

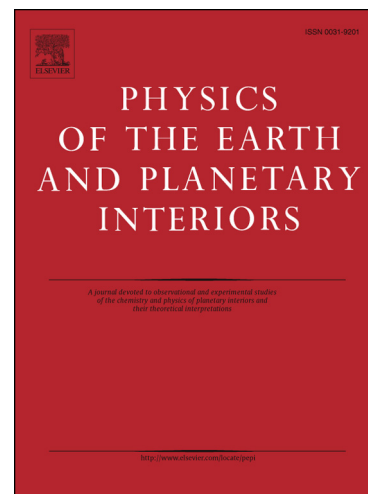
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Dynamic triggering of earthquakes is promoted by crustal heterogeneities and bimaterial faults

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1 Dynamic triggering of earthquakes is promoted by
2 crustal heterogeneities and bimaterial faults

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7 **Abstract**

Remotely triggered earthquakes and aftershocks constitute a great challenge in assessing seismic risk. A growing body of observations indicates that significant earthquakes can be triggered by moderate to great earthquakes occurring at distances of up to thousands of kilometers. Currently we lack the knowledge to predict the location of triggered events. We present numerical simulations showing that dynamic interactions between material heterogeneities (e.g. compliant fault zones, sedimentary basins) and seismic waves focus and enhance stresses sufficiently to remotely trigger earthquakes. Numerical simulations indicate that even at great distances (>100km), the amplified transient dynamic stress near heterogeneities is equivalent to stress levels near the source rupture tip (<5km). Such stress levels are widely considered capable of nucleating an earthquake rupture on a pre-stressed fault. Analysis of stress patterns in dynamic rupture simulations which include a heterogeneous zone with a range of material and geometrical properties reveals various mechanisms of stress enhancement. We conclude that both stiff

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and weak heterogeneities may focus stress waves to form zones of enhanced stress, and that bimaterial interfaces distort under static and dynamic loading in a way that induces local stress concentrations. Our work provides insights for understanding non-uniform distribution of remotely triggered seismicity and recurrence of such events along complex fault-systems and near magmatic intrusions and geothermal zones.

8 *Keywords:* remotely triggered seismicity, dynamic rupture simulation,
9 forecasting earthquake interaction, stress shadow, bimaterial interface,
10 fault-system stability, seismic wave amplification

11 **1. Introduction**

12 Earthquake triggering is the process by which stress changes associated
13 with an earthquake can induce or retard seismic activity in the surrounding
14 region. Static stress changes are permanent and produce increased seismicity
15 rates where stress increases (stress triggering), or decreased seismicity rates
16 where stress decreases (stress shadowing). Calculations of static Coulomb
17 stress transfer have proven to be a powerful tool in explaining near-field
18 aftershock distributions (King et al., 1994; Stein et al., 1997; Harris and
19 Simpson, 1998; Pondard et al., 2007; Sumy et al., 2014). Dynamic stress
20 changes due to the passage of seismic waves cause transient dynamic stress
21 oscillations and as such are positive everywhere at some point in time. The
22 physical origin of dynamic triggering remains one of the least understood
23 aspects of earthquake nucleation. We assess some of the mechanisms in-

24 volved in dynamic triggering. The majority of previous studies have focused
25 on near-field static stress changes that trigger aftershocks, and some studied
26 dynamic stress patterns near fault tips (Finzi and Langer, 2012a,b; Lozos
27 et al., 2012). However in this work we focus on dynamic triggering far away
28 from the fault and aim to elucidate some of the path-dependent mechanisms
29 occurring in RTS. While these mechanisms are also present in near field we
30 focus on remote triggering far away from the earthquake source where the
31 contributions from the static stress changes are small and the path-dependent
32 dynamic effects are dominant. The current work reveals how certain fault-
33 zone structures may dynamically amplify and focus seismic waves and induce
34 nucleation of RTS. While a great amount of attention has focused on fore-
35 casting near-field aftershocks the topic of RTS remains a great challenge in
36 seismic hazard analysis.

37 Remotely triggered seismicity (RTS) has been reported following numer-
38 ous large earthquakes such as the 2002, M7.9 Denali and the 1992, M7.3
39 Landers earthquakes (Eberhart-Phillips et al., 2003; Steacy et al., 2005; Hill
40 et al., 1993). RTS at extremely large distances (>1000 km) has been as-
41 sociated with passing S and surface waves (Gomberg and Davis, 1996; Kilb
42 et al., 2000; Gomberg et al., 2003; Lei et al., 2011). In fact, RTS is often
43 described as the result of extremely weak stress perturbations acting on criti-
44 cally stressed faults (van der Elst and Brodsky, 2010). We investigate another
45 mechanism of importance in RTS, where low amplitude stress perturbations
46 may be amplified sufficiently by certain tectonic structures or heterogeneities

47 to induce nucleation along faults that are not necessarily critically stressed.

48 Dynamic stress waves also affect induced seismicity in the near-field as
49 they do far from the source event. Examples include reported seismicity
50 following moderate ($M < 7$) earthquakes (Hough, 2005) and dynamically trig-
51 gered complex multi-segment earthquake sequences (Finzi and Langer, 2012a;
52 Hill and Prejean, 2007; Hough, 2005). In fact, dynamic stress waves and their
53 interaction with various fault structures is often considered as an explana-
54 tion for aftershock patterns that deviate from those of static stress patterns
55 (Freed, 2005).

