

# Beam diagnostics

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## Abstract

Most beam measurements are based on the electro-magnetic interaction of fields induced by the beam with their environment. Beam current transformers as well as beam position monitors are based on this principle. The signals induced in the sensors must be amplified and shaped before they are converted into numerical values. These values are further treated numerically in order to extract meaningful machine parameter measurements. The lecture introduces the architecture of an instrument and shows where in the treatment chain digital signal analysis can be introduced. Then the use of digital signal processing is presented using tune measurements, orbit and trajectory measurements as well as beam loss detection and longitudinal phase space tomography as examples. The hardware as well as the treatment algorithms and their implementation on Digital Signal Processors (DSPs) or in Field Programmable Gate Arrays (FPGAs) are presented.

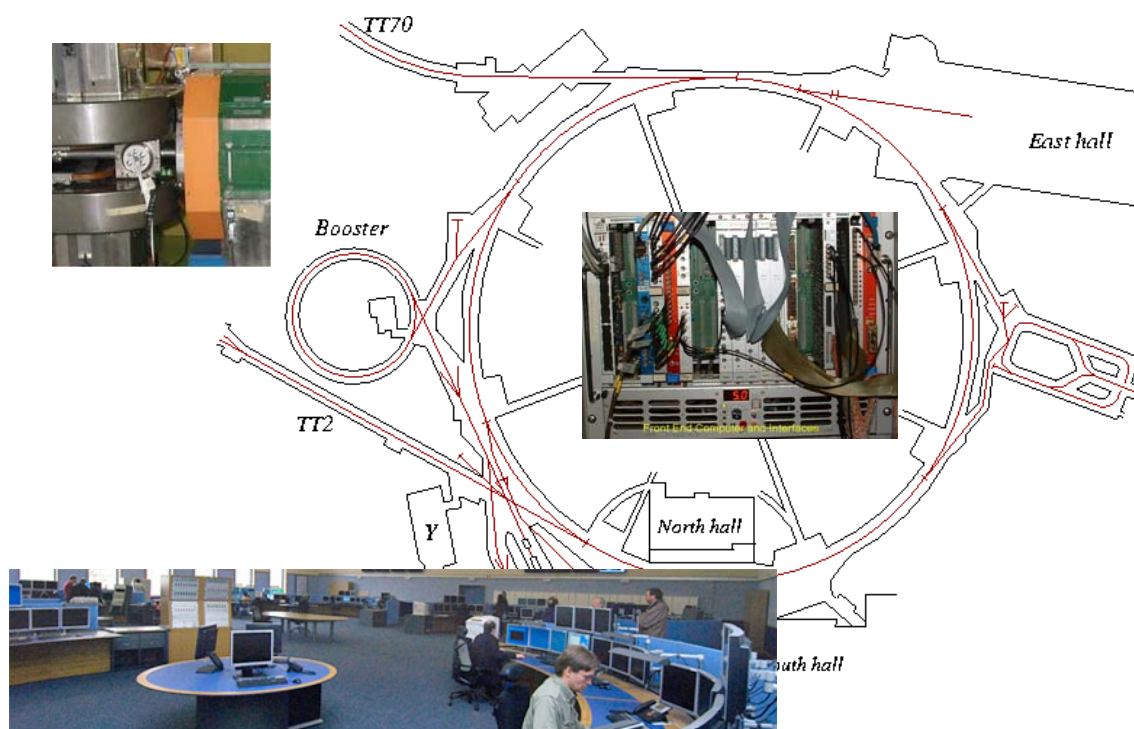
## 1 Introduction

### 1.1 Architecture of an instrument

Even though this CAS school is dedicated to *digital signal processing*, it is still a CERN Accelerator School and as such it should talk about techniques used in accelerators. Digital signal processing is a very technical field of electronic engineering and computer science and many people working in this field are not necessarily experts in accelerator physics. For this reason the lectures on beam diagnostics try to bridge the gap between accelerator physics and its measurements of beam parameters and the purely informatics and electronics aspects of digital signal processing.

Before looking at a few dedicated beam instruments, using digital signal processing principles, in some detail, let us first analyse the architecture of a beam measurement instrument in general. It consists of the following elements:

- The sensor (and maybe actuator) interacting with the beam
- The front-end analog electronics
- Cabling to get the signals from the accelerator tunnel to an equipment area
- Conversion of the sensor signals to digital values
- Data acquisition and control (readout of the digital values)
- Transformation of the acquired values to humanly understandable machine parameter values
- Transfer of the results to the control room
- Graphical representation and interpretation of the results



**Fig. 1:** The architecture of a measurement system

In order to avoid signal loss and capture of electro-magnetic noise, the first-stage electronics must be installed as close as possible to the sensor. On the other hand it may be subject to very high radiation doses (some kGrays). Therefore the front-end electronics is installed as near to the sensor as possible but as far away as necessary to protect the electronics from radiation damage. Typical cable length from the detector to the first stage electronics is a few (1–10) metres. The signal is amplified and shaped in this first stage of the electronics. The amplified analog signals are then transferred to the equipment gallery and digitized. In case of smaller machines like the PS, where the equipment gallery can be reached within some 100 m, the analog signals are transferred to the equipment rack and digitized there. In very big machines, like the LHC, where the distance from the underground tunnel to the equipment galleries at the surface may be 1 km or more, the analog signals are digitized in an equipment gallery in the tunnel and serial transmission is used to transfer the digital values to the surface. The digital results are stored in registers or memories and read out by front-end computers (called Device Stub Controllers (DSCs) at CERN). All front-end computers are connected through a local area network which also connects to operator consoles (PC-type computers with several screens attached to them) from which operators control the machine and from where they have access to measurement results in the form of numbers or graphical representation.

Digital signal processing may come into play at several levels, as soon as the sensor signals have been digitized. This may be the case in the equipment gallery in the machine tunnel for big machines or in the equipment room at the surface, but it may also take place only at the level of the operator consoles. Often the front-end computers are used to do the calculations, sometimes special FPGA or DSP based equipment take over this task, sometimes, for slow applications or very compute intensive ones, the operator consoles or special number-crunching machines execute the DSP algorithms.

Figure 1 shows the layout of a typical instrument in the PS. The sensor, here a beam position monitor, is connected to its analog front-end. The amplified signal is sent to the equipment room with

its VME base front-end computer  $\sim 150$  m away. There the data are read out, pre-treated and then transferred to the main control room at a distance of some 5 km.

## 2 Tune measurements

As a first typical example, where digital signal processing techniques are used in beam diagnostics, we shall have a look the the machine tune  $Q$ .

### 2.1 What is the machine tune?

When a particle is not exactly on its design orbit it will not pass through the centre of the machine's focusing quadrupoles and therefore it will experience a focusing force, which will lead to so-called betatron oscillations. The number of oscillations around the closed orbit is called the betatron tune. This is true for horizontal as well as for vertical displacements. If the number of oscillations corresponds to an integer value, then each small imperfection in the machine will lead to a small kick, which will be repeated each time the particle passes that point. This leads to a (integer) resonance, which will result in the loss of the beam. It can easily be shown that the same is true for half integer tunes and in fact any particle for which  $l \cdot Q_h + m \cdot Q_v = r$  holds where  $Q_h$  and  $Q_v$  are the horizontal and vertical tune values. The tune diagrams show these lines of instability, see Fig. 2.

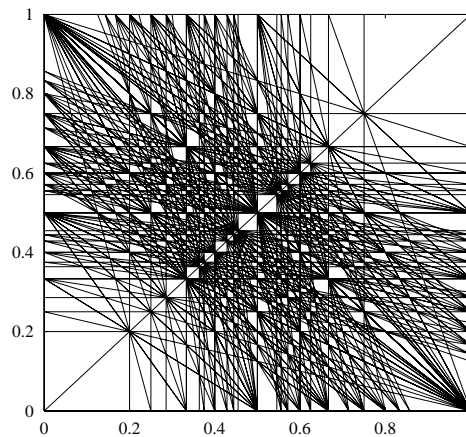


Fig. 2: The tune diagram

The machine must operate in a resonance-free zone of the tune diagram (the working point) Fig. 3, in order to avoid beam blow-up and finally loss of the beam. This shows the importance for a precise determination of the tune values.

