PHYSICS POTENTIAL OF SPS UPGRADE IN REGARD TO BETA/EC BEAMS

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Abstract

The goal for future neutrino facilities is the determination of the $[U_{e3}]$ mixing and CP violation in neutrino oscillations. This will require precision experiments with a very intense neutrino source. With this objective the creation of neutrino beams from the radioactive decay of boosted ions by the SPS of CERN from either beta or electron capture transitions has been propossed. We discuss the capabilities of such facilities as a function of the energy of the boost and the baseline for the detector. We conclude that the SPS upgrade to 1000 GeV is crucial to have a better sensitivity to CP violation if it is accompanied by a longer baseline. We compare the physics potential for two different configurations. In the case of beta beams, with the same boost for both β^+ (neutrinos) and β^- (antineutrinos), the two setups are: I) $\gamma = 120$, L = 130 Km (Frejus); II) $\gamma = 330$, $L=650~{\rm Km}$ (Canfranc). In the case of monochromatic EC beams we exploit the energy dependence of neutrino oscillations to separate out the two parameters U(e3) and the CP phase δ . Setup I runs at $\gamma = 90$ and $\gamma = 195$ (maximum achievable at present SPS) to Frejus, whereas Setup II runs at $\gamma = 195$ and $\gamma = 440$ (maximum achievable at upgraded SPS) to Canfranc. The main conclusion is that, whereas the gain in the determination of U(e3) is rather modest, setup II provides much better sensitivity to CP violation.

1. INTRODUCTION

Neutrinos are very elusive particles that are difficult to detect. Even so, physicists have over the last decades successfully studied neutrinos from a wide variety of sources, either natural, such as the sun and cosmic objects, or manmade, such as nuclear power plants or accelerated beams. Spectacular results have been obtained in the last few years for the flavour mixing of neutrinos obtained from atmospheric, solar, reactor and accelerator sources and interpreted in terms of the survival probabilities for the beautiful quantum phenomenon of neutrino oscillations [1, 2]. The weak interaction eigenstates ν_{α} ($\alpha = e, \mu, \tau$) are written in terms of mass eigenstates ν_k (k = 1, 2, 3) as $\nu_{\alpha} = \sum_k U_{\alpha k}(\theta_{12},\theta_{23},\theta_{13};\delta)\nu_k$, where θ_{ij} are the mixing angles among the three neutrino families and δ is the CP violating phase. Neutrino mass differences and the mixings for the atmospheric θ_{23} and solar θ_{12} sectors have thus been determined. The third connecting mixing $|U_{e3}|$ is bounded as $\theta_{13} \leq 10^{\circ}$ from the CHOOZ reactor experiment [3]. The third angle, θ_{13} , as well as the CPviolating phases δ , remain thus undetermined. Besides the approved experiments Double CHOOZ [4], T2K [5] and NOVA [6], a number of experimental facilities to significantly improve on present sensitivity have been discussed in the literature: neutrino factories (neutrino beams from boosted-muon decays) [7, 8, 9], superbeams (very intense conventional neutrino beams) [10, 11, 12, 13] improved reactor experiments [14] and more recently β -beams [15]. The original standard scenario for beta beams with lower $\gamma = 60/100$ and short baseline $L = 130~\mathrm{Km}$ from CERN to Frejus with ${}^{6}He$ and ${}^{18}Ne$ ions could be improved using an electron capture facility for monochromatic neutrino beams [16]. New proposals also include the high Q value 8Li and 8Be isotopes in a $\gamma = 100$ facility [17]. In this paper we discuss the physics reach that a high energy facility for both beta beams [18] and EC beams may provide with the expected SPS upgrade at CERN. In Section 2 we discuss the virtues of the suppressed oscillation channel $(\nu_e \rightarrow \nu_\mu)$ in order to have access to the parameters θ_{13} and δ . The interest of energy dependence, as obtainable in the EC facility, is emphasized. In Section 3 we compare the beta beam capabilities at different energies and baselines using two ions, one for neutrinos, the other for antineutrinos. In Section 4 we present new results on the comparison between (low energies, short baseline) and (high energies, long baseline) configurations for an EC facility with a single ion. Section 5 gives our conclusions and outlook.

