

# The transverse momentum distribution of the Higgs boson at the LHC\*

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We present QCD predictions for the transverse momentum ( $q_T$ ) distribution of the Higgs boson at the LHC. At small  $q_T$  the logarithmically-enhanced terms are resummed to all orders up to next-to-next-to-leading logarithmic accuracy. The resummed component is consistently matched to the next-to-leading order calculation valid at large  $q_T$ . The results, which implement the most advanced perturbative predictions available at present for this observable, show a good stability with respect to theoretical uncertainties. The numerical program *HqT*, used to perform the calculation, is briefly discussed.

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The search for the Higgs boson is one of the highest priorities of the LHC physics program [1]. In the last years a significant effort has been devoted to refining the theoretical predictions for the various Higgs production channels and the corresponding backgrounds, which are now known to next-to-leading order accuracy (NLO) in most of the cases [2]. In the case of gluon–gluon fusion, which is the main Standard Model Higgs production channel, even next-to-next-to leading order (NNLO) QCD corrections have been computed, although in the large- $M_t$  approximation ( $M_t$  being the mass of the top quark). The result has been obtained first for the total rate [3], and more recently for fully exclusive distributions [4]. Among the possible observables, an important role is played by the transverse-momentum spectrum of the Higgs boson, whose knowledge may help to enhance the statistical significance of the signal over the background.

When the transverse momentum  $q_T$  of the Higgs boson is of the order of its mass  $M_H$ , the perturbative series is controlled by a small expansion parameter,  $\alpha_S(M_H^2)$ , and the fixed-order prediction is reliable. The leading order (LO) calculation [5] shows that the large- $M_t$  approximation works well as long as both  $M_H$  and  $q_T$  are smaller than  $M_t$ . In this framework, the NLO QCD corrections have been known for some time [6, 7, 8, 4].

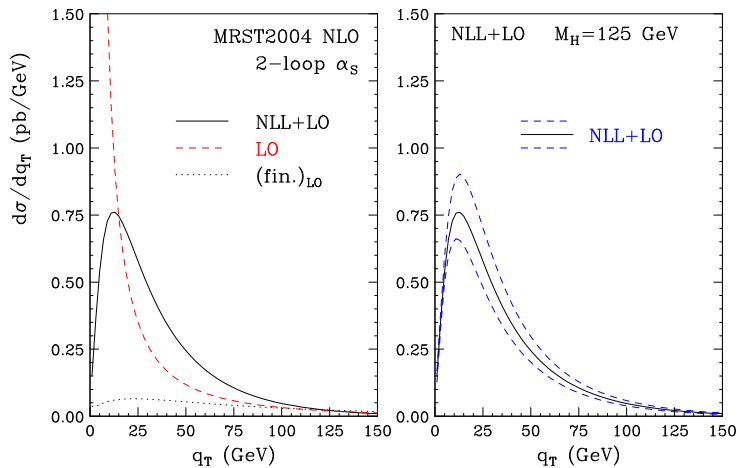
The small- $q_T$  region ( $q_T \ll M_H$ ) is the most important, because it is here that the bulk of events is expected. In this region the coefficients of the perturbative series in  $\alpha_S(M_H^2)$  are enhanced by powers of large logarithmic terms,  $\ln^m(M_H^2/q_T^2)$ . To obtain reliable perturbative predictions, these terms have to be systematically resummed to all orders in  $\alpha_S$  [9]. In the case of the Higgs boson, the resummation has been explicitly worked out at leading logarithmic (LL), next-to-leading logarithmic (NLL) [10], [11] and next-to-next-to-leading logarithmic (NNLL) [12] level. The fixed-order and resummed approaches then have to be consistently matched at intermediate values of  $q_T$ , so as to avoid double counting.

In the following we present predictions for the Higgs boson  $q_T$  distribution at the LHC within the formalism of Refs. [13]–[15]. In particular, we include the best perturbative information that is available at present: NNLL resummation at small  $q_T$  and NLO calculation at large  $q_T$ .

An important feature of our formalism is that a unitarity constraint on the total cross section is automatically enforced, such that the integral of the spectrum reproduces the known fixed-order results. More details are given in Ref. [15]. Other phenomenological results can be found in Ref. [16].

