alignments are 89% accurate<sup>4</sup>. To verify that the additional information available in a sequence profile assists in wrapping, the original motif recognizers were modified to also produce a sequence-structure alignment. We find meaningful improvements: BetaWrap's beta-helix wraps are 67% accurate, and Wrap-and-Pack achieves 75% accuracy on the beta-trefoils.

Because of the quality of sequence-structure alignment, BetaWrapPro is able to use SCWRL to generate accurate 3-D structures of its template motifs. The accurately aligned regions of the beta-helix template average less than 2.0 Å RMSD (Table 3.1). The side-chain predictions placed onto the backbone by SCWRL are consistent with SCWRL's re-

<sup>&</sup>lt;sup>4</sup>We treat a residue as accurately aligned if it is within four position shifts of the exact position.

PDB	<i>p</i> -score	Alignment acc	RMSD (Å)	$\chi_1$ correct	$\chi_{1+2}$ correct	% identity	BLAST score
1air	0.0001	1.00	1.21	0.63	0.23	18	0.06
1bn8	0.0009	1.00	1.31	0.62	0.43	22	0.06
1ee6	0.0032	1.00	1.70	0.55	0.24	14	0.04
1jta	0.0001	1.00	1.45	0.71	0.32	12	0.02
1bhe	0.0001	0.80	0.97	0.67	0.34	19	0.03
1czf	0.0005	1.00	1.43	0.72	0.46	11	0.18
1rmg	0.0002	0.94	1.29	0.54	0.36	17	0.07
1dab	0.0001	1.00	1.39	0.60	0.41	18	1.0
1dbg	0.0001	1.00	2.83	0.66	0.45	14	0.02
1qjv	0.0012	0.66	2.13	0.45	0.29	11	0.82
1 idk	0.0014	1.00	1.47	0.55	0.35	16	2.8
1h80	0.0015	0.14	1.40	0.67	0.50	11	0.23
Average	0.0023	0.88	1.55	0.61	0.42	16	

Table 3.1: Beta-helix cross-validation

Cross-validation score and modeling accuracy for the beta-helix structures in the database as packed onto the minimum-energy template structure from outside its own SCOP family. Families are separated by a single line. The *p*-score is the BetaWrapPro score of the sequence. RMSD, dihedral angle correctness, and aligned sequence identity are calculated only on the accurately aligned residues of the structure. Aligned sequence identity is the identity between the target and template structure it was aligned to by BetaWrapPro; BLAST *E*-score is the expectation score bl2seq [101] gives to its best alignment between the entire target and template sequences.

PDB	<i>p</i> -score	Alignment acc	RMSD (Å)	$\chi_1$ correct	$\chi_{1+2}$ correct	% identity	BLAST score
1bff	0.111	1.00	3.79	0.52	0.39	10	0.011
1g82	0.041	1.00	6.23	0.56	0.50	7	2.6
2i1b	0.012	1.00	5.59	0.47	0.22	13	1.1
lirp	0.011	1.00	4.12	0.36	0.34	12	0.077
2ila	0.010	1.00	5.65	-	-	7	no hits
1wba	0.038	1.00	3.58	0.51	0.55	7	0.99
1tie	0.041	1.00	2.51	0.46	0.35	15	1.7
3bta	0.013	0.08	-	-	-	13	3.2
1a8d	0.009	none	-	-	-	5	0.23
average	0.038	0.89	4.50	0.48	0.39	10	-

Table 3.2: Beta-trefoil cross-validation

Cross-validation score and modeling accuracy for the beta-trefoil structures in the database as packed onto the minimum-energy template structures from outside its own SCOP family. Superfamilies are separated by double lines, families by single lines. For an explanation of each column, see Table 3.1. Note that the structure 2ila in the PDB does not include side-chain coordinates. We do not report structure prediction result for 3bta because only four residues are accurately aligned.



Figure 3-2: Side-chain packing example

The actual structure (in gray) superimposed on the predicted structure of pectate lyase C from *E. chyrsanthemi* (PDB id 1air). Green represents 0 Å RMSD and red 5 Å. The B1 section of the wrap is to the right.

ported performance on near-native backbones [10, 49, 41], with 61% of  $\chi_1$  and 42% of  $\chi_{1+2}$  angles correct<sup>5</sup>. Figure 3-2 shows a sample model superimposed on the solved structure. The aligned regions of the beta-trefoils average 4.5 Å RMSD (Table 3.2). Much of this deviation is due to the fact that some beta-strands are often seven residues long in the structure, whereas they are five long in the template. This leads to various off-by-two errors in the alignment, but with the advantage of predicting both those trefoils with five-residue and seven-residue strands. In addition, because the beta-trefoil predictions are made across both superfamilies and families, with at most only one structure available from within the same superfamily (rather than just family as in the beta-helices), there is greater structural deviation between the template backbones and the actual structure. The  $\chi_1$  angles are predicted correctly for 48% of residues, and  $\chi_{1+2}$  for 39%. The decrease in  $\chi$  accuracy compared to the beta-helices is to be expected, given the larger backbone deviation. Importantly, Tables 3.1 and 3.2 show that even when there is very low sequence identity between the target sequence and the structure used to model it, BetaWrapPro is able to predict an accurate structure for the aligned region.

### **3.3.2** Comparison to Other Methods

We compare BetaWrapPro to several popular methods for fold recognition and sequencestructure alignment. We expect BetaWrapPro will perform better because it is tailored to the beta-structural folds, and this indeed turns out to be the case. As reported previously [12, 69], neither PSI-BLAST nor HMMer succeed in recognizing these folds across families. PSI-BLAST failed to recognize beta-helices in a leave-family-out cross-validation (with the exceptions of the pectate lyase and pectin lyase families, and a couple examples across these families and the galacturonase family), and HMMER performed slightly worse. PSI-BLAST and HMMer perform even more poorly on the beta-trefoils. For alignment accuracy, we compared the output of PSI-BLAST, PROSPECT Version 2 [109] and RAPTOR [108]. In all cases, we recreated the leave-family-out testing method used throughout this work, excluding from the PSI-BLAST database or the PROSPECT and RAPTOR template libraries all proteins in the same SCOP family as the target sequence.

<sup>&</sup>lt;sup>5</sup>Dihedral angles are counted as correct if they are within 40° of the angle in the solved structure.

	Beta	WrapPro	PSI-	BLAST	PROSPECT		RAPTOR	
PDB	Exact	Within 4	Exact	Within 4	Exact	Within 4	Exact	Within 4
1air	0.88	1.00	0.76	0.95	0.78	0.90	0.87	0.95
1bn8	0.94	1.00	0.78	0.78	0.88	0.95	0.88	0.95
1ee6	1.00	1.00	none	none	0.29	0.32	0.35	0.43
1jta	0.94	1.00	0.74	0.75	0.74	0.80	0.87	0.81
1 idk	0.94	1.00	0.77	0.81	0.74	0.83	0.88	0.94
1bhe	0.80	0.80	none	none	none	0.08	0.50	0.58
1czf	1.00	1.00	none	none	0.24	0.34	0.54	0.58
1rmg	0.94	0.94	none	none	0.38	0.59	0.50	0.58
1dab	1.00	1.00	none	none	0.35	0.37	none	none
1dbg	0.94	1.00	none	none	0.22	0.37	0.59	0.67
1h80	none	0.14	none	none	0.20	0.43	none	0.25
1qjv	0.66	0.66	none	none	0.20	0.27	none	0.17
total	0.91	0.88	0.76	0.81	0.44	0.52	0.66	0.62

Table 3.3: Beta-helix alignment accuracy comparison

Percent of sequence-structure alignment correct for several programs on the beta-helices. "None" denotes that no residues were correctly aligned.

	Beta	WrapPro	PSI-	PSI-BLAST		PROSPECT		RAPTOR	
PDB	Exact	Within 4	Exact	Within 4	Exact	Within 4	Exact	Within 4	
1bfg	0.33	1.00	0.15	0.45	0.22	0.87	0.38	1.00	
1g82	0.17	1.00	none	none	0.35	0.57	none	none	
21bi	0.33	1.00	0.15	0.45	0.48	0.57	none	0.40	
1irp	0.33	1.00	none	none	none	none	0.75	1.00	
2ila	0.33	1.00	none	none	0.47	0.73	0.40	0.62	
1wba	0.50	1.00	none	none	0.08	0.42	none	1.00	
1tie	0.58	1.00	none	none	0.23	0.68	0.25	0.58	
3bta	none	0.08	none	none	none	none	none	none	
1a8d	none	none	none	none	none	0.03	none	none	
total	0.30	0.89	0.15	0.45	0.30	0.77	0.45	0.78	

Table 3.4: Beta-trefoil alignment accuracy comparison

Percent of sequence-structure alignment correct for several programs on the beta-trefoils. "None" denotes that no residues were correctly aligned.

