Т	WICKOCLINC: A MECHANISTIC MODEL OF ABOVE, BELOW AND WITHIN-CANOPY MICKOCLIMATE		
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9	HIGHLIGHTS		
10 11 12 13 14 15 16 17 18	<ul> <li>Climate experienced by organisms differs from data used in most ecological studies, which typically use data derived from weather stations.</li> <li>We present an ecologically-relevant model for predicting the climate experienced by organisms.</li> <li>The model uses first-principles physics and can thus be applied in any terrestrial environment.</li> <li>The model was verified and validated with data from four widely geographically distributed forest sites.</li> <li>The model provides reasonably accurate estimates of microclimate.</li> </ul>		
19	ABSTRACT		
20 21	Climate strongly influences ecological patterns and processes at scales ranging from local to global. Studies of ecological responses to climate usually rely on data derived from weather stations, where		

temperature and humidity may differ substantially from that in the microenvironments in which 22 organisms reside. To help remedy this, we present a model that leverages first principles physics to 23 24 predict microclimate above, within, and below the canopy in any terrestrial location on earth, made 25 freely available as an R software package. The model can be run in one of two modes. In the first, heat 26 and vapour exchange within and below canopy are modelled as transient processes, thus accounting for 27 fine temporal-resolution changes. In the second, steady-state conditions are assumed, enabling 28 conditions at hourly intervals or longer to be estimated with greater computational efficiency. We 29 validated both modes of the model with empirical below-canopy thermal measurements from several 30 locations globally, resulting in hourly predictions with mean absolute error of 2.77°C and 2.79°C for 31 the transient and steady-state modes respectively. Alongside the microclimate model, several functions 32 are provided to assist data assimilation, as well as different parameterizations to capture a variety of habitats, allowing flexible application even when little is known about the study location. The model's
modular design in a programming language familiar to ecological researchers provides easy access to
the modelling of site-specific climate forcing, in an attempt to more closely unify the fields of
micrometeorology and ecology.

Key words: temperature, climate, mechanistic model, biophysical ecology, evapotranspiration, R
package.

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## 40 **1. INTRODUCTION**

41 Temperature and water availability influence almost every ecological pattern and process, from the 42 chemical reactions that control photosynthesis (Ingenhousz, 1779; Kumarathunge et al., 2019), to the 43 global distribution of biomes (Gardner et al., 2020; Geiger, 1954; Köppen, 1884). Over the last two centuries thousands of ecological studies have investigated relationships between organisms and 44 45 climate and one of the great challenges in modern ecology is to predict responses to climate change. A 46 common feature of many of these studies is that the climate data used are derived or modelled from 47 weather station data (Bramer et al., 2018; Potter et al., 2013). The microclimatic conditions experienced by organisms can differ vastly from the conditions  $\sim 1.5$  m above the ground, measured inside a weather 48 49 station screen (Maclean et al., 2019; Suggitt et al., 2011). Consequently, meteorological data will often 50 incorrectly predict physical exposure to critical climate thresholds and the timing of climate-sensitive biological events (Baker, 1980; Perez and Feeley 2020). Microclimatic conditions in low-lying 51 52 vegetation are also far more spatially and temporally variable than inside weather stations (Bennie et 53 al., 2008; Lenoir et al., 2017), implying that the climatic niches of species, fundamental to predicting 54 their distributions changes, cannot be accurately established by the methods normally used. Neglecting 55 this variability, which can provide microrefugia or allow for thermoregulation, can also lead to 56 overestimation of extinction rates (Suggitt et al., 2018). There is thus a clear need to develop methods 57 that estimate microclimatic conditions of the environments in which organisms reside.

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59 In fields outside ecology, the modelling of microclimates has a long history. Many of the methods used 60 still owe their origins to the pioneering work by Richardson (1922), who demonstrated the basic laws of turbulent mixing in the surface layer of the atmosphere. In the 1950s, Monin & Obukhov (1954), 61 62 extended this platform and, building on work by Prandtl (1925), provided a generalised, universal 63 method for characterising wind speed and temperature profiles above the surface of a vegetation canopy 64 under non-neutral conditions. The methods developed by these earlier pioneers in microclimatology still form the basis of most models that are in use today (see e.g. Ali et al., 2018; Bruse, 2014). 65 66 Ecologists, however, have been surprisingly slow to adopt these more mechanistic approaches, and 67 there is a still a tendency to derive microclimatic surfaces using statistical approaches (Fick and

Hijmans, 2017; Greiser et al., 2018; Meineri and Hylander, 2017). While potentially very good at
capturing spatial variation in microclimate, the potential for models fitted using statistical inference to
forecast novel conditions is somewhat questionable (Buckley et al., 2018; Evans, 2012; Nabi, 1985).

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72 Nevertheless, the last few years have witnessed renewed ecological interest in microclimatology 73 (Bramer et al., 2018; Lembrechts et al., 2019; Potter et al., 2013), in part driven by the availability of 74 models written using programming languages with which ecologists are familiar (Lembrechts and 75 Lenoir, 2019). One of the most widely used microclimate models in ecology, that of Porter et al. (1973), 76 has been incorporated into the R package 'NicheMapR' (Kearney and Porter, 2017). Although flexible 77 and widely tested, it requires pre-adjustment of input forcing to account for terrain and canopy shading 78 effects as well as mesoclimatic processes such elevation and cold air drainage. It is also designed to be 79 run for single point locations. Building on the model of Bennie et al. (2008), Maclean et al. (2017) 80 developed methods for modelling mesoclimatic effects, released as an R-package 'microclima', which 81 is able to produce gridded estimates of microclimate (Maclean et al., 2019). Both models have 82 subsequently been combined into a single framework (Kearney et al., 2020) and have also been developed for application in forecasting future climate (Maclean, 2020). Importantly, however, they 83 84 were designed primarily for modelling above-canopy microclimate, and have principally been applied 85 to determine microclimatic conditions over short vegetation. The environmental physics underpinning 86 the models are associated with exchange above a vegetated surface and do not explicitly consider the microclimate within canopies. However, tropical forests alone host at least two-thirds of the worlds 87 88 terrestrial biodiversity (Gardner et al., 2009), and with the exception of soil biota, the majority of 89 remaining species spend at least some of their time among vegetated canopies (Lowman et al., 1996; 90 Nakamura et al., 2017). In addition, thermal tolerances of plants are more sensitive to leaf temperatures 91 than ambient air temperatures (Michaletz et al., 2016; Perez and Feeley 2020) and critical thermal 92 thresholds can vary even within the canopy of a single tree (Curtis et al., 2019). Means of determining 93 the microclimatic conditions across and below the canopy are therefore much needed.

