



# Large Extra Dimensions and Quantum Black Holes

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# Outline

- ⌘ Motivation

- ⌘ “Large” Extra Dimensions

  - ⌘ Some history is always nice...

  - ⌘ Newtonian gravity and ED (Inverse Square Law Test)

  - ⌘ Models for ED

    - ⌘ Arkani-Hamed, Dimopoulos, Dvali (and others)

    - ⌘ Randall-Sundrum

- ⌘ Black Holes

  - ⌘ Black Holes in astronomy

  - ⌘ Black Holes in accelerators

  - ⌘ Black Holes from cosmic rays

- ⌘ Experimental Bounds on the Planck Scale

- ⌘ Conclusions

# Motivation:

## A quantum theory of gravity?

- ⊗ Two major problems have not been resolved yet:
  - ⊗ The hierarchy problem
  - ⊗ The cosmological constant problem
- ⊗ The existence of new dimensions can help in the resolution of these two conundrums and might (dis)prove the fact that gravity becomes strong at sub-millimeter distances (ADD and RS)
- ⊗ New physics phenomena can be brought to light if we consider that the fundamental Planck scale could be as low as 1TeV for “ $n > 1$ ” (ADD)
- ⊗ If  $M_{Pl} \sim m_{EW}$ , black hole production and evaporation could be observed in collisions of elementary particles

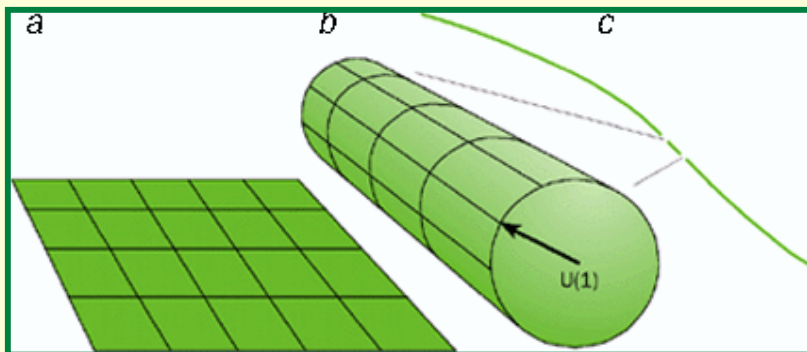


# Large Extra Dimensions

Where are they?

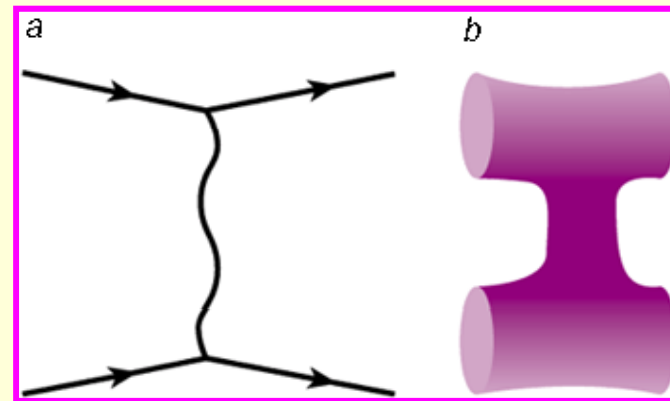
# A bit of history...

- ⌘ Once upon a time (1921), Theodor Kaluza in the hope of unifying gravitation and electromagnetism extended general relativity by including the  $U(1)$  symmetry of electromagnetism by adding a 4th spatial dimension.
- ⌘ In 1926, Oskar Klein proposed that the fourth spatial dimension is curled up (compactified) in a circle of very small radius “ $R$ ”, therefore a particle moving a short distance along that axis would return where it began.



Source: PhysicsWorld

- ⌘ In the 1970's and 1980's there's been renewed interest in (multiple) extra dimensions: SUSY and string theory.
- ⌘ From 1998 onwards, new models have surfaced (ADD, RS, etc.) which address the hierarchy problem by exploiting the geometry of spacetime.



Source: PhysicsWorld

Gravity is automatically included in string theory; there is a vibration mode with the properties of the graviton.

# Extra Dimensions in Newtonian Gravity



The idea is to know how gravity behaves at distances  $< 1\text{mm}$ , does it still abide by the  $r^{-2}$  law or does it change because of the presence of extra compactified dimensions ( $r^{1-D}$ )?

⊖ If the extra dimensions were **non-compact**, they would change the law of gravity away from being  $r^{-2}$  and the equations of motion of Newtonian gravity would not longer predict stable orbits.

$$dl^2 = g_{ij} dx^i dx^j = dr^2 + r^2 d\Omega_{D-1}$$

$$\nabla^2 \Phi = \partial_i (\sqrt{g} g^{ij} \partial_j \Phi) \sim \partial_r (r^{D-1} \partial_r \Phi)$$

$$\nabla^2 \Phi = 0 \Rightarrow F = -m \partial_r \Phi \sim \frac{G_D}{r^{D-1}}$$

⊖ If the extra dimensions were **compact**, the force law would still remain as the inverse square law and we could set a lower bound on the Planck Scale.

$$dl^2 = g_{ij} dx^i dx^j$$

$$dl^2 = dr^2 + r^2 d\Omega_{D-2} + R^2 d\alpha^2$$

$$\sqrt{g} \sim R r^{D-2}$$

$$F \sim \frac{G_D}{2\pi R r^{D-2}} = \frac{G_{\hat{D}}}{r^{\hat{D}-1}}$$

$$\hat{D} \equiv D-1, \quad G_{\hat{D}} \equiv \frac{G_D}{2\pi R}$$



# Eöt-Wash Experiment: Sub-mm Tests of Inverse Square Law (ISL)

2006

Yukawa addition

$$V(r) = -G \frac{m_1 m_2}{r} \left[ 1 + \alpha e^{-r/\lambda} \right]$$

$r \geq R$  : experimentally relevant

$\alpha = 8n/3$  : dimensionless strength parameter

$\lambda$  : length scale

Maximum size of ED ( $r_1 \gg r_{i=2, \dots, n}$ )  
EDs are compactified in a torus

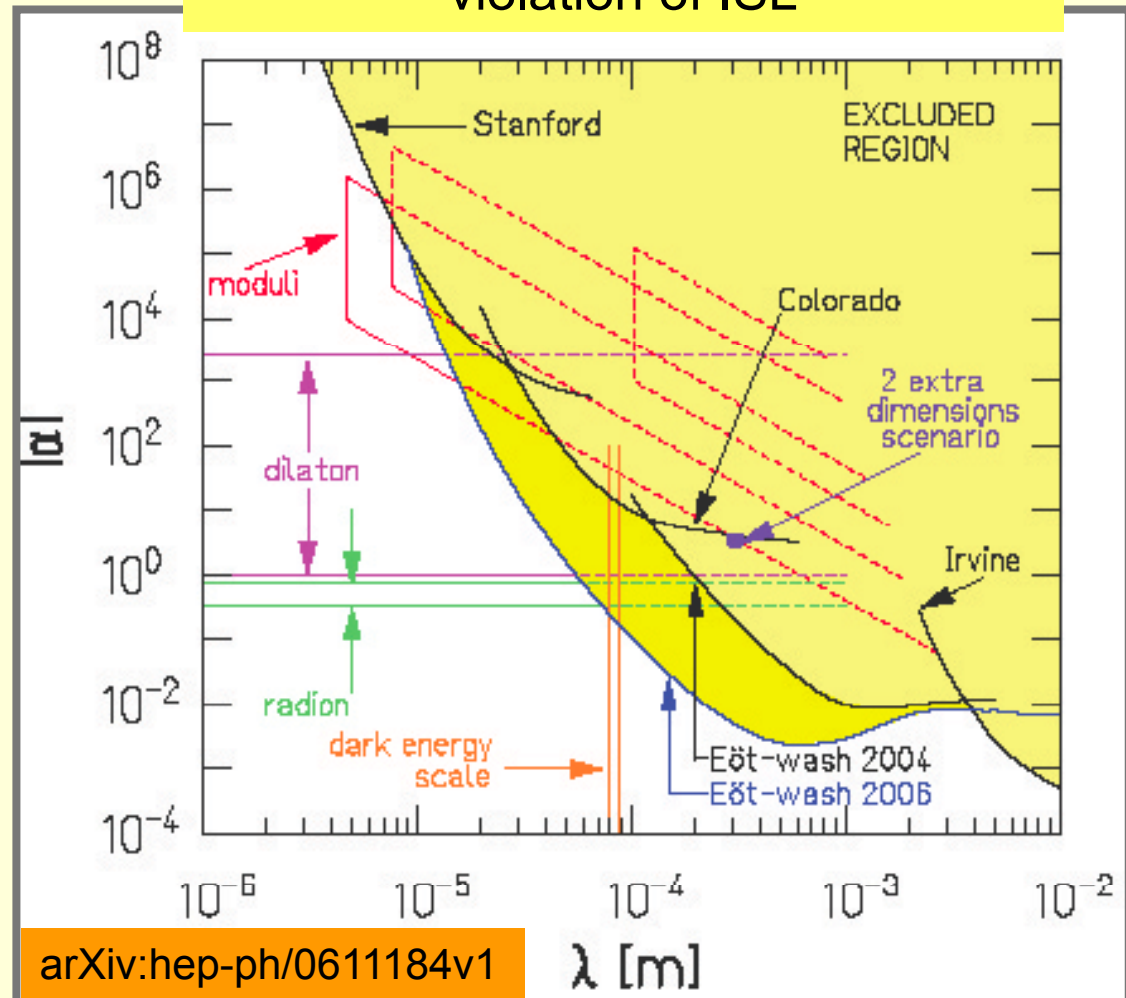
Any  $|\alpha| \leq 1$  must have  $\lambda \leq 56 \mu\text{m}$

