



**UNIVERSITI PUTRA MALAYSIA**

**PROBLEM RESTRUCTURING IN INTEGER PROGRAMMING  
FOR REDUCT SEARCHING**

**UNGKU AZMI ISKANDAR UNGKU CHULAN**

**FSKTM 2003 2**

**PROBLEM RESTRUCTURING IN INTEGER PROGRAMMING  
FOR REDUCT SEARCHING**

**UNGKU AZMI ISKANDAR UNGKU CHULAN**

**MASTER OF SCIENCE  
UNIVERSITI PUTRA MALAYSIA  
2003**



**PROBLEM RESTRUCTURING IN INTEGER PROGRAMMING  
FOR REDUCT SEARCHING**

**By**

**UNGKU AZMI ISKANDAR UNGKU CHULAN**

**Thesis Submitted to the School of Graduate Studies Universiti Putra Malaysia  
In Fulfillment of the Requirements for the Degree of Master of Science**

**May 2003**



***What's the best toy one man can find?***

***The mind, and its infinite possibilities.***



Abstract of thesis presented to the Senate of Universiti Putra Malaysia in fulfillment of the requirements for the degree of Master of Science.

**PROBLEM RESTRUCTURING IN INTEGER PROGRAMMING  
FOR REDUCT SEARCHING**

**By**

**UNGKU AZMI ISKANDAR UNGKU CHULAN**

**May 2003**

**Chairman : Associate Prof. Dr. Haji Md. Nasir Sulaiman**  
**Faculty : Computer Science and Information Technology**

Standard Integer Programming / Decision Related Integer Programming (SIP/DRIP) is a reduct searching system that finds the reducts in an information system. These reducts are the minimal attributes of the information system that are useful in classificatory task. They can describe the whole information system when implementing discernment. In effect, they are very useful in generating rules when solving the classification problem that is inherent in data mining.

The thesis emphasizes mainly on the improvement of the original SIP/DRIP algorithm in term of performance. By using problem restructuring, the searching time and memory are minimized. Simultaneously the approach adheres to an essential criterion of the original method. That is, to improve performance without sacrificing the quality of the reduct.



Problem restructuring changes the input of the SIP/DRIP without losing any of input's essential properties. In other words, no loss of knowledge occurs with problem restructuring. Only the structural order changes, with the contents kept intact. This hypothetically ensures that no adverse distortion transpired within SIP/DRIP.

Restructuring is done by speculating a promising structure for the input to SIP/DRIP based on the potentiality of the attributes in the information system. It uses a non-expensive approach to predict potentiality. Simply, based on the total covering of each attributes within the information system. Although this measurement is just an approximation, it can be proven to work.

To implement the experiment, five data sets were taken. They are gathered from the UCI machine learning repositories. Results are measured by comparing the performance of SIP/DRIP with and without problem restructuring. In addition, the length of reducts generated by both approaches are also compared to ensure that no quality deterioration occurred along the way.

Experimental results have shown that problem restructuring generally improves SIP/DRIP for all the data sets. This means that on average, it would enhance the performance of SIP/DRIP. The consumption of time and space were minimized quite significantly. Furthermore, the quality of the solutions was also successfully maintained. There was no increase in reduct length when using it.

The concept offered by the approach is an additional component to SIP/DRIP. It complements the process of searching done. By giving more consideration to the initial

problem space and not just the searching of the solution, the performance of SIP/DRIP has been humbly improved.

Abstrak tesis dikemukakan kepada Senat Universiti Putra Malaysia sebagai memenuhi keperluan untuk Master Sains.

**PENSTRUKTURAN MASALAH DALAM PENGATURCARAAN INTEGER  
UNTUK PENCARIAN REDUKSI**

Oleh

**UNGKU AZMI ISKANDAR UNGKU CHULAN**

**Mei 2003**

**Pengerusi : Prof. Madya Dr. Haji Md. Nasir Sulaiman**  
**Faculti : Sains Komputer dan Teknologi Maklumat**

'Standard Integer Programming / Decision Related Integer Programming' (SIP/DRIP) adalah sejenis sistem pencarian reduksi yang mencari reduksi minimum dalam sistem maklumat. Reduksi –reduksi minimum ini merupakan atribut minimum yang berguna dalam aktiviti pengelasan. Mereka boleh menerangkan keseluruhan sistem maklumat semasa proses pembezaan. Oleh itu, mereka amat berguna untuk menghasilkan undang-undang pengkelasan semasa menyelesaikan masalah pengkelasan, yang sememangnya biasa dalam perlombongan data.

