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### **Propagation probability and spread rates of self-sustained smouldering fires under controlled moisture content and bulk density conditions**

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1 **Propagation probability and spread rates of self-sustained**  
2 **smouldering fires under controlled moisture content and bulk density**  
3 **conditions**

4

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13

14 **Abstract**

15 The consumption of large areas of peat during wildfires is due to self-sustained  
16 smouldering fronts that can remain active for weeks. We study the effect of peat  
17 moisture content and bulk density on the horizontal propagation of smouldering fire in  
18 laboratory-scale experiments. We used milled peat samples at moisture contents  
19 between 25% and 250% *MC* (mass of water per mass of dry peat) and bulk densities,  
20  $\rho$ , between 50 and 150 kg m<sup>-3</sup>. The samples were burnt inside an insulated box of  
21 22×18×6 cm. An infrared camera monitored the ignition, spread and extinction. Peats  
22 below 150% *MC* are likely to self-sustain smouldering for more than 12 cm when  $\rho$   
23 was below 75 kg m<sup>-3</sup> (expected fraction of peat burnt = 0.5). When  $\rho$  was 150 kg m<sup>-3</sup>,  
24 the critical moisture content for self-sustained propagation was 115% *MC*. A linear  
25 model estimated a significant effect ( $R^2=0.77$ ) of *MC* and  $\rho$  on the fire spread rate  
26 ranging between 2 and 5 cm h<sup>-1</sup>. The increase of *MC* had a stronger effect on the spread  
27 rate than the increase of  $\rho$ . The variation of  $\rho$  had a higher effect on the spread rate when  
28 *MC* was low than when *MC* was high.

29

30 **Brief summary**

31 We have coupled laboratory scale observations of smouldering fires with statistical  
32 models to analyse the self-sustained propagation and spread rates for horizontal  
33 distances which have not been researched before. Our findings enable the effects of

34 peat moisture and density conditions on smouldering propagation dynamics to be  
35 understood.

36

37 **Additional Keywords:** peatland, fire behaviour, horizontal front, lateral, peat fire,  
38 propagation dynamics.

39

## 40 **Introduction**

41 Smouldering is an incomplete form of combustion affecting organic materials, such as  
42 the peat stored in peatlands and forest soils (Rein 2009). The propagation of  
43 smouldering fires is known to be very slow compared to flaming fires, moving at few  
44 centimetres per hour (Wein 1983, Frandsen 1991). The consumption of large areas of  
45 peat is often caused by self-sustained smouldering fires, which remain active and  
46 slowly propagating for weeks or months (Rein 2013).

47 During a peat fire, the carbon stored in the ground is released to the atmosphere. The  
48 incomplete smouldering combustion in peat emits a higher proportion of carbon  
49 emissions (e.g. CO, CH<sub>4</sub>) than flaming fires in vegetation (Hadden 2011). These gasses  
50 contribute significantly to global emissions of greenhouse gases (Turetsky et al. 2014).  
51 Smouldering peat fires also affect the roots of vegetation close to the surface, often  
52 causing lethal plant damage and habitat losses (Miyanishi and Johnson 2002; Page et al.  
53 2002; Davies et al. 2013). The landscape after a peat fire is often heterogeneous, as peat  
54 is consumed in irregular patches (Shetler et al. 2008). In the burnt areas, deep layers of  
55 dense peat become the new surface with a different constitution and properties (Prat-  
56 Guitart et al. 2011). These post-burn surfaces are often opportunities for colonising  
57 species and have the potential to enhance biodiversity (Benscoter and Vitt, 2008).

58

### 59 *Factors driving smouldering fire ignition*

60 The ignition of a smouldering fire in peat is often caused by a heat source near the  
61 surface, such as a lightning strike, adjacent flaming vegetation (Rein 2013) or burning  
62 pine cones (Kreye et al., 2013). The start of a smouldering fire is controlled by the  
63 properties of the ignition source (intensity and duration), peat conditions (primarily  
64 moisture content, bulk density and mineral content) and the oxygen availability  
65 (Frandsen 1987; Ohlemiller 2002; Hadden et al. 2013; Huang and Rein 2014). Of these,  
66 peat moisture content is the main factor limiting the ignition of peat (Van Wagner 1972;  
67 Frandsen 1987, 1991). Water in peat acts as a heat sink, requiring a large amount of  
68 energy to evaporate the water before reaching temperatures at which the pyrolysis  
69 process begins (Rein 2013). The probability of peat ignition and initial horizontal  
70 propagation of at least 10 cm from an ignition source has been estimated in previous  
71 studies (Frandsen 1997; Lawson et al. 1997; Reardon et al. 2007). When the moisture  
72 content (*MC*) of the peat is between 110 and 200% (gravimetric moisture content, mass  
73 of water per mass of dry peat expressed as a percentage) there is a 50% probability of

74 starting a smouldering peat fire (Frandsen 1987; Frandsen 1997; Reardon et al. 2007;  
75 Rein et al. 2008). Frandsen (1997) predicted the probability of ignition and early  
76 horizontal propagation as a function of *MC* (%), mineral content (%) and bulk density  
77 ( $\text{kg m}^{-3}$ ). Reardon et al. (2007) however, predicted the ignition and early propagation  
78 using only moisture and mineral content, suggesting that bulk density was implicitly  
79 included in the quantification of the other two peat properties.