Largest ED:

$$n=1, R \leq 44 \mu\text{m}$$

$$M_{D(n=2)} \geq 3.2 \text{ TeV}/c^2$$

95% C.L. constraints on Yukawa violation of ISL

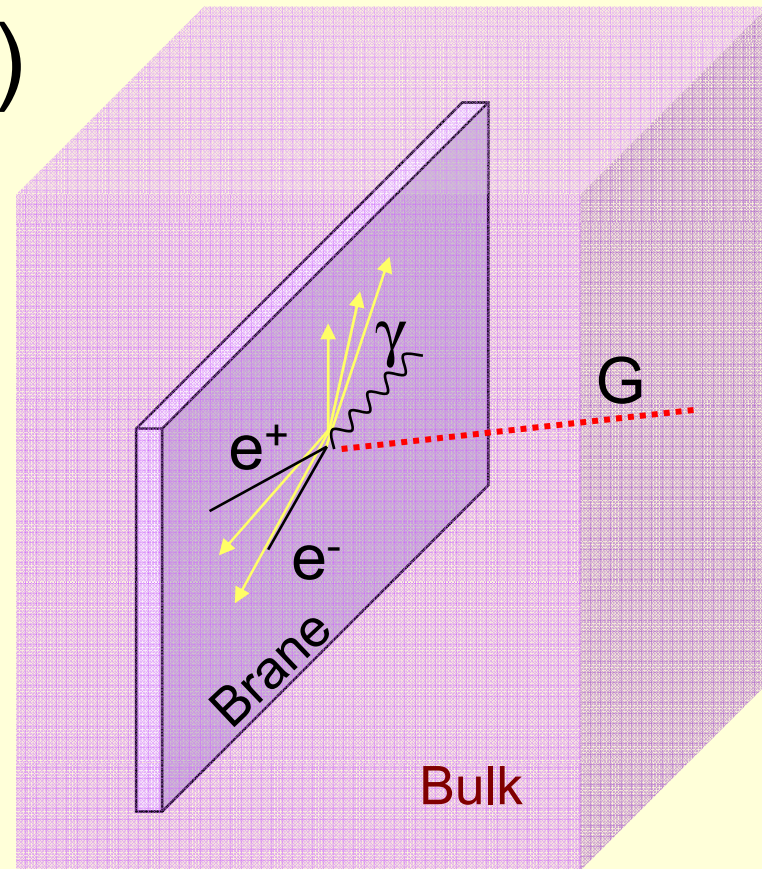


arXiv:hep-ph/0611184v1

$\lambda$  [m]

# The New Models for ED: Arkani-Hamed Dimopoulos-Dvali (ADD)

- ⊖ We live in a **3+1** dimensional subspace called a 3-brane embedded in a **D=(3+n+1)** dimensional spacetime: the “**bulk.**”
- ⊖ The “n” dimensions transverse to the 3-brane have a common size R.
- ⊖ Depending on theory : only gravity and other non-SM fields propagate in the full (4+n)-dimensional spacetime; all SM fields are confined to a 3-brane extended in the non-compact dimensions.
- ⊖ Assume that gravity is unmodified over the 33 orders of magnitude between 1cm down to the Planck length  $\sim 10^{-33}$  cm. **What are the “supposed” effects on Newtonian gravity?**



$$V(r) = \frac{1}{M_{Pl}^2} \frac{m_1 m_2}{r} \Rightarrow \frac{1}{M_{Pl(3+n)}^{(n+2)}} \frac{m_1 m_2}{r^{n+1}} \text{ for } r \ll R$$

$$V(r) = \frac{1}{M_{Pl}^2} \frac{m_1 m_2}{r} \Rightarrow \frac{m_1 m_2}{M_{Pl(3+n)}^{(n+2)} R^n} \frac{1}{r} \text{ for } r \gg R$$

$$G_N = \frac{1}{(M_{PL(4+n)})^2} \equiv 1/M_D^2$$

$$M_D \sim 1 \text{TeV}$$

$$M_D^2 = M_{Pl(4+n)}^{2+n} R^n$$



# ADD (II)

Physics Letters B 429 (1998) 263-272  
 Physics Letters B 436 (1998) 257-263  
 Physics Letters B 441 (1998) 96-104

- Assuming  $M_{\text{Pl}(4+n)} \sim m_{\text{EW}}$ , with  $m_{\text{EW}}$  being the only short distance scale in theory, and following the gravitational potential given by Gauss' law in  $(4+n)$  dimensions we obtain that the size of the extra dimensions is:

$$R \sim 10^{\frac{30}{n}-17} \text{ cm} \times \left( \frac{1 \text{ TeV}}{m_{\text{EW}}} \right)^{1+\frac{2}{n}}$$

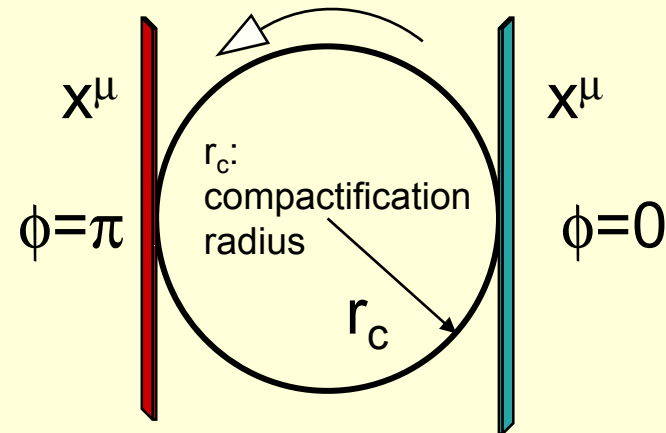
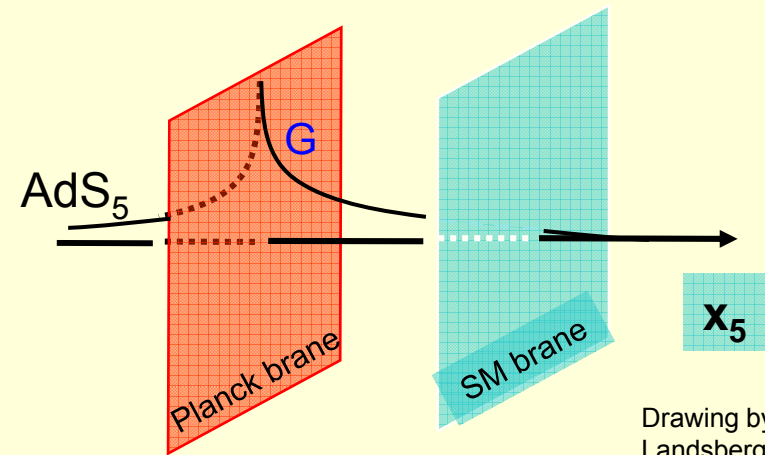
Radius of Compactified Dimensions

Number of ED

- For  $n=1$   $R \sim 10^{13}$  cm: deviations of Newtonian gravity over solar system distances; empirically excluded.
- For  $n>2$ , gravity modified noticeable at distances smaller than currently probed experimentally.
- For  $n=2$  ( $R \sim 100 \mu\text{m} - 1 \text{ mm}$ ) rather  $R < 44 \mu\text{m}$ ; experimental evidence is within our reach.
- A  $(4+n)$  dimensional graviton and other non SM fields will propagate into the bulk.
- SM fields remain localized\* within the thickness of the 3-brane.

# The New Models for ED: Randall-Sundrum (RS)

- Though ADD eliminates the hierarchy problem between  $M_{Pl}$  and  $m_{EW}$ , it introduces a new hierarchy between  $m_{EW}$  and the compactification scale  $\mu_c \sim 1/R$ .
- RS propose a **non-factorizable** 4D-metric multiplied by a “warp” factor  $e^{-2kr_c\phi}$ , which changes rapidly as a function of an additional dimension.
- This metric is a solution to Einstein’s equations with two 3-branes.
- Coupling constant of an individual KK excitation to matter or other gravitational modes is set by  $m_{EW}$ .
- Properties of this model determined by the mass of the graviton and the ratio  $k/M_{Pl}$ .



$$ds^2 = e^{-2kr_c|\phi|} \eta_{\mu\nu} dx^\mu dx^\nu - r_c^2 d\phi^2$$

$$\bar{M}_{Pl} \equiv M_{Pl} / \sqrt{8\pi}$$

Phys. Rev. Lett. **83**, 17 (1999)



# The New Models for ED: Experimental Signatures

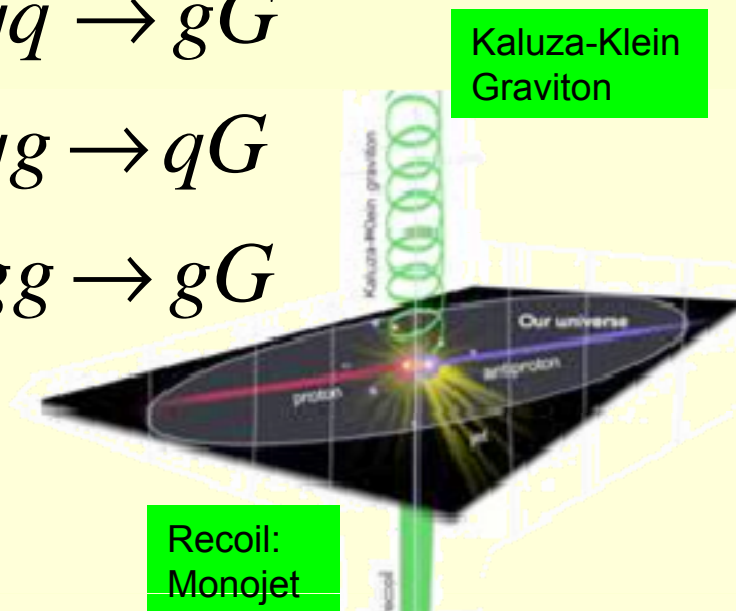


## ADD

$$q\bar{q} \rightarrow gG$$

$$qg \rightarrow qG$$

$$gg \rightarrow gG$$

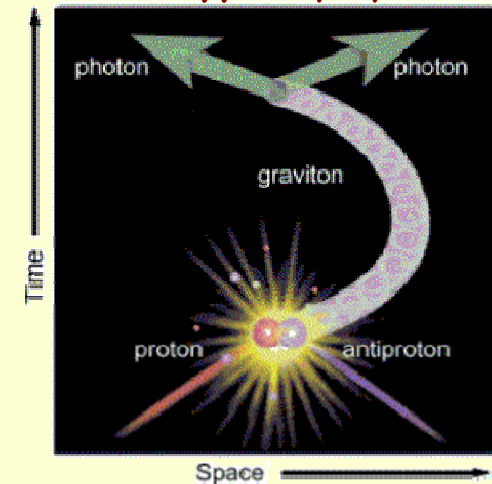


The graviton will be undetected leaving the final state gluon or quark to produce a single jet : jet + missing  $E_T$ .