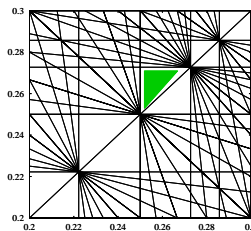


Fig. 3: The working point

## 2.2 Measuring the tune

In order to measure the tune values, the betatron oscillations must be observed. This can be done by placing beam-position monitors all around the accelerator ring and observing the beam trajectory. Since normally the beam circulates on its closed orbit with very small (unmeasurable deviations) the beam is usually coherently excited with a kicker magnet. As we have seen in the previous section we are actually only interested in the non-integer part of the tune and this can be measured with a single beam-position monitor. In Fig. 4 you can clearly see that it is not possible to distinguish  $q$  from  $1 - q$  and that, in addition to the base frequency, higher harmonics can be fitted to the data measured by the pick-up.

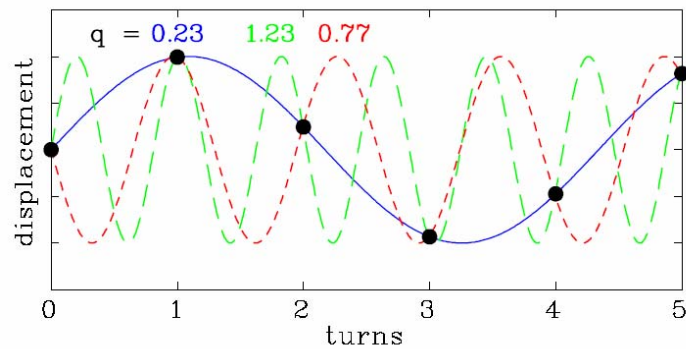


Fig. 4: Measuring tune with a single pick-up

The measurement at the CERN PS and PS Booster works as follows: The beam is excited with a kicker in short intervals (minimum 5 ms) (Fig. 5). The beam position is measured by a pick-up (PU) delivering horizontal and vertical difference signals which are proportional to the beam displacement. The PU is of shoebox type, consisting of a metal box with a diagonal cut. In fact, the PU used here (Fig. 6) combines horizontal and vertical cuts in a single device with four taps to extract the signals from the left/right and upper/lower plates.

A passive hybrid circuit, being virtually insensitive to radiation, is mounted directly on the pick-up (the denominations pick-up (PU) and beam position monitor (BPM) are used interchangeably). The hybrid combines the signals from the PU plates and converts them to difference ( $\Delta$ ) and sum ( $\Sigma$ ) signals.



Fig. 5: The tune kicker

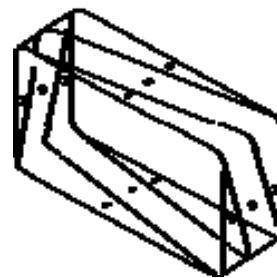


Fig. 6: Pick-up electrodes

During acceleration the beam may undergo slow but rather large closed-orbit variations which are filtered out by a Beam Orbit Signal Suppressor (BOSS).

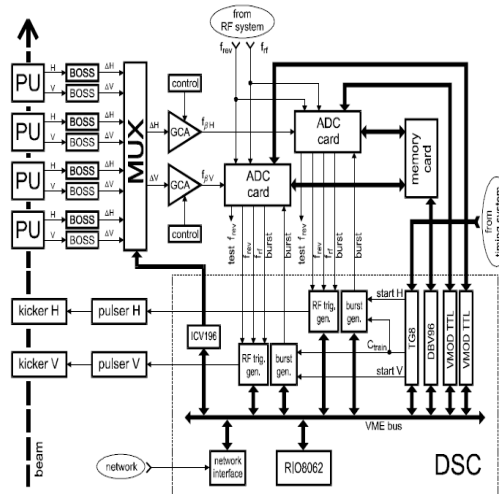


Fig. 7: Tune measurement electronics

Figure 7 shows the architecture of the readout electronics at the PS Booster. The Booster actually consists of four vertically stacked synchrotrons. The MUX is used to select the position signals from any of the four Booster rings. The difference signal is not only proportional to the displacement but also to the beam intensity, which may vary by several orders of magnitude. This is taken care of by a Gain Controlled Amplifier (GCA). The signal is converted to digital values with a 14-bit ADC and 2048 converted values are stored in a memory card. A digital signal processor card (DBV96) with a Motorola 96002 Digital Signal Processor accesses these data over a dedicated high-speed memory bus.

The results are stored in DSP memory and can be transferred to the VME processor through a communication mailbox implemented in the DSP. From there the results are transferred over the local area network to the operator consoles in the control room for visualization.

### 2.3 Calculating the tune

As can be seen from Fig. 4 the frequency of the measured signal is related to the revolution frequency and the oscillation mode through

$$f_{\beta} = (m \pm q) f_{\text{rev}}, \quad (1)$$

where  $m$  is the integer number of oscillations and  $q$  is the non-integer part of the tune. Since the integer part of the tune stays constant, only  $q$  needs to be measured. This reduces the equation to

$$\frac{f_{\beta}}{f_{\text{rev}}} = q. \quad (2)$$

As already mentioned, the closed orbit is not centred and stable during acceleration which results in an additional component of the revolution frequency in the signal. A convenient way to calculate  $q$  is to sample the PU signal at a rate proportional to the revolution frequency and to perform FFT analysis on  $N$  samples. Using a sampling rate of  $k \cdot f_{\text{rev}}$  ( $k$  is the over-sampling ratio)  $q$  can be determined by

$$q = k \frac{n_{\beta}}{N}, \quad (3)$$

where  $n_{\beta}$  is the bin number in the FFT spectrum.

### 2.4 Data handling

After the start of the measurement the beam is kicked (Figs. 8 and 9) and 2048 beam positions are measured and stored in a dedicated memory card. These data are transferred to the DSP and the memory is again freed to take new data. Through this double buffering, data can be taken while the previous batch is processed by the DSP.

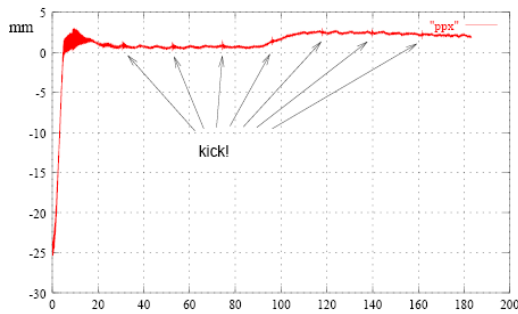


Fig. 8: Kicking the beam

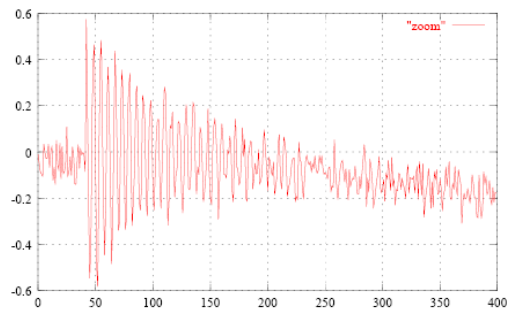


Fig. 9: Zoom of the kick

The Fourier transform expects a signal that constitutes one cycle of a periodic signal. Since our signal is cut out of the stream of oscillations in an arbitrary manner, discontinuities occur when extending it to a periodic wave form (Fig. 10).

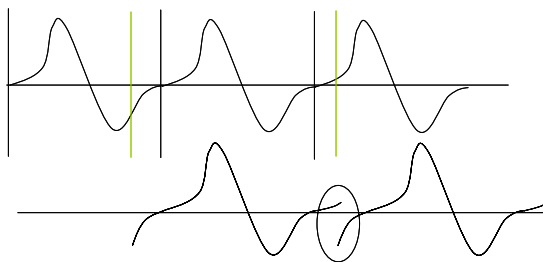


Fig. 10: Periodic extension of the position signal

For the calculation of the Fourier spectrum a 1024 point complex FFT is used, followed by an algorithm to extract the real signal spectrum from the complex spectrum data.

From the Fourier spectrum the  $q$  value must be found through a peak search routine. Since the over-sampling ratio in Eq. (3) amounts to 4, only a quarter of the power spectrum needs to be looked at.  $Q$  can only take values between 0.1 and 0.5 which means that the search is limited to a window of 50 and 256. The peak search algorithm first looks for the bins for which

- the power value  $V^2$  is bigger than the next value:

$$V^2(n-1) < V^2(n)$$

This phenomenon can be corrected by windowing. Each value is multiplied by a coefficient which approaches zero at the edges of the window. Typical windowing functions are shown in Fig. 11. For the tune measurement system the Blackman–Harris function is used. The values are pre-calculated and stored as coefficients in a table at initialization of the DSP.