56 To date, the underlying mechanisms for remote triggering remain a mat-
57 ter of continuing debate (Brodsky and Prejean, 2005; Prejean and Hill, 2009;
58 Lei et al., 2011; Gomberg, 2013). It is well established that directivity effects
59 can cause enhanced RTS in the rupture direction (Gomberg, 2013). How-
60 ever directivity and other source related effects cannot always fully explain
61 why in some cases faults close to the source remain inactive whereas for
62 the same earthquake distant faults are triggered. Therefore additional in-
63 formation such as path-dependent effects and local stress amplifications are
64 required in order to determine if a fault-zone is likely to experience RTS. Re-
65 cently, stress amplification on remote faults was also shown to be associated
66 with dynamic interactions between seismic waves and geological structures
67 (Gomberg, 2013). In her paper, Gomberg (2013) proposes that certain fault
68 structures repeatedly experience RTS due to local dynamic interactions with
69 passing seismic waves. In this paper we elucidate the mechanisms underpin-

70 ning these interactions.

71 Many studies have shown how structural features such as low-velocity
72 fault zones (Fohrmann et al., 2004) or sedimentary basins (Gomberg et al.,
73 2004; Hartzell et al., 2010) can cause trapped waves and seismic wave am-
74 plification. Stress-enhancing interactions were also described in studies of
75 wave reflection off the Moho or the Earth’s core (Lin, 2010; Hough, 2007)
76 and dynamic stress concentration along bimaterial interfaces (Stoneley, 1924;
77 Burridge, 1973; Finzi and Langer, 2012a; Lei et al., 2011). While the phe-
78 nomena of “seismic waves focusing”, excitation of bimaterial interfaces and
79 large scale wave reflections have long been studied in various geophysical
80 contexts, only a few recent studies account for such processes in the context
81 of remotely triggered seismicity (Lin, 2010; Lei et al., 2011; Gomberg, 2013).

82 We extend these studies by showing numerically how significant stress
83 concentrations due to material heterogeneities far from a source earthquake
84 may induce remotely triggered seismicity. We show how even smaller magni-
85 tude earthquakes can trigger far-field seismicity by considering the effect of
86 crustal heterogeneities such as fault zones, basins and igneous bodies. While
87 other studies (Fohrmann et al., 2004; Gomberg, 2013) have solely focused on
88 the interactions between seismic waves and low-velocity zones, we demon-
89 strate how dynamic interactions between the seismic waves and both compli-
90 ant and stiff geological structures may induce remotely triggered seismicity
91 in and around these structures.

92 **2. Methods**

93 *2.1. Numerical simulations of dynamic stress transfer in a heterogeneous* 94 *crust*

95 In order to simulate remotely triggered seismicity we set up a Finite
96 Element model domain where we solve the wave equation for dynamic rupture
97 at a fault. Excitation of distant faults and bimaterial interfaces is studied by
98 calculating Coulomb Failure Stress (CFS) throughout the model domain and
99 by noting potentially significant occurrences of anomalously low and high
100 values. Two principal triggering criteria are used to measure the likelihood
101 of RTS. One is the threshold of peak transient CFS of the radiating seismic
102 waves (Hill et al., 1993; Gomberg et al., 1997). A second criterion calculates
103 the magnitude of the cumulative energy exerted at the fault (Brodsky et al.,
104 2000). In the discussion we compare these two measures and show they give
105 slightly different estimations of the likelihood of RTS.

106 We show that path effects are as important as source effects for RTS by
107 examining the dynamic stress-enhancing interactions between seismic waves
108 and heterogeneities embedded in the model domain. While most natural het-
109 erogeneities represent weakened zones such as damaged fault-zones and sedi-
110 mentary basins, we also examine stress-enhancing interactions in the presence
111 of a stiff zone (e.g. Vauchez et al. (1998) and Tommasi et al. (1995)). This
112 enables a better understanding of the various stress-enhancing mechanisms.

113 We simulate tectonic loading and dynamic rupture using the same method
114 as our previous study of multi-segment dynamic stress patterns (Finzi and

115 Langer, 2012a). We use the 2D finite element code esys.escript (Gross et al.,
116 2007). The fault (see Figure 1) is embedded in a homogeneous medium
117 with rigidity $G_0 = 30$ GPa, first Lamé parameter $\lambda = 30$ GPa, density $\rho =$
118 2700 kg/m^3 and shear wave velocity $v_S = 3333 \text{ m/s}$. The model domain is
119 loaded with a stress tensor such that the unruptured source fault is optimally
120 aligned with respect to the Coulomb Failure stress under the condition of a
121 static coefficient of friction $\mu_s = 0.6$ (for more modelling constraints see
122 Supplementary material).

123 The simulated earthquakes along the source fault are 60 km long with
124 $M_w 7$, an average slip of approximately 5 m and a maximum slip of 9 m at
125 hypocentral depth (values chosen to be consistent with geologic observations;
126 Wells and Coppersmith (1994)). Furthermore, the prescribed fault friction
127 parameters ensure that simulated earthquakes exhibit sub-shear pulse-like
128 ruptures.

129 A material heterogeneity in the form of a compliant/stiff zone of 8 km by
130 16 km is located at one fault length or 60 km East of the source fault (model
131 A). Simulation results for two fault lengths separation between model and
132 heterogeneity zone (model B) can be found in the Supplementary material
133 section. The compliant material zone has a rigidity $G_A = 0.7 G_0$. As the first
134 Lamé parameter and density are kept unchanged, the shear wave speed in the
135 heterogeneity is $v_A = \sqrt{0.7} v_S$. The material properties of the stiff zone are
136 $G_A = 1.3 G_0$ and $v_A = \sqrt{1.3} v_S$. While a material contrast of 30% is large in
137 terms of typical lithology variations in the crust, it represents various tectonic

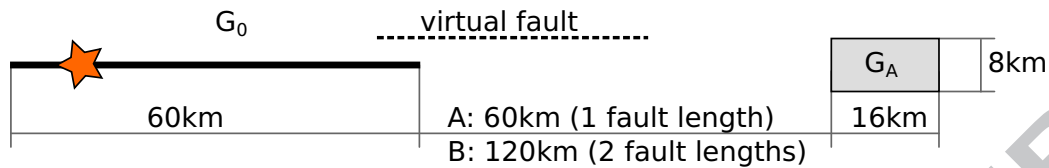


Figure 1: Model configuration for simulating dynamic stress to explore the occurrence of remotely triggered seismicity at the vicinity of material heterogeneities. The distance between the source earthquake and the heterogeneity is sufficient to assure that static stress changes induced by the earthquake are insignificant at the heterogeneity. The distance was either one fault length (model setup A) or two fault lengths (model setup B). The model has a background rigidity G_0 and the heterogeneity has a rigidity G_A . The virtual fault is used to calculate a normalized stress level.