PSI-BLAST was run on the PDB data set described in Section 3.4, Materials and Methods, filtered to 90 percent sequence identity. The default *E*-score cutoff for inclusion of 0.001 was used, and all searches converged within three rounds. PROSPECT was run using secondary structure prediction and evolutionary information from the same PDB90 used for PSI-BLAST, and *z*-scores were calculated with the -reliab option. RAPTOR was run with all default options.

As Tables 3.3 and 3.4 show, BetaWrapPro produces more accurate sequence-structure alignments to the template across the entire range of the folds than more general methods . BetaWrapPro finds an alignment with at least some residues correct for all but one tested sequence while the other tested programs often fail to align anything. In fact, on the beta-

helices, PSI-BLAST fails to produce any alignment at all on 67% of the tested structures. While PROSPECT and RAPTOR do find alignments for most of the beta-helices, their alignment quality is substantially worse than BetaWrapPro. PSI-BLAST fails to align 88% of the beta-trefoils, PROSPECT 22%, and RAPTOR 33%. We remark that the percentage of correctly aligned residues for the beta-trefoils are exactly comparable between all methods because they are each searching for a motif that is exactly 60 residues long. In the case of the beta-helices, BetaWrapPro alignments are for a 65-residue motif, while the alignments of other programs may be longer or shorter.

Finally, we mention that Liu et al. [66] have recently produced a fold recognizer tailored, like BetaWrapPro, specifically for the beta-helix fold, and achieve 100% sensitivity. They report 100% specificity on an unspecified version of PDB25 and have not made their program available, so it is not possible to perform a direct comparison to BetaWrapPro.

### 3.3.3 Recognition of Unknown Sequences

BetaWrapPro identifies a number of putative beta-helices in the SWISS-PROT data set (see Section 3.4, Materials and Methods). These include a number of bacterial autotransporters, including probable outer membrane proteins in *Chlamydia pneumoniae* (SWISS-PROT ID Q9Z813), *Chlamydia muridarum* (Q9PL47), and *Bordetella parapertusis* (P24328); AcfD from Vibrio cholerae (Q9KTQ4); adhesion and penetration protein precursor (P44596) and a putative surface exposed virulence protein from *Haemophilus influenzae* (P25927); and C5 epimerase from *Pseudomonas aeruginosa* (Q51371). We further note that while 44% of the sequences in SWISS-PROT are derived from mammals, mammalian sequences make up only 12% of the beta-helix sequences that BetaWrapPro identifies from the same database, supporting preliminary species distribution claims [12, 22].

BetaWrapPro also successfully identifies the newly-solved beta-helical protein Jun a 1 [22] (PDB ID 1pxz), an allergen from *Juniperus ashei*, with a *p*-score of 0.0001, and filamentous hemagglutinin [18] (1rwr) from *Bordetella pertussis* (*p*-score = 0.0014), despite a lack of significant sequence identity to previously solved beta-helix structures. These proteins were not included in the training set, as the structures were not available at the time.

Among putative beta-trefoils identified are the Kunitz-type proteinase inhibitor BbCI (P83051) from *Bauhinia bauhinioides*, agglutinin-like protein 3 (P46590) from *Candida albicans*, and protein B17 (P33878), a proposed virulence factor in the smallpox virus [89]. Complete lists of high-scoring sequences detected and their BetaWrapPro scores can be found at the same location as our web server.

# **3.4 Materials and Methods**

### **3.4.1** Sequence Databases

As our basic sequence database, we use the June 8, 2004 release of the NCBI non-redundant PDB data set, filtered to exclude sequences with more than 25% sequence identity. All positive and negative sequence databases for evaluating BetaWrapPro are derived from this database.

The beta-helix database is made up of sequences that are part of the pectin lyase-like superfamily of the single-stranded right-handed beta-helix SCOP fold. This superfamily is comprised of eight individual SCOP families, represented by 12 unique sequences in our database. Although the beta-helix fold class contains four additional SCOP superfamilies, these only contain one or two representative structures. For this reason, and because several of the structures (e.g. 1hf2 and 1k4z, by visual inspection and PDB coordinates) do not map directly onto the single-stranded right-handed beta-helix template that we consider in this study, these superfamilies were omitted from the main portion of this study.

In addition, it has been observed [21] that the leucine-rich repeat and single-stranded left-handed beta-helix folds are detected by BetaWrap, since they are also beta-helical-like folds, albeit not those of interest in this work. These were filtered out on the grounds that they conform to well-characterized repeat patterns and are easily detected (Pfam [6] families LRR and Hexapep, respectively). Since the last revision of SCOP, four beta-helices have been identified (PDB ids 1pxz, 1rwr, 10gm, 1ru4 in Table 3.5). As the new structures have not yet been classified into a SCOP superfamily, they were also excluded

PDB	Description	Species	BLAST hit	BetaWrap	BetaWrapPro
1pxz	Major pollen allergen	Juniperus ashei	$1 \text{pcl} (1 \times 10^{-20})$	0.00074	0.00046
1ru4	Pectate lyase 9A	Erwinia chrysanthemi	1dbg $(4 \times 10^{-4})$	0.0021	0.0047
logo	Dextranase	Penicillium minioluteum	1rmg (0.052)	0.0022	0.00015
1gq8	Pectin Methylesterase	Daucus carota	1qjv (2 × 10 <sup>-30</sup> )	0.0046	0.00015
1ee6	Pectate lyase	Bacillus sp.	1czf (0.005)	0.011	0.0032
1h80	iota-carageenase	Alteromonas sp.	1qjv (0.004)	0.021	0.0023
1rwr	Filamentous Hemagglutinin	Bordetella pertussis	1tsp (1.8)	0.041	0.0020

Table 3.5: New beta-helices

Beta-helix structures deposited in the PDB since the original BetaWrap appeared, and their P-values according to BetaWrap and BetaWrapPro. Also given is the protein from the original BetaWrap training set that is most similar (by BLAST [2] alignment), and the bl2seq [101] *E*-score of the best alignment of the two sequences.

from our beta-helix database, although BetaWrapPro does recognize them as beta-helices. In addition, we removed the beta-helix structure from the tailspike of bacteriophage P22 (PDB id 1tsp). Unlike all other known beta-helices, 1tsp is a trimer in its natural state, which gives it a significantly different surface exposure pattern than other helices. As such, although BetaWrapPro recognizes it as a beta-helix, we do not include it in this study. The PDB-minus set of non-beta-helical proteins is composed of the 6566 sequences in the PDB which are not described above. Of course, this PDB-minus includes the beta-trefoil sequences.

The beta-trefoil database is composed of members of the SCOP beta-trefoil fold that appear in our basic sequence database. Beta-trefoil structures from SCOP superfamilies other than the two we concern ourselves with (STI-like, cytokine) were also filtered out of the trefoil database. Although BetaWrapPro does recognize these sequences correctly, most of the structures contain multiple trefoils. Because of the limited number of hydrogenbonded residues between leaves, BetaWrapPro is has difficulty distinguishing accurately between leaves in adjacent trefoils. The PDB-minus of non-beta-trefoil sequences consists of the 6564 sequences which are not in the classes above, but naturally also contains the beta-helix sequences.

Potential new beta-helices and beta-trefoils were identified from the SWISS-PROT sequence database (Release 44.0 of 05 July, 2004), which was filtered to a 40% sequence identity non-redundant set of representatives, containing 48,269 sequences. Redundancy filtering was accomplished using the CD-HIT program [65].

### **3.4.2** Pairwise Residue Databases

Pairwise residue correlations for beta-trefoil prediction were taken from Menke et al. [69]. Beta-helix residue correlations were derived by the same method as in Berger et al. [7], from a beta structure database from the PDB-minus. STRIDE [32] was used to detect parallel and anti-parallel beta-sheets whose residue surface accessibility values alternated between values below 0.05 and above 0.15. 3211 protein chains contributed to the statistics.

### **3.4.3** Structure Databases

A database of template backbone structures was assembled from representative structures. For the beta-helices, a five-rung section corresponding to the rung template was extracted from a representative of each SCOP family. This also included a "buffer" residue on the open end of each strand (which is not included in the final structure), yielding a template backbone of 85 residues, reduced to 65 residues for output. The buffer was found to increase side-chain prediction accuracy, presumably by providing more of the physical restraints found in the true structure. The backbones were taken from PDB structures 1jta, 1k5c, 1qcx, 1gq8, 1dbg, 1dab, 1h80, and 1tsp. The beta-trefoil database was constructed with one representative structure from each SCOP family. The structures contain only the 60 residues in the beta-strands in the trefoil template, as there is often, but not always, only one residue between adjacent strands. The backbones come from structures 1ijt, 1n4k, 1abr, 1jly, 1wba and 1dfc.

### **3.4.4** Training and Testing

BetaWrapPro also uses BetaWrap as a quick filter for probable false positive results. Possible beta-helices with a BetaWrap alignment score of less than -25 (corresponding to a BetaWrap p-score of about 0.070) are discarded. This allows for faster execution by not requiring a PSI-BLAST search for every sequence.

