Analysis and Design Considerations for High

Performance Caches

by

Helen H. Ruan

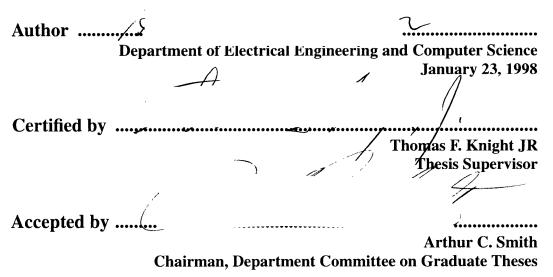
Submitted to the Department of Electrical Engineering and Computer Science in Partial Fulfillment of the Requirements for the Degrees of Bachelor of Science in Electrical Engineering and Master of Engineering in Electrical Engineering and Computer Science

at the

MASSACHUSETTS INSTITUTE OF TECHNOLOGY January 1998

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Abstract

Memory access is the major bottleneck of today's high-performance microprocessors. This thesis provides a systematic and quantitative analysis of the performance trade-offs of major cache (fast memory) topologies. It allows early insight into these trade-offs because performance and costs are controlled by circuit and layout level issues which are difficult to evaluate at initial stages in a design. The thesis establishes a common reference frame that incorporates many implementation possibilities. Within this frame, objective comparisons are made to observe the behavior of caches of various sizes and bandwidths. The approach was to first optimize the speed of a building block, and then to use the block consistently to design larger cache circuits, such as 16Kbyte and 32Kbyte single-ported, and 8Kbyte and 16Kbyte dual-ported to achieve different optimization goals. The simulation results of the circuits are collected in the R Spreadsheet. It presents the effectiveness of the design considerations for optimizing speed, bandwidth, and area (to reduce power consumption) to meet a variety of specifications. One result is that doubling the size of an 8Kbyte single-ported cache in the common reference frame increases the access time by less than 10%. The results are process-independent, allowing the spreadsheet to serve as a convenient reference for cache design and research.

Thesis Supervisor: Thomas F. Knight JR Title: Senior Research Scientist

Acknowledgments

This thesis would not have been possible without the support of many people. The following individuals and organizations have been most generous with their support throughout my thesis work period.

- First, I would like to express my gratitude to Intel Corporation for selecting me as a student of the MIT-Intel Cooperative Program and for giving me the opportunity to work on the foremost microprocessor core designs. My co-op experiences at the company helped me tremendously by giving me a head start in choosing and learning about the technical areas I needed to understand for my thesis.
- I would like to thank Intel's MRL (Microprocessor Research Labs) and the microprocessor core design group in Oregon for providing me with the opportunity to do research and the design facility I needed to implement the work for this thesis. Cache design and circuit design experts at Intel gave me extremely valuable technical support while I was working on my third co-op assignment.
- I would also like to thank my thesis advisor Thomas Knight for pinpointing key technical issues. His comments have helped widen my perspectives. My co-op advisor Jesus del Alamo, who serves as the liaison between MIT and Intel, also supported me by making sure that my thesis work progressed smoothly at Intel and MIT. I thank my technical mentor David Harris too for all his encouragement and help.
- Most importantly, I would like to thank my loving family: my parents and my brother. They have always been there for me. The curiosity about science and high-tech has always been in my blood because of my parents. They encourage and inspire me all the time. I would like to dedicate this thesis to them.

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Chapter 1

Introduction

Memory access is the major bottleneck of today's high-performance microprocessors. In modern processors, several levels of on-chip and off-chip caches are employed to speed up memory access. The rapidly advancing computer industry requires caches to have shorter access times and higher bandwidths, while maintaining acceptable cache hit ratio, to increase the performance of high-end products. The access time, bandwidth, and hit ratio are the standard performance measurements of the cache. They directly affect the speed of instruction-issue, data utilization rate, number of pipeline stages, clock speed, area, cost, and power consumption of processors.

How do we compare good cache designs? How do we even define good cache designs? Different microprocessors have different specifications and are designed with different circuit methodologies and are fabricated by different process technologies as well. It is difficult even to compare the cache performance of different generations of microprocessors designed by the same company. Without objectively comparing high-performance caches and studying design trade-off of them using the same reference frame, how do we absorb and combine the best design techniques to design future high-performance caches? Facing numerous implementation possibilities, I create a common reference frame to compare design trade-offs of optimally designed caches. The frame is created by considering various design issues, combining current optimization techniques and using my own optimization method.

The main goal of this thesis is to provide researchers and designers with first order estimates of access time, area, and bandwidth trade-offs of different cache topologies, which can assist in choosing the cache topology that best meets specifications without heavily depending on simulation circuits. Moore's law dictates that we will design larger and larger circuits; even simulating circuits for feasibility studies will require more significant manpower and CPU time. Figure 1 shows the design flow and typical iterative steps taken during a processor design. The framework can reduce iterative circuit feasibility studies and increase the efficiency of preliminary chip floor-planning. Also in top down chip designs, architects do high-level planning and circuit designers try to meet specifications defined by architects. The thesis research starts from circuit level, taking layout and device level issues into consideration to collect design trade-off information; then the information is propagated from bottom up to set some architectural requirements. This two-way vertical communication can efficiently produce optimized caches. The low-level information also impacts the design of datapaths and floorplans of a cache's neighboring chip components, because interconnects from output drivers of data to other parts of the chip could contribute significant RC delays, as the technology process keeps scaling down.

Moreover, it is important to study how the behavior of caches changes with variable sizes and topologies for the same fabrication process. It is even more interesting to see how this behavior changes with variable process technologies. Devices work faster, reach saturation earlier, and become smaller as the devices' geometric parameters shrink. Interconnects experience increasing fringing and coupling capacitive effect as their geometric parameters shrink. Circuits become more noise-sensitive as the voltages and interconnects are scaled down. How does a cache's performance change when its building blocks change their behaviors in deeper sub-micron technologies? The circuits in this thesis are designed such that the performance ratios obtained are independent of process technologies. The performance ratios include comparing the access time and bandwidth of caches of different micro-architecture based on extensive realistic designs and simulations in 0.25 micron

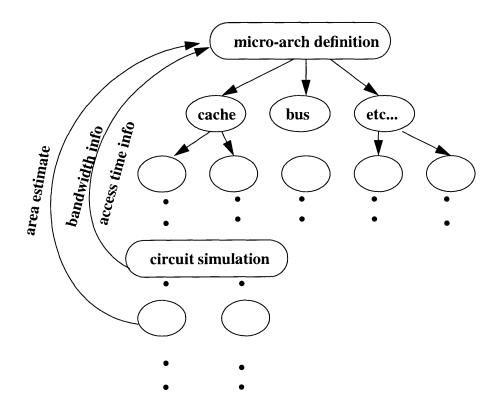
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CMOS process. The circuits are optimally tuned at transistor level. Components from the public domain are used to avoid dependency on implementation details imposed by different processor companies. Therefore, the results give objective comparisons among different cache topologies. For example, each bit cell is a standard 6-transistor RAM cell which is most widely used in the industry.