Tesis ini menekankan kepada peningkatan prestasi algoritma SIP/DRIP. Dengan menggunakan penstrukturan masalah, masa carian dan penggunaan memori dapat diminimakan. Pendekatan ini tertakluk kepada kriteria utama SIP/DRIP, iaitu peningkatan prestasi tanpa menjejaskan kualiti reduksi minimum.



Penstrukturan masalah menstruktur semula input SIP/DRIP tanpa menghilangkan mana-mana sifat input yang penting. Dalam ertikata lain, tiada kehilangan maklumat yang berlaku dan hanya struktur urutan input yang berubah. Secara hipotesis, ini menjamin bahawa tiada kesan buruk akan berlaku ketika penggunaan SIP/DRIP bersama penstrukturan masalah.

Penstrukturan dilakukan dengan menjana spekulasi mengenai struktur yang baik berpandukan kepada potensi atribut dalam sistem maklumat. Ia menggunakan kaedah yang tidak terlalu mahal dalam meramalkan potensi atribut. Ini dilakukan dengan mengira jumlah tutupan yang dirangkumi oleh atribut di dalam sistem maklumat. Walaupun pengiraan ini hanyalah suatu anggaran, kegunaannya boleh dibuktikan.

Untuk menjalankan eksperimen, lima set data telah diambil. Mereka dikumpul daripada *UCI machine learning repositories*. Keputusan diukur dengan membandingkan output SIP/DRIP bersama penstrukturan masalah dan tanpanya. Sebagai tambahan, panjang reduksi yang dijanakan oleh kedua-dua pendekatan turut dibandingkan untuk memastikan bahawa tiada penjejasan kualiti berlaku.

Hasil eksperimen menunjukkan bahawa penstrukturan masalah secara kasarnya meningkatkan prestasi SIP/DRIP bagi kesemua set data. Ini bermaksud bahawa secara purata, ia meningkatkan prestasi SIP/DRIP. Penggunaan masa dan ruang memori bagi proses carian telah dikurangkan dengan signifikannya. Tambahan pula, kualiti reduksi telah berjaya dikekalkan. Tiada penambahan panjang reduksi berlaku semasa menggunakan penstrukturan masalah.

Konsep yang diutarakan oleh pendekatan ini adalah sebagai komponen tambahan kepada SIP/DRIP. Ia membantu proses carian dengan mempertimbangkan ruang asal masalah dan bukan hanya kepada proses carian. Dengan rendah diri, prestasi SIP/DRIP telah berjaya ditingkatkan.

## **ACKNOWLEDGEMENTS**

Alhamdulillah, all praises to Allah s.w.t, the only true God that rules the earth, and everything beyond it. Nothing can be accomplished without His consent. He is the all merciful, all giving. Never once has He left me in moments of despair. He is the all powerful, all knowing, the creator which bestowed me with the wisdom to take a pace in this odyssey of knowledge. I am forever indebted to His unconditional care.

I would like to express my greatest appreciation to the supervisor committee, lead by Assoc. Prof. Dr. Md. Nasir Sulaiman, Assoc. Prof. Dr. Ramlan Mahmood and Assoc. Prof. Mohd Hasan Selamat for their inspiring guidance and support in my quest for intellectual revelation. May Allah swt return their kindness and altruism. In addition, I would like to extend my gratitude to Dr. Azuraliza Abu Bakar and Pn. Norwati for their ongoing support and motivation that have helped me to overcome obstacles along the way. Finally, I thank my family and friends for their support, and everyone else that has helped and contributed to this research.

**Ungku Azmi Iskandar Ungku Chulan**

**May 2003**



I certify that an Examination Committee met on 9<sup>th</sup> of May 2003 to conduct the final examination of Ungku Azmi Iskandar Ungku Chulan on his Master of Science thesis entitled "Problem Restructuring in Integer Programming for Reduct Searching" in accordance with Universiti Pertanian Malaysia (Higher Degree) Act 1980 and Universiti Pertanian Malaysia (Higher Degree) Regulations 1981. The Committee recommends that the candidate be awarded the relevant degree. Members of the Examination Committee are as follows:

**ALI MAMAT, Ph. D.**

Associate Professor  
Faculty of Computer Science and Information Technology  
Universiti Putra Malaysia  
(Chairman)

**MD. NASIR SULAIMAN, Ph.D.**

Associate Professor  
Faculty of Computer Science and Information Technology  
Universiti Putra Malaysia  
(Member)

**RAMLAN MAHMUD, Ph.D.**

Associate Professor  
Faculty of Computer Science and Information Technology  
Universiti Putra Malaysia  
(Member)

**HASAN SELAMAT**

Associate Professor  
Faculty of Computer Science and Information Technology  
Universiti Putra Malaysia  
(Member)