138 settings in which soft sediments accumulate in a basin or accretionary prisms
 139 bounded by stiffer material (Gomberg (2013); Shani-Kadmiel et al. (2012,
 140 2014); Hartzell et al. (2010) and DESERT group studies, e.g. Weber et al.
 141 (2009)) and across large faults such as the San Andreas (Brietzke and Ben-
 142 Zion (2006) and references therein). Figure 1 shows the configuration of
 143 our simulations, and other configurations used to test specific hypotheses
 144 are explained further in the discussion (see also Supplementary material for
 145 more details). Rupture is initiated at the star location in Figure 1 and after
 146 a short bilateral propagation phase, it proceeds unilaterally East towards the
 147 heterogeneous zone.

148 2.2. Analysis: peak transient CFS as a fault stability criterion

149 We conduct multiple dynamic rupture simulations assigning different elas-
 150 tic properties and geometrical characteristics to the material heterogeneity.
 151 To determine whether a rupture could nucleate on a remote fault in our

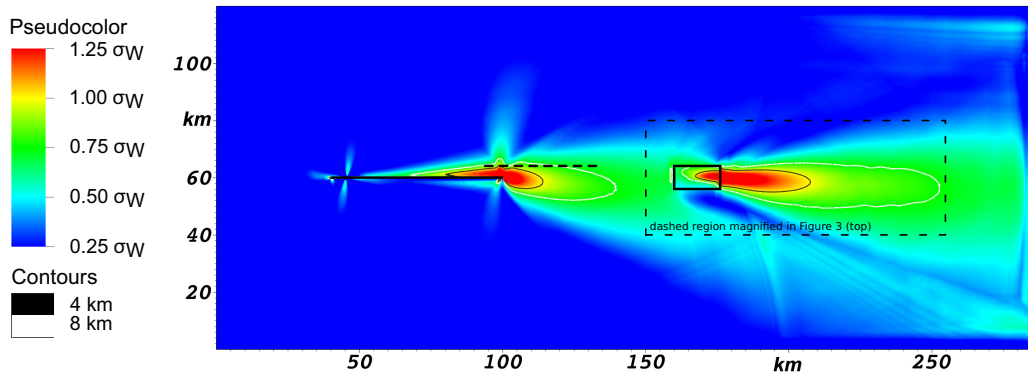


Figure 2: The normalised optimally oriented peak transient CFS is calculated such that the highest optimally aligned transient stress that occurs at the virtual fault (dashed line near primary fault) is set to $\sigma_W = 1$. All values above one suggest that triggering is likely to occur according to the “Wesnousky 4 km-rule”.

152 model domain we calculate the peak transient Coulomb failure stress (peak
 153 transient CFS) on optimally oriented faults throughout the model domain.
 154 As in Finzi and Langer (2012a) we normalize the peak transient CFS values
 155 using its maximal value along a virtual fault parallel to the source fault at
 156 a distance of 4 km and with an overlap of 6 km (Figure 2). Normalizing by
 157 the stress level at a distance of 4 km, we adhere to a common assumption
 158 pertaining that ruptures are likely to jump step-overs as wide as 4 km but not
 159 wider (Wesnousky, 2006; Harris and Day, 1993). From this procedure it fol-
 160 lows that normalised peak transient CFS values larger than 1 indicate that
 161 dynamic stresses may be sufficient to induce remotely triggered seismicity
 162 (on pre-stressed faults of suitable orientation).

163 3. Results

164 We describe the dynamic stress enhancement patterns in this section and
165 in section 4 we discuss different possible mechanisms for the observed dy-
166 namic stress enhancement. Certain stress enhancement features in our re-
167 sults are analogous to those previously observed in simulations of dynamic
168 stress patterns in fault step-over zones (Finzi and Langer, 2012a,b). For
169 example, during the far-field loading of the model domain, (static) stress
170 concentrations occur along the edges of the simulated material heterogeneity
171 in the same way that was reported in simulations of segmented fault systems
172 with weak step-over zones (Finzi and Langer, 2012b, Figure 4b). We there-
173 fore focus here on dynamic stress enhancement at large distances and refer
174 the reader to our previous work for details on static stress concentrations at
175 material heterogeneities.

176 3.1. *Stress concentration along bimaterial interfaces and within the material* 177 *heterogeneity*

178 Simulations with compliant zones at large distances from the source earth-
179 quake exhibit significant stress concentrations along the leading (Western)
180 and tailing (Eastern) bimaterial edges of such zones and within the weak
181 zone (Figure 3). The normalised peak transient CFS pattern near the lead-
182 ing edge (marked X) exhibits elongated areas with increased stress. This can
183 also be seen, albeit with lower stress magnitudes, West of the tailing edge
184 interface (marked Y in Figure 3) and in simulations with a stiff heterogeneity

185 (Figure 4). Along the Northern edge of the heterogeneity there is an area
186 (marked Z) with elevated peak transient CFS values. The area marked Z
187 is located in the vicinity of a region of bimaterial contrast that experiences
188 non-uniform straining when stressed.