2. SUPPRESSED NEUTRINO OSCILLATION

The observation of CP violation needs an experiment in which the emergence of another neutrino flavour is detected rather than the deficiency of the original flavour of the neutrinos. At the same time, the interference needed to generate CP-violating observables can be enhanced if both the atmospheric and solar components have a similar magnitude. This happens in the suppressed $\nu_e \to \nu_\mu$ transition. The appearance probability $P(\nu_e \to \nu_\mu)$ as a function of the distance between source and detector (L) is given by [19]

$$P(\nu_e \to \nu_\mu) \simeq s_{23}^2 \sin^2 2\theta_{13} \sin^2 \left(\frac{\Delta m_{13}^2 L}{4E}\right) + c_{23}^2 \sin^2 2\theta_{12} \sin^2 \left(\frac{\Delta m_{12}^2 L}{4E}\right) + \tilde{J} \cos \left(\delta - \frac{\Delta m_{13}^2 L}{4E}\right) \frac{\Delta m_{12}^2 L}{4E} \sin \left(\frac{\Delta m_{13}^2 L}{4E}\right), \quad (1)$$

where $\tilde{J} \equiv c_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin 2\theta_{13}$. The three terms of Eq. (1) correspond, respectively, to contributions from the atmospheric and solar sectors and their interference. As seen, the CP violating contribution has to include all mixings and neutrino mass differences to become ob-

servable. The four measured parameters $(\Delta m_{12}^2, \theta_{12})$ and $(\Delta m_{23}^2, \theta_{23})$ have been fixed throughout this paper to their mean values [20].

Neutrino oscillation phenomena are energy dependent (see Fig.1) for a fixed distance between source and detector, and the observation of this energy dependence would disentangle the two important parameters: whereas $|U_{e3}|$ gives the strength of the appearance probability, the CP phase acts as a phase-shift in the interference pattern. These properties suggest the consideration of a facility able to study the detailed energy dependence by means of fine tuning of a boosted monochromatic neutrino beam. As shown below, in an electron capture facility the neutrino energy is dictated by the chosen boost of the ion source and the neutrino beam luminosity is concentrated at a single known energy which may be chosen at will for the values in which the sensitivity for the (θ_{13}, δ) parameters is higher. This is in contrast to beams with a continuous spectrum, where the intensity is shared between sensitive and non sensitive regions. Furthermore, the definite energy would help in the control of both the systematics and the detector background. In the beams with a continuous spectrum, the neutrino energy has to be reconstructed in the detector. In water-Cerenkov detectors, this reconstruction is made from supposed quasielastic events by measuring both the energy and direction of the charged lepton. This procedure suffers from non-quasielastic background, from kinematic deviations due to the nuclear Fermi momentum and from dynamical suppression due to exclusion effects [21].

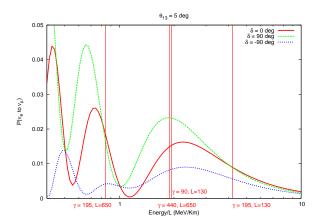


Figure 1: The appearance probability $P(\nu_e \to \nu_\mu)$ for neutrino oscillations as a function of the LAB energy E/L, with fixed connecting mixing. The three curves refer to different values of the CP violating phase δ . The vertical lines are the energies of our simulation study in the EC facility.

From general arguments of CPT invariance and absence of absorptive parts the CP-odd probability is odd in time and then odd in the baseline L (formally). Vacuum oscillations are only a function of E/L so that, at fixed L, the CP-odd probability is odd in the energy (formally). This proves that the study of neutrino oscillations in terms of neutrino energy will be able to separate out the CP phase δ

from the mixing parameters. A control of this energy may be obtained from the choice of the boost in the EC facility with a single ion. In order for this concept to become operational it is necessary to combine it with the recent discovery of nuclei far from the stability line, having super allowed spin-isospin transitions to a giant Gamow-Teller resonance kinematically accessible [22]. Thus the rare-earth nuclei above ^{146}Gd have a small enough half-life for electron capture processes. This is in contrast with the proposal of EC beams with fully stripped long-lived ions [23]. We discuss the option of short-lived ions [16].

3. BETA-BEAM CAPABILITIES AT DIFFERENT ENERGIES AND BASELINES

A first question to be answered is: Is the sensitivity to CP violation and θ_{13} changing with energy at fixed baseline? Fixing the baseline to CERN-Frejus (L=130 Km) [18], one notices that, for $\gamma>80$, the sensitivity to both θ_{13} and δ changes rather slowly because the flux at low energies in the continuous spectrum does not reduce significantly. Then it is not advantageous to increase the neutrino energy unless the baseline is correspondingly scaled to remain close to the atmospheric oscillation maximum as suggested by the E/L dependence.