---

**GULAM RUSUL RAHMAT ALI, Ph.D.**  
Professor/Deputy Dean  
School of Graduate Studies,  
Universiti Putra Malaysia

Date: 27 MAY 2003

This thesis is submitted to the Senate of University Putra Malaysia has been accepted as fulfillment of the requirements for the degree of Master of Science. The members of the Supervisory Committee are as follows:

**MD. NASIR SULAIMAN, Ph.D.**

Associate Professor  
Faculty of Computer Science and Information Technology  
Universiti Putra Malaysia  
(Member)

**RAMLAN MAHMUD, Ph.D.**

Associate Professor  
Faculty of Computer Science and Information Technology  
Universiti Putra Malaysia  
(Member)

**HASAN SELAMAT**

Associate Professor  
Faculty of Computer Science and Information Technology  
Universiti Putra Malaysia  
(Member)



---

**AINI IDERIS, Ph.D.**  
Professor/ Dean  
School of Graduate Studies  
Universiti Putra Malaysia

Date: 11 JUL 2003



## DECLARATION

I hereby declare that the thesis is based on my original work except for quotations and citations, which are given the proper acknowledgement. I also declare that it has not been previously submitted to any other degree at UPM or other institutions.



(Ungku Azmi Iskandar Ungku Chulan)

Date : 27/5/03

## TABLE OF CONTENTS

<b>DEDICATION</b>	ii
<b>ABSTRACT</b>	iii
<b>ABSTRAK</b>	vi
<b>ACKNOWLEDGEMENTS</b>	ix
<b>APPROVAL SHEET</b>	x
<b>DECLARATION FORM</b>	xiii
<b>LIST OF TABLES</b>	xv
<b>LIST OF FIGURES</b>	xvii
<b>LIST OF ABBREVIATIONS</b>	xx
<b>1 INTRODUCTION</b>	
1.1 Introduction	1
1.2 Problem Statement	3
1.3 Objective	4
1.4 Scope	4
1.5 Contribution	5
1.6 Organization of Thesis	5
<b>2 LITERATURE REVIEW</b>	
2.1 Introduction	8
2.2 Data Mining	10
2.2.1 Data Mining Task	11
2.2.2 Modeling Classification	14
2.2.3 Data Mining Challenges	16
2.3 Reduct Searching System	20
2.3.1 Genetic Algorithm	20
2.3.2 Holte 1R	23
2.3.3 Dynamic Reduct	25
2.3.4 SIP/DRIP	27
2.4 Summary	49
<b>3 REDUCT SEARCHING ADVANCEMENT</b>	
3.1 Introduction	50
3.2 Rough Sets and Classification	51
3.2.1 Set Covering Problem	53
3.2.2 Propositional Satisfiability Problem	55
3.3 Problem Representation	56
3.4 Reduct Searching System	58
3.4.1 SIP/DRIP	58
3.4.2 Branch and Bound	64
3.4.3 Input Processing	65
	70



3.5	Searching Process	71
3.5.1	Proposing Solution	72
3.5.2	Computing Solution	74
3.5.3	Conflict Analysis	77
3.5.4	Non-chronological Backtracking	79
3.5.5	Updating the Problem Space	81
3.5.6	Algorithm	83
3.6	SIP/DRIP Complexity	84
3.7	Benefits and Disadvantages	85
3.8	Problem Restructuring	86
3.8.1	Motivation	90
3.8.2	Understanding Problem Restructuring	96
3.8.3	Analyzing Problem Structure	105
3.8.4	Restructuring the Problem Structure	107
3.8.5	Space and Time Complexity	110
3.8.6	Semantics of Problem Structure	114
3.8.7	Illustration of Errors and Probable Solutions	118
3.8.8	Rationale of Non Deterministic Solution	119
3.8.9	Benefits and Risks of Problem Restructuring	122
3.8.10	Related Approach	126
3.9	Summary	
<b>4</b>	<b>EXPERIMENTATION AND RESULTS</b>	
4.1	Introduction	128
4.2	Implementation of Experiment	131
4.3	Experimentation Cases	136
4.3.1	Australian Credit Card (AUS)	137
4.3.2	Cleveland Heart Disease (CLV)	141
4.3.3	Lymphography (LYM)	145
4.3.4	American Mushroom (AM)	149
4.3.5	Voting Records (VR)	153
4.4	Discussion	157
4.5	Summary	165
<b>5</b>	<b>CONCLUSION AND FUTURE WORK</b>	
5.1	Conclusion	167
5.2	Future Work	170
	<b>BIBLIOGRAPHY</b>	173
	<b>APPENDICES</b>	