189 *3.2. Stress focusing by material heterogeneities*

190 A prominent feature in all our simulated stress patterns consists of a
191 very large stress lobe with high peak transient CFS values stretching from
192 the weak zone away from the source event (Figures 2 and 3). The enhanced
193 stress lobe for a compliant zone is comparable in size to the rupture length,
194 and it exhibits peak transient CFS values as large as those observed at 2-
195 3 km from the termination point of the source rupture. This stress lobe
196 appears to radiate from near the heterogeneity and disperse/subside as the
197 waves propagate away from the heterogeneity. In simulations with a material
198 heterogeneity comprised of a stiff zone ($G_A = 1.3G_0$), equivalent enhanced
199 peak transient CFS lobes are formed, however there are two lobes stretching
200 from near the Eastern corners of the heterogeneity and not oriented in the
201 direction of rupture but rather in SE and NE directions (Figure 4) with the
202 lobe in SE direction being stronger.

203 The difference in the strength of the lobes originates in a non-zero back-
204 ground stress for the CFS calculation and the different directions of the
205 seismic waves. The Coulomb failure stress is calculated including the static
206 portion for the normal and shear stress. The normal stress component of

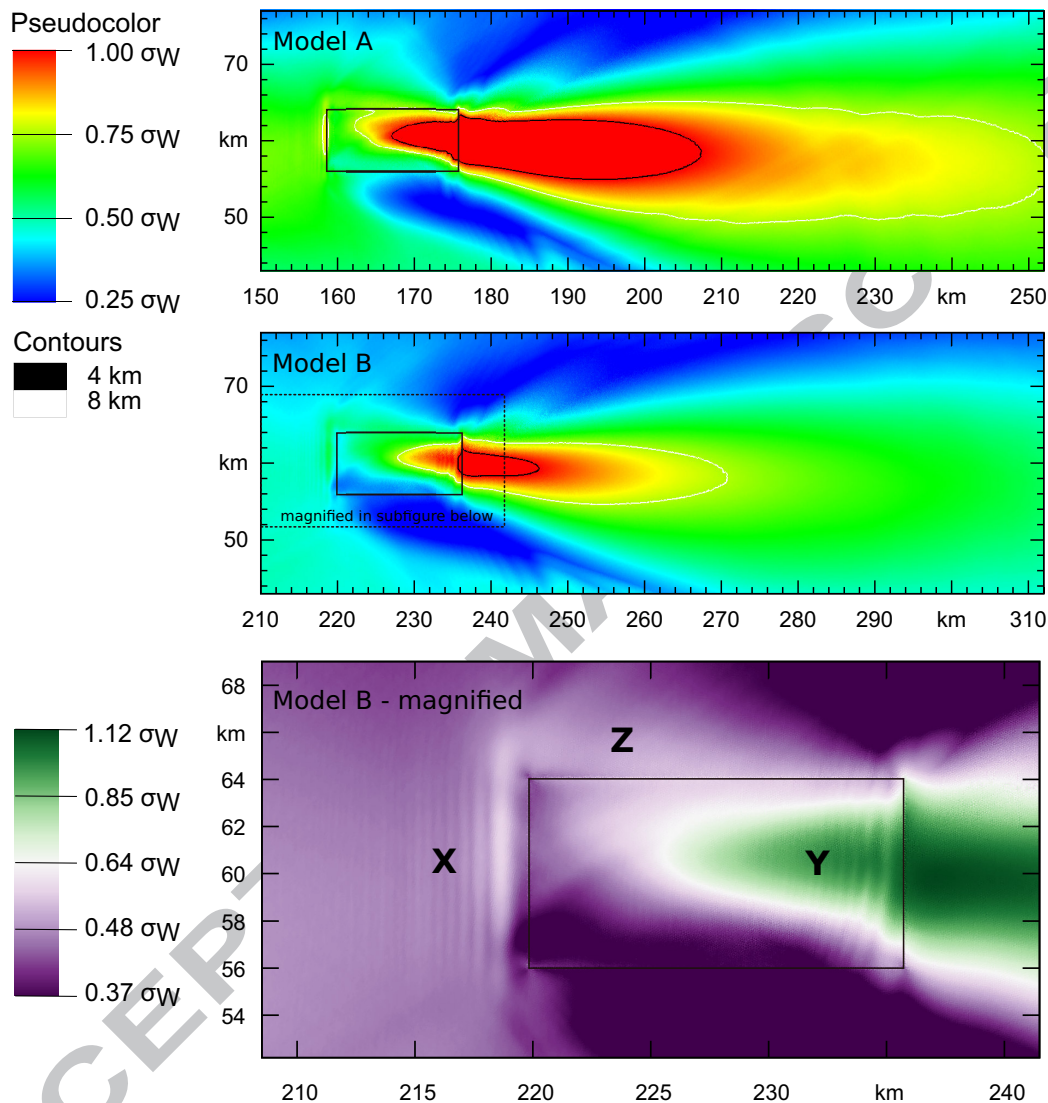


Figure 3: Close up view of stress patterns within the heterogeneity. Model A (top figure) shows the region around a compliant heterogeneity at 1 fault length away from the source fault and Model B (center figure) shows it at 2 fault lengths. The bottom figure shows an enlarged view of the center figure with a different color scale where Markers X and Y show patterns of equidistant elongated areas, Z shows elevated stress level outside the heterogeneity.