## RS

⊗ Narrow G (high mass) resonance:

- ⊗ Width of the resonance determined by  $k/M_{Pl}$ ,
- ⊗ Two parameters needed to define the model ( $k$  and  $r_c$ )
- ⊗ Graviton detected when it decays into  $e^+e^-$ ,  $\gamma\gamma$ , or  $\mu^+\mu^-$





# The New Models for ED: Experimental Backgrounds



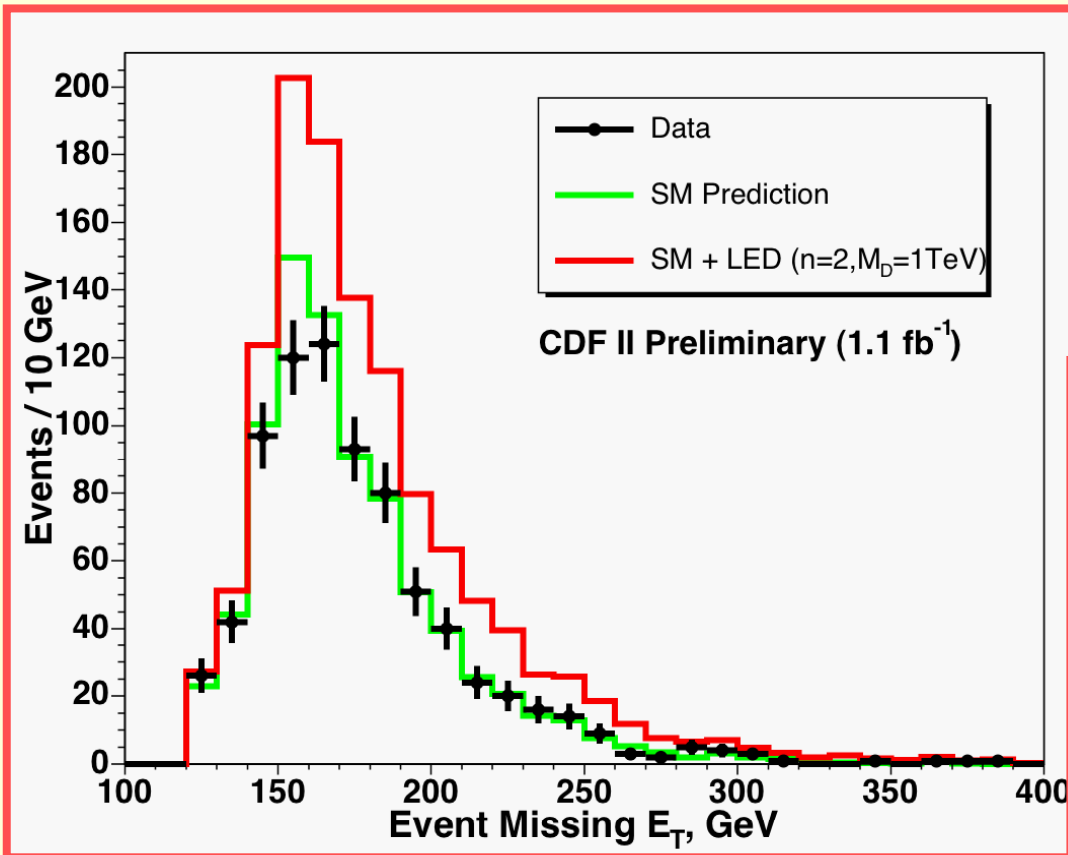
## ADD

- ⊗ The most important backgrounds are:
  - Electroweak:
    - 1-jet +  $Z \rightarrow \nu\nu$  and  $W \rightarrow l\nu$ : where  $l$  is lost
  - QCD:
    - Jets mismeasured: 6% of the total background

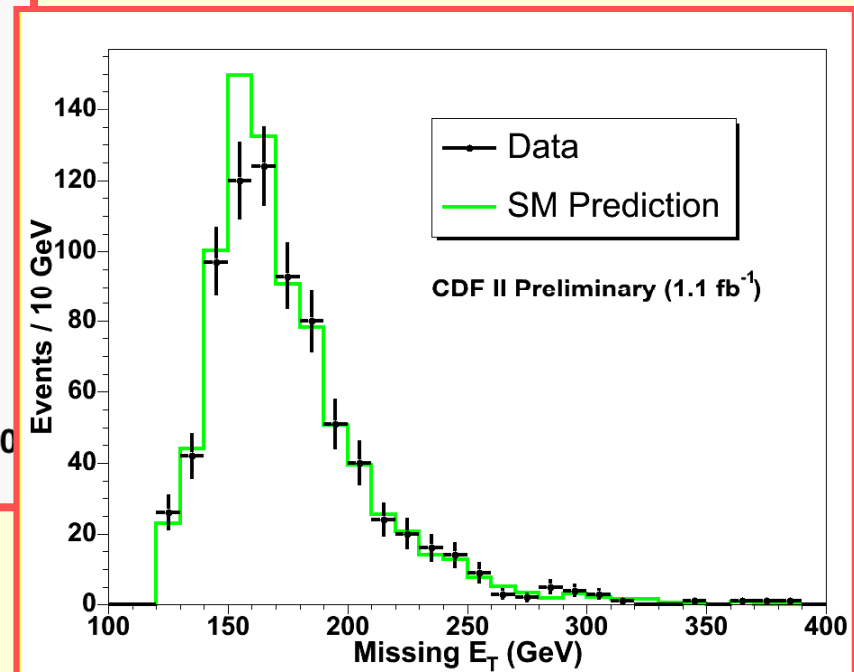
## RS

- ⊗ Based on channel search strategy:
  - Dilepton signal:
    - SM Drell-Yan
    - QCD and W+jets
    - Higher order EW processes
    - $W+\gamma$  and  $\gamma\gamma$  (for dielectron channel)
    - Cosmic rays (for dimuon channel)
  - Diphoton signal:
    - SM diphoton production
    - Single  $\gamma$  + jet faking  $\gamma$  ( $\pi^0$ )

# The New Models for ED: Experimental Limits on Monojet Search - ADD



Comparison of event missing  $E_T$  with SM distribution.



Comparison of the event missing  $E_T$  distribution in candidate sample with hypothetical signal from SM + LED.

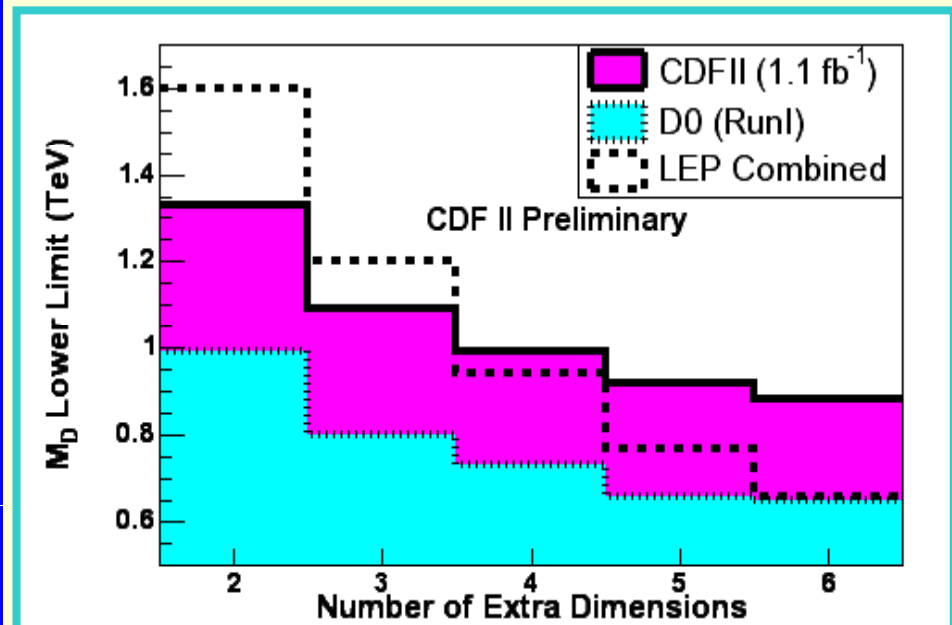
# The New Models for ED: Experimental Limits on Monojet Search - ADD



95%CL Limits on  $M_D$  for Run II in TeV for  $n=2-6$  compared with limits from Run I.

Limit comparison on number of EDs for LEP, DØ-Run I and CDFII.

$n$	$M_D$ (TeV/ $c^2$ ) 368 pb $^{-1}$	$M_D$ (TeV/ $c^2$ ) 1.1 fb $^{-1}$	R(mm) 368 pb $^{-1}$	R(mm) 1.1 fb $^{-1}$
2	1.16	1.33	0.36	0.27
3	0.98	1.09	$3.7 \times 10^{-6}$	$3.1 \times 10^{-6}$
4	0.90	0.99	$1.1 \times 10^{-8}$	$9.9 \times 10^{-9}$
5	0.85	0.92	$3.5 \times 10^{-10}$	$3.2 \times 10^{-10}$
6	0.83	0.88	$3.4 \times 10^{-11}$	$3.1 \times 10^{-11}$