## LIST OF TABLES

<b>Table</b>	<b>Page</b>
3.0 Space Complexity	108
3.1 Static Variable Ordering and Problem Restructuring	125
3.2 CSP, SCP and SAT	126
4.1 Node (AUS)	137
4.2 Time (AUS)	137
4.3a Node Severity and Improvement – Frequency and Average (AUS)	138
4.3b Node Severity and Improvement - Maximum and Minimum (AUS)	138
4.4a Time Severity and Improvement – Frequency and Average (AUS)	139
4.4b Time Severity and Improvement - Maximum and Minimum (AUS)	139
4.5 Quality of Solution (AUS)	140
4.6 Node (CLV)	141
4.7 Time (CLV)	142
4.8a Node Severity and Improvement - Frequency and Average (CLV)	142
4.8b Node Severity and Improvement - Maximum and Minimum (CLV)	142
4.9a Time Severity and Improvement - Frequency and Average (CLV)	143
4.9b Time Severity and Improvement - Maximum and Minimum (CLV)	143
4.10 Quality of Solution (CLV)	144
4.11 Node (LYM)	145
4.12 Time (LYM)	146
4.13a Node Severity and Improvement - Frequency and Average (LYM)	146
4.13b Node Severity and Improvement - Maximum and Minimum (LYM)	146



4.14a	Time Severity and Improvement - Frequency and Average (LYM)	147
4.14b	Time Severity and Improvement - Maximum and Minimum (LYM)	147
4.15	Quality of Solution (LYM)	148
4.16	Node (AM)	149
4.17	Time (AM)	150
4.18a	Node Severity and Improvement - Frequency and Average (AM)	150
4.18b	Node Severity and Improvement - Maximum and Minimum (AM)	150
4.19a	Time Severity and Improvement - Frequency and Average (AM)	151
4.19b	Time Severity and Improvement - Maximum and Minimum (AM)	151
4.20	Quality of Solution (AM)	152
4.21	Node (VR)	153
4.22	Time (VR)	154
4.23a	Node Severity and Improvement - Frequency and Average (VR)	154
4.23b	Node Severity and Improvement - Maximum and Minimum (VR)	155
4.24a	Time Severity and Improvement - Frequency and Average (VR)	155
4.24b	Time Severity and Improvement - Maximum and Minimum (VR)	156
4.25	Quality of Solution (VR)	156



## LIST OF FIGURES

<b>Figure</b>		<b>Page</b>
2.0	Hybrid Algorithm	22
2.1	Holte 1R Algorithm	24
2.2	Dynamic Reduct Algorithm	26
2.3	Set Covering Problem	28
2.4	Matrix Reduction : Row and Column Elimination	29
2.5	Row Reduction Illustration	30
2.6	Row Reduction Illustration : Unit Row	31
2.7	Column Reduction	31
2.8	Random Greedy Algorithm	33
2.9	ITEG Algorithm	36
2.10	GIPP Algorithm	38
2.11	Davis Putnam Proof Procedure	39
2.12	Reduction and Partitioning Illustration	43
2.13	Hypergraph Illustration : Representing CNF	44
2.14	Hypergraph Illustration : Partitioning and Reordering	45
2.15	Local Search Algorithm	48
3.0	Problem Solving Process	51
3.1	Reduct Searching	51
3.2	Set Covering Problem Example	53
3.3	Set Covering Problem	55
3.4	Problem Representation	57



3.5	Integer Programming Model Algorithm	62
3.6	Input and Output of Branch and Bound	65
3.7	Minimum Literal Length Theory Illustration	66
3.8	Clause Subsumption Example	68
3.9	Input Processing Algorithm	69
3.10	Clause Database	69
3.11	Simplified Searching Process in SIP/DRIP	70
3.12	Proposing Solutions	71
3.13	Lower Bound : Case I	72
3.14	Lower Bound Scenario	73
3.15	Lower Bound : Case II	73
3.16	Computing Lower Bound	73
3.17	Lower Bound Conflict	75
3.18	Logical Conflict	76
3.19	Upper Bound Conflict	76
3.20	Non-chronological Backtracking Algorithm	77
3.21	Non-chronological Backtracking Illustration	78
3.22	Updating the Problem Space Due to Conflict	80
3.23	Sample Problem Space	80
3.24	Updating Problem Space Illustration	81
3.25	SIP/DRIP Algorithm	82
3.26	Problem Restructuring and SIP/DRIP	85
3.27	Real Life Scenario	87
3.28	Best Case Scenario	87
3.29	Worst Case Scenario	88