Score thresholds were learned by training on the positive beta-helix and beta-trefoil databases against the corresponding negative database. In all cases, we performed leave-family-out training, both for learning the statistical profiles and for structure prediction,

i.e. never packing a sequence onto a backbone from its own SCOP family. From this, we derive a probability, the *p*-score, which is a measure of what percent of non-beta-helix or non-beta-trefoil proteins score above a particular pairwise structural alignment score.

Structure prediction accuracy was tested by a leave-family-out cross-validation on the known structures listed above. We ensured that each sequence was packed only onto structures from a different SCOP family. Fold recognition and alignment quality were tested on the sequence and structure databases described above.

### **3.4.5 Running Time**

The main limiting factor for BetaWrapPro execution speed is the PSI-BLAST search performed for each input sequence, which requires time proportional to the size of the search database and the length of the query sequence. This can be avoided in some cases (when searching for only the beta-helix fold) by using BetaWrap as a quick filter for probable false positive results. The second greatest performance limitation is side-chain packing, which may require anything from a few seconds to several minutes per backbone. In this experiment, about 40 hours of computer time were required to process the PDB used. This figure could be improved substantially by running PSI-BLAST searches and side-chain packing in parallel.

### 3.5 Discussion

Our results indicate that evolutionary information in the form of profiles generated by sequence alignments, when used in conjunction with statistics about pairwise residue-residue interactions occurring between adjacent beta-strands on an abstract structural template can allow accurate fold recognition and sequence-structure alignment for the beta-helix and beta-trefoil folds. Even when undetectable by straightforward sequence similarity searches across a SCOP superfamily or fold, selective pressure on residues that stabilize a fold ought to constrain evolutionary substitution at these locations and evidence of the amino acid substitutions compatible with the fold should be present within the profile. We take advantage of the fact that beta-strand interactions act as a stabilizing mechanism for the beta-helices and beta-trefoils by considering the potential mutations suggested by the target's profile when evaluating pairwise beta-strand alignments.

We thus obtain a novel recognition and alignment method devised specifically for diverse sequence mainly-beta structural supersecondary motifs, which allows 3-D modeling between a sequence and structure that have very low sequence similarity. The improved specificity of the BetaWrapPro method gives us greater confidence in the prediction of beta-helices and beta-trefoils. Moreover, our program's ability to produce 3-D structures of newly predicted beta-helices and beta-trefoils is useful in identifying novel structures, predicting functional residues, and designing mutational studies that could in turn lend support to the prediction.

We have found that sequences with a beta-helix p-score of less than 0.002 have a strong likelihood of forming the fold, and those with a p-score of less than 0.01 may. For the trefoils, sequences with a p-score of less than 0.05 are likely to form the fold.

### **3.5.1 Biological Implications**

The majority of the beta-helical protein structures deposited in the Protein Data Bank (PDB) are carbohydrate binding proteins involved in host cell recognition, infection, or penetration. One large beta-helix family is the pectate lyase family, required for virulence in soft rot plant disease. Initial sequence homology studies have suggested that these proteins are representatives of a large class of virulence factors not limited to plant disease: homologous sequences are found, for example, in *Yersinia pseudotuberculosis*. Right-handed beta-helix domains have also been found among the virulence factors and adhesins of microorganisms, including *Salmonella typhimurium* phage P22 [97], the plant pathogen *Aspergillus niger* [67], and the whooping cough pathogen *Bordetella pertussis* [30]. Thus the accurate prediction of beta-helices in microbial or viral sequences is likely to be a useful early warning method for identifying proteins playing a role in cell attachment and penetration.

In addition, beta-helices may be novel targets of anti-bacterial agents. It is known that beta-helices use the lateral surface of the helix to bind polysaccharides and related molecules. We suspect that this function is particularly important for bacteria and viruses that bind to cell surfaces. Insights into the details of the mechanism of glycolysis and the specific amino acid residues involved for both lyases and hydrolases are aided by crystal-lographic structures of these proteins complexed with their carbohydrate substrates. The active site is located in a groove on the elongated lateral surface in the B3-T3-B1 region of the domain [96]. This general use of an elongated surface rather than a crevice is quite different from the active site clefts in conventional enzymes and may underlie the selection for this elongated fold. By locating this region in an unsolved sequence, researchers can focus their efforts on a much smaller section of the protein. Since parallel beta-helices appear to be relatively rare in mammals and humans, such inhibitors may be very specific for their protein substrates. In addition, since they will be sugar analogues, solubility and transport problems should be relatively easy to overcome.

The prediction and subsequent confirmation of the beta-helical conformation of a pollen allergen is of particular interest. Given the role of beta-helices as microbial virulence factors and toxins, it is not surprising that the immune system mounts an efficient response to these proteins. It may be that where a plant pollen surface protein has evolved a beta-helical fold for dealing with polysaccharide metabolism, the immune system responds as if to a microbial pathogen.

The beta-trefoil SCOP superfamilies that BetaWrapPro was tested with include the interleukin-1 cytokines, promoters of mammalian immune system response, appetite regulation [80], and insulin secretion [20], among other functions. The same superfamily contains the fibroblast growth factors, important for cell growth and differentiation. The STI-like superfamily includes neurotoxins produced by both *Clostridium tetani* and *Clostridium botulinum*, and homologues of *Salmonella typhimurium*-derived T-cell inhibitor, which acts to subvert the host's immune response to invaders [4]. Rather than acting as enzymes like the beta-helices, the beta-trefoils interact with receptor proteins to induce specific behaviors in a cell.

As with the beta-helices, the ability to recognize and model the beta-trefoils has various uses for the scientific community, including working towards a better understanding of the structure-function relationship of new trefoils. This may be useful for structural studies, identifying new trefoils, and drug discovery and design.

# 3.5.2 Web Server

A BetaWrapPro server is available at http://betawrappro.csail.mit.edu.
### Chapter 4

# An Integrated Markov Random Field Method for Recognizing Beta-Structural Motifs

### 4.1 Introduction

One of the most successful and powerful methods for the prediction of protein structural motifs to date has been profile Hidden Markov Methods. There are several successful HMM packages that are widely used in structural motif recognition including HM-Mer [27, 94] and SAM [53]. However, HMMs have a fundamental limitation that they cannot capture long-range dependencies— a particular problem for beta-structural motifs, because hydrogen-bonded residues in beta-strands can be a long way, and a variable distance apart in sequence. In previous work, we therefore introduced several alternative methods to identify particular beta-structural motifs from sequence. BetaWrap [12, 21] recognizes right-handed pectate lyase-like parallel beta-helices; Wrap-and-Pack [69] recognizes betatrefoils, and BetaWrapPro (see Chapter 3), built on the previous two programs, presents an improved method to recognize both folds. All these methods were particular types of threaders that were specifically tailored to beta-structural motifs: they searched for residues that could be hydrogen-bonded pairs forming beta-sheets in a template. It was shown that they outperformed other motif-recognition methods such as PSI-BLAST [3], HMMs [27] and threaders such as Raptor [108] on these particular folds. While the beta-sheet signal these methods recovered proved to be a powerful statistical signal, our previous methods ignored information in other sequence positions, such as could be captured in an HMM. For folds where a strong one-dimensional sequence signal is also present (like some of the beta-propeller folds, discussed below), it is clear that this discards important information that could improve the quality of motif recognition.

In this chapter, we present the best of both worlds, i.e. a general method that is able to capture local sequence information as an HMM, but at the same time, discover residues that interact in beta-strands that participate in beta-sheet formation. We do both at once using a special set of Markov random fields (MRFs) [72], a generalization of HMMs that allows for arbitrary statistical dependencies. However, we restrict the type of MRF that we consider to those that calculate only pairwise dependencies between beta-strand pairs. When not too many pairs of adjacent beta-strands interleave in the one-dimensional sequence order, this results in a MRF whose optimal scoring function can be tractably computed using multi-dimensional dynamic programming.

The method we introduce, SMURF (Sequence Motifs Using Random Fields) is applicable to most parallel and anti-parallel beta-structural motifs. Here, we test it on three fold classes– namely, the six, seven and eight-stranded beta-propeller fold. The propeller fold classes make a good test case for our method, because several families have a strong sequence signature. We find that our method outperforms ordinary HMMs in cross-validation on the beta-propeller superfamilies on the NCBI non-redundant subset of the Protein Data Bank (PDB) [8].

**Previous work.** We note that the idea of using a random field for protein structural motif recognition did not originate with us; Liu et al. [66] proposed a conditional random field framework for incorporating long-distance features into Markov-type models. They built a CRF predictor for the right-handed parallel beta-helix motif, that performed somewhat better than our original BetaWrap algorithm (though not than its successor, BetaWrap-Pro [68]). However, Liu et al's approach used the same hand-generated template and many



Figure 4-1: A 7-bladed beta-propeller

of the hand-generated features of BetaWrap, and these features were all specific only to the beta-helix fold and no others. On the other hand, this paper presents a general, automated method that can be applied to *all* beta-structural motifs. For our new method, template construction is automatic from a protein multiple structure alignment and requires no human intervention.