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95 In contrast to above the canopy, however, the physics of microclimate below-canopy is not fully 96 resolved. Above-canopy, the transport of heat and vapour can accurately be described from estimates 97 of atmospheric turbulence using K-theory (i.e. using a flux gradient approach). Emerging understanding 98 (see e.g. Baneree *et al.*, 2017), suggests that *K*-theory often fails to describe turbulent transport in plant 99 canopies. Many of its assumptions are violated because within-canopy air turbulence is an intermittent 100 process: infrequent wind gusts sweeping downward through the trunk space from the air above are 101 responsible for much of the exchange of heat, vapour and momentum between the canopy and the 102 atmosphere. The 'effective diffusivity' of heat and vapour is more often a function of the vertical 103 distribution of heat and water vapour sources or sinks within the canopy than of the turbulence level. 104 Simulation of within-canopy turbulence is thus improved upon by using Lagrangian (e.g. Raupach,

105 1989) or Eulerian (e.g. Katul and Albertson, 1999) advection-diffusion models. The utility of such 106 models for ecological applications, however, is severely limited by their need to specify length and time 107 scales for the wind field. K-theory models are least valid when they are used to estimate within-canopy 108 water vapour and heat exchange, but it is by virtue of this fact that it is still possible to simulate realistic 109 in-canopy microclimates using K-theory. This apparent inconsistency arises for two reasons. First, 110 although the source-sink strengths and hence the distribution of heat and momentum fluxes are 111 extremely sensitive to the shape of measured profiles (Finnigan, 2000; Raupach and Thom, 1981), the converse relationship means that shape of the temperature and wind profiles are insensitive to flux 112 uncertainties and can be generated by integration of an appropriate distribution of sources. Second, both 113 temperature and humidity are related strongly to latent heat fluxes, which in turn are more strongly 114 controlled by stomatal conductance than by turbulence within the canopy (Jarvis and McNaughton, 115 116 1986). In consequence, a realistic representation of the distribution of foliage density, net radiation and 117 stomatal conductance in various layers of a canopy, coupled with a relatively uncertain model of 118 atmospheric transfer within the canopy, will tend to adequately reproduce temperature, vapour and wind 119 profiles (Monteith and Unsworth, 2013).

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121 Thus, despite evolving views of the processes driving turbulence within plant canopies, different models 122 developed over several decades (e.g. Bailey et al., 2016; Baldocchi and Meyers, 1998; Goudriaan, 1977; 123 McNaughton and Van den Hurk, 1995; Waggoner et al., 1969) have all used a similar approach. First, 124 the vertical distribution of radiant energy within the canopy is quantified from foliage density and 125 radiation transmission. Second, the net radiation absorbed by each leaf is divided up into sensible and 126 latent heat, making appropriate assumptions about stomatal and leaf boundary layer conductance. Last, 127 the transfer of air within different layers of the canopy is modelled using a variety of different 128 approaches (e.g. K-theory, Langrangian or Eularian models) and have all been shown to perform in a 129 similar fashion and relatively well (Bache, 1986; Dolman and Wallace, 1991). Nevertheless, a practical, 'off-the-shelf' model that can be used by ecologists to estimate microclimate conditions is still lacking. 130

Here we develop an integrated above/below-canopy and soil microclimate model, in the R programming 131 132 environment, for application in ecological research. The model, based on first principles physics, is 133 designed to be flexible, enabling application in almost any terrestrial environment though its intended 134 focus is primarily to estimate within-canopy temperatures. Through its modular design, and careful 135 selection of vegetation parameters typical of a given vegetation derived from literature, it can be applied with little knowledge of the particular study location (as a minimum, just a user-specified broad habitat 136 137 type). However, the option to alter parameters (for example, stomatal conductance, or leaf area at 138 varying heights in the canopy) is included to enable more complex, bespoke parametrisations where 139 possible. The model can also be run using freely available climate data using tools that we have 140 previously developed for downloading (Duffy, 2020; Kearney et al., 2020).

# 142 **2.** MODEL DESCRIPTION

#### 143 *2.1 Overall model structure*

The model is designed to be run at single-point locations, using a time-series of climate forcing data 144 145 (temperature, humidity, wind speed, atmospheric pressure and incoming solar radiation). It can be run 146 in two modes at time-increments ranging from seconds to days. For application where very finetemporal resolution data might be needed, heat and vapour exchange are modelled as transient 147 processes, and heat storage by the canopy, and the exchange of heat between different layers of the 148 149 canopy, are considered explicitly, with the capacity to simulate wind gusts thus bi-passing limitations associated with K-theory. Alternatively, for application at time increments of an hour or longer, below-150 151 canopy heat and vapour exchange are assumed to attain steady state, and the temperatures and soil 152 moisture are determined using energy balance equations that sum to zero. In this latter mode, the model 153 has been integrated with `NicheMapR` package (Kearney and Porter, 2017) and uses the rapid 154 processing capacity of Fortran routines therein to compute soil moisture and temperature. It also enables 155 explicit modelling of snow.

In the transient mode, the canopy and soil profiles are divided into a user-specified number of layers 156 (with a default of 20). For each layer, the user specifies canopy properties (e.g. leaf area, leaf angle 157 distribution, leaf reflectance and maximum stomatal conductance) and soil (e.g. bulk density, mineral, 158 159 organic, quartz and clay content, Campbell 1985), or alternatively these are estimated for each layer by 160 specifying habitat or soil type or providing single values for the entire canopy and soil profile. In the steady-state mode, the user specifies a height below ground or above/within the canopy, and the leaf 161 area above this point and for the canopy in total must be specified (although the option to estimate these 162 163 by specifying a habitat type is also included). In both modes, above-canopy temperature, humidity and 164 wind profiles are calculated using K-theory with estimates of bulk aerodynamic resistance derived from 165 canopy properties. Within the canopy, radiation transmission and wind profiles are also estimated from canopy properties. These, in turn, are used to estimate turbulent transfer within the canopy and boundary 166 167 layer and stomatal conductance for each canopy layer. Heat balance equations for each canopy layer 168 are then linearized, enabling simultaneous calculation of leaf and air temperatures. Time-dependent differential equations for each canopy and soil node are then specified and storage and simultaneous 169 170 exchanges of heat and vapour between each layer then computed. In the transient mode, storage is 171 considered both for soil and the canopy, but in the steady-state mode, only storage in the soil is 172 considered. The model returns a time-series of temperature, humidity and wind speeds at user-specified heights or depths. 173

- 174 Below we provide a general overview of the equations used in the model. All symbols and their units
- are described in Table 1, and further details of these equations and their derivation are provided in
- 176 Appendix A.

