Application of Robotic Technologies for the Fabrication Of Traditional Chinese Timber Joints

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The traditional Chinese building design was influenced by the climate and the sociogeographical conditions of the different regions in China. They were usually constructed out of wood relying on timber-joint based construction systems. Amongst the wide variety of the structural elements, the Dougong (bucket arch) is one of the most common components of traditional wooden framework buildings, presenting a high level of complexity. Parametric design and robotic technology enable new possibilities regarding its fabrication and application in contemporary architecture. Our paper will explore how the Dougong components could be reinvented through the use of parametric tools and robotic fabrication methods and thus applied to contemporary architectural structures. We will analyse and compare the properties of the original Dougong with the reinvented unit by using finite element analysis and digital optimization tools. Our findings will provide an insight into the traditional construction principles of the joint and how these can inform a design and fabrication framework for its application in contemporary buildings.

Keywords: *Dougong joint, timber structures, parametric design, robotic fabrication, optimization algorithm*

INTRODUCTION
A brief history of the Dougong joint
The Dougong bucket arch is an independent category, withing the traditional Chinese timber framework systems. It consists of many different types of Dou (square load-bearing member) and Gong (arch load-bearing member), (Liang, 2005). During the Qing dynasty, there were even specialised Dougong making craftsmen, called Dougong carpenters (Pan, 2011).

Historically, the main structure of traditional Chinese buildings is a load-bearing timber framework while the walls are part of the building. The roof's structural load is transferred from the beam purlin to the pillar into the structural system. There is a complex component named Dougong, which is a transition component between the beam purlin and the pillar. It has been a unique element of Chinese architecture for thousands of years. (Liang, 1985)

The earliest Dou appeared during the bronze age of the Shang and Zhou Dynasties, and the appear-

ance of Gong followed later (Pan, 2011). According to Yang Hongxun's 'Architectural Archaeology Study of Tomb Buildings, Murals and Burial Artefacts, the structure of Dougong had been widely used and achieved its mature stage since the Han dynasty, 206 BC-220 AD, (Liu, 1982).

The proportions and the name of the Dougong components before the Song Dynasty (960-1279) are difficult to retrieve since there are not related sources to refer to. However, two important historic rulebooks the Yin Zhao Fa Shi and the Gongchen Zuofa Zeli provide both standards and structural regulations for buildings and building components. The first was completed by Li Jie in the Song Dynasty (960-1279) while the second was published by the Ministry of Construction of the Qing Dynasty in 1734. In this paper, we mainly focus on studying the Dougong developed during the Qing dynasty (1636-1911) as a large number of buildings from this period have been preserved and can provide a reliable database for analysis.

Dougong types
The size, the structure, the technology and the materials of at least thirty different Dougong joints are recorded in the historic rulebook Gongchen Zuofa Zeli. They can be classified based on their function and position inside the building (Ma, 2003). A first classification can be obtained by dividing the Dugong into two main categories according to its position: a Dougong located in the extension of the building is called 'the external eave Dougong' and the one located inside the eaves is called 'the inner eave Dougong'. Furthermore, the external eave Dougong can be divided into an intermediate set, a column set and corner set (Ma, 2003). This paper will mainly focus on the external eave Dougong, and particularly the intermediate set (Figure 1).
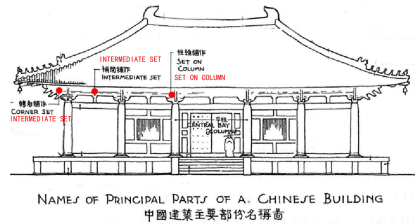

Figure 1
Principal parts of a Chinese timber-frame building. (Drawn by the 'Society for Research in Chinese Architecture')