80

### 81 *Self-sustained smouldering propagation*

82 Once ignited a smouldering fire propagates by drying and igniting the fuel ahead of the  
83 smouldering front (Frandsen 1997; Huang et al. 2015). In smouldering combustion,  
84 peat particles undergo endothermal pyrolysis forming char, also known as regime I,  
85 followed by exothermal oxidation reactions where char is converted to ash, regime II  
86 (Hadden et al. 2013, Huang et al. 2015). The energy released during the exothermal  
87 oxidations is transferred to the surrounding environment, some being radiated to the  
88 atmosphere and some conducted to the peat particles ahead of the smouldering front. If  
89 the energy of this combustion of peat particles in the smouldering front produces  
90 sufficient energy to overcome the heat losses to the surroundings, the smouldering front  
91 spreads away from the ignition point and become an independent self-sustained front  
92 (Ohlemiller 1985). A smouldering front can then propagate into the peat both vertically  
93 and horizontally. However, it is the front propagating horizontally that is primarily  
94 responsible for the large areas of peat consumed, as vertical propagation is generally  
95 extinguished by deeper layers of wet peat (Wein 1983; Miyanishi and Johnson 2002;  
96 Usup et al. 2004). The propagation mechanisms of smouldering fires in peats are  
97 complex and further research is needed to understand how the peat conditions affect  
98 the dynamics of self-sustained fire propagation.

99 In this paper, we analyse the horizontal propagation dynamics of smouldering fires  
100 moving away from an ignition source under a range of controlled moisture content and  
101 bulk density conditions. We used beta regressions to estimate the propagation distance  
102 as a function of moisture content and bulk density. We also estimate the spread rate of  
103 the fire when self-sustained smouldering propagation was observed. Finally we use a  
104 linear model to relate the properties of the peat to the spread rate of smouldering fires.  
105 The purpose of this experimental research is to enable key peat conditions (moisture  
106 content and bulk density) that influence smouldering propagation to be understood.

107

108

## 109 **Materials and methods**

### 110 *Experimental set-up*

111 Laboratory smouldering experiments were designed to control environmental and peat  
112 conditions. Commercial milled peat (*Shamrock Irish Moss Peat*, Bord Na Mona,  
113 Ireland) was used to be consistent with previous studies (Belcher et al. 2010; Hadden  
114 et al. 2013) and because commercially milled peat reduces extraneous sources of  
115 variation due to their homogeneous properties (Frandsen 1987, 1991; Zaccone et al.  
116 2014; Prat et al. 2015). The peat was placed in a 22×18×6 cm insulated burnbox made  
117 of fibreboard with a thermal conductivity of 0.07-0.11 W m<sup>-1</sup> K<sup>-1</sup>, similar to peat  
118 (Frandsen 1987, 1991; Benschoter et al. 2011; Garlough and Keyes 2011). Peats were  
119 oven dried at 80°C for 48 h. Water was added to the dry peat until the required *MC* was  
120 achieved. The moist peat was sealed in a plastic bag for the 24 h prior to the experiment  
121 to allow equilibration. The prepared peats had 25, 100, 150, 200 and 250% *MC*. This  
122 range of moisture contents represents peat conditions that are susceptible to  
123 smouldering ignition (Frandsen 1987; Rein et al. 2008; Benschoter et al. 2011).

124 A range of peat bulk densities ( $\rho$ , dry mass of peat per unit volume of wet peat) was  
125 included in our experimental data. Two bulk density treatments ( $BD_1$ ,  $BD_2$ ) were  
126 created for each moisture content 1) the peat was spread into the burnbox until it filled  
127 the volume ( $BD_1$ ) and 2) the peat was compressed into the burnbox until it filled the  
128 volume ( $BD_2$ ). This second treatment increased bulk density by reducing the bulk  
129 volume and the air spaces inside the sample.

130 An electric igniter coil was situated along one side of the box and used to ignite a 2 cm  
131 wide section of dry peat (approximately ~0% *MC*). The coil delivered 100 W for 30  
132 min, similar to the heat provided by surface burning vegetation (Rein et al. 2008). This  
133 ignition protocol was sufficient to start a smouldering front in the dry peat section,  
134 which then attempted to spread to the adjacent peat sample. An infrared camera  
135 (*ThermaCAM SC640*, FLIR Systems, US) was used to image the radiative energy flux  
136 from the smouldering peat surface (Prat-Guitart et al. 2015). The position of the  
137 smouldering front was identified using the infrared images, which provided information  
138 at a resolution of 0.05×0.05 cm (one pixel). The camera took images every minute,  
139 creating sequences of between 300 and 700 images for each burn test. Experiments for  
140 each combination of *MC* and bulk density treatment were replicated four times. Due to  
141 a small amount of moisture evaporation ([Table S1](#) in [Supplementary Material](#) available

142 from the journal website), the moisture content conditions of the peat samples were  
143 assumed to be constant throughout the duration of the burning experiments.