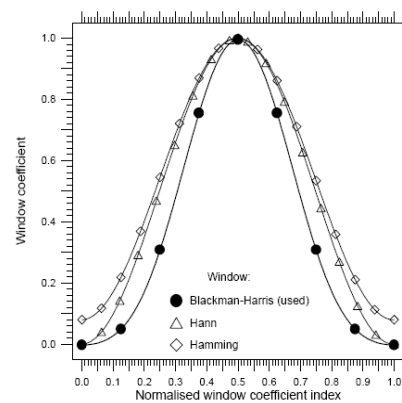


Fig. 11: Windowing functions

- the power value  $V^2$  is bigger than the following value:  $V^2(n+1) < V^2(n)$
- the power value satisfying the first two conditions is the biggest in the observed range
- the power value is at least three times as big as the arithmetic mean of all power bins. The value 3 has been determined experimentally.

If these conditions cannot be fulfilled then either the signal is too small or the spectrum is too noisy.

Most of the mathematics code for the DSP has been written in the C language except for small parts like the arithmetic mean, which has been implemented in assembler for reasons of speed.



Fig. 12: The frequency spectrum

### 2.5 Spectrum interpolation

When just taking into account the bin in which the peak is found, the resolution for  $Q$  is very limited. In order to improve the resolution one can

- increase the number of points, but this would increase the computing time and therefore slow down the system;
- decrease the over-sampling, but this would lead to a degradation to the system input dynamics;
- interpolate between adjacent bins.

The betatron frequency spans over several bins, not only because of the discrete FFT but also because the incoming signal is not a pure harmonic but includes attenuated revolution frequency components, noise, etc. Interpolation allows one to find the peak position with a resolution better than a bin. The exact form of the peak is unknown but it could be shown that using a parabolic shape, which is easy to calculate, can improve the  $Q$ -value calculations significantly.

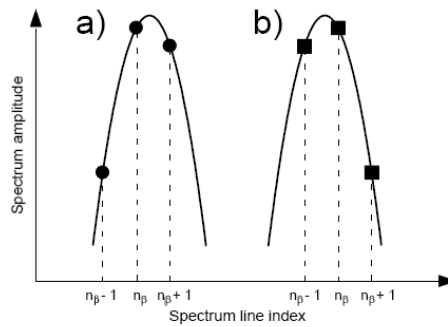


Fig. 13: Tune value interpolation

### 2.6 Measurement results

During the acceleration cycle the beam is kicked every 5 ms and the  $Q$  value is calculated for each of these kicks. A front-end computer reads the results from the DSP and passes them on to an application program in the central control room where the evolution of the tune during the cycle can be observed in graphical form (Fig. 14). The application program also allows the control of the measurement interval, amplifier gains, start of measurement in the cycle and other parameters.



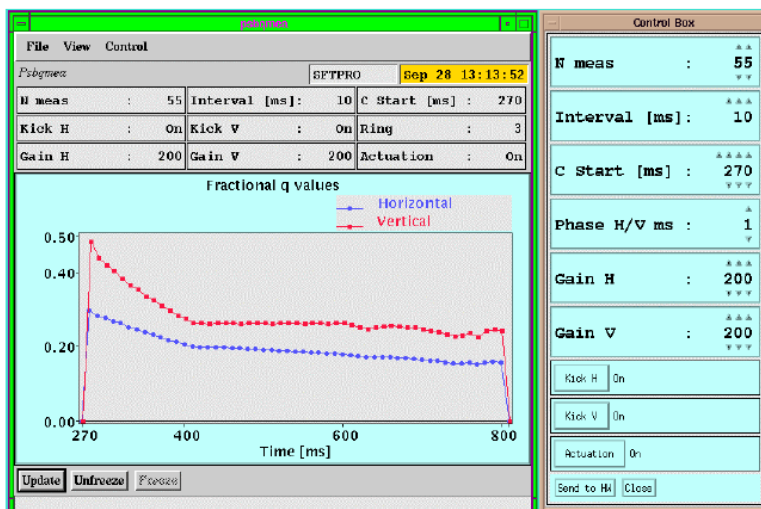


Fig. 14: Tune measurement results

### 2.7 Further improvements

As can be seen from Fig. 9 the position peaks are very sharp because the beam bunch is short with respect to the revolution frequency. As a result the signal power is distributed over many harmonics in the frequency spectrum. By rectifying the signal with a simple diode and capacitor circuit (see Fig. 15) the signal spectrum can be pushed to the base band and thus the signal power in the tune line to be measured can be significantly increased. This shows that a careful balancing between analog and digital methods is needed.

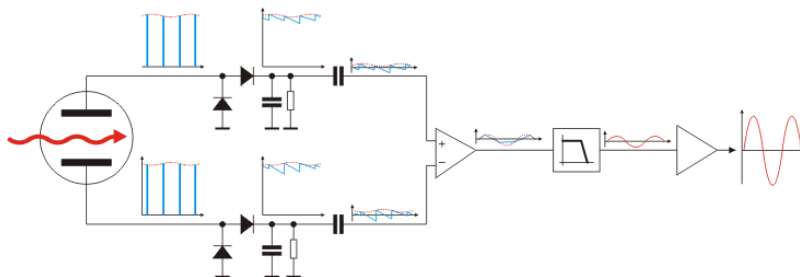
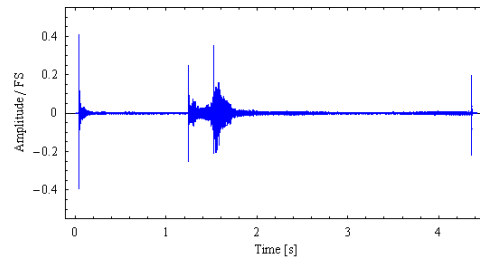


Fig. 15: Base band  $Q$  measurement system

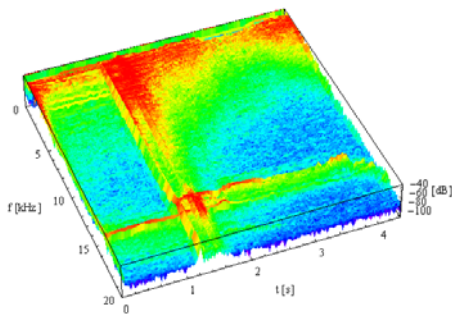
Through this trick it was possible to measure tunes in the SPS without artificial coherent excitation of the beam.

Figure 16 shows beam oscillations as they arise during an acceleration cycle in the CERN SPS. The first strong peaks are due to injection, the last peak is created when the ejection kicker is activated. Figure 17 shows a waterfall model of the corresponding frequency spectra. It can be seen that the frequencies fall into the audio range which allows one to use very powerful and cheap audio range which allows one to use very powerful and cheap audio systems for data acquisition.





**Fig. 16:** Natural beam oscillations



**Fig. 17:** Waterfall model of frequency spectra

The tune measurement system described in the previous sections was state of the art some 10 years ago but it is still in operation today. The DSP chip is now obsolete and the software development system consisting of C-compiler, assembler and debugger uses PC hard- and software that are no longer available.

Upgrades of the digital hardware are foreseen where the DSP will be replaced by a field programmable gate array (FPGA) allowing much increased calculation speed. Like this 128 000 data points can be treated instead of the 2048 and  $Q$  interpolation will not be needed any

more. This shows the common problem that digital hardware and its associated software tools are evolving much faster than the accelerators which have lifetimes of several decades (the CERN PS was inaugurated in 1955!).

### 3 Trajectory measurements

#### 3.1 Trajectories and orbits

When particles are injected into a circular accelerator, injection errors may occur, resulting in coherent oscillations around the closed orbit. These oscillations may be caused by beam displacement and/or wrong injection angle and may cause emittance blow-up through filamentation. The oscillations can be seen when beam positions are measured turn by turn. When traversing transition (the moment when due to acceleration the orbit radius starts shrinking instead of increasing) the beam may undergo trajectory changes. This also occurs at ejection. Other effects during acceleration may also influence the trajectories. For this reason it is desirable to be able to measure beam trajectories at any time during the acceleration cycle.

