

Electric-Double-Layer-Modulation Microscopy

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The electric double layer (EDL) formed around charged nanostructures at the liquid-solid interface determines their electrochemical activity and influences their electrical and optical polarizability. We experimentally demonstrate that restructuring of the EDL at the nanoscale can be detected by dark-field scattering microscopy. Temporal and spatial characterization of the scattering signal demonstrates that the potentiodynamic optical contrast is proportional to the accumulated charge of polarizable ions at the interface and that its time derivative represents the nanoscale ionic current. The material specificity of the EDL formation is used in our work as a label-free contrast mechanism to image nanostructures and perform spatially resolved cyclic voltammetry on an ion-current density of a few attoamperes, corresponding to the exchange of only a few hundred ions.

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I. INTRODUCTION

The storage and recovery of energy in batteries, solvation of molecules, filtration by membranes, and many transport processes in liquid environments are dictated by the interaction of ions with charged surfaces and the formation of the electric double layer (EDL) [1]. The EDL consists of a layer of ions in solution that screens the surface charge at the interface, with a thickness ranging from less than one to a few tens of nanometers, depending on the ionic strength of the solution. The formation of the EDL involves several time scales [2], such as the relaxation time $\tau_D = \lambda_D^2/D$, where D is the diffusion constant and λ_D is the Debye length, and the charging time $\tau_c = \lambda_D L/D$, where L is the representative system size. The Debye length is often used as a measure of the EDL thickness. The small volumes and short time scales associated with the formation of the EDL make direct access to its local dynamics experimentally challenging. Previous experimental observations of the EDL on the nanoscale have been based on amperometric measurements with scanning-probe methods [3,4], nanopores [5,6], or ultramicroelectrodes [7,8], which require a current signal above the background thermal current fluctuations. Visualization of the contrast of the EDL optically, on the other hand, probes the accumulated charge and provides direct access to spatial information of the ionic current. Optical study of the spatial ion accumulation and transport is an enabling approach, built on a distinct working principle, which combines the power

of optical microscopy with electrochemical amperometric analysis.

Changes to the optical reflectivity of a homogeneous flat electrode in contact with an electrolyte as a function of its electric potential, referred to as electroreflectance, have been observed previously and attributed to modulations of the optical properties of both the metal and the electrolyte [9,10]. The connection between electroreflectance and the restructuring of the EDL has been postulated and tested for large flat surfaces using ellipsometry [11] but separation of the changes caused by conduction electrons in the metallic layer to electromodulation from the contribution of the electrolyte EDL has been challenging [12,13]. More recently, the influence of the electrode potential on elastic light scattering (ELS) from plasmonic nanoparticles that exhibit a localized plasmon resonance [14–16] and for two-dimensional materials [17] has been detected. In those experiments, the signal from the EDL is not separated from the plasmonic and electronic effects caused by variation of the charge density inside the nano-object or at the surface. The influence of the EDL on the scattering cross section of 5-nm silica nanoparticles has been indirectly measured by changing the salt concentration in a quantum-noise-limited measurement [18].

Here, we experimentally demonstrate that continuous tuning of the EDL composition can be directly visualized by measuring the ELS from any type of nanoparticle and even the surface roughness on top of a capacitively charged surface. We refer to this intensity change in the ELS as the potentiodynamic optical contrast (PDOC). The temporal response of the PDOC is influenced mostly by the

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physical adsorption of counter ions with different optical polarizability (related to bulk refractive index) compared to the solvent. We demonstrate this effect by quantifying the temporal relaxation of the PDOC, which is directly related to the charging time of the EDL. We also show that the magnitude of the PDOC is related to the optical polarizability of the ions. We observe that deposited nanoparticles from other materials exhibit a different pattern than the underlying indium-tin-oxide (ITO) substrate due to different electrochemical properties. This difference enables visualization of small nanoparticles that otherwise cannot be differentiated from background scattering. By accurately measuring the PDOC as a function of applied potential, we can perform the optical equivalent of cyclic voltammetry, at the attoampere-current level, on a single nanoparticle.

