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Re-implementation of TranSIESTA and N-terminal NEGF

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Abstract

DFT+NEGF methods are the basis of theoretically calculating the transport properties of nanostructures. In TranSIESTA [1, 2] the NEGF implementation is currently scaling with N^3 which limits the sizes of systems, in terms of orbitals, that can be investigated. In this work we present a re-implementation of TranSIESTA which scales order- N . Using the intrinsic block-tri-diagonal form of the Hamiltonian we use the recursive Green's function method to calculate the density matrix in non-equilibrium. We also report of TranSIESTA being extended to handle $N \geq 1$ electrodes in a generic implementation to allow the investigation of complex structures, the N -electrode setup is straight forwardly implemented and extended similarly to [3].

Re-implementation of TranSIESTA DFT-NEGF method

- Governing NEGF equations

$$\rho_{\text{neq}} \propto -\frac{1}{\pi} \int_{-\infty, \text{BZ}}^{\infty} d\epsilon d\mathbf{k} \left[\mathbf{G}_{\mathbf{k}}(\epsilon) - \mathbf{G}_{\mathbf{k}}^{\dagger}(\epsilon) \right] \eta_F(\epsilon)$$

$$\rho_{\text{neq}} \propto -\frac{1}{\pi} \int_{-\infty, \text{BZ}}^{\infty} d\epsilon d\mathbf{k} \left\{ \left[\mathbf{G}_{\mathbf{k}}(\epsilon) - \mathbf{G}_{\mathbf{k}}^{\dagger}(\epsilon) \right] \eta_{F, \epsilon_1}(\epsilon) - \mathbf{G}_{\mathbf{k}}(\epsilon) \sum_{\epsilon' \neq \mu_{\epsilon} \neq \mu_{\epsilon'}} \Gamma_{\epsilon, \mathbf{k}}(\epsilon') \left[\eta_{F, \epsilon'}(\epsilon) - \eta_{F, \epsilon_1}(\epsilon) \right] \mathbf{G}_{\mathbf{k}}^{\dagger}(\epsilon) \right\}$$

- Full sparsity pattern utilisation (huge memory decrease)
- Calculating $\mathbf{G}_{\mathbf{k}}(\epsilon)$:

$$\mathbf{G}_{\mathbf{k}}^{-1}(\epsilon) = \epsilon \mathbf{S}_{\mathbf{k}} - \mathbf{H}_{\mathbf{k}} - \sum_{\epsilon} \Sigma_{\mathbf{k}}^{\epsilon}(\epsilon) = \begin{pmatrix} A_1 & C_2 & 0 & \dots \\ B_1 & A_2 & C_3 & 0 & \dots \\ 0 & B_2 & \dots & \dots & \dots \\ \dots & 0 & \dots & \dots & C_p \\ \dots & \dots & \dots & B_{p-1} & A_p \end{pmatrix}$$

- Block-tri-diagonal (BTD) Hamiltonian is intrinsic, algorithm for inverting BTD [4, 5] (recursive Green's function method)
- Non-equilibrium contour integral correction term:

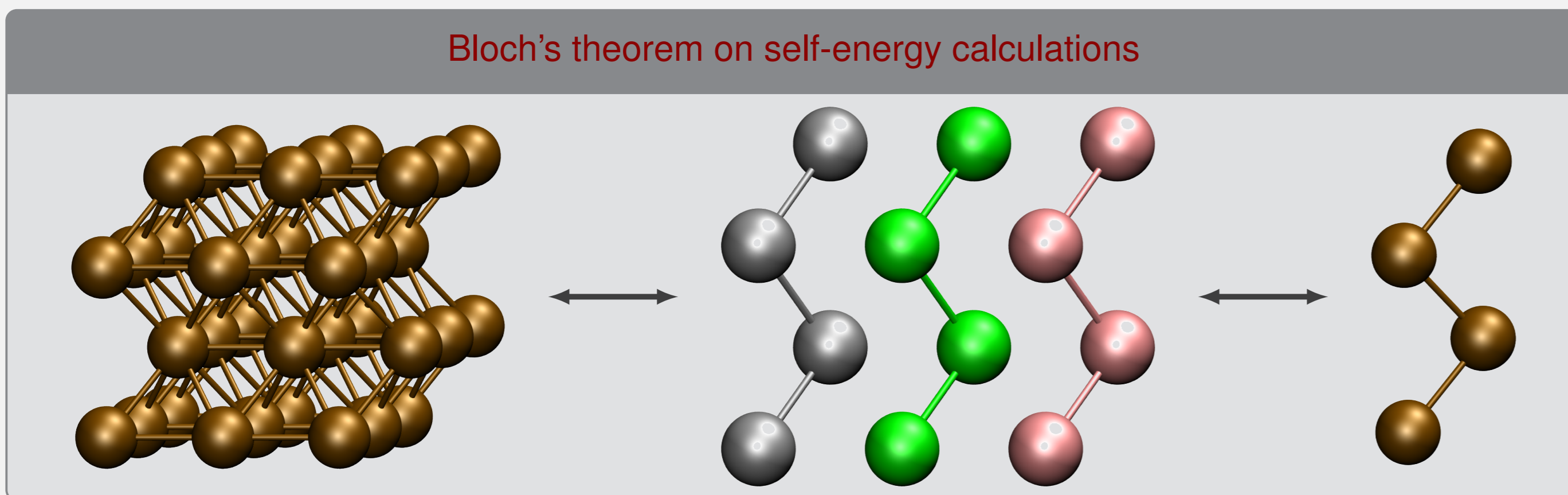
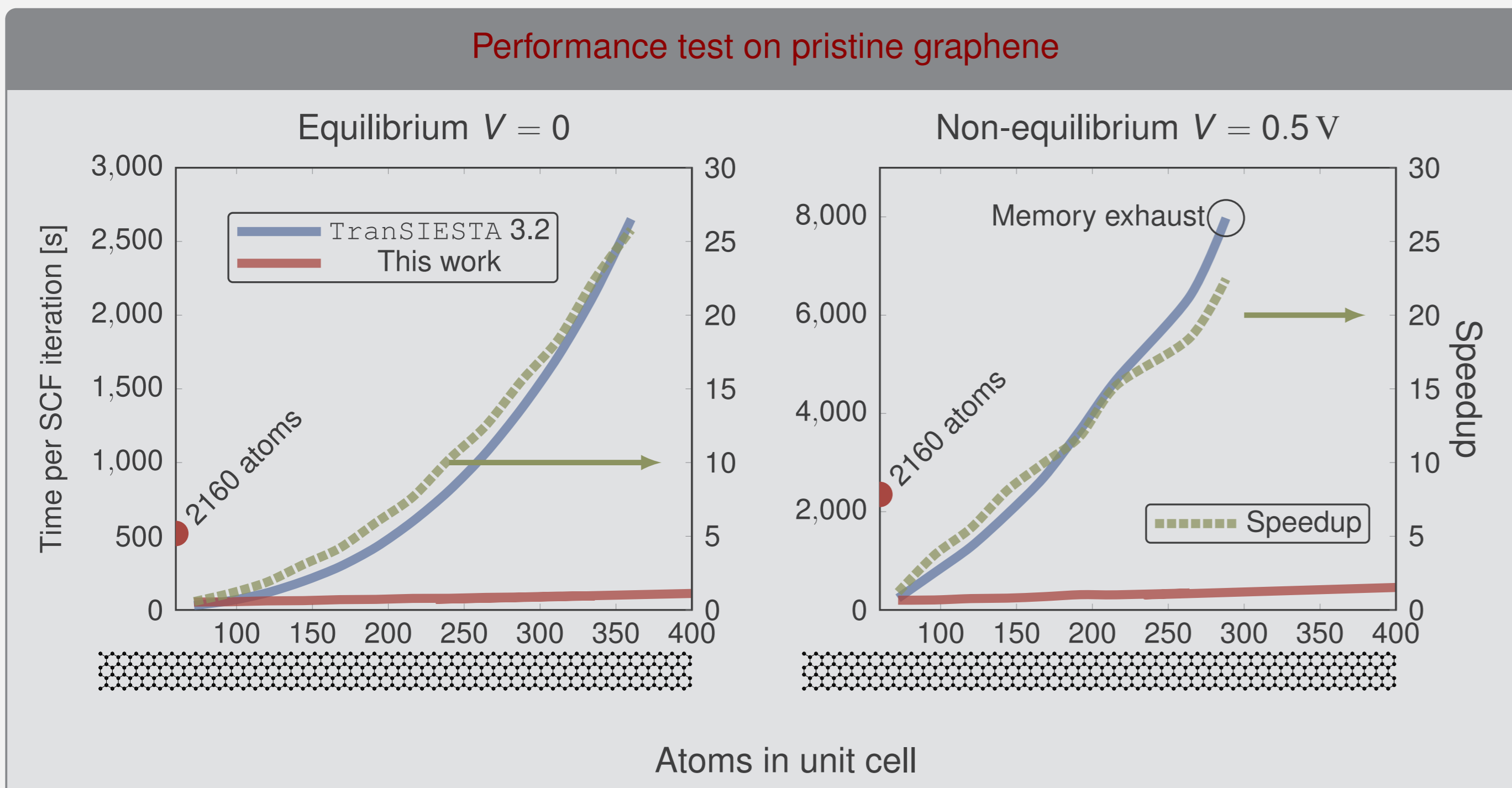
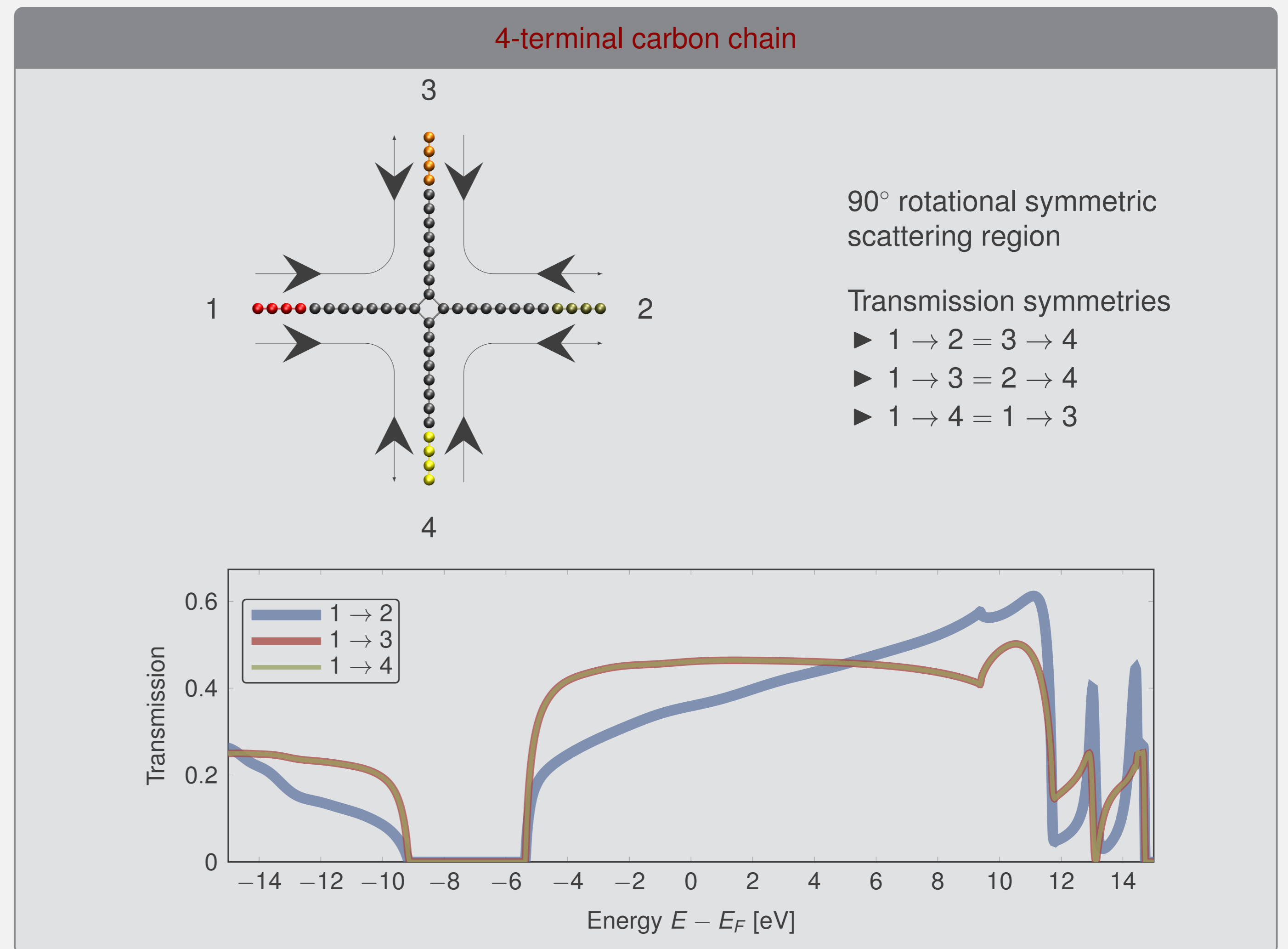
$$\Delta_{\mathbf{k}}^{\epsilon} \propto \mathbf{G}_{\mathbf{k}}(\epsilon) \Gamma_{\mathbf{k}}^{\epsilon}(\epsilon) \mathbf{G}_{\mathbf{k}}^{\dagger}(\epsilon)$$

