

Experimental Techniques for Low-Temperature Measurements

Cryostat Design, Material
Properties, and Superconductor
Critical-Current Testing

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