With the present SPS of CERN the maximum energy reachable for the 6He ion corresponds to $\gamma=150$. Fixing this value of γ for both 6He and ^{18}Ne we may ask: Is the sensitivity to θ_{13} and δ changing with the baseline? Particularly for the CP phase δ , L=300 Km is clearly favoured [18]. There is neither an existing nor an envisaged laboratory at this particular distance from CERN.

Equipped with these previous results, it is of interest to make a comparison between the physics reach for two different Beta Beam Setups. With the same γ for both neutrino and antineutrino sources, Setup I corresponds to $\gamma=120,\ L=130$ Km (Frejus), whereas Setup II is for $\gamma=330,\ L=650$ Km (Canfranc). Setup II needs the upgrade of the SPS until proton energies of 1000 GeV. The associated determinations of θ_{13} and δ are presented in Fig. 2. The main conclusion is that Setup II is clearly better for the CP violating phase. Not only the high energy Setup provides a better precision, but it is able to resolve the degeneracies. In [18] one may find the associated sensitivities of these Setups for each parameter θ_{13} and δ . As a consequence, a R&D effort to design Beta Beams for the upgraded CERN SPS $(E_p=1000$ GeV) appears justified.

4. EC-BEAM CAPABILITIES AT DIFFERENT ENERGIES AND BASELINES

Electron Capture is the process in which an atomic electron is captured by a proton of the nucleus leading to a nuclear state of the same mass number A, replacing the proton by a neutron, and a neutrino. Its probability amplitude is proportional to the atomic wavefunction at the origin, so that it becomes competitive with the nuclear β^+

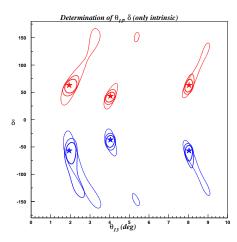


Figure 2: Determination of (θ_{13}, δ) for the Setups I) and II), as explained in the text.

decay at high Z. Kinematically, it is a two body decay of the atomic ion into a nucleus and the neutrino, so that the neutrino energy is well defined and given by the difference between the initial and final atomic masses (Q_{EC}) minus the excitation energy of the final nuclear state. In general, the high proton number Z nuclear beta-plus decay (β^+) and electron-capture (EC) transitions are very "forbidden", i.e., disfavoured, because the energetic window open Q_{β}/Q_{EC} does not contain the important Gamow-Teller strength excitation seen in (p,n) reactions. There are a few cases, however, where the Gamow-Teller resonance can be populated (see Fig.3) having the occasion of a direct study of the "missing" strength. For the rare-earth nuclei above ^{146}Gd , the filling of the intruder level $h_{11/2}$ for protons opens the possibility of a spin-isospin transition to the allowed level $h_{9/2}$ for neutrons, leading to a fast decay. Our studies for neutrino beam preparation have used the ^{150}Dy ion with half live of 7.2 min, a Branching Ratio to neutrino channels of 64% (fully by EC) and neutrino energy of 1.4 MeV in the C.M. frame as obtained from its decay to the single giant Gamow-Teller resonance in the daugther $^{150}Tb^*$. A neutrino (of energy E_0) that emerges from radioactive decay in an accelerator will be boosted in energy. At the experiment, the measured energy distribution as a function of angle (θ) and Lorentz gamma (γ) of the ion at the moment of decay can be expressed as $E = E_0/[\gamma(1-\beta\cos\theta)]$. The angle θ in the formula expresses the deviation between the actual neutrino detection and the ideal detector position in the prolongation of one of the long straight sections of the Decay Ring. The neutrinos are concentrated inside a narrow cone around the forward direction. If the ions are kept in the decay ring longer than the half-life, the energy distribution of the Neutrino Flux arriving to the detector in absence of neutrino oscillations is given by the Master Formula

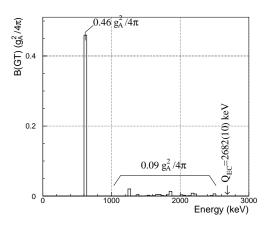


Figure 3: Gamow-Teller strength distribution in the EC/β^+ decay of ^{148}Dy .