Dougong components
The Dougong balances the weight of the roof and transfers its loads from the roof to the pillars. Traditionally it was built manually, requiring a significant amount of time for its completion. It is composed of five different components (Figure 2), which include: the Gong, Qiao, Ang, Dou, and Sheng, (Liang 2006).
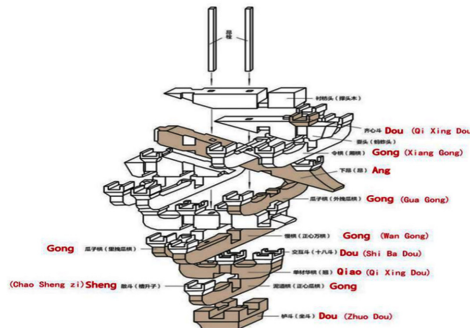

Figure 2
Components' of the Dougong

In modern years the ancient knowledge and applications of the Dougong are disappearing. We are confident that parametric design tools and robotic fabrication techniques could be used for the reinvention of the joint and ensure its survival into the modern era. In particular, our research will try to answer the following questions:

1. How can we simplify the Dougong elements by using parametric modelling tools and robotic fabrication techniques?

2. How could a reinvented joint be applied in contemporary architecture?

To achieve this we will start by studying different cases studies which have applied robotic technology to reproduce wooden joints. We will then propose a framework which will integrate the traditional construction and design principles embedded in the Dougong and will allow us to reinvent the ancient joint.

RESEARCH CONTEXT AND LITERATURE

Digitalisation and robotic reproduction of elements of a Japanese traditional timber system are being described by Takabayashi et al. (2018). In their experiment, the Japanese team introduced a novel method for the robotic reproducing a roof corner detail of a Japanese pagoda by using five tools; a circular saw, a square chisel, a vibration chisel, a router and a five axes KUKA KR 6R 700 robotic arm to reproduce the different joint components. The robotic toolpath was generated by a specifically developed CAM programme. As Japanese timber systems are based on Chinese systems, this method provides valuable insights into designing and creating Chinese joints too. However, this study does not attempt to reinvent the traditional elements, neither examines their application on modern-day design driven by robotic technology and parametric design tools.

The research team led by Mikayla and Kevin (2018) investigated the use of parametric tools and robotic technology to reproduce traditional joints, suitable for contemporary architectural applications. They employed a 6-axis ABB IRB 6700 robotic arm and the HAL Grasshopper plug-in, to produce a set of physical prototypes using mortise splices and curved splices in their attempt to explore possible new joints. As a starting point, the researchers fabricated a simple physical model by using a CNC mill to identify possible deficiencies. The data from that first experiment helped them to identify and resolve issues before proceeding with the robotic fabrication.

The research team led by Böhme explored the potential of applying robotic fabrication for the reconstruct a historical joint employing parametric tools and a KUKA KR125/2 and Agilus KR6 R900 Sixx robotic arms. The experiment's findings suggested that the process can be successful without modifying the joint's geometry.

The team led by Yuan Feng explored how to use a 5 axis CNC router to design and fabricate a structural installation based on a traditional Chinese eaves rafter. Firstly, they analyzed the bending moments of the joint by using the Grasshopper plugin Millipede. After finding out about the underlying structural principles, they designed an umbrella-shaped structural installation by using a unit based on the traditional rafter proportions. In the structural simulation stage, the topology function was applied to optimize the dimensions of the unit before proceeding with its robotic fabrication.

Chai and Yuan, (2018) fabricated a complex wooden pavilion at the University of Tongji, using a gantry robotic system and the Grasshopper plugin Karamba3D, as well as a KUKA R2700 robotic arm. They developed a band-saw end-effector and applied it to fabricate curved wooden beams and mortise-tenon joints. The experiment proves that robotic arms can fabricate complex wooden structures with their band-saw end-effector more efficiently and accurately than with a CNC mill.

Finally, in a case study conducted at the University of Sydney (Mitchell, 2017), Dove, an open-source software plugin was used for developing a 3D model of a timber joint. The physical prototype was fabricated by a KUKA KR60 6-axis robot and a milling spindle end-effector. They have also developed a tool, which is reducing milling time, simplifying the too paths and saves material.

All the projects presented here are investigating how to reproduce building components or building parts by employing robotic technology based on the proportions of the original structure. In contrast, our work will focus on how we could re-invent the Dougong joint, thus to apply it in contemporary design solutions.

