Zero-forcing Electrical Filters for Direct Detection Optical Systems

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Abstract — Intersymbol interference in direct detection optical systems can limit the channel spacing in frequency division multiplexing and prevent multilevel signaling. We investigate a zero-forcing electrical filter to cancel intersymbol interference and compare its performance with a matched filter and a rectangular response filter, for *M*-ary amplitude modulation.

I. Model

In our model, the receiver front-end is composed of an optical filter, a photodetector and a low-pass electrical filter as shown in Figure 1. The photodiode is modelled as a square-law de-

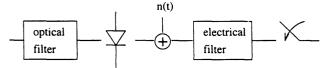


Figure 1: The receiver front-end includes an optical filter, a photodiode and a low-pass electrical filter followed by a baud rate sampler.

vice whose output is proportional to the magnitude square of the received signal envelope. The thermal noise n(t) from the electronics is assumed to be the dominant noise and is modelled as additive white Gaussian noise.

II. ZERO-FORCING FILTERS

Without loss in generality, we design the filter for sampling time t = 0. The output of the electrical filter at this time is

$$\sum_{i}\sum_{j}a_{i}a_{j}\int p_{i,j}(\sigma) h(\sigma)d\sigma + N, \qquad (1)$$

where h(t) is the *time-reversed* impulse response of the electrical filter, $p_{i,j}(t) = \operatorname{Re}\{p(t-iT)p^*(t-jT)\}, p(t)$ is the complex envelope of the received optical pulse taking into account the transmit pulse and the channel response, $p^*(t)$ is the complex conjugate of p(t), a_k (taken as real here) is the kth transmit amplitude, and N is the noise at the sampled output. We write the integral $\int p_{i,j}(t)h(t)dt$ as an inner product $\langle p_{i,j}, h \rangle$ where $\langle x, y \rangle \equiv \int x(t)y(t)dt$.

We define the ISI space, I, as the space spanned by $p_{i,j}(t)$'s without $p_{0,0}(t)$, the desired signal. The signal space is defined as the space spanned by I and $p_{0,0}(t)$. A filter h(t) is a zero-forcing filter if the sampled output has no ISI, i.e. we want the output of h(t) to depend only on a_0a_0 at sampling time t = 0. A necessary and sufficient condition for h(t) to be a zero-forcing filter is

$$\langle p_{i,j}, h \rangle \neq 0$$
, if $i = j = 0$, and
 $\langle p_{i,j}, h \rangle = 0$, otherwise. (2)

For filters that satisfy (2), we are interested in the one that minimizes the noise variance when $\langle p_{0,0}, h \rangle$ is set equal to a constant. The time-reversed impulse response of this filter, if it exists, is proportional to the component of $p_{0,0}(t)$ orthogonal to I.

III. FABRY-PEROT INTERFEROMETER

We consider a Fabry-Perot filter as the optical demultiplexing filter [1]. The envelope of the impulse response is well approximated by $\frac{1}{\tau}e^{-t/\tau}$ for $t \ge 0$. The envelope of the transmit pulse is equal to 1 in $[0, \frac{\log_2 M}{R}]$ and 0 otherwise, where M is the number of signaling levels and R is the bit rate. The symbol set is equal to $\{\sqrt{\frac{i}{M-1}} \mid 0 \le i \le M-1\}$. We keep the bit rate fixed and plot the normalized eye opening for different τ' , where $\tau' = \tau R$ is a parameter proportional to bandwidth efficiency in units of (b/s/Hz). The normalized eye opening is the vertical opening of an eye-diagram when the electrical filter has unit energy. We consider a filter matched to the postdetection electrical pulse $p_{0,0}(t)$ (single pulse transmitted), the minimum noise variance zero-forcing filter, and a filter with rectangular impulse response on $[0, \frac{\log_2 M}{R}]$. For the rectangu-

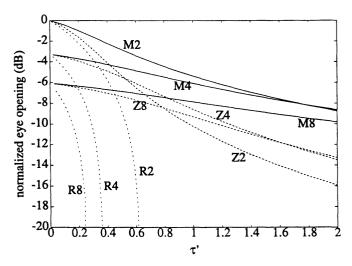


Figure 2: The optical filter is a Fabry-Perot interferometer. The curves are labelled as follows: (M) matched filter curve, (Z) zero-forcing filter, (R) rectangular filter, and (2,4,8) level signaling.

lar filter, there is no advantage to multilevel signaling, same as in [1]. On the other hand the zero-forcing filter performs much better and there is advantage to four level signaling for large values of τ' .

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References

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