II. POTENTIODYNAMIC OPTICAL CONTRAST OF THE EDL

In this section, we present an estimation for the expected PDOC that is caused by the change in the ion concentrations inside the EDL as a function of the surface potential. The details of this derivation are presented in the Appendix A. We use a nanosphere with a uniformly charged surface as a model system. Because we are mainly interested in the ELS from the EDL, we only consider changes due to the reconfiguration of ions outside the particle. The optical contrast of the EDL can be used to study dielectric particles, semiconductor nanocrystals, and metallic scatterers with plasmon resonance frequencies far from the visible range.

Because the EDL is much thinner than the wavelength of the incident light, the details of the charge distribution inside the EDL have a negligible influence on the ELS intensity. This model matches the physical conditions for surface potentials much larger than the characteristic potential $k_B T/e \approx 25$ mV, in which the charge screening is mostly due to the Stern layer. The total number of excess counter ions, N , necessary for screening the nanosphere at surface potential V is given by $(Ve/k_B T)(a^2/\lambda_B \lambda_S)$, where λ_B is the Bjerrum length and λ_S represents the thickness of the charge screening layer. In the Rayleigh scattering regime, the polarizability of the combined system of the nanosphere and the EDL is a volumetric sum of its constituents. Using the Rayleigh polarizability and the phenomenological linear relation between the refractive index and the salt concentration $n_{\text{mix}} = n_w + Kx_s$, where x_s is the ratio between the number densities of the salt ions and the solvent molecules [19] and n_w is the refractive index of water, we arrive at the scaling result

$$\frac{\alpha_{\text{EDL}}}{\alpha_p} \simeq \frac{2K(m^2 + 2)}{n_w(m^2 - 1)} \frac{\frac{Ve}{k_B T}}{4\pi a \lambda_B \lambda_S \rho_w}, \quad (1)$$

where ρ_w is the number density of water molecules (considering an aqueous solution) and m is the ratio between the refractive indexes of the particle and the water. For a typical dielectric material ($m = 1.3$) and alkali-halide salts [19], the prefactor is roughly 3. Using $\rho_w = 33 \text{ nm}^{-3}$ and $\lambda_B = 0.7 \text{ nm}$ for water and a typical $\lambda_S = 1 \text{ nm}$, we arrive at $\alpha_{\text{EDL}}/\alpha_p \approx 0.04$ for a 10-nm (-radius) nanoparticle in a NaCl solution at a surface potential of $V = 1 \text{ V}$.

III. EDL-MODULATION MICROSCOPY

To image such small changes in polarizability due to the reconfiguration of the EDL, we use a customized total-internal-reflection optical microscope. Similar to other interferometric-enhanced imaging techniques [20,21], the static scattering from the nanoparticle acts as a reference for the homodyne detection of the changes in the polarizability of the (subwavelength) particle surroundings. Ultimately, the imaging resolution is fixed by the optical diffraction. Therefore, the measured signal in each diffraction-limited spot is proportional to the total change of the EDL polarizability in the diffraction volume. It is essential that the reference intensity is kept stable, with fluctuations smaller than the scattering contribution from the EDL. For our measurements, the signal-to-reference ratio is on the order of 10^{-3} to 10^{-2} .

IV. RESULTS

We perform PDOC measurements on nanoparticles or grown nanostructures on top of ITO-coated glass cover slips (Diamond Coatings, 70–100 ohms per square). As the counter electrode, we use a second ITO-coated acrylic sheet separated from the substrate using double-sided adhesive tape, forming a 100- μm -thick flow cell. This configuration enables liquid exchange inside the flow cell while investigating the same field of view of the substrate with different electrolyte solutions. Unless specified otherwise, the applied potentials have a balanced triangle-shape waveform and the scattering images are recorded at 200 frames/s.

In Fig. 1, we present a typical scattering image of the surface of the ITO substrate. The ITO surface contains regions of high scattering intensity in the shape of parallelograms [see Fig. 1(b)], with sharp edges and corners, in the middle of comparatively smoother regions of 10 times to 100 times lower scattering signal. Using an atomic force microscope, we can detect the presence of sparse grains of height roughly 20 nm in geometrically recognisable areas [Fig. 1(e)]. The sharp boundaries confining these grains are indicative of the crystallographic origin of their formation, attributed to the stress release in the deposited layer during the annealing of ITO [22,23]. We can use the fairly homogeneous size distribution of