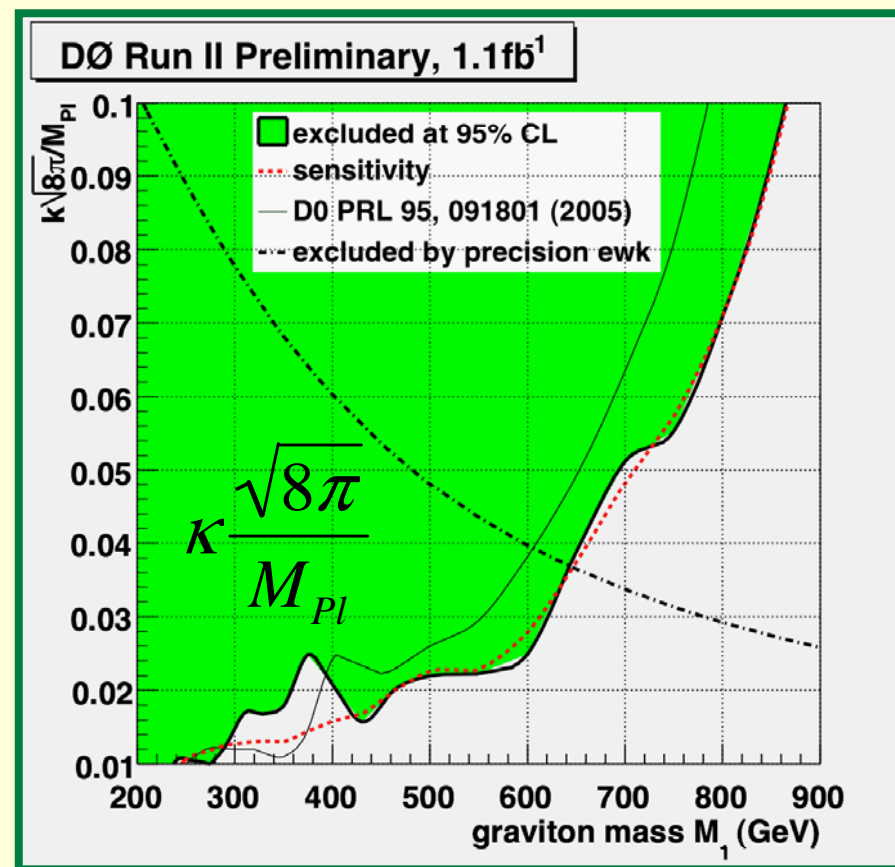
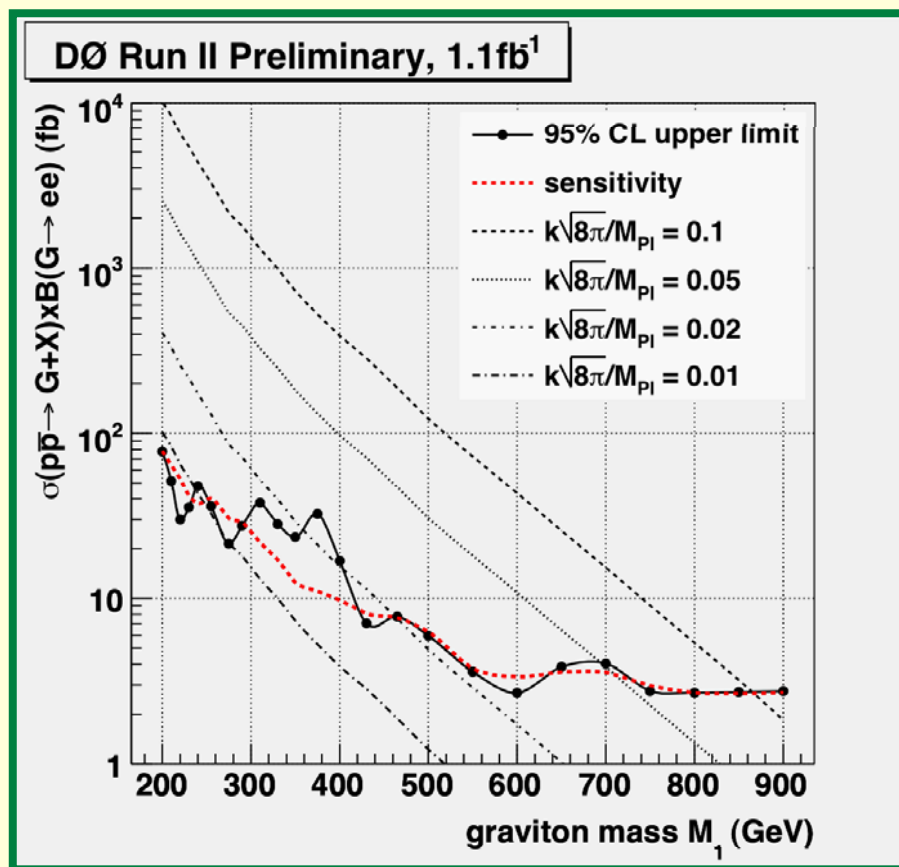




# The New Models for ED: Experimental Limits on Diphoton/Dielectron Search - RS

95% Confidence Level Upper Limit with assumed fixed K-factor=1.34

DØnote 5195-CONF

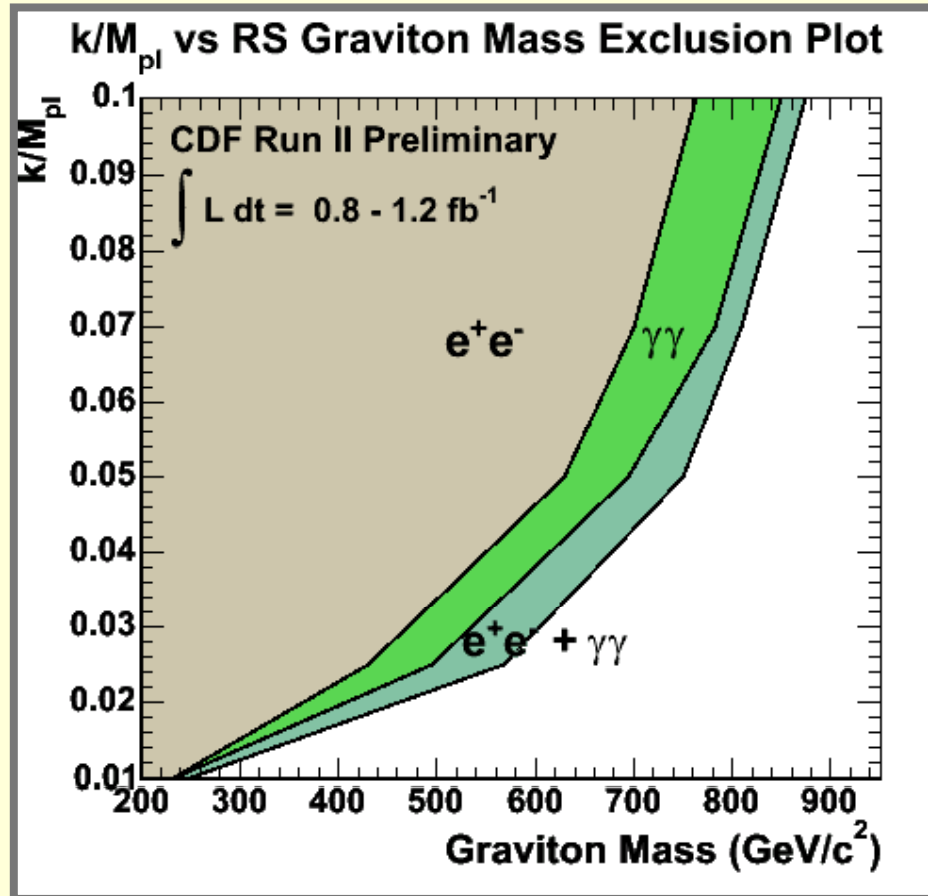
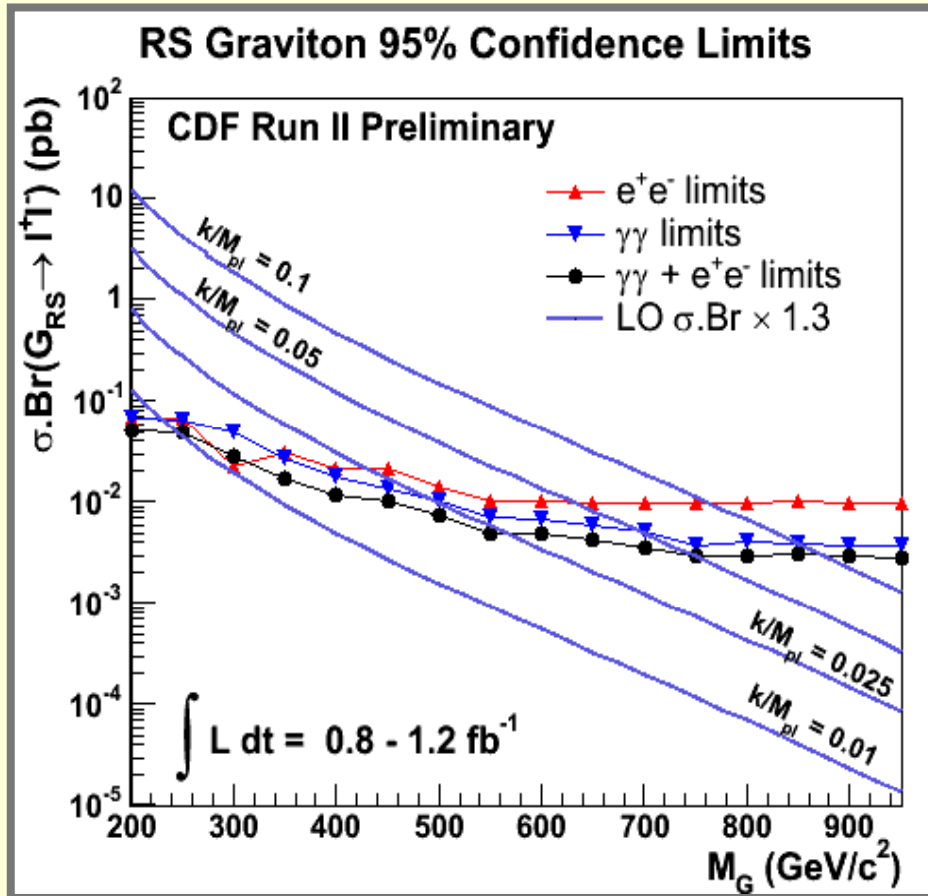


$$\sigma(p\bar{p} \rightarrow G + X) \times B(G \rightarrow e^+ e^-)$$

$$M_1 < 865 \text{ GeV for } \kappa\sqrt{8\pi}/M_{Pl} = 0.1$$

$$M_1 < 240 \text{ GeV for } \kappa\sqrt{8\pi}/M_{Pl} = 0.01$$

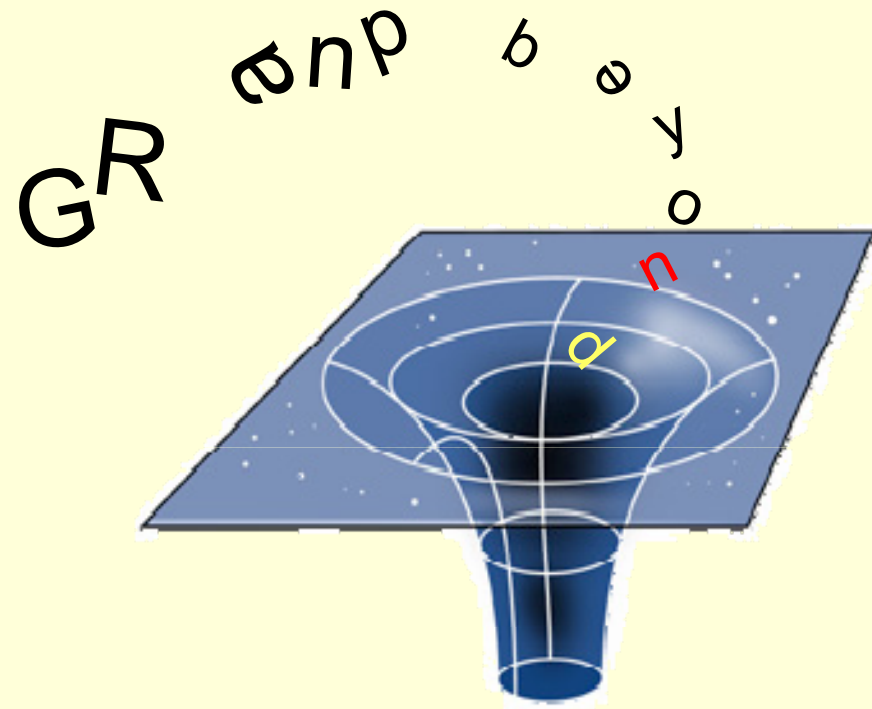
# The New Models for ED: Experimental Limits on Diphoton/Dielectron Search - RS



The combination of both dilepton and diphoton RS Graviton decay channels increases the exclusion region to masses below 875 (244)  $\text{GeV}/c^2$  for  $k/M_{pl}=0.1$  (0.01).