- Term Definition Units Wind attenuation coefficient \_ а b Exponent for water release from soil -Drag coefficient \_  $C_d$ Volumetric specific heat capacity of vegetation  $J \cdot m^{-3} \cdot K^{-1}$  $C_D$  $J \cdot m^{-3} \cdot K^{-1}$ Volumetric specific heat capacity of soil  $C_{\underline{H}}$ Specific heat of air at constant pressure  $J \cdot mol^{-1} \cdot K^{-1}$  $c_p$ Zero plane displacement d m Thermal diffusivity  $m^2 \cdot s^{-1}$  $D_H$ Vapour pressure Pa е Vapour pressure of leaf Pa  $e_{L}$ Saturated vapour pressure Pa  $e_s$  $mol \cdot m^{-2} \cdot s^{-1}$ Ε Evaporation rate of water Molar conductance  $mol \cdot m^{-2} \cdot s^{-1}$ g Stomatal conductance  $mol \cdot m^{-2} \cdot s^{-1}$  $g_c$  $mol \cdot m^{-2} \cdot s^{-1}$ Maximum stomatal conductance  $g_{cmx}$  $mol \cdot m^{-2} \cdot s^{-1}$ Leaf boundary layer conductance for heat  $g_{Ha}$ Grashof number \_  $G_r$  $mol \cdot m^{-2} \cdot s^{-1}$ Leaf conductance for vapour  $g_{v}$ Conductance for heat by turbulent transfer  $mol \cdot m^{-2} \cdot s^{-1}$  $g_t$ Canopy height h m Η Sensible heat flux density  $W \cdot m^{-2}$ Relative turbulence intensity  $i_w$ \_ Mixing length m  $l_m$ Transmission fraction of longwave radiation through  $l_{tr}$ \_ the canopy  $W \cdot m^{-1} \cdot K^{-1}$ Thermal conductivity k Extinction coefficient for canopy radiation K \_ transmission Ratio of radiation incident on inclined leaves in each \_  $m_i$ canopy layer relative to the horizontal Thomas algorithm forward-backward weighting factor \_ п Atmospheric pressure Pa  $p_a$ Fraction of sunlit leaves \_  $p_s$ Plant area index  $P_{AI}$ \_ Prandtl number \_  $P_r$ Fractional foliage volume  $P_{v}$ \_ Photosynthetically active radiation absorbed by a leaf  $mol \cdot m^{-2} s^{-1}$  $Q_a$ Value of  $Q_a$  when  $g_v$  is at 50% of maximum  $mol \cdot m^{-2} s^{-1}$ *Q*<sub>*a*50</sub>  $W \cdot m^{-2}$ Total radiation absorbed by canopy layer  $R_{abs}$  $W \cdot m^{-2}$ Total radiation emitted by canopy layer R<sub>em</sub> Flux density of beam radiation on a horizontal surface  $W \cdot m^{-2}$  $R_h^0$ above the canopy
- **Table 1.** List of symbols used in equations.

Term	Definition	Units
$R_{b}^{P_{AI}}$	Flux density of beam radiation below plant area $P_{AI}$	W·m <sup>-2</sup>
$R_d^0$	Flux density of diffuse radiation above the canopy	$W \cdot m^{-2}$
$R_d^{P_{AI}}$	Flux density of diffuse radiation below plant area $P_{AI}$	W·m <sup>-2</sup>
R <sub>e</sub>	Reynolds number	-
$r_1$	Leaf reflectivity (longwave radiation)	-
Rlabs	Longwave radiation absorbed by canopy layer	$W \cdot m^{-2}$
R <sub>l</sub> <sup>can</sup>	Longwave radiation emitted by canopy to each layer	$W \cdot m^{-2}$
$R_l^{em}$	Emitted longwave radiation	$W \cdot m^{-2}$
$R_{l}^{sky}$	Longwave radiation emitted by sky	$W \cdot m^{-2}$
r <sub>s</sub>	Leaf reflectivity (shortwave radiation)	-
$R_s^{abs}$	Shortwave radiation absorbed by canopy layer	$W \cdot m^{-2}$
$R_s^{PAI}$	Flux density of shortwave radiation below plant area	$W \cdot m^{-2}$
t	Time step	s
$T_{d+z_H}$	Temperature at heat exchange surface of canopy	K
$T_i$	Temperature at time <i>j</i>	K
$T_{\tau}$	Temperature at height z	К
$T_I$	Leaf temperature	К
$u^*$	Friction velocity of wind	$\mathbf{m} \cdot \mathbf{s}^{-1}$
$u_h$	Wind speed at top of canopy	$\mathbf{m} \cdot \mathbf{s}^{-1}$
$u_{\pi}$	Wind speed at height z	$\mathbf{m} \cdot \mathbf{s}^{-1}$
$V_d$	Volumetric density of vegetation	kg·m <sup>-3</sup>
W	Mean leaf width	m
x	Ratio of vertical to horizontal projections of a	
	representative volume of foliage	
$x_d$	Characteristic dimension of leaf	m
Ζ	Height	m
Ζ	Solar zenith angle	0
$Z_H$	Roughness length for heat	m
$Z_{LA}$	Mean leaf-air distance	m
$Z_M$	Roughness length for momentum	m
λ	Latent heat of vaporization of water	J⋅mol <sup>-1</sup>
θ	Volumetric soil moisture fraction	-
$\theta_s$	Saturated volumetric soil moisture fraction	-
$\hat{ ho}$	Molar density of air	mol·m <sup>-3</sup>
σ	Stefan-Boltzman constant	$W \cdot m^{-2} \cdot K^{-4}$
$\psi_e$	Air entry water potential	J·kg <sup>-1</sup>
$\psi_{H}$	Diabatic correction for heat	-
$\psi_M$	Diabatic correction for momentum	-
Ω	Canopy clumping factor	-

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# 2.2 Solar radiation

181 Radiation is the key source of heat within a canopy and has a major bearing on rates of 182 evapotranspiration. The net radiation flux is determined by the balance of incoming shortwave radiation 183 and emitted longwave radiation, a portion of the latter of which is also absorbed by leaves. Direct 184 radiation is partitioned into direct (beam) and diffuse components, both of which are attenuated by the 185 canopy. Following Campbell (1986) and Campbell & Norman (2012), the flux density of beam radiation 186  $R_b^{P_{AI}}$  under plant area  $P_{AI}$  is described as follows:

$$R_b^{P_{AI}} = R_b^0 \left\{ (1 - \Omega) \exp\left(-\sqrt{1 - r_s} K P_{AI}\left(\frac{1}{1 - \Omega}\right)\right) + \Omega \right\}$$
(1a)

187 where  $R_b^0$  is the flux density of beam radiation on a horizontal surface above the canopy,  $r_s$  is the 188 reflectance of leaves to shortwave radiation,  $\Omega$  (scaled between 0 and 1) describes how clumped the 189 canopy is such that some radiation passes directly though canopy gaps. *K*, the extinction coefficient of 190 light, represents the area of shadow cast on a horizontal surface by the canopy divided by the plant area 191 of the canopy, and depends on the ratio of vertical to horizontal projections of a representative volume 192 of foliage, *x*:

193 
$$K = \frac{\sqrt{x^2 + \tan^2 Z}}{1.774(x + 1.182)^{-0.733}}$$

where Z is the solar zenith angle. For diffuse radiation, the leaf angle distribution is unimportant, and(1a) becomes

$$R_d^{P_{AI}} = R_d^0 \left\{ (1 - \Omega) \exp\left(-\sqrt{1 - r_s} P_{AI}\left(\frac{1}{1 - \Omega}\right)\right) + \Omega \right\}$$
(1b)

196 where  $R_d^0$  is the flux density of diffuse radiation above the canopy,  $R_d^{P_{AI}}$  is the flux density of below 197 plant area  $P_{AI}$ . The temperature of leaves is dependent on the amount of radiation absorbed. Assuming 198 the canopy to be made up of *n* layers, each with a plant area,  $P_{AI}[i]$ , such that  $P_{AI}$  represents the plant 199 area above any given layer, then the flux density of solar radiation absorbed ( $R_s^{abs}$ ) by each layer is

$$R_s^{abs} = P_{AI}[i](1 - r_s)(p_s m_i R_s^{PAI} + (1 - p_s) R_s^{PAI})$$
(2)

200

201 where  $R_s^{PAI}$  is the flux density of solar radiation below plant area  $P_{AI}$  given by  $R_b^{P_{AI}} + R_d^{P_{AI}}$  and  $p_s$  is the 202 fraction of sunlit leaves given by

203 
$$p_{s} = (1 - \Omega) \left( \frac{1 - \exp\left(-KP_{AI}\frac{1}{1 - \Omega}\right)}{P_{AI}K} \right) + \Omega$$

and  $m_i$  is the ratio of radiation incident on inclined leaves in each canopy layer relative to the horizontal, which from Campbell (1990) is approximated as follows:

206

207  $m_i = \exp\{1.206x^{0.407} - 4.89 - (0.412x^{0.317} + 1.324)\log(90 - Z)\}^{-1}$ 

208 2.3 Longwave radiation

From the Stefan–Boltzman law, the flux density of longwave radiation emitted by vegetation,  $R_l^{em}$ , with plant area  $P_{AI}[i]$  is

$$R_l^{em} = P_{AI}[i](1-r_l)\sigma T_L^4 \tag{2a}$$

where  $r_l$  is reflectance to longwave radiation,  $\sigma$  is the Stefan-Boltzman constant and  $T_L$  is the temperature of the leaf. A portion of emitted radiation is then reabsorbed. The absorbed longwave radiation,  $R_l^{abs}$ , depends on sky emissivity and upwards and downwards transmission through the canopy

$$R_{l}^{abs} = P_{AI}[i](1 - r_{l})(R_{l}^{sky} + R_{l}^{can})$$
(2b)

215 where  $R_l^{sky}$  is longwave radiation absorbed and re-emitted downward from the sky, given by 216  $R_l^{sky} = \varepsilon_s(l_{tr})^2 R_l^{em}$  and  $R_l^{can}$  is radiation absorbed and re-emitted downward from the canopy, given by 217  $R_l^{can} = (1 - l_{tr}) R_l^{em}$ , where  $\varepsilon_s$  is sky emissivity and  $l_{tr}$  is transmission of longwave radiation through the 218 canopy given by  $l_{tr} = (1 - \Omega) \exp\left(-\sqrt{1 - r_l} P_{Al}\left(\frac{1}{1-\Omega}\right)\right) + \Omega$ .

## 219 2.4 Wind, conductance and temperature above-canopy

Wind profiles above the canopy dictate heat and vapour exchange between the canopy and air above it,
and therefore ultimately determine temperature and vapour profiles. It can generally be assumed that
radiative fluxes have a negligible effect on air temperature directly. However, the canopy itself acts as
a heat exchange surface, enabling exchange of heat with surrounding air via a process of eddy diffusion.
Following Campbell and Norman (2012) the wind profile is describe as follows:

$$u_{z} = \frac{u^{*}}{0.4} \ln \frac{z - d}{z_{M}} + \psi_{M}$$
(3)

where  $u_z$  is wind speed at height *z*, *d* is the height above ground within the canopy where the wind profile extrapolates to zero,  $z_m$  the roughness length for momentum,  $\psi_M$  is a diabatic correction for momentum (see Appendix A) and  $u^*$  is the friction velocity, which gives the wind speed at height  $d + z_m$ .

229 The equation that describes the temperature profile is given as follows:

$$T_z = T_{d+z_H} - \frac{H}{0.4\hat{\rho}c_p u^*} \left( \ln \frac{z-d}{z_H} + \psi_H \right)$$
<sup>(4)</sup>

where  $T_z$  is temperature at height z,  $T_{d+z_H}$  is the temperature at the height of the exchange surface  $d + z_H$ ,  $z_H$  is the roughness length for heat transfer,  $\psi_H$  the diabatic correction for heat and  $\hat{\rho}$  and  $c_p$  the specific heat and molar density of air respectively. The sensible heat flux H is, in effect, the net heat supplied to the canopy surface as determined from the balance of radiative, latent and ground heat fluxes. Coefficients d,  $z_M$  and  $z_H$  can be derived through empirical measurement of temperature and wind profiles, but the model includes more general expressions of these derived by Shaw & Pereira (1982)

- as functions  $P_{AI}$  and canopy height (*h*). The diabatic correction factors account for the fact that strong surface heating causes overturning of the air layers, with resultant increases in turbulence and mixing and vis-versa. Further details of how these are calculated are provided in Appendix A.
- Heat conductance,  $g_t$  (mol·m<sup>-2</sup>·s<sup>-1</sup>) between any two heights  $z_1$  and  $z_0$  above-canopy, expressed in molar form is then given by

$$g_t = \frac{0.4\hat{\rho}u^*}{\ln\left(\frac{z_1 - d}{z_0 - d}\right) + \psi_H}$$
(5)

# 2.5 Wind, and heat conductance below-canopy

From Inoue (1963), Cionco (1972) and Goudriaan (1977), a wind profile within the canopy can bederived as follows:

$$u_z = u_h \exp\left(a\left(\frac{z}{h} - 1\right)\right) \tag{6}$$

where  $u_z$  is wind speed at height *z* within the canopy,  $u_h$  is wind speed at the top of the canopy at height *h*, and *a* is a wind attenuation coefficient given by  $a = \frac{c_d P_{AI} h}{2l_m i_w}$ , where  $c_d$  is a drag coefficient that varies with leaf inclination and shape,  $i_w$  is a coefficient describing relative turbulence intensity and  $l_m$  is the mean mixing length, equivalent to the free space between the leaves and stems. From Goudriaan (1977)

248  $l_m = \sqrt{\frac{4wh}{\pi P_{AI}}}$ , for vegetation that is long and narrow, or  $l_m = \sqrt[3]{\frac{6w^2h}{\pi P_{AI}}}$  for leaves shaped more like squares, 249 where *w* is the mean width of leaves and stems. Within-canopy heat conductance between any two 250 heights  $z_1$  and  $z_0$  below-canopy is then given by

$$g_t = \frac{u_h l_m i_w a}{\left(\exp\left(\frac{-az_0}{h-1}\right) - \exp\left(\frac{-az_1}{h-1}\right)\right)\psi_H}$$
(7)

where  $\psi_H$  is a within-canopy diabatic correction factor for heat (see Appendix A). It is also necessary to calculate conductance,  $g_{Ha}$ , between the leaf and air. When wind speeds are moderate to high, conduction is predominantly under laminar forced convection and from e.g. Campbell & Norman (2012) is given by

$$g_{Ha} = \frac{0.664\hat{\rho}D_H R_e^{0.5} P_r^{0.5}}{x_d}$$
(8a)

where  $D_H$  is thermal diffusivity,  $x_d$  is the characteristic dimension of the leaf ( $x_d \approx 0.7$ w),  $R_e$  is the Reynolds number, and  $P_r$  is the Prandtl number. When wind speeds are low, an expression that is adequate for leaves is given by (Campbell and Norman, 2012)

$$g_{Ha} = \frac{0.54\hat{\rho}D_H (G_r P_r)^{0.25}}{x_d}$$
(8b)

where  $G_r$  is the Grashof number. When the leaf is cooler than the air, the heat transfer is only half as efficient so the constant 0.54 becomes 0.26. Equations (8a & b) describe conductance one would measure under minimal turbulence. Based on measurements by Mitchell (1976), and following Campbell & Norman (2012), turbulence is accounted for by using an enhancement factor of 1.4. Formulae for computing the Reynolds, Prandtl and Grashof numbers are provided in Appendix A.