$$\frac{d^2 N_{\nu}}{dS dE} = \frac{1}{\Gamma} \frac{d^2 \Gamma_{\nu}}{dS dE} N_{ions}$$

$$\simeq \frac{\Gamma_{\nu}}{\Gamma} \frac{N_{ions}}{\pi L^2} \gamma^2 \delta(E - 2\gamma E_0), \qquad (2)$$

with a dilation factor $\gamma >> 1$. It is remarkable that the result is given only in terms of the branching ratio and the neutrino energy and independent of nuclear models. In Eq. (2), N_{ions} is the total number of ions decaying to neutrinos. For an optimum choice with $E \sim L$ around the first oscillation maximum, Eq. (2) says that lower neutrino energies E_0 in the proper frame give higher neutrino fluxes. The number of events will increase with higher neutrino energies as the cross section increases with energy. To conclude, in the forward direction the neutrino energy is fixed by the boost $E=2\gamma E_0$, with the entire neutrino flux concentrated at this energy. As a result, such a facility will measure the neutrino oscillation parameters by changing the γ 's of the decay ring (energy dependent measurement) and there is no need of energy reconstruction in the detector.

For the study of the physics reach associated with such a facility, we combine two different energies for the same ^{150}Dy ion using two Setups. In all cases we consider 10^{18} decaying ions/year, a water Cerenkov Detector with fiducial mass of 440 Kton and both appearance (ν_{μ}) and disappearance (ν_{e}) events. Setup I is associated with a five year run at $\gamma=90$ (close to the minimum energy to avoid atmospheric neutrino background) plus a five year run at $\gamma=195$ (the maximum energy achievable at present SPS), with a baseline L=130 Km from CERN to Frejus. The results for Setup I are going to be compared with those for Setup II, associated with a five year run at $\gamma=195$ plus a five year run at $\gamma=440$ (the maximum achievable at the upgraded SPS with Proton energy of $1000~{\rm GeV}$), with a baseline $L=650~{\rm Km}$ from CERN to Canfranc.

For the Setup I we generate the statistical distribution of events from assumed values of θ_{13} and δ . The corresponding fit is shown in Fig. 4 for selected values of θ_{13} from 6^o

to 1° and covering a few values of the CP phase δ . As observed, the principle of an energy dependent measurement (illustrated here with two energies) is working to separate out the two parameters. With this configuration the precision obtainable for the mixing (even at 1 degree) is much better than that for the CP phase.

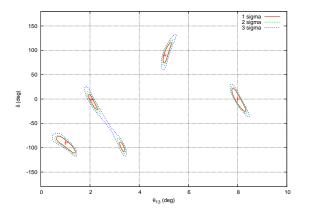


Figure 4: Setup I. Fit for (θ_{13}, δ) from statistical distribution.

The corresponding exclusion plots which define the sensitivity to discover a non-vanishing mixing $\theta_{13} \neq 0$ and CP violation $\delta \neq 0$ are presented in Fig. 5 and Fig. 6 for varying confidence levels. For 99% CL the sensitivity to a non-vanishing mixing is tipically around 1 degree. The corresponding sensitivity (99% CL) to see CP violation becomes significant for $\theta_{13} > 4^o$ with values of the phase δ around 30^o to be distinguished from zero.

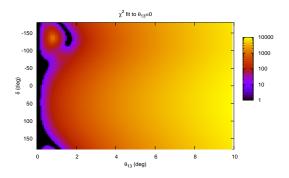


Figure 5: Setup I. θ_{13} sensitivity.

In the case of Setup II the longer baseline for $\gamma=195$ leads to a value of E/L well inside the second oscillation. In that case the associated strip in the (θ_{13}, δ) plane has a more pronounced curvature, so that the two parameters can be better disantangled. The statistical distribution generated for some assumed values of (θ_{13}, δ) has been fitted and the χ^2 values obtained. The results are given in Fig. 7. Qualitatively, one notices that the precision in the mixing is somewhat (but no much) better than that in Setup I. On the contrary, the precision reachable for the CP phase is much

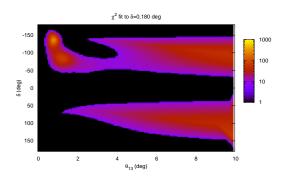


Figure 6: Setup I. CPV sensitivity.

better than that for Setup I. One should emphasize that this improvement in the CP phase has been obtained with the neutrino channel only, using two appropriate different energies.