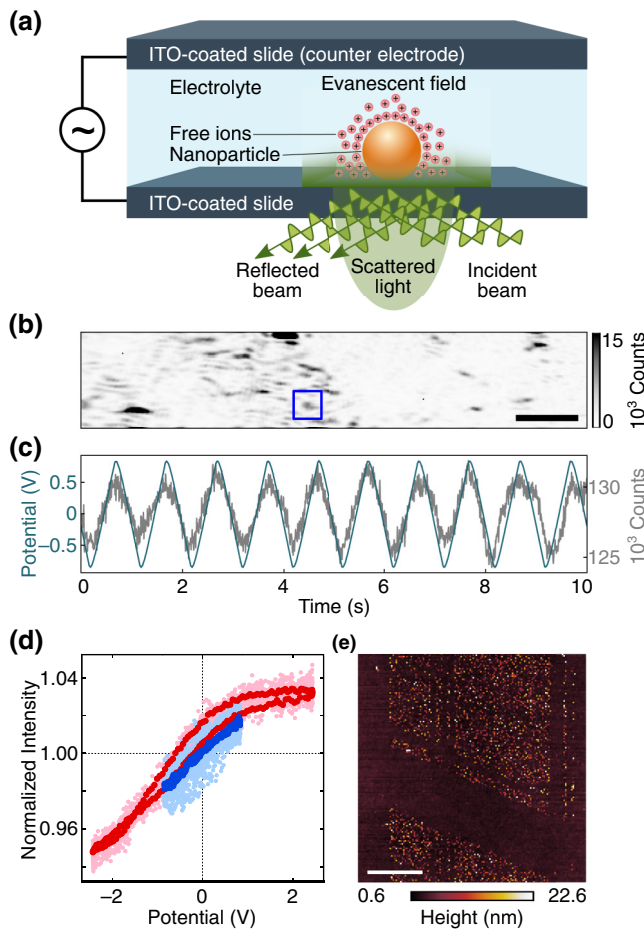


FIG. 1. Measurement of the potentiodynamic contrast of the EDL on a rough surface. (a) The setup for measurement of the PDOC and the electrochemical cell configuration. (b) A typical scattering image from the ITO surface (scale bar $2\mu\text{m}$). (c) The scattering intensity from the grain, annotated by a square in (b), plotted while changing the surface potential in a triangle-shape waveform. (d) The normalized intensity change plotted as a function of the cell potential for 100 cycles (light symbols) and the average of all cycles after correction for drift (bold symbols) for two different sweeping amplitudes. (e) An atomic-force-microscope scan of the ITO surface (scale bar $4\mu\text{m}$).

these grains on the ITO rough regions, and the straight boundaries of these regions, to distinguish between ITO grains and other particles or contamination that resides on the surface. For the cell potentials and electrolyte solutions used here, the ITO surface proves to be very stable and shows no irreversible change for a phosphate buffer at pH 7, when the cell potential is kept within ± 1.5 V.

Due to their electrochemical stability, we can use the ITO nanograins as reference scatterers for measuring the EDL signal. We record the ELS while alternating the potential of the ITO substrate relative to the counter electrode. By subtracting the average scattering signal over

an entire cycle from each frame, we obtain the PDOC and simultaneously correct for any drift in background intensity. For some of the spots, these intensity oscillations are visible above the measurement noise, even for a single cycle, after correcting for the drift. Figure 1(b) depicts the average dark-field scattering image of the ITO surface. The ELS intensity from a single speckle spot is plotted in Fig. 1(c) as a function of the applied potential for ten cycles. For low cell potentials, the relation between the contrast and the substrate potential is close to linear at any instant, in agreement with the prediction for EDL restructuring. At higher potentials, however, we observe a nonlinear dependence and a phase lag between the PDOC and the applied potential [Fig. 1(d)].

Next, we investigate the time dependence of the PDOC for a linear sweep and for a step reversal of the substrate potential, while simultaneously measuring the current passing through the cell. For a linear sweep, the electric current reaches a constant value after a certain relaxation time. The PDOC follows the potential with a lag that is comparable to that relaxation time and matches the charging time τ_c of the flow cell. This relaxation behavior is more evident when applying a square potential, in which the current stops after τ_c , due to screening, and the PDOC saturates. The saturation of the current for a linear potential sweep and relaxation to null for a step change in the potential both point toward the absence of sustained Faradaic currents at the electrodes. To make a direct comparison, we plot the integrated electric current during the cycle, i.e., the accumulated charge, on top of the PDOC signal (Fig. 2). We observe an almost perfect overlap between the two curves, confirming that the PDOC is proportional to the accumulated charge at the substrate.