144

#### 145 *Self-propagation distance of peat fires*

146 Once the fire self-extinguished, we recorded the final position of the smouldering at  
147 distance ( $D$ ) away from the igniter. A value between 0 and 1 indicated the fraction ( $y$ )  
148 of peat consumed along a transect across the width of the burnbox at distance  $D$  from  
149 the igniter. These fractions were transformed to avoid zeros and ones by  $y_D = [y$   
150  $(N-1)+1/2]/N$ , where  $N$  is the sample size (Smithson and Verkuilen 2006). Beta  
151 regressions were used to estimate the association of  $y_D$  to the peat's bulk density  $\rho$  (kg  
152  $m^{-3}$ ) and moisture content,  $MC$ , with a logit link function for the expectation of  $y_D$  given  
153 by <equation 1>

154

$$155 \quad P_{y_D} = 1 / \left( 1 + \exp(-(\beta_D + \beta_{D1} \rho + \beta_{D2} MC)) \right) \quad (1)$$

156

157 where  $\beta_D$ 's are the regression coefficients. A total of seven beta regressions were fitted  
158 for values of  $D$  at 6, 8, 10, 12, 14, 16 and 18 cm. Each regression was a different analysis  
159 to avoid autocorrelation of residuals. A beta regression can be viewed as a flexible form  
160 of logistic regressions that allows for a continuous response variable (modelled by beta  
161 distribution) and skew in the response distribution (modelled by the precision parameter  
162 of beta distribution) (Cribari-Neto and Zeileis 2010). Similar to our beta regressions,  
163 logistic regressions were used in past studies with success/failure data to estimate the  
164 probability of peat ignition and early propagation 10 cm away from the ignition region  
165 (Frandsen 1997; Lawson et al. 1997; Reardon et al. 2007).

166

#### 167 *Image processing*

168 The infrared images were corrected for the distortion caused by the angle of the infrared  
169 camera. The burnbox surface area was represented by approximately 150,000 pixels,  
170 each of them giving information about the dynamics of the smouldering front during  
171 the experiment. For every pixel, we built a profile of the radiated energy flux throughout  
172 the time duration of the burn (Prat-Guitart et al. 2015). The radiative energy flux  
173 increased when an approaching smouldering front heated the area, indicating that the  
174 peat was being dried prior to the start of the combustion processes, pyrolysis and

175 oxidations. The start of the smouldering combustion ( $t^L$ ) was defined as the first time a  
 176 pixel's radiative energy flux increased at a rate of  $10 \text{ W m}^{-2} \text{ min}^{-1}$  or more. For every  
 177 experiment, we obtained a matrix of  $t^L$  giving the time when the leading edge of the  
 178 smouldering front reached each pixel.

179 As a method to prevent boundary effects from the burnbox edges to the smouldering  
 180 front, 2 cm of pixels close to the sides were removed from each image. The pixels from  
 181 the 6 cm closest to the igniter were also excluded to avoid effects of the ignition heating  
 182 coil. The area of pixels left, approximately 60% of the burnbox surface, was used for  
 183 the subsequent image analysis and estimation of the spread rates. The image processing  
 184 was undertaken using Matlab and the *Image Processing Toolbox* (Version R2012b  
 185 8.0.0.783, The MathWorks Inc., US).

186

### 187 *Estimation of horizontal spread rates*

188 For each burn we split the  $t^L$  matrix into sub-regions of  $2 \times 2$  cm. We then estimated the  
 189 spread rate and direction of spread for each sub-region by fitting a Generalised Least  
 190 Squares model, assuming a linear smouldering front across the sub-region. This  
 191 approach allows all the data within a sub-region to inform our estimates of spread rate  
 192 and direction. The fitted model is <equation 2>

193

$$194 \quad t^L_i = \beta_{xy0} \beta_x x_i + \beta_y y_i + \varepsilon_i \quad (2)$$

195

$$\varepsilon_i \sim N(0, \sigma^2 A)$$

196

197 where  $x$  and  $y$  are the position of the  $i^{\text{th}}$  pixel within a sub-region. The coefficients  $\beta_x$   
 198 and  $\beta_y$  give the rate at which  $t^L_i$  increases per unit increase in  $x$  and  $y$ , respectively. The  
 199  $\varepsilon_i$  is the error term assumed to be normal distributed with mean zero and with variance-  
 200 covariance matrix  $\sigma^2 A$ . The spatial correlation structure of  $A$  was described with a  
 201 Gaussian semivariogram (Pinheiro et al. 2013). The model was fitted using a maximum  
 202 likelihood. The spread rate of the leading front in the  $x$ -direction was then estimated as  
 203 <equation 3>

204

$$205 \quad S = \frac{1}{\beta_x} \Delta x \quad (3)$$

206



207 where  $S$  is the sub-region spread rate,  $\Delta x$  is the length of a pixel (typically 0.05 cm). A  
208 spread rate was estimated for each sub-region of the burnbox and then a median spread  
209 rate ( $\bar{S}$ ) and median absolute deviation were estimated for each experimental burn.  
210 We looked for detectable changes in spread rate during the long burns (burns lasting  
211 more than 7 h). We tested the constancy of the smouldering spread rate away from the  
212 igniter ( $x$ -direction) across the entire burnbox by regressing the median time taken for  
213 the smouldering front to reach a pixel against linear and quadratic terms in the distance  
214 from the igniter (see [supplementary material](#)). The quadratic term is expected to be zero  
215 if spread rate is constant. For each treatment the significance of the quadratic term was  
216 tested using F-test.