# Black Holes



# Astrophysical Black Holes (I)

- ⊗ Direct prediction of Einstein's General Relativity
- ⊗ BHs are described exactly by the **Kerr** metric with the **Schwarzschild** metric as a special case (set  $a=0$ )

$$ds^2 = \frac{(\Delta - a^2 \sin^2 \theta)}{\rho^2} c^2 dt^2 + \frac{4GMa}{c\rho^2} r \sin^2 \theta d\phi dt - \frac{\rho^2}{\Delta} dr^2 - \rho^2 d\theta^2 - A \frac{\sin^2 \theta}{\rho^2} d\phi^2$$

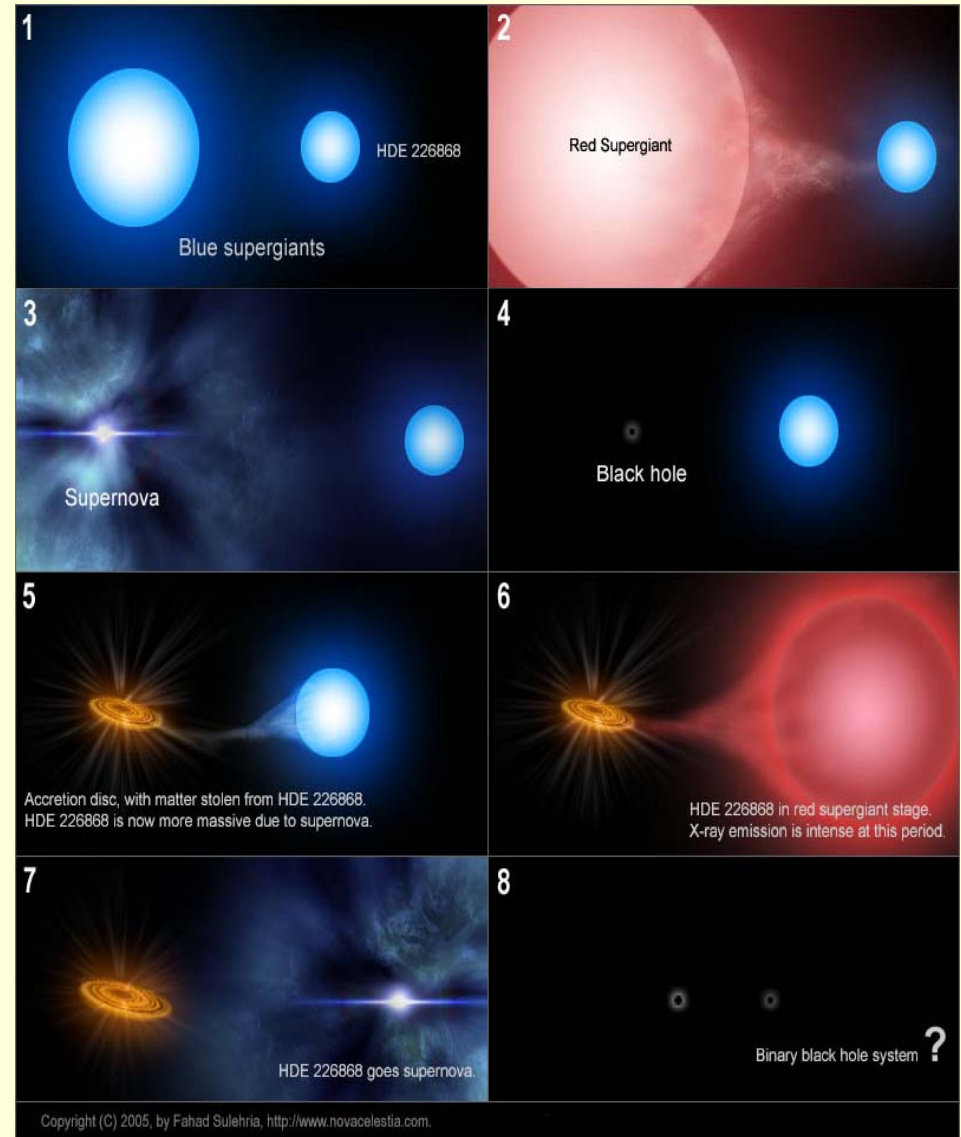
$$\Delta = r^2 - \frac{2GM}{c^2} r + a^2$$

$$\rho^2 = r^2 + a^2 \cos^2 \theta$$

$$A = (r^2 + a^2)^2 - a^2 \Delta \sin^2 \theta$$

- ⊗ The existence of a BH is proven when a horizon is found
  1. Binary star systems or double neutron star binary system
  2. Stellar mass black holes
  3. Super massive BHs located at the center of galaxies

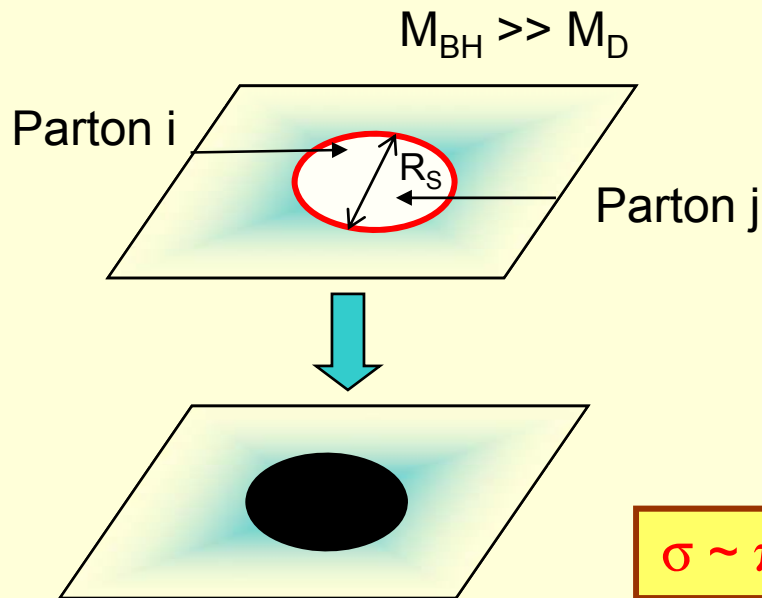
# Astrophysical Black Holes (II)



# Particle Collider Black Holes (I)

Phys. Lett. B 441, 96 (1998)

⊗ Formation: By semi-classical arguments if the impact parameter of a head-on collision between two partons is less than the Schwarzschild radius  $R_S$  corresponding to the center-of-mass energy  $\sqrt{s}$ , then a black hole with mass  $M_{BH}$  is formed.



$$\sigma(M_{BH}) \approx \pi R_S^2 = \frac{1}{M_D^2} \left[ \frac{M_{BH}}{M_D} \frac{8\Gamma\left(\frac{n+3}{2}\right)}{n+2} \right]^{\frac{2}{n+1}}$$

$$R_S(M_{BH}) = \frac{1}{\sqrt{\pi} M_D} \left[ \frac{M_{BH}}{M_D} \frac{8\Gamma\left(\frac{n+3}{2}\right)}{n+2} \right]^{\frac{1}{n+1}}$$

$$\sigma \sim \pi R_S^2 \sim 1 \text{ TeV}^{-2} \sim 10^{-38} \text{ m}^2 \sim 100 \text{ pb}$$

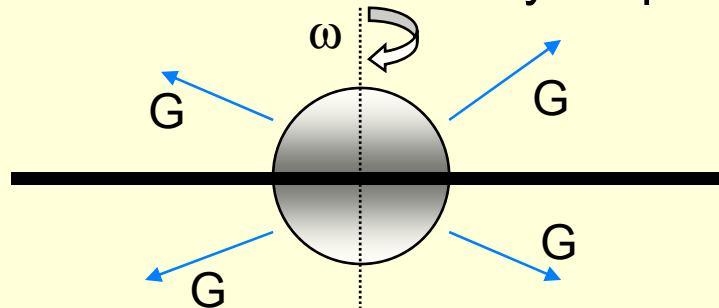
# Particle Collider Black Holes (II)

⊗ BHs evaporate semi-classically in a time  $\tau \sim 10^{-27}$  sec ( $\tau$  is estimated using Stefan's law of thermal radiation)

## ⊗ Evaporation:

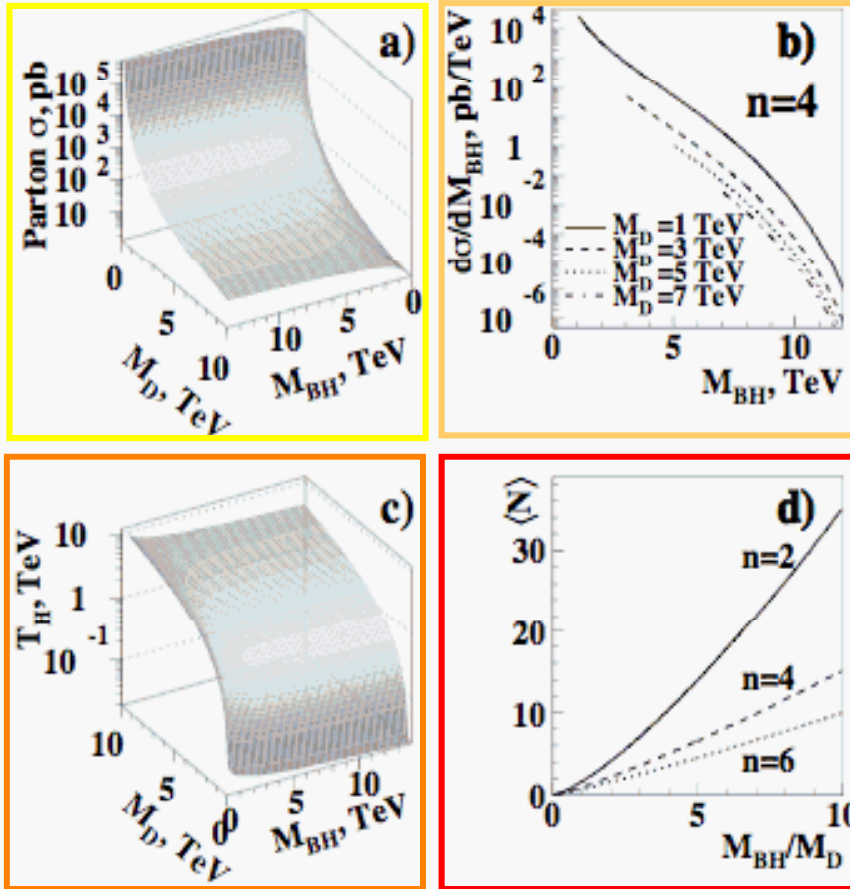
- Balding Phase: BH sheds the hair associated with multipole momenta by emitting gauge radiation (SM fields in the brane and G in the bulk) until it reaches the Kerr solution for a spinning BH (15%)
- Spin-down: BH loses residual angular momentum and becomes a Schwarzschild BH.
- Hawking evaporation “ends”\* when the mass of the BH approaches  $M_D$  via emission of black-body radiation with a characteristic Hawking temperature -  $T_H$ . [semi-classical argument breaks down and a new theory of quantum gravity is needed]

$$T_H = \frac{n+1}{4\pi R_S}$$



# BHs @ The LHC

Phys. Rev. Lett. **87**, 161602 (2001)