While the above observations demonstrate the surface-charging origin of the PDOC, they are insufficient to distinguish between reconfiguration of the EDL and the redox reactions at the surface of the ITO, also known as pseudocapacitance charging [24]. To differentiate between these two effects, we investigate the PDOC response on the same ITO grain for three different anions in the electrolyte solution. Typical responses are shown in Fig. 3(a), next to the simultaneously measured electric current passing through the cell. While the electric current is the same for the three ions, the PDOC in the presence of NaI is almost twice that of NaCl and NaBr for the same cell potential. This observation can be explained by the optical polarizability of the iodide ions relative to chloride and bromide. While the exact calculation of the change in the refractive index of the EDL would require an accurate consideration of the ion hydration and is beyond the scope of this paper, it has been shown empirically that the change in the refractive index is almost proportional to the atomic polarizability [19].

We also observe a difference in the temporal phase lag between the PDOC response and the cell potential for

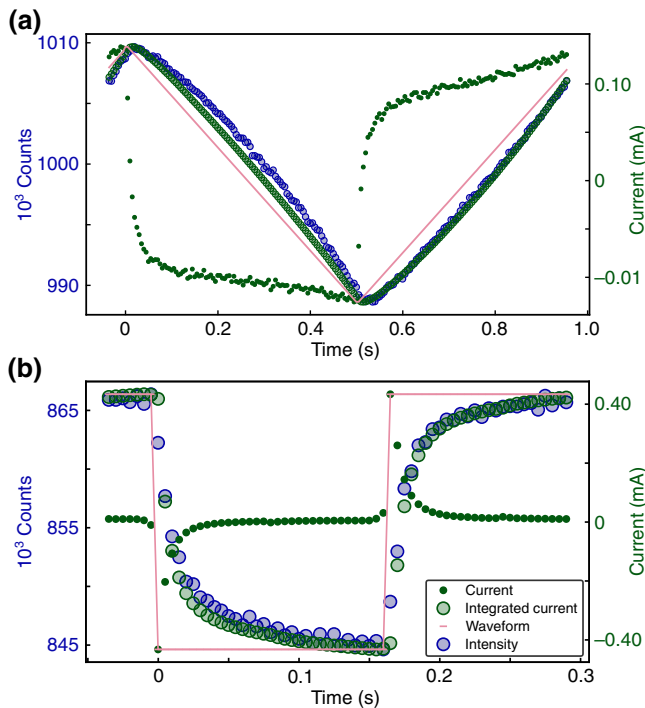


FIG. 2. The optical signal from the electric double layer under a variable surface potential: The measured electric current through the cell for an alternating voltage of (a) a triangle-shape and (b) a square waveform between +1 and -1 V. In both (a) and (b), the measured current is shown using green dots and the applied potential is shown using pink dots. The integrated current (green circles), which corresponds to the accumulated charge at the interface, shows the same temporal behavior as the measured scattering intensity (blue circles, averaged value over several cycles). The exponential change of the current toward equilibrium corresponds to the charging time of the electrochemical cell.

the three electrolytes. This difference is also observed in the electrical measurements and can be attributed to the difference in the surface adsorption dynamics for the three ions. The I - V curves measured simultaneously also exhibit this difference.