217

218

219 *Effect of moisture content and bulk density on the spread rate*

220 The effect of  $MC$  and  $\rho$  on  $\bar{S}$  were examined using a linear model. Even though the bulk  
221 density of the peat was based on a compression treatment ( $BD_1$  and  $BD_2$ ) we took bulk  
222 density to be a continuous variable. The two explanatory variables were standardised  
223 (by subtracting the mean and dividing by the standard deviation). Spread rates were  
224 log-transformed so that model residuals were close to normality. Forward stepwise  
225 model selection was used to arrive at a best-fit model that minimized Akaike  
226 Information Criterion, AIC (Burnham and Anderson 2002). Only the model with the  
227 lowest AIC is reported in the results. [<equation 4>](#)

228

$$229 \quad \log(\bar{S}) = \beta_0 + \beta_1 MC_k + \beta_2 \rho_k + \beta_3 MC_k \times \rho_k + \varepsilon_k \quad (4)$$

230

231 where  $\bar{S}$  is the median spread rate of each burn  $k$ ,  $\beta_0$ ,  $\beta_1$ ,  $\beta_2$  and  $\beta_3$  are the coefficients  
232 of the dependent parameters and  $\varepsilon_k$  are the residuals assumed to be normal distributed.  
233 The data analyses were done with R project statistical software (Version 3.0.2, R Core  
234 Team, 2013), the *betareg* package (Cribari-Neto and Zeileis, 2010) the *ape* package  
235 (Paradis et al. 2004) and the *nlme* package (Pinheiro et al. 2013).

236

237

238 **Results**

239 The milled peats used had an intrinsic bulk density between 50 to 150 kg m<sup>-3</sup> (Fig. 1).  
240 Each MC treatment had a range of bulk densities. Peats with low moisture content  
241 tended to have higher bulk densities than peats with high moisture content (*Spearman*  
242 *correlation* = -0.4, *p-value* =0.02).

243

244 [Figure 1]

245

246 The smouldering front always self-propagated across the entire box (20 cm) when the  
247 moisture content was 25% or 100% (Fig. 2). At these moisture contents, the  
248 smouldering fire was observed to propagate as a single linear front. The smouldering  
249 front always self-extinguished before reaching the end of the burnbox in peats of 200%  
250 and 250% MC. The fronts that self-extinguished were irregular for the last 1-2 cm of  
251 propagation. Peats with 150% MC had an intermediate behaviour, with fronts self-  
252 extinguishing in 75% of the experiments burns (Fig. 2a). Peats with 200% and 250%  
253 MC did not self-sustain propagation in peats with high bulk density. Only peats with  
254 100% MC (low and high bulk density) and peats 150% MC and low bulk density  
255 sustained smouldering for more than 7 h. For these long burns we found no evidence  
256 that the spread rate was changing across the burnbox, as indicated by the non-significant  
257 quadratic term for each of the peat conditions (F-tests for peats with 100% and low bulk  
258 density  $F_{1,48}=1.2, p=0.28$ , 100% and high bulk density  $F_{1,49}=2.9, p=0.09$  and 150% MC  
259  $F_{1,31}=2.0, p=0.17$ ).

260

261 [Figure 2]

262

263

264 *Expected self-propagation distances from an ignition source*

265 Peats at low moisture content were more likely to sustain smouldering propagation for  
266 a longer distance independently of the peat density (Fig. 3). For example, at  $D = 12$  cm  
267 peats with 25% and 100% MC had an expected fraction of peat burnt ( $P_{yD}$ ) of 0.72. At  
268 short distances (between 6 and 10 cm from the ignition region),  $P_{yD}$  was associated with  
269 both the moisture content and the bulk density of the peat (Table 1). Whereas  $P_{yD}$  at  
270 longer distances ( $\geq 12$  cm away from an ignition area) were mainly controlled by the  
271 moisture content of the peat (Table 1,  $D=12$  cm, Fig. S1).

272

273 [Figure 3]

274

275 [Table 1]

276

277

278 *Effect of peat condition on the smouldering spread rates*

279 The spread rates estimated per sub-region,  $S$ , ranged between 0.6 and 9.1 cm h<sup>-1</sup> (Table  
280 2). Due to self-extinction of the fire, experimental burns with moisture contents of 150,  
281 200, 250%  $MC$  had a lower number of sub-regions where  $S$  could be estimated.

282 [Table 2]

283

284 The best-fit model is shown in Table 3. The spread rates,  $\bar{S}$ , were well explained by the  
285 model ( $R^2=0.77$ ). There was a significant effect of  $MC$  and  $\rho$  on the spread rates of  
286 smouldering fires, where the continuous increase of  $MC$  had a stronger effect on the  
287 spread rates than the increase of  $\rho$  (Fig. 4). The interaction term was also significant,  
288 indicating that for low  $MC$  the change in  $\rho$  had a small impact on the spread rates.  
289 However, the decrease of spread rates due to the increase of  $\rho$  was stronger with higher  
290  $MC$ . (e.g.  $-0.015\pm 0.005$  cm kg<sup>-1</sup> m<sup>-3</sup> h<sup>-1</sup> for peats with 25%  $MC$  and  $-0.022\pm 0.009$  cm  
291 kg<sup>-1</sup> m<sup>-3</sup> h<sup>-1</sup> for peats with 100%  $MC$ ).

292

293 [Table 3]

294

295

296 [Figure 4]

297

298

## 299 Discussion

300 Our results support that peat moisture content is the main factor predicting the self-  
301 sustained propagation of peat fires. High peat bulk density contributes to increase the  
302 effect of moisture content on the dynamics of smouldering propagation. Peats  $\leq 100\%$   
303  $MC$  had a than a 70% probability of self-sustaining propagation beyond the initial 12  
304 cm ( $P_{yD} \geq 0.72$ ). Under these conditions, oxidation reactions along the smouldering  
305 fronts produced sufficient energy to overcome heat losses, dry the peat and ensure the  
306 self-sustained propagation (Bencoster et al. 2011; Huang and Rein 2015). Even though

307 the front propagated for 20 cm in all bulk densities tested (Fig 2), the spread rates were  
308 significantly slower when bulk density was high (Table 2).