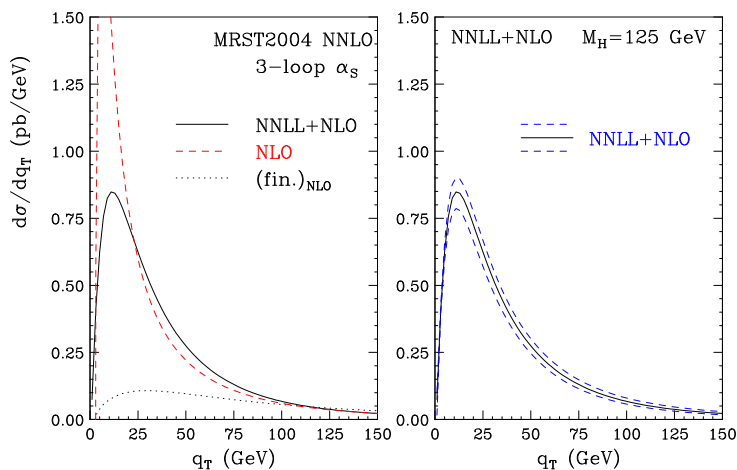
We now present quantitative results from Ref. [15] at NLL+LO and NNLL+NLO accuracy. At NLL+LO (NNLL+NLO) accuracy the NLL (NNLL) resummed result is matched to the LO (NLO) perturbative calculation valid at large  $q_T$ . Our calculation is implemented in the numerical program HqT, which can be downloaded from [17]. The code is an improved version of the original program used in Ref. [14], the main difference being in the matching procedure, which is now performed using the results of Ref. [8].

The numerical results in Figs. 1 and 2 are obtained by choosing  $M_H = 125$  GeV and using the MRST2004 set of parton distributions [18]. At NLL+LO, NLO parton densities and 2-loop  $\alpha_S$  are used, whereas at NNLL+NLO we use NNLO parton densities and 3-loop  $\alpha_S$ . The NLL+LO results at the LHC are shown in Fig. 1. In the left panel, the full NLL+LO result (solid line) is compared with the LO one (dashed line) at the default scales  $\mu_F = \mu_R = M_H$ . We see that the LO calculation diverges to  $+\infty$  as  $q_T \rightarrow 0$ . The finite component, obtained through the matching procedure, is also shown (dotted line). The effect of the resummation, relevant below  $q_T \sim 100$  GeV, leads to a



**Figure 1:** LHC results at NLL+LO accuracy.

physically well defined distribution at  $q_T \rightarrow 0$ . In the right panel we show the NLL+LO band obtained by varying  $\mu_F$  and  $\mu_R$  simultaneously and independently between  $0.5M_H$  and  $2M_H$ , imposing  $0.5 \leq \mu_F/\mu_R \leq 2$ . The integral of the spectrum agrees with the total NLO cross section to better than 1%. The corresponding NNLL+NLO results are shown in Fig. 2. In the left panel, the full



**Figure 2:** LHC results at NNLL+NLO accuracy.

result (solid line) is compared with the NLO one (dashed line) at the default scales  $\mu_F = \mu_R = M_H$ . The NLO result diverges to  $-\infty$  as  $q_T \rightarrow 0$  and, at small values of  $q_T$ , it has an unphysical peak that is produced by the numerical compensation of negative leading and positive subleading logarithmic contributions. The finite component (dotted line) vanishes smoothly as  $q_T \rightarrow 0$ , showing the quality of our matching procedure. The NNLL+NLO resummed result is slightly harder than the NLL+LO one, and its integral is in very good agreement with the NNLO total cross section. The right panel of Fig. 2 shows the scale dependence computed as in Fig. 1. Comparing Figs. 1 and 2,

we see that the NNLL+NLO band is smaller than the NLL+LO one and overlaps with the latter at  $q_T \lesssim 100$  GeV. This suggests a good convergence of the resummed perturbative expansion. Other sources of perturbative uncertainty give smaller effects [15].

In summary, considering the above results, the perturbative uncertainty of the NNLL+NLO spectrum is of about 10% at intermediate and small  $q_T$ , where the bulk of the events is concentrated. At very small  $q_T$  ( $q_T \lesssim 10$  GeV) non-perturbative effects should be taken into account, whereas at large  $q_T$  the perturbative uncertainty increases. Our results for the  $q_T$  spectrum are thus fully consistent with those on the total NNLO cross section [3].

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