We have shown, hitherto, that the PDOC obtained by dark-field ELS microscopy is an optical indicator of the optical polarizability of accumulated ions (charges) around ridges or grains on a flat substrate. Furthermore, we observe that the temporal hysteresis behavior of the cyclic optical contrast depends on both the type of salt and the sweeping rate of the cell potential. As such, the PDOC of each grain can be viewed as a local nano-electroscope placed directly on the surface that can be used for studying the heterogeneity of surface interactions with the electrolyte, akin to conventional cyclic voltammetry. While, for electrochemically inert ITO, the EDL reconfiguration is the main source of changes to the scattering intensity, other material-specific

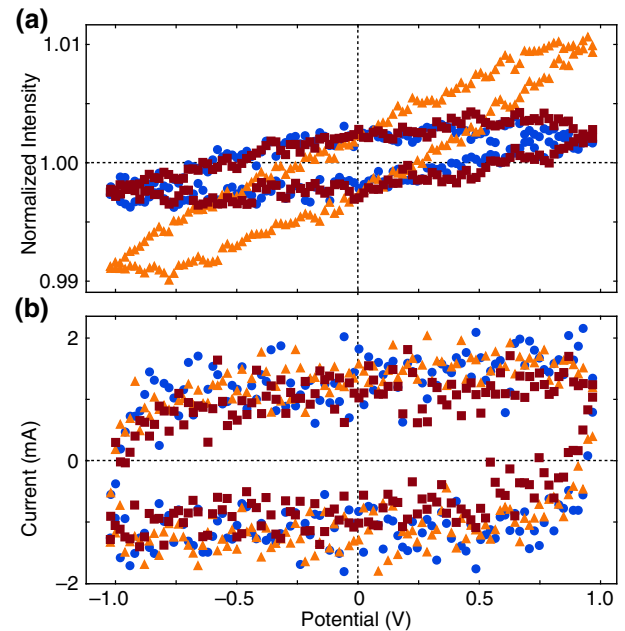


FIG. 3. (a) The average PDOC contrast for the same ITO grain for three different salts and (b) the electric cyclic voltammogram of the ITO substrate of the same measurements as in (a). The measured salts are NaCl (blue circles), NaBr (red squares), and NaI (orange triangles).

surface reactions can influence the dynamics. As such, the PDOC can be seen as a material-specific contrast mechanism. To showcase this specificity, we perform EDL-modulation microscopy of Cr nanoparticles deposited on ITO.

To fabricate a recognizable pattern, we deposit a few nanometers of Cr on the ITO-coated slides through a SiN membrane containing an array of micrometer-size holes, which is used as a stencil. We depict the recorded scattering image in Fig. 4(a). The ELS from Cr deposits is comparable in magnitude to that of the ITO grains in the rough regions. The Cr deposits can be identified by their geometrical arrangement on a triangular lattice, dictated by the stencil. The average PDOC over several cycles for one of the Cr particles and for one ITO grain are depicted in Figs. 4(c) and 4(d). We attribute this difference to electro-oxidation of the Cr deposits. We can identify all other positions on the surface that exhibit the same PDOC response by correlating each pixel intensity over time with the obtained reference. In Fig. 4(b), we depict the covariance of each pixel with the two different references corresponding to Cr and ITO particles, in blue and red, respectively. The position of the Cr deposits, colored in blue, matches the pattern expected from the triangular mesh used for deposition. This separation between the two materials cannot be done based on the scattering signal in panel (a).

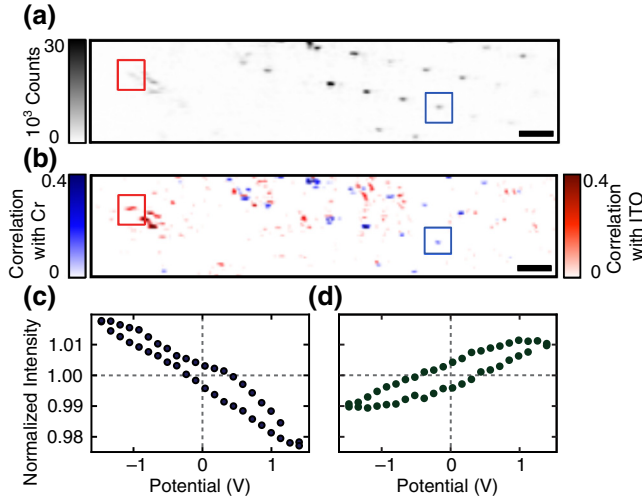


FIG. 4. (a) A dark-field scattering image of the ITO substrate after the deposition of Cr through a SiN stencil (scale bar $4\mu_m$). The deposition locations are on a triangular lattice. (b) The blue color scale shows the average covariance of each pixel intensity with the PDOC curve of a Cr particle, while the red color scale shows the covariance with the PDOC curve and an ITO grain. The corresponding reference PDOC curves are depicted in panels (c) and (d). All pixels with a covariance of less than 0.1 with either of the two references are colored in white for clarity.