309 Peats above 150% *MC* had a high probability of extinction after propagating through  
310 12 cm of peat. This suggests that when the moisture content is higher than 150%, the  
311 amount of energy required to evaporate water ahead of the smouldering front is too  
312 high to self-sustain propagation for more than 12 cm. For distances of  $\geq 12$  cm we found  
313 no effect of bulk density on propagation (Table 1). This could be because (a) the bulk  
314 density does not affect the fraction of peat burnt at  $D \geq 12$  cm, suggesting that moisture  
315 content of the peat is the main predictor of  $P_{yD}$  or (b) there is an effect of bulk density  
316 on  $P_{yD}$  when  $D \geq 12$  cm but our data has limited power to detect this effect. To increase  
317 the power to detect effects of bulk density, future research should consider a larger  
318 sample size and greater variety of moisture content and bulk density treatments within  
319 the range tested.

320 The estimated  $P_{yD}$  smouldering propagation for distances up to 10 cm from an ignition  
321 source is comparable with the probability of ignition and early propagation estimated  
322 in previous studies on natural peat soils (Frandsen 1997, Lawson et al. 1997, Reardon  
323 et al. 2007). In those studies, the 50% probability of ignition and 10 cm propagation  
324 had a moisture content threshold of 120% *MC* for *Sphagnum* and feather moss peats  
325 with bulk densities between 20 and 60 kg m<sup>-3</sup> and mineral contents below 30% (mass  
326 of mineral content per total mass of dry peat) (Frandsen 1997). In our analysis, peats  
327 below 160% *MC* and similar bulk densities have a  $P_{yD} = 0.5$  at  $D = 12$  cm, indicating  
328 that there is a 50% probability of self-sustain smouldering for more than 12 cm (Fig.  
329 2). However, denser peats with 130 kg m<sup>-3</sup> have a  $P_{yD} = 0.5$  at  $D = 10$  cm only when  
330 the peat moisture content is below 113% *MC* (Fig. 3). Using milled peats, Frandsen  
331 (1987) established a comparable threshold for peat ignition and early propagation of  
332 110% *MC* and bulk density of 130 kg m<sup>-3</sup>.

333 Compared to peats with low bulk density, the peats with high bulk density produce  
334 more energy due to the oxidation of a greater mass of peat particles (Ohlemiller 1985).  
335 However, the modification of bulk density through compression implies that high bulk  
336 density peats hold a larger mass of water per unit volume. For a successful self-  
337 propagation, all this water needs to be evaporated by the energy released from the  
338 adjacent smouldering front. Frandsen (1991) suggested that the rate of mass  
339 consumption is not sensitive to the bulk density of the peat. In that sense, the energy  
340 required to keep on-going self-sustained smouldering propagation should be

341 proportional to the mass of peat being consumed. We found that the spread rate of the  
342 smouldering front is sensitive to the bulk density of the peat and the effect depends  
343 upon the moisture content of the peat (Table 3). For example, the spread rate in peats  
344 with high bulk density and low moisture contents (i.e. 25, 100% MC) is not affected as  
345 much as in peats with high moisture contents (i.e. 150-250% MC). Peats with high  
346 moisture content and high bulk density have a reduced rate of O<sub>2</sub> diffusion and a larger  
347 amount of water to be evaporated before combustion. These conditions cause slower  
348 spread rates and shorter propagation distances (Ohlemiller 2002, Belcher et al. 2010;  
349 Hadden et al. 2013). The effect of the oxygen availability to the smouldering reaction  
350 zone was not considered in Frandsen 1991, as a constant oxygen flow was supplied  
351 through the burning peat to avoid the extinction of the fire.

352 The spread rate of the smouldering fronts was analysed for the first time as a function  
353 of peat conditions. The effects of moisture content and bulk density upon spread rates  
354 are consistent with the estimates of energy required to dry and heat the peat (Fig. S2  
355 and Fig. S3, estimated energy required to start thermal decomposition of peat for each  
356 peat moisture content and bulk density treatment are available in the Supplementary  
357 material). More mass of water per unit volume requires more energy to evaporate and  
358 start combustion (Fig. S2). However, peats with 100% MC and bulk density below 100  
359 kg m<sup>-3</sup> have a higher energy demand and propagated slower than peats with 150 and  
360 200% MC and bulk density below 75 kg m<sup>-3</sup> (Fig. S3). For a given moisture content,  
361 there is more energy needed to carry on smouldering combustion when the bulk density  
362 increases (Fig. S3). Increasing peat's bulk density, there is a larger energy production  
363 during the oxidation of the larger mass of peat. However, this energy produced is  
364 smaller than the energy necessary to evaporate the water in the peat. As a consequence,  
365 the spread rate of the fire is slower or not self-sustained (Fig. 4).

366

### 367 *Controlled smouldering tests*

368 It should be noted that our experiments were at a laboratory scale and peat conditions  
369 were controlled. Therefore caution should be taken when using our results at the field  
370 scale. The peat conditions (i.e. bulk density, mineral content, peat composition) can be  
371 very heterogeneous in real ecosystems (McMahon et al. 1980). Our laboratory-scale  
372 experiments intentionally removed these sources of variation. This allowed us to focus  
373 on the effect of two important peat conditions (moisture content and the bulk density)  
374 on the smouldering propagation dynamics.