**The beta-propeller folds.** The beta-propeller folds are noted for their extreme sequence, functional, and phylogenetic diversity [33, 79, 81]. They are found throughout the tree of life, and their functions range from signaling, to transport, to cell-cycle, to ligand binding, to involvement in mediating protein-protein interactions. One superfamily, the neuramindases, are particularly important to human health in that they are often virulence factors. Best known as a virulence factor in influenza (and several of the anti-virals used to treat influenza are neuramindase inhibitors), they are also virulence factors for many bacteria.

Beta-propellers are often observed as part of multi-domain proteins. Each propeller has between a four and eight-fold access of symmetry: the repeating motif is termed a *blade* of the propeller. In addition, some propellers have an open topology, and others are closed. Each blade is formed by a twisted four-stranded anti-parallel beta-sheet motif.



Figure 4-2: HMMER hidden Markov model

HMM generated by HMMER, with states for matching multiple domains removed. Square states output a residue, round states do not. The grayed out states are removed from the model, as no paths from Begin to End include them.

Some families of beta-propellers have characteristic sequence repeats; the best known of these is the Pfam family of WD40 repeats (also known as WD or beta-transducin repeats). Here the repeating units serve as a rigid scaffolding for protein interactions while coordinating multi-protein complex assemblies; the specificity of the proteins is determined by the sequences outside the repeats themselves. In this paper, we consider the six, seven and eight-bladed propeller folds. There are also a handful of four-bladed and five bladed propellers known; We do not examine the four-bladed propellers because there are insufficient solved structures in the PDB for a cross-validation experiment.

While HMM-based methods can identify WD40 repeats with high success rates, finding a model that will recognize other beta-propeller folds is a much more difficult problem.

### 4.2 Algorithm

The diagram in Figure 4-2 shows how a profile HMM is typically designed for protein motif recognition. In addition to begin and end states, there are match states corresponding to each sequence position, insertion states, and deletion states.

In our MRF, the main difference is that we do not allow insertions or deletions in positions corresponding to match states along a beta-strand: that is, once we match a residue in sequence with the first residue in a beta-strand, subsequent residues must match to the fol-



Figure 4-3: Anti-parallel beta-strand dependencies SMURF states for two hydrogen-bonded anti-parallel beta-strands, each four residues long, with two intervening match states. Pairwise dependencies indicated by dotted lines. Insertion and deletion states not shown. There would be 3 insertion and 2 deletion states between the beta-strands.

lowing beta-strand positions until the end of the beta-strand without insert or delete states. Note that to run SMURF, it is first necessary to parse the match states of the HMM to indicate which match states participate in beta-strands, and which tuples of beta-strand residues are to be paired. Below, we show how to generate such a parse automatically from a protein multiple-structure alignment.

The dependency diagram for SMURF for a pair of anti-parallel beta-strands appears in Figure 4.2. An edge between two states indicates that the probabilities for those states are dependent on one another. The way we approximate the scores of the MRF is to decompose our log-likelihood score into a linear combination of two components. The first component is an HMM component, and the second component is a beta-strand pair component. The HMM component is calculated as if the long-range dependency edges were not there; that is, it is just the score that the profile HMM would give for placing a residue in that match state. The beta-strand pair component is calculated using the pairwise probability frequency tables from our previous program BetaWrap. Rather than using conditional probabilities, SMURF uses the probability that the two residues are hydrogen bonded in a beta-sheet.

More formally, let the sequence have residues  $r_1, \ldots, r_n$ , and the MRF have match states  $m_1, \ldots, m_l$ , deletion states  $d_1, \ldots, d_l$ , and insertion states  $i_1, \ldots, i_{l-1}$ . And suppose that  $r_1 \ldots r_k$  and match states  $m_1 \ldots m_s$  have been assigned. Then, for the probability of assigning  $r_k$  to the next match state  $m_j = m_{s+1}$  we have three cases, depending on whether the current state is a deletion state, an insertion state, or a match state:

$$\begin{aligned} Pr[m_j \mid r_k, d_{j-1}] &= HMM[m_j, r_k] \times Transition[d_{j-1}, m_j] \times Betastrand[r_k, \overline{r}_k, m_j, \overline{m}_k] \\ Pr[m_j \mid r_k, i_{j-1}] &= HMM[m_j, r_k] \times Transition[i_{j-1}, m_j] \times Betastrand[r_k, \overline{r}_k, m_j, \overline{m}_k] \\ Pr[m_j \mid r_k, m_{j-1}] &= HMM[m_j, r_k] \times Transition[m_{j-1}, m_j] \times Betastrand[r_k, \overline{r}_k, m_j, \overline{m}_j] \end{aligned}$$

Here the beta-strand component is only calculated when the particular match state  $m_j$  participates in a beta-strand that is matched with a state  $\overline{m}_j$  earlier in the sequence template. In fact, this component is the main difference between our MRF and an ordinary HMM. The only other difference is that, recall that we have modified the typical profile HMM to not allow insertion states along beta-strands. So the transition probabilities above come directly from HMM training, except:

> $Transition[m_j \mid m_{j-1}] = 1$  if  $m_{j-1}, m_j$  in the same beta-strand  $Transition[m_j \mid d_{j-1}] = 1$  if  $m_j$  is in a beta-strand

We also can write down the probabilities of entering the jth deletion or insertion state; they are the same as for an ordinary HMM, except, again recall that we have modified the typical profile HMM not to allow deletion or insertion states along beta-strands (as noted below).

$$Pr[d_j \mid m_{j-1}] = Transition[d_j, m_{j-1}]$$
$$Pr[i_j \mid m_j] = Transition[i_j, m_j] \times HMM[i_j, r_k]$$

where  $Transition[d_j, m_{j-1}] = 0$  if  $m_j$  is in a beta-strand,  $Transition[i_j, m_{j-1}] = 0$  if  $m_{j-1}$  and  $m_j$  are both in the same beta-strand, and from the HMM transition probabilities

otherwise.

$$Pr[d_j \mid d_{j-1}] = Transition[d_j, d_{j-1}]$$

$$Pr[d_j \mid i_{j-1}] = 0$$

$$Pr[i_j \mid i_j] = Transition[i_j, i_j] \times HMM[i_j, r_j]$$

$$Pr[i_j \mid d_j] = 0$$

Finally, the probability of the begin state is calculated similar to the probability of assigning  $m_j$  to  $r_k$ , except the score is multiplied by a constant dependent on  $m_j$ . The probability of the end state is simply a constant dependent on  $m_j$ . Just like HMMER, we divide all probabilities by the probability of the "null model" when calculating the actual score. The null model is the probability of seeing the sequence by chance, based on the background residue frequency in proteins in general. Note that when actually calculating these scores, we instead calculate the logs, so that all products become summations.

### 4.3 Results

We tested our methods on the 6,7, and 8-bladed propeller folds classes, where we did a leave-superfamily-out cross validation on each fold. We compared the results of our method, SMURF, to the popular HMM program HMMer on the NCBI non-redundant PDB, with all beta-propellers removed. Both algorithms were trained on the same Matt alignments. The results appear in Table 4.1.

We also ran SMURF on a large database of sequences of unsolved structures, namely, version 14.9 of UniRef50 [100], which is filtered to 50% sequence identity. Table 4.2 gives a sample of interesting sequences that SMURF predicts to contain seven-bladed propeller domains, but both Blast and HMMER would have missed these sequences (for the purposes of our table, a sequence is said to be missed by Hmmer if the Hmmer E-value is greater than 0.1.) Note that these are mostly long proteins, and the propeller structure is only one of multiple domains contained in each protein. We calculated p-values by assuming the scores form a Gaussian distribution, and using the scores corresponding to observed p-values of

	6-bla	ıded	7-bla	uded	8-bladed			
% True Negatives	HMMER	SMURF	HMMER	SMURF	HMMER	SMURF		
97	52	68	80	83	0	40		
96	52	72	80	87	20	40		
95	60	80	87	93	20	40		
94	64	88	90	97	40	40		
93	68	92	90	97	40	40		
92	68	92	90	100	40	80		
91	72	92	90	100	40	100		
90	72	92	93	100	40	100		

Table 4.1: Our results versus HMMer 3.0

The numbers represent the percent of true positives correct for a given threshold of percent of true negatives on a leave-superfamily-out cross-validation. The non-redundant structure database used to generate the true negative rate had all beta-propellers removed. Structures with fewer than 150 residues were also removed from the test set, as they are too short to fold into beta-propellers with six or more blades. Both algorithms give such sequences low scores due to their length, resulting in inflated numbers. SMURF's results are in bold.