Consequently, once designers have chosen the right topology, the framework of the thesis can help designers do cache component optimizations. It is more effective to do local optimizations within a globally optimized structure. In addition, the thesis focuses on analyzing and modeling first-level caches because primary caches need to be fast for any microprocessor. Given that the access time has to be optimized, can we do better jobs in optimizing other aspects of cache performance? I try to optimize bandwidth, area, and power as well.

Chapter 2 discusses existing work done on cache modeling. It explains what current cache models have achieved, how accurate they are, and what they lack. Chapter 3 introduces critical high-level issues that readers need to bear in mind while reading implementation details. Chapter 4 presents the details of circuit designs. Chapter 5 presents circuit simulation results and explains their significance. Chapter 6 is the conclusion, including the future outlook of cache designs. The framework presented here can certainly be expanded for higher-level on-chip or off-chip caches.

FIGURE 1. A Simplified Version of Design Flow



This figure is an extremely simplified version of the actual flow of chip design. Designers can keep looping from micro-arch definition to circuit simulation and back to definition, if the best cache topologies are not chosen correctly in the decision making stage.

Chapter 2

Existing Work on Cache Modeling

There are publications on modeling cache access time by people in industry and academia. Wilton and Jouppi at DEC Western Research Lab published their first cache models in 1994 [17], then made improvements in 1996 [16]. They modeled each component's delay in the critical path, assumed designing with 0.8 micron CMOS process, and estimated gate delays of the critical path using Horowitz's transistor models [17]. The transistor-level models take various input rise times and output capacitive loads into consideration, which makes the analytical models more realistic than some early work done on cache modeling. However, Horowitz's transistor models developed in 1983 might not be adequate to model today's short channel devices. Horowitz assumed that a transistor stack operates in linear regime and approximated on-resistance of the stack [8]. Later Sakurai and Newton generated the "Alpha-Power Law" to model series-connected MOS-FET circuits [14]. Sakurai proved that the delay through a transistor stack does not grow linearly with the number of transistors in the stack, because the transistor near the output operates in saturation regime, instead of linear regime as assumed by Horowitz. The topmost transistor can easily enter saturation when the channel length is short. Sakurai's model proved that Horowitz's transistor stack model to be pessimistic [13]. More recently McFarland further developed transistor delay models by Horowitz and Sakurai [9]. McFarland used curve fitting more extensively, which involves even more mathematical steps. All the analytical transistor models are valuable to both research and product development. But when they are used in generating cache models like Jouppi did, the steps involved are somewhat tedious. Wilton and Jouppi wrote a tool "Cacti" to make their models user-friendly [16]. However, as the technology process changes, adjustments need to

be made to their analytical models, in particular, Sakurai's models might be more accurate to characterize the behavior of deep submicron devices. Also Jouppi modeled only singleported caches. Multiported caches have become increasingly popular, due to their microarchitectural advantages. Furthermore, past efforts seem to have focused on obtaining optimal partitioning of cache arrays. This thesis shows that seeking optimal partitioning is an unnecessary, misleading, and inefficient use of design time.

One of the goals of the thesis is to compare the access time of different circuit topologies, not the absolutely accurate delay of each cache. Certain assumptions are made to avoid using complicated device-level analytical models to approximate cache access time. All the existing analytical models relied on curve fitting to some extent, which means that they must be changed as the process technology changes just like empirical models. Simplicity is effective, robust and user-friendly. This thesis presents a spreadsheet of access time, bandwidth, and area ratios among different cache topologies to serve as a quick guide when selecting a particular cache topology to meet designers' needs. The data of the spreadsheet is collected from actual circuit implementations and simulations. All the circuits are designed and simulated in 0.25 micron process, instead of 0.8 micron used by Jouppi.

Chapter 3

High-Level Issues

Since later chapters are dedicated to describing implementation details, this chapter presents some high-level implementation issues. In today's microprocessor chip design, neither having aggressive micro-architecture with inadequate circuit implementation nor having poor micro-architecture with fast circuits is effective in utilizing design time and manpower. It is much more effective to optimize design of specific components, after choosing a globally optimized structure.

How to determine a globally optimized structure is quite challenging. Different microprocessor companies prioritize optimization features differently when designing primary caches. For instance, one primary cache design might replicate its primary cache to double its bandwidth like DEC Alpha 21164 [5]. This introduces on-chip cache consistency problems. Every time data is stored into one cache, the other primary cache must be updated accordingly, which costs extra power. Another cache design might divide a large cache into smaller banks to shorten array access time, but this increases interconnect length for data to be delivered to destinations. If many loads reference to the bank that has the longest interconnect between data output tristate buffer and destinations, the overall latency of loading and delivering data might increase. Also, banking a large cache to shorten access time or banking caches to increase bandwidth often involves replicating decoders and predecoders. This kind of organization can take more area than other kinds of cache organizations.

It consumes manpower and CPU time to design and simulate all the possible cache topologies to analyze design trade-offs in varying cache sizes and bandwidths. The circuit designs presented here try to globally optimize caches in speed, area, power and bandwidth together as much as possible, using circuit components in the public domain. The spreadsheet in this thesis contains a limited number of combinations but enough data to compare the performance ratio of different globally optimized caches. The spreadsheet contains data for 8K, 16K, & 32KByte caches which are often seen in many contemporary designs. The next few sections present some of the high-level issues of this thesis work which need to be noticed before diving into the details of implementation work.