375 Our burnbox size was designed to be suitable for the study of horizontal propagation  
376 across greater distances than in previous studies (Frandsen 1987; Frandsen 1997;  
377 Reardon et al. 2007), enhancing our understanding of propagation in larger sample  
378 sizes. The duration of our experiment and the size were limited by a maximum burn  
379 duration of 12 h in order to minimise the effect of diurnal variation in ambient  
380 temperature and humidity. The spread rates and the expected fractions of peat burnt  
381 were both estimated assuming constant moisture content and bulk density throughout  
382 the duration of an experiment. During our experiments there were not any moisture  
383 content changes that could have a substantial effect on the smouldering fire propagation  
384 (Table A1). However, substantial changes of moisture content or bulk density during  
385 the experiment duration could cause variation in the estimated spread rates with the  
386 distance.

387 The ignition of the peat along one side of the burnbox enabled a linear propagation of  
388 smouldering fronts moving perpendicular to the igniter coil. This ignition method was  
389 developed to estimate spread rates from infrared images that assume linear propagation  
390 (Prat-Guitart et al. 2015). A depth of only 5 cm of peat was used in this study to focus  
391 solely on horizontal smouldering propagation, avoiding vertical spread of the  
392 smouldering front and limiting the multi-dimensional spread of a peat fire. Previous  
393 experimental studies have examined peat ignition in deeper samples (Rein et al. 2008;  
394 Benscoter et al. 2011). However, deeper peat samples had smouldering fronts  
395 propagating horizontal and vertical, making more complex the study of propagation  
396 dynamics. The properties of the burnbox material created similar thermal insulation as  
397 if the peat sample would be surrounded by more peat (Frandsen 1987, 1991; Benscoter  
398 et al. 2011; Garlough and Keyes 2011). In these insulated conditions, a sample depth  
399 of 5 cm has a small impact in our results and they can be compared to other experiments  
400 looking at horizontal propagation in bigger samples.

401

#### 402 *Application to peatland fires*

403 In this study, the smouldering dynamics were studied in areas of 22×18 cm with  
404 homogeneous moisture content conditions, comparable to the size of a dry patch of peat  
405 moss (Petrone et al. 2004). In peatlands, the moisture content of the surface peat layers  
406 is regulated by the distribution of moss species and the position of the water table  
407 (Thompson and Waddington, 2013b; Waddington et al. 2014). A heterogeneous  
408 distribution of *Sphagnum* mosses is likely to cause a heterogeneous spatial distribution

409 of peat moisture content creating patches of 20-50 cm diameter (Benscoter and Wieder  
410 2003; Petrone et al. 2004). During drought the surface layers dries due to, the lack of  
411 rain, which may then be followed by a decrease in the water table position (Chivers et  
412 al. 2009; Sherwood et al. 2013; Kettridge et al. 2015). In such circumstances, dry peats  
413 in the surface layers have less than 250% *MC* (Benscoter et al. 2011; Terrier et al. 2014;  
414 Lukenbach et al. 2015), thus being vulnerable to peat fires.

415 After a peat fire, the new surface layer is closer to the water table and consequently  
416 having a reduced fire danger. Previous studies suggested that peat fires are common in  
417 peatland ecosystem cycles (Turetsky et al. 2002). The consumption of surface layers of  
418 peat reduces the accumulation of organic material allowing *Sphagnum* mosses to access  
419 the water table being less dependent on external water inputs (Benscoter and Vitt 2008).  
420 Post fire surfaces also enable the roots of vegetation to uptake ground water and  
421 nutrients from deep mineral layers.

422 In peatlands, peat bulk density strongly depends on the vegetation cover and the  
423 temporal changes in the water table behaviour (Davies et al. 2013; Sherwood et al.  
424 2013; Thompson and Waddington 2013a). Deep peat layers often have a higher degree  
425 of decomposition and a higher bulk density compared to surface layers (Benscoter et  
426 al. 2011; Thompson and Waddington 2014). Following turf cutting in drained  
427 peatlands, new dense and dry layers of bare peat become exposed at the surface being  
428 vulnerable to new peat fires.

429 Peats with 25% *MC* were included in the analysis to have a representation of very dry  
430 peats in our sample. However, such dry peats are uncommon in natural peatlands  
431 (Terrier et al. 2014; Lukenbach et al. 2015), being restricted to the surface of drained  
432 peatlands under extreme drought. In the present study, bulk density was experimentally  
433 manipulated using two peat compression treatments, which produced a range of bulk  
434 densities. Dry peats (25% *MC*) were only experimentally tested with high bulk densities  
435 between 108 and 145 kg m<sup>-3</sup>. The high bulk density of 25% *MC* peats is due in part to  
436 the structure of milled peats and the relatively low expansion of peat particles when a  
437 small quantity of water is added to the peat sample (Huang and Rein 2015). The reduced  
438 expansion of the relatively dry peat (25% *MC*) compared to the greater expansion of  
439 relatively wetter peat ( $\geq 100\%$  *MC*) caused the negative collinearity between moisture  
440 content and bulk density. If we exclude peats with 25% *MC* we find no collinearity  
441 between *MC* and  $\rho$  (*Spearman correlation* = -0.07, *p-value* = 0.7). Therefore, the  
442 negative collinearity between *MC* and  $\rho$  (Fig. 1) is caused by the peats with 25% *MC*.



443 This collinearity could contribute to the interaction reported in the spread rate model  
444 (Table 3) and effect extrapolated predictions of spread rates (Dormann et al., 2013).  
445 The same spread rate model but excluding peats with 25% *MC*, had similar  $\beta_0$ ,  $\beta_1$  (*MC*)  
446 and  $\beta_2$  ( $\rho$ ) coefficients but no significant interaction term. Therefore, the main effects  
447 of moisture content and bulk density on the spread rates are qualitatively not affected  
448 by the collinearity.