Protein name	ID	Tax.	Residues	<i>p</i> -value
VCBS	Q3AQB0	Chlorobium chlorochromatii CaD3	320-643	$1.88 \times 10^{-5}$
Cell surface protein	Q8TJS8	Methanosarcina acetivorans	649-949	$1.77 \times 10^{-5}$
LVIVD repeat protein	B8FMG9	Desulfatibacillum alkenivorans	265-551	$2.67 \times 10^{-5}$
Adhesin-like protein	A5UMT3	Methanobrevibacter smithii	492-776	$3.56 \times 10^{-5}$
Like Esoderm induction early response 2	UPI0001662B14	Homo sapiens	355-608	$5.17 \times 10^{-5}$
Cell wall surface anchor family protein	Q6MN16	Bdellovibrio bacteriovorus	1672-2000	$1.44 \times 10^{-4}$
WiSP family protein	Q83NF7	Tropheryma whipplei	1180-1482	$1.46 \times 10^{-4}$
CHU large protein	A8UMR3	Flavobacteriales bacterium ALC-1	70-341	$4.96 \times 10^{-4}$
Beige/BEACH domain containing protein	A2DVS7	Trichomonas vaginalis	2110-2369	$7.86 \times 10^{-4}$
Flagellar hook-associated 2-like protein	A3DHJ1	Clostridium thermocellum	206-523	$2.86 \times 10^{-3}$

Table 4.2: Selected SMURF predictions

Some proteins predicted by SMURF to contain 7-bladed propeller domains. The residues denotes the location in the protein sequence of the best SMURF match to the structural motif.

0.2 and 0.1 to calculate the Gaussian distribution.

### 4.4 Methods

**Template Construction.** For each of the known 3-D structures from the fold class in the training set, it is marked which residue positions participate in a beta-strand (using the Ras-Mol algorithm to decide if a position participates in a beta-strand, see [85]). Each residue in a beta-strand also determines which residues in which other beta-strand it is paired with using the same program. The training structures are then aligned using the Matt multiple

Before:			
Seq1 Seq2 Seq3 Seq4 Seq5	VVDGD-A VVDGDK- LD-GDLI VI-GDL- VI-GDL- 1	LLVGFSEGSVN-YLYDG-GET-KLR- -LLV-GFSEGSLQ-SMYDS-GETVKLR- AFVSRGQAFIQDSVGTYVLK -IAFVSRGYDSVGTYVLKV- IAF-SAGYIQDSVGTY-LKV- 2345 5432	ING ING U L 1
After: Seq1 Seq2 Seq3 Seq4 Seq5	VVDGD- VVDGDK LD-GDL VI-GDL VI-GDL	LVGFSEGSVN-YLYDG-GET-KLR LLV-GFSEGSLQ-SMYDS-GETVKLR FVSRGQAFIQDSVGTYVL IAFVSRGYDSVGTYVLKV IAF-SAGYIODSVGTY-LKV	ING ING L L L
10	1	234 432	1

Figure 4-4: Template construction

Example of the template construction phase modifying a pair of hydrogen-bonded anti-parallel beta-strands in Matt alignment containing five structures. The positions labeled with the same number are hydrogen-bonded to each other, in all sequences with a residue in corresponding numbered positions. Intervening residues are removed from the four-residue consensus beta-strand pair. Fewer than half the structures have a residue in position five in the first strand, so both position fives are removed from the beta-strand. Residues outside all consensus beta-strand pairs are never removed.

structure alignment program (see Chapter 2), and we call a position in the alignment betaconserved if more than half the structures in the alignment mark that position as participating in a beta-sheet. A pair of positions in the alignment is a beta-conserved pair if more than half the structures in the alignment mark both positions as being hydrogen bonded with each other in the beta-sheet. Two beta-conserved pairs AB and CD are said to be adjacent if in more than half the structures of the alignment, A is adjacent to C and B is adjacent to D, and AB and CD are hydrogen-bonded to each other in the same beta-sheet. Template beta-conserved strands consist of the maximal contiguous sets of adjacent beta-conserved strand pairs, together with the information of which residue positions are hydrogen bonded. Note that since these template positions may only be occupied by positions that are identified as beta-strands in a majority of the structures, there could be residues in other structures between these positions in the Matt alignment, creating gap positions in the structural alignment in the middle of the template beta-conserved strands. This is undesirable, so we will remove these positions; this includes possibly deleting residues from sequences when we remove the corresponding position from the template structural alignment. In the resulting alignment, the beta-conserved template strands are always contiguous.

The output of this phase is a sequence alignment derived from the Matt structural alignment with annotated beta-strand residue positions and the residue positions to which they are paired. See Figure 4-4 for an example the template construction phase on an alignment. This multiple sequence alignment, together with the locations of the template beta-strands is the input to the next training phase.

Model Training Phase. The training phase trains both an HMM on the multiple sequence alignment, and also, pairwise probabilities on the paired residue positions in the template beta-strands. The HMM portion of the training is exactly the default HMM training from HMMer version 3, except that every template beta-strand position is always included in the output model. For the pairwise probabilities in the template beta-strands, the "in" and "out" pairwise probability tables from the program BetaWrap are considered [12]. it is determined for each residue position, whether the sum of the pairwise probabilities of seeing the pairs in the training alignment, summed over all structures in the alignment, was more probable from the "buried" or the "exposed" probability table. The position is then labeled buried or exposed accordingly. Note that, while the names buried and exposed come from the solvent accessibility of residue positions in the original BetaWrap algorithm, no claim about solvent accessibility or consistency of solvent accessibility is made in our context. In our case, in a structurally oblivious way, we are simply determining based on the training data which of the two models best predicts the set of residue pairs we see. The output is an HMM where certain states are marked as beta-strand states, and, pairings of hydrogen-bonded beta-strand states are also given. Since the score includes a component from these pairs, and not just the linear score of the HMM component, it is no longer a simple HMM, but rather a MRF, because of the non-linear dependencies between the paired states in constructing the score.

**Score.** For a given test sequence, we seek the parse of the sequence to the states of the training HMM that optimizes the particular score. The score we seek to optimize, over all ways to map the sequence to the states of the MRF model is

 $\alpha \times \log$  (HMM score) +  $\beta \times \log$  (pairwise score)

where the HMM score represents the conditional probability of seeing the sequence given the HMM portion of the model. Experimentally, using a value of one for both  $\alpha$  and  $\beta$ provided the best results on cross-validation (see Table 4.1). The details of how a particular parse of sequence to the states of the MRF is scored has already been given above, in the section on the algorithm. The score of the sequence is then the maximum score obtained over all possible ways to parse the sequence onto the states of the MRF. We next explain how to compute this maximum score.

Computing the Score. The maximum score of a sequence is computed by multidimensional dynamic programming. The dynamic programming takes place on the MRF described above- it has the same beginning states, ending states, match states, insertion states and deletion states as does HMMer HMMs, except some of the states are special beta-strand states. Recall that the beta-strand states consist of sets of contiguous states with no insertion or deletion states allowed between them (the beta-strands), and furthermore, beta-strands are paired with other beta-strands. In particular, the pairwise probabilities for paired beta-strands can only be calculated for the second paired beta-strand, once it has been fixed what residue will be occupying the first position of the pair. Thus, each time we reach a state in the HMM that corresponds to the first residue of the first beta-strand in a set of paired beta-strands, we need to keep track of multiple cases, depending on what sequence position is mapped to that state in the dynamic program. We keep track of this using a multi-dimensional array. For arbitrary gap lengths, this quickly becomes computationally infeasible, so a maximum gap length is defined (and for our purposes is set to the longest gap seen in the training alignment plus 20). When paired beta-strands follow each other in sequence with no interleaving beta-strands between them (which is usually the case for the beta-propellers) the number of dimensions in the table for the portion of the dynamic program that parses the parts of the HMM between the two beta-strands is directly proportional to the maximum gap length.

We now introduce some notation that will help describe the algorithm and analyze its complexity for interleaving pairs of beta-strands. When we look, in order of sequence, at the states in the template MRF, mark the first of a pair of beta-strands with consecutive numbers 1,2,3, and so on, and mark its corresponding paired beta-strand with the same

number. Thus if we have *n* pairs of beta-strands, we get a sequence that contains precisely two occurrences of each of the numbers from 1 to *n*. Now replace the first occurrence of each number with a left parenthesis and the second occurrence with a right parenthesis. Starting with the number 0, walk along the sequence, adding one for every left parenthesis, and subtracting one for every right parenthesis. The maximum size of this total at any intermediate point we call the *interleaving number* of this sequence. We call the last MRF state for the first of each pair of beta-strands the "split" state, and the first MRF state for the second of that pair of beta-strands the "join" state.