3.1 Partitioning Cache Wordline and Bitline Length

Large cache line size requires buffering, which contributes to additional wordline delay. Smaller cache line size (width of the cache) increase bitline loads (height of the cache) which might also increase access time. This is the trade-off between cache access time and bandwidth. As often seen in cache publications, people try or suggest finding optimal ways to partition a cache so that the proportion of wordline length to bitline length gives the best access time [17]. This approach is misleading and is not an efficient use of simulation time. The bitline delay portion is really characterized by an analog circuit because it is small signal differential amplification time, and the rest of the cache is digital. Since analog portion of the cache cannot be pipelined, determining the geometry of a cache should start by looking at the timing requirement first, making sure that the worst case bitline delay does not exceed timing requirements. After determining cache height, the wordline length is determined from the height and the size of the cache. In this work, 128 cells are attached to each pair of bit and bitbar lines, in order to generate enough small differential signals for sense amps to detect fast. This number stays the same for all the caches in this work, since the optimized 8kByte cache serves as the building block for caches of larger sizes or higher bandwidths.

3.2 Determining Degree of Associativity

It is important to separate micro-architecture and circuit design trade-offs, when comparing access time of different circuit topologies that have same cache sizes. In this thesis, the associativity of all the caches needs to be fixed to make objective comparisons. Wayprediction is assumed for all cache circuits. SGI's high-end products MIPS R10000 and R12000 both have way-prediction mechanisms [10]. Way-prediction prevents address translation and tag array access from adding delays to data array access. In order to achieve high hit ratio and to take advantage of way-prediction schemes, the associativity is fixed at 4 here. This is also a circuit hack to reduce access time. Each sense amplifier can only have a limited number of bitline pairs attached together as input to the sense amp, and each bitline pair has to go through a column multiplexor to output line size to match bus width. Therefore, I interleave 4 ways and use way-predication vector as column mux select signals to

- select column with the correct way data
- eliminate a mux delay vertically down the cache
- equalize way select delay of the same bit

So now, the cache has the hit ratio of a 4-way set associative cache and delay time of a direct-mapped cache that has the shortest access time. The circuits in this work are implemented as direct-mapped caches, but they behave like associative caches as well.

3.3 Major Assumptions Made

3.3.1 Data Array Access is Critical

One major assumption made is that the critical path of all the caches is the data array access. In modern cache designs, critical paths often include TLB (Translation Look-aside Buffer) and tag array access to give way-select and hit / miss information. In some cases, the clock tree datapaths for enabling sense amps is also included in the critical path. Although the TLB outputs physical address for tag comparison, it is small and often

implemented using CAM (Content Addressable Memory) arrays or highly associative arrays for quick virtual address translation. Tag array access is similar to data array access with an extra delay due to comparison. But a tag array is also relatively small compared to a data array. Therefore, the assumption is that designers should be able to design TLB and tag array datapaths to match part of the delay of data array access and provide way select signals early enough. For large data arrays, the arrival of hit / miss information generated by TLBs and tag arrays becomes less critical. The data array is pipelined and needs muticycles to output data. The hit/miss information needs to be available only by the end of the last pipestage before data is used by other parts of the chip. Any other timing select signals should also arrive early enough. Basically, designers should not let any select signals worsen the data array latency, which sets tight timing constraints for successive pipestages, this in turn, affects a processor's overall performance.

3.3.2 Begin and End of Access Time

All the access times in this thesis refer to worst case cache read times, because loading data is more critical than storing data. Loads can really stall pipeline. Another assumption is that data array access time starts from address bits latching for indexing data array to output data latching. Both physically indexed, physically tagged caches and virtually indexed, physically tagged caches have micro-architecture and circuit advantages and disadvantages. To keep micro-architecture trade-offs separate from circuit trade-offs, the data array latency starts after address bits become available, regardless of virtual or physical address bits, which is another reason why TLB translation is not included in the critical path. If readers prefer to use physically indexed caches, the TLB access time is added to data array access. But if accessing TLB is the first step for all the cache circuits, including TLB access time does not affect cache performance comparisons significantly. Therefore, the spreadsheet of this thesis contains all the information about data array. Readers can extract information from the spreadsheet to estimate access times of tag arrays and TLBs, because they are all similar arrays from the circuit implementation point of view. The assumptions made above are a means to efficiently study area, speed, and power design trade-offs of current high-performance caches.

3.3.3 Virtually Indexed, Physically Tagged Arrays

I made some assumptions about logic control signals for the fastest array access time. The assumptions set micro-architectural constraints which architects need to consider during architecture definition and chip floor planning. This is the bottom up communication referred to in the previous section.

The building block is assumed to be a virtually indexed, physically tagged cache. As soon as a virtual address is available, the untranslated page offset is used to index the data portion, bypassing address translation by the TLB. For aggressive clock frequencies, cache access often takes more than one cycle. The actual array access pipestage in this work starts from the domino decoder to the output load. Predecoding the array index (wordlines) contributes to part of the delay in the previous pipestage. The time that the virtual address bit travels through all the interconnect to reach the predecoder and the predecoding time must be less or equal to the clock period minus the required setup time of the clock, because predecoded lines must be ready before the setup time of the domino evaluation clock to avoid inadvertently flipping logic. Some readers might argue that virtually indexed, physically tagged caches have synonym problems, meaning the same virtual address is mapped to two different physical locations. There are methods to reduce synonym problems, for example, making sure the tag array does not exceed the size of a physical page.

3.3.4 Way Prediction

Way prediction is the key to make associative caches have the access time of directmapped caches as indicated in section 3.2. This scheme prevents any delay of deciding way hit from joining the critical path, and it also eliminates the way select multiplexor in the critical path. Therefore, way prediction schemes save both array access time and area. Some readers might wonder how the way select information can be ready so fast. To my best knowledge, there are several ways of implementing way prediction schemes, and architects can certainly improve them. Both MIPS R10k and R12k implement way prediction [6]. Difference-bit caches [7] and the path balancing table [12] are also usable, but they limit the degree of associativity.