## 263 2.6 Vapour and latent heat fluxes

Vapour gradients control both evapotranspiration rates and latent heat fluxes and thus have a significant
bearing on temperature and humidity. From Fick's law, the transport of vapour is given by

$$\lambda E = g \frac{\partial e}{p_a} \tag{10}$$

where  $\lambda E$  is latent heat, comprising the latent heat of vapourization of water ( $\lambda$ ) and the evaporation rate (*E*),  $\partial e$  is the vapour pressure gradient and  $p_a$  is atmospheric pressure. For vapour exchange above the canopy or between layers of air within the canopy, the conductance is the same as that for heat. The conductance for vapour loss from leaves ( $g_v$ ), however, also depends on stomatal conductance ( $g_c$ )

270 
$$g_v = 1/(1/g_{Ha} + 1/g_c)$$

Under ample root water supply, non-extreme temperatures and low humidity deficit,  $g_c$  varies through the canopy only in response to variation in photosynthetically active radiation. The stomatal response to the photosynthetically active radiation by an individual leaf ( $Q_l$ ), can be assumed (Kelliher et al., 1995) to be given by a hyperbolic function:

$$g_c = \frac{Q_a}{Q_a + Q_{a50}} g_{cmx} \tag{11}$$

where  $g_{cmx}$  is maximum stomatal conductance and  $Q_{a50}$  is the value of  $Q_a$  when  $g_v = g_{vmx}/2$ . Körner (1995) gives values of  $g_{cmx}$  for most major vegetation types in the world.

It can generally be assumed that the water potential of leaves is such that vapour concentration at the evaporating surface is equal to the saturated vapour concentration at surface temperature, such that  $e_s$ can be determined from leaf temperature ( $T_L$ ). For the soil surface, an equivalent to vapour pressure can, from Campbell & Norman (2012), be calculated as  $e_a = e_s \exp\left((\theta/\theta_s)^{-b}(0.018\psi_e/8.31T_0)\right)$ , where  $e_s$  is calculated using soil surface temperature ( $T_0$ ),  $\theta$  is soil volumetric water content,  $\theta_s$  the saturated water content,  $\psi_e$  the air entry water potential and *b* the exponent for water release. The parameters  $\theta_s$ ,  $\psi_e$  and *b* depend on soil type, but are otherwise constant.

284 2.7

#### 2.7 Below-canopy temperature and humidity

285 Under steady-state, the heat balance equation for the leaves in each canopy layer is as follows:

$$\bar{R}_{abs} - \bar{R}_{em} - \bar{H} - \bar{\lambda}\bar{E} = \bar{R}_{abs} - \varepsilon_s \sigma \bar{T}_L^4 - c_p \bar{g}_{Ha} (\bar{T}_L - \bar{T}_A) - \lambda \bar{g}_v \frac{e_L - \bar{e}_A}{\bar{p}_a} = 0$$
(12)

286 Where  $\bar{R}_{abs}$  is absorbed radiation,  $\bar{R}_{em}$  emitted radiation,  $\bar{H}$  the sensible heat flux,  $\bar{\lambda}E$  the latent heat 287 flux,  $\varepsilon_s$  the emissivity of the leaf,  $\sigma$  the Stefan-Boltzmann constant,  $\bar{T}_L$  the absolute temperature of the 288 leaf,  $\bar{T}_A$  the absolute temperature of the air surrounding the leaf,  $\lambda$  the latent heat of vaporisation of 289 water,  $e_L$  the effective vapour pressure of the leaf,  $\bar{e}_a$  the vapour pressure of air and  $\bar{p}_a$  atmospheric 290 pressure. Throughout, overbars denote a mean over the duration of the time-step.

291 A challenge in solving this equation is the dependency of latent heat and emitted radiation on leaf 292 temperature. The emitted radiation term can be solved readily by linearisation using binomial expansion 293 (see Appendix A). The latent heat term is usually solved algebraically through linearization using the 294 Penman-Monteith equation (Monteith, 1965; Penman, 1948), by assuming that air temperature surrounding a leaf is closely coupled to the air above and uninfluenced by leaf temperature. We 295 explicitly consider the effects of leaf temperature on air temperature, and also the degree of coupling 296 297 with the soil and air above canopy. Defining a term,  $\Delta T_L$ , such that  $T_L = T_A - \Delta T_L$  and a linear 298 expression for air temperature such that  $T_A = a_A + b_A \Delta T_L$ , it can be shown (see Appendix A) that

$$\Delta T_L = \frac{R_{abs} - a_R - a_L}{1 + b_R + b_L + b_L}$$

Where equations for each a and b term are provided in Table 2. Under transient conditions the heat 300 storage of each canopy layer is sufficient to prevent equilibrium. If superscript *j* denotes present time, 301 and j+1 is one time-step in the future it can reasonably be assumed that e.g.  $\overline{T} = 0.5(T^j + T^{j+1})$ . 302 Defining  $m_L$  as the flux density required to heat a m<sup>3</sup> of vegetation by one degree K, given by 303 304  $z_{LA}C_dV_d/tP_{AI}$ , where  $z_{LA}$  is the mean leaf-air distance (equivalent to half the average distance between leaves),  $C_d$  the specific heat capacity of vegetation with volumetric density  $V_d$ , t the duration of each 305 model time step and  $P_{AI}$  the total one-sided plant area per m<sup>2</sup> ground area, an equivalent expression for 306 307 the transient leaf temperature change is given as follows:

$$T_L^{j+1} = T_L^j + \frac{\bar{R}_{abs} - a_R - a_H - a_L}{m_L(1 + b_R + b_H + b_L)}$$
(13)

Expressions for each *a* and *b* under transient conditions are also given in Table 2 and derivation of theequation is in Appendix A.

310 2.8 Soil temperature

In the soil, heat storage is almost always significant, and Fourier's Law is combined with the continuity equation to obtain a time dependent differential equation that describes soil temperature as a function of depth and time:  $C_h \partial T / \partial t = \partial (k \partial T / \partial z) \partial z$ , where  $C_h$  is volumetric specific heat and k thermal conductivity in W·m<sup>-1·</sup>K<sup>-1</sup> ( $k = c_p \partial zg$ ), determined from soil properties and volumetric water content 315 (Appendix A). A closed-form solution to this time-dependent differential equation that extends beyond 316 simple sets of soil properties and boundary conditions is not possible. Following Campbell (1985), a 317 numerical solution is achieved by dividing the soil into layers. Each layer is assigned a node, *i*, at depth, 318  $z_i$ , and with heat storage,  $Ch_i$ , and nodes are numbered sequentially downward such that node *i*+1 319 represents the node for the soil layer immediately below. Conductivity,  $k_i$ , represents conductivity 320 between nodes *i* and *i*+1. The energy balance equation for node *i* is then given by

$$\bar{\kappa}_{i}(\bar{T}_{i+1} - \bar{T}_{i}) - \bar{\kappa}_{i-1}(\bar{T}_{i} - \bar{T}_{i-1}) = \frac{C_{h_{i}}(T_{i}^{j+1} - T_{i}^{j})(z_{i+1} - z_{i-1})}{2\Delta t}$$
(14)

321 where  $\Delta t$  is the time increment, conductance,  $\kappa_i = k_i/(z_{i+1} - z_i)$ , superscript *j* indicates the time at 322 which temperature is determined and overbars indicate means during the time increment.