V. DISCUSSION AND CONCLUSIONS

To conclude, we spatially resolve the reconfiguration of the EDL directly from changes to the optical contrast. At low potentials compared to the electrochemical reaction potential, using fully polarizable electrodes, the potentiodynamic scattering contrast is mostly due to the reconfiguration of the EDL. For higher potentials, surface adsorption or Faradaic reactions start to dominate changes in the optical contrast of the surface surroundings. EDL-modulation microscopy can thus be used to measure the deposition or formation of products on the surface. In this range, the shape and magnitude of the response depend on the sweeping rate. Given that particles as small as 10 nm are detected, the local current passing through this area for the slowest scan rates in our measurements is at the level of 10^{-18} A. By further studying the correspondence between different sweeping modes, EDL-modulation microscopy can build upon the vast knowledge obtained from electrochemical studies. This imaging technique provides significant additional information such as spatial resolution, sensitivity to surface heterogeneity, local ion accumulation, and the possibility of studying deposits, possibly down to single biomolecules. Another operation mode compatible with EDL-modulation microscopy involves a substrate covered with a thin insulating layer. In this mode, the ion configuration at the EDL can be altered by capacitive coupling and the Faradaic reaction will be completely

excluded. This possibility will extend applications to a range of electrolytes that are chemically corrosive for ITO.

While we choose dark-field imaging for this work, the use of EDL modulation as an optical contrast is fully compatible with interferometric scattering microscopy (ISCAT) [20,25]. This method has already proven to be sufficiently sensitive to detect and characterize single proteins based on their polarizability [26]. The combination of this remarkable sensitivity with potentiodynamic control creates a previously untapped contrast mechanism for the chemical-specific optical microscopy of single nanoparticles and single macromolecules. This possibility paves the way for the measurement of chemical reactions such as oxidation and reduction processes on a single protein, or their reaction with antibodies, for an extended period of time.

These results are subject to a priority patent application, UK 1903891.8, filed on March 21, 2019.

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APPENDIX A: ESTIMATION OF THE OPTICAL CONTRAST DUE TO EDL MODULATION

To estimate the change in the scattering amplitude due to the accumulation of ions in the EDL, we calculate the ratio of the polarizability of the thin screening layer to the polarizability of the nanoparticle in the limit of a very large surface potential $V \gg k_B T/e \approx 25$ mV. Because the EDL is much thinner than the wavelength of the incident light, the details of the charge distribution inside the EDL have a negligible influence on the ELS intensity. We consider the screening ions to be uniformly distributed in a layer of thickness $\lambda_S \ll a$, where a is the nanosphere radius. This is a proper approximation for large surface potentials because the screening is mostly due to the compact layer. The total number of excess monovalent ions N necessary for screening the nanosphere is given by $N = CV/e$, where C is the Stern-layer capacitance, $C = 4\pi\epsilon\epsilon_0 a^2/\lambda_S$, and e is the elementary charge. Using the definition of the Bjerrum length $\lambda_B = e^2/4\pi\epsilon\epsilon_0 k_B T$, we can write down the expression for N in a more insightful form:

$$N = \frac{a^2}{\lambda_B \lambda_S} \frac{Ve}{k_B T}. \quad (\text{A1})$$

Assuming a deeply subwavelength nanoparticle, we can use the Rayleigh approximation to calculate the polarizability. In the Rayleigh independent scattering regime, the polarizability of the combined system of the nanosphere and the EDL is the volumetric sum of its constituents. To estimate the optical polarizability of the EDL, we use the empirical linear relation between the refractive index and the salt concentration $n_{\text{mix}} = n_w + Kx_s$, where x_s is the ratio between the number densities of salt ions and solvent molecules [19] and n_w is the refractive index of water. Note that the value of K is only reported for neutral salt solutions. From polarizability considerations for the alkali-halide salts used in this work, the concentration of the halide ions is the dominant term for determining the refractive index of the salt-water mixture. We therefore can employ approximately the same coefficient K and use the excess anion density instead of the salt density in the refractive index change. Since we are interested in the relative changes of the polarizability, we can use any system of units. The Rayleigh polarizability of a scatterer in centimeter-gram-second (cgs) units is defined as

$$\alpha = 3V \frac{m^2 - 1}{m^2 + 2}, \quad (\text{A2})$$

where V is the volume and m is the refractive index of the object divided by that of the surrounding medium.