3.3.5 Control Signals

All the control / enable signals, including way prediction information, must be ready when they are needed. Basically, no extra delay should be introduced by enable signals to the intrinsic array delay. For instance, the sense amplifier enable signal should be ready on time. The data path of the sense amp enable signal should be designed to be effective early enough to sense voltage differentials. Again these constraints affect logic and datapath designs of previous pipeline stages. They require optimal cache component arrangement, which in turn affect floor planning of neighboring FUBs (Function Unit Blocks). The constraints are nontrivial to satisfy. This surely involves design trade-offs in designing neighboring FUBs. But it is important to keep in mind that building the fastest primary caches is the top priority, because they directly affect data utilization rate, which in turn affect the flow through of pipeline stages. Readers can argue that out-of-order instruction execution can hide cache access latency. However, out-of-order or speculative execution is effective only when there is no data-dependency or structural hazard. It is still essential to have fast cache array access and then use out-of-order execution to hide the

latency that takes to deliver data via bus interconnect, which has become increasingly harder to manage as the process technology continues to scale down.

3.3.6 Neighboring FUBs

Neighboring FUBs need to be arranged to allow data to be quickly delivered to destinations. This requirement makes floorplanning challenging, because this might increase interconnect length for later pipestages. It is even more difficult to optimize interconnect delays for those microprocessors that use unified caches. A unified cache stores both instructions and data. Since cached data and instructions are dispatched to different locations, the shortest route to pass data might not be the optimal path for instruction passing. Applying Rent's rule to predict on-chip interconnect density during architectural planning is helpful.

Chapter 4

Implementation Details and Circuits

4.1 Introduce an Optimized Building Block

The simplest formulae, having fewest variables, are often the most powerful ones that can capture a wide range of patterns in phenomena and behaviors of matter. For example, Newton's F=ma is the simplest formula, yet the most powerful law that creates and governs numerous technological disciplines, and affects many aspects of our lives. Inspired by the simplicity and power of Newton's law, I decide to create a simple building block, then build abstractions based on the fundamental unit to cover more cache implementation possibilities. However, the building block itself must be relatively optimized to be meaningful in researching high-performance caches. Readers might think that having a highly optimized building block conflicts with achieving simplicity. Fortunately, the fastest cache, a direct-mapped cache, is the one that has the simplest or minimum number of logic stages in the critical path. Prior to implementing fast circuits, the crucial step is minimizing the number of logic stages in the critical path of accessing caches.

The critical path of accessing a direct-mapped cache begins at the address bits latch, traverses through a predecoder, then the interconnect that has the height of the array, a decoder, turns all the way to the last bit cell hanging off the top word line, goes all the way down to the last bit cell hanging off of the bitlines, then goes through a column selector, a sense amplifier, then drives the output load. For associative caches, there is an additional delay introduced by the multiplexor that selects between ways. In many modern microprocessors, primary caches are at least 2-way set associative. Associativity reduces address conflict, but the hit ratio of a cache does not increase infinitely with the degree of associativity. Also, without optimization, usually the higher the degree of associativity, the slower the caches are. This is because the number of input to the way-select multiplexor is larger, meaning more pass gates (transmission gates) are tied together which contributes more diffusion capacitance to slow down the circuit. It does not make any sense to say that a direct-mapped cache performs better than a two-way set associative cache, because the former has shorter access time. This is like comparing apples with oranges. Set associative caches have microarchitechtural advantages, while direct-mapped caches have circuit advantages. Some microprocessors have 2-way set associative caches, while others have more than 2-way. It is also nonsense to compare the performance among these caches, because their hit ratios differ. The 2-way associative caches are faster, but the hit ratio is lower, which triggers more accesses to on-chip or off-chip secondary caches, degrading the processor's overall performance.

The building block (see Figure 4.1), which is used to analyze caches, optimizes cache performance both in micro-architecture and circuit topology. The key to building a high-performance cache is to achieve the hit ratio of associative caches and the access time of direct-mapped caches. It is crucial to maintain direct-mapped cache access, because those caches use a minimum number of logic stages needed for a functional cache.

4.2 Circuit Topology and Specific Component Design

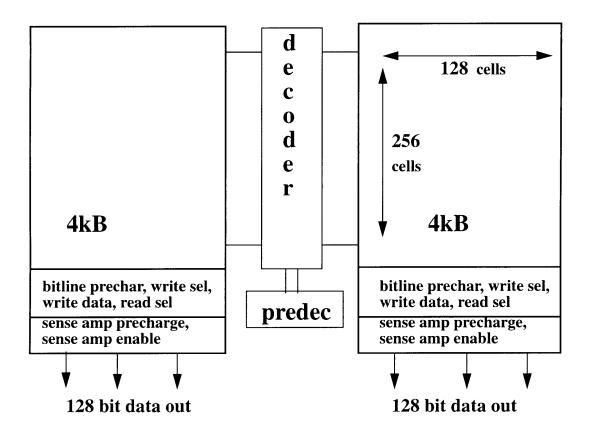


Figure 4.1: 8kB Single-Ported Cache

4.2.1 Predecoder

A predecoder is used to reduce fan-ins to the decoder to speed up circuits. In the circuit design for this thesis, 128 wordlines need to be decoded which requires 7 input address bits (2^7=128). The predecoder groups every two address bits together to parallelize decoding logic. Every pair of two binary bits has four possible combination outputs. In this circuit design, the 7th address bit is all by itself; therefore there are only two possible outputs associated with it. The worst case input capacitive loading of simulation circuits is two binary bits generating four possible outputs using four logic gates in parallel. Each bit of the pair is fed into four logic gates.

4.2.2 Decoder

After the predecoding stage, the predecoded wordlines see interconnect that has a length of the array's height in the worst case delay. This interconnect is modeled during simulation as part of output load of the predecoder and input load to the decoder. Since two address bits predecode into four lines, each of the four is then fed into thirty-two parallel logic gates in the decoder, which generates 128 different wordlines. Each of the logic gates is a 4-input nand or nor gate, depending on how many inversion logic gates address bits go through to reach the decoder. In array designs, the use of dynamic gates should be minimized to reduce dynamic power consumption. In this design, only the decoding stage uses domino gates. Extra care is needed when using domino gates to prevent various noise and charge sharing problems.