- a) Parton-level production cross section
- b) Differential production cross section
- c) Hawking temperature
- d) Average particle multiplicity in BH decays

Parton luminosity approach is used to obtain the production cross section. The sum  $dL/dM_{BH}$  is over all types of initial partons.

$$\frac{d\sigma(pp \rightarrow BH + X)}{dM_{BH}} = \frac{dL}{dM_{BH}} \hat{\sigma}(ab \rightarrow BH) \Big|_{\hat{s}=M_{BH}^2}$$

$$\frac{dL}{dM_{BH}} = \frac{2M_{BH}}{s} \sum_{a,b} \int_{M_{BH}^2/s}^1 \frac{dx_a}{x_a} f_a(x_a) f_b\left(\frac{M_{BH}^2}{sx_a}\right)$$

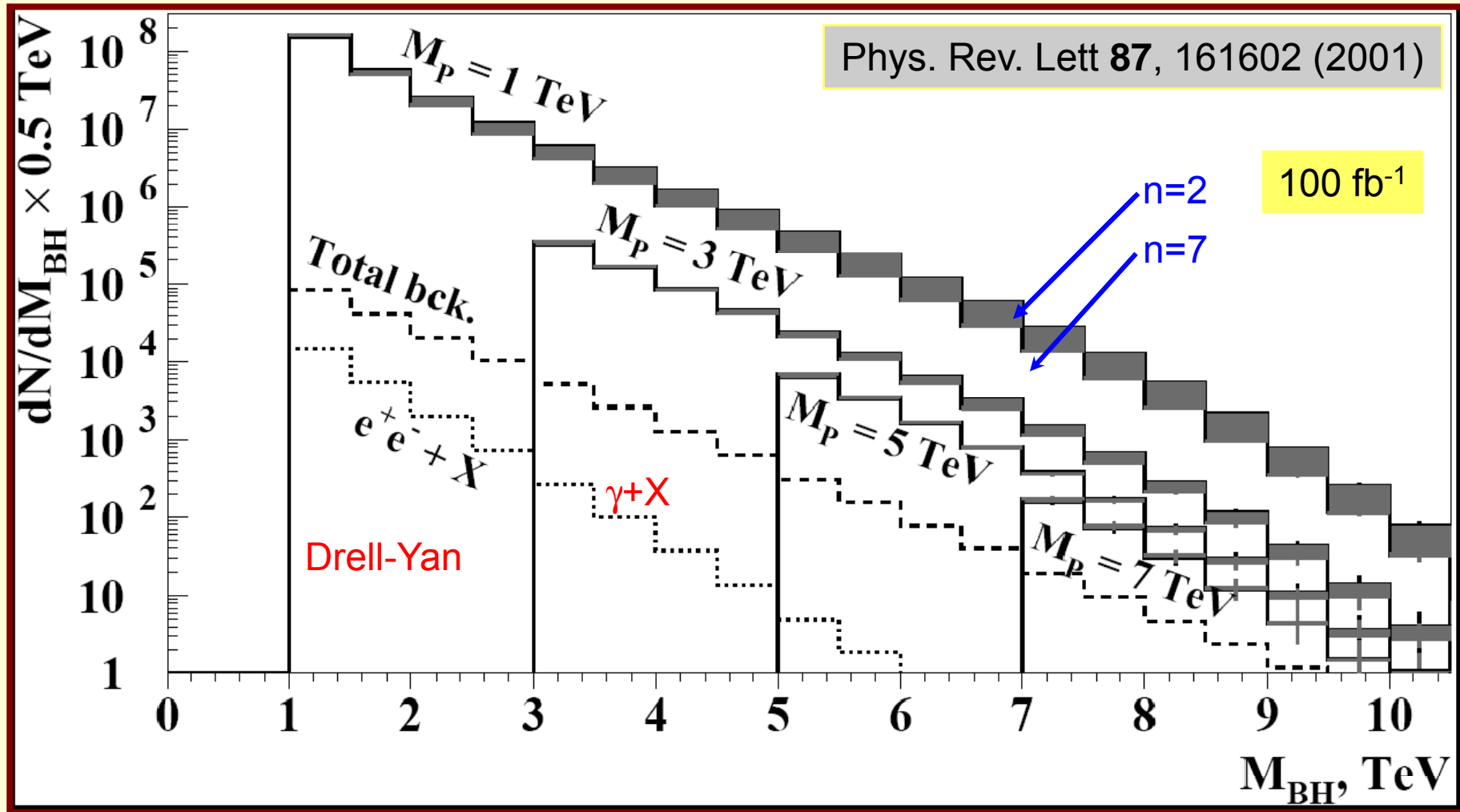
Valid up to  $\sim 100\text{TeV}$  (VLHC)

$$T_H = M_{Pl} \left( \frac{M_{Pl}}{M_{BH}} \frac{n+2}{8\Gamma\left(\frac{n+3}{2}\right)} \right)^{1/(n+1)} \quad \frac{n+1}{4\sqrt{\pi}} = \frac{n+1}{4\pi R_S}$$

$$\langle N \rangle \approx \frac{2\sqrt{\pi}}{n+1} \left( \frac{M_{BH}}{M_{Pl}} \right)^{n+2} \left( \frac{8\Gamma\left(\frac{n+3}{2}\right)}{n+2} \right)^{\frac{1}{n+1}}$$

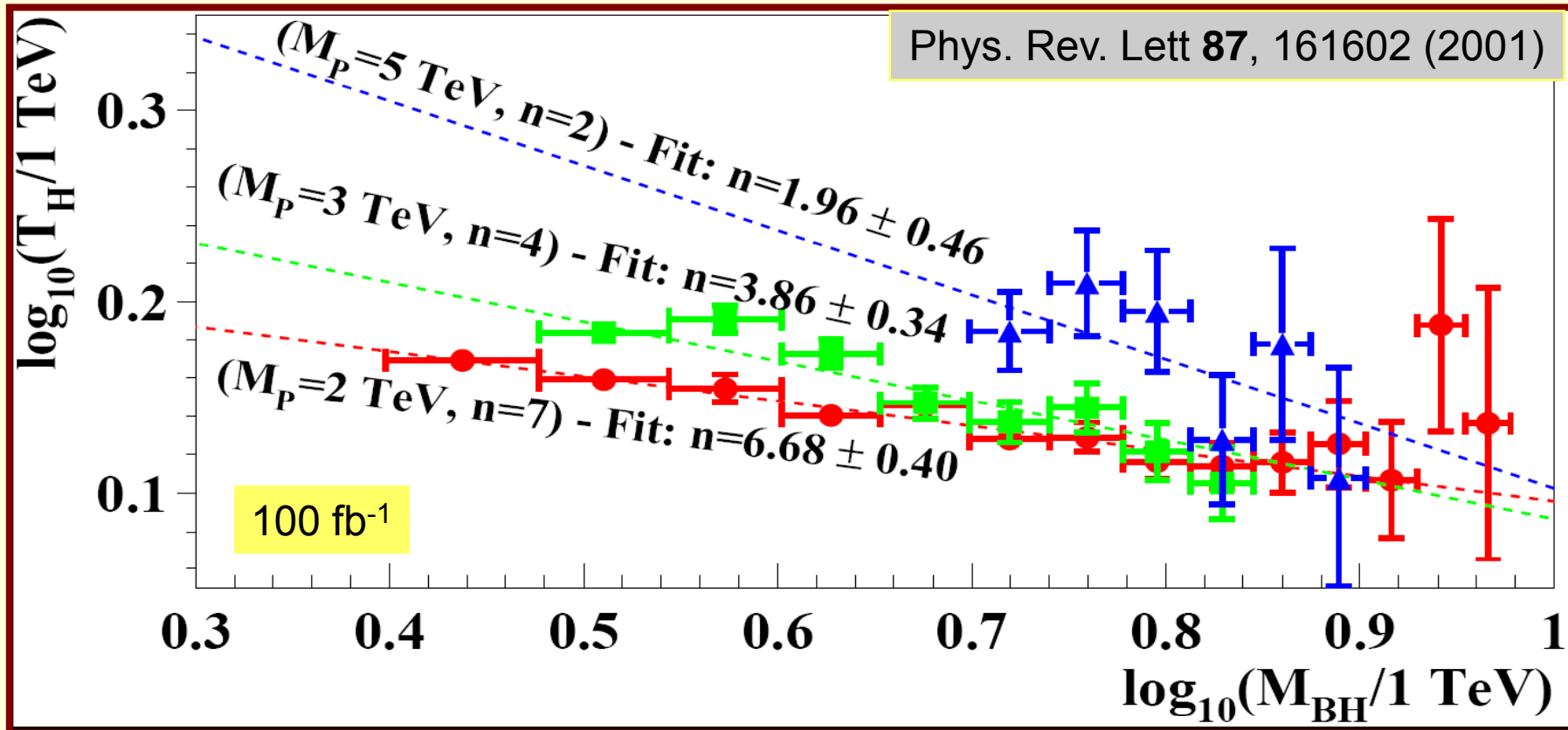
Holds for  $M_{BH} \gg T_H$  ( $N \gg 1$ )

# LHC Potential for BH Creation



Spectrum of BH produced at the LHC with subsequent decay into final states tagged with an electron or a photon