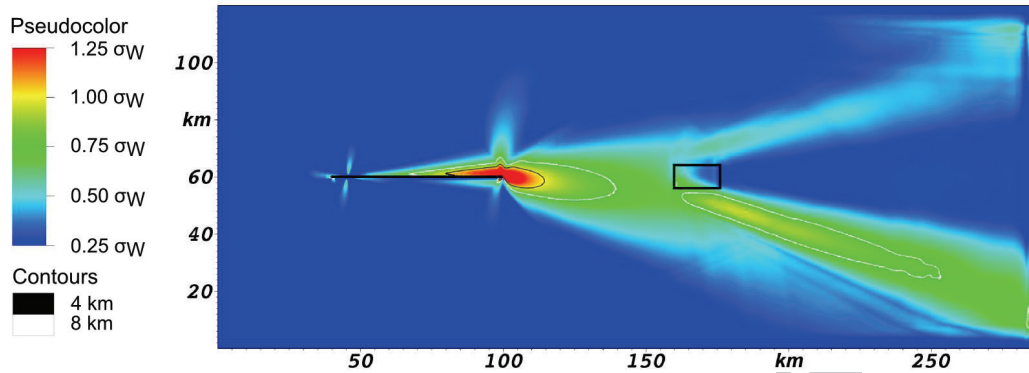


Figure 4: Enhanced stress beyond a stiff material heterogeneity. Simulation results exhibiting large lobes of enhanced peak transient CFS induced by stress wave focusing as they pass through the heterogeneity (see discussion and Figure 5). Stress waves seem to be diffracted / diverted to the SE direction forming a stress shadow East of the heterogeneity and enhanced peak transient CFS SE (and NE) of it.

207 the dynamic wave has an amplitude with opposite signs for waves travelling
 208 North and South. For further information see Supplementary material and
 209 Langer et al. (2010) for quasi-static tectonic loading.

210 4. Discussion

211 In interpreting our simulations we separate the stress-enhancing effects
 212 into two different groups. In the first subsection we explain effects that
 213 occur close to the heterogeneity due to strain contrasts and wave amplitude
 214 properties. In the second subsection we focus on effects that occur due to
 215 seismic ray path properties that change due to the heterogeneity.

216 *4.1. Excitation of material interfaces*

217 A wide range of studies have shown the various effects that bimaterial
218 interfaces have on rupture processes and seismic wave propagation. Such
219 studies include descriptions of strain patterns across bimaterial interfaces
220 (Weertman, 1980; Cochard and Rice, 2000), and of unique surface waves
221 that develop along such interfaces (Stoneley, 1924). The effect of bimaterial
222 interfaces on rupture jumps over weak step-over zones separating fault seg-
223 ments was recently described in Finzi and Langer (2012b). Similarly, our
224 current simulations show that dynamically propagating seismic waves induce
225 stress enhancements along the bimaterial edges (Figures 2, 3, 4). Several
226 mechanisms are plausible to explain the localized stress concentrations along
227 the interfaces. These mechanisms include dynamic distortion due to the
228 strain contrast across the interfaces and surface (Stoneley) waves along the
229 locked interface. The higher CFS in area Z in Figure 3 is most likely caused
230 by waves travelling along the bimaterial interface. A wave front extending
231 perpendicular to an interface between different rigidities introduces a sharp
232 gradient in the strain field and locally amplified stress. These mechanisms are
233 not mutually exclusive and we cannot determine the relative contributions
234 of each single mechanism.

235 4.2. Ray path processes (reflection, refraction, scattering, constructive/destructive
236 interference and amplification/reduction of seismic waves at material
237 heterogeneities)

238 The large stress lobes beyond the material heterogeneity show character-
239 istics of focusing such as expected when waves travel through materials of
240 different elastic properties. To verify that the observed stress concentrations
241 are due to optical-like focusing we demonstrate this effect using a simplified
242 model. We calculate ray paths that mimic seismic wave propagation from
243 the source event (simplifying the source and representing it as a point source
244 at the rupture termination point). Figure 5 shows the predicted wave prop-
245 agation paths for seismic waves traveling through a weak zone ($G_A = 0.7 G_0$,
246 Figure 5a) and through a stiff zone ($G_A = 1.3 G_0$, Figure 5b). It is expected
247 that regions with overlapping ray paths may lead to elevated CFS and regions
248 with sparser rays may represent lowered CFS (i.e. stress shadows). Figure 5
249 can be directly compared with Figure 2 and 4 and shows qualitatively a sim-
250 ilar effect due to compliance or stiffness of the material heterogeneity. This
251 simple model effectively demonstrates that ray path processes are important
252 in RTS and may affect the ability to trigger earthquakes and the spatial dis-
253 tribution of triggered seismicity (a topic of recent studies; e.g. Brodsky and
254 van der Elst (2014); van der Elst and Brodsky (2010)).

255 The elongated “ripples” West of the interfaces (marked X and Y in Figure
256 3) may be caused by a superimposition of the shear waves with their reflec-
257 tions at the bimaterial interface. The high peak transient CFS within the

258 heterogeneities could be due to reflections along the top/bottom interfaces
259 and/or interaction between the side interfaces that results in enhancement
260 in a similar way that trapped waves and guided waves may be enhanced.

261 The ray path, scattering and bimaterial effects shown here to be impor-
262 tant for dynamic stress amplifications depend on the wave frequency, the
263 propagation length through the heterogeneity and the relative size of the
264 heterogeneity compared to the wavelength. These factors determine whether
265 elastic focusing/defocusing (multipathing) effects or scattering effects due
266 to the heterogeneity will dominate. Since the finite element method pro-
267 vides a full solution to the elastic wave equation, all the above properties
268 are included and the direct, diffracted, converted and guided waves are mod-
269 elled. Propagation of seismic waves and dynamically triggered seismicity
270 will be affected by both elastic and anelastic properties. Anelastic effects
271 are increasingly important as the frequency of the wave increases, leading
272 to stronger damping of higher frequency waves. Although anelastic attenua-
273 tion is not explicitly included in our numerical model, higher frequency wave
274 amplitudes are artificially attenuated faster than lower frequency waves due
275 to numerical dispersion and dissipation errors present in the finite element
276 method. In this sense there is some form of anelastic attenuation present in
277 our numerical model in addition to the elastic effects we explicitly include:
278 geometrical spreading, elastic focusing/defocusing, scattering and amplifica-
279 tion/reduction of seismic waves due to velocity contrast. We show the relative
280 importance of elastic focusing/defocusing (multipathing) effects by demon-

281 strating a good correlation between simulated stress patterns (Figures 2 –
282 4) and the ray paths calculated without incorporating anelastic or scattering
283 effects (Figure 5).