4.2.3 Wordline Loads

Wordlines that come out of decoders need to travel across the array to reach the last bit cell in each row; therefore, when building simulation circuits, all the capacitive loads seen by the wordlines in actual arrays must be included. Interconnect delay has become increasingly difficult to deal with as the process technology continues to scale down. However, wordlines of arrays are quite manageable compared to bus interconnect for three reasons. The first reason is that all the bit cells are closely abutted, the capacitance of wordlines is dominated by gate capacitance of passgates in each bit cell, instead of wire capacitance. The other reason is that wordlines are widely apart from each other due to bit cell height, meaning not much coupling between wordlines of adjacent rows. The last reason is that wordlines from adjacent rows generally do not switch to opposite polarity at the same time, since only one wordline can be on at a time and the wordline is turned off before its neighboring wordline is fully decoded. When adjacent wires change to opposite polarity at the same time, the cross coupling of wires is doubled as is often seen in bus interconnect. Therefore wordlines of arrays capacitance and resistance are scalable as process changes.

4.2.4 Bit Cells

Each bit cell, which is the most commonly used RAM cell, has six transistors. The transistors should be minimally sized in order to minimize the total cache area. The gates of the two passgates inside each cell are tied to a wordline, and the drain / source of the two passgates are connected to a pair of bit and bitbar lines respectively. The other four transistors are two back to back inverters to latch data. Certain sizing ratios among the six transistors must be maintained to avoid inadvertent flipping of logic.

4.2.5 Bitline Loads

Bitlines loads directly impact on the rate of detection of differential signals. Bitline capacitive loads are mostly drain capacitance of passgates in all the cells that share the same bitlines. Other capacitance comes from drain capacitance of write buffers, read-select muxes, data-in and precharge devices. The bitline of one cell and bit barline from its neighboring cell can cross couple, introducing additional delay which might be severe enough to flip logic. Therefore, bitlines must be carefully laid out to decouple from each other to minimize neighboring interference.

4.2.6 Precharge, Write Buffer, and Read Mux

When the array is not being read, bit and bitbar lines must all be precharged to high to prepare for stores. Typically there is an equalizer, which is one passgate, to maintain equal voltage of the lines. Precharge circuitry must be placed above read select mux on bitlines. The write buffer, as the names suggests, is for storing information into bit cells. Each bitline (bit and bitbar) has an nfet attached to it. Write-enables control the gate of nfets, and data is connected to the other end of nfets. When the write enable is on, data is written onto the bitlines through the turned-on nfet. The read mux is basically designed with tran-

sistors connected in series with bitlines. Read-enables turn on the nfets, then information on the bitlines pass through the nfets flow into sense amplifiers.

4.2.7 Sense Amplifier Precharge and Sense Amplifier

The sense amplifier precharge circuitry is the same as regular precharge, and it is necessary to place it below the read mux and above the sense amplifier. It is the same as regular precharge circuitry, except it needs to be specifically placed on bitlines below the read mux and before the sense amplifier to make sure that both bitline ends of the read mux truly start with equipotential before sensing. The sense amplifier is really an analog differential amplifier that amplifies different voltages on bitlines and corresponding bitbar lines. It should be turned on after a certain differential voltage level is reached, otherwise, it could sense the wrong data due to noise interference. The sense amplifier is triggered by a timer which can turn it on at a precise time to quickly detect and amplify signals without making mistakes. Designers need to look at circuit simulation of bitlines and record the time that at where the correct differential voltage occurs.

4.2.8 Output Loads Modeling

Since this thesis is intended to make a systematically quantitative analysis of cache behavior, I try to cover as many cache topologies as possible to make data analysis realistic. Modeling output loads of sense amps is crucial, because it propagates gain information backwards which affects transistor sizing of previous logic stages. By examining various cache topologies, I conclude that the output loads of senseamps of an array can have six possibilities. The data that comes out of a sense amp is fed into 1) a latch; 2)a mux; 3)several hundred micron long interconnect; 4) a tristate driver; 5)a logic gate; or 6) an inverter to drive interconnect. I measure the capacitance of each possibility seen by data out and use it as the worst case capacitive loads to size circuits backward.

4.3 Timing Requirements

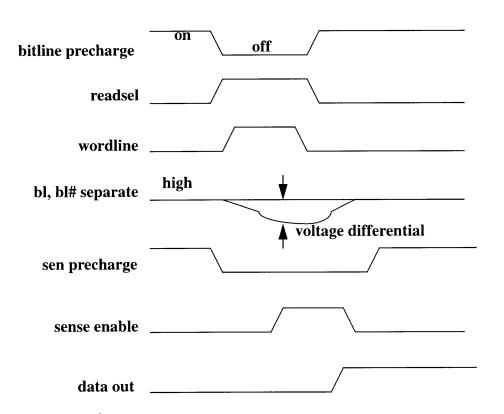


Figure 4.2: Timing Diagram

Figure 4.2 shows how each control signal should be turned on and off with respect to other signals. Memory arrays are vulnerable to glitches. It is important to leave enough margin between transitions of pullup and pulldown signals to avoid glitches and DC power loss. For example, wordline-off and precharge-on should not transition at the same time.

Sense-amp-enable should be on after enough bitline differential is developed as shown in Figure 4.2. The timing is determined by the sensing rate of the design and when it is safe to sense. Turning on the sense amp too early before the adequate bitline differential is reached can output wrong data. This is because the bitlines are originally precharged to high, and turning on the sense amp pull both bitline and bitbar line low at the same time. With noise coupling, the polarity of the bitlines could be reversed, producing wrong data. Turning on the sense amp too late lengthens cache access. The most important timing requirement is to overlap bitline precharge with sensing. This is critical for satisfying multi-cache access in one clock cycle. After many trials, I discover that it is safe to close the bitline soon after the adequate bitline differential is developed. This allows precharging to start before data is out. DEC Alpha 21264 has single-ported primary caches and double pump data in one clock cycle, essentially each read can use only half of a clock cycle to finish [5]. This might not be achieved if the clock speed is even more aggressive than Alpha's and if clock skew and jitter are severe. By overlapping bitline precharge with data sensing in a truly physically dual-ported cache, a read can take the clock cycle using one port, a write can also be satisfied in the same cycle using the second port. Or, issuing two load requests during the same or adjacent clock phase can be satisfied.