METHODOLOGY

Our research method consists of a design experiment and its validation via digital simulation and physical prototyping. In particular, our method includes four main phases and a feedback loop.

In phase one we will analyse the Dougong's components and proportions, based on sources referring to the Qing dynasty, where the Doukou system (bucket mouth system) is used as a standard unit for each building module. This system is an optimised version of the Caifen system, which was developed during the Song dynasty.

In the second phase, we will simplify the joint and develop a digital, parametric modelling framework of a novel design unit, with references to the proportions and the structural properties of the traditional Dougong as well further geometrical properties allowing it to be robotically fabricated.

Phase three includes the structural simulation and optimisation of the design unit. We will test both a linear and a non-linear structure using the Millipede plug-in for Grasshopper. Phase three will also include a robotic fabrication simulation using the firmware RoboDK and Grasshopper. A feedback loop to face two is included here, making sure that all simulation results will feedback into the original design starting point. Finally, in phase four, which will not be included in this paper, we will proceed to the validation of or design framework via a physical prototype using a CNC mill and UR 10 robotic arm. The CNC milled prototype will help us to optimize the fabrication process, prior to its final fabrication destination, the UR10 robotic arm. That will also include the development of the appropriate end-effectors. This paper will cover the proportion and mechanical properties study of Dougong, the design methods of the unit, the assembly possibility of the unit, and the simulation and optimization of the unit in Millipede (Figure 3).

DESIGN EXPERIMENT

As previously described, our design experiment consists of the analysis of the traditional Dougong proportions and design rules, as well as the parametrisation of a novel design unit. Firstly, we will study Dougong's proportions by reviewing the two rule books mentioned previously. We will then design the unit according to the mechanical properties as described by Yuan (2012), using the proportions and connection methods as recorded in the books Qishi Yin Zhao Zeli (Liang, 2006) and Gong Chen Zuo Fa (Liang, 2006) and the Chinese ancient archi-
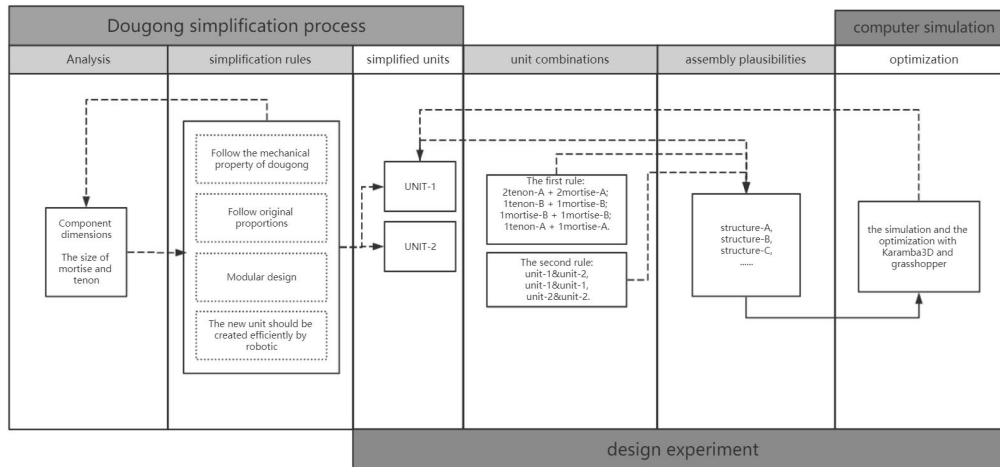