Only part of the Greens function is needed:

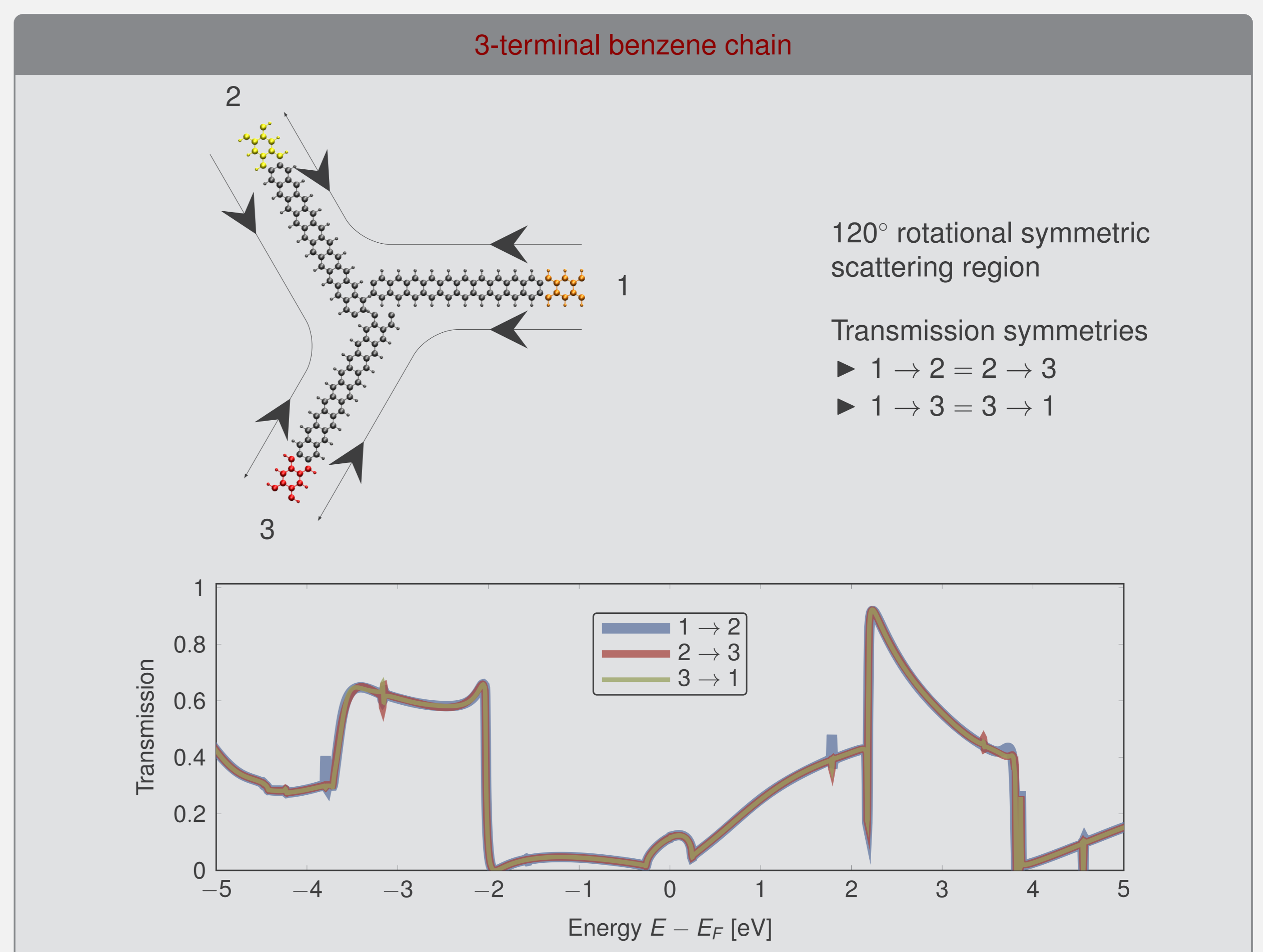
$$\mathbf{G}_{\mathbf{k}}(\epsilon) \Gamma_{\mathbf{k}}^{\epsilon}(\epsilon) \mathbf{G}_{\mathbf{k}}^{\dagger}(\epsilon) \rightarrow \begin{matrix} \blacksquare & \blacksquare & \blacksquare \\ \blacksquare & \blacksquare & \blacksquare \\ \blacksquare & \blacksquare & \blacksquare \end{matrix} \equiv \begin{matrix} \blacksquare & \blacksquare \\ \blacksquare & \blacksquare \end{matrix}$$