449 All the milled peats used in this study had a low mineral content of less than 5%. Natural  
450 peats are characterized as having less than 20-35% mineral content (Turetsky et al.  
451 2014) and often <6% (Benscoter et al. 2011). Previous studies have suggested that large  
452 quantities of mineral content could reduce the capacity of smouldering fires to ignite  
453 and propagate (Frandsen 1987; Hungerford et al. 1995). Our peats had an intrinsic  
454 mineral content of  $2.6 \pm 0.2\%$  similar to the 3.7% of Frandsen's 1987 peats. This implies  
455 that our low mineral content peats would give an upper limit on the spread rates and  
456 propagation distance. However, small quantities of certain minerals such as salts of  
457 calcium or magnesium, common in plant material and soil, have been shown to have  
458 no effect on propagation (Benscoter et al. 2011) or rather enhance heat conduction in  
459 the fuel media that could help the smouldering propagating faster (Frandsen 1998;  
460 Reardon et al. 2007).

461 Differences in bulk density can be associated with other properties of peat soils such as  
462 soil structure, particle size, pore space and decomposition (Ingram 1978). The variation  
463 of these physicochemical properties can also affect the energy produced during peat  
464 oxidation and the energy transferred through peat particles (Reardon et al. 2007; Huang  
465 et al. 2015). The presence of artefacts (e.g. roots, stones, etc.) may also play a role in  
466 creating variability in peat conditions, which could affect the propagation of  
467 smouldering fires. Twigs and roots for example, have been reported to promote the  
468 propagation of smouldering fires (Miyanishi and Johnson 2002; Davies et al. 2013),  
469 this is likely a result of local changes to *MC* around the root.

470 The hydrology of peatlands as well as peat properties should be carefully observed in  
471 order to estimate variations in moisture and bulk density as we have shown that these  
472 peat conditions strongly influence the propagation of smouldering fires even on a fine-  
473 scale. The spatial variability and dynamics of peat conditions remains a challenge to  
474 studies of peat fires in the field (McMahon et al. 1980; Hungerford et al. 1995) and  
475 highlights why laboratory scale studies are required to understand measured effects on  
476 smouldering. The control of individual properties such as moisture content and bulk



477 density can then be used to piece together the broader relationship between peat  
478 conditions and smouldering in the natural environment. Milled peats like those used  
479 here, have been the most utilised alternative to reduce the variability of natural peats  
480 and study the influence of external factors (moisture, mineral content, bulk density,  
481 oxygen availability, etc.) on smouldering combustion of peat (Frandsen 1987, 1991;  
482 Belcher et al. 2010; Hadden et al. 2013; Zaccone et al. 2014; Prat et al. 2015).

483  
484

## 485 **Conclusions**

486 This study has built on previous work on ignition and early horizontal propagation of  
487 smouldering fires in peats. We have coupled laboratory scale observations of  
488 smouldering fires with statistical models to estimate and analyse the fire spread rate  
489 and the expected fraction of peat burnt at distance longer than 12 cm. Our findings  
490 enable understanding the effects of a variety of peat moisture content and bulk density  
491 conditions on smouldering propagation dynamics. Self-sustained fronts were observed  
492 to propagate in peats with moisture content below 150% *MC*. The bulk density of the  
493 peat was also found to affect the propagation of smouldering fires. The increase of bulk  
494 density enhances the effects of moisture content on the propagation dynamics.

495 Our approaches highlighted that laboratory scale experimental research can contribute  
496 to the study of theoretical insights of the behaviour of smouldering fires. Data from this  
497 study is fundamental to integrate a wide range of realistic peat conditions and their  
498 associated horizontal and vertical dynamics to modelling approaches at larger scales.

499  
500

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659

660 **Table 1. Coefficient estimates from beta regression models ( $D=6, 8, 10, 12, 14, 16$  and  $18$  cm) for the expected fraction of peat burnt ( $P_{yD}$ )**  
 661 **at each distance ( $D$ ) from the igniter (equation 1).**

662  $\beta_D$ ,  $\beta_{D1}$  and  $\beta_{D2}$  are coefficients estimates ( $\pm$  standard error) for intercept, bulk density and moisture content. Wald test  $p$ -value significance has  
 663 been added to the coefficients where ‘\*\*\*’  $<0.001$ , ‘\*\*’  $0.01$ , ‘\*’  $0.05$ .  $\Phi$  is the model precision,  $\text{Log-Like}$  is the model Log-likelihood and  $R_p^2$   
 664 is the pseudo R-squared. Sample size in each regression = 36.