Figure 3
Research
methodology
framework

Rule table of the intermediate set (unit: Dou)			
Component name	Length	Width	Height
base block(大斗)	3	3	2
the first transverse bracket arm(单翘)	7.1	1	2
the second transverse bracket arm(重翘)	13.1	1	2
axial oval arm（正心瓜拱）	6.2	1.24	2
axial long arm（正心万拱）	9.2	1.24	2
the first cantilever arm（first-ang）（头昂）	base on the kind of dougong	1	ahead 3, back 2
the second cantilever arm（second-ang）（二昂）	base on the kind of dougong	1	ahead 3, back 2
the third cantilever arm（third-ang）（三昂）	base on the kind of dougong	1	ahead 3, back 2
tail end of *grasshopper headwith sharp poinyed cutout treatment*（shua-tou）（耍头）	base on the kind of dougong	1	2
uppermost piece parallel to *ang* or *qiao* with hempleaf shaped end （撑头木）	base on the kind of Dougong	1	2
outward and inward oval arms（单才瓜拱）	6.2	1	1.4
outward and inward long arms（单才万拱）	9.2	1	1.4
outward and inward regular arms（厢拱）	7.2	1	1.4
purlin socket piece（桁碗）	base on the kind of Dougong	1	base on the kind of Dougong
connection block（十八斗）	1.8	1.48	1
small block（三才升）	1.3or1.4	1.48	1
center block（曹升）	1.3or1.4	1.72	1

tecture woodwork construction technology manual (Ma, Bingjian. 2003). In parallel, other parameters contributing to the efficient robotic fabrication of the unit and its clusters will be applied.

Analysis

There are eleven classes in the Doukou system . The width of the first-class Dou is 19.2cm, thus the width of one Doukou is 19.2cm. Each class is linked to a particular building function and any change from class to class is based on the formula:

1 Dou = 19.2cm + (11- N) * 0.5 Cun, (1Cun=3.33cm), N: the class of Cai (1, 2, 3, 4, ..., 11); Cun is the traditional unit of length in China.

We will use the table and the formula to design all components for our design experiment. The intermediate set will be explored firstly, as described by Ma (2003) in table 1. The distance of the main stress points is 3 Dou according to the proportion analysis of the Dougong components (Table 1). The connection method of the components is based on the principle of mortise and tenon. A tenon is usually located between two stress points. Two stress points are connected with a mortise. One Dougong element is composed of at least one tenon and two mortises.

Parametric design framework of novel design unit

The new unit should respect the proportions and the structural properties of the traditional Dougong allowing the unit to be fabricated by a robotic arm. A way to do that is by minimizing it to the way the components are being connected as well as its mechanical properties as demonstrated in figure 4, (Yuan et al. 2012). We have chosen the second layer of an interlocked bracket set including the first transverse bracket arm and the axial oval arm as shown in Table 1. The length, the width and the height of the two elements are adjusted to integers, the decorative elements and the complex curve can be removed aiming to improve the effectiveness of its robotic fabrication (Table 2).

Rule table of Unit 1 and Unit 2(unit: Dou)		length	width	height
component name		length	width	height
connect ways	tenon.A	0.5	0.5	0.5
	tenon.B	1	1	0.5
	mortise.A	0.5	0.5	0.5
	mortise.B	0.5	0.5	0.5
Unit 1		6	1	2
Unit 2		6	1	2

Dimensional structure of dougong

Layer substructure of dougong

The size of Dou

Tenon–A

Tenon–B

sessing seven design units, A, B, C, D, E, F and G (Figure 8). The key element of structure A is P1.2 (possibility1.3), and the key elements of structure B are P1, P1.2, and P3.3. The connection method of the two structures is P2.2 and P3.2. P1.1 is applied in structure C as the key element. Structure D consists of the P3.3 unit, the structure E consists of the P3, P2 and P1.2 units, and the structures F and G consist of the P1.2 unit.

The structure was developed by two basic rules: Rule one is based on the combinations of unit 1 & unit 2, unit 1 & unit 1 and unit 2 & unit 2. Rule two is based on the combinations of 2 tenon A + 2 mortise A; 1 tenon B + 1 mortise B; 1 mortise B + 1 mortise B; 1 tenon A + 1 mortise A. The & symbol indicates the combination of two units. For example, unit 1 & unit 2 means one element consists of unit 1 and unit 2. The '+' symbol indicates the connection method of two units. For example, 2 tenon A + 2 mortise A means that the two tenon A of one unit connects with the two mortise A of another one unit.