### 323 2.9 Within-canopy heat and vapour exchange

Under transient conditions, the approach described for soil can readily be extended to account for the exchange of heat between different layers of the canopy, with two notable exceptions. First, heat storage in the air is substantially lower than in the soil and prior to computing heat exchange between layers, air layers are merged when the total flux over the time increment exceeds heat capacity. Second, the latent and sensible heat fluxes from the leaf to the air are also considered

$$\bar{g}_{Ha}c_p(\bar{T}_L - \bar{T}_i) + \frac{\lambda\bar{g}_v}{\bar{p}_a}(\bar{e}_L - \bar{e}_a) + \bar{g}_i c_p(\bar{T}_{i+1} - \bar{T}_i) - \bar{g}_{i-1}c_p(\bar{T}_i - \bar{T}_{i-1}) = \frac{c_p\hat{\rho}(1 - P_v)(T_i^{j+1} - T_i^j)(z_{i+1} - z_{i-1})}{2\Delta t}$$
(15)

where  $g_i$  is the molar conductance between canopy layers (7) and  $P_v$  is the fractional foliage volume given by  $V_t[i]P_{AI}[i]/z_t[i]$ , where  $V_t[i]$  is the mean thickness of foliage and  $z_t[i]$  the thickness of each canopy layer *i*.

The system of equations for each canopy layer can be combined with those for the soil layers to form a 332 single set of equations. Assuming  $\overline{T} = nT^{j+1} + (1-n)T^{j}$ , where *n* is a weighting factor in the range 333 0 to 1. Equations (14) and (15) can be re-arranged and solved for  $T^{j+1}$  by Gaussian elimination using 334 335 the Thomas algorithm (Thomas, 1949), when boundary conditions are used to reduce the number of 336 unknowns by two. The upper boundary condition is the conductance  $\bar{g}_0$  between the top of the canopy and the air at reference height determined from (5). A boundary condition at the bottom of the soil 337 338 profile is set by assuming that temperatures are stable and, in the absence of a user-provided value, 339 equivalent to mean air temperature over the duration the model is run.

- 340 Vapour exchange can be handled in a similar way, expect that here, water exchange in the soil is user-
- specified, or in the steady-state mode, calculated using NicheMapR (see running the model) and the
- 342 exchange between air layers is given by

$$\frac{\bar{g}_{v}}{\bar{p}_{a}}(\bar{e}_{L}-\bar{e}_{a}) + \frac{\bar{g}_{i}}{\bar{p}_{a}}(\bar{e}_{i+1}-\bar{e}_{i}) - \bar{g}_{i-1}c_{p}(\bar{e}_{i}-\bar{e}_{i-1}) = \frac{\hat{\rho}(1-P_{v})(e_{i}^{j+1}-e_{i}^{j})(z_{i+1}-z_{i-1})}{2\Delta t}$$
(16)

Again, the system of equations is solved by Gaussian elimination using the Thomas algorithm (seeAppendix A).

345

**346 3. R**UNNING THE MODEL

The model is split into two R packages. The package `microctools` contains a series of `worker` 347 348 functions needed to run the model, such as those needed to compute conductance and radiation 349 transmission. It also contains useful functions not directly needed to run the model, such as for 350 estimating the diffuse fraction of total incoming solar radiation and converting between different humidity measures. The `microclimc` package contains the higher-level functions needed to compute 351 individual elements of microclimate (for example leaf temperature), to run the model in its entirety over 352 353 a single time increment (returning the full suite of microclimate variables for all layers in the canopy), 354 or to run the model for a time-series to return temperature, humidity and wind speed at user-specified heights above or below ground. Package `microctools` is automatically installed when installing 355 `microclimc` and is available on Github: https://github.com/ilyamaclean/microclimc. 356

There are two model run modes. Function `runmodel` runs the full model in transient mode, but in this mode, there are checks to establish whether conditions are steady state or transient, and the model automatically performs calculations accordingly. Function `runmodelS` runs the model in steady-state mode for cases in which predictions for a single height is desired. However, it is encouraged to conduct steady state modelling using the wrapper function `runwithNMR`, which invokes the `NicheMapR` package to calculate soil moisture from rainfall and evapotranspiration. In alternative modes, soil moisture must be specified by the user.

Two sets of parameters are needed to drive the model: (1) vegetation parameters, describing canopy 364 properties for multiple layers within the canopy and (2) soil parameters, enabling heat capacity and 365 conductances within the soil to be calculated. However, a key goal in the development of this model is 366 367 to enable estimates of microclimate with varying amounts of information available. The `microctools` 368 package therefore includes functions that will reproduce reasonable approximations of soil properties 369 simply by specifying a soil type and seasonal variation in and the vertical distribution of foliage and 370 leaf angles from habitat types. Alternatively, where multi-layer information on foliage is available, such 371 as might be derived using a plant canopy analyser or from a series of digital hemispherical photographs taken at different heights in the canopy (see e.g. Thimonier et al., 2010), these data can be used instead. 372

Table 2. Full equations for terms in equation 13 used to simultaneously estimate leaf and air temperatures. Terms are defined in Table 1. Overbars denote means
 during the time increment. Definitions for both steady-state and transient heat exchange are provided. Derivation of the equations is provided in Appendix A.