3.30	Problem Restructuring	89
3.31	Simple Incremental Algorithm	90
3.32	Logic of Search	91
3.33	Original Column Ordering	93
3.34	New Column Ordering	95
3.35	Variable Arrangement	101
3.36	Column Arrangement	101
3.37	Dynamic Covering	103
3.38	Static and Dynamic Covering Illustration	104
3.39	Problem Restructuring Algorithm	106
3.40	Reconstructing the Problem Structure	107
3.41	Many Columns with Similar Column Summation	112
3.42	All Columns with Similar Column Summation	113
3.43	High Column Summation with Intersection	113
3.44	Essential Column with Low Column Summation	114
3.45	Effect of High Column Summation with Intersection	115
3.46	Effect of Essential Column with Low Column Summation	116
3.47	Probable Solution	117
4.0	Experimentation Data Set	131
4.1	Erroneous Problem Restructuring	162
4.2	Alternative Essential Variable	162
4.3	Original Scenario before Problem Restructuring	164
4.4	New Scenario after Problem Restructuring	164



## LIST OF ABBREVIATIONS

SIP/DRIP	Standard Integer Programming/Decision Related Integer Programming
AM	American Mushroom
AUS	Australian Credit Card
BB	Branch and Bound
CLV	Cleveland Heart Disease
CNF	Conjunctive Normal Form
LYM	Lymphography
PR	Problem Restructuring
SCP	Set Covering Problem
SAT	Satisfiability
VR	Voting Record



# CHAPTER 1

## INTRODUCTION

### 1.1 Introduction

In this era of technology, the production of data is growing tremendously even as we speak. To note, data is made and processed everywhere. From computers to credit cards, the mass production of digital data is likely inevitable.

In largely produced data, could there be important information hiding within it? If there is, how can we find it and use it? These are the questions that experts are trying to answer (Cabena et al. 1998). Having information means having power. So, there is no need to explain the motivation that lies behind this quest for information.

Data is usually stored and organized in a database. Figuratively, the attempt of discovering information within data can be related to mining gold. Hence, the phrase data mining refers to the effort of finding information in a vast amount of data.

Information is usually represented in the form of relationship between elements of data. That is, it answers the question of how things are related with one another. Knowing the underlying relationship within elements of data is very useful as we can then predict its effects. Consequently, the information can be put to use in real life situation, like in e-commerce applications (Buchner et al. 1998).



The importance of data mining has gained popularity in the business world (Srivastava et al. 2000). Collected data carries many hidden information on opportunities. By using data mining, better speculations on profits are made possible. Not just that, information gathered from data mining can also help in identifying the factors that can lead to business failure. This way, it allows proper actions to be taken before it is too late.

Due to the increasing demand for data mining, many researchers have devoted their time to studying it. Among its many uses, one of the most popular one is classification. It is simply the act of knowing the class and decision of an object given all its attributes. This trait is natural for human beings. For example, when the sky is dark, it might rain, so we decide to carry an umbrella along.

In business process however, the required classification is not as simple. To speculate the successfulness of a loan for instance, there are numerous factors that interact with one another simultaneously. Furthermore there might be thousands of loans to be processed in a short period of time. So, classification must be done intelligently to make all this doable.

Many classification systems have been developed. Most of them are based on statistical analysis. The problem with this method is the vast amount of processing that must be done. It also requires the help of an expert to give appropriate merits to certain values of the factors. To solve this problem, a more novel approach is proposed by using the rough sets theory.



The theory (Pawlak, 1982) proposes that within any knowledge, there exists a minimum amount of information needed to enable classification. If the minimum knowledge were found, processing of data into information would be more efficient. Plus, this approach does not require any additional information like the statistical approach. As a result, it is hypothetically more preferable.

From the eyes of the rough sets theory, this minimum knowledge is known as the reduct. Searching for it is called the reduct searching problem. The advent of rough sets theory is beginning to materialize the hope for a better way of doing classification. As such, it is the focus of this research.

## **1.2 Problem Statement**

The classification problem is a well-known problem in data mining. The problem states that given a set of attributes for an object, the class of the object is to be found. There are numerous ways to solve the problem. The method of interest is the application of the rough sets theory in developing a solution. One of the requirements of applying the rough sets theory is the finding of reducts. The SIP/DRIP algorithm (Bakar, 2002; Bakar et al. 2000, 2001(a), 2001(b)) fulfills this requirement. It finds the reducts in an information system. Employing the branch and bound searching technology, the SIP/DRIP algorithm consumes exponential time and considerable space. It naturally assumes that the value of each attribute is the same. As such, no attention is given to its ordering. This assumption might be the cause of the inherent weakness in the algorithm.