284 *4.3. Comparing alternative criteria for dynamic triggering*

285 To assess the contribution of stress wave focusing in promoting rupture
286 nucleation and triggered seismicity of a sharp bimaterial interface we con-
287 struct a set of simulations with a material heterogeneity that has no sharp
288 bimaterial interfaces. The rigidity is increasing smoothly from G_0 to G_A
289 towards the center of the heterogeneity. We compare the resulting stress
290 patterns to those in our typical simulations (e.g. compare Figure 6 with Fig-
291 ure 3) and to stress patterns in homogeneous simulations (see Supplementary
292 material). We observe that the far-field effects that could be explained with
293 wave focussing are still observed. However the interface effect along the bi-
294 material interfaces are missing or more likely distributed over a larger area
295 and thus weaker.

296 *4.4. Comparing the two measures used to estimate the likelihood of RTS*

297 The cumulative effect of seismic waves can be determined by calculating
298 the integrated energy density (Brodsky and Prejean, 2005). We present this
299 property here as several researchers (Hill et al., 1993; Brodsky et al., 2000)
300 assume cumulative energy to be important in triggering an earthquake. In
301 Figure 7 we calculate the cumulative squared velocity $E_c = \int \dot{u}^2 dt$ as a proxy

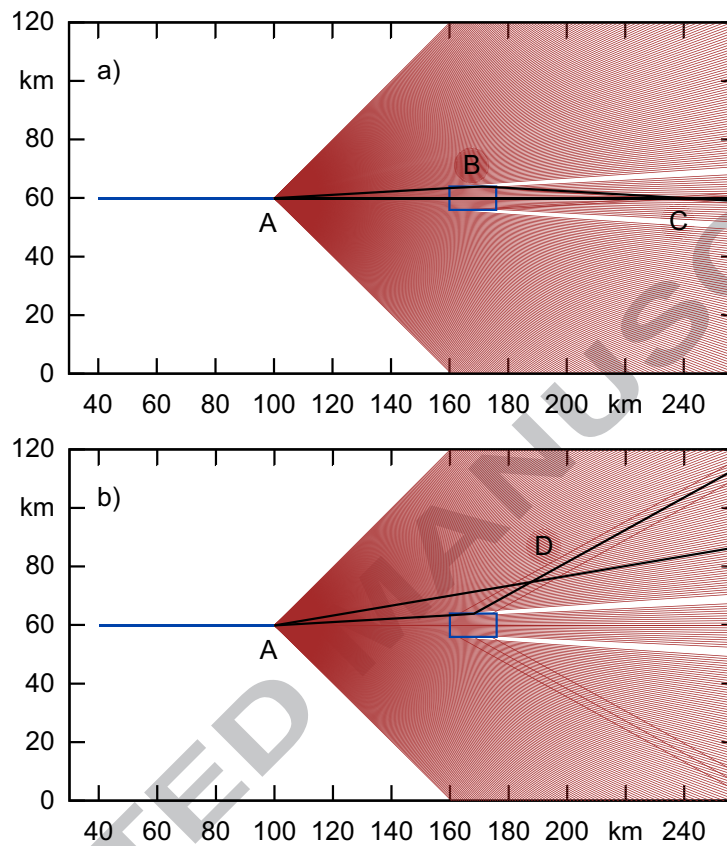


Figure 5: Calculated shear wave propagation paths using a simplified source model to compare with observed stress waves in FEM simulations with a) compliant (Figures 2, 3) and b) stiff (Figure 4) heterogeneities. Regions with overlapping ray paths are expected to have elevated CFS. As the reflected and non-reflected S-waves have similar ray path lengths there is only a slight delay. Wave crests may superimpose and increase peak transient CFS. In the stiff case (Figure b) this is partially due to the fact, that one path of overlapping waves has experienced an alteration in S-wave speed and the other has not. (A) shows the location of rupture arrest with a subset of emitted shear waves. (B) shows internal total reflection along the compliant zone interfaces. (C) shows the overlapping of ray path beyond the compliant zone and (D) shows the overlapping of ray paths past the stiff zone.

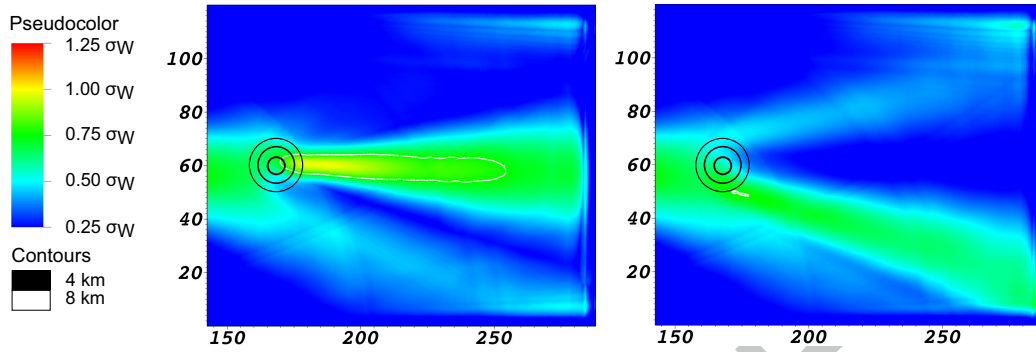


Figure 6: Comparing stress patterns in simulations with a circular heterogeneity with gradual transition between the materials, on the left with a compliant material anomaly and on the right with a stiff material anomaly.