At every split state, the number of dimensions of the dynamic program will be multiplied by the maximum gap length, since the dynamic program has to keep track of scores for each possible sequence position (up to maximum gap length) that could be mapped to that state. At the corresponding join state, the number of dimensions will be reduced by the maximum gap length, since the scoring function can calculate all the pairwise probabilities (and hence the score) of placing that residue into the join state, and then simply take the maximum of all ways to have placed its paired residue into the split state. Thus the number of elements in the multi-dimensional table is never more than sequence length times the maximum gap length raised to the interleaving number power. As noted above, when there are few or no interleaving beta-strand pairs, as is the case with the strand topology of the beta-propellers, this is very computationally feasible. On the other hand, the algorithm may become computationally infeasible for structures with many interleaving beta-strands, such as the parallel beta-helix structures.

#### 4.5 Discussion

A major challenge in protein threading has been to find a tractable way to integrate local sequence information with higher-order structural dependencies in an integrated, computationally tractable, energy function. We have presented a framework, SMURF (Structural Motifs Using Random Fields), that integrates long-distance pairwise correlations involving beta-sheet formation with an HMM using a random field, and tested it on three fold classes, namely the five, six, and seven-bladed propellers. There is nothing in the method, however,

that restricts it to propellers. The method can be applied to any beta-structural motif where there is enough training data, and the number of interleaved pairs of beta-strands is not too great. We will be applying SMURF to additional classes of beta-structural motifs in the future.

### Chapter 5

### Conclusions

#### 5.1 Discussion and Future Work

We have introduced the program Matt and demonstrated that its use of local flexibility yields high-quality multiple structure alignments even when proteins are more distantly homologous. We have introduced the program BetaWrapPro which combines long-distance pairwise correlations involved in beta-sheet formation with sequence profiles and a backbone dependent rotamer library to successfully recognize beta-helices and beta-trefoils from hand-constructed templates of solved structures. Finally, we introduced the program SMURF which can combines automatic template construction using Matt, pairwise beta-sheet probabilities in a manner similar to BetaWrapPro, and profile hidden Markov models into a general method for recognize beta-structural motifs. We now discuss what is yet to be done and future directions.

As a stand alone structure alignment program, Matt is probably the current state of the art for aligning proteins that are distant homologs. However, it may still be possible to improve Matt. For example, Matt currently only uses alpha-carbon coordinates in its alignments. Adding sequence information to its scoring function may well improve alignment accuracy as well as allow it to handle cases where some residues lack alpha-carbon coordinates in the input structures, as is often the case in PDB files. Adding the option to weight structures by either their sequence or structure similarity would reduce the problem of bias when some of the input structures are significantly more similar to each other than others.

Based on X-ray scattering results [56], beta-helices are a possible structure for many prions and amyloids. We are are actively working to apply the methods developed for BetaWrapPro to combine sequence information with CD spectral, X-ray scattering, and electron microscopy data to model and investigate the observed properties of prion tendrils.

However, most of our future research is going to be focused on SMURF. SMURF has yet to be trained and tested on any folds other than the beta-propellers. Running on a broader set of structures will undoubtedly highlight any weaknesses in the current algorithm, and provide more information on what types of beta structures it works well on, and for which structures its memory requirements are prohibitively high. Incorporating profiles of input sequences and adding a side-chain packing algorithm as a post process may increase the accuracy of SMURF as they did with BetaWrapPro. Adding support for multiple hits in a single sequence and improving handling of very long sequences, both of which HMMER already supports, could improve SMURF's results with a minimal impact on runtime and memory usage. Support for other long range dependencies, such as disulfide bonds, could also be added to SMURF. It's also possible to decrease its memory usage significantly. An implementation capable of disk caching or using 64-bit addressing would also make memory usage less of an issue.

Protein structural motif recognition is an easy problem for proteins that are close homologs to proteins of solved structure. For distant homologs, it remains an incredibly challenging problem. Hopefully this thesis has significantly extended the class of protein structures for which we can solve this problem, particularly in the case of beta-structural motifs.

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## Appendix A

**Pairwise Tables** 

Residue	Α	С	D	Е	F	G	Н	I	K	L	М	N	Р	Q	R	S	Т	V	W	Y
Α	5.8	5.5	8.9	19.5	7.5	3.6	12.6	7.8	5.5	8.8	5.4	10.0	6.9	4.6	2.9	6.7	8.4	7.8	7.9	7.4
С	2.2	11.1	3.5	2.4	2.8	4.3	3.1	2.5	5.5	2.8	1.4	3.3	13.9	2.3	2.9	4.3	4.2	2.2	6.1	3.0
D	1.0	1.0	0.8	0.8	0.6	2.1	1.5	0.8	0.8	0.3	0.9	5.0	4.6	0.8	5.8	3.0	0.6	0.8	0.8	0.3
Е	1.6	0.5	0.6	4.8	0.9	0.3	3.1	0.6	11.1	0.4	1.4	0.6	0.6	0.6	0.6	1.2	0.6	0.1	0.6	0.6
F	9.9	9.0	7.1	14.6	11.9	13.8	11.1	8.4	11.1	9.1	11.8	5.0	11.6	13.9	8.8	14.1	11.4	9.0	8.8	11.1
G	2.0	6.0	10.7	2.4	5.9	6.5	7.9	3.6	4.3	3.6	2.9	1.6	13.9	2.3	2.9	3.0	6.0	4.4	2.6	5.2
Н	1.6	1.0	1.7	4.8	1.1	1.8	6.3	0.6	0.9	0.6	0.9	1.6	0.9	2.3	0.9	3.7	1.2	0.2	0.8	0.9
I	17.6	14.1	16.0	17.0	14.3	14.1	11.1	20.5	16.6	17.8	18.8	11.6	9.3	13.9	5.8	15.4	8.4	17.7	15.9	15.7
K	0.2	0.5	0.2	4.8	0.3	0.2	0.2	0.2	0.2	0.4	0.2	0.2	0.2	2.3	2.9	0.6	0.2	0.2	0.2	0.2
L	18.9	14.6	7.1	12.1	14.7	13.8	11.1	17.0	27.7	18.0	16.8	13.3	9.3	11.6	5.8	13.5	15.0	16.0	13.2	16.6
M	2.2	1.5	3.5	7.3	3.7	2.1	3.1	3.5	3.1	3.3	5.9	1.6	2.3	9.3	2.9	0.6	4.2	2.9	2.6	3.3
N	1.2	1.0	5.3	0.9	0.4	0.3	1.5	0.6	0.9	0.7	0.4	0.9	2.3	4.6	2.9	1.2	3.6	0.7	4.4	0.3
Р	0.6	3.0	3.5	0.6	0.7	2.1	0.6	0.3	0.6	0.3	0.4	1.6	0.6	2.3	0.6	1.2	0.6	0.2	3.5	0.6
Q	0.4	0.5	0.6	0.6	0.9	0.3	1.5	0.5	5.5	0.4	1.9	3.3	2.3	0.6	2.9	1.8	0.6	0.6	1.7	0.3
R	0.2	0.5	3.5	0.5	0.4	0.3	0.5	0.1	5.5	0.1	0.4	1.6	0.5	2.3	0.5	0.6	2.4	0.6	1.7	1.5
S	2.2	3.5	8.9	4.8	3.6	1.8	9.5	2.3	5.5	2.1	0.4	3.3	4.6	6.9	2.9	8.6	0.6	1.6	4.4	2.1
Т	2.9	3.5	1.7	2.4	2.9	3.6	3.1	1.2	2.5	2.4	3.4	10.0	2.3	2.3	11.7	0.6	2.4	3.0	1.7	3.3
v	22.2	15.1	21.4	4.8	19.3	22.1	6.3	22.2	16.6	21.1	19.8	16.6	6.9	20.9	26.4	13.5	25.3	25.4	12.3	19.7
W	1.8	3.5	1.7	1.7	1.5	1.0	1.5	1.6	1.7	1.4	1.4	8.3	9.3	4.6	5.8	3.0	1.2	1.0	3.5	2.7
Y	4.9	5.0	1.7	4.8	5.6	6.1	4.7	4.7	5.0	5.2	5.4	1.6	4.6	2.3	14.7	4.3	6.6	4.7	7.9	4.9

#### Table A.1: Solvent inaccessible beta residue conditional probabilities

Pairwise conditional probability tables of solvent inaccessible residue pairs used by BetaWrapPro to detect beta-helices. The value in row i, column j is the probability of residue i appearing in a beta-strand given that it is aligned with residue j. They were calculated from a hand annotated set of amphipathic parallel and anti-parallel beta-sheets from a subset of the PDB containing no beta-helices.