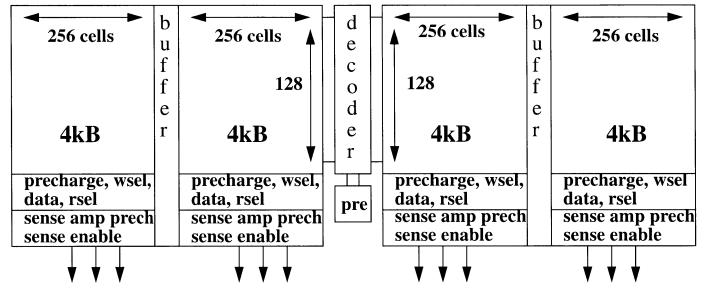
4.4 Building Abstractions

4.4.1 16kB Single-Ported Caches

Having the building block done, it is time to build abstractions on top of it. It is interesting to see how a cache's behavior changes when its size is increased. As stated before, having a larger cache can reduce address conflict, thereby increasing hit ratio. To look at it from another angle, increasing the size can also increase the bandwidth of the cache, depending on the width of the data bus.

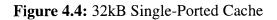
One way of implementing the 16 kB cache using the building block is to replicate the 8kB cache array and all the peripheral circuits, and place them symmetrically so that the address bits can reach both predecoders at the same time. Replicating caches allows the access time to stay the same as that of the 8kB and doubles the original bandwidth. The trade-off is that replication introduces on-chip cache consistency management. Every time one cache is updated, the twin copy also needs to be updated, wasting power. The activity factor of arrays should be kept low to save power. Another trade-off is replicating decoder and predecoder costs extra area.

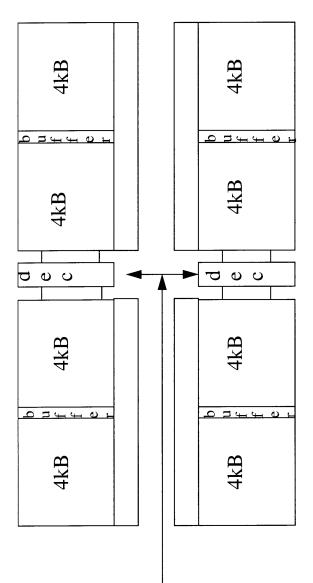
The other way of implementing the 16kB using the building block is to internally buffer wordlines (see Figure 4.3). The buffer for each wordline introduces some additional area, but it is relatively smaller compared to having an extra set of a decoder and a predecoder. Buffers add a little more delay, but they can also speedup wordline for the second 8kB array. This is because the decoder fans out symmetrically in two directions, seeing twice the wordline loads and interconnect. The buffer in a wordline sees only one set of wordline loads and interconnect. Having two 8kB array adjacent to each other might make the final data out travel some extra interconnect in successive pipestages, depending on how data is dispatched with respect to the location of the arrays. With optimal sizing, the 16kB with internal buffering can still have array access done in one clock cycle.



4.4.2 32kB Single-Ported Caches

Now the 16kB cache becomes the building block for a 32kB cache (see Figure 4.4). The replication method is recommended to make sure array access can be done in one clock cycle.



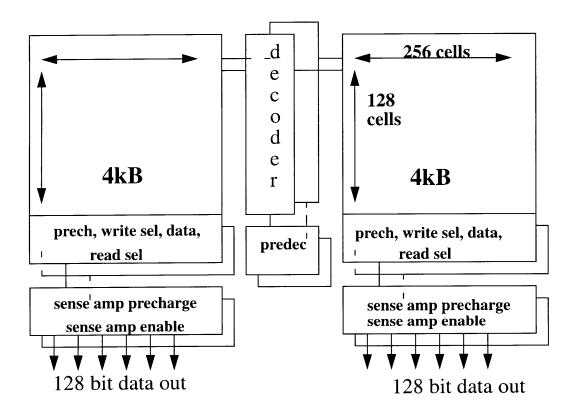




4.4.3 8kB Dual-Ported Caches

Now back to the 8kB cache, except this time each bit cell is physically dual-ported (see Figure 4.5). The latch in each cell sees twice the diffusion capacitance. Each cell also sees two pairs of bit and bitbar lines. These additional features inevitably increase the original cell size. Layout designers need to especially careful place bitlines to minimize wire coupling when both ports of the cell are being used simultaneously.





Dual-ported caches double the bandwidth of single-ported caches. If the timing rules are strictly followed in Sec 4.3, two reads to the same cell or different cell or one read and one write to the same cell or different cells can be done in one clock cycle. How does this micro-architectural advantage affect circuit performance? The worst case access time is

when having two reads to the same cell because all the capacitive loads of the singleported cell are doubled. However, this does not mean the array access is twice as slow, since reading bitlines is a small signal operation, only detecting bitline differential matters, instead of developing full rail to rail signals. The area increase does make wordlines and bitlines somewhat longer. Good layout designs do not make the interconnect twice as long as that of a single-ported cache. The interconnect within memory array is much more manageable than bus interconnect because bit cells are so closely abutted and gate and drain capacitance dominates over wire capacitance. Wordlines and bitlines are separated by transistors, so cross coupling is not severe. Another difference between memory and bus interconnect is that memory wires never have a Miller factor of 2. Current in wordlines all move in the same direction, from the decoder to the cell. For dual-ported array, if two adjacent cells are doing read and write respectively at the same time, each bitline sees only one opposite transition occurring in the wire of its neighboring cells.

A dual-ported cache can also finish an array access in one clock cycle. An important control signal requirement is that there should be two sets of enable signals for the two ports within each cell to satisfy one load and one store in the same cell using one clock cycle. Therefore, compared to single-ported caches, dual-ported caches take twice the area, double bandwidth, and can also have array access done in one clock cycle with careful sizing devices. The 8kB dual-ported cache is now the building block for a larger dual-ported array, just like the 8kB single-ported cache

4.5 Process Independent

The circuits are designed so that the performance ratios obtained are process independent, because all the different cache topologies use the same 8kbyte cache building block. This means that transistor sizing of all the peripheral circuits stay the same. Singleported and dual-ported have different bitcell sizes which contribute to differences in

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arrays' heights and widths. Decoders of dual-ported caches see a longer interconnect, but the decoders of the single-ported caches are sized to be able to tolerate a few hundred micron interconnect differences. Also, the interconnect within cache array is much more manageable than bus interconnect, because wordline capacitance is dominated by gate capacitance and bitline capacitance is dominated by diffusion capacitance because array cells are closely abutted together. Transistor capacitances are linearly scalable with process change. Therefore the array access time ratio among caches stay roughly the same for new process technologies which allow the information provided by this thesis to serve as a reference for future cache studies and designs.