In contrast to the beam trajectory, the beam orbit is the average beam position over several turns in the machine. During acceleration the orbit may move considerably and beam losses may occur due to aperture limitations. It is therefore important to be able to measure the orbit all along the acceleration cycle.

#### 3.2 Synchronization

In order to measure beam trajectories it is necessary to have a large number of BPMs in the machine evenly distributed along the accelerator ring. In the CERN PS there are 40 PUs while in the LHC several thousands will be installed. Since the accelerator can treat several particle-bunches (depending

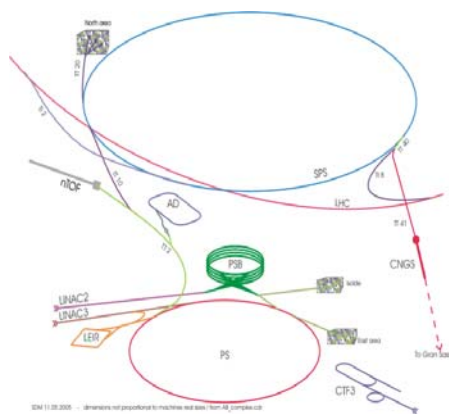
on the RF frequency) at the same time, each bunch must be measured turn by turn and the position data saved for the whole accelerator cycle. Another, but less flexible method, is to define beforehand the time interval during the acceleration cycle we are interested in and save the data for this interval only.

For low-energy accelerators, where the particle has not yet reached the speed of light, the acceleration will result in a speed increase and therefore in an increase of the revolution frequency. This means that the integration gate, needed for integration of the BPM's  $\Sigma$  and  $\Delta$  signals must be continuously adapted to the revolution frequency. The current trajectory measurement system installed in the PS can measure one bunch during two turns every 5 ms and has a very complex synchronization system associated to it, following the revolution frequency in order to generate the integration gate supplied to the ADC.

In order to complicate things further, the RF harmonic number (the number of RF cycles per revolution, which is equal to the maximum number of bunches that can be accelerated) can be modified during the acceleration cycle. This allows the splitting of bunches into several bunchlets or the recombination of several bunchlets into one big bunch. In such a case, the number of integration gates must be changed on the fly.

The CERN control system allows several operators at different operator consoles to access data from the same measurement system. For example, one operator wants to check the orbit at injection, while another one wants to see the orbit at transition and this should be possible for the same accelerator cycle.

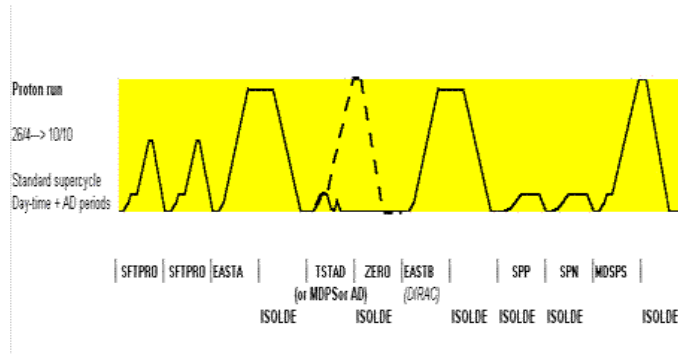
As can be seen from Fig. 18, the PS can take particles from Linac2 or Linac3 and it can eject particles to experimental areas (East Hall or nTOF), it can create antiprotons for the Antiproton Decelerator (AD), or it can transfer protons to the SPS for fixed-target physics or for injection into the LHC.



**Fig. 18:** Different beams in the PS

For maximum flexibility the PS implements a concept called *pulse-to-pulse modulation* (ppm) which allows assembling a series of different acceleration cycles into a so-called super-cycle which is repeated. At any moment it is possible to add or remove any of the individual acceleration cycles using a super-cycle editor. In this way several *users* can use the machine at the same time, everybody getting a few time slices of the global beam time.

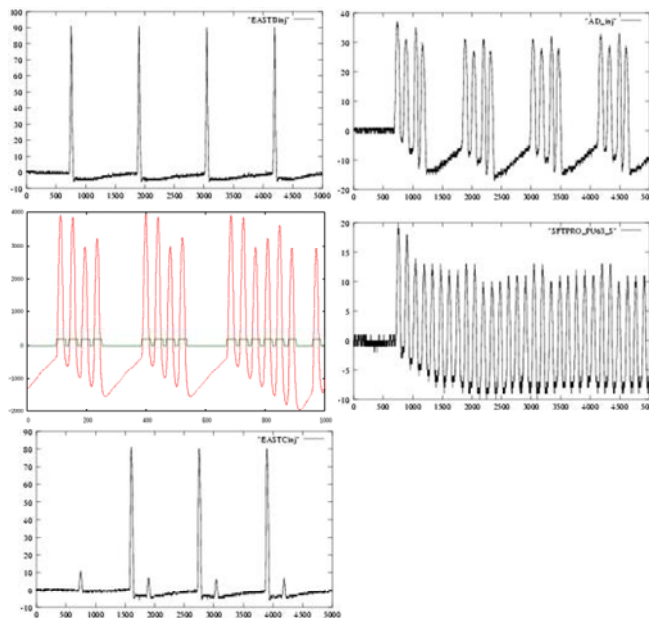
Figure 19 shows a typical super-cycle. For low proton energy the cycle time in the PS is 1.2 s while for high energy the cycle time is doubled. For these cycles the Booster may accelerate two cycles where the one accelerated during the time the PS is busy is extracted from the Booster directly to ISOLDE. The first text line under the cycle diagram denotes the cycles in the PS (SFPRO, EASTA, etc.) while the second line shows additional cycles in the PS Booster.



**Fig. 19:** The PS super-cycle

The consequence of this flexibility is that the trajectory measurement system must deal with a great variety of different types of beams (Fig. 20):

- EASTB: a single bunch on  $h = 8$
- AD: four bunches on  $h = 8$
- LHC: four bunches on  $h = 7$ , two additional bunches are injected on a consecutive Booster cycle
- SFTPRO: eight bunches fill all buckets on  $h = 8$
- EASTC: A small bunch is injected into the first RF bucket, a second, much more intense bunch is injected into bucket no. 7. The intense bunch is ejected at 14 GeV. The small one is further accelerated and extracted to a different area later in the cycle.



**Fig. 20:** Beam types in the PS

### 3.3 Readout requirements

In order to provide trajectory data at any time within the acceleration cycle, the bunch positions must be calculated turn by turn, from injection into the machine until ejection. This can be done by simply sampling the  $\Sigma$  and  $\Delta$  signals coming from each BPM in the machine, fast enough to numerically integrate them and subsequently calculate the position from the integration results. It is by far easiest to use a fast sampling clock, asynchronous to the revolution frequency. With a bandwidth of the pre-amplifiers located near the BPMs of 30 MHz and expecting at least four samples for a 30 ns bunch, we need a sampling frequency of 120 MHz. Since an acceleration cycle in the PS can take 2 s, we need at least 300 Msamples per signal and therefore a total of  $8 * 3 * 2 * 300$  Mbytes (eight bunches, three signals per pickup, 2 bytes per sample).

From these quick calculations it can easily be seen that it will be necessary to treat the data on the fly, such that only position-data for each bunch and not individual ADC samples are stored. The idea is therefore to use an FPGA to read out the ADC samples, create integration gates synchronous to the bunch frequency on the fly, and perform online baseline correction and integration. Figure 20 clearly shows how the baseline moves depending on the number of bunches and their intensity in the machine.

### 3.4 Readout electronics

As we have seen in the previous section, the electronics must be capable of

- Reading ADC samples at a rate of  $\sim 120$  Msamples/s
- Synchronizing to the bunch frequency
- Generating the integration gate and numerically integrating the signal
- Finding the baseline and correcting for baseline movement
- Storing the integrated and baseline-corrected  $\Sigma$  and  $\Delta$  signals in a large memory being capable of keeping all values acquired during a 2 s acceleration cycle
- Giving access to the acquired data to the external world

The only way this can be done with today's technology is by use of a fast FPGA associated with big memories.

Figure 21 shows the basic electronics layout. The data coming from the ADC (light blue) block is treated by the FPGA (violet) and stored in memory (yellow). The data can be read out by a single-board computer with Ethernet interface.