SIMULATION AND OPTIMIZATION

The optimization and simulation process consists of two parts. The first part includes the comparison of the mechanical properties of the original Dougong with those of the new unit by using the plugin Millipede. The second part focuses on optimizing the cross-section of the new unit employing a genetic algorithm by using the Galapagos plugin for Grasshopper. The max-deflection of the structure will be minimized after optimization, which will enhance its stiffness. We chose to analyse and optimize the P1.2 joint, as it is very similar to the original Dougong. The new unit is built based on the first Cai level, equal to one Dou (19.2 cm) x 1.5 Dou (28.8cm) x 6 Dou (115.2cm).

The optimisation of the joint is focusing on the values of three main parameters: the Young's Mod-

We have parametrized the two main Dougong units in Grasshopper (Figure 6). The units are composed of four elements: tenon A, tenon B, mortise A and mortise B (Figure 5).

There are three main rules of connection possibilities (Table 3): unit 1 & unit 2, unit 1 & unit 1 and unit 2 & unit 2. Furthermore, every connection type includes three different unit groups: the square-shape (P1, P2, and P3), the T-shape (P1.1, P2.1, and P3.1), the cross-shape (P1.2, P2.2, P3.2) and L-shape(P1.3, P2.3, and P3.3) respectively, which is the basic shape of the assembly (Figure 7). According to these rules, the combination of different units will produce different results of assembly. In this study, we are as-

| RULE	2tenon.A + 2mortise.A	1mortise.B + 1mortise.B	1tenon.A+ 1mortise.A	1tenon.B + 1 mortise .B
unit-1&unit-2	P1(possibility1)	P1.1(possibility1.1)	P1.2(possibility1.2)	P1.3(possibility1.3)
unit-1&unit-1	P2(possibility2)	P2.1(possibility2.1)	P2.2(possibility2.2)	P2.3(possibility2.3)
unit-2&unit-2	P3(possibility3)	P3.1(possibility3.1)	P3.2(possibility3.2)	P3.3(possibility3.3)
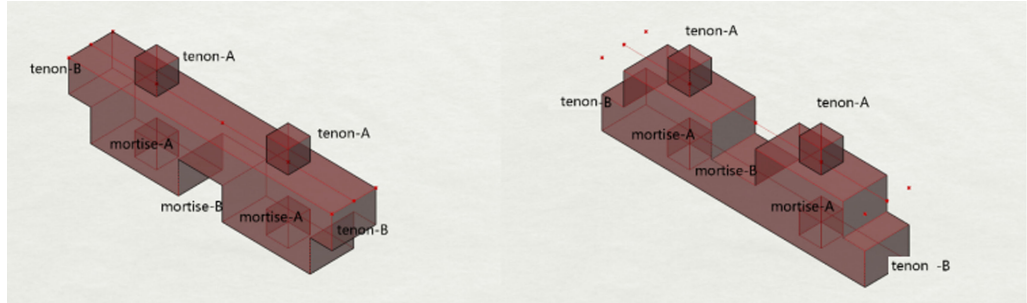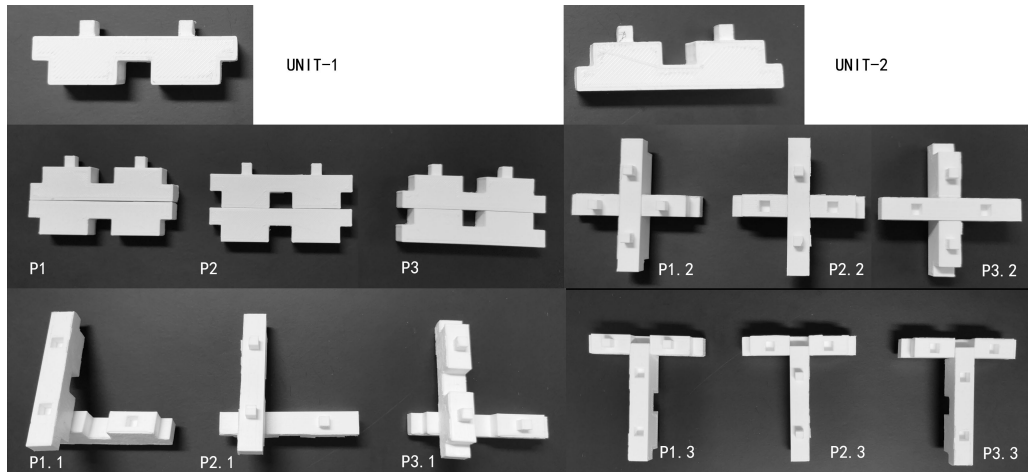
ulus, the Poisson's ratio and the mass density. The Young's Modulus is used to measure the stiffness of solid materials, while the Poisson's ratio describes the contraction of a material in the direction of loading. We will compare the displacement on 4 points on the z-axis of the two structures (Figure 9). We are assuming that the structures are subjected to a uniform load of 1000 N/m^2. According to the Millipede analysis results, the displacement of the four points on the original Dougong is 1.04e-6 m, 1.21e-6 m, 1.08e-6 m, and 9.92e-7 m. The displacement of the points on the P1.2 joint is 1.06e-6 m, 1.25e-6 m, 1.10e-6 m and 1.08e-6 m. The difference between the displacement of the four points is only 0.02e-6 m, 0.04e-6m, 0.02e-6m, and 0.08e-6m, which proves that the mechanical properties of the original Dougong and the new unit are similar.