Chapter 5

Results, Observations, and Analysis

The data collection part of this work involves extensive circuit design and simulation work (drawing, sizing, and simulating several ten thousand MOSFET transistors) in 0.25 micron CMOS process. Table 5.1 presents design trade-offs of varying cache sizes and bandwidths. All the data are normalized to the numerical values of the optimized fundamental building block 8kB single-ported cache as shown in row 1 of Table 5.1. It is important to realize that this building block already minimizes the atomic array access time which is always the top priority in optimizing primary caches. The following R Spreadsheet presents data to indicate that the cache topology organizations described in this thesis can globally optimize other design aspects at the same time.

	Cache Type	Speed Ratio	Area Ratio	Bandwidth Ratio
1	8kB Single-Ported	1	1	1
2	16kB Single-Ported Buffered Wdline	1.096	2	1 to 2
3	32kB Single-Ported Replicated Buff- ered 16kB Single- Ported, Placed in Symmetry	1.096*	4	1 to 4
4	8kB Dual-Ported	1.119	1.93	2
5	16kB Dual-Ported Replicated 8kB DP, Placed in Symme- try	1.119*	3.86	2 to 4

 Table 5.1: R Spreadsheet

Note: * means that the result in the replication case is obtained by assuming the current drive strength at the input in the previous case is maintained.

5.1 Doubling Cache Size and Minimizing Area

Doubling the 8kB cache size does not double the access time. In fact, the access time increases by only 9.6%, if the cache is implemented using the cache type in row 2 of Table 5.1. When a 16kB cache is implemented as Figure 4.3, the extra delay is primarily introduced by the wordline delay through the first 8kbyte and the delay of the wordline buffer between it and the second array. All the other circuit delays stay the same. This 16kbyte cache is pseudo cache banking. The cache is really split in half and has the option to be used as a bigger cache to store information or to be used to double output data. This is why the 16kB single-ported cache can either remain the same or double the bandwidth of the 8kB single-ported cache, depending on a designer's choice. The area of this 16kB is roughly doubled because the buffers need to be large enough to optimize the delay of wordlines and other control signals that travel in the same direction as the wordlines.

For smaller size caches like 16kB, I suggest using wordline buffering (buffering wordlines between two optimized 8kB) as described above, instead of replicating caches as seen in some microprocessor designs. Replication can achieve the same access time as the 8kB. However, power consumption doubles every time one of the two 8kB is updated, in order to maintain cache consistency. Also, only placing the replicated cache symmetrically as the mirror image of the original 8kB allows the access time to remain the same as that of the 8kB. If the floor plan of neighboring FUBs only allow the two 8kB caches to be placed adjacently, then this replication scheme increases access time in the worst case delay. This scheme increases area more than the wordline buffering technique due to extra routing signals to reach the second 8kB, in addition to increasing power consumption.

Buffering wordlines and Replicating caches as mentioned above are basically 2 types of the cache banking technique. When banking large caches, the height of the cache (the analog portion) is determined by whether reading bitlines can be done within one clock cycle, because this analog portion of the array cannot be pipelined as mentioned in Section 3.1. Once the height is determined, then designers need to balance the width of each bank with the total number of banks.

Number of Banks = Cache Size / Bank Size
$$(5.1)$$

Bank Size= Width * Height (5.2)

Time to Read the Height of each array < 1 Clock Period of the Current Domain (5.3) When designing large caches, the time to propagate data through the interconnect

between cache data-out and various destinations affects the arrangement of banks, which in turn limits the total number of banks. Because of neighboring FUBs' locations, cache banks cannot be arbitrarily placed; otherwise it causes data to travel longer routes to reach destinations in successive pipeline stages. Having fast cache array access but traveling much longer interconnect to reach destinations, resulting in more pipestages, can unfavorably increase overall load latencies. Designers need to consider how much time margin there is in the pipestage after accessing caches, and use Equations 5.1, 5.2, 5.3 together to arrange cache topologies. Section 5.2 gives an example of minimizing the interconnect delay after cache access.

5.2 Quadrupling the Cache Size or Bandwidth

Having a 32kB cache can certainly increase cache hit ratio, but by how much would quadrupling the cache size of 8kB increase the access time? If the 32kB is arranged as suggested here, the access time only increases by 9.6% from the access time of the 8kB as shown in row 3 of Table 5.1. Designers should replicate the 16kB single-ported cache and place the two identical 16kB symmetrically. And each of the 16kB should be built from the 8kB by buffering wordlines. Again the bandwidth ratio could be two to four, depending on designers' needs. The area of this 32kB is roughly quadrupled, less than the area needed for other kinds of topologies, because this cache organization tries to minimize the

area consumed by interconnect. On modern microprocessor chips, the area is determined by interconnect density rather than transistor density.

5.3 Doubling Bandwidth

5.3.1 Minimizing Area and Increasing Some Access Time

In order to double cache bandwidth and minimize area, I suggest to use a dual-ported cache as shown in row 4 of Table 5.1. The dual-ported cache has additional delay on the bitlines because each bit cell sees at least twice the capacitive loads down the bitlines. The access time is increased by 11.9%, compared to that of the 8kB single-ported. However, the area is only 1.93 times that of the 8kB instead of twice, which is a substantial saving for much larger caches. Dual-ported cache has a micro-architectural advantage. With the timing requirement described in Section 4.4, the dual-ported cache allows back to back loads and stores in one clock cycle, thereby doubling cache bandwidth.

5.3.1 Minimizing Access Time, Increasing Area and Power

If a designer's goal is to minimize access time and double bandwidth, the replication method works well. The implementation is to replicate the entire 8kB single-ported cache and place the two caches symmetrically to minimize interconnect length, so that the two caches can output data in the same time as a single 8kbyte cache. This is true only if the current drive strength at the input of the single 8kbyte cache is maintained at the input of this replication topology. This makes the circuits before the cache slightly slower because of the relatively small capacitance of the additional latch. As mentioned in Section 5.1, the trade-off is that extra power is consumed in order to maintain cache consistency between the two. The two caches are decoded using the exact same address bits, and the two store the same data. Every time data is stored in one cache, the other cache must be updated too. Writing into cache involves powering up the entire 8kB array. Also placing two caches

symmetrically affects the floor-planning of neighboring Function Unit Blocks, putting pressure on other FUB designs because they might see longer interconnect delays.