- TranSIESTA is generalised for complete N -terminal NEGF solution method

- $N = 1$ allows slab calculations using the Green's function technique which ensures a bulk slab
- $N > 2$ allows complex electrode structures
 - ▷ STM setups (3-terminal devices)
 - ▷ Molecules attached to several terminals



- Using the MUMPS library [6, 7], we also implement TranSIESTA in a fully sparse method allowing the user to decide amongst algorithms
- Improved contour algorithms to better approximate $\int d\epsilon$ integrals
 - ▷ Gauss-Fermi quadrature re-calculated
 - ▷ Gauss-Legendre, utilise DOS position in complex plane to reduce points
 - ▷ Composite Newton-Cotes methods implemented for non-equilibrium, Simpson, Simpson 3/8, Boole



Conclusion

- Re-implemented TranSIESTA to realise bigger simulation cells
- Using recursive Green's function methods we achieve an order- N scaling for extended systems
- Implemented a fully sparse solution method which is based on the MUMPS library
- Reducing computational load by only calculating *what is needed*
- Utilising Bloch's theorem we reduce complexity of periodic electrodes by expanding self-energies
- Improved algorithms for estimating the integration in the complex plane and along the real-axis
- Generalised TranSIESTA to handle N -electrodes, taking advantage of the above mentioned computational improvements

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