The second part focuses on optimizing the cross-section of the new unit by using the Galapagos plugin for Grasshopper. We chose the P1.2 joint, as the object of the analysis due to its similarity to the original Dougong. We have used the same property values as in the previous simulation. The max-deflection of the structure is 1.375e-6m and 1.055e-6 m before

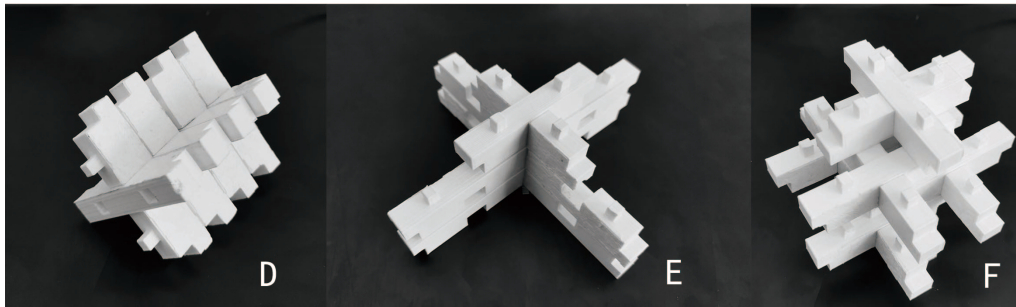Figure 8
The different assembly possibilities of the reinvented Dougong elements
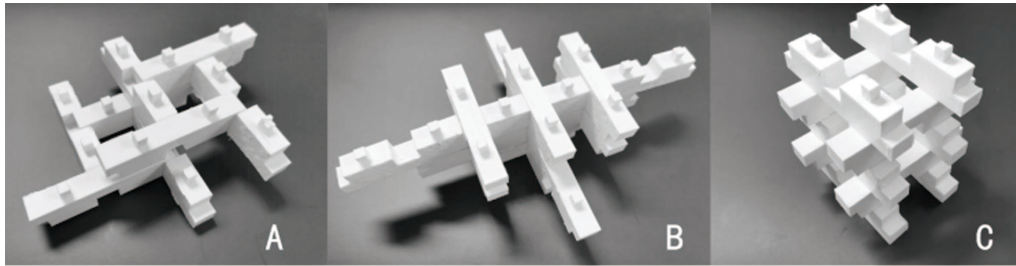
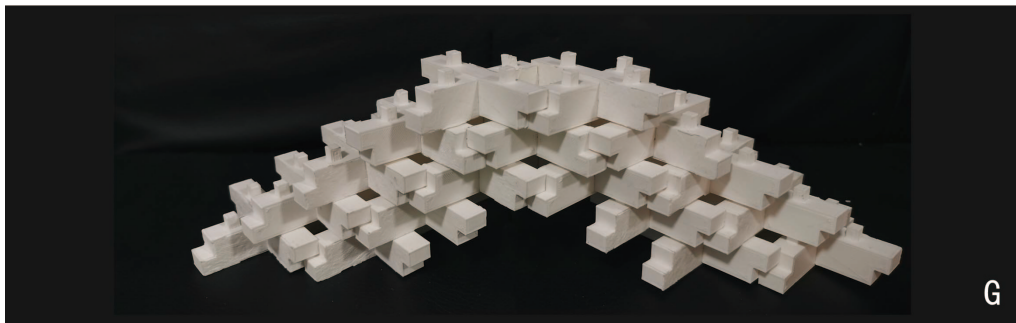Structure-A: (P2.3) +(P2.3)   Structure-B: (P1) + (P1.2) + (P3.3)   Structure-C: P1.1