Residue	A	С	D	E	F	G	Н	I	K	L	М	N	P	Q	R	S	Т	V	W	Y
А	5.4	7.6	4.0	2.9	5.0	4.0	4.7	5.0	2.8	5.5	4.4	3.6	3.1	2.0	4.1	3.4	2.7	5.4	2.1	5.9
C	2.3	10.2	0.4	0.2	2.5	0.5	0.9	0.8	0.9	1.2	0.8	1.0	1.5	0.3	1.6	1.4	1.2	1.0	2.1	1.8
D	3.8	1.2	2.4	2.1	2.5	4.0	5.2	3.5	6.7	3.2	3.5	3.6	1.5	4.8	6.4	5.3	3.7	2.1	4.3	2.7
E	5.4	1.2	4.0	5.1	7.6	4.0	5.6	5.7	15.8	6.4	10.6	9.3	7.9	7.3	13.0	5.1	8.0	6.0	7.6	4.6
F	4.6	7.6	2.4	3.8	6.7	7.6	7.1	2.4	2.6	4.0	7.0	2.5	3.1	2.7	1.1	5.3	3.6	2.9	4.3	3.7
G	2.7	1.2	2.8	1.4	5.5	3.5	4.2	3.0	0.7	4.0	6.1	4.1	1.5	1.7	2.9	2.9	1.8	2.0	3.2	3.7
н	3.8	2.5	4.5	2.5	6.3	5.2	2.8	2.8	3.0	3.0	4.4	2.0	4.7	2.7	2.2	3.4	3.3	3.4	2.1	4.9
I	8.9	5.1	6.5	5.5	4.6	8.1	6.1	13.1	6.9	9.4	9.7	5.1	6.3	6.6	6.8	7.0	5.4	7.6	7.6	5.9
K	5.8	6.4	14.7	17.9	5.9	2.3	7.5	8.1	8.6	7.7	10.6	8.8	3.1	9.4	5.9	5.3	7.2	6.5	9.8	11.8
L	10.0	7.6	6.1	6.4	8.0	11.1	6.6	9.6	6.7	10.3	5.3	3.1	14.2	6.2	5.2	6.5	4.8	10.9	7.6	6.5
M	1.9	1.2	1.6	2.5	3.3	4.0	2.3	2.4	2.2	1.2	3.5	1.5	1.5	1.3	2.0	1.4	1.0	1.4	1.0	0.6
N	2.7	2.5	2.8	3.8	2.1	4.6	1.8	2.1	3.2	1.2	2.6	3.1	3.1	4.5	4.5	3.1	3.7	1.8	4.3	4.0
Р	0.7	1.2	0.4	1.0	0.8	0.5	1.4	0.8	0.3	1.9	0.8	1.0	1.0	0.6	1.1	0.4	0.7	1.2	2.1	2.4
Q	2.3	1.2	5.7	4.4	3.3	2.9	3.7	4.1	5.0	3.8	3.5	6.7	3.1	8.3	3.4	3.9	5.9	4.5	6.5	4.6
R	6.9	8.9	11.4	12.2	2.1	7.6	4.7	6.5	4.9	4.9	7.9	10.3	7.9	5.2	2.7	6.8	8.4	8.2	10.9	5.9
S	5.4	7.6	9.0	4.4	9.3	7.0	6.6	6.3	4.1	5.7	5.3	6.7	3.1	5.5	6.4	8.7	10.3	4.5	5.4	6.8
Т	6.9	10.2	10.2	11.3	10.1	7.0	10.4	7.9	9.0	6.8	6.1	12.9	7.9	13.6	12.8	16.5	15.7	11.3	2.1	4.3
v	11.6	7.6	4.9	7.0	6.7	6.4	9.0	9.2	6.7	12.8	7.0	5.1	11.1	8.7	10.3	6.0	9.3	11.3	9.8	9.3
W	0.7	2.5	1.6	1.4	1.6	1.7	0.9	1.5	1.6	1.5	0.8	2.0	3.1	2.0	2.2	1.2	0.3	1.6	2.1	1.2
Y	7.3	7.6	3.6	3.2	5.0	7.0	7.5	4.1	7.1	4.5	1.7	6.7	12.6	5.2	4.3	5.3	2.1	5.4	4.3	8.6

Table A.2: Solvent accessible beta residue conditional probabilities

Pairwise conditional probability tables of solvent accessible residue pairs used by BetaWrapPro to detect beta-helices. The value in row i, column j is the probability of residue i appearing in a beta-strand given that it is aligned with residue j. They were calculated from a hand annotated set of amphipathic parallel and anti-parallel beta-sheets from a subset of the PDB containing no beta-helices.

Residue	A	С	D	Е	F	G	Н	I	K	L	М	N	Р	Q	R	S	Т	V	W	Y
Α	5.8	4.3	10.0	8.3	5.8	5.2	5.4	6.7	5.9	8.0	7.4	5.9	6.1	6.4	5.4	5.5	7.9	8.6	4.9	4.4
С	2.4	18.4	2.9	3.3	2.8	4.7	4.7	2.5	3.3	2.5	2.3	7.1	4.6	3.7	3.7	3.3	2.7	2.4	15.6	3.9
D	3.2	1.7	3.3	2.2	1.4	1.3	4.7	1.9	3.2	1.1	2.0	5.3	1.8	1.6	3.7	2.7	2.7	2.6	2.4	1.1
Е	3.2	2.3	2.7	2.1	2.3	1.3	2.9	2.0	4.0	2.1	2.5	5.0	2.5	4.4	5.9	3.3	4.0	2.0	3.8	2.8
F	6.2	5.4	4.8	6.4	9.3	9.5	5.8	8.9	5.3	6.4	10.1	3.4	6.1	6.0	7.4	6.0	5.3	7.7	8.2	8.4
G	3.2	5.3	2.5	2.1	5.5	6.5	4.7	4.2	1.7	4.0	3.2	4.3	6.4	3.3	2.2	4.8	4.0	4.8	4.5	4.2
н	1.0	1.6	2.7	1.4	1.0	1.4	2.2	1.0	1.0	1.1	1.8	1.5	2.1	1.5	1.9	1.3	2.1	0.8	0.4	1.8
I.	12.1	8.1	10.4	9.5	15.0	12.3	9.8	17.4	11.5	14.2	7.9	5.9	6.4	13.0	9.5	9.2	9.2	12.2	10.7	10.3
K	2.7	2.7	4.6	4.8	2.3	1.3	2.5	3.0	2.9	1.9	3.1	3.1	1.1	4.8	2.2	4.5	4.3	3.4	5.3	6.2
L	15.1	8.4	6.5	10.0	11.2	12.1	10.9	14.8	7.5	17.0	12.7	10.8	11.1	12.3	9.8	10.9	9.9	14.7	9.1	9.7
Μ	2.7	1.6	2.3	2.4	3.5	1.9	3.6	1.6	2.4	2.5	6.1	3.7	5.7	1.5	4.0	1.9	3.5	2.1	1.6	2.4
N	1.3	2.7	3.5	2.8	0.7	1.5	1.8	0.7	1.4	1.3	2.2	4.3	1.8	2.6	2.1	1.6	2.9	0.8	1.1	1.5
Р	1.1	1.6	1.0	1.2	1.1	1.9	2.2	0.7	0.4	1.1	2.9	1.5	2.9	0.7	0.8	1.3	1.4	1.0	3.8	2.2
Q	2.3	2.4	1.9	4.1	2.1	1.9	2.9	2.6	3.7	2.4	1.4	4.3	1.4	1.5	2.4	3.0	1.6	2.1	1.1	5.1
R	2.3	2.7	4.8	6.4	2.9	1.5	4.3	2.2	2.0	2.2	4.5	4.0	1.8	2.7	2.6	2.5	4.2	2.2	3.3	5.5
S	2.5	2.6	3.8	3.8	2.5	3.4	3.3	2.3	4.3	2.6	2.3	3.4	3.2	3.7	2.7	6.3	4.4	3.1	3.3	3.0
Т	5.2	3.2	5.6	6.9	3.3	4.3	7.6	3.4	6.2	3.5	6.3	9.0	5.0	2.9	6.7	6.5	6.8	3.8	1.6	6.0
V	22.4	11.1	21.5	13.4	18.7	20.2	11.6	17.7	18.9	20.5	14.7	9.9	13.9	15.2	13.8	17.7	14.8	19.8	10.2	15.1
W	1.5	8.4	2.3	2.9	2.3	2.2	0.7	1.8	3.4	1.5	1.3	1.5	6.1	0.9	2.4	2.2	0.7	1.2	2.2	2.4
Y	3.5	5.6	2.7	5.9	6.3	5.5	8.0	4.6	10.8	4.2	5.2	5.6	9.6	11.2	10.6	5.4	7.3	4.7	6.5	3.7

Table A.3: Solvent inaccessible twisted beta-strand residue conditional probabilities

Pairwise conditional probability tables of solvent inaccessible residue pairs used by BetaWrapPro to detect beta-trefoils. The value in row i, column j is the probability of residue i appearing in a beta-strand given that it is aligned with residue j. They were calculated using an automated search for twisted amphipathic strands in a non-redundant structure database with the beta-trefoils removed.