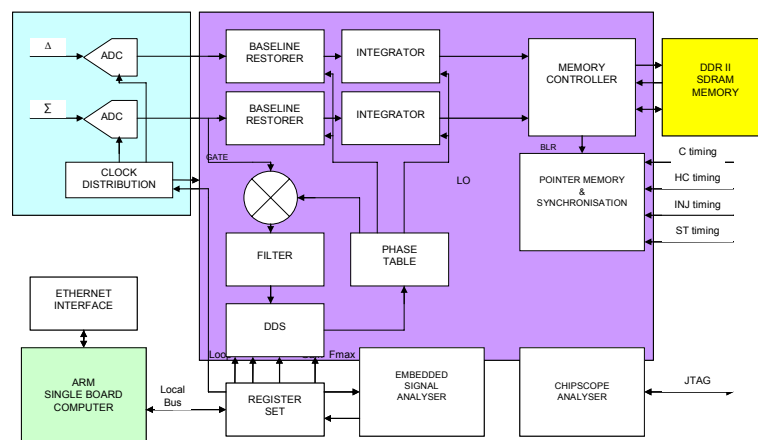


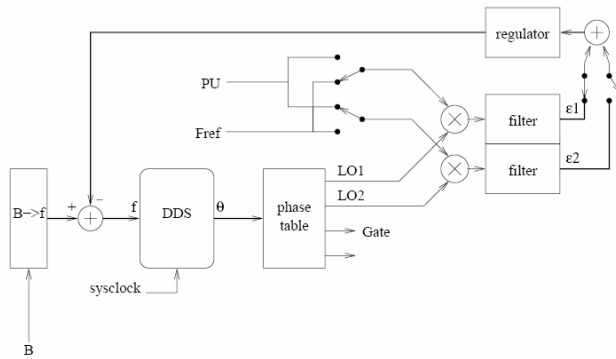
Fig. 21: Trajectory measurement electronics

**3.5 The algorithms**

In order to develop the algorithms for synchronization, baseline correction, and numeric integration for the different types of beams shown in Fig. 20, the FPGA is first programmed as a chart recorder, sampling—passing every sample from the ADC through to the memory. Like this only parts of the acceleration cycle can be recorded but by changing the acquisition trigger any time-slice in the cycle can be selected. The acquired data are read out from the memory and stored on files. The algorithms can be developed in MathLab or as offline C programs and can be tested on real data.

**3.5.1 The PLL**

The basic idea for synchronization is a numerical phase-locked loop. The local oscillator (LO) is implemented as a direct digital synthesizer (DDS). The phase of this DDS is compared to the BPM signal and the phase error is filtered and fed back to keep the DDS synchronized. The initial guess of the LO frequency is determined from the measured magnetic field in the accelerator from which the particle energy and thus its speed and revolution frequency can be calculated.



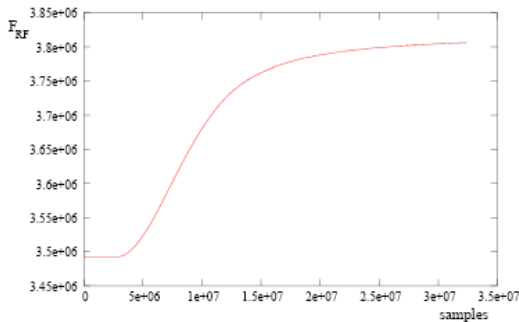
**Fig. 22:** Phase-locked loop

Each incoming PU sample is compared with the phase table to decide if it is part of the signal or part of the baseline. The phase table is simply a circular buffer addressed by the highest significant bits of the DDS phase accumulator. The content of the phase table depends on the harmonic number and is pre-loaded before the start of the acceleration cycle. In case of RF gymnastics (see Section 3.7) the phase table

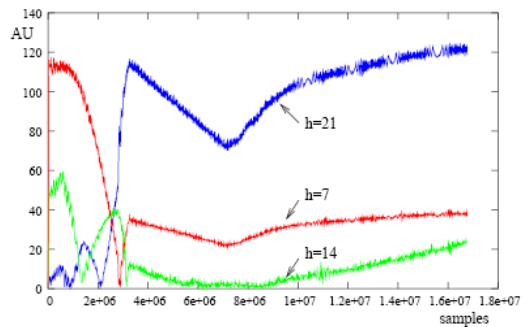
must be switched to new values on the fly.

The problem is similar at injection: Before having beam in the machine there are no signals coming from the PUs. Instead a reference signal coming from the RF system is used for synchronization. Once the beam is circulating in the machine an external timing pulse switches to the new reference frequency.

These algorithms can be easily tested offline on the data taken with the chart recorder.



**Fig. 23:** Measured frequency swing during acceleration



**Fig. 24:** Frequency contents during bunch splitting

### 3.5.2 Baseline correction

The PU together with its load resistance delivers a high-pass filtered, and therefore differentiated version of the beam signal. The baseline restorer uses a low-pass filter and therefore an integrator, with the same cut-off frequency as the PU thus compensating the differentiation effect. When integrating, however, the integration constant is not known and a DC level may be added to the signal. Since we know that this DC level should be zero, a second accumulator is added, which is only active when the ADC sample is part of the baseline, which can be deduced from the synchronization PLL.

### 3.6 Algorithm implementation in the FPGA

In the first, offline approach, the PLL in Fig. 22 was implemented in a C program. The filter was a second-order Butterworth low-pass filter whose coefficients were determined using a Matlab program.

$$H_F = 9.8 \cdot 10^{-6} \frac{1 + 2z^{-1} + z^{-2}}{1 - 1.9911z^{-1} + 0.9911z^{-2}}$$

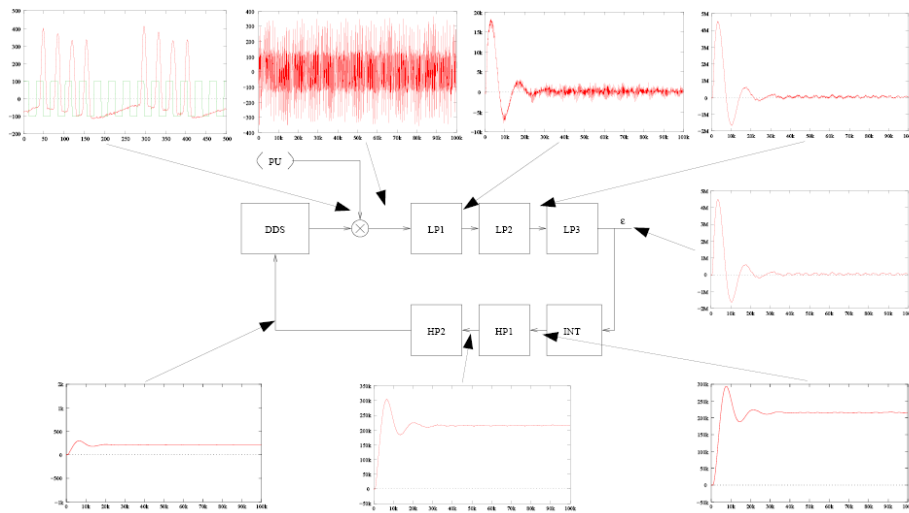


Fig. 25: Splitting the loop filter

Once implemented in the FPGA the algorithms must be capable of swallowing the data coming from the PU, which means a rate of  $\sim 120$  MHz. Calculating this formula in floating point is simply not feasible. Therefore the algorithm was reviewed and replaced by a series of low-pass filters followed by an integrator and high-pass filters using exclusively integer calculations in such a way that the coefficients can be calculated with a few shifts and additions. By subdividing the filter into several stages, pipelining the algorithm in the FPGA becomes possible. Because of the large ratio between sample rate and the dominant system frequencies, a few clock cycles of pipeline delay do not affect the loop dynamics. Once the baseline is corrected and the signal is synchronized, the phase table is used to generate the integration gate. All  $\Sigma$  and  $\Delta$  samples within the integration gate are added and the results stored in memory. The positions can then be calculated through

$$x = S_x \frac{\Delta_x}{\Sigma}$$

### 3.7 Harmonic number changes

Synchronization is largely complicated through harmonic number changes. By changing the RF frequency the bunches can be split into several sub-bunches (bunch-splitting) or the distribution of the bunches on the ring circumference may be modified (batch compression).