To estimate the polarizability of the EDL, we have to subtract the polarizability of the neutral solvent and to linear order with x_s , we obtain

$$\alpha_{\text{EDL}} = 4\pi a^2 \lambda_S \frac{2Kx_s}{n_w}. \quad (\text{A3})$$

We use the total number of excess ions at a given electrode potential to estimate the ratio

$$x_s = \frac{N}{4\pi a^2 \lambda_S \rho_w}, \quad (\text{A4})$$

where ρ_w is the number density of the water molecules and we again use the assumption that the screening charges are uniformly distributed in a layer of thickness $\lambda_S \ll a$. By combining Eqs. (A3) and (A4), we arrive at a simple formula for the EDL polarizability:

$$\alpha_{\text{EDL}} = \frac{2KN}{n_w \rho_w}. \quad (\text{A5})$$

It is worth mentioning that the EDL polarizability depends only on the total number of excess ions inside the double layer in the Rayleigh approximation that we use. Finally, we can combine this polarizability with that of the spherical scatterer to obtain Eq. (1) of the main text.

TABLE I. The anion polarizability and solid refractive indexes of the alkali-halide salts.

Salt	Anion polarizability	Solid refractive index
NaCl	14.6	1.54
NaBr	21	1.64
NaI	32	1.78

APPENDIX B: OPTICAL PROPERTIES OF ALKALI-HALIDE SALTS

We cannot find any measurement in the literature for the refractive index of solvated ions in the EDL. The anion polarizability of the halide anion [27] and bulk refractive index of the solid salt [28], collected in Table I, can be used as rough guide for comparing the measured potentiodynamic contrasts for the three salts used in this paper.

- [1] J. Lyklema, in *Fundamentals of Interface and Colloid Science* (Academic Press, London, 1995), Vol. 2, Chap. 3, p. 3.
- [2] Martin Z. Bazant, Katsuyo Thornton, and Armand Ajdari, Diffuse-charge dynamics in electrochemical systems, *Phys. Rev. E* **70**, 021506 (2004).
- [3] Liam Collins, Stephen Jesse, Jason I. Kilpatrick, Alexander Tselev, Oleksandr Varenyk, M. Baris Okatan, Stefan A. L. Weber, Amit Kumar, Nina Balke, Sergei V. Kalinin, and Brian J. Rodriguez, Probing charge screening dynamics and electrochemical processes at the solid-liquid interface with electrochemical force microscopy, *Nat. Commun.* **5**, 3871 (2014).
- [4] Cameron L. Bentley, James Edmondson, Gabriel N. Meloni, David Perry, Viacheslav Shkirskiy, and Patrick R. Unwin, Nanoscale electrochemical mapping, *Anal. Chem.* **91**, 84 (2019).
- [5] Ralph M. M. Smeets, Ulrich F. Keyser, Diego Krapf, Meng-Yue Wu, Nynke H. Dekker, and Cees Dekker, Salt dependence of ion transport and DNA translocation through solid-state nanopores, *Nano Lett.* **6**, 89 (2006).
- [6] Daniel G. Haywood, Anumita Saha-Shah, Lane A. Baker, and Stephen C. Jacobson, Fundamental studies of nanofluidics: Nanopores, nanochannels, and nanopipets, *Anal. Chem.* **87**, 172 (2015).
- [7] Xiaoyin Xiao and Allen J. Bard, Observing single nanoparticle collisions at an ultramicroelectrode by electrocatalytic amplification, *J. Am. Chem. Soc.* **129**, 9610 (2007).
- [8] T. Albrecht, S. Horswell, L. K. Allerston, N. V. Rees, and P. Rodriguez, Electrochemical processes at the nanoscale, *Curr. Opin. Electrochem.* **7**, 138 (2018).
- [9] Wilford N. Hansen and Arnold Probst, Electromodulation of the optical properties of gold, *Phys. Rev.* **174**, 500 (1968).

