

Are Magnus Bruaset Aslak Tveito (Eds.)

Numerical Solution of Partial Differential Equations on Parallel Computers

With 201 Figures and 42 Tables

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