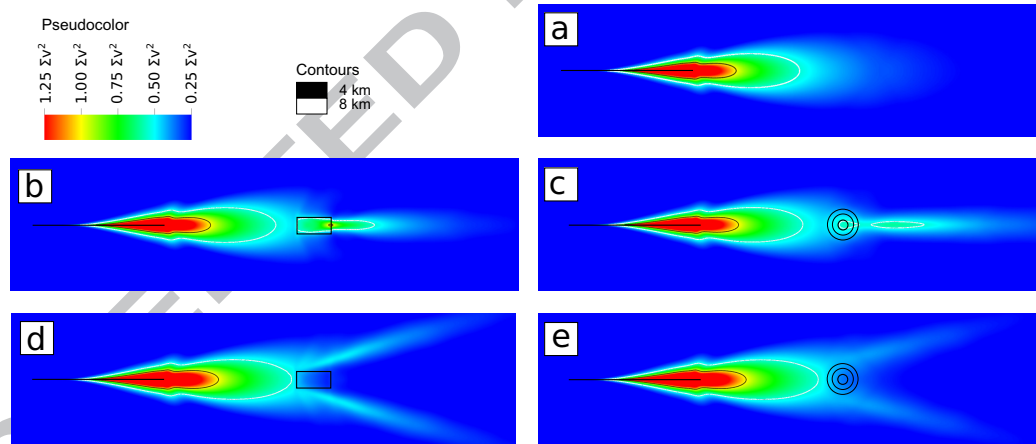


Figure 7: Overview showing normalized integrated squared velocity over the whole simulation time for a) no heterogeneity, b) a compliant rectangular bimaterial heterogeneity, c) a compliant circular smooth heterogeneity, d) a stiff rectangular bimaterial heterogeneity, e) a stiff circular smooth heterogeneity.

302 for integrated energy density. We normalise E_c to $E_{cn} = 1$ for the highest
303 value of E_c at the virtual fault from Figure 1. From Figure 7 we can see that:

- 304 1. In contrast to the plot with peak transient CFS the integrated energy
305 density is symmetric about the source fault. As mentioned in sub-
306 section 3.2 the asymmetry for peak transient CFS is due to non-zero
307 background stress and the way CFS is calculated. The background
308 particle velocity however is zero and therefore the amplitude of the
309 velocity vector depends solely on the dynamic component of particle
310 movement which results in a symmetric energy shape.
- 311 2. The focusing effect is significant even where the heterogeneity is not de-
312 limited by sharp bimaterial interfaces (see significant focusing in Figure
313 7c).
- 314 3. Only the superposition of the two effects (wave focusing and stress
315 enhancement along interfaces) is sufficient to induce integrated energy
316 density levels equivalent to those at ≈ 5 km from the rupture tip (a
317 level which suggest that RTS is plausible).
- 318 4. When comparing Figure 2 (top) and Figure 7b one can observe that
319 the 'potentially unstable' region near the heterogeneity seems much
320 smaller when considering the integrated energy index rather than the
321 peak transient CFS as a triggering criteria. That is, the area confined
322 by an 'energy level at 4 km' contour (Fig. 7b, black line) is much
323 smaller than that outlined by the 'stress level at 4 km' contour (Figure
324 2, black line). This shows that at least in our model the choice of an

325 indicator for seismic risk is important. Using the peak transient CFS
326 as an indicator means a much larger region would have to be considered
327 for seismic hazard assessment than if one used cumulative energy.

328 It has been shown in theoretical work on metamaterials (Farhat et al.,
329 2012) and in experiments (Dubois et al., 2013), that complex geometry and
330 material contrast may lead to local regions with low cumulative energy which
331 is in agreement with Figure 7d. This supports the notion that natural stress
332 focusing and stress shadows can be significant, and even could be as strong
333 as in artificial seismic cloaking experiments (Brûlé et al., 2014).

334 At larger distances between source fault and the heterogeneity ($>3-5$ fault
335 lengths) the focusing effect is expected to be minor compared to the effect
336 of bimaterial interface excitation. This can be seen when comparing the
337 two subfigures of Figure 3. The angle of reflecting waves along the top and
338 bottom edges of the heterogeneity gets lower with distance to the source fault
339 and thus less ray paths would be overlapping at similar location and time
340 (see Figure 5). The size and geometry of the heterogeneity can have various
341 effects on ray paths and stress enhancement. For example bent interfaces
342 could have a large effect in dispersing or focusing stresses. The effect would
343 depend on the direction of wave entry (like dispersing and converging lenses).
344 Secondly the stress lobes in and outside the heterogeneity would change, as
345 an elongated heterogeneity may behave like a fault zone that traps waves
346 and enhances stress within and along the interfaces.