Structure-D: P3.2   Structure-E: (P3)+(P2)+(P1.2)   Structure-F: P1.2

Structure-G: P1.2

and after optimization. The new width and height of the cross-sections of the two units are 1.12 Dou (21.5cm) and 1 Dou (19.2cm), (Figure 10). The volume of one unit is 0.051 mˆ3 and 0.038 mˆ3 before and after optimization.

Figure 9
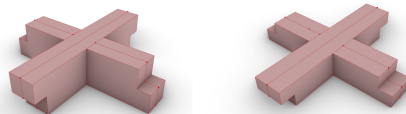The four points used on the displacement analysis

Figure 10
The digital model of the P1.2 joint (left) before optimization and the model (right) after optimization in Millipede

DISCUSSION AND CONCLUSION

The paper is exploring a strategy for simplifying the elements of Dougong to make it more suitable for contemporary architectural applications. According to the mechanical properties and proportions of the Dougong, we simplified two elements of the interlocking bracket set via adjusting the dimensions to integers and removing the decorative elements and the complex curves. Furthermore, we designed two units and defined two rules of connecting the units based on the original connection of Dougong. The inter-combination of the unit will form different assembly possibilities following the described rules. We have explored seven assembly possibilities and simulated a connection structure in the Millipede. The cross-section of the unit was optimized to be 1.12 Dou in width, 1 Dou in height.

After analysing the results we have concluded to the following: firstly, the displacement differences between the points of the original Dougong and the connection P1.2 are only 0.02e-6 m, 0.04e-6m, 0.02e-6m, and 0.08e-6m, which proves that the properties of the two structures are similar, thus our design method is feasible. The volumes of the two structures are 0.157mˆ3 and 0.102mˆ3, which means that the material usage of the new unit is less than the one in the original Dougong. Secondly, when the cross-sectional size of the new unit is 1 Dou in height and 1.11 Dou in width, the volume of the structure P1.2 should be 0.076 mˆ3 according to the optimization. However, the volume value before the optimization was 0.102 mˆ3. The difference is 0.026 mˆ3, which means that the material usage of the unit could be reduced. At the same time, the difference between the max-deflection of the structure is 3.2e-7m, which means that the property of the structure is enhanced. Overall, it becomes evident that the simplified and optimized joint has the potential to be integrated into design solutions, as it does not only have a very similar structure and mechanical properties with the original joint but also has a simpler shape and uses less material.

However, as we currently only focused on the intermediate Dougong set, we will continue applying this method to design a new unit based on the study of the set on the column and the corner set, and finally, make a data table to facilitate the robotic process of the wood unit. We will also explore the specific use of these structures on modern designs, such as the structure of the bridge and the structure of the pavilion, all of which need to be completed in cooperation with robot technology and Millipede.

IMAGE CREDITS

Figure 4: Yuan, JL, Shi, Y, Chen, W and Wang, J 2012, 'Finite element model of Dou-Gong based on energy dissipation by friction-shear', Journal of Building Structures, 06, p. 33.

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[1] https://manual.karamba3d.com/appendix/a.4-back ground-information/a.4.3-tips-for-designing-statically-f easible-structures#table-a-2-3-2-loads-for-typical-scena rios