665

$D$ (cm)	$\beta_D$	$\beta_{D1} (\rho)$	$\beta_{D2} (MC)$	$\Phi$	$\text{Log-Lik}$	$R_p^2$
6	6.53 $\pm$ 1.18 ***	-0.032 $\pm$ 0.008 ***	-0.018 $\pm$ 0.003 ***	1.53 $\pm$ 0.38 ***	57.11	0.71
8	6.81 $\pm$ 1.19 ***	-0.034 $\pm$ 0.008 ***	-0.021 $\pm$ 0.003 ***	1.52 $\pm$ 0.37 ***	56.98	0.77
10	4.79 $\pm$ 1.16 ***	-0.021 $\pm$ 0.008 **	-0.018 $\pm$ 0.003 ***	1.09 $\pm$ 0.25 ***	53.36	0.68
12	3.23 $\pm$ 1.09 **	-0.008 $\pm$ 0.008	-0.018 $\pm$ 0.003 ***	1.16 $\pm$ 0.26 ***	54.01	0.71
14	3.23 $\pm$ 1.09 **	-0.008 $\pm$ 0.008	-0.018 $\pm$ 0.003 ***	1.16 $\pm$ 0.26 ***	54.01	0.71
16	3.23 $\pm$ 1.09 **	-0.008 $\pm$ 0.008	-0.018 $\pm$ 0.003 ***	1.16 $\pm$ 0.26 ***	54.01	0.71
18	2.79 $\pm$ 1.09 *	-0.003 $\pm$ 0.008	-0.018 $\pm$ 0.003 ***	1.22 $\pm$ 0.28 ***	53.07	0.73

666

667 **Table 2. Estimated spread rates of the experimental smouldering fires.**

668 *MC* is the moisture content, *BD* is the bulk density treatment,  $\rho$  is the mean bulk density ( $\pm$  standard deviation). Num. Burns is the total number  
 669 of experimental burn replicates. Num. Sub-regions is the total number of sub-regions used to estimate spread rates, *S*, across all experimental  
 670 burn replicates.  $\bar{S}$  is the median spread rate ( $\pm$  median absolute deviation) for repeated burns under the same *MC* and *BD* conditions.

671

<i>MC</i> (%)	<i>BD</i>	$\rho$ (kg m <sup>-3</sup> )	Num. Burns	Num. Sub-regions	<i>S</i> Min-max (cm h <sup>-1</sup> )	$\bar{S}$ (cm h <sup>-1</sup> )
25	<i>BD</i> <sub>1</sub>	116 ± 9	4	191	2.3 – 7.2	4.33 ± 0.91
100	<i>BD</i> <sub>1</sub>	80 ± 7	4	178	1.0 – 7.8	2.63 ± 1.08
150	<i>BD</i> <sub>1</sub>	62 ± 5	4	96	1.0 – 4.8	2.07 ± 0.59
200	<i>BD</i> <sub>1</sub>	60 ± 10	4	45	1.2 – 5.2	2.16 ± 0.62
250	<i>BD</i> <sub>1</sub>	71 ± 9	3	6	1.0 – 2.2	1.42 ± 0.43
25	<i>BD</i> <sub>2</sub>	141 ± 5	3	147	1.5 – 6.2	2.86 ± 0.75
100	<i>BD</i> <sub>2</sub>	80 ± 8	4	179	0.6 – 9.1	1.71 ± 0.90
150	<i>BD</i> <sub>2</sub>	111 ± 8	3	13	0.7 – 1.9	1.23 ± 0.45
200	<i>BD</i> <sub>2</sub>	124 ± 11	3	–	–	–
250	<i>BD</i> <sub>2</sub>	114 ± 3	3	–	–	–

672



673 **Table 3. Best-fit linear model for median spread rates ( $\bar{S}$ ).**

674 Coefficients  $\beta_0, \beta_1, \beta_2, \beta_3$  are parameter estimates for variables: peat moisture content, bulk density and the interaction between them. Number of  
675 data points in the model = 36,  $R^2 = 0.77$ . Residual standard error: 0.173.

676

	<i>Estimate</i>	<i>Standard error</i>	<i>p-value</i>
$\beta_0$ (Intercept)	0.514	0.056	<0.001
$\beta_1$ (MC)	-0.545	0.061	<0.001
$\beta_2$ ( $\rho$ )	-0.325	0.058	<0.001
$\beta_3$ (MC $\times$ $\rho$ )	0.151	0.046	0.003

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680

681 **Figure captions**

682

683 **Fig. 1.** Bulk density of the peat samples as a function of moisture content. Circles are  
684 peat samples treated with  $BD_1$  and triangles are peats treated with  $BD_2$ .

685

686 **Fig. 2.** Hours taken by the smouldering front ( $t^L$ ) to self-propagate through the peat  
687 sample until self-extinction. Circle, triangle, square, diamond and star correspond to  
688 25, 100, 150, 200 and 250% moisture content, respectively. (a) uncompressed peats  
689 (treatment  $BD_1$ ) and (b) compressed peats (treatment  $BD_2$ ). Standard errors of the  
690 means are smaller than the symbol size. Lines are linear regression fits. Only moisture  
691 contents where self-sustained smouldering propagation occurred are plotted.

692

693 **Fig. 3.** Expected fraction of peat burnt ( $P_{yD}$ ) to a distance,  $D$ , away from the ignition  
694 region.  $D$  values of 6 cm, 8 cm, 10 cm and 12 cm are shown, results from  $D=14$  cm, 16  
695 cm and 18 cm are similar to  $D=12$  cm (Table 1). Panels are for (a) 25%, (b) 100%, (c)  
696 150%, (d) 200% and (e) 250% moisture content. Symbols represent fractions of peat  
697 burnt ( $y$ ) along a transect at distance  $D$ .

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699 **Fig. 4.** Spread rate as a function of peat bulk density (y-axis is on a square-root scale).  
700 Panels are for (a) 25%, (b) 100%, (c) 150%, (d) 200% and (e) 250% moisture content.  
701 Each dots and error bar corresponds to median spread rate and median absolute  
702 deviation for an experimental burn. Solid lines correspond to model predictions (Table  
703 3) and dashed lines the prediction's 95% confidence intervals.

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