347 5. Conclusions and implications for Seismic Hazard Analysis

348 While numerous studies have indicated that dynamic stress may be large
349 enough to trigger rupture at large distances from the source event, few pro-
350 vide explanations for the distribution and location of RTS and for the ob-
351 servations of recurring RTS. In such studies it is often assumed that pre-
352 stress levels alone determine which faults are brought to failure by dynamic
353 stress perturbations. This implies that until scientists are able to measure
354 pre-stress levels on each fault, it would be impossible to identify faults and
355 structures on which remotely triggered seismicity is more likely to occur. In
356 the present study we show that geological structures can induce, enhance and
357 focus stresses and achieve local CFS increase that is much higher than typi-
358 cally considered in studies of triggered seismicity. Such stress concentrations
359 can trigger an earthquake on faults that would otherwise not be considered
360 critically stressed. We propose a set of simple mechanisms that may be
361 used to explain the occurrence (and recurrence) of remotely triggered seis-
362 micity, and to assess whether certain fault-zones are susceptible to RTS. In
363 particular, our results show that geological structures (i.e. weak or stiff het-
364 erogeneities) can significantly influence stress enhancement and seismic wave
365 focusing, and therefore can promote the occurrence of RTS. This conclusion
366 is significantly supported by observations of geological structures that exhib-
367 ited RTS following more than one source earthquake (e.g. geothermal zones
368 exhibiting RTS after both the 1992 Landers and the 2002 Denali earthquakes;
369 Hill et al. (1993); Prejean et al. (2004)). It is further supported by indication

370 that seismic wave amplification, extended duration, and enhanced shaking
371 along the Queen Charlotte sedimentary trough enabled the remote triggering
372 of the 2013 M7.5 Craig Earthquake, British Columbia (Gomberg, 2013). Fi-
373 nally, our work asserts that geological structures such as accretionary prisms
374 along subduction zones and sedimentary basins along transform plate bound-
375 aries may constitute zones of enhanced probability for dynamic triggering (as
376 recently suggested by Gomberg (2013)). We therefore propose that detailed
377 models of dynamic stress interactions should be used to identify fault zones
378 that are likely to be triggered remotely by future earthquakes

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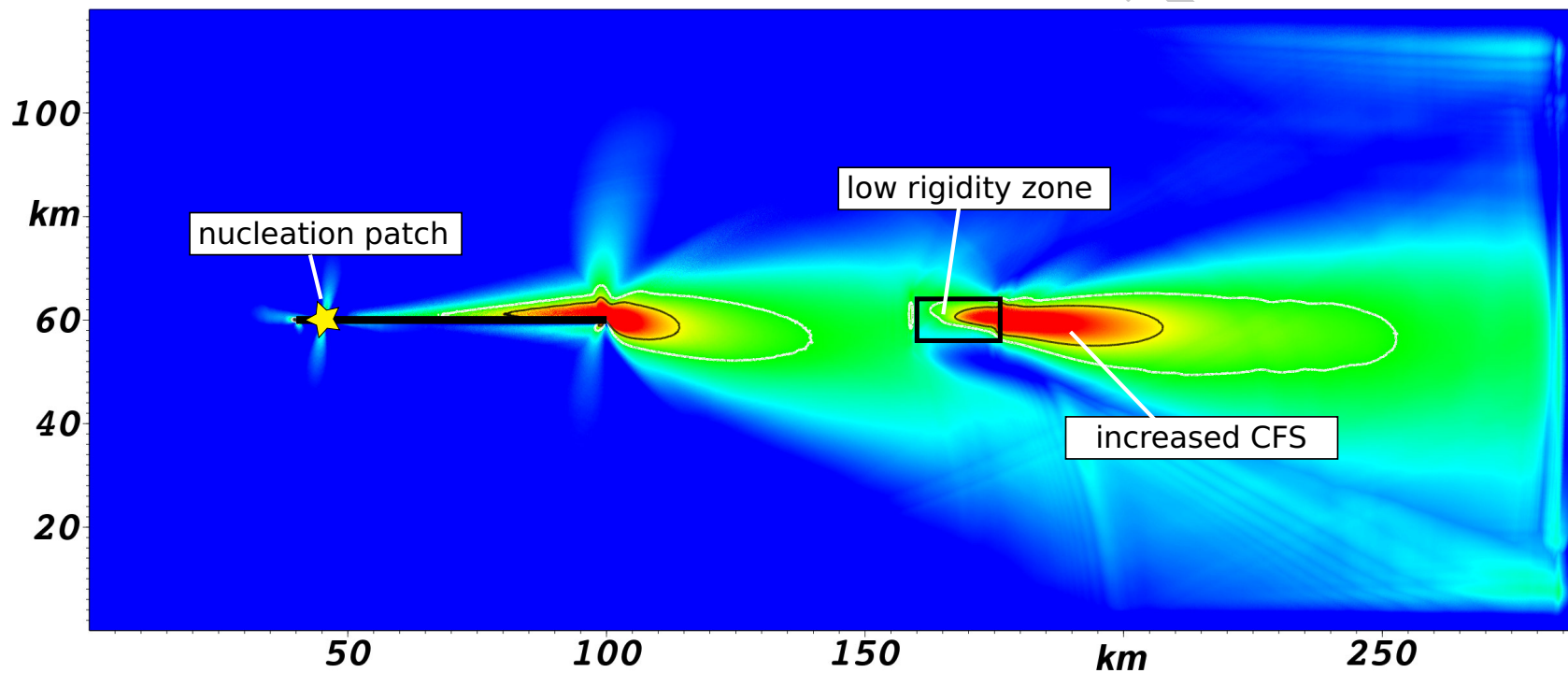
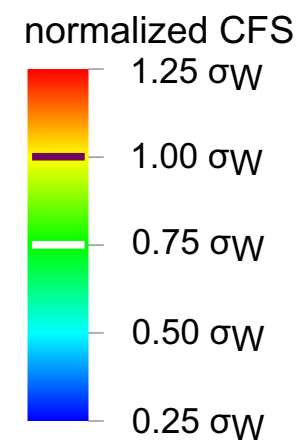
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Pseudocolor plot of peak transient Coulomb failure stress (CFS): At $\sigma_w \geq 1$ remotely triggered rupture nucleation is likely.

We simulate dynamic fault rupture and stress interactions in a heterogeneous model.

Dynamic stress levels around and beyond heterogeneities are significantly amplified.

These increased stress levels are strong enough to trigger earthquakes.

Basins and weak fault-zones are prone to experience remotely triggered seismicity.

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