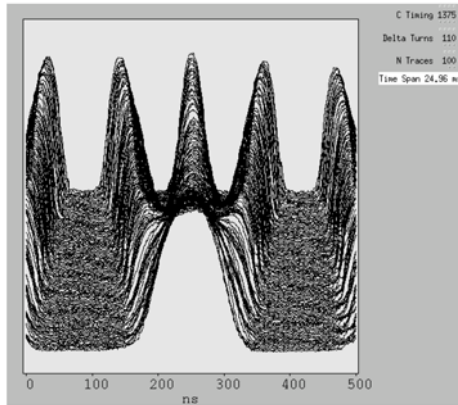


Fig. 26: Bunch Splitting

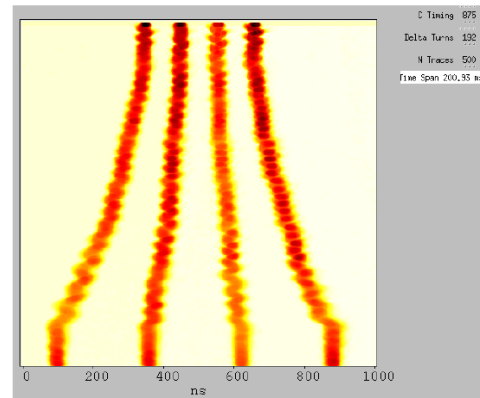


Fig. 27: Batch compression

The frequency contents of the PU signals during triple splitting (a bunch is split into three as seen in Fig. 26) is plotted in Fig. 24. At a certain moment, determined by an external timing signal one must decide to switch from measuring the position of a single bunch to measuring the positions of the three bunchlets. This moment corresponds to the crossing of the blue ( $h = 21$ ) and the red ( $h = 7$ ) frequency lines in Fig. 24.

In order to find back the position in the table of measured  $\Sigma$  and  $\Delta$  values where the switch has happened, address pointers, linked to these external timing events, must be kept in a separate table.

### 3.8 Integration

Last not least, the baseline corrected sum and difference signals must be integrated, which is done by simple addition of the samples within the integration gate calculated by the synchronization algorithm.

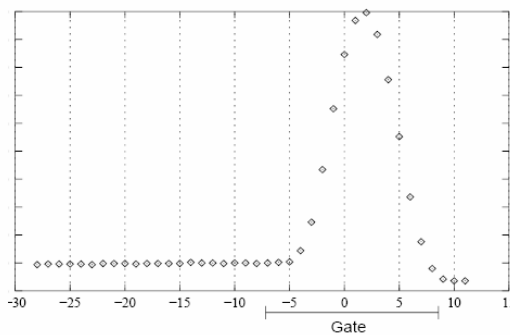


Fig. 28: Integration



Fig. 29: Energy of a LHC bunch at 7 TeV



## 4 Machine protection systems

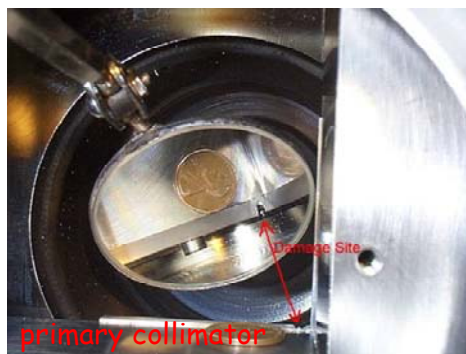
While in low-intensity and low-energy accelerators the beam cannot do much harm even if the whole beam is lost in the vacuum chamber, this is clearly not the case for high-energy and high-intensity machines. Even at the CERN Linac, a machine with a top energy of 50 MeV, 160 mA during a 200  $\mu$ s beam pulse and a repetition rate of 1.2 s it was possible to burn a hole in one of the vacuum joints. How much more critical is the problem in the LHC, where we shall have 2808 bunches at 7 TeV? People amuse themselves calculating the equivalent kinetic energy of known everyday objects. The energy of single bunch in the LHC at top energy corresponds to a 5 kg bullet at 800 km/h<sup>1</sup> and don't forget that there are 2808 of them in the machine. On the other hand, these bunches circulate in a magnetic field which is generated by supra-conducting magnets. The loss of a very tiny fraction of these particles will result in a magnet quench, and the loss of a big amount, concentrated in a small volume, will result in destruction of the equipment.

At the Tevatron, even though its beam power is 200 times less than the power in an LHC beam, a hole was drilled into the primary collimator (Fig. 31), when the beam was displaced by 3 mm due to insertion of a movable device, when it was supposed to be out of the vacuum chamber. The secondary collimator was

largely  
damaged and  
16 magnets  
quenched.



**Fig. 30:** Ionization chamber



**Fig. 31:** Beam damage

### 4.1 Machine protection using beam loss monitors

The strategy for machine protection at the LHC is based on the measurement of beam loss with dedicated Beam Loss Monitors (BLMs). When a high-energy particle is lost, it will produce a particle shower whose energy is partially absorbed in the surrounding magnet coil but part of which can be detected by the BLMs. As long as the calibration factor of energy deposition in the magnet coils with respect to the energy deposited in the BLM is known, the BLM signals can be used to trigger beam dumps as soon as the energy deposition in the magnets gets to a level where a magnet quench must be feared. By dumping the beam and thus avoiding a quench, long beam downtime can be avoided. For even bigger beam losses, where the magnets or other equipment are at risk of destruction, this is even more true.

<sup>1</sup> Rüdiger Schmidt, <http://rudi.home.cern.ch/rudi/docs/VisitLHCWuppertal2006.ppt>

On the other hand, the levels for triggering beam dumps must not be set too low because this may prevent running the machine altogether.

In order to set the trigger levels correctly, the allowable losses must be known. These depend on the energy of the primary particle and on the loss duration as can be seen from Fig. 32. It is therefore important to integrate the measured losses over several time periods and set corresponding thresholds for each of these integration periods. Only like this can short and strong losses be treated as well as smaller but prolonged losses.

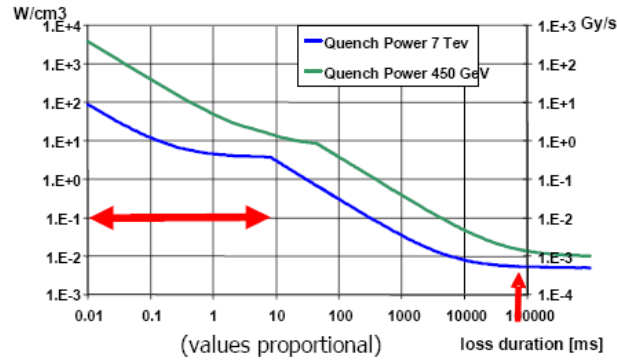


Fig. 32: Quench levels

For safety systems, in addition to the standard technical specifications like dynamic range, resolution, response time, etc., the *Mean Time Between Failure* (MTBF) is an important parameter. It defines how secure the system actually is. When the security system itself fails it must go into a failsafe state, which, as a consequence, makes the protected system unavailable.

Most of today's machine protection systems use ionization chambers as their BLMs (the LHC BLM can be seen in Fig. 30). These are gas-filled detectors ( $N_2$  in case of the LHC BLMs) with the following properties:

- High dynamic range ( $10^8$ )
- Very good resistance to radiation (several MGray/year)
- High reliability and availability

The BLM signal is integrated using a charge-balanced integrator and converted to a proportional frequency with a current-to-frequency converter (CFC). This method allows the handling of a very high dynamic range. The CFC frequency is counted over a period of  $40 \mu s$ . For very low currents and to allow faster response, an ADC was added. The converted signal is transported from the machine, some 80 m underground to the surface through optical fibres. Eight detectors are multiplexed onto an optical link and the links are doubled. The digital signal treatment is performed by a radiation-resistant FPGA which

- reads out the converted signal,
- encodes the values in order to prepare them for transmission over the redundant optical serial links,
- multiplexes values from eight detectors onto a signal transmission channel,
- performs CRC calculations.

The electronics on the surface receives the values from the optical links, checks the CRC, demultiplexes the signals from the eight BLMs and gives access to the beam loss values through the

VME bus. It also connects to the Beam Interlock System (BIC) generating beam dumps, should this be

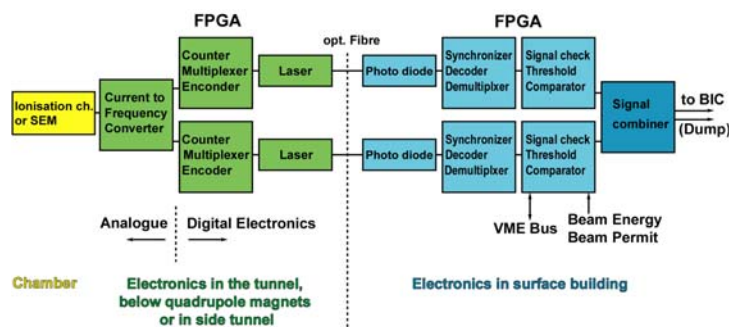


Fig. 33: Layout of the BLM electronics

necessary.