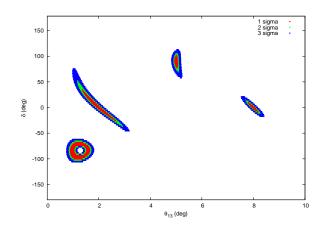


Figure 7: Setup II. Fit for (θ_{13}, δ) from statistical distribution.

The corresponding exclusion plots which define the sensitivities to discover a non-vanishing mixing $\theta_{13} \neq 0$ and CP violation $\delta \neq 0$ are presented in Fig. 8 and Fig. 9 for varying confidence levels. For 99% CL the sensitivity to a non-vanishing mixing is, as before, significant up to around 1 degree. The corresponding sensitivity (99% CL) to see CP violation for $\theta_{13} > 4^o$ becomes now significant with values of the phase δ around 20^o to be distinguished from zero.

At the time of the operation of this proposed Facility in Setup II it could happen that the connecting mixing θ_{13} is already known from the approved experiments for second generation neutrino oscillations, like Double CHOOZ, T2K and NOVA. To illustrate the gain obtainable in the sensitivity to discover CP violation from the previous knowledge of θ_{13} we present in Fig. 10 the expected sensitivity with the distribution of events depending on a single parameter δ for a fixed known value of θ_{13} . The result is impressive: even for a mixing angle of one degree, the CP violation

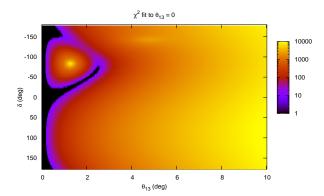


Figure 8: Setup II. θ_{13} sensitivity.

Figure 10: Setup II. CPV sensitivity for the statistical distribution depending on a single parameter δ , assuming previous information on θ_{13} .

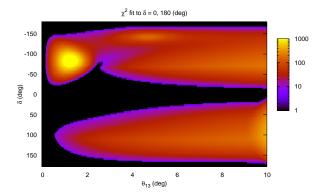


Figure 9: Setup II. CPV sensitivity for the statistical distribution depending on two parameters (θ_{13} and δ).

sensitivity at 99.7% CL reaches values around 10^{o} .

5. CONCLUSIONS AND OUTLOOK

The simulations of the physics output for both Beta and EC beams indicate:

- 1) The upgrade to higher energy ($E_p=1000~{\rm GeV}$) is crucial to have a better sensitivity to CP violation, which is the main objective of the next generation neutrino oscillation experiments, iff accompanied by a longer baseline.
- 2) The best E/L in order to have a higher sensitivity to the mixing U(e3) is not the same than that for the CP phase. Like the phase-shifts, the presence of δ is easier to observe when the energy of the neutrino beams enters into the region of the second oscillation. The mixing is better seen around the first oscillation maximum, instead.

In particular, Setup II in EC beams, i.e., with $\gamma's$ between 195 and 440 and a baseline L=650 Km (Canfranc), has an impressive sensitivity to CP violation, reaching precisions around 20^o , for 99% CL, or better (if some knowledge on the value of θ_{13} is already established).

Besides the feasibility studies for the machine, most important for physics is the study of the optimal configuration by combining low energy with high energy neutrino beams, short baseline with long baseline and/or EC monochromatic neutrinos with $^6He~\beta^-$ antineutrinos.

Among the possible systematics associated with the proposed experiments one should define a program to determine independently the relevant cross sections of electron and muon neutrinos and antineutrinos with water in the relevant energy region from several hundreds of MeV's to 1 GeV or so.

The result of the synergy of Neutrino Physics with Nuclear Physics (EURISOL) and LHC Physics (SPS upgrade) for the Facility at CERN could be completed with the synergy with Astroparticle Physics for the Detector, which could be common to neutrino oscillation studies with terrestrial beams, atmospheric neutrinos (sensitive to the neutrino mass hierarchy through matter effects [24]), Supernova neutrinos and Proton decay.

The analysis shown in this paper shows that the proposals discussed here merit R&D studies in the immediate future for all their ingredients: Facility, Detector and Physics.