Steady-state	Transient
$a_E = \frac{\bar{g}_{tR}\bar{e}_R + \bar{g}_{t0}\bar{e}_0 + \bar{g}_{\nu}e_s[\bar{T}_R]}{\bar{a}_s + \bar{a}_s + \bar{a}_s}$	$\frac{0.5t\bar{g}_v}{z_{LA}}\Delta_V[T_L^j]\Delta T_L$
9tR + 9t0 + 9v	$a_{E} = \frac{1}{1 + 0.5t \left(\frac{\bar{g}_{tR}}{z_{R} - z_{i}} + \frac{\bar{g}_{t0}}{z_{i}} + \frac{\bar{g}_{v}}{z_{LA}}\right)}$
$b_E = \frac{\Delta_V[\bar{T}_R]}{\bar{a}_E + \bar{a}_E + \bar{a}_E}$	$\frac{0.5t\bar{g}_v}{z_{LA}}\Delta_V[T_L^j]\Delta T_L$
$y_{tR} + y_{t0} + y_v$	$b_{E} = \frac{1}{1 + 0.5t \left(\frac{\bar{g}_{tR}}{z_{R} - z_{i}} + \frac{\bar{g}_{t0}}{z_{i}} + \frac{\bar{g}_{v}}{z_{LA}}\right)}$
$a_R = \varepsilon_s \sigma a_A{}^4$	$a_R = \varepsilon_s \sigma T_L^{j^4}$
$b_R = 4\varepsilon_s \sigma \left( a_A{}^3 b_A + \overline{T}_R{}^3 \right)$	$b_R = \varepsilon_s \sigma 2 T_L^{j^3}$
$a_H = 0$	$a_H = c_p \bar{g}_{Ha} \left( T_L^j - a_A \right)$
$b_H = c_p \bar{g}_{Ha}$	$b_H c_p \bar{g}_{Ha} (0.5 - 0.5 b_A)$
$a_L = \frac{\lambda \bar{g}_v}{\bar{p}_a} (e_s[\bar{T}_R] - a_e)$	$a_L = \frac{\lambda \bar{g}_v}{\bar{p}_a} \left( e_s \left[ T_L^j \right] - a_e \right)$
$b_L = \frac{\lambda g_v}{\bar{p}_a} (\Delta_V[\bar{T}_R] - b_E)$	$b_L = \frac{\lambda g_v}{\bar{p}_a} \left( 0.5 \Delta_V [T_L^j] - b_E \right)$
$a_A = \frac{\bar{g}_{tR}\bar{T}_R + \bar{g}_{t0}\bar{T}_0}{\bar{g}_{tR} + \bar{g}_{t0}}$	$a_{L} = \frac{T_{a}^{j} + \frac{0.5}{m_{a}} \left\{ \frac{\bar{g}_{tR}}{z_{R} - z_{i}} \bar{T}_{R} + \frac{\bar{g}_{t0}}{z_{i}} \bar{T}_{0} + \frac{\bar{g}_{Ha}}{z_{LA}} T_{L}^{j} + \frac{\lambda \bar{g}_{v}}{z_{LA} \bar{p}_{a}} \left( e_{L}^{j} + 0.5 e_{s} \left[ T_{L}^{j} \right] \right) - \frac{\lambda \bar{g}_{v}}{z_{LA} \bar{p}_{a}} a_{E} + \frac{\lambda \bar{g}_{t0}}{z_{i} \bar{p}_{a}} \bar{e}_{0} - \frac{\lambda \bar{g}_{t0}}{z_{i} \bar{p}_{a}} a_{E} \right\}}{\frac{1}{2} \left\{ \frac{1}{2} \left( \frac{1}{2} - \frac{1}{2} \right) - \frac{\lambda \bar{g}_{v}}{z_{LA} \bar{p}_{a}} \right\} - \frac{\lambda \bar{g}_{v}}{z_{LA} \bar{p}_{a}} a_{E} + \frac{\lambda \bar{g}_{v}}{z_{i} \bar{p}_{a}} \bar{e}_{0} - \frac{\lambda \bar{g}_{v}}{z_{i} \bar{p}_{a}} a_{E} \right\}}$
	$1 + \frac{0.5}{m_a} \left( \frac{\lambda \bar{g}_{t0}}{z_i \bar{p}_a} + \frac{\bar{g}_{t0}}{z_i} + \frac{\bar{g}_{Ha}}{z_{LA}} \right)$
$b_A = \frac{\bar{g}_{Ha}}{\bar{g}_{tR} + \bar{g}_{t0}}$	$b_{A} = \frac{\frac{0.5}{m_{a}} \left( 0.5 \frac{\overline{g}_{Ha}}{z_{LA}} + \frac{\lambda \overline{g}_{v}}{z_{LA} \overline{p}_{a}} \left( 0.5 \Delta_{V} \left[ T_{L}^{j} \right] - b_{E} \right) + \frac{\lambda \overline{g}_{10}}{z_{i} \overline{p}_{a}} b_{E} \right)}{1 + \frac{0.5}{m_{a}} \left( \frac{\lambda \overline{g}_{10}}{z_{i} \overline{p}_{a}} + \frac{\overline{g}_{10}}{z_{i}} + \frac{\overline{g}_{10}}{z_{i}} \right)}, \text{ where } m_{a} = c_{p} \hat{\rho} (1 - V_{d}) / t P_{AI}$

375

376 A similar ethos is used with regards to input weather data. The standard input is a data file of 377 temperature, humidity, wind speed, air pressure, sky emissivity and incoming solar radiation, but where 378 one or more of these variables are unavailable, we point the users to options for retrieving them. The R 379 package 'microclima' (Kearney et al., 2020; Maclean et al., 2019) contains functions for downloading, and interpolating to hourly, the required climate data from the NOAA-NCEP reanalyses programme 380 (Kanamitsu et al., 2002). Similarly, the R-package 'mcera5' (Duffy, 2020) contains similar functions 381 382 for retrieving data from the ECMWF ERA5 reanalysis programme (Hersbach, 2016). Full instructions for running the model are available as a vignette included with the package, provided in Appendix B. 383 384 The model can be run in time-steps ranging from one second to daily, with the time-increment controlled by the climate forcing data provided. 385

#### **4. MODEL VALIDATION**

Both steady-state and transient modes of the model were validated using hourly empirical temperature 387 388 measurements from four sites representing temperate deciduous and coniferous forests (Table 3; Lee et 389 al., 1999; Munger and Hadley 2020; Templer et al., 2019; Teramoto et al., 2019)). Only validation data 390 sampled according to best practices for micrometeorological observation (i.e. use of ultrafine-wire 391 thermocouples; de Podesta et al., 2018; Rebmann et al., 2018) were used. Heights at which temperature was measured varied between sites (between 1.0 and 10.0 metres) but were always below the uppermost 392 393 layers of the forest canopy; predictions were made for the same heights as measurements. The model 394 was parameterized using biome-specific estimates of vegetation and soil profile parameters that are 395 built into the package (see package details and vignette in Appendix B for details and the full list of parameters and default estimates). 396

We provided ERA5 hourly reanalysis data (Hersbach, 2016) as reference macroclimate and climate forcing to the microclimate model, corresponding to the times and points modelled. For the steady-state mode, daily resolution NCEP-DOE Reanalysis II precipitation estimates were provided for the soil moisture module (Kanamitsu et al. 2002). Because proper handling of snow cover and sub-freezing temperatures in the model is still under active development for the transient model, we constricted input data and predictions to only spring, summer and autumn months. For the purposes of this manuscript only air temperature predictions are validated (Figs. 1 and 2).

In the steady-state mode of the model, calculations are conducted simultaneously for all temporal timesteps, and therefore running the model for one year of data took an average of 5.28 seconds (on a single 2.2 GHz Intel i7 core with 4.0 GB of total memory). The transient mode, accessed via the function `runmodel`, must be run in sequence for each timestep, and so took an average of 194.9 seconds for the same time period. The steady-state and transient mode predicted below-canopy temperatures with similar accuracy (Mean absolute error 2.77 (transient) and 2.79 (steady-state); root mean square error 3.48 (both); 80.0% of variance explained (transient) and 79% (steady-state); Table 4). It should be noted
that some of the error is likely due to errors associated with climate data used to drive the models.

Below-canopy temperatures were typically less variable than macroclimate temperatures, which was 412 413 generally captured by the model in both of its modes. Both the steady-state and transient model underestimated forest temperature to a moderate degree (empirical SD: 5.93; steady-state estimate SD: 414 5.44; transient estimate SD: 4.67). At the Fuji Hokuroku and Hubbard Brook site there is also evidence 415 of a fairly consistent over-estimation of temperatures. This may in part be attributable to altitudinal 416 417 differences between validation sites and the coarse-resolution ERA5 data, which differ on average by 418 111 meters from the mean elevation across the ~25-kilmetre ERA5 grid cells. For the purpose of reproducibility by users, and so as to provide a conservative estimate of model performance, we did not 419 420 attempt to correct for these elevation differences.