5.4 Doubling Cache Size, Quadrupling Bandwidth without Quadrupling Area

The best way to quadruple the bandwidth of the 8kB without quadrupling the area is to use a 16kB dual-ported cache by replicating 8kB dual-ported and place the two banks symmetrically. The area ratio is 3.86 (see row 5 of Table 5.1) instead of 4 by replicating the 8kB or internally banking into multiples of 8kB.

5.5 Power Issues

Lowering microprocessor power dissipation is one of the most important design issues nowadays in order to meet customers' needs, especially for mobile computing and handheld products. Every chip maker continues to increase the clock speed to achieve faster computing.

F=Clock Frequency, A=Activity Factor

Equation 5.4 indicates four factors that affect dynamic power dissipation. As mentioned in Section 4.2.2, minimizing the use of dynamic circuits reduces dynamic power dissipation due to high switching frequencies. Since F continues to increase, lowering V is a popular method because the power decreases quadratically. However, V cannot be brought lower than semiconductor device operating voltages, which leaves the options of lowering C and A. Reducing area consumption certainly lowers C. Since the total on-chip array area is at least 40% of the total die area, reducing array area has a noticeable effect on lowering C. The area of each bit cell should be minimized, meaning the minimally allowable sizes should be assigned to the six transistors of each cell as mentioned in Section 4.2.4. For 16kB primary caches, buffering wordlines between two 8kB banks is more desirable than replicating one 8kB cache bank as mentioned in Section 5.1. The extra set of one decoder and one predecoder costs more area than the total area of buffers. Buffering wordlines costs more access time than replication, but for caches of this size, buffering does not significantly increase cache access time. Finally, lowering the activity factor of cache arrays, that is, powering arrays down when they are not needed, also decreases power consumption. This topic is a specific implementation detail; therefore, it is not discussed further.

5.6 A Few Cautionary Words

Before designing the circuits, I make certain assumptions already listed in Chapter 3. The assumptions are realistic and practical for readers to consider when they try to select the best cache topologies to meet their own specifications. I use circuit components in the public domain to design the caches listed in the spreadsheet to allow a wide range of users to consider and apply my design strategies. Chapter 4 describes implementation details of the reference frame. The numerical values that I use for the array dimensions are not magic numbers. Readers should pay more attention to the approaches. All the approaches listed are valid for implementing both direct-mapped and associative caches. The actual circuit designs here are really the circuit implementations of direct-mapped caches; however, I assume way-predication mechanisms are available to make the circuits behave like associative caches (see Section 3.2 and 3.3.4). This thesis is not intended to tell readers that the design strategies listed here are the ultimate optimization techniques for final production circuit designs. However, this thesis provides globally optimized structures as starting points to help users efficiently choose the right cache topologies to meet their needs. Users can then use various circuit hacks to do local optimizations to obtain even better speed ratio [2], [4], and [11]. These local optimizations are implementation details set by individual organizations. The data in the spreadsheet is process-independent so it can serve as a reference for future process technology designs as well.

Chapter 6

Conclusion

6.1 Summary of the Research

The primary goal of this thesis was to systematically and quantitatively analyze performance trade-offs of major cache topologies. It is difficult to compare the performance of different cache implementations, because they have different specifications and are designed with different circuit and simulation methodologies. In order to make objective comparisons, I first established a reference frame by using circuit components in the public domain to design the frame. While designing the reference frame, I realized that I would need to design a building block and to use it consistently in implementing caches with different sizes and bandwidths. More importantly, the building block had to be optimized in speed, so that the reference frame would be a truly effective, meaningful tool for comparing cache performance. In the meantime, I strove to design circuitry so the results would be process-independent. I optimized the building block to obtain the hit ratio of an associative cache and the access time of a direct-mapped cache. After finishing the building block, I designed and simulated caches with different sizes and bandwidths, then collected data for the spreadsheet.

Although the R Spreadsheet looks simple, it has high information content. It shows how to optimize area and / or bandwidth in addition to optimizing speed. The most challenging part of the work was to efficiently and effectively organize circuit topologies: Without depending on specific implementation details of any existing cache work, the designs in this thesis include a variety of high-performance cache implementations along with my own design strategies. Fortunately efficient ways were found to optimize caches in speed, bandwidth, and area, all three, providing different cache topology choices with similar performances. As a result of these efficient approaches, the spreadsheet represents a variety of cache implementation schemes.

Based on the data collected from realistic cache designs and simulations of several ten thousand transistors, the thesis describes design trade-offs and design considerations for concurrent high-performance caches which can serve as a convenient reference for designers during the topology definition phase. This quick reference shows how the behavior of caches change as their sizes and bandwidths are increased. The performance ratios presented are accurate for new process technologies because they are process-independent. Section 5.5 points out how readers should interpret the spreadsheet.

6.2 Expansions Based on the Groundwork

This thesis focuses on optimizing data arrays of primary caches (see Section 3.3.1). The approaches can be applied to analyzing tag arrays. The main additional features of tag arrays are comparators, and the rest of the components of tag arrays are the same as those of data arrays. The work presented here can be extended to analyze and design any on-chip or off-chip cache. For example, 3-D visualization is currently one of the main forces pushing the computing industry. Graphic chips must have high-bandwidth and fast caches. The results of this thesis can certainly be applied to designing high-speed and high-bandwidth SRAMS for computer graphic applications.

6.3 Future Outlook of Memory Designs

Out-of-order instruction execution [3] and non-blocking caching techniques will continue to be employed to help hide cache latency. Further explorations of way-prediction schemes are needed, because they are a powerful means of reducing access time [1]. Way-predictions require fast tag array access and effective recording of tag array access patterns. More levels of on-chip cache hierarchy can be introduced to reduce overall data access time and cache miss penalty. However, adding more levels of cache along with increasing bandwidth will inevitably increase total cache area, thereby die area, which in turn, will increase fabrication cost within the same process technology. Bringing DRAM on-chip has been a continuing effort made by industry and academia [15]. The most attractive thing about a DRAM is its high density. However, the drastically different DRAM process technology hinders the integration of a DRAM and the rest of the chip. Also, DRAMs have thermal tolerance different from other components of the chip. The increasing demand for high cache bandwidth will trigger innovative process integration technologies to be developed probably at higher costs initially. If DRAMS are indeed brought onto widely sold commercial chips one day, it will bring revolutionary changes to computer architecture and chip design.

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