REFERENCES

- [1] Y. Fukuda et al., Phys. Rev. Lett. 81 (1998) 1562.
- [2] Q. R. Ahmad *et al.*, Phys. Rev. Lett. **89** (2002) 011301 and 011302.
- [3] M. Apollonio et al., Phys. Lett. B 466 (1999) 415.
- [4] Double-Chooz, Th. Lasserre, Nucl. Phys. Proc. Suppl. 149 (2005) 163, [hep-ex/0409060].
- [5] T2K Collaboration, K. Kaneyuki, Nucl. Phys. Proc. Suppl. 145 (2005) 178-181.
- [6] D. S. Ayres et al. [NOvA Collaboration], [hep-ex/0503053].
- [7] S. Geer, Phys. Rev. **D57** (1998) 6989 [hep-ex/0210192]
- [8] A. De Rújula, M.B. Gavela and P. Hernández, Nucl. Phys. B547 (1999) 21 [hep-ex/0210192].

- [9] For the extensive literature see for example the reviews M. Apollonio, et al, [hep-ex/0210192]; J. J. Gómez-Cadenas and D. A. Harris, Ann. Rev. Nucl. Part. Sci. 52 (2002) 253 and the annual proceedings of the International Nufact Workshop.
- [10] Y. Itow et al, Nucl. Phys. Proc. Suppl. 111 (2002) 146, [hep-ex/0106019].
- [11] A. Para and M. Szleper, [hep-ex/0110032]; D. Ayres *et al*, [hep-ex/0210005]; I. Ambats *et al*. [NOvA Collaboration], FERMILAB-PROPOSAL-0929
- [12] B. Autin et al, CERN/PS 2002-012.
- [13] H. Minakata and H. Nunokawa, Phys. Lett. B 495 (2000) 369 [arXiv:hep-ph/0004114]. J. J. Gómez-Cadenas et al. [CERN working group on Super Beams Collaboration], [hep-ph/0105297]. H. Minakata and H. Nunokawa, JHEP 0110 (2001) 001, [hep-ph/0108085]. P. Huber, M. Lindner and W. Winter, Nucl. Phys. B 645 (2002) 3 [hep-ph/0204352]. G. Barenboim et al., [hep-ex/0206025].
- [14] V. Martemianov et al, Phys. Atom. Nucl. 66 (2003) 1934-1939; Yad.Fiz. 66 (2003) 1982-1987 [hep-ex/0211070]; H. Minakata et al, Phys. Rev. D 68 (2003) 033017 [Erratumibid. D 70 (2004) 059901] [hep-ph/0211111]. Phys. Lett. B 580 (2004) 216 [hep-ph/0309323]. P. Huber, M. Lindner, T. Schwetz and W. Winter, Nucl. Phys. B 665 (2003) 487 [hep-ph/0303232]. F. Ardellier et al., [hep-ex/0405032].
- [15] P. Zucchelli, Phys. Lett. **B532** (2002) 166.
- [16] J. Bernabeu *et al.*, JHEP **0512** (2005) 014, [hep-ph/0505054].
- [17] C. Rubbia, A. Ferrari, Y. Kadi and V. Vlachoudis, Nucl. Instrum. Meth. A 568, 475 (2006), [hep-ph/0602032].
- [18] J. Burguet-Castell, D. Casper, E. Couce, J. J. Gomez-Cadenas and P. Hernandez, Nucl. Phys. B 725, 306 (2005), [hep-ph/0503021].
- [19] A. Cervera et al., Nucl. Phys. B 579 (2000) 17; Erratum-ibid B 593 (2001) 731.
- [20] M. C. Gonzalez-Garcia, Global Analysis of Neutrino, in Nobel Symposium 2004: Neutrino Physics, Haga Slott, Enkoping, Sweden, 19-24 Aug 2004, [hep-ph/0410030].
- [21] J. Bernabeu, Nucl. Phys. B 49 (1972) 186.
- [22] A. Algora et al., Phys. Rev. C 70 (2004) 064301.
- [23] J. Sato, Phys. Rev. Lett. **95** 131804 (2005), [hep-ph/0503144].
- [24] M. C. Banuls, G. Barenboim and J. Bernabeu, Phys. Lett. B 513, 391 (2001) [arXiv:hep-ph/0102184]; J. Bernabeu, S. Palomares-Ruiz, A. Perez and S. T. Petcov, Phys. Lett. B 531, 90 (2002); J. Bernabeu, S. Palomares Ruiz and S. T. Petcov, Nucl. Phys. B 669, 255 (2003).