Residue	A	С	D	Е	F	G	Н	I	K	L	М	N	Р	Q	R	S	Т	v	W	Y
A	4.8	4.9	4.9	2.8	5.5	7.2	7.2	4.7	4.0	5.7	3.0	4.2	3.9	5.7	3.1	3.3	2.8	5.1	4.0	4.5
C	2.1	16.5	2.5	1.0	1.9	2.5	0.9	2.6	0.9	1.7	3.0	0.7	1.1	1.3	1.5	1.2	1.1	2.0	1.5	2.0
D	4.0	4.6	3.9	2.7	2.7	4.1	4.5	2.7	6.1	2.1	3.0	4.2	3.7	4.1	6.0	4.2	4.6	2.3	2.5	2.1
E	3.9	3.2	4.7	3.1	4.6	3.1	6.9	6.1	12.1	5.0	3.0	8.1	6.0	5.2	11.1	6.3	9.8	5.7	5.5	4.5
F	5.8	4.6	3.5	3.4	6.8	9.3	3.7	4.7	3.5	4.3	4.2	2.7	6.9	6.5	4.5	3.7	2.4	5.3	5.0	6.6
G	5.8	4.6	4.0	1.8	7.1	6.5	3.5	3.8	2.3	3.2	5.6	2.9	3.0	3.1	1.8	2.8	2.7	4.4	2.7	3.6
н	4.1	1.2	3.1	2.8	2.0	2.5	3.7	1.7	1.9	1.7	1.6	2.5	3.4	2.2	2.3	4.3	3.1	2.1	3.0	2.5
I	7.6	10.0	5.5	7.0	7.2	7.7	5.0	14.2	6.2	9.1	7.5	3.0	5.7	5.0	6.4	5.1	3.9	9.0	8.7	6.8
K	6.2	3.2	11.7	13.3	5.2	4.3	5.2	5.9	4.5	6.9	11.0	6.4	3.7	6.2	3.4	8.3	9.5	6.3	6.5	6.8
L	10.7	7.5	4.9	6.8	7.7	7.6	5.8	10.7	8.5	14.5	10.7	6.4	8.0	7.3	8.7	6.4	4.8	10.1	10.0	7.3
M	1.4	3.2	1.7	1.0	1.8	3.1	1.3	2.1	3.2	2.5	1.9	1.7	3.9	2.2	1.1	2.1	1.5	1.5	3.2	2.4
N	2.6	1.0	3.3	3.6	1.6	2.2	2.8	1.2	2.6	2.1	2.3	7.4	2.5	4.3	2.3	3.8	4.0	2.1	2.7	2.9
P	1.8	1.2	2.1	1.9	3.0	1.7	2.8	1.6	1.1	1.9	4.0	1.9	4.1	1.7	2.1	1.9	2.0	1.7	7.7	1.7
Q	5.5	2.9	4.8	3.5	5.9	3.7	3.7	2.9	3.8	3.7	4.7	6.6	3.4	5.7	4.3	5.2	5.7	3.2	3.7	3.7
R	4.3	4.6	10.3	10.9	5.9	3.1	5.6	5.4	3.1	6.3	3.5	5.1	6.2	6.2	3.4	6.3	6.5	8.2	7.7	6.8
S	4.2	3.6	6.6	5.8	4.5	4.4	9.8	4.0	6.9	4.3	6.1	7.8	5.3	7.1	5.9	8.8	8.7	3.7	4.2	4.9
T	5.3	4.6	10.8	13.1	4.2	6.4	10.4	4.5	11.6	4.8	6.3	12.1	8.0	11.3	8.9	12.7	13.8	6.5	3.7	5.5
V	12.1	10.7	6.6	9.5	11.9	12.8	8.7	13.1	9.7	12.5	7.7	7.9	8.7	7.9	14.0	6.9	8.2	13.0	8.7	10.7
W	1.7	1.5	1.3	1.6	2.0	1.4	2.2	2.3	1.8	2.2	3.0	1.9	7.1	1.7	2.4	1.4	0.8	1.6	2.5	1.9
Y	6.2	6.3	3.6	4.4	8.7	6.1	6.1	5.8	6.1	5.3	7.5	6.4	5.0	5.3	6.8	5.3	4.0	6.3	6.2	12.6

Table A.4: Solvent accessible twisted beta-strand residue conditional probabilities

Pairwise conditional probability tables of solvent accessible residue pairs used by BetaWrapPro to detect beta-trefoils. The value in row i, column j is the probability of residue i appearing in a beta-strand given that it is aligned with residue j. They were calculated using an automated search for twisted amphipathic strands in a non-redundant structure database with the beta-trefoils removed.

Residue	A	С	D	E	F	G	Н	I	K	L	М	N	Р	Q	R	S	Т	V	W	Y
A	4.9	4.8	4.1	3.5	4.5	5.7	7.8	4.5	2.9	4.4	4.3	4.1	4.4	3.8	3.2	5.2	4.7	4.6	6.7	3.8
C	1.6	2.3	3.1	2.4	1.9	1.6	2.4	1.5	2.6	1.3	1.5	1.5	1.3	1.6	2.6	3.6	1.9	1.7	2.7	2.2
D	3.6	3.9	2.2	2.0	4.1	3.9	3.1	3.4	3.1	3.6	3.7	5.6	4.0	2.1	2.5	3.4	3.3	3.4	2.2	2.8
E	5.5	5.5	5.7	4.3	6.5	6.9	4.5	6.8	6.1	6.8	7.5	4.1	4.2	4.7	5.7	4.7	5.4	7.2	5.5	5.6
F	4.6	4.4	4.2	5.5	4.1	5.0	6.7	5.8	3.3	4.6	5.1	3.0	4.2	4.3	6.0	5.4	4.7	4.2	5.7	4.4
G	5.0	3.9	4.0	5.6	3.2	6.1	4.5	3.5	4.6	4.0	1.7	4.4	5.0	5.3	4.8	5.2	5.5	3.8	4.0	5.3
н	2.9	3.2	1.2	1.8	3.3	2.1	2.0	2.3	1.8	2.8	2.5	1.8	2.5	2.1	2.0	3.0	2.8	2.5	2.6	1.6
I	8.1	5.9	9.0	9.8	6.9	7.3	10.5	7.6	8.2	6.1	6.9	7.7	7.5	6.1	7.9	6.9	9.6	6.9	6.8	6.5
K	6.6	7.7	6.8	6.3	6.9	6.1	5.8	7.3	8.3	6.8	5.7	7.7	5.8	8.2	6.1	3.9	5.0	6.6	5.6	8.2
L	9.6	5.2	11.3	9.6	6.8	8.8	7.6	8.8	7.9	8.9	8.0	7.9	8.5	7.4	10.1	11.2	9.7	8.7	6.3	7.0
M	2.3	1.4	1.7	3.1	1.6	2.1	2.4	2.0	1.9	1.9	2.3	2.0	3.7	1.6	2.1	1.3	2.7	1.7	1.7	1.9
N	3.1	4.8	2.7	2.2	3.4	3.5	3.6	2.9	2.0	2.5	4.0	2.0	2.3	5.0	3.2	3.7	2.2	3.0	1.4	2.7
P	2.8	2.0	2.4	2.3	1.8	1.6	1.6	1.8	2.4	2.0	2.6	2.1	2.9	3.2	2.1	1.9	2.0	2.5	3.1	2.0
Q	4.6	3.2	3.8	2.3	4.2	3.6	3.8	4.4	4.1	4.5	4.3	4.3	2.3	2.2	3.5	2.7	3.7	4.1	6.4	5.5
R	5.8	5.0	6.8	6.1	7.1	5.1	5.1	5.7	6.2	6.4	4.8	7.2	6.2	7.6	5.4	5.0	4.4	6.4	5.6	5.9
S	5.3	7.5	5.2	5.7	7.5	6.8	4.7	6.7	3.4	6.4	4.4	6.3	5.2	6.8	4.1	4.1	3.4	5.1	5.1	6.1
Т	7.4	9.6	6.7	5.7	9.7	8.0	6.0	7.9	9.5	9.0	8.8	6.4	6.7	7.4	6.6	8.4	8.3	9.5	6.3	9.0
l v	8.9	9.1	13.3	13.1	9.9	8.8	10.7	9.5	9.7	11.0	13.2	11.2	11.8	11.1	11.2	11.4	11.7	11.4	7.7	9.8
W	1.4	1.7	1.9	3.0	1.8	1.1	2.7	1.9	2.3	2.0	1.3	3.0	1.3	1.6	3.2	1.4	2.2	1.5	1.3	1.2
Y	6.0	8.9	3.7	5.9	4.8	5.8	4.5	5.8	9.6	5.0	7.3	7.6	9.8	7.9	7.7	7.5	6.6	5.1	13.1	8.4

Table A.5: Solvent inaccessible twisted beta-strand one-off residue conditional probabilities

Pairwise conditional probability tables of off-by-one residue pairs used by BetaWrapPro to detect beta-trefoils. The value in row i, column j is the probability of solvent inaccessible residue i appearing in a beta-strand given that it is aligned with a residue adjacent to j. They were calculated using an automated search for twisted amphipathic strands in a non-redundant structure database with the beta-trefoils removed. Note that the table with solvent accessibility of the row and column residues exchanged can be calculated from this table.

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