#### 4.2 The data acquisition board

We have already seen an electronics layout consisting of ADCs, an FPGA reading out the converted signals and treating them through fast digital signal processing algorithms implemented as VHDL code in the FPGA, followed by memory, used to store the final result. Some sort of access to this memory is needed in order to further treat the result and make it available on the operator consoles in the control room in the form of easily readable numerical values, tables, or graphs.

The requirement of FPGAs connected to some sort of external signal in conjunction with access to the final stored data is general enough to allow the design of a generic card which can be used for a variety of applications.



Fig. 35: Photo of the Data Acquisition Board

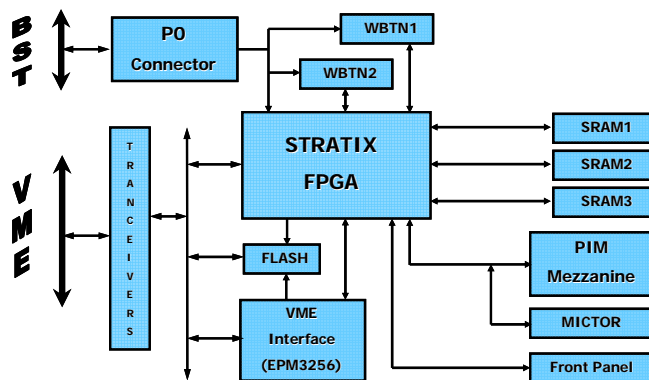


Fig. 34: Block diagram of the Data Acquisition Board

The Data Acquisition Board (DAB) is implemented as a VME board built around an Altera Stratix FPGA. The FPGA can be boot-strapped through a flash memory containing the FPGA code. This memory is also accessible via the VME bus. In addition, external timing signals (Beam Synchronous Timing (BST)) can be accessed by the FPGA and used within the FPGA algorithms. In order to be as flexible as possible the FPGA has access to a local mezzanine bus. Mezzanine boards implement the application-specific hardware. Like this the DAB can be used to treat signals from the orbit system, based on several thousands of BPMS, it can be used by intensity measurements systems

where signals from beam current transformers are treated, or it can be used to handle the communication protocol in order to read out signals from the beam loss system.

### 4.3 Data treatment for the beam loss system

#### 4.3.1 Data treatment in the tunnel

The signal coming from the BLM is converted into frequency for coarse conversion, where a counter is used to get the final coarse value. The voltage measured on the ADC is the remainder between the last count and the first count from the next acquisition. Before sending these data to the optical communication channels, the ADC and counter data are combined to a 20 bit loss figure. Eight such values are encoded, multiplexed, and sent to the surface electronics after a CRC value has been added.

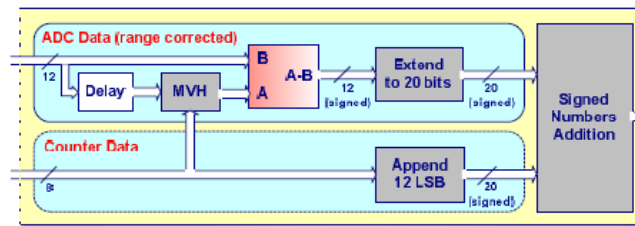


Fig. 36: Beam-loss dynamic range

#### 4.3.2 Data treatment on the surface

The data treatment algorithms in the DAB, installed at the surface, must perform the following actions:

- Receive the values from the electronics in the tunnel via the optical fibres.
- De-multiplex the data coming from different BLMs.
- Check the CRC and compare the data coming from the redundant communication channels. If the data from the two channels differ: decide which one is right.
- Calculate successive sums in order to see fast big losses as well as slow small losses.
- Compare the successive sums to threshold values in order to trigger beam dumps should the losses be too high.
- Give access to beam-loss data for inspection in the control room together with status information.
- Keep measured data in a circular buffer for post mortem analysis.
- Provide error reporting.

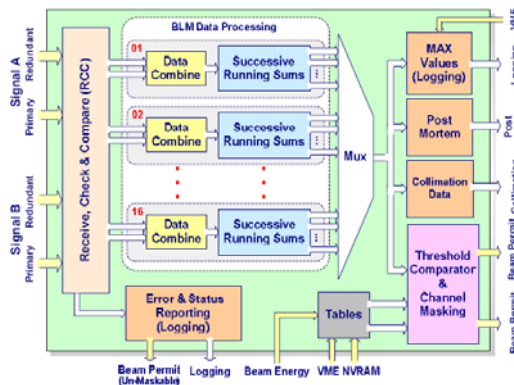


Fig. 37: Algorithms treating the BLM signals

As can be seen from Fig. 32, the threshold levels above which a beam dump must be triggered, depend on the beam energy and the loss duration. For this reason the loss values are integrated using running sums. Twelve integration periods, spanning from 40  $\mu$ s to 84 s are made available.

The calculation of running sums is rather simple. Each incoming value is added to a register, while the oldest value of the interval is subtracted again. Of course all values making up the sum must be kept.

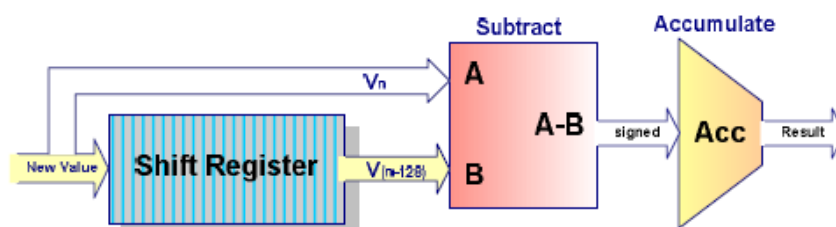


Fig. 38: Calculating running sums

Another way to handle the calculations would be to use a long shift register and always add the difference between the first and the last values.

The longer the integration interval, the longer the shift register must become. This problem can be overcome by using partial sums instead of keeping all previous values. This results in a cascade of shift registers and adders as shown in Fig. 39. In addition, a multi-point shift register is used calculating two running sums at once.

Of course, the latency of the sum output for each running sum depends on the time the previous sum needs for its calculation and therefore increases for longer integration periods. The running sums are compared with threshold values, dependent on the particle energy and a dump trigger is issued if the losses exceed those threshold values.

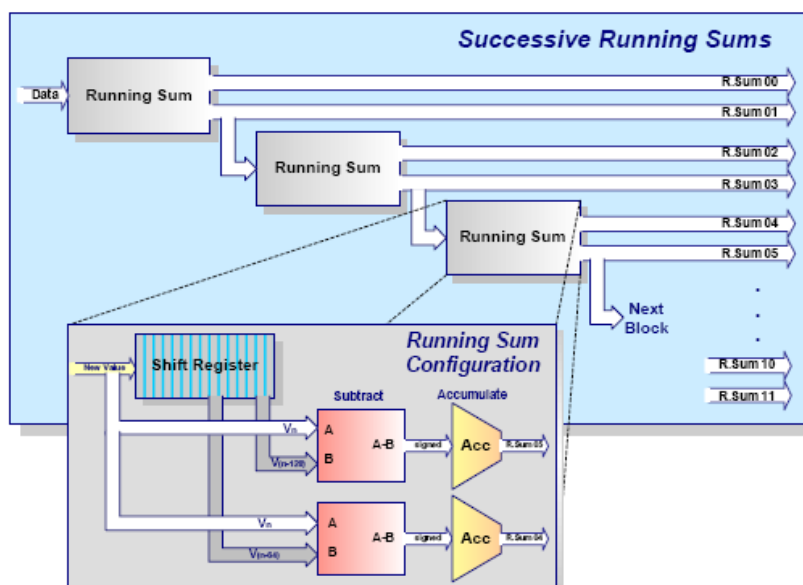


Fig. 39: Cascade of running sums

Apart from triggering beam dumps, the loss values are used for online viewing and logging as well as for post mortem analysis. The values for the last 20 000 turns (40  $\mu$ s samples) as well as the 82 ms summed values of acquired data during the last 45 minutes are available. In addition status information about the functioning of each individual BLM station is transferred from the tunnel to the surface electronics allowing online supervision of the whole system.