# BHs and ED @ the LHC



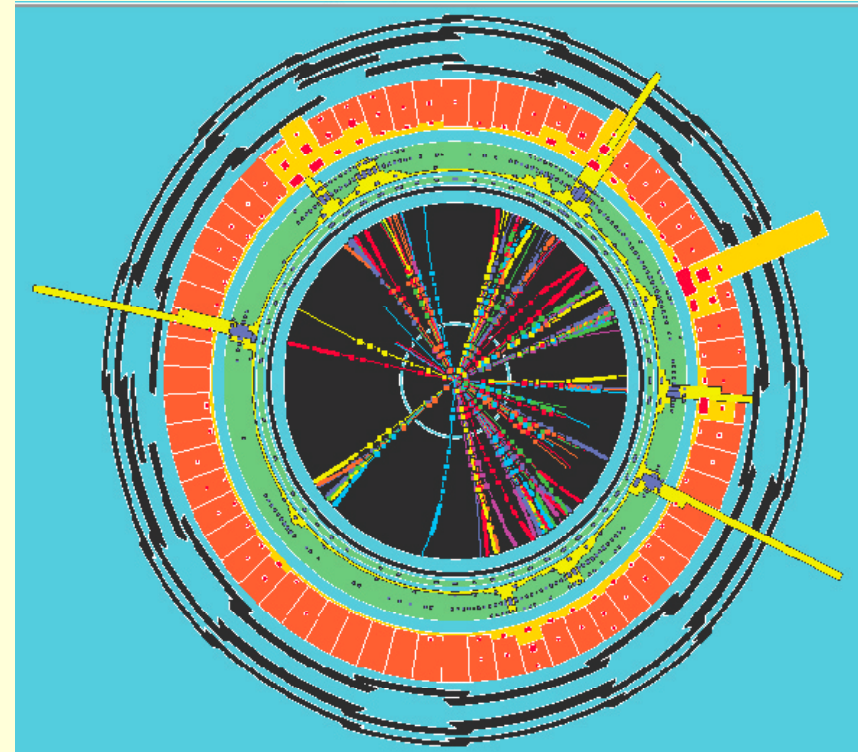
$$\log_{10}(T_H / 1 \text{ TeV}) = -\frac{1}{n+1} \log_{10}(M_{BH} / 1 \text{ TeV}) + \text{const}$$

Slope of straight line fit gives the dimensionality of space



# BHs Signatures & Decay

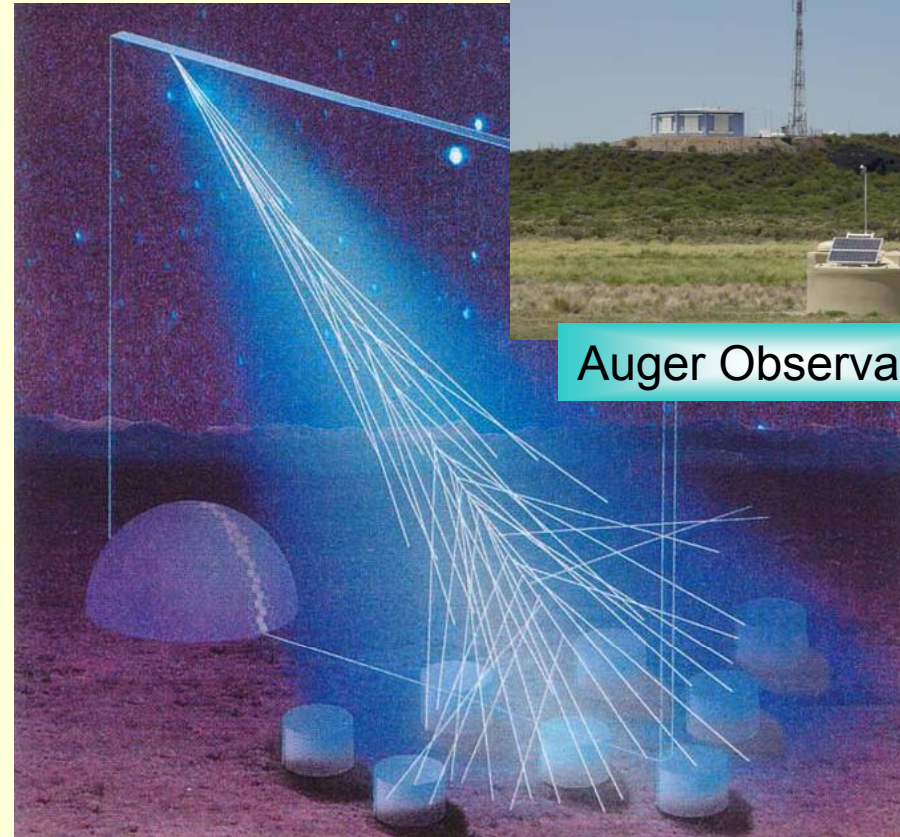
- ⌚ BH decays equally to all modes without a large boost in the lab frame
- ⌚ Hadronic to leptonic activity 5:1 (from the Hawking evaporation phase)
- ⌚ Hadronic to photonic activity 100:1 (from the Hawking evaporation phase)
- ⌚ High multiplicity
- ⌚ High sphericity due to high multiplicity and moderate boost factor in the lab frame  $\langle \gamma\beta \rangle \leq 1$
- ⌚ Visible transverse energy of the order of 1/3 of the total energy
- ⌚ Emission of a few hard visible quanta at the end of the evaporation phase
- ⌚ Suppression of hard perturbative scattering processes



ATLAS - Atlantis Event Display

# Cosmic Rays Black Holes (I)

- ⊗ They occur when ultra-high energy cosmic rays (UHECR) interact with the Earth's atmosphere (e.g., cosmic neutrinos with  $E_\nu > 10^6$  GeV).
- ⊗ BH cross section uses the flat disk approximation and assumes  $M_{\text{BH}} = \sqrt{s}$ .
- ⊗ BH production is not suppressed by perturbative couplings and it is enhanced by the sum over all partons.
- ⊗ Since the interaction length of the neutrinos  $L$ , is  $1.7 \times 10^7$  kmwe ( $\text{pb}/\sigma$ ) is large compared to the Earth's atmospheric depths (0.36 kmwe), they produce black holes uniformly at all atmospheric depths.



Auger Observatory

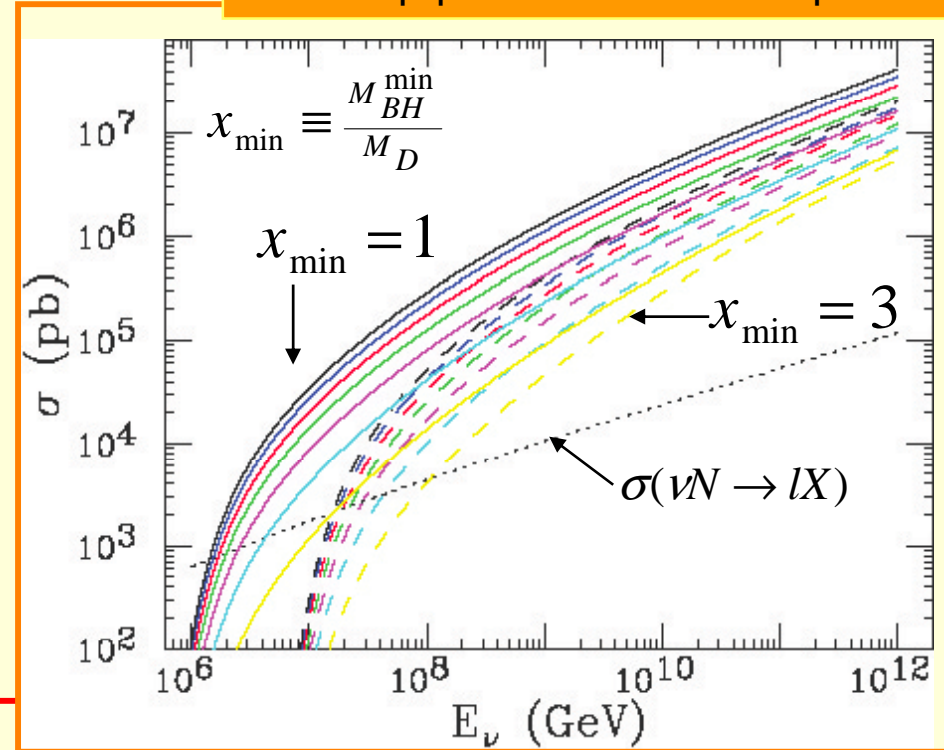
Akeno Giant  
Air Shower  
Array  
(AGASA)



# Cosmic Rays Black Holes (II)

arXiv:hep-ph/0112247 v3 30 Apr 2002

- ⊗ For showers with large enough zenith angles, the likelihood of interaction is maximized and the background from hadronic cosmic rays eliminated.
- ⊗ There is a minimum BH mass for which the cross section is valid,  $x_{\min} \equiv M_{\text{BHmin}}/M_D$



Cross sections for  $n=1, \dots, 7$  from below,  $M_D = 1 \text{ TeV}$ .

$$\sigma(\nu N \rightarrow BH) = \sum_i \int_{(M_{BH}^{\text{Min}})^2/s} dx \hat{\sigma}_i(\sqrt{xs}) f_i(x, Q)$$

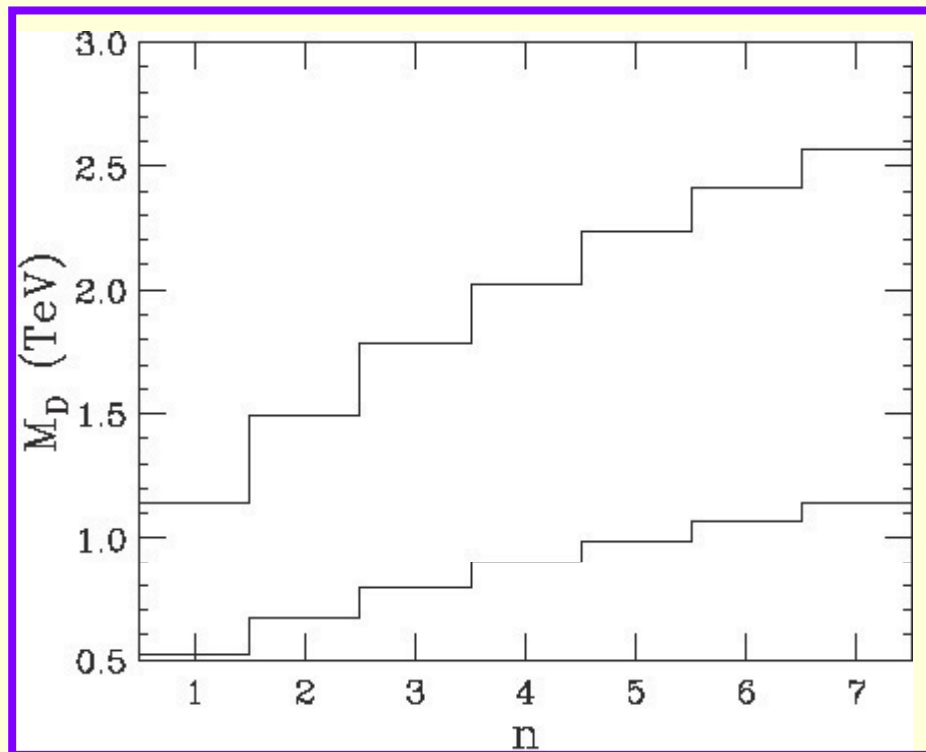
$$s = 2m_N E_\nu$$

The sum is over all partons in the nucleon and the  $f_i$ 's are the parton distribution functions