421

### 422 **5.** MICROCLIMATE PROFILES

## 423 *5.1 Thermal Profiles*

Typical profiles obtained by the model are shown in Figures 3 and 4 and highlight the magnitude of 424 425 differences in climatic conditions within the soil and above or below canopy. Here temperature and humidity profiles were predicted for a location in Cornwall, United Kingdom (50.2178°N, 5.32656°W) 426 427 for a deciduous forest (Fig. 3) and short grassland (Fig. 4). In both instances, vegetation parameters were derived automatically by specifying a habitat type. In forest, under both dry and humid warm 428 429 daytime conditions, air temperature averaged over one hour were predicted to have a maximum in mid-430 canopy. These findings are consistent with those of other studies (e.g. Finnigan, 2000), and indicative 431 of a zone of high radiation absorption associated with high foliage density and reduced heat exchange 432 with air above-canopy caused by greater distance and reduced wind speed. In contrast, leaf temperatures 433 were predicted to be highest near the top of the canopy, where self-shading is lowest. At night, leaf 434 temperatures are lowest near the top of the canopy, particularly under clear-sky conditions. Here a lower proportion of the radiation emitted by a leaf would be expected to be absorbed and re-emitted by the 435 canopy. In contrast, differences in canopy air temperatures were predicted to be modest. The cooling 436 effect of leaves is offset by greater heat exchange with air above the canopy. The relative humidity 437 438 profile reflects three factors. On the one hand, relative humidity would be expected to be lowest where 439 temperatures are higher, as for a given vapour pressure relative humidity is primarily a function of 440 temperature. However, evapotranspiration from leaves and vapour exchange with air above the canopy 441 are also important. Despite limitations in the extent to which K-theory accurately captures canopy 442 turbulence, the predicted wind profiles are remarkably similar to empirically-derived profiles reported 443 in other studies (e.g. Raupach and Thom, 1981).

	Latitude,		Temperature	Measurement		
Name	Longitude	Vegetation	sensor	height (m)	Time start	Time end
		Mixed				
Borden Forest		hardwood/coniferous	Aspirated			
Research		forest dominated by red	copper-			
Station,	44°19′N,	maple and eastern white	constantan			
Ontario, Canada	79°56′W	pine, 22 m canopy height	thermocouples	1.7	1/04/1998	29/10/1998
Harvard Forest			Campbell			
Hemlock		Hemlock-dominated	Scientific CS215			
Tower,		temperate forest with	sensor with			
Massachusetts,	42°32′N,	mixed maple, oak, and	aspirated			
United States	72°11′W	pine, 23 m canopy height	radiation shield	1	4/04/2017	31/10/2017
Fuji Hokuroku						
Flux		Deciduous and evergreen	Vaisala			
Observation		needleleaf forest,	HMP45A,			
Site,		predominantly Japanese	platinum			
Yamanashi,	35°27′N,	larch. 23 m canopy	resistance			
Japan	138°46′W	height	thermometer			
-						
				10	3/05/2019	30/09/2019
			Campbell			
			Scientific CS215			
Hubbard Brook		Red maple-dominated	sensor with			
Experimental	43°57′N,	mixed temperate forest,	aspirated			
Forest	71°42′W	22 m canopy height	radiation shield	6	1/04/2013	30/09/2013

**Table 3.** Descriptions of sites and empirical temperature measurements used for model validation.





Fig. 1. Steady-state model predictions of temperature plotted across empirical measurements at four forested sites. Measurements were taken at heights ranging
 from 1.0 m to 10.0, but all below the uppermost layers of canopy. Both thermal measurements and predictions were taken at hourly time-steps for 5-7 months
 per site, and here subsets of time series are plotted to demonstrate diel variability.



**Fig. 2**. Transient model predictions of temperature plotted across empirical measurements at four forested sites. Transient predictions had moderately lower error than steady-state predictions (fig. 1), although the model did not accurately predict temperatures near freezing.



455 Fig 3. Modelled temperature (left), relative humidity (middle) and wind profiles (right) above, below
456 and within a 15 m tall deciduous forest canopy on four days with contrasting weather conditions. Dotted
457 lines in temperature profiles represent leaf temperatures, solid lines air temperature



458 Fig 4. Modelled temperature (left), relative humidity (middle) and wind profiles (right) above, below
459 and within a 25 cm height grassland on four days with contrasting weather conditions. Dotted lines in
460 temperature profiles represent leaf temperatures, solid lines air temperature

Table 4. Microclimate model average performance in steady-state and transient modes. Mean absolute
 error, root mean square error, and Pearson's correlation coefficients reported are relative to the
 empirical temperature measurements.

Variable	Steady-State	Transient
Avg. run time (1 year		
timeseries)	5.28 s	187.80 s
MAE	3.3	2.77
RMSE	4.15	3.48
$r^2$	0.803	0.8

In the grassland, particularly in sunny conditions, air temperature decreases with height above-canopy 465 466 and is highest at points near the top of the canopy. Temperatures in the soil decrease with depth. At 467 night, under cold, clear-sky conditions when air temperature is lower than that of the deepest soil layer, 468 the profile is reversed. Under overcast conditions, when air temperatures are similar to ground temperatures, variation in temperature with height is minimal, though there is a distinct zone close to 469 the soil surface where temperatures are lower. Leaf temperature profiles are broadly similar to air 470 temperature profiles within the canopy. As with deciduous forest, relative humidity profiles partially 471 472 reflect the temperature profiles, being lowest where temperatures are higher. However, is noticeable that during dry sunny conditions relative humidity is highest within the vegetation itself, despite warmer 473 temperatures, reflecting the zone of evapotranspiration. Wind profiles are typical of those empirically 474 475 observed (Campbell and Norman, 2012), and, though partially affected by diabatic turbulence, are 476 broadly consistent irrespective of conditions.

477

#### 478 **6.** CONCLUDING REMARKS

Our model, written for the R programming environment, complements existing R packages for 479 modelling microclimate (Kearney and Porter, 2017; Maclean et al., 2019), but extends the utility of 480 these packages by enabling ecologists to predict adequately the microclimate above, within, and below 481 dense canopies, such as those of forests. Since many organisms live in forest environments, this is likely 482 483 to be particularly useful. A key goal in developing our model was to enable estimates of microclimate with varying amounts of information available. In consequence, default parameters drawn from 484 485 literature are provided for broad habitat and soil types, but in circumstances where more detailed site-486 specific information, this can be readily incorporated. Estimates of snow cover and its effects on 487 temperature can be accounted for by invoking the snow subroutine within the `NicheMapR` package, 488 which builds nodes of snow above the surface conditional on the amount of precipitation, and thereby 489 influencing albedo and surface-air heat exchange. Accounting for snow would be especially valuable 490 for improved predictions near freezing, a current limitation of our model. Predictions of below-canopy 491 soil temperatures are currently provided by the model, yet these are primarily to estimate heat exchange

with the air. Accurate soil temperature predictions are contingent upon capturing dynamic soil moisture,which in the steady-state mode can be achieved via integration with `NicheMapR`.

494 Time series of sub-canopy temperatures from four forest locations globally are used to test the model. 495 The results indicate that temperatures can be estimate with a moderate degree of accuracy. A degree of 496 error is to be expected, however, as the climate forcing datasets used to drive the model are themselves imperfect and used we used default vegetation parameters associated with the broad habitat types of 497 these sites rather than quantifying vegetation structure in situ. Improvements in model fit would be 498 499 expected with finer-tuning of model parameters to account for local conditions and by correcting the 500 climate forcing data, for example by accounting for elevation effects (see e.g. Maclean et al. 2019). Nevertheless, even without doing so, the mean error of temperature measurements is only in the order 501 of 2.5-3°C. 502

Though there are still uncertainties in understanding of the microclimatic processes operating below canopy, many of the fundamental principles of microclimate modelling have been resolved decades. However, few of these insights have diffused into the field of ecology and the lack of integration between ecology and micrometeorology is perhaps one of the most remarkable examples of a disciplinary division. While many of the principles of microclimate modelling were resolved decades ago, in the very situations in which such models are much needed, they are rarely utilised. Here we utilised principles of environmental physics to provide a step forward in bridging this gap.

510

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518

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