Part of the recorded data will be used

- to drive an on-line event display in the control room and
- write an extensive logging database both at a refresh rate of 1 Hz.

Other parts of the same processing units, initiated by external triggers, will provide fast updates of the loss pattern seen. For example:

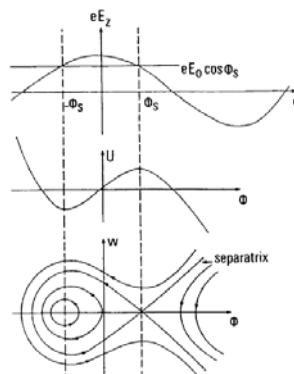
- For the automated collimator adjustments, it will record and provide the last 20 ms by 640  $\mu$ s integrals.
- At every beam injection and scheduled dump, 100 ms worth of data will be pushed to the relevant systems to be used to verify the correctness of those procedures.
- A detailed post mortem analysis study will be possible, in the event of an unforeseen dump, by analysing the last 1.7 s by 40  $\mu$ s integrals stored in the electronics for each channel.

## 5 Phase-space tomography

Up to now we have only looked at digital signal treatment where the calculations were done on the fly and which had to be very fast in order to keep pace with the incoming data flow. However, sometimes it may be enough to collect the raw data and treat them using digital signal processing algorithms only after the acceleration cycle. A typical example for such a system is the measurement of longitudinal phase space distributions using tomography.

### 5.1 Longitudinal phase space

Consider a circular machine with a single RF cavity for acceleration, powered with a sinusoidal accelerating field. Synchronous particles having exactly the correct phase with respect to the RF field will get the pre-determined energy increase while particles coming early will be accelerated less and particles coming late will be accelerated more. This results in a movement in phase space shown in Fig. 40. The longitudinal profile, measured with a wall current monitor, for example, corresponds to a projection of the phase-space distribution onto the  $\Phi$  axis.



**Fig. 40:** Longitudinal phase space



Observing the bunch profile for many turns in the machine corresponds in fact to making ns  $\Phi$  axis ‘rotating’ around the phase-space distribution.

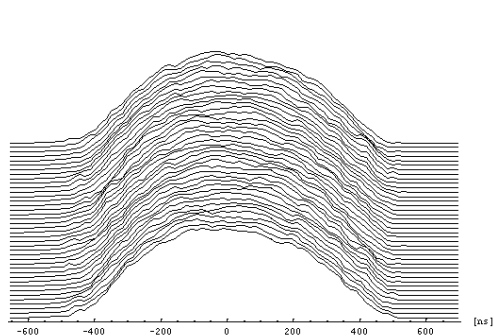


Fig. 41: Bunch profiles

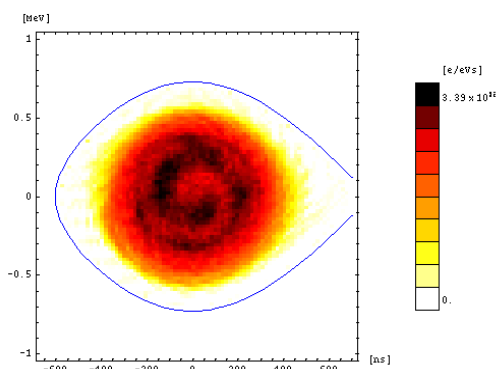


Fig. 42: Reconstructed phase space

Medicine uses similar measurements to visualize three-dimensional structures in the human body. Many X-ray images are produced with an X-ray camera rotating around the patient’s body. The 3-dimension object is re-constructed using Algebraic Reconstruction Techniques (ARTs).

The principle is rather simple (the implementation, however, can be rather complex and requires a lot of computing power): The X-ray image, which is in fact a projection of the three-dimensional object onto the camera axis, is back-projected. This means that the content of a one-dimensional bin is distributed over a two-dimensional array of cells that could have contributed to that bin. A first reconstructed version of the original object is obtained. Projecting this reconstructed object and comparing the result to the projection of the original object yields differences. These differences can again be back-projected yielding an improved reconstruction. Doing this for many images allows the



Fig. 43: CT scanner

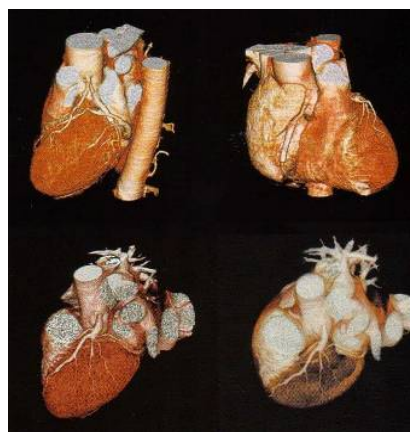
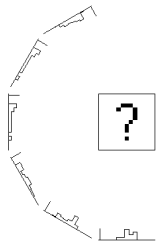


Fig. 44: Results from CT reconstruction

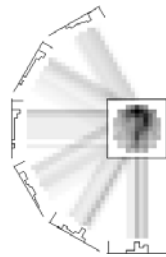
re-construction of the original object.

The method of ART can be applied to the profiles obtained from wall current monitors measuring bunch profiles over many turns. While the individual measurements do not exhibit any detailed phase-space information, the reconstructed phase-space plot displays a wealth of interesting details which cannot be observed otherwise.

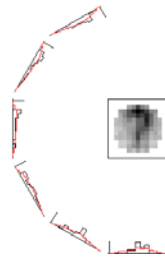




**Fig. 45:** Projection



**Fig. 46:** Back projection



**Fig. 47** Projection of back-projected image



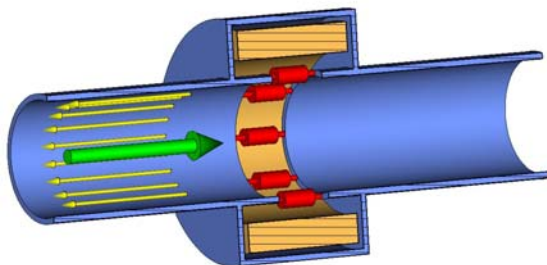
**Fig. 49:** After 50 iterations

## 5.2 Particle tracking

The reconstruction technique explained in the previous section only works as long as the projections are taken with a constant rotation of the viewpoint: the object is rotated in front of the camera always at the same rotation angle, which would correspond to a circular movement in longitudinal phase space. Unfortunately, however, the synchrotron motion of particles represents large non-linearities. These non-linearities are taken into account by tracking particles in a simulated machine in order to build maps describing the evolution in phase space. These maps are taken into account for the reconstruction.

## 5.3 The hardware

When a beam travels through the vacuum pipe, an image current, equal in intensity with the primary beam but travelling in opposite direction, is created. By creating a gap in the vacuum chamber and bridging it with resistors, this image current can be measured. Such a wall current monitor (WCM) can have a very large bandwidth (typically in the GHz range) and the longitudinal shape of the particle bunches can be measured. The WCM signal is amplified and measured with a fast oscilloscope.



**Fig. 49:** The Wall Current Monitor (WCM)

Of course the signal must be measured on a turn-by-turn and bunch-by-bunch basis which requires an oscilloscope trigger synchronous to the revolution frequency. The problem is similar to the one described in the section on trajectory measurements.

A front-end computer is dedicated to the trigger timing while the scope trace data are directly read out by the application program via a dedicated (GPIB) Ethernet link thus improving data transfer speed.

The bunch profiles (see Fig. 41) are used as input to the ART algorithm. In a first version the ART code was implemented in Mathematica™ because of its large mathematical libraries. Later, however, it was implemented in High Performance Fortran-90 which allows parallelization and execution on several processors, further reducing execution time. Many tricks were played like the use of integer arithmetic instead of floating point when this was possible as well as extensive use of tables,

e.g., for the calculation of trigonometric functions. Like this the execution time could be reduced from hours to some 15 to 20 seconds.

## 6 Conclusions

Beam diagnostics is a field spanning a great number of disciplines: Machine physics, analog and digital electronics, and computer science. Quite naturally digital signal processing methods are employed to extract physically meaningful and easily understandable results from the raw signals created with the beam instrumentation sensors. Using a few typical measurement applications as examples, these lectures try to bridge the gap between the methods employed in digital electronics and the beam physics using the power of these methods.

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