- [10] A. Bewick, F. A. Hawkins, and A. M. Tuxford, Studies of the electrical double layer and of adsorbed species on electrodes using modulated specular reflectance spectroscopy, *Surf. Sci.* **37**, 82 (1973).
- [11] Margaret Stedman, Effect of the electrical double layer on the reflectance and ellipsometry of electrolyte-conductor interfaces, *Chem. Phys. Lett.* **2**, 457 (1968).
- [12] J. D. E. McIntyre, Electrochemical modulation spectroscopy, *Surf. Sci.* **37**, 658 (1973).
- [13] D. M. Kolb, W. Boeck, Kai-Ming Ho, and S. H. Liu, Observation of Surface States on Ag(100) by Infrared and Visible Electroreflectance Spectroscopy, *Phys. Rev. Lett.* **47**, 1921 (1981).
- [14] Ana M. Brown, Matthew T. Sheldon, and Harry A. Atwater, Electrochemical tuning of the dielectric function of Au nanoparticles, *ACS Photonics* **2**, 459 (2015).
- [15] Caleb M. Hill, Robert Bennett, Chen Zhou, Shane Street, Jie Zheng, and Shanlin Pan, Single Ag nanoparticle spectroelectrochemistry via dark-field scattering and fluorescence microscopies, *J. Phys. Chem. C* **119**, 6760 (2015).
- [16] Chad P. Byers, Benjamin S. Hoener, Wei-Shun Chang, Stephan Link, and Christy F. Landes, Single-particle plasmon voltammetry (spPV) for detecting anion adsorption, *Nano Lett.* **16**, 2314 (2016).
- [17] Hao Zhu, Fenni Zhang, Hui Wang, Zhixing Lu, Hong-yuan Chen, Jinghong Li, and Nongjian Tao, Optical imaging of charges with atomically thin molybdenum disulfide, *ACS Nano* **13**, 2298 (2019).
- [18] N. P. Mauranyapin, L. S. Madsen, M. A. Taylor, M. Waleed, and W. P. Bowen, Evanescent single-molecule biosensing with quantum-limited precision, *Nat. Photonics* **11**, 477 (2017).
- [19] Ni An, Bilin Zhuang, Minglun Li, Yuyuan Lu, and Zhen-Gang Wang, Combined theoretical and experimental study of refractive indices of water-acetonitrile-salt systems, *J. Phys. Chem. B* **119**, 10701 (2015).
- [20] Philipp Kukura, Helge Ewers, Christian Müller, Alois Renn, Ari Helenius, and Vahid Sandoghdar, High-speed nanoscopic tracking of the position and orientation of a single virus, *Nat. Methods* **6**, 923 (2009).
- [21] Jaime Ortega Arroyo and Philipp Kukura, Non-fluorescent schemes for single-molecule detection, imaging and spectroscopy, *Nat. Photonics* **10**, 11 (2016).
- [22] G. Kavei, Y. Zare, and A. Mohammadi Gheidari, Evaluation of surface roughness and nanostructure of indium tin oxide (ITO) films by atomic force microscopy, *Scanning* **30**, 232 (2008).
- [23] S. Gardonio, L. Gregoratti, D. Scaini, C. Castellarin-Cudia, P. Dudin, P. Melpignano, V. Biondo, R. Zamboni, S. Caria, and M. Kiskinova, Characterization of indium tin oxide surfaces after KOH and HCl treatments, *Org. Electron.* **9**, 253 (2008).
- [24] Allen J. Bard, György Inzelt, and Fritz Scholz, *Electrochemical Dictionary* (Springer Science & Business Media, Heidelberg, 2008).
- [25] Gavin Young and Philipp Kukura, Interferometric scattering microscopy, *Annu. Rev. Phys. Chem.* **70**, 301 (2019).
- [26] Gavin Young *et al.*, Quantitative mass imaging of single biological macromolecules, *Science* **360**, 423 (2018).
- [27] Peter Schwerdtfeger and Jeffrey K. Nagle, 2018 table of static dipole polarizabilities of the neutral elements in the periodic table, *Mol. Phys.* **117**, 1200 (2019).
- [28] Mikhail N. Polyanskiy, Refractive index database, <https://refractiveindex.info>, accessed on 2019-07-26.