$$\sigma(\nu N \rightarrow BH) \propto \left[ \frac{1}{M_D^2} \right]^{2+n}$$

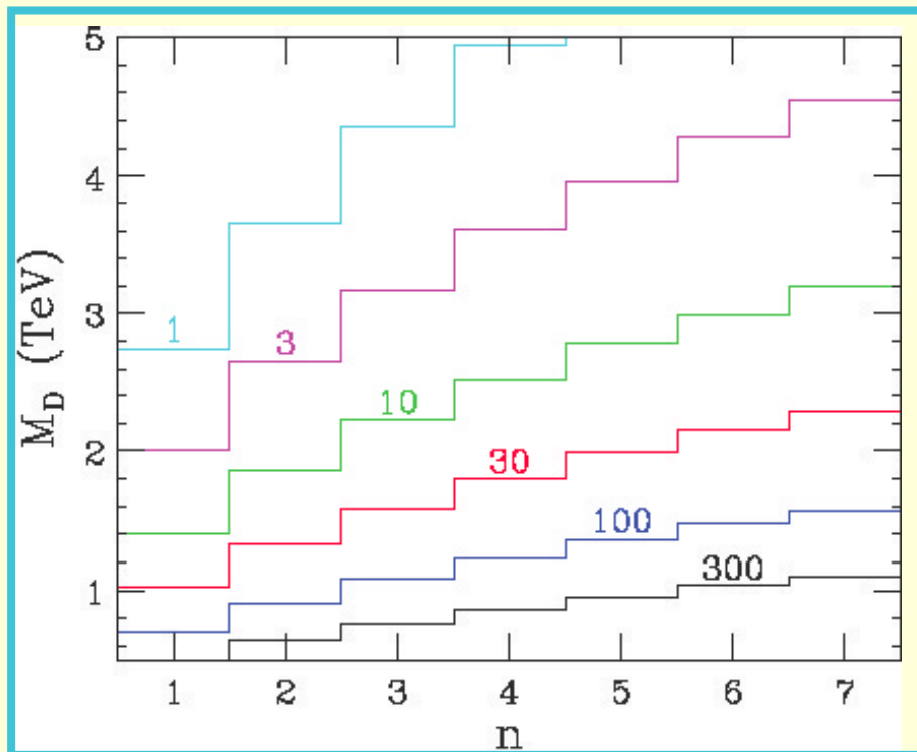
# Cosmic Rays Black Holes (III)

AGASA



95% C.L. upper and lower bounds on  $M_D$  for various  $n$ , given 6 candidate events above a background of 1.72 events in 1710.5 live days ( $x_{\min} = 1$ )

AUGER



No. BHs detected by ground array in 5-Auger site years ( $x_{\min} = 1$ ).

# Experimental Bounds on $M_D$ [TeV] at 95% CL

n	AGASA		AUGER	EOT-WASH	DØ (ADD) [HLZ]	
	xmin=1	xmin=3	xmin=1		DiMuon	DiElectron DiPhoton
2				3.2	1.09	1.67
3					1.27	1.70
4	> 1.3 - 1.5	> 1.0 - 1.1	3.0*		1.07	1.43
5					0.97	1.29
6			2.0		0.90	1.20
7	> 1.6 - 1.8	> 1.1 - 1.3			0.85	1.14
GRW					1.07	1.43
Hewett $\lambda_{\pm} = 1$					0.96/0.93	1.28

n	CDF (ADD)	LEP	LHC (ADD)			ASTROPHYS.
	(K=1.3)	(Avg.)	1 TeV	3 TeV	5 TeV	
2	1.33	1.60	$1 \pm 1\%$	$3 \pm 3.3\%$	$5 \pm 40\%$	> 600 - 1800
3	1.09	1.20	$1 \pm 1\%$	$3 \pm 7.5\%$	$5 \pm 48\%$	> 10 - 100
4	0.99	0.94	$1 \pm 1\%$	$3 \pm 9.5\%$	$5 \pm 54\%$	
5	0.92	0.77	$1 \pm 1\%$	$3 \pm 17\%$	Fit Fails	
6	0.88	0.66	$1 \pm 1\%$	$3 \pm 23\%$		
7			$1 \pm 1\%$	$3 \pm 24\%$		

1. \*For  $n \geq 4$
2. GRW: Giudice-Rattazzi-Wells
3. HLZ: Han-Lykken-Zhang

DØ Note 4336-Conf - FINAL Version 2/25/04  
DØ Note 4349-Conf - Version 2.1 FINAL 3/17/04  
arXiv:hep-ex/0506063 v2 16 Nov 2005

# Summary & Conclusions

- Experimentally consistent lower limits on  $M_{Pl}$  have been set to the 95% C.L.
- Up to the present, no “direct” experimental evidence of the existence of the graviton has been unveiled.
- The number of extra dimensions and their characteristics (compactified or warped) is still undetermined.
- Gravity is either intrinsically weak or is strong but diluted in the extra dimensions.
- If gravity is strong at 1 TeV, extra dimensions could be discovered through black holes from particle colliders or cosmic ray experiments. If not, we go back to the drawing board.



# Back-up Slides

# Other References

- ⌘ Antoniadis I., Journal of Physics: Conf. Series **8** (2005) 112-121
- ⌘ Cavaglia M., arXiv:hep-ph/0210296 v1
- ⌘ Cavaglia M., arXiv:hep-th/0404050 v2
- ⌘ Cavaglia M., Das S. and Maartens R., Class. Quantum Grav. **20** (2003) L205-L212
- ⌘ Giddings S.B. and Thomas S. , Phys. Rev. D **65**, 056010 (2002)
- ⌘ Kiefer C., arXiv:gr-qc/9803049 v2
- ⌘ Harris C.M. et al., JHEP05(2005) 053
- ⌘ Hoyle C. D. et al., Phys. Rev. D **70**, 042004 (2004)
- ⌘ Hawking S. W. , Commun. Math. Phys. **43**, 199-220(1975)
- ⌘ Misner Ch., Thorne K. and Wheeler J.A.: Gravitation. Freeman 1973.
- ⌘ Polchinski J.: String Theory, Vol I: An Introduction to the Bosonic String. Cambridge University Press 1998.
- ⌘ Raine D. and Thomas E. Black Holes: An Introduction. Imperial College Press 2005.





# Eöt-Wash Experiment: Sub-mm Tests of Inverse Square Law (ISL)

2004 Results

Yukawa addition

$$V(r) = -G \frac{m_1 m_2}{r} \left[ 1 + \alpha e^{-r/\lambda} \right]$$

$r \geq R$  : experimentally relevant

$\alpha = 8n/3$  : dimensionless strength parameter

$\lambda = R$  : length scale

Maximum size of ED ( $r_1 \gg r_{i=2, \dots, n}$ )  
EDs are compactified in a torus

Largest ED:

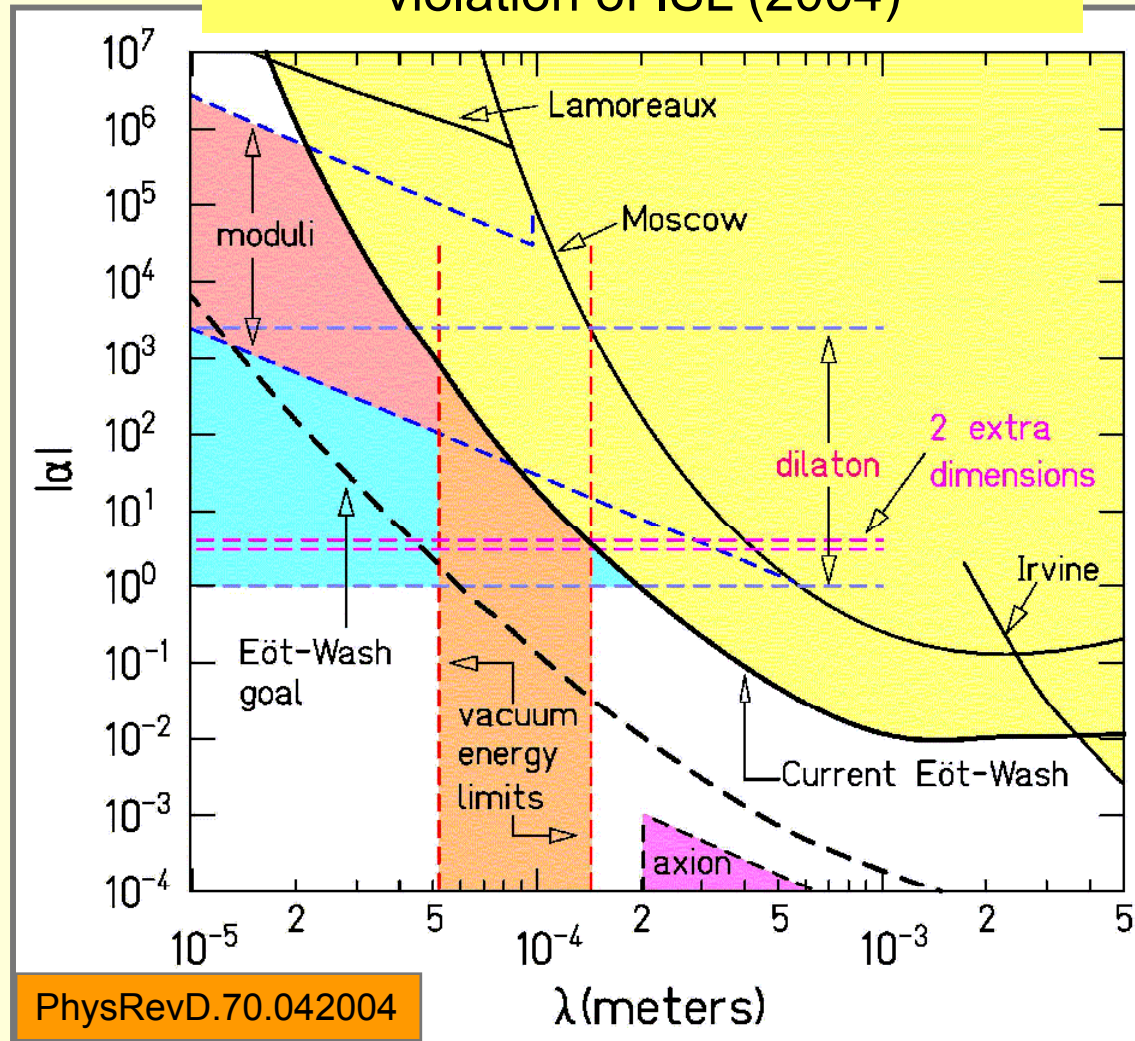
$$n=1, R \leq 160 \mu\text{m}$$

Two EDs:

$$n=2, R \leq 130 \mu\text{m}$$

$$M_D \geq 1.7 \text{ TeV}/c^2$$

95% C.L. constraints on Yukawa violation of ISL (2004)



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